# Topic 2 Basic Logic Gates

#### **Electronic Switch – Transistors**

## • Transistors are the basis of binary digital circuits

Transistors operate at 2 values
 H / L or
 On / Off or
 1 / 0

#### Evolution of electronic switches

- 1930s: Relays

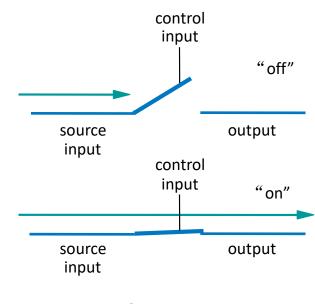
- 1940s: Vacuum tubes

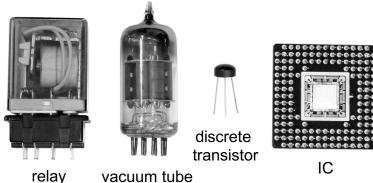
- 1950s: Discrete transistor

- 1960s: Integrated circuits (ICs)

• Initially just a few transistors on IC

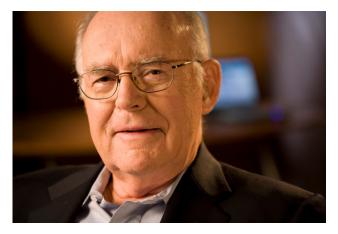
• Then tens, thousands, millions...

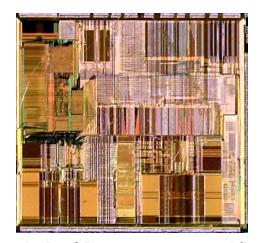




#### Moore's Law

- IC capacity doubling about every 18 months for several decades
  - Known as "Moore's Law" after Gordon Moore, co-founder of Intel
    - Predicted in 1965 predicted that components per IC would double roughly every 18 months or so
  - For a particular number of transistors, the IC shrinks by half every 18 months
    - Enables incredibly powerful computation in incredibly tiny devices
  - Today's ICs hold billions of transistors
    - The first Pentium processor (early 1990s) had only 3 million

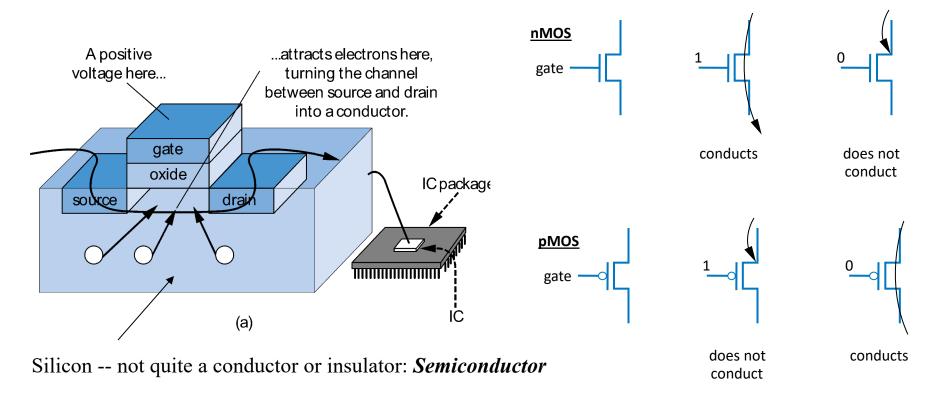




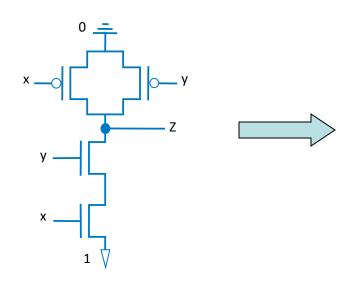
An Intel Pentium processor IC having millions of transistors

#### **CMOS** Transistor

- CMOS Complementary Metal-Oxide-Semiconductor
- Transistors with CMOS technology



#### **AND Logic**

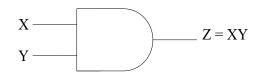


X	Y	Z = XY
0	0	0
0	1	0
1	0	0
1	1	1

Truth Table

#### **Definition of AND operation**

 $Z = X \cdot Y$  means Z = 1 if and only if both X = 1 and Y = 1; **AND** operator Variable



2-input AND gate

#### **Truth Table**

#### • Truth table creates the relationship between the inputs and outputs

- Must include all the inputs to the device in the left columns
- Must include all the outputs of the device in the right columns
- The behavior of the circuit is implied by the table

Inputs $ \begin{bmatrix} I1 & \longrightarrow \\ I2 & \longrightarrow \\ I3 & \longrightarrow \end{bmatrix} $	Digital Circuit	→O1 >	Outputs
---------------------------------------------------------------------------------------------------------------	--------------------	-------	---------

Number of combinations is 2<sup>N</sup>; N is the number of the inputs

bl	e <sub> </sub>	nputs		Outp	uts
	Ĭ1		I3	01	O2
	0	0	0	?	?
	0	0	1	?	?
	0	1	0	?	?
	0	1	1	?	?
	1	0	0	?	?
	1	0	1	?	?
	1	1	0	?	?
	1	1	1	?	?

### **Example of Truth Table**

а	b	F			
0	0				
0	1				
1	0				
1	1				
(a)					

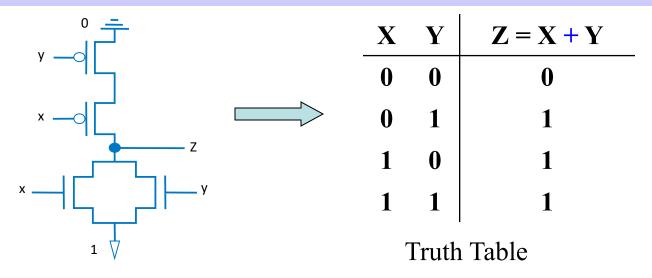
а	b	С	F			
0	0	0				
0	0	1				
0	1	0				
0	1	1				
1	0	0				
1	0	1				
1	1	0				
1	1	1				
(h)						

(a)

а	b	С	d	F
0	0	0	0	
0	0	0	1	
0	0	1	0	
0	0	1	1	
0	1	0	0	
0	1	0	1	
0	1	1	0	
0	1	1	1	
1	0	0	0	
1	0	0	1	
1	0	1	0	
1	0	1	1	
1	1	0	0	
1	1	0	1	
1	1	1	0	
1	1	1	1	
		(c)	)	

(C)

#### **OR** Logic



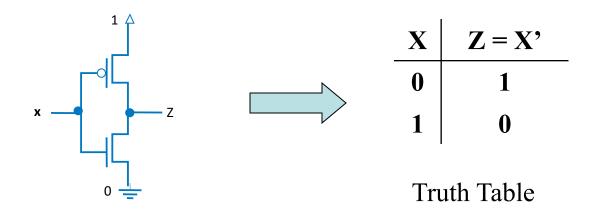
#### Definition of OR operation

Z = X + Y means Z = 1 if either X=1 or Y=1, or both;

OR operator X = X + Y Z = X + Y

2-input OR gate

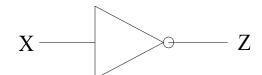
#### **NOT Logic**



#### Definition of NOT operation

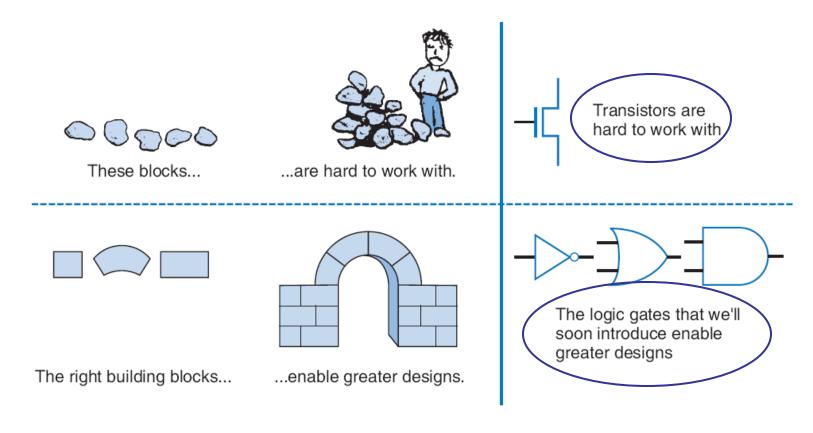
Z = X or  $Z = \overline{X}$  means Z = 0 if X = 1; Z = 1 if X = 0; Z is the complement of X

NOT operator



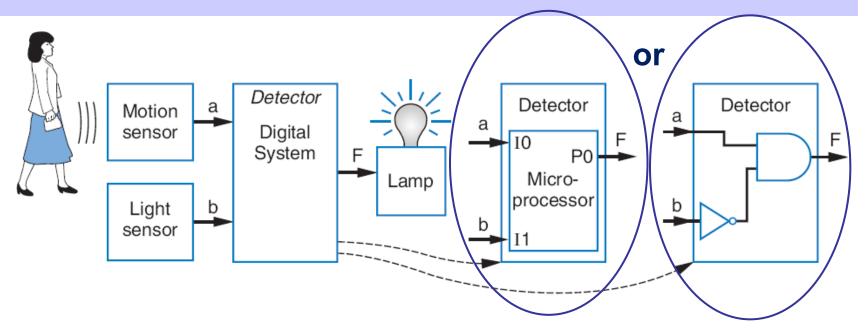
NOT gate/Inverter

#### **Logic Gates**



• "Logic gates" are better digital circuit building blocks than switches (transistors)

#### Logics in Human Language



#### Motion-in-dark example

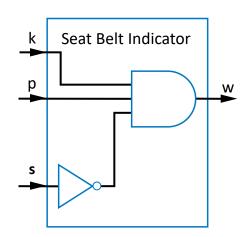
- a: signal from motion sensor, b: signal from light sensor
- Human/programming language: Turn on lamp (F=1) if motion sensed (a) and no light (not b)
- Logic Equation: F = a AND NOT(b) = ab'
- Logic circuit: implementation of equation using logic gates

#### **Example: Seat Belt Warning Light System**

- Design circuit for warning light
- Sensors
  - s: seat belt fastened
  - k: key inserted
  - p: person in seat
- Function description
  - Light on if person in seat,
     and seat belt not fastened,
     and key inserted
- Logic equationw = p AND NOT(s) AND k

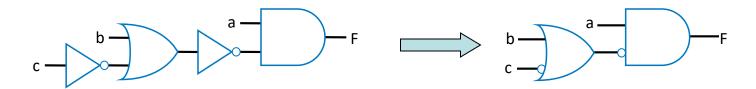






## **Example: Implement Logic Equation with Logic Gates**

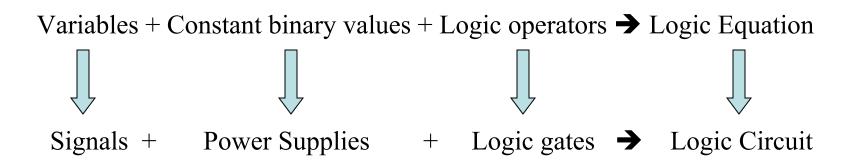
• Q: Implement the following equation with logic gates: F = a AND NOT( b OR NOT(c) )



Precedence of Logic Operations

#### From Logic Equation to Logic Circuit

• There exists a correspondence between a Logic Equation and its logic circuit.

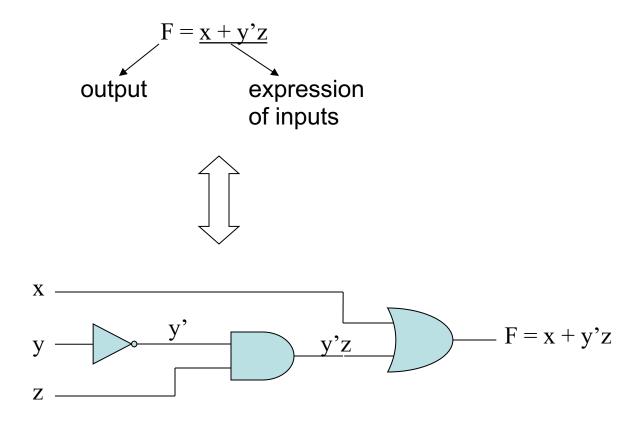


#### Logic Circuit:

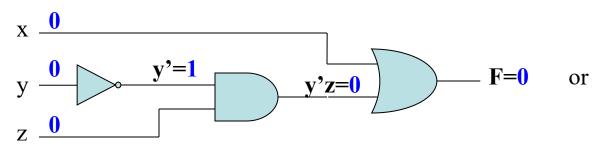
A net of logic gates.

#### Logic Equation and Logic Circuit

•  $F = x OR (NOT y AND Z) = x + y' \cdot z = x + y'z$ 



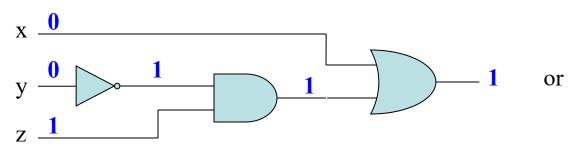
•  $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$ 



$F = 0 + 0 \cdot \bullet 0$
$= 0 + 1 \cdot 0$
= 0 + 0
=0

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	?	?	?
0	1	0	?	?	?
0	1	1	?	?	?
1	0	0	?	?	?
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

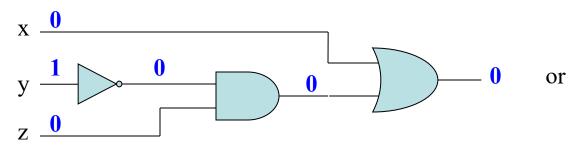
•  $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$ 



$F = 0 + 0' \bullet 1$
$=0+1 \bullet 1$
= 0 + 1
= 1

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	?	?	?
0	1	1	?	?	?
1	0	0	?	?	?
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

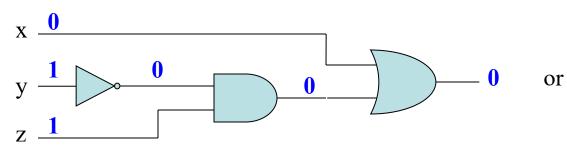
•  $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$ 



$F = 0 + 1' \cdot 0$
$= 0 + 0 \bullet 0$
= 0 + 0
= 0

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	?	?	?
1	0	0	?	?	?
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

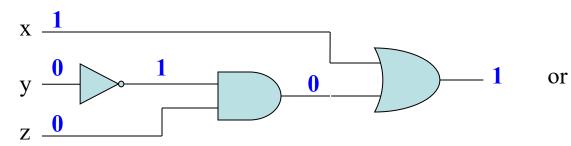
•  $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$ 



F = 0 + 1 • 1
$= 0 + 0 \cdot 1$
= 0 + 0
=0

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	?	?	?
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

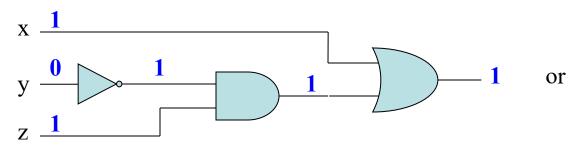
•  $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$ 



$F = 1 + 0 \cdot \bullet 0$
$=1+1 \bullet 0$
= 1 + 0
= 1

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	1	0	1
1	0	1	?	?	?
1	1	0	?	?	?
1	1	1	?	?	?

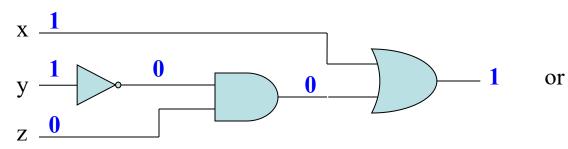
•  $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$ 



F = 1 + 0'• 1
$= 1 + 1 \cdot 1$
= 1 + 1
= 1

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	1	0	1
1	0	1	1	1	1
1	1	0	?	?	?
1	1	1	?	?	?

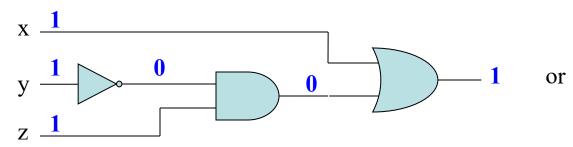
•  $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$ 



$F = 1 + 1' \bullet 0$
$=1+0 \bullet 0$
= 1 + 0
= 1

X	y	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	1	0	1
1	0	1	1	1	1
1	1	0	0	0	1
1	1	1	?	?	?

•  $\mathbf{F} = \mathbf{x} + \mathbf{y}^{2}\mathbf{z}$ 



$F = 1 + 1' \cdot 1$
$= 1 + 0 \cdot 1$
= 1 + 0
= 1

X	у	Z	y'	y'z	F
0	0	0	1	0	0
0	0	1	1	1	1
0	1	0	0	0	0
0	1	1	0	0	0
1	0	0	1	0	1
1	0	1	1	1	1
1	1	0	0	0	1
1	1	1	0	0	1

#### **Build A Truth Table: Another Approach**

b

С

а	b	F		
0	0			
0	1			
1	0			
1	1			
(a)				

а	b	С	F		
0	0	0			
0	0	1			
0	1	0			
0	1	1			
1	0	0			
1	0	1			
1	1	0			
1	1	1			
(b)					

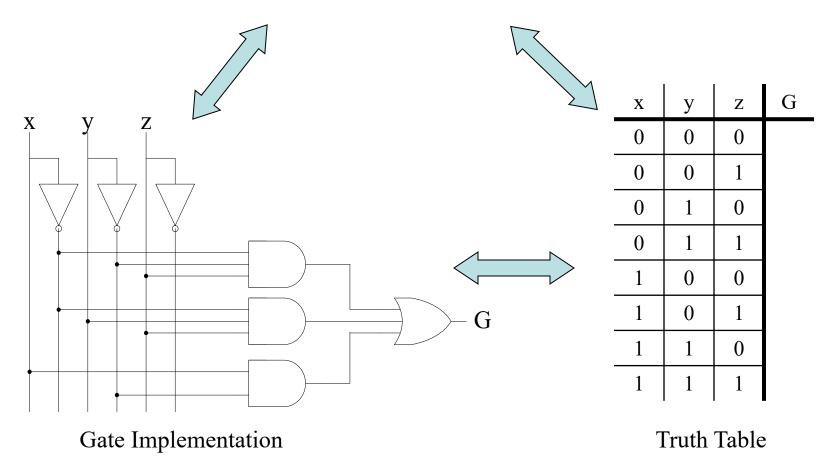
0 (c)

 Q: Use truth table to define function F(a,b,c) that is 1 only when abc is 5 or greater in binary

F	С	b	а	а
0	0	0	0	0
0	1	0	0	0
0	0	1	0	0
0	1	1	0	0
0	0	0	1	1
1	1	0	1	1
1	0	1	1	1
1	1	1	1	1

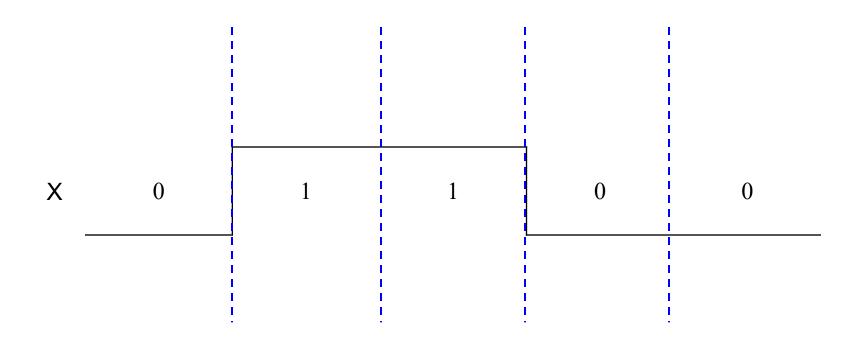
## Representations of I/O Relationship: Equation, Truth Table, & Circuit

• Another example: G = x'y'z + x'yz + xy'



## Timing Diagram: Another Representations of I/O Relationship

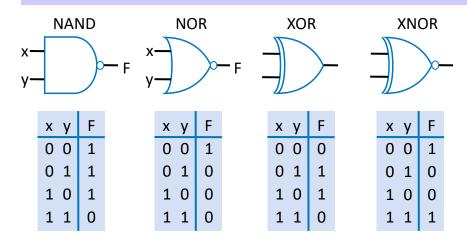
• Timing diagram of one signal shows the response to changes on a signal in voltage levels with time



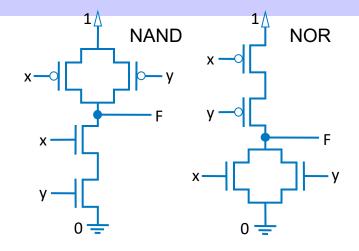
### **Timing Diagrams for Gates**

хy	F				 	 	
0 0	0	X	0	1	1	0	0
0 1	0	<b>X</b>		-			<del></del>
1 0	0				 	 	   
1 1	1	Υ .	0	0	1	1	0
x+y	F						
0 0	0	X•Y	0	0	1	0	0
0 1	1						
1 0	1	V.V	0	1	1	1	0
1 1	1	X+Y	U	1	1	<u> </u> 	
X	F				 		
0	1	X'	1	0	0	1	1
_1	0				 	 	 

#### **More Gates**



- NAND: Opposite of AND ("NOT AND")
- NOR: Opposite of OR ("NOT OR")
- XOR: outputs 1 when inputs have odd number of 1's
- XNOR: Opposite of XOR ("NOT XOR")



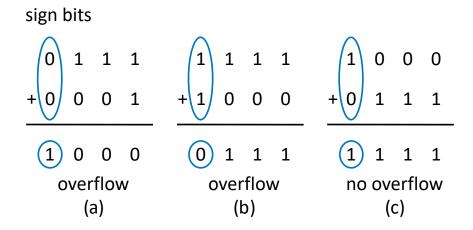
- AND in CMOS: NAND with NOT
- OR in CMOS: NOR with NOT
- So NAND/NOR more common

#### **Recall: Detecting Overflow - Method 1**

#### Overflow detection logic

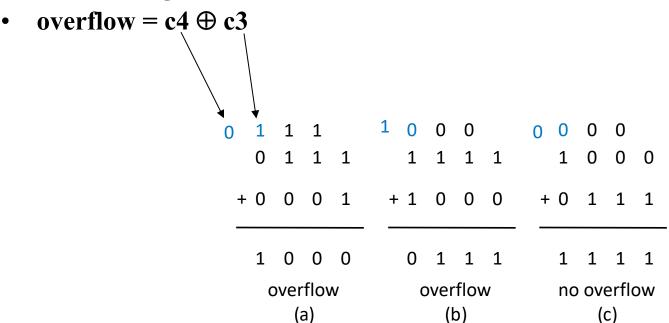
- Two numbers' sign bits are the same but are different from the result's sign bit
- If the two numbers' sign bits are different, overflow is impossible
  - Adding a positive and negative can't exceed largest magnitude positive or negative

#### 4-bit example



#### **Detecting Overflow - Method 2**

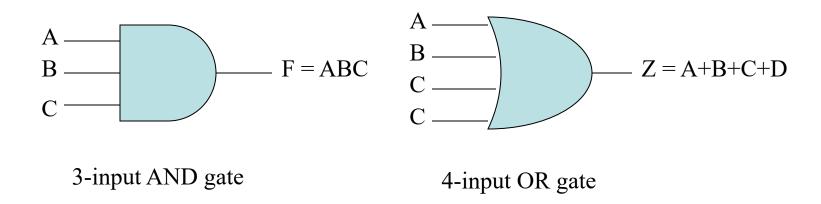
• Simpler method: Detect difference between carry-in to sign bit and carry-out from sign bit



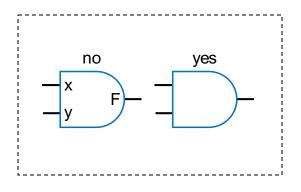
If the carry into the sign bit column differs from the carry out of that column, overflow has occurred.

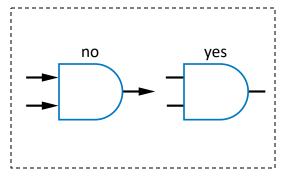
#### **Gates with Multiple Inputs**

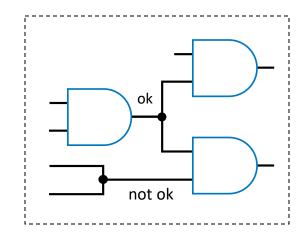
- AND and OR gates may have more than two inputs
- Three-input AND gate responds with logic 1 output if and only if all three inputs are logic 1 (may be generalized)
- Four-input OR gate responds with logic 1 if any input is logic 1; its output becomes 0 if and only if all inputs are logic 0 (may be generalized)



### **Some Circuit Drawing Conventions**







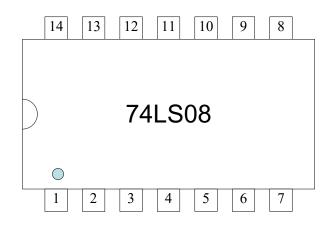
#### **Integrated Circuit**

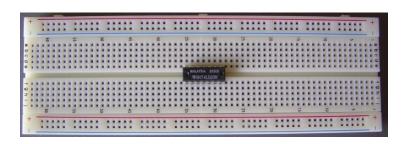
- Integrated Circuit (IC) chip
  - Contains logic components and/or devices for constructing digital circuits
- Integration Levels
  - Small-Scale Integration (SSI)
    - Fewer than 10 gates
  - Medium-Scale Integration (MSI)
    - 10 to 1000 gates
  - Large-Scale Integration (LSI)
    - Thousands of gates
  - Very Large-Scale Integration (VLSI)
    - Millions of gates
  - Ultra Large-Scale Integration (ULSI)
    - Billions of gates

**—** ...

#### **Integrated Circuit**

- TTL Transistor-Transistor Logic
- **ECL** Emitter-Coupled Logic
- **MOS** Metal-Oxide Semiconductor
- **CMOS** Complementary MOS





Chip placed on breadboard

