

# Databases & External Memory Indexes, Write Optimization, and Crypto-searches

Michael A. Bender  
Tokutek & Stony Brook

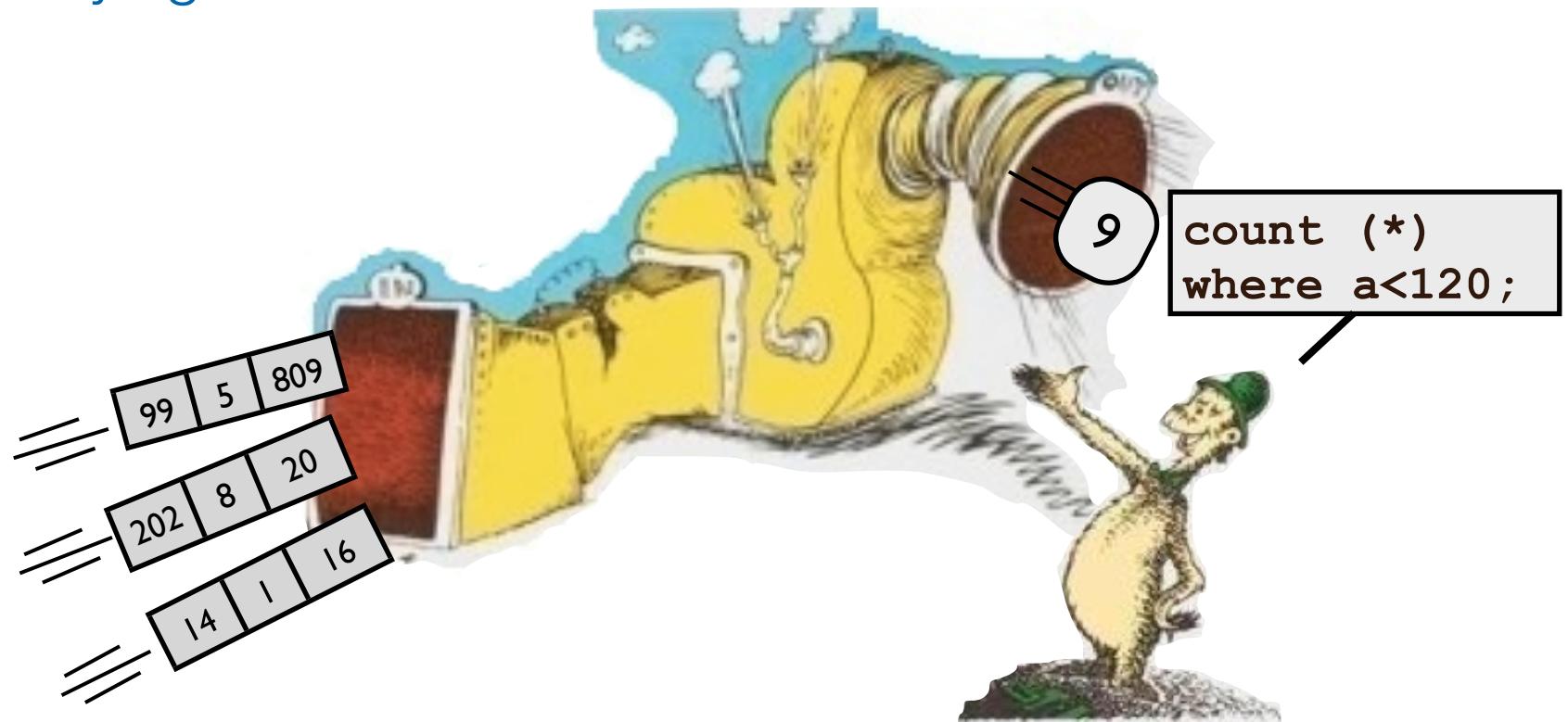
Martin Farach-Colton  
Tokutek & Rutgers



# What's a Database?

## DBs are systems for:

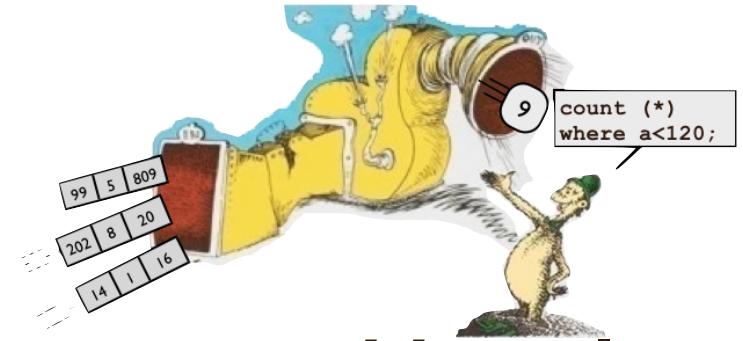
- Storing data
- Querying data.



# What's a Database?

**DBs are systems for:**

- Storing data
- Querying data.



**DBs can have SQL interface or something else.**

- We'll talk some about so-called NoSQL systems.

**Data consists of a set of key,value pairs.**

- Each value can consist of a well defined tuple, where each component is called a field (e.g. relational DBs).

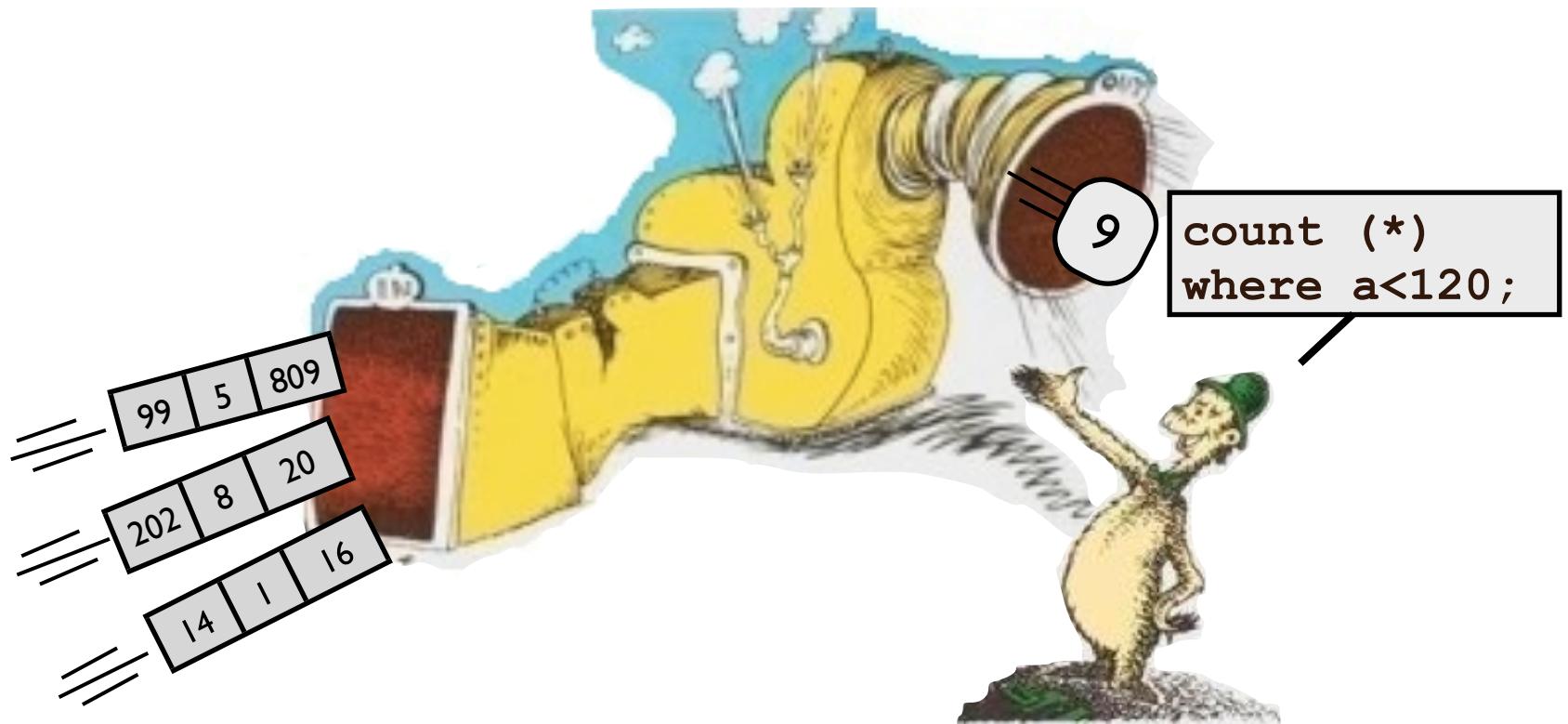
**Big Data.**

- Big data = bigger than RAM.

# What's this database tutorial?

## Traditionally:

- Fast queries  $\Rightarrow$  sophisticated indexes and slow inserts.
- Fast inserts  $\Rightarrow$  slow queries.



**We want fast data ingestion + fast queries.**

# What's this database tutorial?

## Database tradeoffs:

- There is a query/insertion tradeoff.
  - ▶ Algorithmicists mean one thing by this claim.
  - ▶ DB users mean something different.
- We'll look at both.

## Overview of Tutorial:

- Indexes: The DB tool for making queries fast
- The difficulty of indexing under heavy data loads
- Theory and Practice of write optimization
- From data structure to database
- Algorithmic challenges from maintaining two indexes

# Row, Index, and Table

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

## Row

- Key,value pair
- key = a, value = b,c

## Index

- Ordering of rows by key
- Used to make queries fast

## Table

- Set of indexes

```
create table foo (a int, b int, c int,  
primary key(a));
```

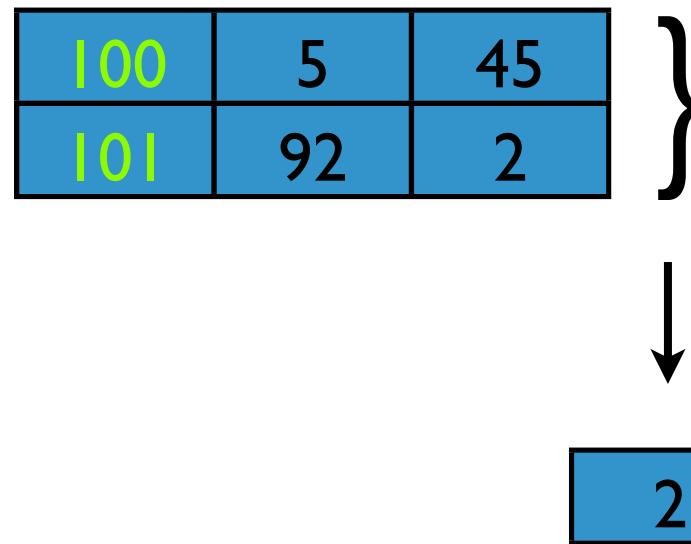
# An index can select needed rows

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

```
count (*) where a<120;
```

# An index can select needed rows

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45



```
count (*) where a<120;
```

# No good index means slow table scans

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

```
count (*) where b>50 and b<100;
```

# No good index means slow table scans

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45



3

```
count (*) where b>50 and b<100;
```

# You can add an index

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

b	a
5	100
6	165
23	206
43	412
56	156
56	256
92	101
202	198

```
alter table foo add key(b);
```

# A selective index speeds up queries

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

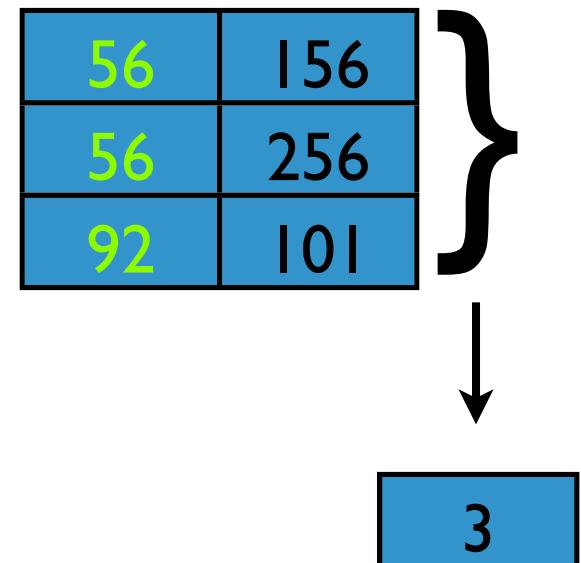
b	a
5	100
6	165
23	206
43	412
56	156
56	256
92	101
202	198

```
count (*) where b>50 and b<100;
```

# A selective index speeds up queries

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

b	a
5	100
6	165
23	206
43	412
56	156
56	156
56	256
92	101



```
count (*) where b>50 and b<100;
```

# Selective indexes can still be slow

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

b	a
5	100
6	165
23	206
43	412
56	156
56	256
92	101
202	198

**sum(c) where b>50;**

# Selective indexes can still be slow

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

b	a
5	100
6	165
23	206
43	412
56	156
56	256
92	101
202	198

56	156
56	256
92	101
202	198



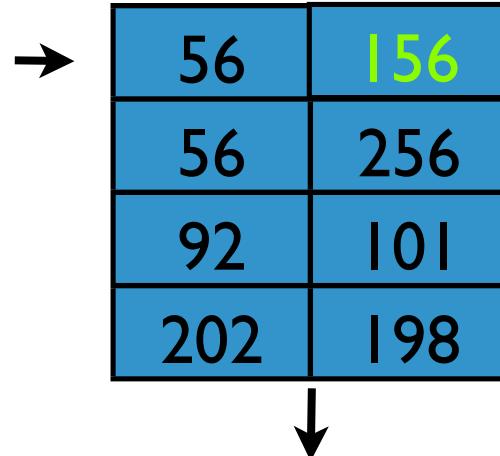
Selecting  
on b: fast

`sum(c) where b>50;`

# Selective indexes can still be slow

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

b	a
5	100
6	165
23	206
43	412
56	156
56	256
92	101
202	198



Selecting  
on b: fast  
Fetching info for  
summing c: slow

`sum(c) where b>50;`

# Selective indexes can still be slow

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

b	a
5	100
6	165
23	206
43	412
56	156
56	256
92	101
202	198

56	156
56	256
92	101
202	198

156	56	45
-----	----	----

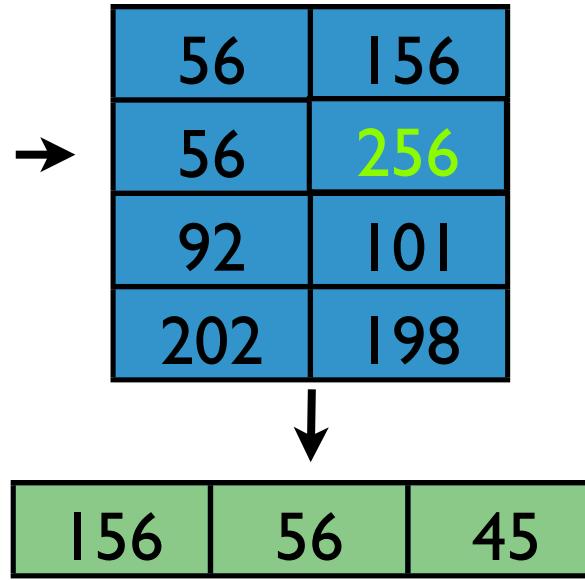
Selecting  
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**sum(c) where b>50;**

# Selective indexes can still be slow

a	b	c
100	5	45
101	92	2
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165	6	2
198	202	56
206	23	252
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412	43	45

b	a
5	100
6	165
23	206
43	412
56	156
56	256
92	101
202	198



Selecting  
on b: fast  
Fetching info for  
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# Selective indexes can still be slow

a	b	c
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b	a
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23	206
43	412
56	156
56	256
92	101
202	198

56	156
56	256
92	101
202	198

↓

156	56	45
256	56	2

Selecting  
on b: fast  
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# Selective indexes can still be slow

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

Poor data locality

b	a
5	100
6	165
23	206
43	412
56	156
56	256
92	101
202	198

`sum(c) where b>50;`

56	156
56	256
92	101
202	198

Selecting  
on b: fast  
Fetching info for  
summing c: slow

156	56	45
256	56	2
101	92	2
198	202	56

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# Covering indexes speed up queries

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

b,c	a
5,45	100
6,2	165
23,252	206
43,45	412
56,2	256
56,45	156
92,2	101
202,56	198

```
alter table foo add key(b,c) ;  
sum(c) where b>50 ;
```

# Covering indexes speed up queries

a	b	c
100	5	45
101	92	2
156	56	45
165	6	2
198	202	56
206	23	252
256	56	2
412	43	45

b,c	a
5,45	100
6,2	165
23,252	206
43,45	412
56,2	256
56,45	156
92,2	101
202,56	198

56,2	256
56,45	156
92,2	101
202,56	198



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```
alter table foo add key(b,c);  
sum(c) where b>50;
```

# DB Performance and Indexes

**Read performance depends on having the right indexes for a query workload.**

- We've scratched the surface of index selection.
- And there's interesting query optimization going on.

**Write performance depends on speed of maintaining those indexes.**

***Next: how to implement indexes and tables.***

# An index is a dictionary

## Dictionary API: maintain a set $S$ subject to

- $\text{insert}(x)$ :  $S \leftarrow S \cup \{x\}$
- $\text{delete}(x)$ :  $S \leftarrow S - \{x\}$
- $\text{search}(x)$ : is  $x \in S$ ?
- $\text{successor}(x)$ : return min  $y > x$  s.t.  $y \in S$
- $\text{predecessor}(y)$ : return max  $y < x$  s.t.  $y \in S$

# A table is a set of indexes

## **A table is a set of indexes with operations:**

- Add index: `add key(f1, f2, ...);`
- Drop index: `drop key(f1, f2, ...);`
- Add column: adds a field to primary key value.
- Remove column: removes a field and drops all indexes where field is part of key.
- Change field type
- ...

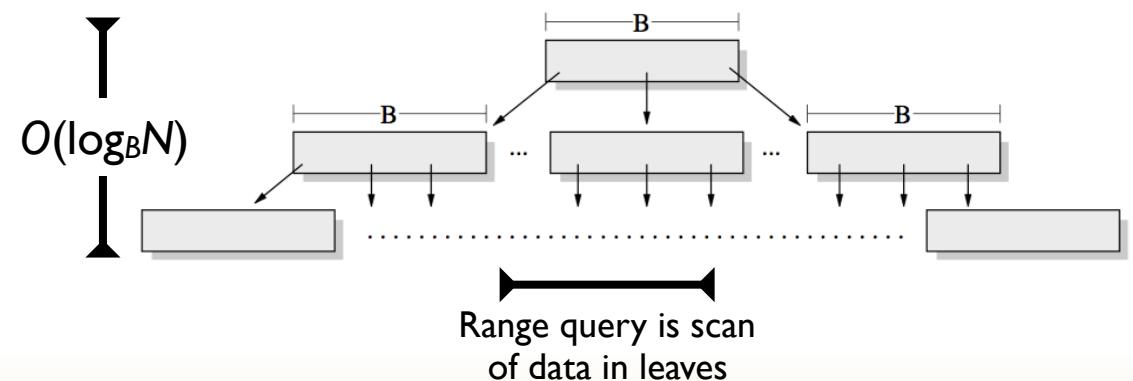
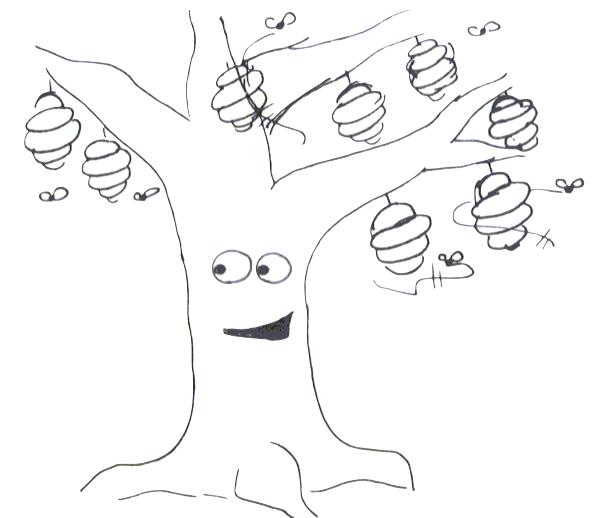
**Subject to index correctness constraints.**

*We want table operations to be fast too.*

# Indexes are typically B-trees

## B-tree performance:

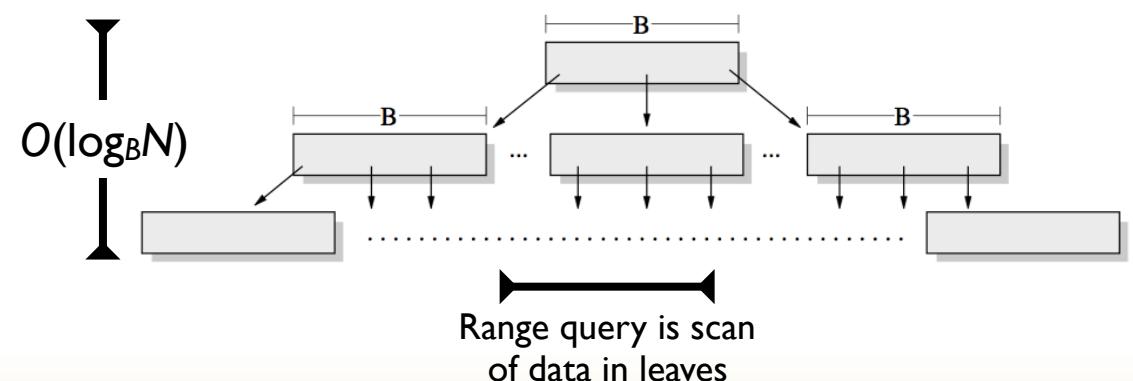
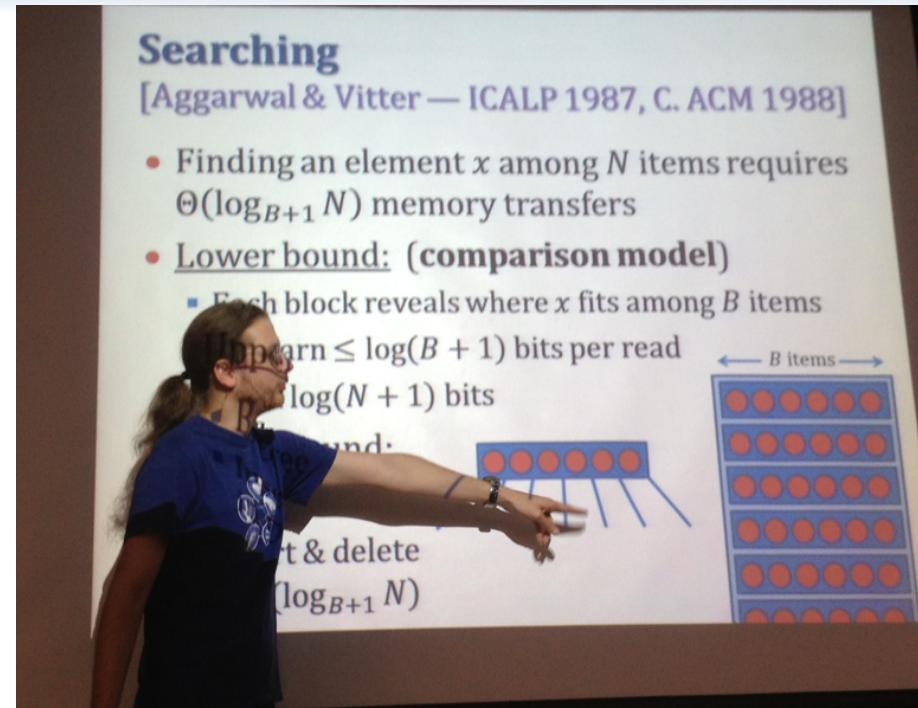
- Point queries:  $O(\log_B N)$  I/Os.
  - ▶ Matches lower bound for DAM model.
- Range queries of  $K$  elements:  $O(\log_B N + K/B)$  I/Os.
  - ▶ We'll talk about B-tree aging later.
- Insertions:  $O(\log_B N)$  I/Os.



# Indexes are typically B-trees

## B-tree performance:

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- Insertions:  $O(\log_B N)$  I/Os.



# Worst-case analysis is a fail

**Some indexes are easy to maintain, others not.**

- The database is chugging along nicely.
- You add an index.
- Performance tanks --- inserts can run 100x slower.

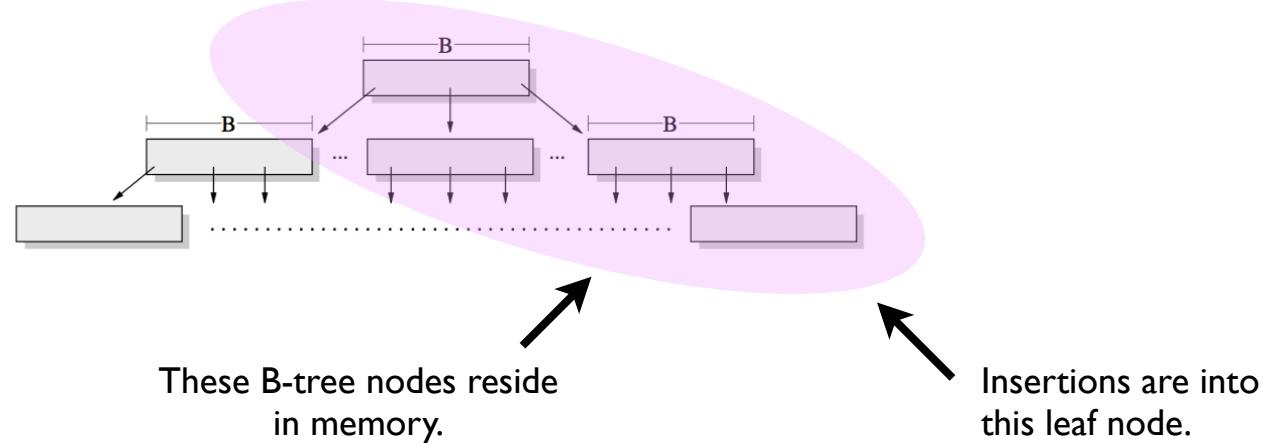
# Indexes and Performance Anomalies

**Databases can exhibit performance anomalies when indexes are modified.**

- “I’m trying to create indexes on a table with 308 million rows. It took ~20 minutes to load the table but 10 days to build indexes on it.”
  - ▶ MySQL bug #9544
- “Select queries were slow until I added an index onto the timestamp field... Adding the index really helped our reporting, BUT now the inserts are taking forever.”
  - ▶ Comment on mysqlperformanceblog.com
- “They indexed their tables, and indexed them well,  
And lo, did the queries run quick!  
But that wasn’t the last of their troubles, to tell—  
Their insertions, like molasses, ran thick.”
  - ▶ Not from *Alice in Wonderland* by Lewis Carroll

# B-trees and Caching: Sequential Inserts

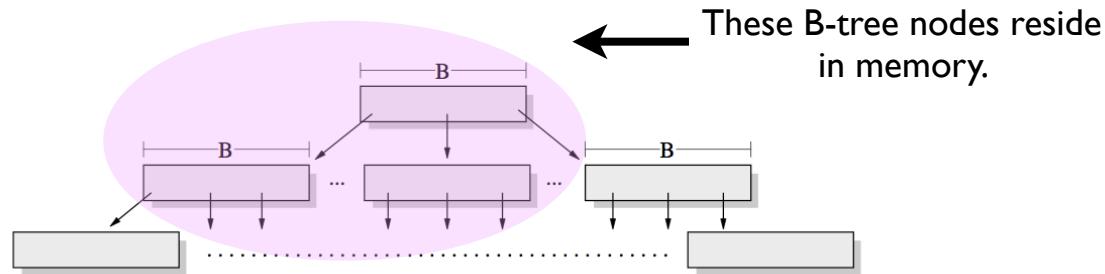
**Sequential B-tree inserts run fast because of near-optimal data locality.**



- One disk I/O per leaf (though many elements are inserted).
- $O(1/B)$  I/Os per row inserted.
- Performance is limited by disk-bandwidth.

# B-trees and Caching: Random Inserts

**High entropy inserts (e.g., random, ad hoc) in B-trees have poor data locality.**



- Most leaves are not in main memory.
- This achieves worst case performance:  $O(\log_B N)$ .
- $\leq 100$ 's inserts/sec/disk ( $\leq 0.2\%$  of disk bandwidth).
  - Two orders of magnitude slower than sequential insertions.

# B-tree insertion: DB Practice

**People often don't use enough indexes.  
They use simplistic schema.**

- Sequential inserts via an autoincrement key.
  - ▶ Makes insertions fast but queries slow.
- Few indexes, few covering indexes.

t	b	c
1	5	45
2	92	2
3	56	45
4	6	2
5	202	56
6	23	252
7	56	2
8	43	45

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**Adding sophisticated indexes helps queries.**

- B-trees cannot afford to maintain them.

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8	43	45

**Adding sophisticated indexes helps queries.**

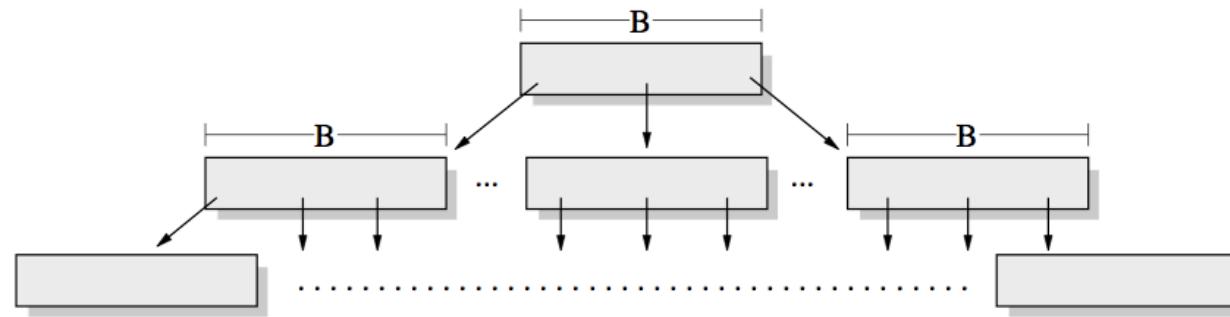
- B-trees cannot afford to maintain them.

*If we speed up inserts, we can maintain the right indexes, and speed up queries.*

# Write-Optimized External Dictionaries

## What we want:

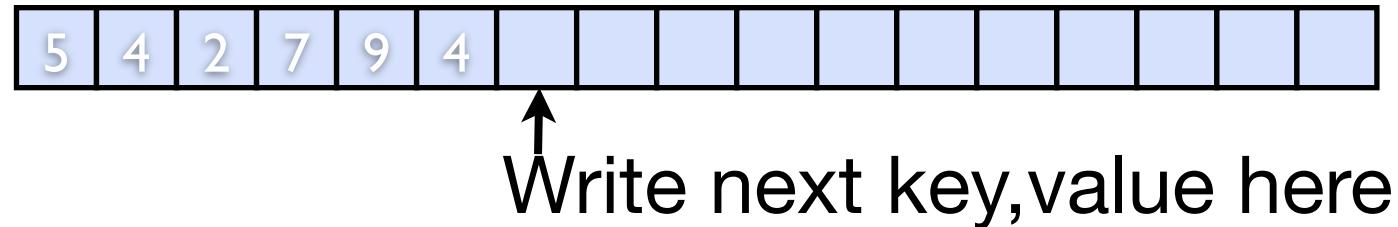
- B-tree API. Better insert/delete performance.



There's a  $\Omega(\log_B N)$  lower bound for searching...  
... *but not for inserting.*

# Write-Optimized External Dictionaries

**Append-to-file beats B-trees at insertions.**



## Pros:

- Achieve disk bandwidth even for random keys.
- Ie, inserts cost amortized  $O(1/B)$ .

## Cons:

- Looking up anything requires a table scan.
- Searches cost  $O(N/B)$ .

# Write-Optimized External Dictionaries

structure	insert	point query
B-tree	$O\left(\frac{\log N}{\log B}\right)$	$O\left(\frac{\log N}{\log B}\right)$
append-to-file	$O\left(\frac{1}{B}\right)$	$O\left(\frac{N}{B}\right)$
write-optimized	$O\left(\frac{\log N}{\varepsilon B^{1-\varepsilon} \log B}\right)$	$O\left(\frac{\log N}{\varepsilon \log B}\right)$
write-optimized ( $\varepsilon=1/2$ )	$O\left(\frac{\log N}{\sqrt{B}}\right)$	$O\left(\frac{\log N}{\log B}\right)$

## Some optimal write optimized structures:

- Buffered repository tree [Buchsbaum, Goldwasser, Venkatasubramanian, Westbrook 00]
- $B^\varepsilon$ -tree [Brodal, Fagerberg 03]
- Streaming B-tree [Bender, Farach-Colton, Fineman, Fogel, Kuszmaul, Nelson 07]
- Fractal Tree Index [Tokutek]
- xDict [Brodal, Demaine, Fineman, Iacono, Langerman, Munro 10]

# Write optimization techniques in production

## Online insert buffer

- InnoDB, Vertica

## Offline insert buffers

- OLAP, OLAP, OLAP

## Cascading

- LSM trees in Bigtable, Cassandra, H-Base

## Asymptotically optimal data structures

- Buffered Repository Trees (BRT),  $B^\epsilon$  -tree: Tokutek
- Cache-oblivious Lookahead Arrays (COLA): Tokutek, Acunu

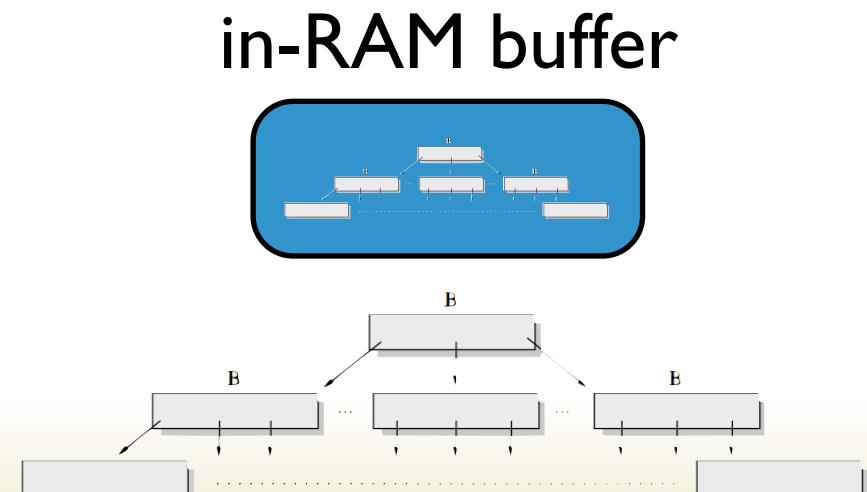
Heuristic techniques for getting more productive work done when we touch a B-tree leaf



# Write optimization techniques in production

## B-trees with an online in-RAM buffer

- Flush multiple operations to same leaf
- To query: search in buffer and in B-tree.



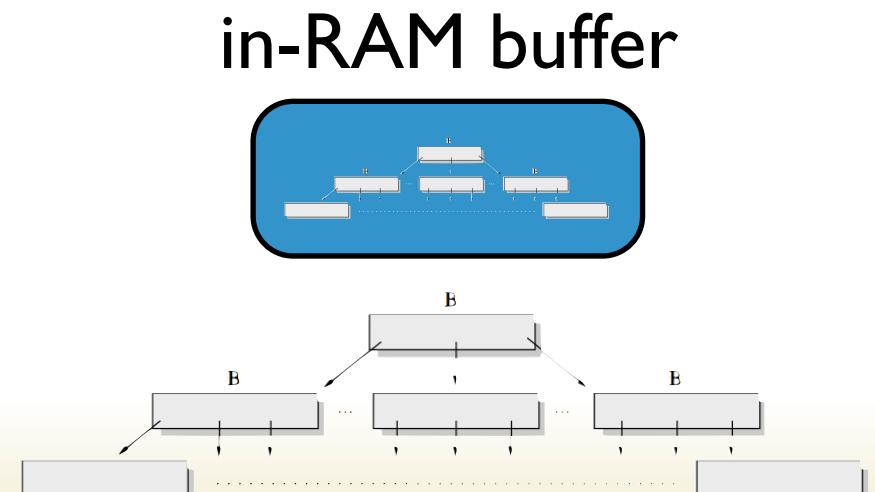
# Write optimization techniques in production

## B-trees with an online in-RAM buffer

- Flush multiple operations to same leaf
- To query: search in buffer and in B-tree.

## Analysis Experience

- Smooths out the “dropping out of memory” cliff.
- Improves inserts by a small constant (say, 1x-4x).



# Write optimization techniques in production

## B-trees with an online in-RAM buffer

- Flush multiple operations to same leaf
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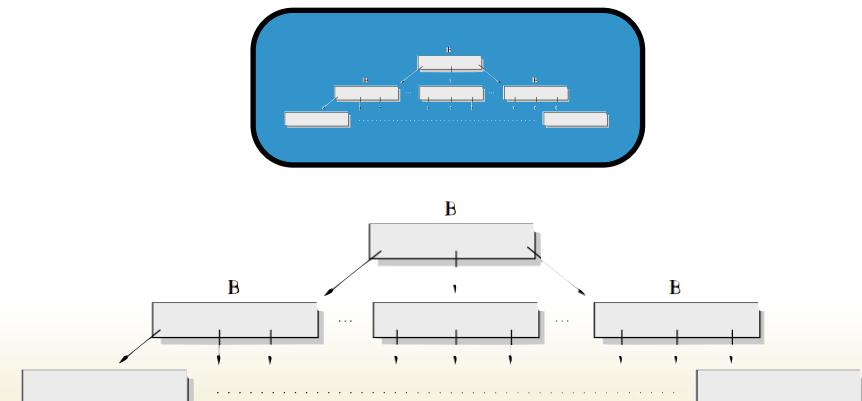
## Analysis Experience

- Smooths out the “dropping out of memory” cliff.
- Improves inserts by a small constant (say, 1x-4x).

## Used in

- InnoDB, Vertica, ...

## in-RAM buffer



# Write optimization techniques in production

## **OLAP: B-tree with an offline log of inserts**

- When log gets big enough (say  $cN$ ), sort and insert.
  - ▶ Or do this operation during scheduled down time.
- To queries: search in B-tree.
  - ▶ There's a time lag before data gets into queryable B-tree, so queries are on stale data.
  - ▶ This is called data latency.

# Write optimization techniques in production

## **OLAP: B-tree with an offline log of inserts**

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## **Analysis**

- $cB$  insertions per leaf.
- Increasing  $c$  increases throughput but also latency.

# Write optimization techniques in production

## **OLAP: B-tree with an offline log of inserts**

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## **Analysis**

- $cB$  insertions per leaf.
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## **Marketing is king**

- Not clear why this is OnLine Analytical Processing.

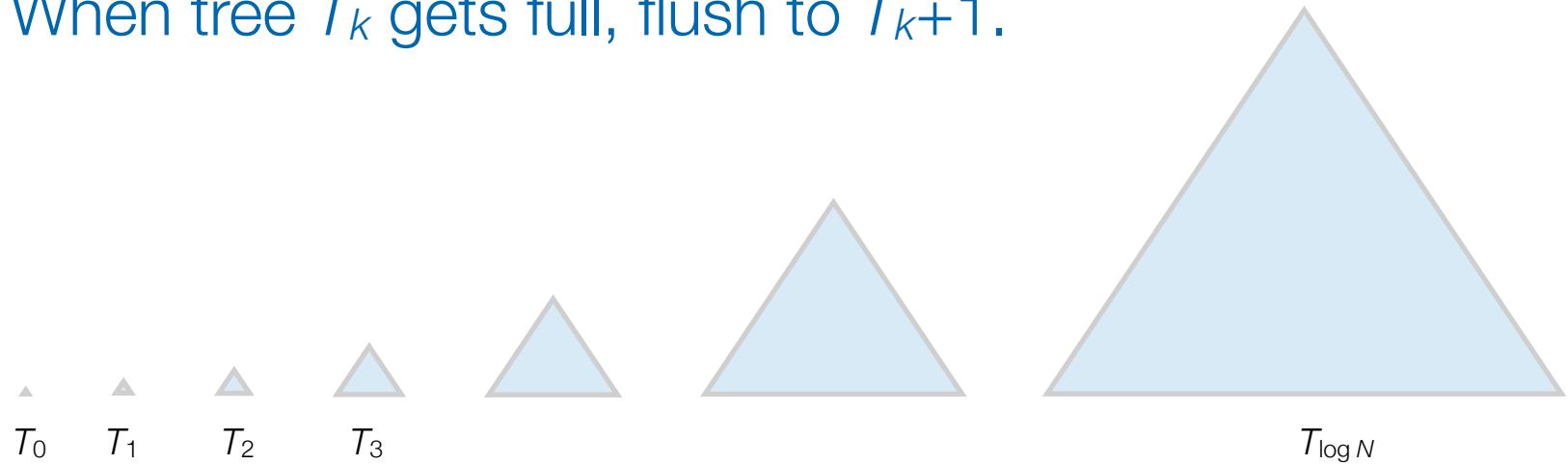
# Write optimization techniques in production

## Cascading:

[O'Neil, Cheng, Gawlick, O'Neil 96]

## Log structured merge (LSM) trees

- Maintain cascading B-tree  $T_1, \dots, T_{\log N}$ ,  $|T_i| < c^i$
- When tree  $T_k$  gets full, flush to  $T_{k+1}$ .



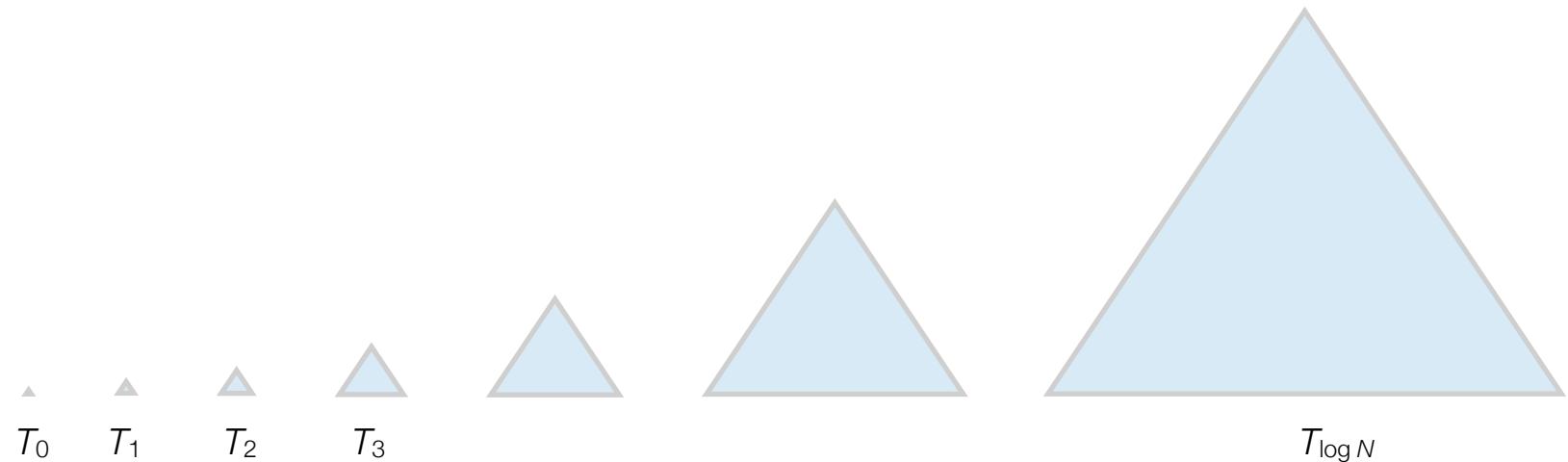
## LSM Analysis

- Inserts:  $O((\log N)/B)$ . ✓
- Queries:  $O(\log N \log_B N)$ . ✗

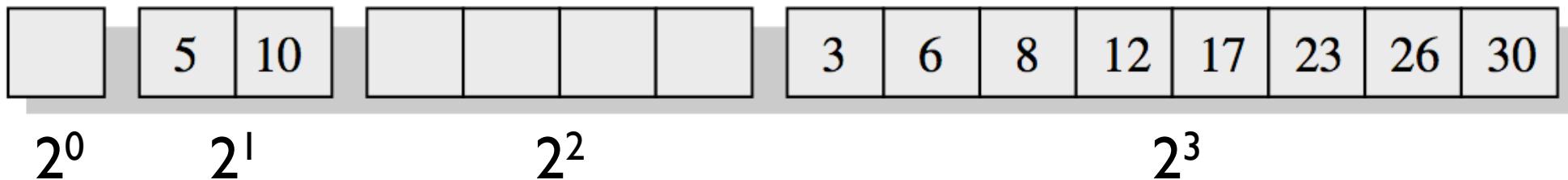
# Write optimization techniques in production

## LSMs in production:

- Big-Table, Cassandra, H-base
- Bloom filters to improve performance.
- Some LSM implementations (e.g. Cassandra, H-base) don't even have a successor operation, because it runs too slowly.



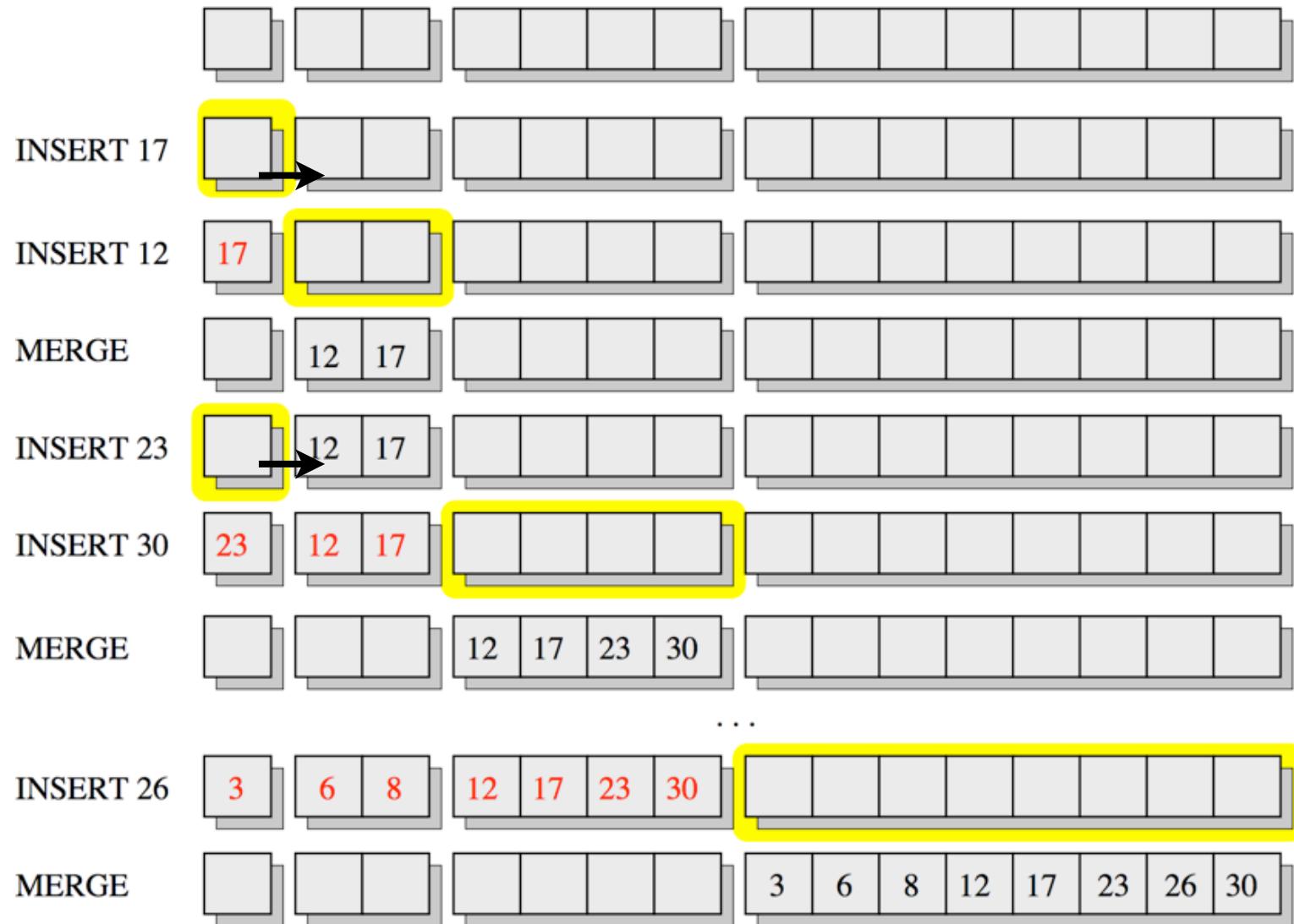
# Simplified CO Lookahead Tree (COLA)



**$O((\log N)/B)$  insert cost &  $O(\log^2 N)$  search cost**

- It's an LSM, except we keep arrays instead of B-trees.
- A factor of  $O(\log_B N)$  slower on searches than an LSM.
- We'll use “fractional cascading” to search in  $O(\log N)$ .

# COLA Insertions (Similar to LSMs)



# Analysis of COLA



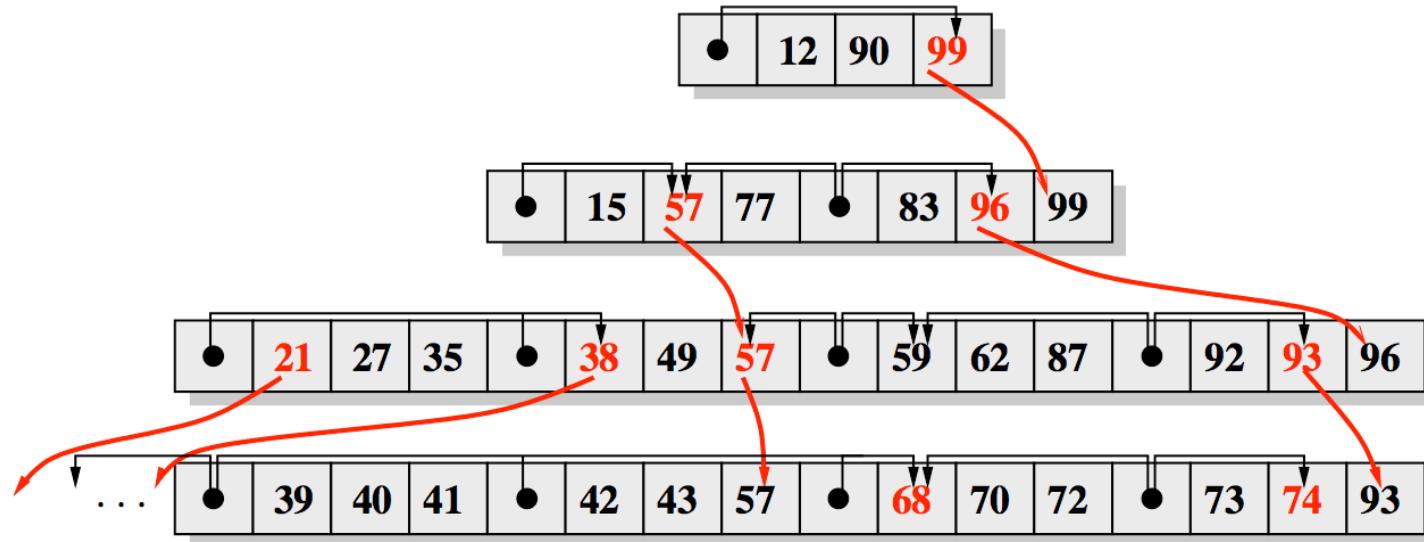
## Insert Cost:

- cost to flush buffer of size  $X = O(X/B)$
- cost per element to flush buffer =  $O(1/B)$
- max # of times each element is flushed =  $\log N$
- insert cost =  $O((\log N)/B)$  amortized memory transfers

## Search Cost

- Binary search at each level
- $\log(N/B) + \log(N/B) - 1 + \log(N/B) - 2 + \dots + 2 + 1$   
=  $O(\log^2(N/B))$

# Idea of Faster Key Searches in COLA



**$O(\log (N/B))$  search cost**

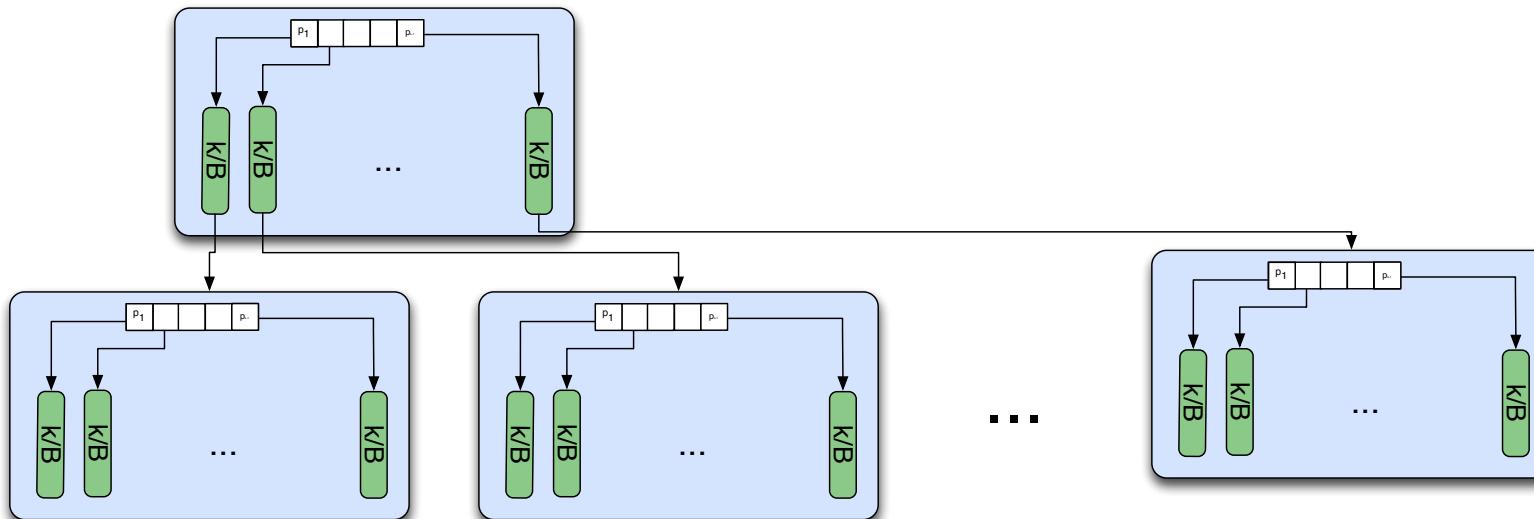
- Some redundancy of elements between levels
- Arrays can be partially full
- Horizontal and vertical pointers to redundant elements
- (Fractional Cascading)

## Arrays can grow by bigger factors

- Larger growth makes insertions slower but queries faster.
- It's the same tradeoff curve as a  $B^\epsilon$ -tree. (See below.)
- In order to get the full tradeoff curve, you need a growth factor that depends on  $B$ .
  - ▶ You loose cache-obliviousness.
- The xDict achieves  $O(\log_B N)$  searches while staying cache-oblivious.
  - ▶ We don't know of an implementation, but would love to hear about it.

## k-tree with $k/B$ edge buffers

- Branching factor of  $k$ .
- Each branch gets a buffer of size  $k/B$ .
  - ▶ All buffers in a node total size  $B$ .
- When a buffer fills, flush to child.



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The diagram illustrates the blocking of a B-tree using edge buffers. It shows a hierarchical tree structure where nodes are logically grouped together. The top level has  $M$  elements with a fan-out of  $M/B$ . The tree is shown across multiple levels, with each level having a height of  $O(\log_{M/B} \frac{N}{B})$ . The nodes at each level contain green squares representing data elements and red squares representing buffers. The main idea is to logically group nodes together and add buffers. Insertions are done in a "lazy" way, where elements are inserted into buffers. When a buffer runs full, elements are pushed one level down.

Blocking of B-tree: Buffer-tree

$M$  elements  
fan-out  $M/B$

$B$

$O(\log_{M/B} \frac{N}{B})$

- Main idea: Logically group nodes together and add buffers
  - Insertions done in a "lazy" way – elements inserted in buffers
  - When a buffer runs full elements are pushed one level down

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Databases and External Memory

# $B^\epsilon$ -tree Performance

**Searches:  $O(\log_k N)$**

**Insertions:**

- Cost to flush a buffer:  $O(1)$ .
- Cost to flush a buffer, per element:  $O(k/B)$ .
- # of flushes per element = height of tree:  $O(\log_k N)$ .
- Total amortized cost to flush to a leaf:  $O(k \log_k N / B)$ .
- Pick  $k = B^\epsilon$ 
  - ▶ Searches:  $O((1/\epsilon) \log_B N)$ , as good as B-tree for constant  $\epsilon$ .
  - ▶ Insertions:  $O(\log_B N / \epsilon B^{1-\epsilon})$ , as good as LSMs.

Write optimization. ✓ What's missing?

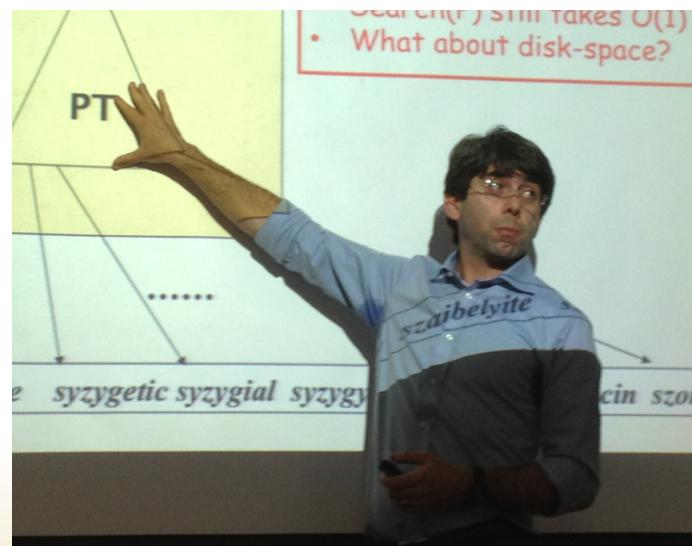
## A real implementation must deal with

- Variable-sized rows
- Concurrency-control mechanisms
- Multithreading
- Transactions, logging, ACID-compliant crash recovery
- Optimizations for the special case of sequential inserts and bulk loads
- Compression
- Backup

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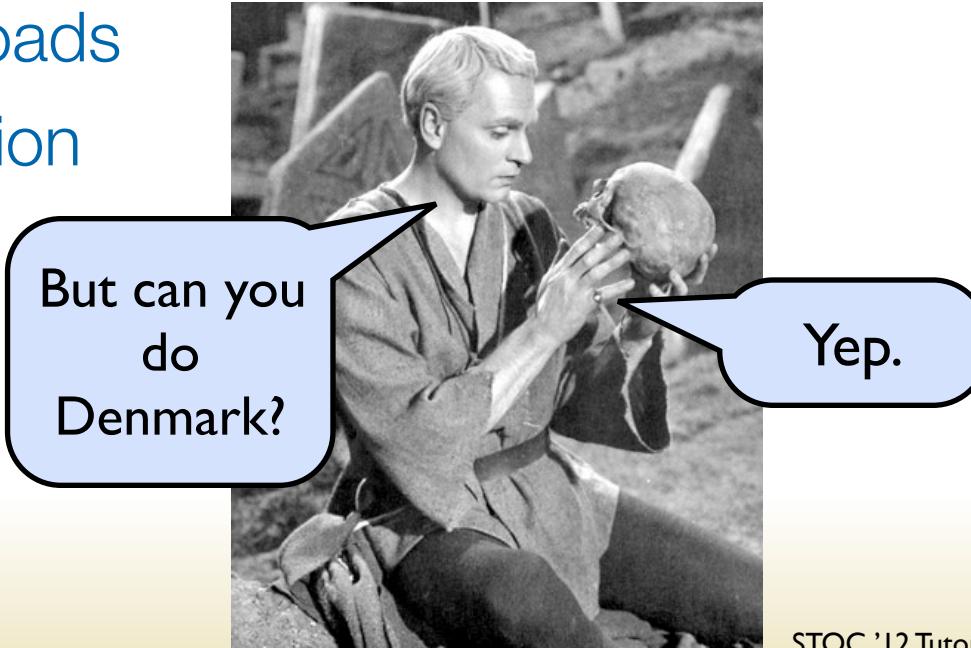
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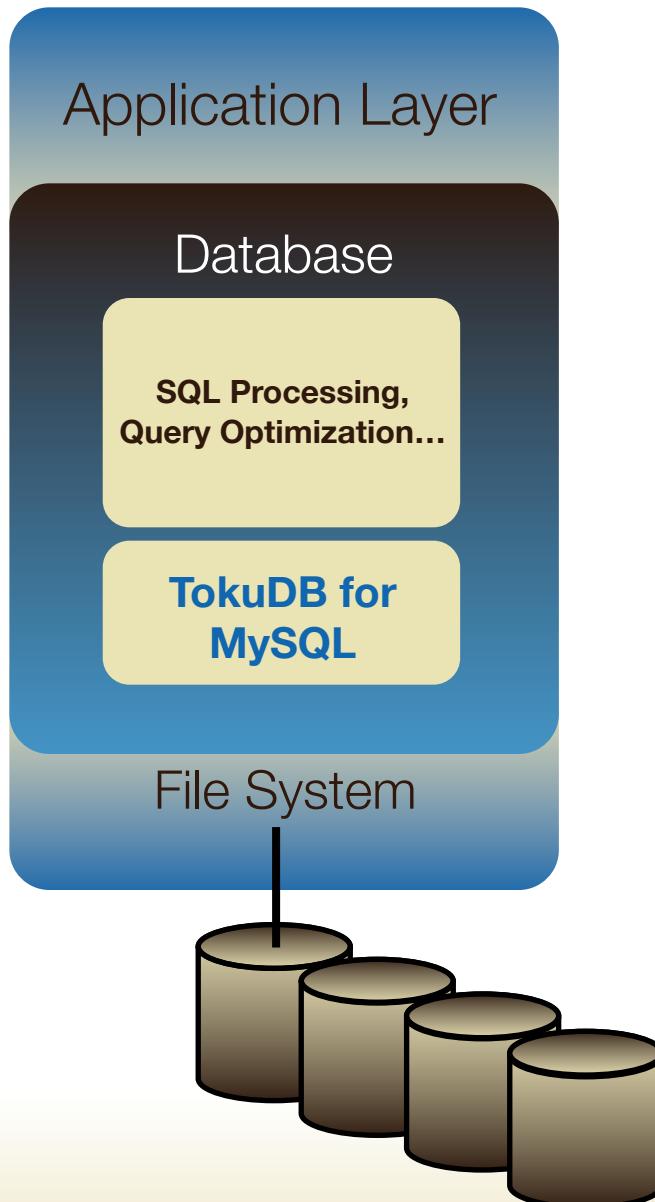
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# Fractal Trees are $B^\varepsilon$ -tree+COLA+Stuff



## TokuDB®, an industrial-strength Fractal Tree

- Berkeley DB API (a B-tree API)
- Full featured (ACID, compression, etc).

## TokuDB is a storage engine for MySQL

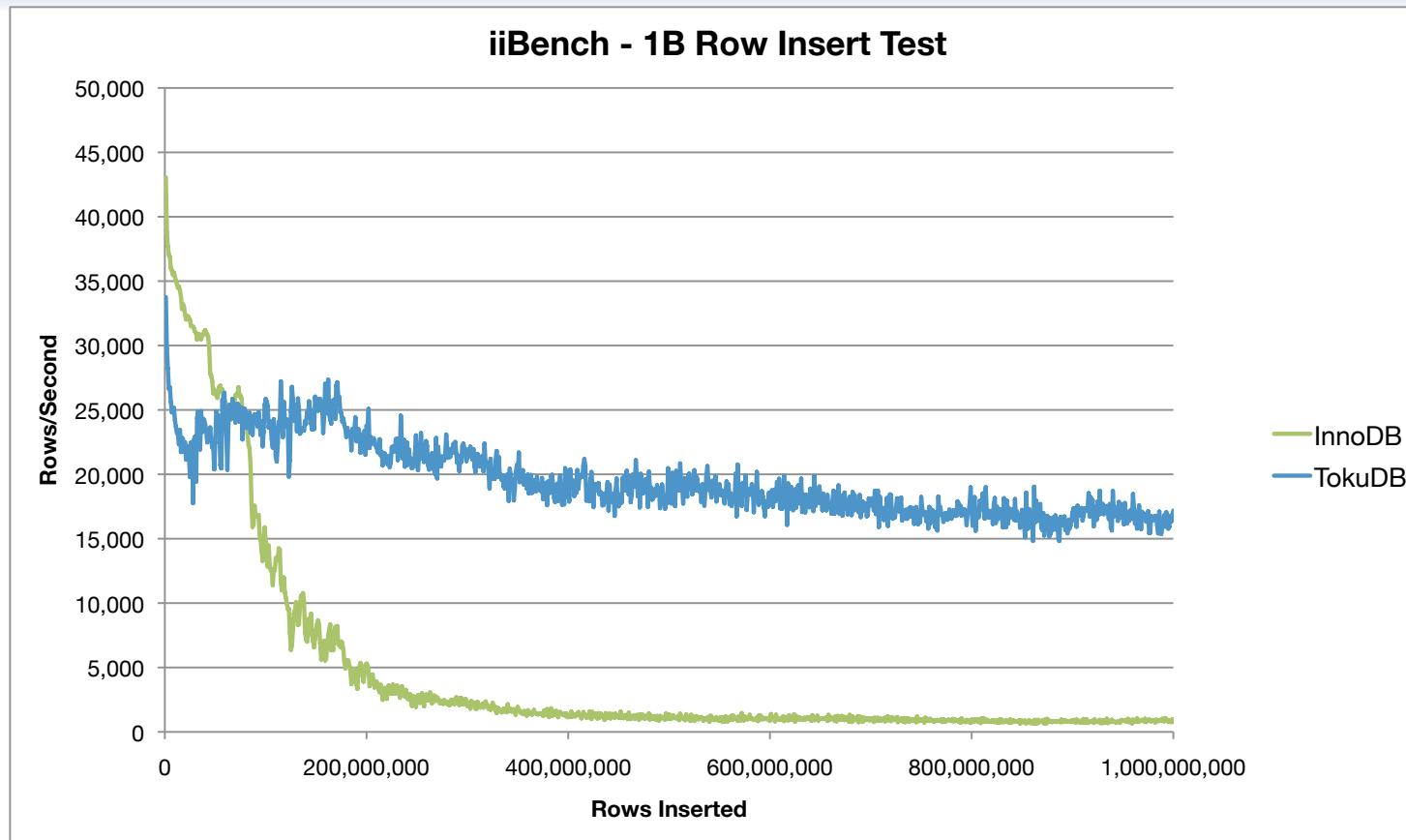
- Role of storage engine: maintains on-disk data

## TokuDB inherits Fractal Tree speed

- 10x-100x faster index inserts

*Tokutek is marketing this technology.*

# iiBench Insert Benchmark is CPU bound



**Fractal Trees scale with disk bandwidth not seek time.**

- But in practice, there's another bottleneck -- we are CPU bound. We cannot (yet) take full advantage of more cores or disks. This must change. (not what I expected from theoretical mode).

# Fun Thing about Write Optimization

## Time to fill a disk in 1973, 2010, and 2022.

- log data sequentially, index data in B-tree, index in Fractal Trees.

Year	Size	Bandwidth	Access Time	Time to log data on disk	Time to fill disk using a B-tree (row size 1K)	Time to fill using Fractal tree* (row size 1K)
1973	35MB	835KB/s	25ms	39s		
2010	3TB	150MB/s	10ms	5.5h		
2022	220TB	1.05GB/s	10ms	2.4d		

*Fancy indexing structures may be a luxury now, but they will be essential by the decade's end.*

\* Projected times for fully multi-threaded version

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# Remember Tables?

**A table is a set of indexes where:**

- One index is distinguished as *primary*.
  - ▶ The key of the primary index is *unique*.
- Every other index is called *secondary*.
  - ▶ There's a bijection 'twixt the rows of a secondary and primary indexes.
  - ▶ The value of a secondary index is the key of the primary index for the corresponding row.

**Constraints have performance impact.**

- Why?

a	b	c	b	a
100	5	45	5	100
101	92	2	6	165
156	56	45	23	206
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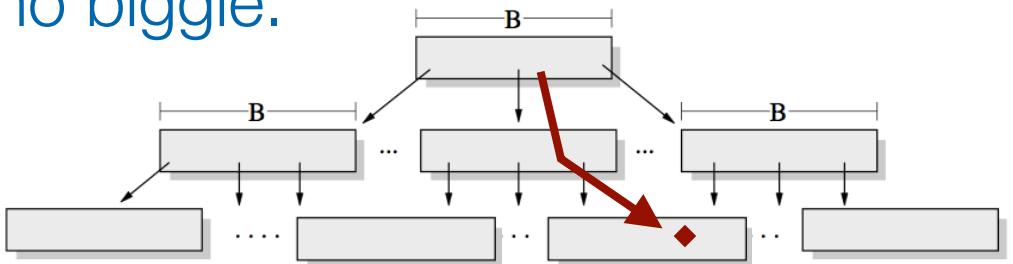
# Uniqueness Checking...

**Uniqueness checking has a hidden search:**

```
If Search(key) == True  
    Return Error;  
Else  
    Fast_Insert(key,value);
```

**In a B-tree uniqueness checking comes for free**

- On insert, you fetch a leaf.
- Checking if key exists is no biggie.



# Uniqueness Checking...

**Uniqueness checking has a “crypto-search”:**

```
If Search(key) == True  
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Else  
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```

**In a write-optimized structure, that pesky search can throttle performance**

- Insertion messages are injected.
- These eventually get to “bottom” of structure.
- Insertion w/Uniqueness Checking 100x slower.
- Bloom filters, Cascade Filters, etc help.

[Bender, Farach-Colton, Johnson, Kraner, Kuszmaul, Medjedovic, Montes, Shetty, Spillane, Zadok 12]

# Uniqueness Checking...

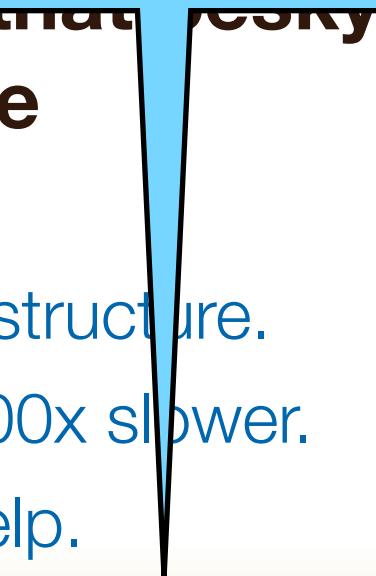
## Uniqueness checking has a cost

```
If Search(key) == True  
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Else  
    Insert(key,value);
```

In a worst case, every search requires a full traversal of the balanced structure, that is,  $O(n)$  time performance.

- Insertions are slow because keys are injected.
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# How do deletes work?

## Tombstone message?

- A tombstone message is a message that kills a row once it meets up with it.
- But in order to insert a tombstone message into secondary indexes, we need to know the value by which they have been indexed.
- This requires a search in the primary index.

## How do we solve this?

- In this case, by considering the use cases for deletions in DBs.
- We can make range deletions fast, for example.

# Are there other crypto searches?

## Oh yes!

- Traditional row locking for transactions.
  - ▶ Solve by having a new data structure for locking, rather than locking at the leaf.
- Deletions with primary-only index.
  - ▶ Even without secondary indexes, the semantics of deletion usually require a return message to say that the deleted key existed, and an error if you try to delete something that didn't exist to begin with.
  - ▶ Solve by convincing customers to accept the faster semantics.
- ...

# Conclusion

**DB indexing is a rich field.**

**Data structures make a big difference here.**

**There are loads of open problems.**

- But they are usually only interesting if you take the time to really learn the use case.

**What does Tokutek mean?**

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Toku → 得 → To Profit

↓  
**若**

Cacher → Cache → Cache-Oblivious Analysis

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To Hide

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- 1. Cache-Oblivious Analysis
- 2. ???
- 3. Profit