Lab Assignment (Basic Gaussian Elimination)

1. Use Gaussian elimination to solve the system of linear equations

$$x_1 + 5x_2 = 7$$
$$-2x_1 - 7x_2 = -5.$$

- Follow the Gaussian elimination algorithm
- Show your calculation step by step
- 2. Use Gaussian elimination to solve the system of linear equations

$$2x_2 + x_3 = -8$$
$$x_1 - 2x_2 - 3x_3 = 0$$
$$-x_1 + x_2 + 2x_3 = 3.$$

- Follow the Gaussian elimination algorithm
- Show your calculation step by step
- 3. Use Gaussian elimination to solve the system of linear equations

$$x_1 - 2x_2 - 6x_3 = 12$$

$$2x_1 + 4x_2 + 12x_3 = -17$$

$$x_1 - 4x_2 - 12x_3 = 22.$$

- Follow the Gaussian elimination algorithm
- Show your calculation step by step
- 4. Make your own subroutine or function to solve Ax = b using Gaussian elimination.
- Input : a $n \times n$ matrix A, a $n \times 1$ vector b
- Output: x