



Ve270 Introduction to Logic Design

Homework 1

Assigned: May 14, 2020

Due: May 21, 2020, 2:00pm.

A pop quiz will be given on the due date.

1. Fill out the blank spaces, assuming unsigned numbers. Show steps to earn partial credits. (8 points)

$$11011101.001_2 = \underline{\quad}221.125_{10} = \underline{\quad}DD.2_{16}$$

$$63.89_{10} = \underline{\quad}111111.1110_2 = \underline{\quad}77.7_8 = \underline{\quad}2100.220_3$$

2. Fill out the blank spaces, assuming 2's complement numbers. (16 points)

$$-71_{10} = \underline{\quad}10111001_2 = \underline{\quad}B9_{16}$$

$$71_{10} = \underline{\quad}01000111_2 = \underline{\quad}47_{16}$$

$$10110101101_2 = \underline{\quad}-595_{10}$$

$$FBA9_{16} = \underline{\quad}1111\ 1011\ 1010\ 1001_2 = \underline{\quad}-1111_{10}$$

3. Perform the following arithmetic operations step by step, assuming 2's complement numbers: (12 points)

$$(6FA49D + 73BD)_{16} = 70185A_{16} \quad \text{no overflow.}$$

$$(10100 - 10101001)_2 = 01001011_2 \quad \text{no overflow.}$$

$$(534 - 265)_8 = 7247_8 \quad \text{with overflow.} \quad (247_8 \text{ with overflow is also acceptable}).$$

$$\begin{array}{r} 11011 \\ 6FA49D \\ + 73BD \\ \hline 70185A \end{array}$$

$$\begin{array}{r} 11101000 \\ 11110100 \\ + 01010110 \\ \hline 01001011 \end{array}$$

$$\begin{array}{r} 1000 \\ 534 \\ + 512 \\ \hline 7247 \end{array}$$

4. Problem 2.14 (Boolean equation = logic equation) (4 points)

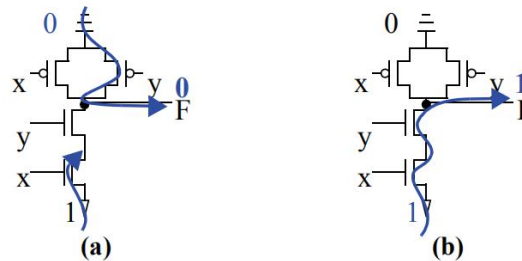
2.14 Evaluate the Boolean equation $F = a \text{ AND } (b \text{ OR } (c \text{ AND } d))$ for the given values of variables $a, b, c,$ and d :

- a. $a=1, b=1, c=0, d=1$
- b. $a=0, b=0, c=0, d=1$
- c. $a=1, b=0, c=0, d=0$
- d. $a=1, b=0, c=1, d=1$

- a) $F = 1 \text{ AND } (1 \text{ OR } (0 \text{ AND } 1)) = 1 \text{ AND } (1 \text{ OR } 0) = 1 \text{ AND } 1 = 1$
- b) $F = 0 \text{ AND } (0 \text{ OR } (0 \text{ AND } 1)) = 0 \text{ AND } (0 \text{ OR } 0) = 0 \text{ AND } 0 = 0$
- c) $F = 1 \text{ AND } (0 \text{ OR } (0 \text{ AND } 0)) = 1 \text{ AND } (0 \text{ OR } 0) = 1 \text{ AND } 0 = 0$
- d) $F = 1 \text{ AND } (0 \text{ OR } (1 \text{ AND } 1)) = 1 \text{ AND } (0 \text{ OR } 1) = 1 \text{ AND } 1 = 1$

5. Problem 2.16 (10 points)

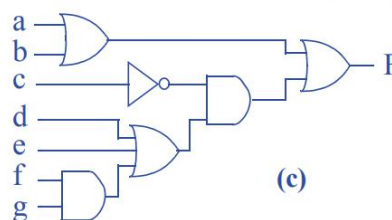
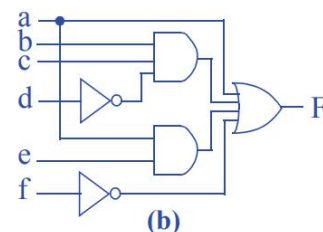
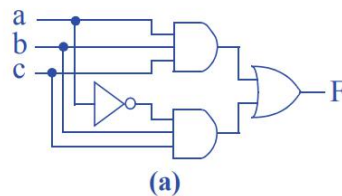
2.16 Show the conduction paths and output value of the AND gate transistor circuit in Figure 2.14 when: (a) $x = 1$ and $y = 0$, (b) $x = 1$ and $y = 1$.



6. Problem 2.19 (10 points)

2.19 Convert each of the following equations directly to gate-level circuits:

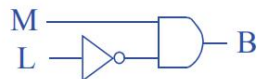
- a. $F = abc + a'bc$
- b. $F = a + bcd' + ae + f'$
- c. $F = (a + b) + (c' * (d + e + fg))$



7. Problem 2.20 (10 points)

2.20 Design a system that sounds a buzzer inside a home whenever motion outside is detected at night. Assume a motion sensor has an output M that indicates whether motion is detected (M=1 means motion detected) and a light sensor with output L that indicates if light is detected (L=1 means light is detected). The buzzer inside the home has a single input B that when 1 sounds the buzzer. Capture the desired system behavior using an equation, and then convert the equation to a circuit using AND, OR, and NOT gates.

$$B = M * L'$$



8. Problem 2.35 (10 points)

2.35 Convert each of the following Boolean equations to a truth table:

a. $F(a, b, c) = a' + bc'$

b. $F(a, b, c) = (ab)' + ac' + bc$

c. $F(a, b, c) = ab + ac + ab'c' + c'$

d. $F(a, b, c, d) = a'bc + d'$

Inputs			Outputs
a	b	c	F
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	0

(a)

Inputs			Outputs
a	b	c	F
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

(b)

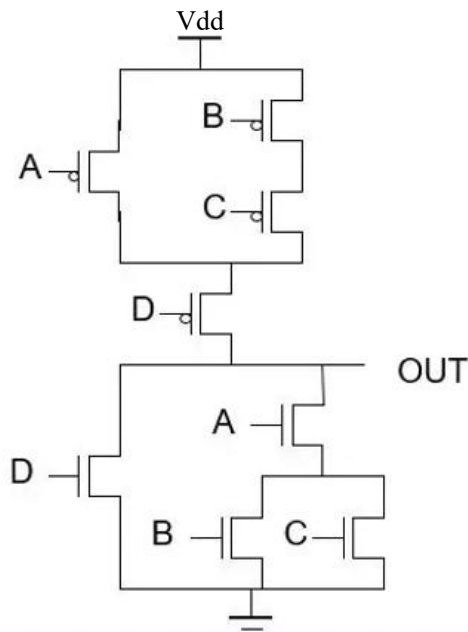
Inputs			Outputs
a	b	c	F
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

(c)

Inputs				Outputs
a	b	c	d	F
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	1
1	0	0	0	1
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	1
1	1	1	1	0

(d)

9. Build a truth table for the following circuit. (10 points)



$$out = D' \cdot (A' + B' \cdot C')$$

(optional)

A	B	C	D	out
0	0	0	0	1
0	0	0	1	0
0	0	1	0	1
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

10. Given a logic equation $F = a'bc' + b'c + abc$, draw an output waveform for F based on the given input waveforms. (10 points)

