$$AD : AB = AH : AC$$

$$\implies (b-h) : c = (c-a) : b$$

$$\implies c(c-a) = b(b-h)$$

$$\implies c^2 = b^2 + ac - bh$$

$$DH : BC = AH : AC$$

$$\implies h : a = (c-a) : b$$

$$\implies bh = a(c-a)$$

$$\implies a^2 = ac - bh$$
(2)