

How Does Knowledge Graph Embedding Extrapolate to Unseen Data: a Semantic Evidence View

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Abstract

Knowledge Graph Embedding (KGE) aims to learn representations for entities and relations. Most KGE models have gained great success, especially on **extrapolation** scenarios. Specifically, given an **unseen** triple (h, r, t) , a trained model can still correctly predict t from $(h, r, ?)$, or h from $(?, r, t)$, such extrapolation ability is impressive. However, most existing KGE works focus on the design of delicate triple modeling function, which mainly tells us how to measure the plausibility of observed triples, but offers limited explanation of why the methods can extrapolate to unseen data, and what are the important factors to help KGE extrapolate. Therefore in this work, we attempt to study the KGE extrapolation of two problems: 1. How does KGE extrapolate to unseen data? 2. How to design the KGE model with better extrapolation ability? For the problem 1, we first discuss the impact factors for extrapolation and from relation, entity and triple level respectively, propose three **Semantic Evidences** (SEs), which can be observed from train set and provide important semantic information for extrapolation. Then we verify the effectiveness of SEs through extensive experiments on several typical KGE methods. For the problem 2, to make better use of the three levels of SE, we propose a novel GNN-based KGE model, called **Semantic Evidence aware Graph Neural Network (SE-GNN)**. In SE-GNN, each level of SE is modeled explicitly by the corresponding neighbor pattern, and merged sufficiently by the multi-layer aggregation, which contributes to obtaining more extrapolative knowledge representation. Finally, through extensive experiments on FB15k-237 and WN18RR datasets, we show that SE-GNN achieves state-of-the-art performance on Knowledge Graph Completion task and performs a better extrapolation ability¹.

1 Introduction

Knowledge Graphs (KGs) like Freebase (Bollacker et al. 2008) and WordNet (Miller 1995) are significant resources to support numerous artificial intelligence applications, such as recommendation system (Wang et al. 2018), question answering (Yasunaga et al. 2021) and text generation (Zhang

et al. 2020), etc. KGs store graph-structured knowledge in triple form (h, r, t) . To integrate symbolic knowledge into numerical down-stream applications, Knowledge Graph Embedding (KGE) technique that attempts to encode the relations and entities into low-dimensional embeddings, has attracted increasing attention. The core idea of KGE is to design triple modeling function $f(h, r, t)$, that can predict correct tail entity t from $(h, r, ?)$, or head entity h from $(?, r, t)$, by scoring high for positive triple (h, r, t) , and low for negative triples (h', r, t) and (h, r, t') ².

Many KGE models have been proposed and can be categorized into three families (Wang et al. 2017; Arora 2020), which are Translational Distance Models like TransE (Bordes et al. 2013), RotatE (Sun et al. 2019); Semantic Matching Models like DistMult (Yang et al. 2015), ComplEx (Trouillon et al. 2016), ConvE (Dettmers et al. 2018); and GNN-based Models like R-GCN (Schlichtkrull et al. 2018), CompGCN (Vashishth et al. 2020b). Most of these KGE models have gained great success, especially on **extrapolation** scenarios, which is that given an **unseen** triple (h, r, t) , a well trained model can still correctly predict t from $(h, r, ?)$ or h from $(?, r, t)$, such ability is impressive. However, most existing KGE works focus on the design of delicate triple modeling function, but explains little about why the methods can extrapolate to unseen data, and what are the important factors to help KGE extrapolate. Therefore in this work, we attempt to, from a data relevant view, study KGE extrapolation of two problems: 1. How does KGE extrapolate to unseen data? 2. How to design the KGE model with better extrapolation ability?

For the problem 1, for an unseen triple (h, r, t) , we treat the prediction from $(h, r, ?)$ to t with a semantic matching idea. For a good extrapolative matching, $(h, r, ?)$ and t must have obtained some semantic relatedness during training, and we consider the relatedness may come from three levels: the individual r part with t (relation level), the individ-

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¹Our code is available at <https://github.com/renli1024/SE-GNN>

²This prediction process is also called Knowledge Graph Completion task, which shares many common concepts with Knowledge Graph Embedding.

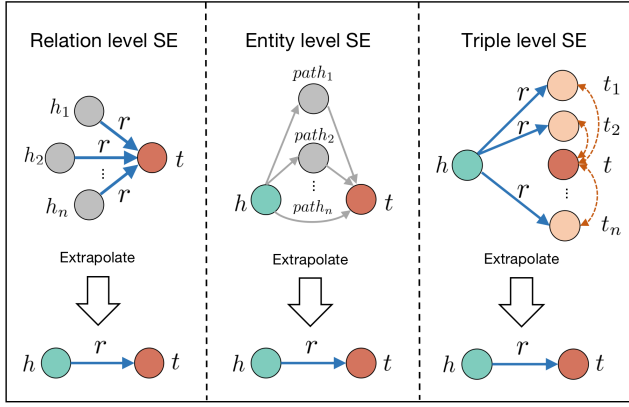


Figure 1: The demonstration of three levels of Semantic Evidence.

ual h part with t (entity level), and the combination $(h, r, ?)$ part with t (triple level). We name such three factors as **Semantic Evidence (SE)**, to indicate the supporting semantic information they provide for extrapolation. Then, we quantify the SEs with three corresponding metrics respectively. For relation level, it is measured by the co-occurrence of r and t in train set; for entity level, it is the path connections from h to t in train set; for triple level, it is the similarity between existed ground truth entities of $(h, r, ?)$ and t . The demonstration of three levels of SE can be seen in figure 1. Furthermore, we verify the effectiveness of SEs through extensive experiments on several typical KGE methods, and demonstrate that SEs serve as an important role for understanding the extrapolation ability of KGE.

For the problem 2, based on the conclusion of problem 1, Semantic Evidences are important for designing KGE models with powerful extrapolation ability. However, current works capture the SE information mainly through an implicit and insufficient way, which limits their extrapolation performance. Hence in this work, to make better use of the three levels of SE, we propose a novel GNN-based KGE model, called **Semantic Evidence aware Graph Neural Network (SE-GNN)**. In SE-GNN, each level of SE is modeled explicitly by corresponding neighbor pattern, and merged sufficiently by the multi-layer aggregation mechanism of GNNs, which contributes to obtaining more extrapolative knowledge representation. The model architecture is demonstrated in figure 3.

In summary, our main contributions are as follows:

- We are the first to explore KGE extrapolation problem, from a data relevant and model independent view, and further introduce three levels of Semantic Evidence to understand the extrapolation ability of KGE. We also conduct extensive experiments on various typical KGE models to verify our assumption.
- We dive into the way of designing the KGE model with better extrapolation ability, through explicitly and sufficiently modeling the Semantic Evidences into knowledge embedding. We propose a novel GNN-based KGE method called SE-GNN, which helps the learned knowl-

edge representation achieve more improved extrapolation performance.

- Through extensive experiments on FB15k-237 and WN18RR datasets of extrapolative Knowledge Graph Completion task, we demonstrate the validity of our introduced Semantic Evidence concept and SE-GNN method.

2 Related Work

Knowledge Graph Embedding Knowledge Graph Embedding is an active research area. Based on the scoring function and whether global graph structure is utilized, literature works can be divided into three families (Wang et al. 2017; Arora 2020). (i) **Translational Distance Models** apply distance-based scoring functions and model relations as some operation, like addition operation in TransE (Bordes et al. 2013), hyper-plane addition in TransH (Wang et al. 2014), complex field rotation in RotatE (Sun et al. 2019), etc. (ii) **Semantic Matching Models** utilize similarity-based scoring function. DistMult (Yang et al. 2015) proposes a multiplication model to represent the likelihood of a fact. ComplEx (Trouillon et al. 2016) models the triple matching function in complex domain. ConvE (Dettmers et al. 2018), InteractE (Vashishth et al. 2020a) apply neural network for similarity modeling. (iii) **GNN-based Models** tend to capture the structure characteristics of KGs through Graph Neural Networks. R-GCN (Schlichtkrull et al. 2018) introduces a relation-specific transformation to merge the relation information when neighbor aggregating. CompGCN (Vashishth et al. 2020b) proposes various composition operations for neighbor aggregation to model the structure pattern of multi-relational graph.

Extrapolation Ability Study In Machine Learning Theory field, there are many works that attempt to study the generalization and extrapolation ability of Neural Networks or Multilayer perceptrons (MLPs) (Haley and Soloway 1992; Barnard and Wessels 1992; Bietti and Mairal 2019; Ba et al. 2020; Xu et al. 2021). Like in (Xu et al. 2021), it is proved that ReLU MLPs can not extrapolate most nonlinear functions, but can extrapolate linear function when the training distribution is sufficiently diverse. And for Graph Neural Networks, it is showed that they can encode non-linearity in architecture and features to help extrapolation. However, the conclusions of above works cannot directly apply to KGE field. Because the analysis of Neural Networks mostly concentrates on classification or regression task, with only one single object or distribution. For Graph Neural Networks, the study is also mainly about node classification or graph classification task. While for KGE task, there are three targets (h, r, t) mutually influencing and serving as a matching task between $(h, r, ?)$ and t , which makes the extrapolation analysis of KGE differs from the correspondence in ML field. In addition, in Knowledge Graphs there are abundant data pattern and fact interdependency that can be mined, which is very important to understand the extrapolation performance of KGE. Therefore, in this work we focus on a data relevant and model independent view to study the KGE extrapolation problem.

3 Knowledge Graph Embedding Extrapolation

In this section, we firstly give the definition of KGE extrapolation problem. Then we introduce three levels of Semantic Evidence to explain the extrapolation ability of KGE models. Finally we conduct experiments on various typical KGE models to verify our assumption.

3.1 Problem Definition

A knowledge graph is denoted as $\mathcal{G} = (\mathcal{E}, \mathcal{R}, \mathcal{F})$, where \mathcal{E} and \mathcal{R} represent the set of entities and relations, and $\mathcal{F} = \{(h, r, t)\} \subseteq \mathcal{E} \times \mathcal{R} \times \mathcal{E}$ is the set of triple facts. For the KGE learning process, firstly \mathcal{F} will be partitioned into train, valid and test set, denoted as \mathcal{F}_{tr} , \mathcal{F}_{va} , \mathcal{F}_{te} respectively. The model will be trained on \mathcal{F}_{tr} and the best parameters will be selected according to \mathcal{F}_{va} , then the extrapolation performance will be evaluated on unseen dataset \mathcal{F}_{te} .

KGE task aims to predict t given $(h, r, ?)$, or h given $(?, r, t)$. Here we treat the prediction task with the idea of semantic matching between query and answer, and without loss of generality, we denote both directions as $\text{query}(h, r) \rightarrow t$. Under such denotation, the extrapolation problem we want to study is that why the KGE model is only trained for high scoring of $\text{query}(h, r) \rightarrow t$, $(h, r, t) \in \mathcal{F}_{tr}$, but can still perform well for unseen data $\text{query}(h, r) \rightarrow t$, $(h, r, t) \in \mathcal{F}_{te}$ ³.

3.2 Extrapolate with Semantic Evidences

For a good extrapolative matching $\text{query}(h, r) \rightarrow t$, $\text{query}(h, r)$ and t must have obtained some semantic relatedness during training. We consider the relatedness may come from three levels: the individual r part with t (relation level), the individual h part with t (entity level) and the combination $\text{query}(h, r)$ part with t (triple level), demonstrated as follows:

- **Relation level** relatedness between r and t : In train set if t frequently occur with queries containing r , i.e. there are many $\text{query}(h_i, r) \rightarrow t$ in \mathcal{F}_{tr} , the r will contain information to predict t . From intuition this can be regarded as entity type information. Instantly, for $\text{query}(h_i, \text{born_in})$, the probability of predicting location *Florida* should be higher than predicting movie *Iron_Man*, no matter what the specific h_i is.
- **Entity level** relatedness between h and t : In train set if there are observed queries or indirect queries from h to t , this will close their semantic relevancy and provide evidences for other queries between h and t . For example, $\text{query}(h, \text{is_mother}) \rightarrow e_1$ and $\text{query}(e_1, \text{is_father}) \rightarrow t$ will bring confidence for predicting $\text{query}(h, \text{is_grandmother}) \rightarrow t$. Under the graph view, this can be regarded as the *path* from h to t .

³The unseen data does not mean the new entity or relation, but the new triple combination. In fact all the entities and relations in \mathcal{F}_{te} should occur in \mathcal{F}_{tr} , in order to learn their embeddings.

- **Triple level** relatedness between $\text{query}(h, r)$ and t : For $\text{query}(h, r)$, it may exist other ground truth entities t' in train set. If the model has been trained for $\text{query}(h, r) \rightarrow t'$, meanwhile t and t' share much similarity, it will be natural for the model to extrapolate to $\text{query}(h, r) \rightarrow t$. For example, if we have known $\text{query}(\text{James_Cameron}, \text{profession}) \rightarrow \text{film_director}$ and screen_writer , it is not difficult to predict $\text{query}(\text{James_Cameron}, \text{profession}) \rightarrow \text{film_producer}$.

All above relatednesses are from train set and can be observed, so for a KGE model, though it does not train for the unseen data $\text{query}(h, r) \rightarrow t$, it has gained enough information from observed triples to make the prediction. We name such relatedness as **Semantic Evidence (SE)**, to indicate the supporting semantic information they provide for extrapolation. We demonstrate the three levels of SE in figure 1. In addition, we also do the extensive case study for the three levels of SE, to provide an intuitive demonstration about how the Semantic Evidence helps extrapolate. The case study content is placed in appendix A because of the space limitation.

3.3 Experiment Verification

In this section, we attempt to verify the effectiveness of the proposed SE concept through experiments. Firstly, for an unseen prediction $\text{query}(h, r) \rightarrow t$, we propose three corresponding metrics to quantify the evidence strength of each SE as follows:

- S_{rel} for relation level SE: It is the number of triples in train set that satisfy (h_i, r, t) , which can be formulated as:

$$S_{rel} = |\{(h_i, r, t) | (h_i, r, t) \in \mathcal{F}_{tr}\}|$$

where $|\text{set}|$ denotes the element number of a set.

- S_{ent} for entity level SE: It is the number of path from h to t in train set, indicating the semantic relevancy of h and t . For simplification, we limit the path length ≤ 2 . S_{ent} is formulated as:

$$S_{ent} = |\{(h, r_i, t) | (h, r_i, t) \in \mathcal{F}_{tr}\}| + |\{(h, r_i, e_k, r_j, t) | (h, r_i, e_k), (e_k, r_j, t) \in \mathcal{F}_{tr}\}|$$

- S_{tri} for triple level SE: It is the similarity measurement between t and $\text{query}(h, r)$'s ground truth entity t' in train set:

$$S_{tri} = \sum_{t'} \text{Sim}(t, t'), (h, r, t') \in \mathcal{F}_{tr}$$

For similarity function $\text{Sim}(t, t')$, though there have been proposed many entity similarity computing methods for KGs (Choudhury et al. 2015; Zhu and Iglesias 2017; Sun et al. 2018), most of them need external information like entity category, description text, etc. Here we hope for a method that only relates to KG itself, so we take the idea of Distributional Semantic Hypothesis: *words that are used and occur in the same contexts tend to purport similar meanings* (Harris 1954), and measure the entity similarity according to its neighbor structure (context).

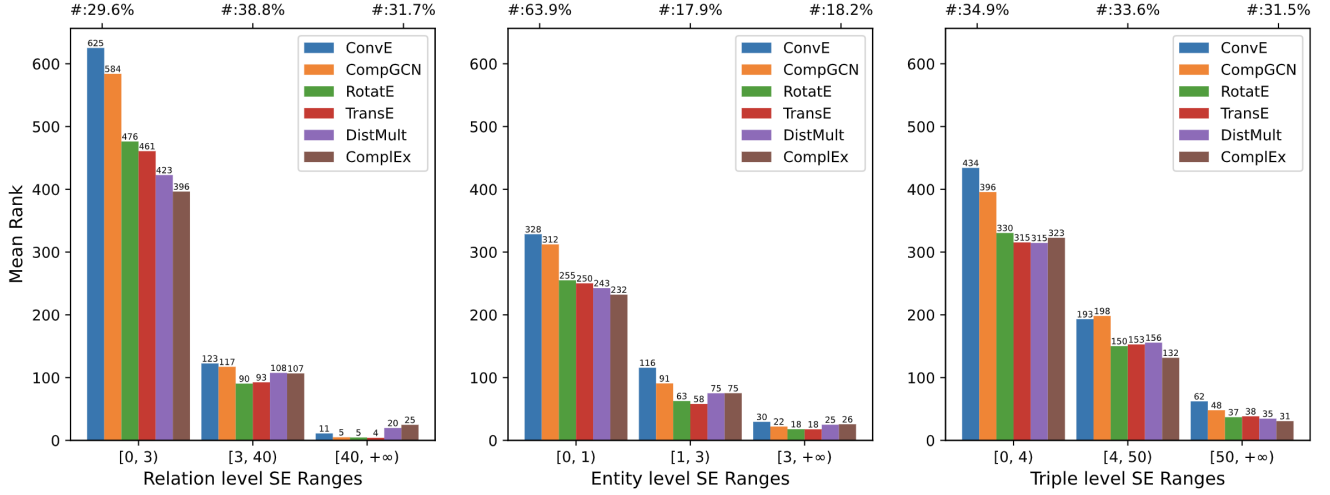


Figure 2: KGE extrapolation performance on different SE ranges. The test data of FB15k-237 is divided into three ranges based on evidence metric. Bottom x-axis denotes the metric value, top x-axis denotes the data portion of each range and y-axis denotes the Mean Rank of model prediction result (low value indicates good performance, and 1 is the best).

This can be formulated as the number of common neighbor entity-relation pairs that t and t' share:

$$\text{Sim}(t, t') = |\{(h_i, r_i) | (h_i, r_i, t) \in \mathcal{F}_{tr}\} \cap \{(h_i, r_i) | (h_i, r_i, t') \in \mathcal{F}_{tr}\}|$$

Then we reproduce several typical KGE models and analyze their extrapolation performance under different SE configurations. Specifically, we use FB15k-237 dataset (Toutanova and Chen 2015), a frequently used public KG dataset, and compute the above three SE metrics for each data query $(h, r) \rightarrow t$ in test set. For each SE, we divide the data evenly into three ranges with ascending order of metric value. Hence the three ranges represent the low, medium and high evidence strength respectively. One exception is for entity level SE, that because the range $[0, 1)$ cannot be divided further, the proportion of three ranges is about 6:2:2. Then we select six typical KGE models of different types, which are TransE, RotatE (Translational Distance Models), DistMult, ComplEx, ConvE (Semantic Matching Models), CompGCN (GNN-based Models), and evaluate their prediction results on each SE range. The results are demonstrated in figure 2.

We can see that for **all models** it exists a consistent better prediction result with evidence strength increasing. When there is abundant SE, all the KGE models can perform a good extrapolation result, like the rightmost range of each SE in figure 2. And if the SE is lacked, the models' extrapolation ability will also be limited, like the leftmost range. In addition, we also conduct the similar experiment verification on WN18RR dataset (Dettmers et al. 2018), and the results are placed in figure 6 of appendix B. It can be seen that these is the same phenomenon on WN18RR dataset. This further verifies the strong correlation between SE and extrapolation performance. That is to say, regardless of the specific method selected, the models always extrapolate well to data with high SE evidence, which verifies that the proposed SE

is a reasonable data view explanation to understand the impressive extrapolation ability of KGE.

4 Semantic Evidence aware GNN

In this section, to make better use of the Semantic Evidence information for more extrapolative knowledge representation, we propose a novel GNN-based KGE model called **Semantic Evidence aware Graph Neural Network (SE-GNN)**, which is designed to model the three levels of SE explicitly and sufficiently.

4.1 Modeling SEs with Neighbor Pattern

Knowing from previous section, Semantic Evidences are important to design KGE models with powerful extrapolation ability. However, for most current KGE works, there is no awareness of such extrapolation factors and they capture the SE information mainly through an implicit and insufficient way, which limits their extrapolation performance. Hence in this work, we explicitly treat each SE as different neighbor pattern and model them sufficiently through multi-layer aggregation mechanism of GNNs, for obtaining more extrapolative knowledge representations.

Specifically, for relation level SE, it describes the overall relation-entity interactions, which can be captured through neighbor relation pattern of an entity. By aggregating all the connected relations, we can get the representation as:

$$\mathbf{s}_i^{rel} = \sigma \left(\sum_{(e_j, r_j) \in \mathcal{N}_i} \alpha_{ij}^{rel} W^{rel} \mathbf{r}_j \right) \quad (1)$$

$\mathbf{s}_i^{rel} \in \mathbb{R}^n$ denotes the relation level SE representation of entity e_i , where n is hidden dimension. $\mathbf{r}_j \in \mathbb{R}^n$ is the embedding of relation r_j . $\mathcal{N}_i = \{(e_j, r_j) | (e_j, r_j, e_i) \in \mathcal{F}_{tr}\}$ denotes e_i 's neighbor entities, associated with connecting relation in train set. $W^{rel} \in \mathbb{R}^{n \times n}$ is linear transformation

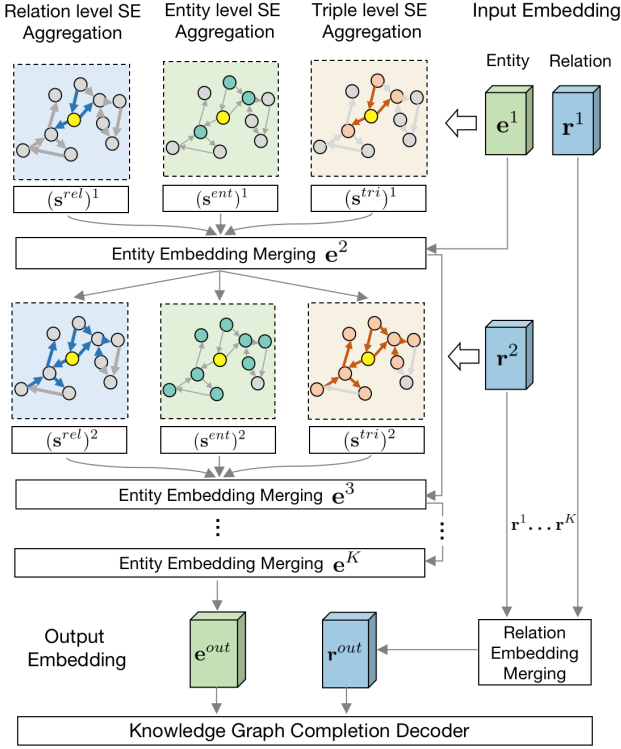


Figure 3: The model architecture of SE-GNN. The blue, green and orange graph represents relation, entity and triple level SE aggregation process respectively. The yellow node is the example center node of neighbor aggregation. By layer-wise iteration, SE-GNN can access a wide range of graph structure and model the deep interaction of SEs. Finally, the output entity and relation embedding are fed into a Knowledge Graph Completion decoder to perform the extrapolation.

matrix and σ is non-linear activation function. α_{ij}^{rel} is aggregation attention, which is computed as:

$$\alpha_{ij}^{rel} = \frac{\exp(\mathbf{r}_j^T \mathbf{e}_i)}{\sum_{(e_k, r_k) \in \mathcal{N}_i} \exp(\mathbf{r}_k^T \mathbf{e}_i)} \quad (2)$$

$\mathbf{e}_i \in \mathbb{R}^n$ is the embedding of entity e_i . We use dot product to dynamically compute the attention importance of neighbor relation r_j to center entity e_i .

For entity level SE, it describes the path connection information between entities, and can be captured from neighbor entity pattern. With aggregating neighbor entities once, we can capture all the 1 length paths, and we can access to longer paths by iterative multi-layer aggregation. Here we only introduce a single layer formulation and we will introduce the whole model architecture in section 4.2:

$$\mathbf{s}_i^{ent} = \sigma \left(\sum_{(e_j, r_j) \in \mathcal{N}_i} \alpha_{ij}^{ent} W^{ent} \mathbf{e}_j \right) \quad (3)$$

$\mathbf{s}_i^{ent} \in \mathbb{R}^n$ is the entity level SE representation of e_i . α_{ij}^{ent} is

aggregated attention and computed as follows:

$$\alpha_{ij}^{ent} = \frac{\exp(\mathbf{e}_j^T \mathbf{e}_i)}{\sum_{(e_k, r_k) \in \mathcal{N}_i} \exp(\mathbf{e}_k^T \mathbf{e}_i)} \quad (4)$$

For triple level SE, it describes the triple similarity characteristics from the neighbor structure view, where both neighbor entities and relations should be considered. We design the aggregation function as:

$$\mathbf{s}_i^{tri} = \sigma \left(\sum_{(e_j, r_j) \in \mathcal{N}_i} \alpha_{ij}^{tri} W^{tri} \varphi(\mathbf{e}_j, \mathbf{r}_j) \right) \quad (5)$$

where $\varphi(\mathbf{e}, \mathbf{r})$ is the composition function to fuse the entity and relation information. The selection includes addition function: $\varphi(\mathbf{e}, \mathbf{r}) = \mathbf{e} + \mathbf{r}$; multiplication function: $\varphi(\mathbf{e}, \mathbf{r}) = \mathbf{e} * \mathbf{r}$; Multilayer Perceptron: $\varphi(\mathbf{e}, \mathbf{r}) = \text{MLP}([\mathbf{e} || \mathbf{r}])$, where $||$ is vector concatenation operation. The attention weights α_{ij}^{tri} is computed similarly as:

$$\alpha_{ij}^{tri} = \frac{\exp(\varphi(\mathbf{e}_j, \mathbf{r}_j)^T \mathbf{e}_i)}{\sum_{(e_k, r_k) \in \mathcal{N}_i} \exp(\varphi(\mathbf{e}_k, \mathbf{r}_k)^T \mathbf{e}_i)} \quad (6)$$

4.2 Model Architecture

In section 4.1, we introduce the neighbor aggregation method to model each SE and obtain the corresponding representation of \mathbf{s}_i^{rel} , \mathbf{s}_i^{ent} and \mathbf{s}_i^{tri} . The three embeddings provide important evidences to help the model extrapolate. We merge them with original knowledge embedding as:

$$\mathbf{e}'_i = \mathbf{e}_i + \mathbf{s}_i^{rel} + \mathbf{s}_i^{ent} + \mathbf{s}_i^{tri} \quad (7)$$

This can be seen as one single aggregation layer of GNN, which only captures the SE information in 1-hop neighborhood. To acquire the multi-hop neighbor information and model the deeper interaction of SE components, we introduce a multi-layer version for SE aggregation, which is demonstrated in figure 3. We take the output \mathbf{e}'_i as the next layer's input, and aggregate iteratively as:

$$\mathbf{e}_i^{l+1} = \mathbf{e}_i^l + (\mathbf{s}_i^{rel})^l + (\mathbf{s}_i^{ent})^l + (\mathbf{s}_i^{tri})^l \quad (8)$$

\mathbf{e}_i^{l+1} denotes the embedding of e_i in $(l+1)$ -th layer. $(\mathbf{s}_i^{tri})^l$ is the triple level SE embedding in l -th layer, which is computed from \mathbf{e}_i^l and \mathbf{r}_i^l :

$$(\mathbf{s}_i^{tri})^l = \sigma \left(\sum_{(e_j, r_j) \in \mathcal{N}_i} (\alpha_{ij}^{tri})^l (W^{tri})^l \varphi(\mathbf{e}_j^l, \mathbf{r}_j^l) \right) \quad (9)$$

where $(\alpha_{ij}^{tri})^l$ is computed in the same way as equation 6. The layer-wise embedding of $(\mathbf{s}_i^{rel})^l$ and $(\mathbf{s}_i^{ent})^l$ can be obtained in the similar way. In first layer, \mathbf{e}^1 is the initialized embedding, and after K layers' aggregation, we take \mathbf{e}^K as the output entity embedding.

With regard to relation embedding, we initialize different \mathbf{r}^l for each layer, in the consideration that relations may play a different role in different layer. For output relation embedding, we concat all the \mathbf{r}^l used and merge them together by

a transform matrix W^{out} . Hence the output of SE-GNN is formulated as:

$$\begin{aligned} \mathbf{e}^{out} &= \mathbf{e}^K \\ \mathbf{r}^{out} &= W^{out} \text{Concat}(\{\mathbf{r}^l | l = 1, \dots, K\}) \end{aligned} \quad (10)$$

Then we utilize the output embedding to perform the prediction from $(h, r, ?)$ to t or from $(?, r, t)$ to h . To align with the terminology in previous work, here we also denote this process as Knowledge Graph Completion (KGC) task. We choose ConvE (Dettmers et al. 2018) as our decoder, which uses 2D convolutional neural network to match query (h, r) and answer t . We refer readers to original paper for more details, and here we directly denote the model function as:

$$\mathbf{q} = \text{ConvE}(\mathbf{h}, \mathbf{r}) \quad (11)$$

$\mathbf{q} \in \mathbb{R}^n$ is the computed query embedding. \mathbf{h} and \mathbf{r} are taken from \mathbf{e}^{out} and \mathbf{r}^{out} . Note that in fact any KGC decoder can be considered here, while this is not the focus of this paper. We leave the more explorations to the future work.

Then we use binary cross entropy loss to measure the matching between \mathbf{q} and potential answer entities \mathbf{t} :

$$\begin{aligned} \mathcal{L} = -\frac{1}{N} \sum_t & 1(t) \cdot \log(m(\mathbf{q}, \mathbf{t})) + \\ & (1 - 1(t)) \cdot \log(1 - m(\mathbf{q}, \mathbf{t})) \end{aligned} \quad (12)$$

where N is the total number of candidate entities, and $m(\mathbf{q}, \mathbf{t}) \in [0, 1]$ is the matching function of query \mathbf{q} and entity \mathbf{t} . We use dot product in this work:

$$m(\mathbf{q}, \mathbf{t}) = \text{Sigmoid}(\mathbf{q}^T \mathbf{t}) \quad (13)$$

$1(t) \in \{0, 1\}$ is the denotation function that outputs 1 for positive entity and 0 for negative entity.

5 Experiments

5.1 Experiment Setup

We conduct experiments of Knowledge Graph Completion task on two commonly used public datasets: FB15k-237 (Toutanova and Chen 2015) and WN18RR (Dettmers et al. 2018). The detailed introduction of two dataset are provided in appendix C.

We measure the model performance by five frequently used metrics: MRR (the Mean Reciprocal Rank of correct entities), MR (the Mean Rank of correct entities), Hits@1, Hits@3, Hits@10 (the accuracy of correct entities ranking in top 1/3/10). We follow the filtered setting protocol (Bordes et al. 2013) for evaluation, i.e. all the other true entities appearing in train, valid and test set are excluded when ranking. In addition, based on the observation of (Sun et al. 2020), to eliminate the influence of abnormal score distribution, if prediction targets have the same score with multiple other entities, we take the average of upper bound and lower bound rank as the result. Additional experimental details are provided in the appendix D.

5.2 Results of Knowledge Graph Completion task

Our baselines are selected from three categories which are **Translational Distance Models**: TransE (Bordes et al. 2013), RotatE (Sun et al. 2019), PaiRE (Chao et al. 2021); **Semantic Matching Models**: DistMult (Yang et al. 2015), ComplEx (Trouillon et al. 2016), TuckER (Balazevic and Allen 2019), ConvE (Dettmers et al. 2018), InteractE (Vashishth et al. 2020a), PROCRUSTES (Peng et al. 2021); **GNN-based Models**: R-GCN (Schlichtkrull et al. 2018), KBGAT (Nathani et al. 2019), SACN (Shang et al. 2019), A2N (Bansal et al. 2019), CompGCN (Vashishth et al. 2020b). The results are demonstrated in table 1, from which we can know that:

- In view of the five metrics on two datasets, SE-GNN achieves 9 of 10 SOTAs, which is an overall best performance compared to baselines. And for the exception of MR report on WN18RR, SE-GNN still gets the competitive result with regard to the most baselines.
- SE-GNN obtains obvious improvement compared to CompGCN, which is a typical GNN-based KGE model. This shows that the aggregation function in SE-GNN for modeling three levels of SE information is a more sufficient way and performs a better extrapolation ability.
- In addition, we can see that the improvement of SE-GNN is more evident on FB15k-237 dataset. We think this is because in FB15k-237 there are more than 200 types of relation (table 3 in appendix C) and the data interactions are very complex, which makes the extrapolation scenario more challenging. In this case, the explicit modeling of SEs will play a more important role to help extrapolation.

In the overall consideration across metrics on two datasets, SE-GNN obtains the best extrapolation performance on unseen test data, which indicates the effectiveness of our proposed method.

5.3 Effective Modeling of Semantic Evidences

In this section, we tend to verify that SE-GNN is capable of effectively modeling the Semantic Evidences. Like in section 3.3, we evaluate the extrapolation performance of SE-GNN in different SE ranges. To control the variables, we compare the results with ConvE, which is our selected decoder in SE-GNN. So the only difference here is that in SE-GNN, explicit modeling of three levels of Semantic Evidence is introduced before decoder (equation 10), while in ConvE, entity and relation embedding are directly fed into the decoder, with implicit modeling of SE information. The results are demonstrated in figure 4. We can see that SE-GNN performs better for all levels of SE across all ranges, which shows SE-GNN can capture the SE information more effectively and possess better extrapolation ability.

5.4 Ablation Study of each Semantic Evidence

To evaluate the effect of each SE part, we do the ablation study of only removing one SE modeling part and simultaneously removing two of them. The results are demonstrated in table 2. We can observe that the performance degrades for

Models	FB15k-237					WN18RR				
	MRR	MR	H@1	H@3	H@10	MRR	MR	H@1	H@3	H@10
Translational Distance										
TransE (Bordes et al. 2013) [†]	.330	173	.231	.369	.528	.223	3380	.014	.401	.529
RotatE (Sun et al. 2019)	.338	177	.241	.375	.533	.476	3340	.428	.492	.571
PaiRE (Chao et al. 2021)	.351	160	.256	.387	.544	-	-	-	-	-
Semantic Matching										
DistMult (Yang et al. 2015) [†]	.308	173	.219	.336	.485	.439	4723	.394	.452	.533
ComplEx (Trouillon et al. 2016) [†]	.323	165	.229	.353	.513	.468	5542	.427	.485	.554
TuckER (Balazevic and Allen 2019)	.358	-	.266	.394	.544	.470	-	.443	.482	.526
ConvE (Dettmers et al. 2018)	.325	244	.237	.356	.501	.430	4187	.400	.440	.520
InteractE (Vashishth et al. 2020a)	.354	172	.263	-	.535	.463	5202	.430	-	.528
PROCRUSTES (Peng et al. 2021)	.345	-	.249	.379	.541	.474	-	.421	.502	.569
GNN-based										
R-GCN (Schlichtkrull et al. 2018)	.248	-	.151	-	.417	-	-	-	-	-
KBGAT (Nathani et al. 2019) [‡]	.157	270	-	-	.331	.412	1921	-	-	.554
SACN (Shang et al. 2019)	.350	-	.260	.390	.540	.470	-	.430	.480	.540
A2N (Bansal et al. 2019)	.317	-	.232	.348	.486	.450	-	.420	.460	.510
CompGCN (Vashishth et al. 2020b)	.355	197	.264	.390	.535	.479	3533	.443	.494	.546
SE-GNN (ours)	.365	157	.271	.399	.549	.484	3211	.446	.509	.572

Table 1: Model reports on FB15k-237 and WN18RR test set. The best results are in **bold**. [†] denotes that we reproduce the results using the code⁴. [‡] means that the results of KBGAT are from (Sun et al. 2020) because original results suffer from same score evaluation problem, which is discussed in section 5.1. Other results are from the published paper.

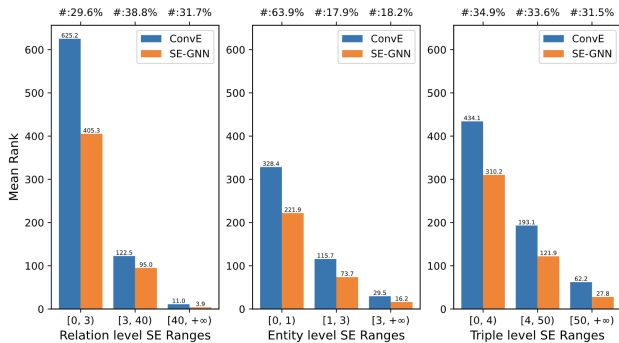


Figure 4: The performance comparison of SE-GNN and ConvE under the same Semantic Evidence configuration.

all six variants of SE-GNN, which shows the effectiveness of each SE modeling part.

In addition, we consider that for most GNN-based KGE works like R-GCN (Schlichtkrull et al. 2018), CompGCN (Vashishth et al. 2020b), the core idea is to merge the relation and entity together when neighbor aggregating. This can be regarded as the *w/o relation & entity SE* variant of SE-GNN, which only models the triple SE part. While both our SE extrapolation analysis and the ablation experiments show that it is insufficient, and separately modeling relation and entity information are also beneficial for KGE task.

⁴<https://github.com/DeepGraphLearning/KnowledgeGraphEmbedding>, commit ID: 2e440e0

Models	FB15k-237			
	MRR	MR	H@1	H@10
SE-GNN	.365	157	.271	.549
w/o relation SE	.361	168	.264	.542
w/o triple SE	.359	173	.262	.537
w/o entity SE	.360	172	.265	.539
w/o relation & entity SE	.357	179	.257	.532
w/o relation & triple SE	.355	181	.254	.535
w/o entity & triple SE	.352	185	.249	.525

Table 2: Ablation study of three SEs, where w/o means removing the corresponding modeling part in SE-GNN.

6 Conclusion

In this paper, we make the attempt to study the KGE extrapolation problem from a data relevant and model independent view. We show that there are three levels of Semantic Evidence that play an important role when predicting unseen data, which are the co-occurrence between relations and entities, the path connection between entities, and the similarity between observed entities and predicted entities. Then we verify the effectiveness of SEs through extensive quantitative experiments and qualitative case study. Based on such observation, we design a novel SE-GNN model to obtain more extrapolative knowledge representation and achieve consistent improvement on different datasets. Some future directions include exploiting more extrapolative evidences and designing more elaborated SE modeling method.

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References

- Arora, S. 2020. A Survey on Graph Neural Networks for Knowledge Graph Completion. *CoRR*, abs/2007.12374.
- Ba, J.; Erdogdu, M. A.; Suzuki, T.; Wu, D.; and Zhang, T. 2020. Generalization of Two-layer Neural Networks: An Asymptotic Viewpoint. In *8th International Conference on Learning Representations, ICLR 2020, Addis Ababa, Ethiopia, April 26-30, 2020*. OpenReview.net.
- Balazevic, I.; and Allen, C. 2019. TuckerER: Tensor Factorization for Knowledge Graph Completion. In *Proceedings of the 2019 Conference on Empirical Methods in Natural Language Processing and the 9th International Joint Conference on Natural Language Processing, EMNLP-IJCNLP 2019, Hong Kong, China, November 3-7, 2019*, 5184–5193. Association for Computational Linguistics.
- Bansal, T.; Juan, D.; Ravi, S.; and McCallum, A. 2019. A2N: Attending to Neighbors for Knowledge Graph Inference. In *Proceedings of the 57th Conference of the Association for Computational Linguistics, ACL 2019, Florence, Italy, July 28-August 2, 2019, Volume 1: Long Papers*, 4387–4392. Association for Computational Linguistics.
- Barnard, E.; and Wessels, L. 1992. Extrapolation and interpolation in neural network classifiers. *IEEE Control Systems Magazine*, 12(5): 50–53.
- Bietti, A.; and Mairal, J. 2019. On the Inductive Bias of Neural Tangent Kernels. In *Advances in Neural Information Processing Systems 32: Annual Conference on Neural Information Processing Systems 2019, NeurIPS 2019, December 8-14, 2019, Vancouver, BC, Canada*, 12873–12884.
- Bollacker, K. D.; Evans, C.; Paritosh, P.; Sturge, T.; and Taylor, J. 2008. Freebase: a collaboratively created graph database for structuring human knowledge. In *Proceedings of the ACM SIGMOD International Conference on Management of Data, SIGMOD 2008, Vancouver, BC, Canada, June 10-12, 2008*, 1247–1250. ACM.
- Bordes, A.; Usunier, N.; García-Durán, A.; Weston, J.; and Yakhnenko, O. 2013. Translating Embeddings for Modeling Multi-relational Data. In *Advances in Neural Information Processing Systems 26: 27th Annual Conference on Neural Information Processing Systems 2013. Proceedings of a meeting held December 5-8, 2013, Lake Tahoe, Nevada, United States*, 2787–2795.
- Chao, L.; He, J.; Wang, T.; and Chu, W. 2021. PairRE: Knowledge Graph Embeddings via Paired Relation Vectors. In *Proceedings of the 59th Annual Meeting of the Association for Computational Linguistics and the 11th International Joint Conference on Natural Language Processing, ACL/IJCNLP 2021, (Volume 1: Long Papers), Virtual Event, August 1-6, 2021*, 4360–4369. Association for Computational Linguistics.
- Choudhury, A.; Sharma, S.; Mitra, P.; Sebastian, C.; Naidu, S. S.; and Chelliah, M. 2015. SimCat: an entity similarity measure for heterogeneous knowledge graph with categories. In *Proceedings of the Second ACM IKDD Conference on Data Sciences, Bangalore, CoDS 2015, India, March 18-21, 2015*, 112–113. ACM.
- Dettmers, T.; Minervini, P.; Stenetorp, P.; and Riedel, S. 2018. Convolutional 2D Knowledge Graph Embeddings. In *Proceedings of the Thirty-Second AAAI Conference on Artificial Intelligence, (AAAI-18), the 30th innovative Applications of Artificial Intelligence (IAAI-18), and the 8th AAAI Symposium on Educational Advances in Artificial Intelligence (EAAI-18), New Orleans, Louisiana, USA, February 2-7, 2018*, 1811–1818. AAAI Press.
- Haley, P. J.; and Soloway, D. 1992. Extrapolation limitations of multilayer feedforward neural networks. In *[Proceedings 1992] IJCNN International Joint Conference on Neural Networks*, volume 4, 25–30. IEEE.
- Harris, Z. S. 1954. Distributional structure. *Word*, 10(2-3): 146–162.
- Miller, G. A. 1995. WordNet: A Lexical Database for English. *Commun. ACM*, 38(11): 39–41.
- Nathani, D.; Chauhan, J.; Sharma, C.; and Kaul, M. 2019. Learning Attention-based Embeddings for Relation Prediction in Knowledge Graphs. In *Proceedings of the 57th Conference of the Association for Computational Linguistics, ACL 2019, Florence, Italy, July 28-August 2, 2019, Volume 1: Long Papers*, 4710–4723. Association for Computational Linguistics.
- Peng, X.; Chen, G.; Lin, C.; and Stevenson, M. 2021. Highly Efficient Knowledge Graph Embedding Learning with Orthogonal Procrustes Analysis. In *Proceedings of the 2021 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, NAACL-HLT 2021, Online, June 6-11, 2021*, 2364–2375. Association for Computational Linguistics.
- Schlichtkrull, M. S.; Kipf, T. N.; Bloem, P.; van den Berg, R.; Titov, I.; and Welling, M. 2018. Modeling Relational Data with Graph Convolutional Networks. In *The Semantic Web - 15th International Conference, ESWC 2018, Heraklion, Crete, Greece, June 3-7, 2018, Proceedings*, volume 10843 of *Lecture Notes in Computer Science*, 593–607. Springer.
- Shang, C.; Tang, Y.; Huang, J.; Bi, J.; He, X.; and Zhou, B. 2019. End-to-End Structure-Aware Convolutional Networks for Knowledge Base Completion. In *The Thirty-Third AAAI Conference on Artificial Intelligence, AAAI 2019, The Thirty-First Innovative Applications of Artificial Intelligence Conference, IAAI 2019, The Ninth AAAI Symposium on Educational Advances in Artificial Intelligence, EAAI 2019, Honolulu, Hawaii, USA, January 27 - February 1, 2019*, 3060–3067. AAAI Press.
- Sun, H.; Ren, R.; Cai, H.; Xu, B.; Liu, Y.; and Li, T. 2018. Topic Model Based Knowledge Graph for Entity Similarity

- Measuring. In *15th IEEE International Conference on e-Business Engineering, ICEBE 2018, Xi'an, China, October 12-14, 2018*, 94–101. IEEE Computer Society.
- Sun, Z.; Deng, Z.; Nie, J.; and Tang, J. 2019. RotatE: Knowledge Graph Embedding by Relational Rotation in Complex Space. In *7th International Conference on Learning Representations, ICLR 2019, New Orleans, LA, USA, May 6-9, 2019*. OpenReview.net.
- Sun, Z.; Vashishth, S.; Sanyal, S.; Talukdar, P. P.; and Yang, Y. 2020. A Re-evaluation of Knowledge Graph Completion Methods. In *Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics, ACL 2020, Online, July 5-10, 2020*, 5516–5522. Association for Computational Linguistics.
- Toutanova, K.; and Chen, D. 2015. Observed versus latent features for knowledge base and text inference. In *Proceedings of the 3rd workshop on continuous vector space models and their compositionality*, 57–66.
- Trouillon, T.; Welbl, J.; Riedel, S.; Gaussier, É.; and Bouchard, G. 2016. Complex Embeddings for Simple Link Prediction. In *Proceedings of the 33rd International Conference on Machine Learning, ICML 2016, New York City, NY, USA, June 19-24, 2016*, volume 48 of *JMLR Workshop and Conference Proceedings*, 2071–2080. JMLR.org.
- Vashishth, S.; Sanyal, S.; Nitin, V.; Agrawal, N.; and Talukdar, P. P. 2020a. InteractE: Improving Convolution-Based Knowledge Graph Embeddings by Increasing Feature Interactions. In *The Thirty-Fourth AAAI Conference on Artificial Intelligence, AAAI 2020, The Thirty-Second Innovative Applications of Artificial Intelligence Conference, IAAI 2020, The Tenth AAAI Symposium on Educational Advances in Artificial Intelligence, EAAI 2020, New York, NY, USA, February 7-12, 2020*, 3009–3016. AAAI Press.
- Vashishth, S.; Sanyal, S.; Nitin, V.; and Talukdar, P. P. 2020b. Composition-based Multi-Relational Graph Convolutional Networks. In *8th International Conference on Learning Representations, ICLR 2020, Addis Ababa, Ethiopia, April 26-30, 2020*. OpenReview.net.
- Wang, H.; Zhang, F.; Wang, J.; Zhao, M.; Li, W.; Xie, X.; and Guo, M. 2018. RippleNet: Propagating User Preferences on the Knowledge Graph for Recommender Systems. In *Proceedings of the 27th ACM International Conference on Information and Knowledge Management, CIKM 2018, Torino, Italy, October 22-26, 2018*, 417–426. ACM.
- Wang, Q.; Mao, Z.; Wang, B.; and Guo, L. 2017. Knowledge Graph Embedding: A Survey of Approaches and Applications. *IEEE Trans. Knowl. Data Eng.*, 29(12): 2724–2743.
- Wang, Z.; Zhang, J.; Feng, J.; and Chen, Z. 2014. Knowledge Graph Embedding by Translating on Hyperplanes. In *Proceedings of the Twenty-Eighth AAAI Conference on Artificial Intelligence, July 27 -31, 2014, Québec City, Québec, Canada*, 1112–1119. AAAI Press.
- Xu, K.; Zhang, M.; Li, J.; Du, S. S.; Kawarabayashi, K.; and Jegelka, S. 2021. How Neural Networks Extrapolate: From Feedforward to Graph Neural Networks. In *9th International Conference on Learning Representations, ICLR 2021, Virtual Event, Austria, May 3-7, 2021*. OpenReview.net.
- Yang, B.; Yih, W.; He, X.; Gao, J.; and Deng, L. 2015. Embedding Entities and Relations for Learning and Inference in Knowledge Bases. In *3rd International Conference on Learning Representations, ICLR 2015, San Diego, CA, USA, May 7-9, 2015, Conference Track Proceedings*.
- Yasunaga, M.; Ren, H.; Bosselut, A.; Liang, P.; and Leskovec, J. 2021. QA-GNN: Reasoning with Language Models and Knowledge Graphs for Question Answering. In *Proceedings of the 2021 Conference of the North American Chapter of the Association for Computational Linguistics: Human Language Technologies, NAACL-HLT 2021, Online, June 6-11, 2021*, 535–546. Association for Computational Linguistics.
- Zhang, H.; Liu, Z.; Xiong, C.; and Liu, Z. 2020. Grounded Conversation Generation as Guided Traverses in Commonsense Knowledge Graphs. In *Proceedings of the 58th Annual Meeting of the Association for Computational Linguistics, ACL 2020, Online, July 5-10, 2020*, 2031–2043. Association for Computational Linguistics.
- Zhu, G.; and Iglesias, C. A. 2017. Computing Semantic Similarity of Concepts in Knowledge Graphs. *IEEE Trans. Knowl. Data Eng.*, 29(1): 72–85.

	Extrapolating Cases	Observed Evidences in Train Set	SE-GNN Rank	TransE/RotatE/DistMult ComplEx/ConvE Rank
Relation level SE	(San Diego, <code>travel_month</code> , ?) → <code>December</code>	(Miami, <code>travel_month</code> , <code>December</code>) (Zurich, <code>travel_month</code> , <code>December</code>) (Melbourne, <code>travel_month</code> , <code>December</code>) ...	1	[1, 1, 1, 1, 1]
	(The Orphanage (film), <code>language</code> , ?) → <code>Spanish</code>	(Midnight in Barcelona (film), <code>language</code> , <code>Spanish</code>) (Todo sobre mi madre (film), <code>language</code> , <code>Spanish</code>) (The Treasure of the Sierra Madre (film), <code>language</code> , <code>Spanish</code>)...	1	[2, 1, 2, 1, 2]
	(Amy Pohler, <code>gender</code> , ?) → <code>Female</code>	(Erika Christensen, <code>gender</code> , <code>Female</code>) (Nancy Snyderman, <code>gender</code> , <code>Female</code>) (Olivia Williams, <code>gender</code> , <code>Female</code>) ...	1	[1, 1, 2, 1, 1]
Entity level SE	(Robert Downey Jr, <code>live_in</code> , ?) → <code>New York City</code>	(Robert Downey Jr, <code>friendship</code> , Jenifer Aniston, <code>live_in</code> , <code>New York City</code>) (Robert Downey Jr, <code>place_of_birth</code> , Manhattan, <code>administrative_parent</code> , <code>New York City</code>) (Robert Downey Jr, <code>spouse</code> , Sarah Jessica Parker, <code>live_in</code> , <code>New York City</code>) ...	2	[2, 2, 2, 7, 7]
	(England, <code>contains</code> , ?) → <code>Watford</code>	(England, <code>contains</code> , Hertfordshire, <code>contains</code> , <code>Watford</code>) (England, <code>second_level_divisions</code> , Hertfordshire, <code>contains</code> , <code>Watford</code>) (England, <code>administrative_parent</code> , UK of GB and NI, <code>contains</code> , <code>Watford</code>) ...	5	[28, 37, 15, 9, 21]
	(Amber Riley, <code>profession</code> , ?) → <code>Theatre actress</code>	(Amber Riley, <code>meanwhile_award</code> , Diana Agron, <code>profession</code> , <code>Theatre actress</code>) (Amber Riley, <code>meanwhile_award</code> , Jessalyn Gilsig, <code>profession</code> , <code>Theatre actress</code>) (Amber Riley, <code>meanwhile_award</code> , Naya Rivera, <code>profession</code> , <code>Theatre actress</code>) ...	1	[1, 1, 1, 1, 1]
Triple level SE	(Freshman Program, <code>major</code> , ?) → <code>Computer Science</code>	(Freshman Program, <code>major</code> , <code>Mathematics</code>) & <code>Mathematics ~ Computer Science</code> (Freshman Program, <code>major</code> , <code>Electrical Eng.</code>) & <code>Electrical Eng. ~ Computer Science</code> (Freshman Program, <code>major</code> , <code>Chemical Science</code>) & <code>Chemical Science ~ Computer Science</code>	1	[7, 8, 2, 2, 1]
	(Dorothy Fields, <code>profession</code> , ?) → <code>Lyricist</code>	(Dorothy Fields, <code>profession</code> , <code>Songwriting</code>) & <code>Songwriting ~ Lyricists</code> (Dorothy Fields, <code>profession</code> , <code>Scenario Writer</code>) & <code>Scenario Writer ~ Lyricists</code> (Dorothy Fields, <code>profession</code> , <code>Dramatist</code>) & <code>Dramatist ~ Lyricists</code>	1	[1, 1, 1, 1, 1]
	(RoboCop (film), <code>genre</code> , ?) → <code>Thriller film</code>	(RoboCop (film), <code>genre</code> , <code>Action movie</code>) & <code>Action movie ~ Thriller film</code> (RoboCop (film), <code>genre</code> , <code>Murder mystery</code>) & <code>Murder mystery ~ Thriller film</code> (RoboCop (film), <code>genre</code> , <code>Superhero movie</code>) & <code>Superhero movie ~ Thriller film</code>	1	[2, 2, 3, 5, 1]

Figure 5: Case study of Semantic Evidences on FB15k-237 dataset. The symbol \sim means that two entities are semantically similar. The rank result is the prediction rank of correct entity in all entities (low value indicates good performance). The best rank results are marked as **bold**.

Appendix

A Case study of Semantic Evidence

In this section, we tend to provide an intuitive demonstration about how the Semantic Evidence helps extrapolate to unseen data and hence this information is important for KGE task. For each Semantic Evidence, we select multiple example cases from FB15k-237 test set, and list their corresponding evidences and prediction results of different KGE models. The cases are demonstrated in figure 5.

For relation SE, the idea is that the co-occurrence between relation and tail entity can help extrapolate. For example, for the extrapolative prediction (San Diego, `travel_month`, ?) → `December`, if the model has observed large amounts of co-occurrences of `travel_month` and `December` in train set, it will be aware of the month type of `December` and also know that `December` is a popular time for traveling, which is beneficial for the model to perform a new `travel_month` prediction on `December` entity. Note that there are three levels of SE information that can help extrapolate in the meantime, and in this case relation evidence just serves as one part.

For entity SE, the idea is that the connection / path between entities can help extrapolation. Like in the case (Robert Downey Jr, `live_in`, ?) → `New York City`, in the train set we know that Downey was born in `New York City`, his wife lives in `New York City`, his friend lives in `New York City`, etc. These connections between Robert Downey Jr and `New York City` will enhance their semantic relevancy and help the model to predict “some relation” between them, such as `live_in`.

For triple SE, it follows the idea that if prediction holds for one entity, it should also hold for a similar one. For example, if we have known that Freshman Program contains the major of Mathematics, Electrical Engineering, Chemistry Science, it is natural to infer that it also contains Computer Science, which is a similar major of the observed ones.

Above three levels of Semantic Evidence are important to help model do extrapolating, in order to make better utilize these information we design SE-GNN model. From the two rightmost columns, we can see that compared to the typical KGE models, SE-GNN can predict the answer entities more accurately and perform a better extrapolation performance, which verifies the effectiveness of our proposed Semantic Evidence concept and SE-GNN method.

B Correlation between SE and Extrapolation Performance on WN18RR Dataset

In this section we compute the extrapolation performance of various KGE models on different SE ranges on WN18RR dataset, which is demonstrated in figure 6. Because there are much low evidence test data in WN18RR dataset, it is hard to evenly divide the test data into three ranges. Therefore we divide the data into [0, 1) and [1, Max] two ranges instead, which can respectively represent the data **with evidence** and **without evidence** (Max denotes the max value of corresponding evidence metric). From the results, we can see that the correlation between evidence strength and extrapolation performance also holds on WN18RR dataset, for all models and across all evidences, which further verifies the effectiveness of SE. Note that because of the various data

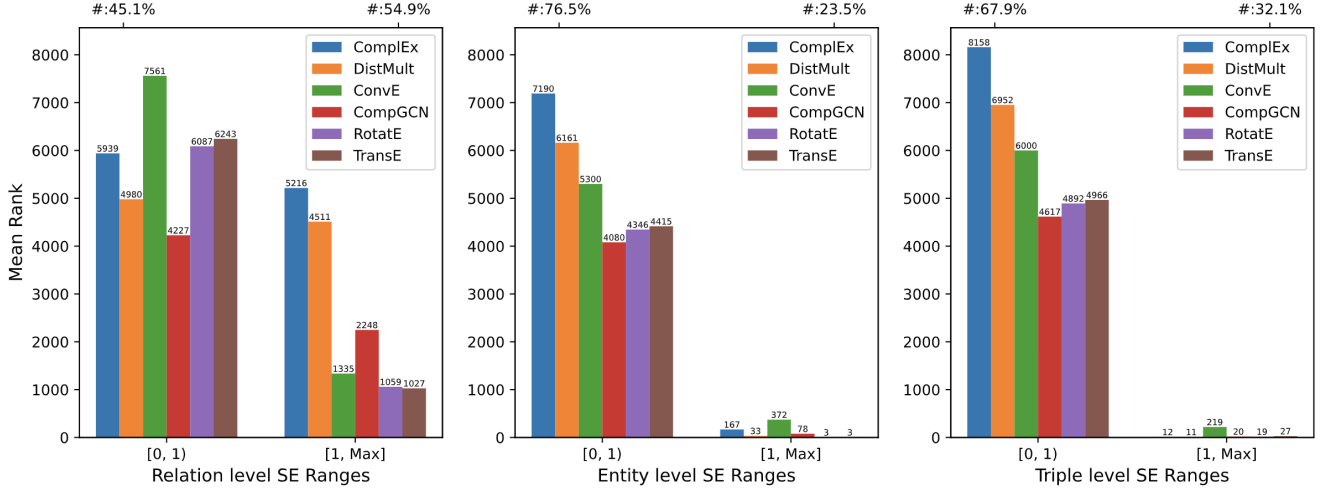


Figure 6: Extrapolation performance of KGE models on different SE ranges on WN18RR dataset. The bottom x-axis denotes the range value, the top x-axis denotes the data portion of each range and y-axis denotes the Mean Rank of model prediction result (low value indicates good performance, and 1 is the best).

characteristics, different dataset may reveal a different focus on three levels of SE when extrapolating. Like in WN18RR dataset, there are only 11 types of relation (demonstrated in table 3). Such simple pattern makes relation level SE a less important role compared to FB15k-237 dataset, which has an abundant relation set of 237 types. Hence in figure 6, there is a weaker downward trend for relation level SE, and the entity and triple level SE play a more important role when extrapolating.

C Dataset Statistics

In this section we provide the information of FB15k-237 and WN18RR dataset used in our experiment.

- FB15k-237 (Toutanova and Chen 2015) contains entities and relations from Freebase, which is a large common-sense knowledge base. FB15k-237 is a pruned version of FB15k (Bordes et al. 2013) dataset, with duplicate and inverse relations being removed to prevent direct prediction. Furthermore, FB15k-237 also ensures that every triple (h, r, t) in valid and test set does not have any direct connection (h, r', t) in train set, to make the prediction more challenging.
- WN18RR (Dettmers et al. 2018) is derived from WordNet, a lexical database of semantic relations between words. Similar to FB15k-237, WN18RR is pruned from WN18 (Bordes et al. 2013) dataset by removing the duplicate and inverse relations, while there is no direct connection restriction in WN18RR.

Each dataset is split into train, valid and test sets and the statistics of two datasets are summarized in table 3.

D Experimental Details

In this section we discuss some more details of our experiment implementation. Following CompGCN (Vashishth

Dataset	FB15k-237	WN18RR
# entity	14,541	40,943
# relation	237	11
# train triple	272,115	86,835
# valid triple	17,535	3,034
# test triple	20,466	3,134

Table 3: Dataset statistics

et al. 2020b), we transform the knowledge graph to undirected graph by introducing an inverse edge (t, r^{-1}, h) for each edge (h, r, t) , which aims to pass the information bidirectionally and enhance graph connectivity. In addition, like ConvE (Dettmers et al. 2018), we also introduce an inverse version for each relation when predicting. For the two directions $(h, r, ?)$ to t and $(?, r, t)$ to h of a triple prediction, we transform them as $(h, r, ?)$ to t and $(t, r^{-1}, ?)$ to h . This can unify the prediction format and improve computational efficiency.

Furthermore, during the aggregation process of SE-GNN, for each training batch, we randomly remove a proportion of corresponding edges in the knowledge graph. This can prevent the information leakage problem, i.e. the model has seen the prediction edges when aggregating. This can also guide the model to learn the interactions between existed edges and prediction missing edges when aggregating, which is a closer scenario of extrapolation.