Homework 9 Written

August 2nd, 2021 at 11:59pm

Propositional Logic 1 1

A logician tells to his son: "If you don't finish your dinner, you will not play video games afterwards." After the son finishes his meal, he is sent to bed right away.

Which mistake did he make by thinking that he would be able to play video games after dinner? Set the event "finish dimmer" as F, "play video games after dinner? 2 Propositional Logic 2 gentere can be transformed into $F \Rightarrow \neg P$, It's equivalent to its antrapositive $P \Rightarrow F$. However, the Write the following sentences in CNF form. Son mixtneds $P \Rightarrow F$ to $F \Rightarrow P$, which is the way is $(\neg p \Rightarrow q) \lor \neg (q \land r)$ $(\neg q \lor \neg r)$ b. $(\neg p \Rightarrow q) \lor \neg (q \land r)$ $(\neg q \lor \neg r)$ b. $(\neg p \Rightarrow q) \vee \neg (q \land r) \qquad r \vee v$ c. $(p \Rightarrow \neg q) \Leftrightarrow ((q \land \neg r) \Rightarrow (\neg p))$ $= ((p \Rightarrow \neg q) \Leftrightarrow ((q \land \neg r) \Rightarrow (\neg p))) \wedge (((q \land \neg r) \Rightarrow (\neg p)) \Rightarrow (p \Rightarrow \neg p))$ B. Propositional Logic $3 = ((\neg p \lor \neg q) \Rightarrow (\neg q \lor r \lor \neg p)) \wedge ((\neg q \lor r \lor \neg p) \Rightarrow (\neg p \lor \neg q))$ $= ((p \land p) \lor (\neg q \lor r \lor \neg p)) \wedge ((q \land \neg r \land p) \lor (\neg p \lor \neg q))$ $= ((p \land p) \lor (\neg q \lor r \lor \neg p)) \wedge ((q \land \neg r \land p) \lor (\neg p \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land \neg r \land p) \lor (\neg p \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land \neg r \land p) \lor (\neg p \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land \neg r \land p) \lor (\neg p \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land \neg r \land p) \lor (\neg q \lor r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land \neg r \land p) \lor (\neg q \lor r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land \neg r \land p) \lor (\neg q \lor r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land r \land r \land p) \lor (\neg q \lor r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land r \land r \land p) \lor (\neg q \lor r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land r \land r \land p) \lor (\neg q \lor r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land r \land r \land p) \lor (\neg q \lor r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land r \lor r \land p) \lor (\neg q \lor r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land r \lor r \lor \neg q)) \wedge ((q \land r \lor r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor r \lor \neg q)) \wedge ((q \land r \lor \neg q))$ $= ((p \land q) \lor (\neg q \lor \neg q)) \wedge ((q \land r \lor \neg q)) \wedge ((q \lor \neg$ Consider a vocabulary with only four propositions, A, B, C, and D. How many models are there for the following sentences? $= \left(\frac{PV7}{P}VrV^{7} \right) \wedge \left(\frac{PV7}{P}V^{7} \right) \wedge \left(\frac{PV7$ a. $B \lor C$. $2 \times 2 \times 3 = 12$ b. $\neg A \lor \neg B \lor \neg C \lor \neg D$. $2 \lor \neg C \lor \neg D$. c. $(A \Rightarrow B) \land A \land \neg B \land C \land D$. - (TAVB) NA MBN CND = False => imodels =0 Propositional Logic 4 We have defined four binary logical connectives.

- a. Are there any others that might be useful? Yes, such as "XOR" \$\overline{\Pi} \text{LMoh} is ABB=

 b. How many binary connectives can there be? There can be it, as there

 c. Why are some of them not very useful?

 Are four propositions AB, 70, 7B, 2516

Because some of them don't make sense. Such as And it's always the, and And it always the, which are not meaning the

5 Propositional Logic 5

The inference rule *Modus Tollens* is written as follows:

$$\frac{\neg q, p \Rightarrow q}{\neg p}$$

Prove that Modus Tollens is equivalent to Modus Ponens, i.e., the latter can be proved from the former, and the other around.

c. Charles doesn't like anything Alice likes.

d. David likes anything everybody else dislikes.

e. I like writing sentences in first-order logic.

f. A parent of my sibling is my parent.

g. A child of my parent, who is not me, is my sibling.

Verson (X): X to a first order (X): X is sentence written

3. First Order (X): X is sentence written
in first order logice

4. Like Write (X) X I is sentence written

Try to use a minimum number of predicates, functions, and constants.

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7 First-Order Logic 2 (Charles, X) | d. $\forall x.y.$ Person(X) $\land (\neg (x = David)) \land (\neg (x = Lavid)) \land (\neg$

 $\forall x,y,l \ SpeaksLanguage(x,l) \land SpeaksLanguage(y,l) \Rightarrow Understands(x,y).$

Everyone who can speak the same language can understand each other.

8 First-Order Logic 3

Consider a first-order logical knowledge base that describes worlds containing people, songs, albums (e.g., "Meet the Beatles") and disks (i.e., particular physical instances of CDs), The vocabulary contains the following symbols:

- Owns(p, d): Predicate. Person p owns disk d.
- Sings(p, s, a): Album a includes a recording of song s sung by person p.
- Wrote(p, s): Person p wrote song s.
- McCartney, Gersharin, BHoliday, Joe, EleanorRigby, TheManILove, Revolver: Constants with the obvious meanings.

Express the following statements in first-order logic:

- a. Gershwin wrote "The Man I Love."
- b. Gershwin did not write "Eleanor Rigby."
- c. Either Gershwin or McCartney wrote "The Man I Love."
- d. Joe has written at least one song.
- e. Joe owns a copy of Revolver.
- f. Every song that McCartney sings on Revolver was written by McCartney.
- g. Gershwin did not write any of the songs on Revolver.
- h. Every song that Gershwin wrote has been recorded on some album. (Possibly different songs are recorded on different albums.)
- i. There is a single album that contains every song that Joe has written.
- j. Joe owns a copy of an album that has Billie Holiday singing "The Man I Love."
- k. Joe owns a copy of every album that has a song sung by McCartney. (Of course, each different album is instantiated in a different physical CD.)
- l. Joe owns a copy of every album on which all the songs are sung by Billie Holiday.

a. Wrote (Grershvin, The Man I Love)
b. - Whote (Gershwin, Eleanor Rigby)
c. Wrote (Gershwin, The Man I Love) V Whote (Me Cartney, The Man I Love)
d. Is, Wrote (Joe, s).
e. Id, (opy of (d, Revolver) A Duns (Joe, d).
f. Ys, Sings (Mc Cartney, S, Revolver) => Wrote (Mc Eartney, s)
g. Ys, Ip Sings (P, S, Revolver) => Twote (Grershwin, s).
h. Ys Wrote (Gershwin, s) => Ia, P, Sings (P, s, a)
i. Ia Vs. Wrote (Joe, s) => Ip, Sings (P, s, a)
j. Ia Sings (Bidoliday, The Man I Love, a) A (Id, Copy of (d, a) A Duns (Joe, d))
k. Ya, Is, Sings (Mc Cartney, s.a) A Id, Copy of (d, a) A Duns (Joe, d)
l. Ya Vs. Sings (Bidoliday, S, a) => Id, Copy of (d, a) A Duns (Joe, d)