

信号与信息处理

2018年5月6日

姓名：姜贵平

学号：SA17011142

1 second-layer

$$\frac{\partial E}{\partial w_{kj}^{(2)}} = \frac{\partial E}{\partial y_k} * \frac{\partial y_k}{\partial w_{kj}^{(2)}} \quad (1)$$

$$= -\frac{1}{y_k} * f'(z_k) * h\left(\sum_{i=0}^D w_{ji}^{(1)} * x_i\right) \quad (2)$$

2 first-layer

$$\frac{\partial E}{\partial w_{ji}^{(1)}} = \frac{\partial E}{\partial y_k} * \frac{\partial y_k}{\partial w_{ji}^{(1)}} \quad (3)$$

$$= -\frac{1}{y_k} * f'(z_k) * w_{kj}^{(2)} * h'\left(\sum_{i=0}^D w_{ji}^{(1)} * x_i\right) * x_i \quad (4)$$

其中：

$$z_k = \sum_{j=0}^M w_{kj}^{(2)} * h\left(\sum_{i=0}^D w_{ji}^{(1)} * x_i\right)$$
$$f'(x_i) = \frac{\exp(x_i) * \sum_{i=1}^K \exp(x_i) - \exp^2(x_i)}{\left(\sum_{i=1}^K \exp(x_i)\right)^2}$$

$$h(x) = \tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

$$h'(x) = \frac{4}{(e^x + e^{-x})^2}$$