Huffman Coding (An Application of Binary Trees and Priority Queues)

Textbook Ch 16.3

Compression

- Definition
 - Reduce size of data
 (number of bits needed to represent data)
- Benefits
 - Reduce storage needed
 - Reduce transmission cost / latency / bandwidth

Huffman Coding

- Proposed by Dr. David A. Huffman in 1952
 - "A Method for the Construction of Minimum Redundancy Codes"
- A form of statistical coding
 - Use variable length codes based on frequency

The Basic Idea

- Not all characters occur with the same frequency!
- Yet all characters are allocated the same amount of space
 - 1 char = 1 byte, be it Θ or X
- Idea: tailoring codes to frequency of characters
 - Use fewer bits to represent frequent characters
 - Use more bits to represent infrequent characters

Example

Symbol	Α	В	С	D
Frequency	12.5%	25%	50%	12.5%
Original Encoding	00	01	10	11
	2 bits	2 bits	2 bits	2 bits
Huffman Encoding	110	10	0	111
	3 bits	2 bits	1 bit	3 bits

Expected size

- Original $\Rightarrow 1/8 \times 2 + 1/4 \times 2 + 1/2 \times 2 + 1/8 \times 2 = 2$ bits / symbol
- Huffman \Rightarrow 1/8×3 + 1/4×2 + 1/2×1 + 1/8×3 = 1.75 bits / symbol

Algorithm

- 1. Scan text to be compressed and count frequencies of all characters.
- 2. Prioritize characters based on their frequencies in text.
- 3. Build Huffman code tree based on prioritized list.
- Perform a traversal of tree to determine all code words.
- 5. Encode the text using the Huffman codes.

Scan the text

Consider the following short text:

Eerie eyes seen near lake.

What characters are present?

```
E e r i space
y s n a r l k .
```

Scan the text

Consider the following short text:

Eerie eyes seen near lake.

What is the frequency of each character in the text?

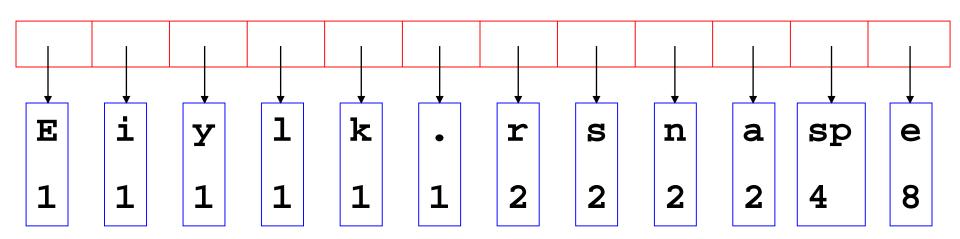
Char	Freq.	Char	Freq.	Char	Freq.
E	1	y	1	k	1
e	8	S	2		1
r	2	n	2		
i	1	a	2		
spac	ce 4	1	1		

Prioritize characters

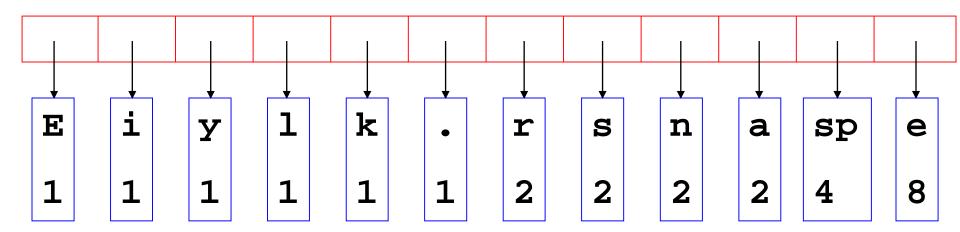
- Create binary tree nodes with character and frequency of each character
- Place nodes in a priority queue
 - The lower the occurrence, the higher the priority in the queue

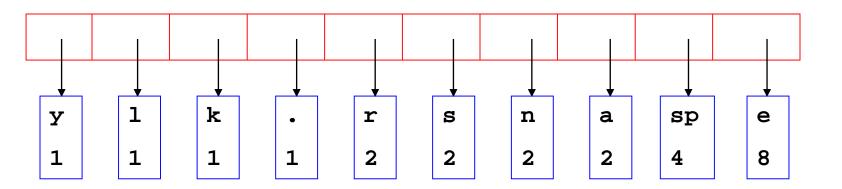
Prioritize characters

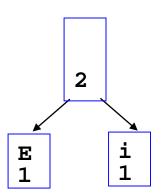
The priority queue after inserting all nodes

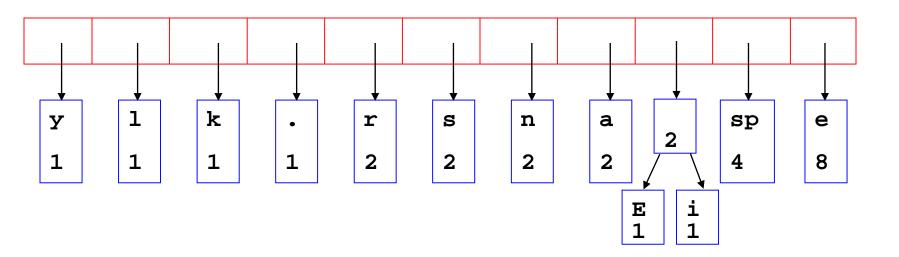


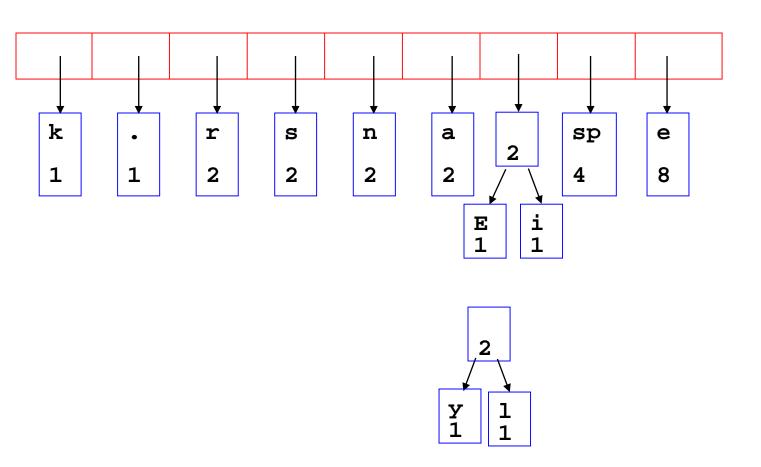
- While priority queue contains two or more nodes
 - Create new node
 - Dequeue node and make it left subtree
 - Dequeue next node and make it right subtree
 - Frequency of new node equals sum of frequency of left and right children
 - Enqueue new node back into queue

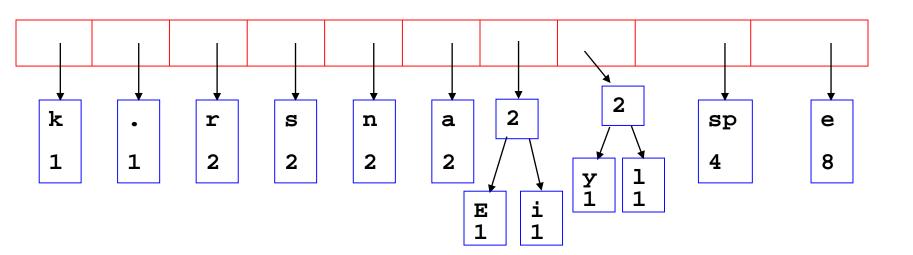


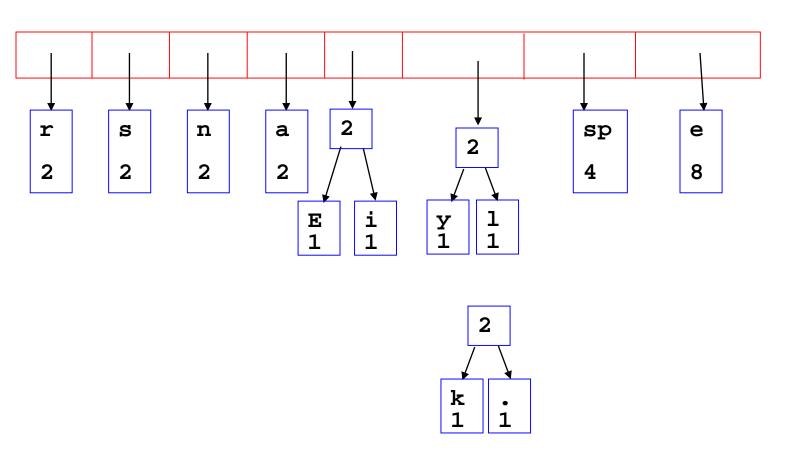


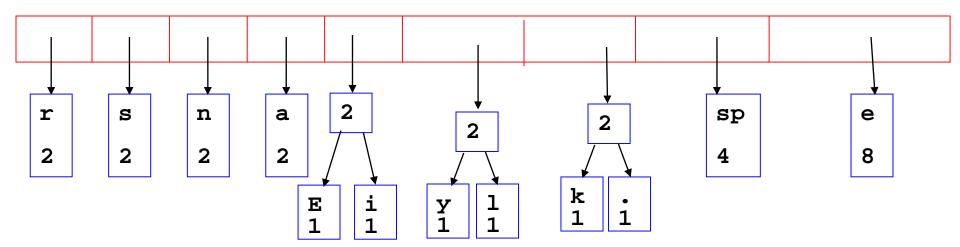


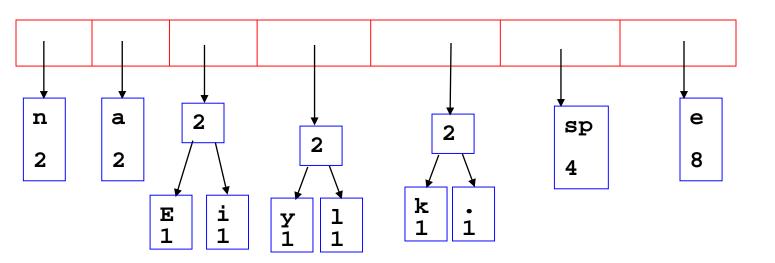


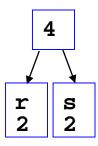


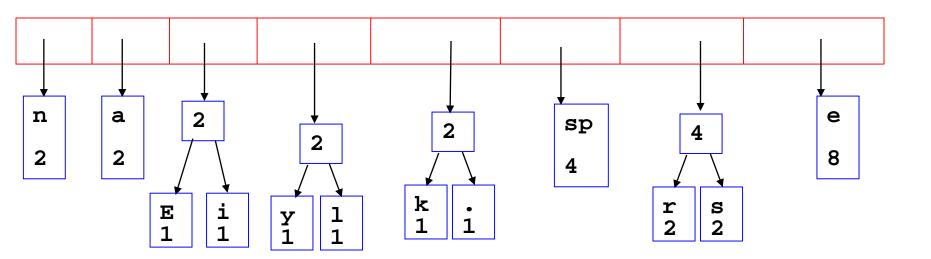


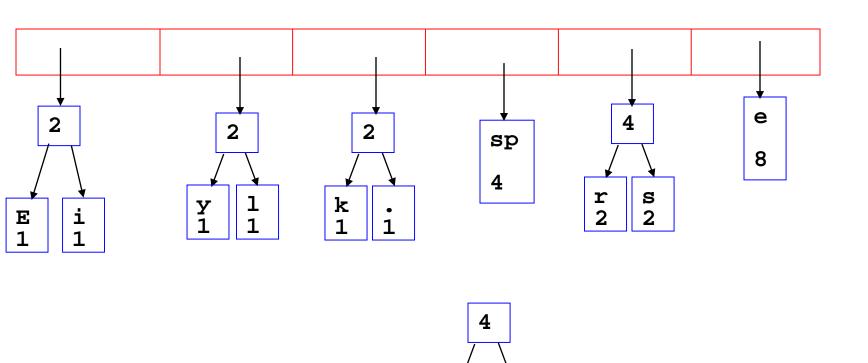




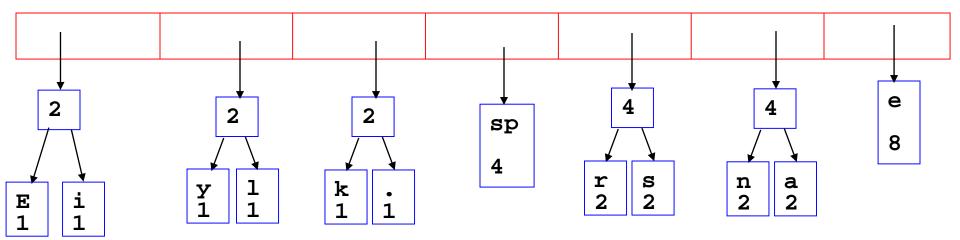


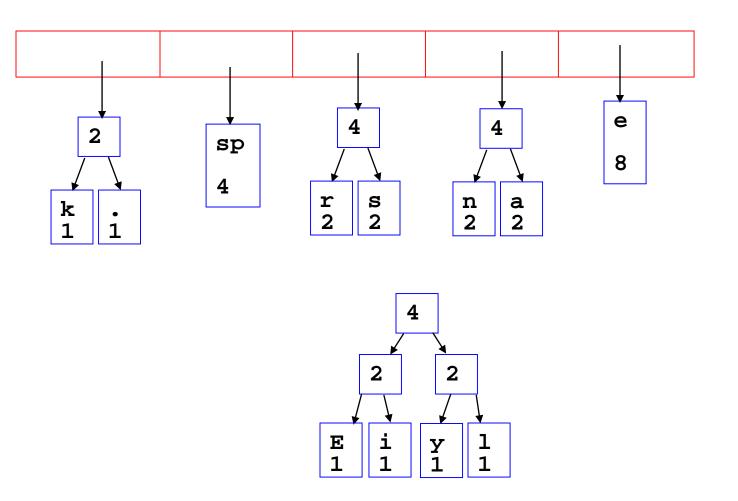


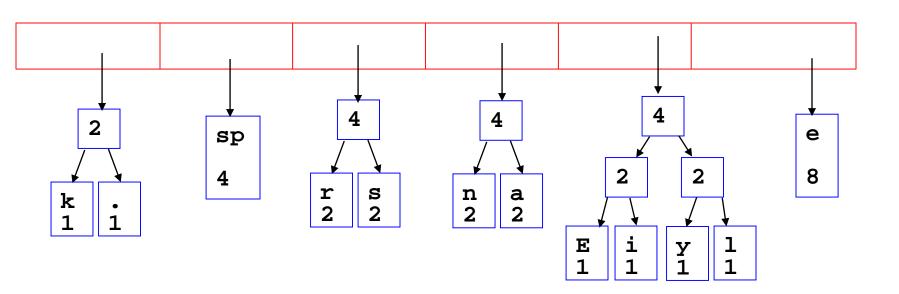


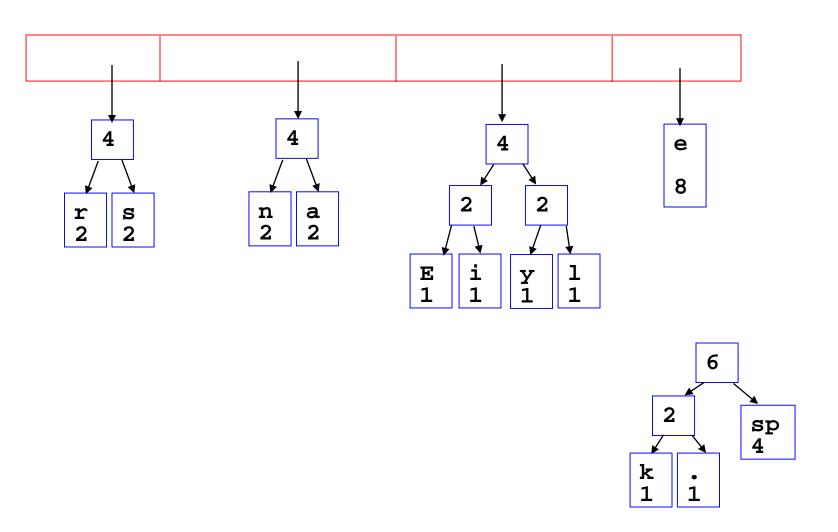


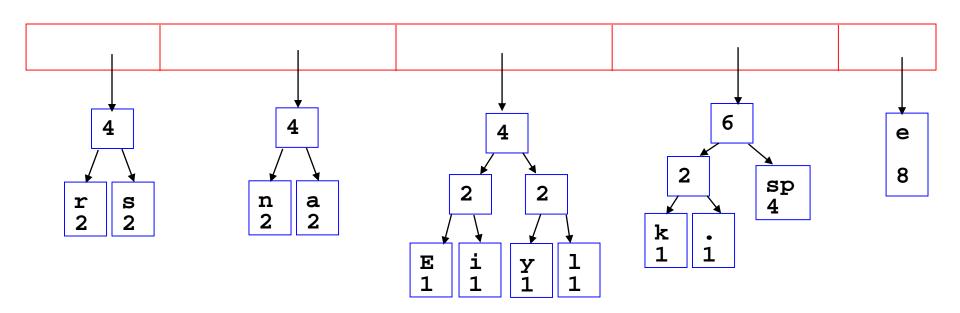
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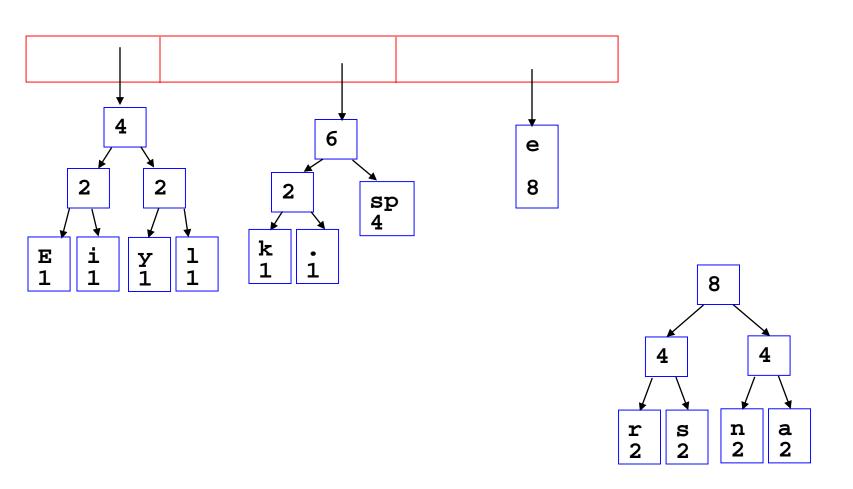


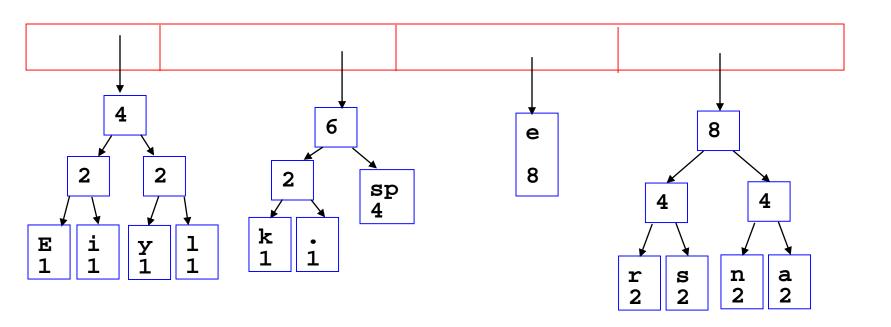


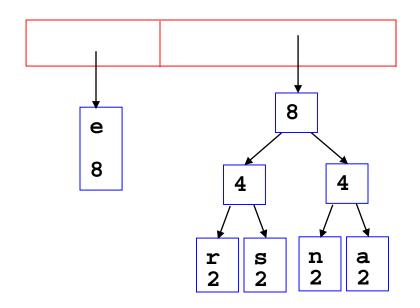


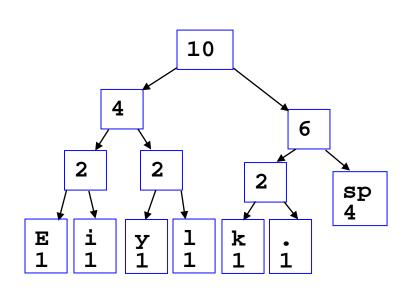


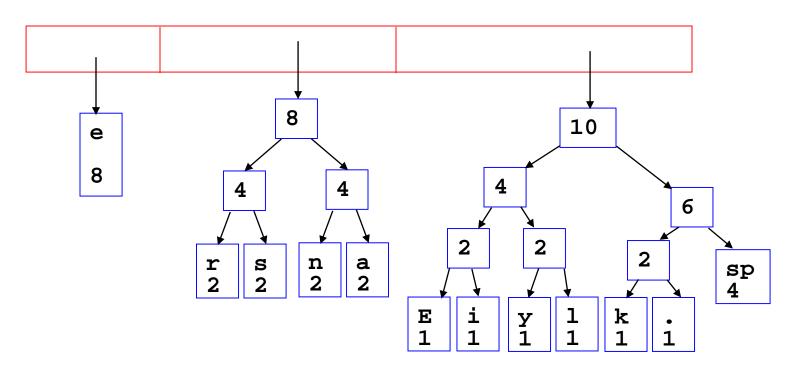


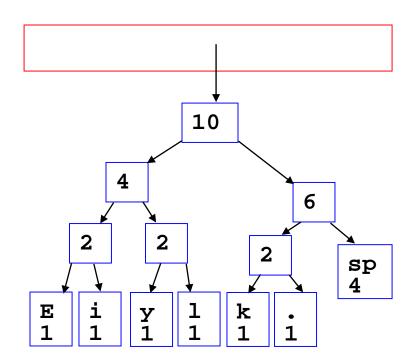


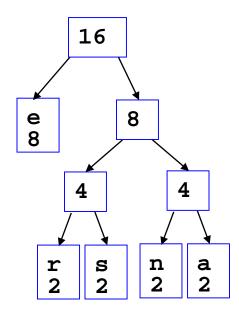


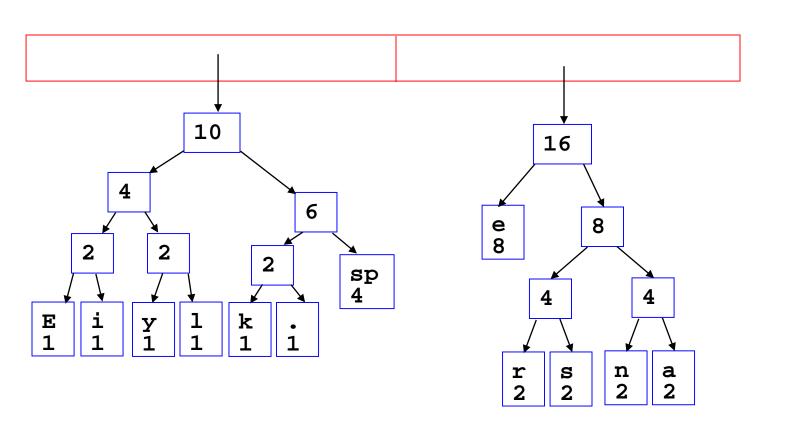


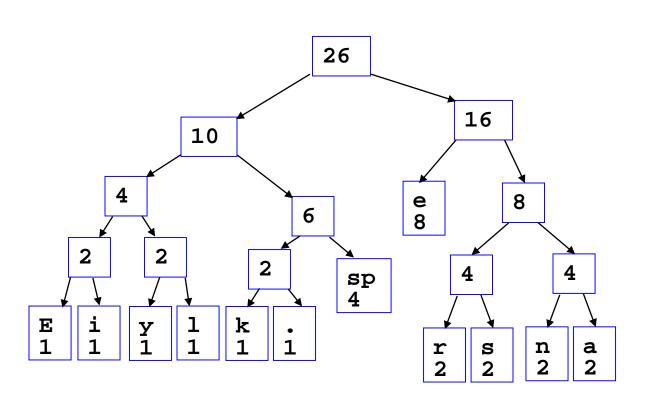








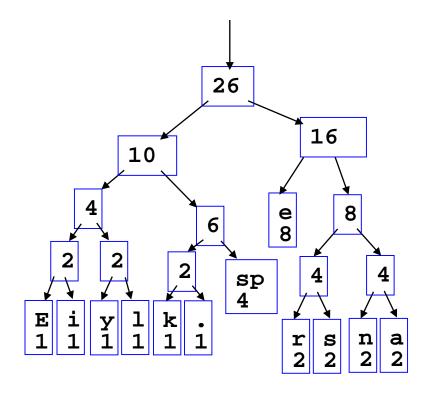




- This tree contains the new code words for each character.
- Frequency of root node should equal number of characters in text.

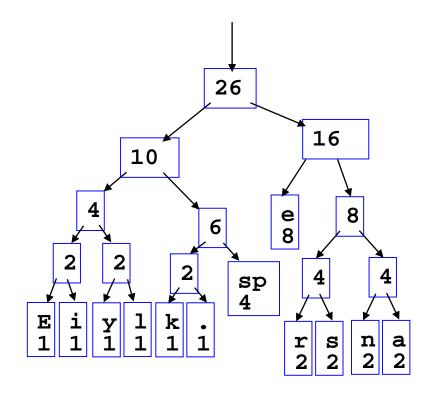
Eerie eyes seen near lake.

1 26 characters



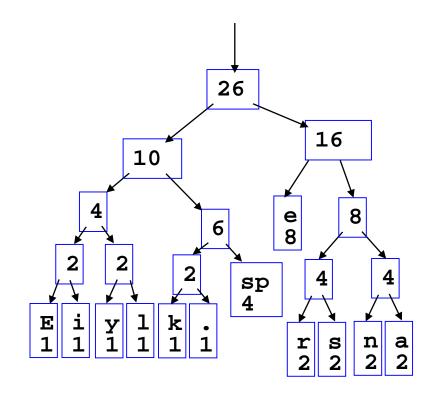
Traverse Tree for Codes

- Perform a traversal of the tree to obtain new code words
 - Going left is a 0
 - Going right is a 1
 - Code word is only completed when a leaf node is reached



Traverse Tree for Codes

Char	Code
E	0000
i	0001
У	0010
1	0011
k	0100
•	0101
space	011
е	10
r	1100
S	1101
n	1110
a	1111



Encoding the File

 Rescan text and encode file using new code words

Eerie eyes seen near lake.

Char	Code
E	0000
i	0001
У	0010
1	0011
k	0100
•	0101
space 011	
е	10
r	1100
S	1101
n	1110
a	1111

Encoding the File

- Have we made things any better?
 - 73 bits to encode the text
 - ASCII would take 8 * 26 = 208 bits

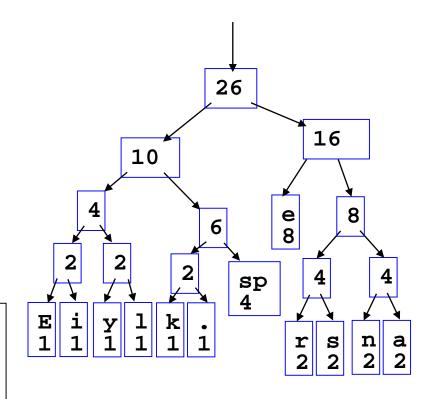
Eerie eyes seen near lake.

Char	Code
E	0000
i	0001
У	0010
1	0011
k	0100
•	0101
space 011	
е	10
r	1100
S	1101
n	1110
a	1111

Encoding the File

- Why is there no need for a separator character?
- Prefix property
 - No code is a prefix of another code

Eerie eyes seen near lake.



Decoding the File

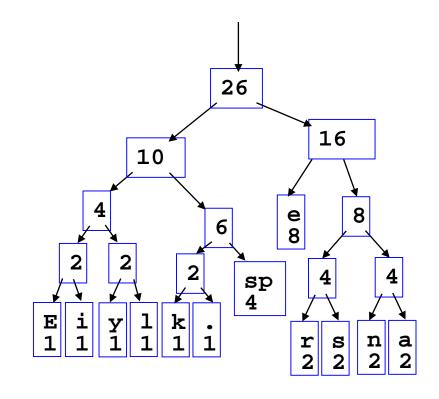
- How does receiver know what the codes are?
- Two solutions
 - Tree constructed for each text file
 - Codes customized for each file
 - Big hit on compression, especially for smaller files
 - Tree predetermined
 - Based on statistical analysis of general text files or file types

Decoding the File

- Once receiver has the tree, it scans incoming bit stream
 - 0 \Rightarrow go left
 - $-1 \Rightarrow$ go right

101000110111101111011 11110000110101

eel snarl.



Summary

- Huffman coding is a technique used to compress files
- Uses statistical coding
 - more frequently used symbols have shorter code words
- Uses two data structures
 - Priority queue
 - Binary tree