



Lecture Objectives

- Understand and implement the concept of functional programming in Python.
- Define and call functions.
- Comprehend the definition of Mathematical, Pure Functions, Anonymous Functions and Higher Order Functions.
- Understand and implement the concept of Object Oriented Programming in Python.



Outline

- Functional Programming
 - Defining Functions
 - Calling Functions
 - Assignment and Scope
 - Mathematical Function
 - Pure Functions
 - Function as Values
 - Anonymous Functions
 - Higher Order Functions
 - List Comprehensions
 - Closures
 - Generators

- Object Oriented Programming
 - Classes
 - Class Variables
 - Operators
 - Encapsulation
 - Duck Typing

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Defining Functions

- A function is a set of statements that take certain inputs, perform especific tasks and produces an output. The general objective of a function is to use this blocks of code instead of rewrite code over again.
- Functions are defined in Python using def_ followed by the function name and, if needed, the function arguments between ().

```
In [1]:    def hello():
        return 'hello world'

In [2]:    hello()
Out[2]: 'hello world'

In [3]:    hw = hello()
#hw
Out[4]: 'hello world'
```



Defining Functions

- Here x is the function argument, and square is the name of the function.
- Several things are different than C and Java:
 - · No need to define a return type
 - · Parameters have no types defined
 - Various ways of passing parameters

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```
In [5]: def square(x):
    return x*x

In [6]: square(4)

Out[6]: 16

In [7]: a = square(5)
    a

Out[7]: 25
```



Calling Functions

- Arguments can be passed to functions using keywords.
- This allows arguments to be (optionally) explicitly identified.
- · We can also specify a default value for an argument, that allow it to be omitted
- This is often seen in data science libraries, for e.g. specifying sensible defaults for algorithm settings:
- sklearn.decomposition.KernelPCA(n_components=None, kernel='linear', gamma=None, degree=3, coef0=1, kernel_params=None, alpha=1.0, fit_inverse_transform=False, eigen_solver='auto', tol=0, max_iter=None, remove_zero_eig=False, random_state=None, copy_X=True, n_jobs=1

```
In [8]:
          def sqnorm(x,y):
              return x*x+y*y
 In [9]:
          a = sqnorm(y=3,x=4)
          b = sqnorm(4, y=3)
          c = sqnorm(4,3)
In [10]:
          a, b, c
Out[10]: (25, 25, 25)
In [11]:
          #specify a default value for an argument, that allow it to be omitted:
          def sqnorm(x,y=0):
              return x*x+y*y
In [12]:
          a = sqnorm(4)
          b = sqnorm(4,2)
In [13]:
          a, b
Out[13]: (16, 20)
```

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Calling Functions

- Arguments are passed to functions depending on their type:
 - Immutable values such as integers and strings are passed by value.
 - Mutable values such as lists are passed by reference

• Integers are passed by value:

```
In [14]: def square(x):
    x = x*x
    return x
```

• Lists are passed by reference:

```
In [16]:
    def listswap(a):
        tmp = a[1]
        a[1] = a[0]
        a[0] = tmp

In [17]:
        l = [1,2]
        listswap(1)
        print(1)
        [2, 1]
```



Assignments and Scope

- Variables in Python need to be assigned before they can be used. The assignment of a variable determines its scope, i.e. where it can be accessed from.
- Assignments made at the top level are global and accessible from anywhere.
- Assignments made in for or while loops are also in scope at the level the loop is defined at.
- Variables assigned within functions are local to that function definition:
- References to objects will first search the local scope, then global.
- Note that if a variable is assigned in the local scope, the local version will be found:

```
In [21]: | print(f())
          print(a)
         12
         5
In [22]:
          #- References to objects will first search the local scope, then global:
          def f():
              a.append(10) # Finds a in global scope
In [23]:
          f()
          print(a)
         [10]
In [24]:
          # - Note that if a variable is assigned in the local scope, the local version will b
          a=[]
          def f():
              a = []
              a.append(10) #Modifies local a
              return a
In [25]:
          print(f())
          print(a)
         [10]
         []
```

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Mathematical functions

- Definition:
 - f(x) has one value
 - For a given x, f(x) is always the same
 - Multiple x can give the same value of f(x)
 - Note that functions in programming languages often do not behave as mathematical functions.



Mathematical functions

 Which of these functions behaves like a mathematical function? (For a given value of the random seed, the sequence of "random" numbers will always be the same)

```
def incr(x,y):
x = [0]
def incr(y):
                                               return x + 1 + y
                                       def unif(a,b,seed):
       x[0] = x[0] + 1
       return x[0] + y
                                               # sets the random seed
                                               random.seed(seed)
def unif(a,b):
                                               # returns a random number
       # returns a random number
                                               t = random.random()
       t = random.random()
                                               return (b-a)*t+a
       return (b-a)*t+
```

```
In [26]:
          x = [0]
          def incr1(y):
              x[0] = x[0] + 1
               return x[0] + y
In [27]:
          def incr2(x,y):
               return x + 1 + y
         Which of these functions behaves like a mathematical function?
In [28]:
          print(incr1(1))
          print(incr2(0,1))
         2
         2
In [29]:
          import random
          def unif1(a,b): # returns a random number
               t = random.random()
               return (b-a)*t+a
In [30]:
          unif1(5,6)
Out[30]:
         5.927594054331711
In [31]:
          import random
          def unif2(a,b): # sets the random seed
               random.seed(6) # returns a random number
               t = random.random()
               return (b-a)*t+a
In [32]:
          unif2(5,6)
```

```
Out[32]: 5.793340083761663
```

Which of these functions behaves like a mathematical function?

(For a given value of the random seed, the sequence of "random" numbers will always be the same)

```
In [33]:
    print(unif1(5,6))
    print(unif2(5,6))
```

5.821954042319727 5.793340083761663



Pure functions

- In programming, pure functions:
 - Always produce the same output when given the same arguments.
 - Have no side effects (no modification of any variables outside of those local to the function, or I/O).
- This restricts functions to behave like mathematical functions.
- In Python there is no way to enforce that a function behaves in this way, but when using functions as arguments to higher order functions it is a good idea to stick to pure functions.

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Functions as values

- In many programming languages, functions can be treated as values, and passed to other functions.
- This means you can do many interesting things:
 - Write functions that apply arbitrary operations based on their parameters.
 - Write functions that generate a function and return it as a value.

```
def map1(f,xs):
    result = []
    for x in xs:
        t = f(x)
        result.append(t)
    return result
```

```
In [35]:
    1 = [3,6,9,12]
    map1(g,1)
```

```
Out[35]: [6, 12, 18, 24]
```



Anonymous functions

- To quickly generate functions in Python, anonymous functions can be built using the **lambda** keyword.
- Although no name is assigned to the function when it is defined, you can assign the function to a variable just like you would with any other value.

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Aside - lambda calculus

- · Why is it called a lambda?
- In many programming languages anonymous functions are referred to as lambdas. This is because of something called the lambda calculus. The lambda calculus can compute anything that a Turing machine can.
- In the lambda calculus we could write this function:

```
lambda x: x*x+1
```

• In the lambda calculus as: λx.x2 +1 (λ is the Greek letter lambda)



Aside - lambda calculus

• Functions application in the lambda calculus is written as:

```
(\lambda x.x2 + 1)5
```

Which is equivalent to:

```
(lambda x: x*x+1)(5)
```

• The key operation in lambda calculus is substituting some variable, here x, with a value, here 5, in an expression.

```
In [36]:
          lambda x: x*x+1
          (lambda x: x*x+1)(5)
Out[36]: 26
In [37]:
          ## Lets redo our Function g as a Lambda function:
          ## We can send the lammda function as a parameter tu value function.
          1 = [3,6,9,12]
          map1(lambda x: 2*x,1)
Out[37]: [6, 12, 18, 24]
In [38]:
         #Although no name is assigned to the function when it is defined, you can assign the
          f = lambda x: x if x>0 else -x
          f(-6)
          #A shorthand for if statements is __A if condition else B__.
Out[38]: 6
```



Higher order functions

- Higher order functions are functions that take other functions as arguments and operate on them, or that return functions as results.
- In programming, higher order functions can be used to write customisable functions, whose operations depend on their arguments. They can also be used to build functions.

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Higher order functions - Maps

- The map operation applies a function to every element of a collection.
- Generally we want to use pure functions, as they have no side effects, i.e.
 functions that behave as mathematical functions. For example generally in a map,
 the order in which the elements will be processed is not defined, and may even be
 performed in parallel on multiple CPU cores or different computers.
- Why maps?
 - Readability Makes it clear you are applying the same function to each list member
 - Correctness Combine existing built-in functions
 - Parallelisable Each function can be applied in a different CPU thread, or on a different computer (see Map Reduce).

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```
In [39]:
    def map1(f,xs):
        result = []
        for x in xs:
            t = f(x)
            result.append(t)
        return result
```

An example – finding the average (mean) of each element of a list of lists:

```
In [40]:
    def mean(xs):
        n = len(xs)
        if n>0:
            s = sum(xs)
            return s/n
        else:
            return 0.0
```

```
In [41]: map1(mean,[[1,2,3],[5,5,4,5],[9,8,3,4,5],[]])
```

```
Out[41]: [2.0, 4.75, 5.8, 0.0]
```



Higher order functions - Filter

- The filter operation applies a condition to each member of a collection and returns a list only containing members for which the condition was true.
- The function passed to filter should return True or False.
- Why maps?
 - Readability Makes it clear you are applying the same function to each list member
 - Correctness Combine existing built-in functions
 - Parallelisable Each function can be applied in a different CPU thread, or on a different computer (see Map Reduce).

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```
In [42]:

def filter1(p,xs):
    result = []
    for x in xs:
        if p(x):
            result.append(x)
    return result
```

Filtering values from a list:

```
In [43]:
    1 = [-3,4,2,-1,0,-9,5]
    filter1(lambda x: x>0,1)
```

Out[43]: [4, 2, 5]

We can combine maps and filters:

Functional programming with the Python Reading Standard Library

Map

 Python has a built-in function map that behaves similarly to our map function defined above. The difference is that it can take any number of iterable objects as inputs

Operators as functions

• For various built-in operators in Python the operator module contains function definitions that can be passed to functions like map

Filter

• There is also a built-in filter function in the standard library.

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```
In [45]: ##First we need to define a function
    def sub(x,y):
        return x-y

In [46]: a = map(sub,[1,2,3],[3,2,1])
    list(a)
```

```
Out[46]: [-2, 0, 2]
```

Notice that here a is not actually a list but a generator, an iterable object. We use list(a) to evaluate a and convert it to a list.

```
In [47]: type(a)
```

Out[47]: map

Out[49]: map

Operators as functions

Maps

For various built-in operators in Python the operator module contains function definitions that can be passed to functions like map. The difference is that it can take any number of iterable objects as inputs:

```
In [48]: import operator
    a = map(operator.sub,[1,2,3],[3,2,1])
    list(a)

Out[48]: [-2, 0, 2]

In [49]: type(a)
```

Filter

There is also a built-in filter function in the standard library:

```
List comprehensions
```



 A quick way to apply some operations to some group of objects is to use a list comprehension. This allows you to build a list by specifying how it should be constructed.

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```
In [51]:
    a = [ x * x for x in range(1,11)]
    a
```

Out[51]: [1, 4, 9, 16, 25, 36, 49, 64, 81, 100]

You can also apply filtering to the for loop:

```
In [52]: b = [ x * x for x in range(1,11) if (x*x)%3==1 ]
b
```

Out[52]: [1, 4, 16, 25, 49, 64, 100]

You can unpack tuples in list comprehensions

```
In [53]:

a = [ (4.0,1.2),(5.6,7.1),(1.1,0.6)]

b = [(x-y)*(x-y) for x,y in a]

b
```

Out[53]: [7.83999999999999, 2.25, 0.2500000000000001]

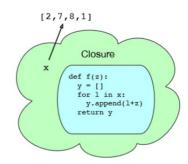
You can also nest for loops inside of the list comprehension:

```
In [54]: c = [(x,y) for x in range(1,3) for y in range(1,4)]
```



Closures

- Functions can also be grouped together with the environment they were defined in. This is known as a closure.
- This allows you to do things like define functions that build and return other functions.
- Global or local variables of any type can be captured in a closure.
- However if the variable captured is a list or dictionary, the closure will store a reference to it, not a copy.



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Out[56]: 8

Global or local variables of any type can be captured in a closure:

```
In [57]:

def g():
    x = [2,7,8,1]
    def f(z):
    y = []
    for l in x:
        y.append(l+z)
    return y
    return f
```

```
In [58]: closure = g() closure(4)
```

Out[58]: [6, 11, 12, 5]

However if the variable captured is a list or dictionary, the closure will store a reference to it, not a copy.

```
In [59]:
          def g():
               x = [2,7,8,1]
               def f(z):
                   y = []
                   for 1 in x:
                       y.append(1+z)
                   return y
               x[2] = 9
               print(x)
               return f
In [60]:
           closure = g()
           closure(4)
          [2, 7, 9, 1]
Out[60]: [6, 11, 13, 5]
```

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Generators

 Generators can be used to lazily construct iterable sequences of objects. A simple way of constructing a generator in Python is to use a syntax very similar to a list comprehension.

```
a = (pow(x,5) \text{ for } x \text{ in } range(pow(10,128)))
```

• If we actually evaluated this as a list comprehension it would run out of memory constructing the list before completing. A generator instead produces an object that can be used to iterate over the list, **only on demand.**

```
In [61]: #a = [pow(x,5) for x in range(pow(10,128))]
#a

In [62]: import itertools
    a = (pow(x,5) for x in itertools.count(1))
    next(a)

Out[62]: 1

In [63]: next(a)

Out[63]: 32

In [64]: next(a)
```

Out[64]: 243

In [65]:

next(a)

Out[65]: 1024

next(a) takes a value from the generator, and updates it to step to the next value in the sequence.

count is a function from the itertools module that returns an iterator that counts up from a starting value



Why?

- These concepts will appear a lot in data science applications, e.g.:
 - Map a function over columns of a data set (e.g. calculate mean of each column)
 - Filter a list of values that match some condition
- The two most common data science languages, Python and R, both support functional programming.
- Recognising common patterns that can be implemented using higher order functions helps you write more concise, readable and reliable code.

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Object-oriented programming

- Encapsulation
 - Data and the functions that work on them are bound together in objects. We might want to hide variables from view outside of the object.
- Composition
 - Objects provide abstraction and can be used as building blocks to construct more complex objects.
- Inheritance
 - Objects can be derived from other objects in a hierarchy.



Classes

- Class definitions are simple, methods are defined as functions inside of the class definition.
- Classes are just collections of Python functions and assignments. When an object of a class is instantiated a new object of that class is created.
- To allow our methods to work with distinct **instances** of objects, methods take an extra first argument, by convention called **self**. This is a reference to the instance of the object that the method was called on.

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• This class has a variable val that belongs to each instance of the class, and can be modified using the set and get methods. We can create an instance of the class using:

```
In [67]:    a = MyClass1()
a
Out[67]: <__main__.MyClass1 at 0x25991665198>
    So if we call set on a MyClass object:
In [68]:    a = MyClass1()
```

```
In [68]:
    a = MyClass1()
    a.set(5) # Calls MyClass.set(a,2)

a.get()
#The actual function call is to MyClass.set(a,...).
```

Out[68]: 5



Instance initialisation

- Class instances in Python are initialised using a special function called __init__.
 This is called when the constructor of the class is invoked.
- If you leave it blank then Python will just create an object of that class with no initialisation.

Class variables

 Variables can be defined inside of a class, these assignments will be made when the class is defined, and are shared attributes between all instances of the class.

```
In [69]:
          class MyClass2:
              def __init__(self,value):
                  self.val = value
                  # A class method
              def set(self,value):
                  # A variable defined in each instance
                  self.val = value
              def get(self):
                  return self.val
In [70]:
          MyClass2(6)
Out[70]: <__main__.MyClass2 at 0x25991665710>
In [71]:
          #Using the default constructor, or specifying arguments to the __init__ function:
          storeA = MyClass1()
          storeA.set(32)
          #print(storeA.get()) # 32
          storeB = MyClass2(64)
          print(storeB.get()) # 64
          print(storeA.get()) # 32
         64
         32
 In [1]:
          ##Class Variables
          class MyClassCounter:
              readCounter = 0 # A class variable
              writeCounter = 0 # A class variable
              def set(self,value): # A class variable for *all* instances.
                  MyClassCounter.writeCounter += 1
                  self.val = value
              def get(self): # A class variable for *all* instances.
                  MyClassCounter.readCounter += 1
                  return self.val
```

```
In [2]:
    storeA = MyClassCounter()
    storeA.set(32)
    print(storeA.get()) # 32
    print(MyClassCounter.readCounter) # 1
    print(MyClassCounter.writeCounter) # 2

32
    1
    1

In [3]:
    storeB = MyClassCounter()
    storeB.set(16)
    print(MyClassCounter.readCounter) # 1
    print(MyClassCounter.writeCounter) # 2

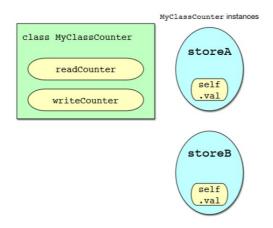
1
```

 Notice that the readCounter and writeCounter variables are shared by both storeA and storeB.

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Classes examples

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Operators

 As we saw with __init__ Python uses special methods in classes for certain language functionality. As well as constructors, you can specify how objects of your class should behave when used with various Python language operators.

Method	Python syntax	Description
init(self,args)	MyClass(args)	Object instantiation
add(self,b)	a + b	Addition
sub(self,b)	a - b	Subtraction
contains(self,b)	b in a	Membership

 Operators like + and - don't necessarily have to perform mathematical addition or subtraction in some way – you can use them as syntactic shortcuts for different operations (e.g. concatenation).

```
In [75]:
    class MyClassAdd:
        def __init__(self,value):
            self.val = value
        def set(self,value):
            self.val = value
        def get(self):
            return self.val
        def __add__(self,x):
            return MyClassAdd(self.val+x.get())
```

Out[76]: 5

If "a + b" and a is an instance of MyClassAddd, then Python will look the class definition of MyClassAddd. If MyClassAddd has a method **add** it will be called with x.**add**(y)



Encapsulation

- When a class is defined, all attributes and methods are public by default, meaning that any attributes of a class instance can be modified outside of the class.
- There are advanced approaches to get around this for now simply be careful when working with classes!

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```
In [77]:
    class MyClass2:
        def __init__(self,value):
            self.val = value
            # A class method
        def set(self,value):
            # A variable defined in each instance
            self.val = value
        def get(self):
            return self.val
```

```
In [78]:
    a = MyClass2(3)
    a
    a.val = 4
    print(a.get())
```



Duck typing

- In Python, we are able to use instances of classes without specifying that a variable must be an object of that specific class. In fact if we write some code that uses objects with a .get() method, any Python object with a .get() method can be used, regardless of which class it belongs to.
- This means that we can define classes whose objects behave exactly like objects of another class, without inheritance. This is known as duck typing.



```
In [79]: #This function will work with instances of any class that have get and set methods:
    def addToStore(s,x):
        value = s.get()
        s.set(value+x)

In [80]: #So we can use it with both MyClass and MyClassCounter:
    a = MyClass2(4)
    b = MyClassCounter()
    b.set(3)
    addToStore(a,3)
    addToStore(b,3)

In [81]: a.get(), b.get()
Out[81]: (7, 6)
```



Summary

- Functions can be treated as values.
- Higher order functions allow common programming patterns to be used and composed easily.
- Supported by the Python standard library.
- Python supports different programming paradigms such as functional and object oriented.

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Questions





References

• Thomas McKinney, Wes 'Python for data analysis : data wrangling with Pandas, NumPy, and IPython'.

In []:	
In []:	