

Preserving Privacy in Federated Learning with Ensemble Cross-Domain Knowledge Distillation

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Abstract

Federated Learning (FL) is a machine learning paradigm where local nodes collaboratively train a central model while the training data remains decentralized. Existing FL methods typically share model parameters or employ co-distillation to address the issue of unbalanced data distribution. However, they suffer from communication bottlenecks. More importantly, they risk privacy leakage risk. In this work, we develop a privacy preserving and communication efficient method in a FL framework with one-shot offline knowledge distillation using unlabeled, cross-domain, non-sensitive public data. We propose a quantized and noisy ensemble of local predictions from completely trained local models for stronger privacy guarantees without sacrificing accuracy. Based on extensive experiments on classification and segmentation tasks, we show that our method outperforms baseline FL algorithms with superior performance in both accuracy and data privacy preservation.

Introduction

The availability of large collections of data has facilitated the recent success of deep learning. However, in many cases, this wealth of data is dispersed over numerous physical locations and controlled by separate entities. Consequently, collaboration among parties, especially clinical institutions, is restricted due to the decentralized nature of the data. This is especially true for medical images where various legal, privacy, technical, and data ownership concerns often make it impractical or even impossible to gather such medical data to a centralized location.

To tackle some of these issues, federated learning (FL) (Shokri and Shmatikov 2015; Yang et al. 2019) has emerged as a practical machine learning paradigm where local models are used to collaboratively train a centralized model using data-free communication. There are several important challenges that make FL markedly different than typical distributed learning. First, privacy is a key concern. It is essential that local data remain protected. Second, communication is a critical bottleneck, so steps must be taken to minimize its detrimental effects. Third, due to the decentralized nature of the collection (leading to different settings), data across various local parties are typically heterogeneous,

rendering the typical machine learning assumption of independent and identical distributions (i.i.d.) invalid.

Mainstream federated learning methods are based on the repeated sharing of parameters or gradients of local models during the training process (McMahan et al. 2017; Smith et al. 2017; Li et al. 2018; Zhao et al. 2018; Hsu, Qi, and Brown 2019; Wang et al. 2020; Karimireddy et al. 2020). Recent applications of FL in medical imaging also share similar features. Sheller et al. (Sheller et al. 2018) share local model gradients for multi-institution collaboration, and Yang et al. (Yang et al. 2021) employ a similar approach for the task of semi-supervised COVID segmentation. Typically, such approaches involve each local model sharing its gradients with a central server after each round of local training on its local data. The central server then aggregates the local model parameters with typical data aggregation techniques (Wang et al. 2020; Li et al. 2020a; Hsu, Qi, and Brown 2020). Each local node then updates its local model with the latest global aggregate, and this process continues. These parameter-based communication methods have many known security weaknesses and are limited only to models with homogeneous architectures. While some methods have shown hope of protecting against data leakage in medical imaging (Li et al. 2019, 2020b), sharing parameters/gradients is highly susceptible to privacy leakage, and stealthy attacks. Some recent works (Zhu, Liu, and Han 2019; Geiping et al. 2020) demonstrated the ability to obtain local private data from publicly shared gradients, further highlighting the associated privacy risks in general and in medical applications in particular.

Another class of approaches in FL is to fuse local models into a single central model based on knowledge distillation (Hinton, Vinyals, and Dean 2015). Knowledge distillation eliminates the requirement for identical model architectures. While (Li and Wang 2019) distills the locally-computed knowledge on auxiliary public data to get around data privacy issues, they assume both the public and private data are sampled from the same underlying distribution. This further exposes the private data to security attacks. Recently proposed FedDF (Lin et al. 2020) relaxes the public data to be unlabeled and non-sensitive (i.e., sampled from another domain). Similarly, (Zhu, Hong, and Zhou 2021) eliminates the prerequisite of public data with a generator and aggregates knowledge in a data-free manner. However, both of

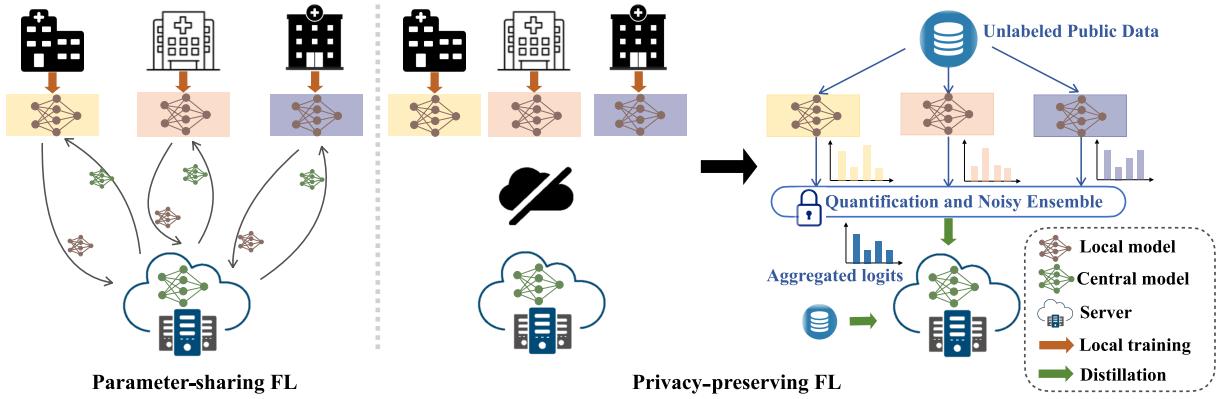


Figure 1: Traditional methods transfer private parameters or gradients from local nodes to a server, risking privacy leakage. Our framework trains local models independently, and only transfers products of the unlabeled public data. We further perturb the local predictions with a quantized and noisy ensemble for a stronger privacy guarantee.

them still exchange model parameters recursively, resulting in privacy vulnerabilities due to model memorization (Zhu, Liu, and Han 2019).

To address these issues, we present a new framework for federated learning (Fig. 1) with several innovations. First, unlike existing FL methods for either general or medical applications, our framework only shares the outputs of public data with one-shot (single round) distillation. The public data is unlabeled and decoupled from the private data. This, by design, eliminates the security vulnerabilities identified in prior works. Second, in contrast to the existing distillation-based FL work (Li and Wang 2019; Lin et al. 2020; Sui et al. 2020; Zhu, Hong, and Zhou 2021) that exclusively train local models incrementally and update them synchronously through online distillation, we keep the local training asynchronous and independent, and then aggregate the local predictions on unlabeled cross-domain public data. This offline strategy largely limits the server’s exposure to local models’ knowledge, reducing the consumption of communication bandwidth and reducing the risk of local information leakage. Furthermore, we deploy quantized and noisy aggregation on the locally-computed logits for stronger privacy guarantees (Dwork, Roth et al. 2014). We experiment with CIFAR10/100 and large-scale chest x-ray datasets, showing very competitive classification results in accuracy, bandwidth, and privacy guarantees. Extensive experiments on image segmentation tasks and text classification tasks also demonstrate our method outperforms prior works with better privacy/performance trade-offs.

Our contributions can be summarized as:

- We propose a one-shot federated learning framework with one-way knowledge distillation (FedKD) on unlabeled, cross-domain, non-sensitive public data, explicitly addressing the communication bottleneck and preserving the privacy of local proprietary data without sacrificing accuracy.
- We introduce a seminal quantized and noisy ensemble before distillation, so that the privacy cost is meaningfully decreased with stronger security guarantees.

- We demonstrated the flexibility and efficiency of the proposed framework with extensive evaluations showing superior performance on accuracy, bandwidth and privacy-preserving capability compared to prior arts, on both classification and segmentation tasks on natural and medical images.

Related Work

Knowledge Ensemble. With the success of knowledge transfer (Hinton, Vinyals, and Dean 2015), recent advancements on ensemble networks are dominated by the student-teacher learning paradigm (Shazeer et al. 2017). Ensemble learning aggregates the knowledge of multiple teachers before it distills the knowledge into the student network. Supervised ensemble learning is dominated by gate learning to design the weight for aggregation (Shazeer et al. 2017; Asif, Tang, and Harrer 2019; Xiang, Ding, and Han 2020). In semi-supervised and self-supervised scenarios, (Wu et al. 2019) and (You et al. 2017) exploit the relative similarity between samples for aggregation weights. Furthermore, co-distillation extends one-way transfer to bidirectional collaborative learning (Song and Chai 2018; Zhu, Gong et al. 2018; Dvornik, Schmid, and Mairal 2019; Guo et al. 2020).

Federated Learning. In parameter-based FL methods, each local model shares its parameters/gradients with the central server after every round of local training on its local data, following which the central server aggregates them by average (McMahan et al. 2017). The result of this aggregation step is then shared by the central server with the local nodes, which in turn update their corresponding local model and proceed with the next training round. This process is then repeated until the stopping criterion is met. A variety of extensions of FedAVG (McMahan et al. 2017; Wang et al. 2020; Li et al. 2020a; Hsu, Qi, and Brown 2020) employ improved aggregation schemes, such as adding momentum (Hsu, Qi, and Brown 2019), and local weighting (Li et al. 2020a; Hsu, Qi, and Brown 2020). Another set of approaches improve local training by incorporating proximal term (Li et al. 2018) or control variations (Karimireddy et al. 2020) to restrict lo-

cal training. However, such sharing of model parameters or gradients can be thought of as a naive way of information exchange, it is highly susceptible to privacy leakage and stealth attacks, as also demonstrated elsewhere (Zhu, Liu, and Han 2019; Geiping et al. 2020).

Federated distillation methods exchange model outputs rather than model parameters. Given that some methods produce central models by distilling knowledge from private data (Zhou et al. 2020; Shin et al. 2020) in the same spirit as those above, there is a growing concern on local data privacy. In contrast, some works (Jeong et al. 2018; Li and Wang 2019) distill with the output of public data. Although model agnostic, these methods select public data based on the prior knowledge of private data. Recently proposed methods FedDF (Lin et al. 2020) and FedGEN (Zhu, Hong, and Zhou 2021) relax the prerequisites of distillation data, but they are still far from privacy-preserving or communication efficient due to the iterative exchange of models over hundreds of rounds. The above mentioned approaches exclusively require many rounds of back-and-forth communication, leading to bandwidth bottlenecks and other inefficiencies.

Privacy Issue. As noted above, parameter-based FL works have been shown to be highly susceptible to privacy leakage (Zhu, Liu, and Han 2019; Geiping et al. 2020). Distillation-based FL works with recursive model exchanges involved (Lin et al. 2020; Zhu, Hong, and Zhou 2021) also post privacy risk. Utilizing unlabeled public data during distillation has proven to be effective in protecting private local data from attackers (Hamm, Cao, and Belkin 2016). PATE (Papernot et al. 2017) also suggests that restricting the student network’s access to the teacher’s network and training with non-overlapping public datasets can further guarantee privacy protection. Unlike PATE, which uses topmost local votes to train the central model, we utilize quantized and noisy logits for aggregation and distillation. This retains more local expertise information and therefore improves the utility of the target model without sacrificing the protection of private data.

Method

In a federated learning setting with K local nodes, each local note hosts a private, labeled dataset $\mathcal{D}^k = \{(\mathbf{x}_i^k, y_i^k) | i = 1, \dots, |\mathcal{D}^k|\}$. A shared, unlabeled public dataset $\mathcal{D}^0 = \{\mathbf{x}_i^0 | i = 1, \dots, |\mathcal{D}^0|\}$ is accessible by the central server and all local nodes. In the first stage of FedKD, the model at each local node k is initialized with model parameters θ^k by training with its own local private data \mathcal{D}^k . Note that FedKD is agnostic to the type of neural network architecture, and hence each local node can have its own specialized architecture suited for the particular distribution of its local data.

In the second stage, the local, private datasets are first disconnected from local training servers to minimize the risk of any data leakage and to protect privacy. The public dataset \mathcal{D}^0 that is hosted on the server and deployed at each local node is then used for one-way knowledge distillation from the local nodes to the server. Local models θ^k , together with the central model θ^s on the server, constitutes a student-

teacher knowledge transfer configuration. The teacher here being an ensemble of multiple local models, one at each local node. The following sections introduce our privacy-preserving ensemble and distillation schemes for various tasks.

Privacy-Preserving Ensemble

The private dataset is denoted $\mathcal{D}^k = \{(\mathbf{x}_i^k, y_i^k) | i = 1, \dots, |\mathcal{D}_k|\}$ ($k \in \mathcal{K}$), where $\mathcal{K} = \{1, \dots, K\}$, $y_i^k \in \mathcal{C}^k$, \mathcal{C}^k is the set of existing classes in the dataset \mathcal{D}^k , and $\mathcal{C}^k \subset \{1, \dots, C\}$ (C is the number of classes across all local nodes). Let $z_i^{ck} = f(\mathbf{x}_i^0, \theta_k, c)$ be the logits of a public data sample \mathbf{x}_i^0 corresponding to class $c \in \mathcal{C}^k$, produced by the model at local node k , where $c \in \{1, \dots, C\}$. We omit i in the following descriptions for simplicity. The conventional aggregation $\tilde{z}^c = \frac{1}{|\mathcal{K}|} \sum_{k \in \mathcal{K}} z^{ck}$ takes an average of all teachers’ logits. However, under the FL setting with a high degree of heterogeneity, a conventional ensemble algorithm is not appropriate primarily due to its inability to cope with the more general scenarios when local nodes are not sharing the exact same set of target classes. To take this into consideration, we introduce an importance weight ω for each local node to reflect the distribution of the local private data:

$$\omega_k^c = \frac{N_k^c}{\sum_{k \in \mathcal{K}} N_k^c}, \quad (1)$$

where for single-label classification, $N_k^c = \sum_{i=1}^{|\mathcal{D}_k|} (y_i^k = c)$ denotes the number of samples of class c used in training the model at local node k .

Inspired by PATE (Papernot et al. 2017), we perturb the locally computed logits with a quantized and noisy ensemble for a stronger privacy guarantee:

$$\tilde{z}^c = \sum_{k \in \mathcal{K}} \omega_k^c \cdot Q(z^{ck}; S) + Lap\left(\frac{1}{\gamma}\right), \quad (2)$$

where Q is the quantization function with $s = 1, \dots, S$ as quantization scale levels, and $Lap\left(\frac{1}{\gamma}\right)$ is the Laplacian distribution with location 0 and scale $\frac{1}{\gamma}$. γ is a privacy parameter to trade off between privacy-preserving capability and accuracy. A smaller γ (i.e., higher noise level) results in stronger privacy guarantee and relatively lower accuracy.

To achieve better communication efficiency, we apply uniform quantization to floating point logits so they occupy fewer bits:

$$Q(z^{ck}; S) = q_s, \text{ if } z^{ck} \in (q_{s-1}, q_s], \quad (3)$$

We determine the quantization intervals $(q_{s-1}, q_s]$ with $q_s = \frac{2(s-1)z^{\max}}{S-1} - z^{\max}$, where $z^{\max} = \max_{i,c,k} |z_i^{ck}|$ is the maximum absolute value of all the logits across public data samples $i = 1, \dots, |\mathcal{D}_0|$ and classes $c = 1, \dots, C$. Thus, Equation (3) becomes:

$$Q(z^{ck}; S) = \lceil \frac{S \cdot z^{ck}}{2z^{\max}} \rceil \cdot \frac{2z^{\max}}{S}, \quad (4)$$

where a smaller S sacrifices more logits precision, while maintaining a higher level of privacy.

During ensemble, we protect the private data at each local node by: (1) transferring only the final prediction inferred with the non-proprietary public data \mathcal{D}^0 ; and (2) perturbing the local outputs with quantization and random noise .

Algorithm 1: Federated Knowledge Distillation (FedKD)

Input: Labeled private datasets $\{\mathcal{D}^k | k \in \mathcal{K}\}$ ($\mathcal{K} = \{1, \dots, K\}$), unlabeled public data \mathcal{D}^0 , central model θ^s , local models $\{\theta^k | k \in \mathcal{K}\}$, T distillation steps, batchsize B , quantization scale S , privacy hyperparameter γ .

Local Training:
Train each local model θ^k with private data \mathcal{D}^k .

Logits Ensemble:
for each sample x_i^0 in \mathcal{D}^0 **do**
 for each local $k \in \mathcal{K}$ **do**
 $z_i^k \leftarrow f(x_i^0, \theta^k)$
 end for
 $\tilde{z}_i \leftarrow \text{aggregate } \{z_i^k; S, \gamma | k \in \mathcal{K}\}$ ▷ Eq. 2
end for

Distillation:
for each distillation step $t = 1, \dots, T$ **do**
 $x^0 \leftarrow$ a batch of public data from \mathcal{D}^0 with size B
 $\tilde{z} \leftarrow f(x^0, \theta^s)$
 Update the central model: $\theta^s \leftarrow \theta^s - \frac{1}{B} \nabla_{\theta^s} \mathcal{L}$ ▷ Eq. 7
end for

One-shot Distillation

Conventional knowledge distillation aggregates all teachers' soft labels subject to the Kullback-Leibler divergence:

$$\mathcal{L} = \sum_c p^c \log \frac{p^c}{q^c}, \quad (5)$$

where p^c and q^c denote the probabilities of a sample of class c for the teacher and student models, respectively. The aggregated logits \tilde{z}^c can be viewed as teacher knowledge, and the output logits of the central model $\tilde{z}^c = f(x_0, \theta_s, c)$ can be viewed as student knowledge. Without loss of generality, we denote the activation by $p^c = \sigma(\tilde{z}^c)$ and $q^c = \sigma(\tilde{z}^c)$. For single-label classification, we obtain the probabilities using softmax activation:

$$p^c = \sigma(\tilde{z}^c) = \frac{e^{\tilde{z}^c/\tau}}{\sum_c e^{\tilde{z}^c/\tau}}, \quad q^c = \sigma(\tilde{z}^c) = \frac{e^{\tilde{z}^c/\tau}}{\sum_c e^{\tilde{z}^c/\tau}}, \quad (6)$$

where τ is a temperature parameter. Hinton et al. (Hinton, Vinyals, and Dean 2015) showed that minimizing Eq. 5 with high τ is equivalent to minimizing the ℓ_2 error between the teacher and student logits, thereby relating cross-entropy minimization to matching logits.

Based on the observations above by Hinton et al. (Hinton, Vinyals, and Dean 2015), we consider the case of $\tau \rightarrow \infty$ so the loss can be written as:

$$\mathcal{L} = \|\tilde{z} - \hat{z}\|, \quad (7)$$

where $\tilde{z} = [\tilde{z}^1, \dots, \tilde{z}^C]$, and $\hat{z} = [\hat{z}^1, \dots, \hat{z}^C]$.

Note that we use one-shot offline distillation where the local nodes predict with each public data sample only once,

and the predicted logits are used to train the central model iteratively. This distillation strategy (1) provides a higher privacy guarantee by executing fewer queries to the local model (limiting the access to local knowledge); and (2) eliminates the iterative and repetitive communication requirement of synchronous updates, improving communication efficiency and flexibility. The overall process is described in Algorithm 1.

Cross-domain Analysis

We argue that with cross-domain public data our framework can distill knowledge from multiple locals with generalizability. In this section we present a performance bound for the aggregated central model, which is built upon prior arts from domain adaptation (Ben-David et al. 2010).

Let the input space be \mathcal{X} , \mathcal{D}^S and \mathcal{D}^T be source and target domain respectively. We denote the ground-truth labeling function as g and the hypothesis function as f , we get the error as $\epsilon_{\mathcal{D}^S}(h, g) = \mathbb{E}_{x \sim \mathcal{D}^S} [|h(x) - g(x)|]$. We denote the risk of h on \mathcal{D}^S and \mathcal{D}^T as $\epsilon_{\mathcal{D}^S}$ and $\epsilon_{\mathcal{D}^T}$. (Ben-David et al. 2010) introduces \mathcal{H} -divergence to evaluate the distance between two domain distributions $\mathcal{U}, \mathcal{U}'$ on the a hypothesis space \mathcal{H} . \mathcal{H} -divergence is defined as $d_{\mathcal{H}}(\mathcal{U}, \mathcal{U}') = 2 \sup_{A \in \mathcal{A}_{\mathcal{H}}} |\Pr_{\mathcal{D}}(A) - \Pr_{\mathcal{D}'}(A)|$, where $\mathcal{A}_{\mathcal{H}}$ denotes a collection of subsets of \mathcal{X} which support the hypothesis in \mathcal{H} . The symmetric different space is defined as $\mathcal{H}\Delta\mathcal{H} = \{h(x) \oplus h'(x) | h, h' \in \mathcal{H}\}$ (\oplus represents the XOR operation). For the generalizability between two domains, we have the following theorem (Blitzer et al. 2008):

Theorem 1. Generalization bounds. *Let \mathcal{H} be a hypothesis space of VC dimension d , \mathcal{U}^S and \mathcal{U}^T be unlabeled samples of size N each, drawn from \mathcal{D}^S and \mathcal{D}^T respectively. For any $h \in \mathcal{H}$ and $\delta \in (0, 1)$, the following holds with probability at least $1 - \delta$ (over the choice of the samples):*

$$\begin{aligned} \epsilon_{\mathcal{D}^T}(h) \leq & \epsilon_{\mathcal{D}^S}(h) + \frac{1}{2} d_{\mathcal{H}\Delta\mathcal{H}}(\mathcal{U}^S, \mathcal{U}^T) \\ & + 4 \sqrt{\frac{2d \log(2N) + \log(\frac{2}{\delta})}{N}} + \lambda, \end{aligned} \quad (8)$$

where $\lambda = \epsilon_{\mathcal{D}^S}(h^*) + \epsilon_{\mathcal{D}^T}(h^*)$ and h^* is the ideal joint hypothesis minimizing the combined error: $h^* = \operatorname{argmin}_{h \in \mathcal{H}} \epsilon_{\mathcal{D}^S}(h^*) + \epsilon_{\mathcal{D}^T}(h^*)$.

In our case, \mathcal{D}^S is the domain of private data distributed across K local nodes: $\mathcal{D}^S = \{\mathcal{D}^k | k \in \mathcal{K}\}$, and $\mathcal{D}^T = \mathcal{D}^0$ is the domain of public data. We assume $|\mathcal{D}^0| = N$, $\sum_{k \in \mathcal{K}} |\mathcal{D}^k| = N$. Given the local model $h_{\mathcal{D}^k}$ trained on data \mathcal{D}^k , we learn central model $h_{\mathcal{D}^0}$ from public data \mathcal{D}^0 through weighted aggregation: $h_{\mathcal{D}^0} = \sum_{k \in \mathcal{K}} \omega_k (h_{\mathcal{D}^k} + n_k(\gamma))$, where $\sum_{k \in \mathcal{K}} \omega_k = 1$, and $n_k(\gamma)$ is the introduced noise parameterized by γ to strengthen the privacy. We have the following weighted noisy generalization bound (please

see the supplementary for details):

$$\begin{aligned} \epsilon_{\mathcal{D}^0}(h_{\mathcal{D}^0}) &\leq \epsilon_{\mathcal{D}^S} \left(\sum_{k \in \mathcal{K}} \omega_k (h_{\mathcal{D}^k} + n_k(\gamma)) \right) + \lambda \omega \\ &+ \sum_{k \in \mathcal{K}} \omega_k \left(\frac{1}{2} d_{\mathcal{H} \Delta \mathcal{H}}(\mathcal{U}^k, \mathcal{U}^0) \right) + 4 \sqrt{\frac{2d \log(2N) + \log(\frac{2}{\delta})}{N}}. \end{aligned} \quad (9)$$

Extension to other tasks

On top of the general single-label classification problem described above, we adapt our method to the multi-label classification and segmentation tasks.

Multi-label Classification: While Eq. 6 corresponds to the single-label classification scenario, our method is also extensible to multi-label classification. In this case, the private data notation from above is changed to $\mathcal{D}^k = \{(\mathbf{x}_i^k, \mathbf{y}_i^k) | i = 1, \dots, |\mathcal{D}^k|\}$ with $\mathbf{y}_i^k \in \{-1, 0, 1\}^c$ where -1, 0, and 1 indicate unknown, negative, and positive for class $c \in 1, \dots, C$, respectively. We have made two other modifications: first, a sigmoid is used as the activation instead of softmax so $p^c = \sigma(\hat{z}^c)$ and $q^c = \sigma(\tilde{z}^c)$; second, in Eq. 1, we define $N_k^c = \sum_{i=1}^{|\mathcal{D}^k|} (\mathbf{y}_i^k(c) = 1)$ as the number of samples labeled as class c for training the model of local node k .

Segmentation: When we extend to the 2D/3D segmentation problem, the private dataset is reformulated as $\mathcal{D}_k = \{(\mathbf{x}_i^k, \mathbf{y}_i^k) | i = 1, \dots, |\mathcal{D}^k|\}, \mathbf{y}_i^k \in \{0, \dots, C\}^{H \times W \times D}$, where 0 denotes the background class, and $H \times W \times D$ is the size of the segmentation mask ($D = 1$ in 2D case). We define $z^{ck} = f(\mathbf{x}^0, \theta^k, c) \in \mathbb{R}^{H \times W \times D}$ as the pixel/voxel-wise prediction of the public data sample \mathbf{x}^0 corresponding to class c produced by the model at local node k , and the output of the central model as $\mathbf{q}^c = \sigma(f(\mathbf{x}^0, \theta^s, c)) \in [0, 1]^{H \times W \times D}$. As in Eq. 2, we aggregate the local inference with an importance weight, where we adapt the count to be pixel/voxel-wisely: $N_k^c = \sum_{i=1}^{|\mathcal{D}^k|} \sum_{h,w,d} (\mathbf{y}_i^{khwd} = c)$. For the segmentation task trained with a typical cross-entropy loss when ground-truth is available, the distillation deploys Eq. 7 pixel/voxel-wisely. For the segmentation task trained with dice loss (Milletari, Navab, and Ahmadi 2016), we apply the soft dice loss to allow the central probability \mathbf{q}^c to match the aggregated pseudo masks $\mathbf{p}^c = \sigma(\hat{z}^c)$:

$$\mathcal{L} = -\frac{1}{C} \sum_{c=1}^C \frac{2 \cdot \sum \mathbf{p}^c \cdot \mathbf{q}^c}{\sum (\mathbf{p}^c)^2 + \sum (\mathbf{q}^c)^2 + \epsilon}, \quad (10)$$

where the summation is pixel/voxel-wise, and ϵ is a small constant to avoid numerical instability.

Experiments

We conduct experiments on image classification and segmentation, and extensive experiments on text classification. For classification tasks, we construct local training sets using heterogeneous data splits with a Dirichlet distribution as in prior works (Hsu, Qi, and Brown 2019). The value of α controls the degree of non-IID-ness. An α of positive infinity indicates identical local data distributions, and a smaller α indicates higher non-IID-ness.

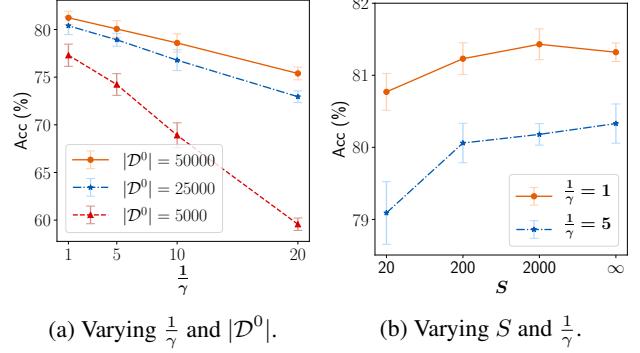


Figure 2: Ablation study on the CIFAR-10 dataset ($K=20$, $\alpha=1$) with varying public data size $|\mathcal{D}^0|$, noise $\frac{1}{\gamma}$, and quantization scale S .

CIFAR10/100 Classification

For classification task we use CIFAR-10/100 (Krizhevsky, Hinton et al. 2009) as datasets for natural images. To keep consistency with the prior arts, we use the same experimental settings as in FedDF (Lin et al. 2020): CIFAR-100 as public data when CIFAR-10 as private data, and downsampled version of ImageNet (32×32) (Deng et al. 2009) as public data corresponding to CIFAR-100 as private data. For each experiment, we sample over three different random seeds as private data split for local training. We report the average accuracy metrics on CIFAR-10 and CIFAR-100 test set corresponding to its private data respectively.

We train each local model individually with SGD and Cosine Annealing, decreasing the learning rate from 0.0025 to 0.001 in 500 epochs with a batch size of 16. For distillation, we use the Adam optimizer, a constant learning rate of 1e-3, and a batch size of 512. We use 200 and 10 epochs for CIFAR-10 and CIFAR-100 respectively. The weight decay is 3e-4 and 0 for local training and distillation, respectively.

The comparison in Table 1 shows that our method achieves a significantly stronger privacy guarantee as well as a far better communication efficiency compared to prior arts, without sacrificing accuracy. Next, we perform ablation studies to validate the efficacy of our ensemble and distillation strategy and show the results in Table 2. The extensive experiments in Table 2 show the distillation accuracy can be improved by a large margin with more access to local information (e.g., local models predicted on dynamically augmented public data multiple times). For an accuracy-privacy trade-off, we restrict that local model to only predict each public sample once in our method. In Figure 2 we study the impact of quantization/noise on the accuracy for different sized public datasets. The left figure suggests that increased noise degrades the ensemble distillation performance, but a (unlabeled) larger public dataset can substantially improves the robustness to noise perturbation. We observe from the right figure that the distillation results are insensitive to data precision, which is also observed in prior work (Shazeer et al. 2017). Thus we use $S=200$ and $\gamma=1$ as default setting

Method	Privacy Guarantee		CIFAR-10			CIFAR-100		
	NO Shared Param.	Noise Perturbation	Accuracy(%) \uparrow $\alpha = 1$	Accuracy(%) \uparrow $\alpha = 0.1$	Bandwidth (GB) \downarrow	Accuracy(%) \uparrow $\alpha = 1$	Accuracy(%) \uparrow $\alpha = 0.1$	Bandwidth (GB) \downarrow
FedAvg (McMahan et al. 2017)	\times	\times	78.57 \pm 0.22	68.37 \pm 0.50	58	42.54 \pm 0.51	36.72 \pm 1.50	63
FedProx (Li et al. 2018)	\times	\times	76.32 \pm 1.95	68.65 \pm 0.77	58	42.94 \pm 1.23	35.74 \pm 1.00	63
FedAvgM (Hsu, Qi, and Brown 2019)	\times	\times	77.79 \pm 1.22	68.63 \pm 0.79	58	42.83 \pm 0.36	36.29 \pm 1.98	63
FedDF (Lin et al. 2020)	\times	\times	80.69 \pm 0.43	71.36 \pm 1.07	58	47.43\pm0.45	39.33 \pm 0.03	63
FedGEN (Zhu, Hong, and Zhou 2021)	\times	\times	80.31 \pm 0.97	68.13 \pm 1.37	58	45.97 \pm 0.23	35.97 \pm 0.31	63
FedMD (Li and Wang 2019)	\checkmark	\times	80.37 \pm 0.37	69.23\pm1.31	6.24	45.83 \pm 0.58	38.86 \pm 0.78	160
<i>Standalone</i>	-	-	61.11 \pm 24.90	28.99 \pm 27.24	-	27.49 \pm 14.76	16.31 \pm 15.75	-
FedKD	\checkmark	\checkmark	80.98\pm0.11	65.46 \pm 3.45	0.078	45.55 \pm 0.38	40.61\pm2.54	2

Table 1: Comparisons on the CIFAR-10 and CIFAR-100 datasets with ResNet-8 when $K=20$. Our FedKD uses $S=200$, $\gamma=1$ for knowledge ensemble, while the competing methods use the setting in FedDF (Lin et al. 2020) with 100 rounds and a sampled fraction as 1 at each communication round. *Standalone*: mean/std performance of all local models. Both logits and parameters are of type float64 for bandwidth calculation.

aggregation scheme	baseline	Eq. 1 $\tau = \infty$	Eq. 1 $\tau = 3$	Eq. 1 $\tau = \infty$	Eq. 1 $50 \times \mathcal{D}^0 $
logits distillation	$\tau = \infty$	$ \mathcal{D}^0 $	$ \mathcal{D}^0 $	$ \mathcal{D}^0 $	$50 \times \mathcal{D}^0 $
# local prediction	79.92	80.01	80.98	81.89	
Accuracy(%) \uparrow		0.078		3.91	
Bandwidth (GB) \downarrow					

Table 2: Ablation study on CIFAR-10 with ResNet-8, $K=20$, $\alpha=1$, $S=200$, $\gamma=1$. With the commonly used aggregation scheme (Lin et al. 2020; Hsu, Qi, and Brown 2020) as baseline, we show the comparison on different aggregation schemes. Besides, we do ablation study with different temperatures for logits distillation (Hinton, Vinyals, and Dean 2015). $|\mathcal{D}^0|$ indicates the number of samples in the public dataset \mathcal{D}^0 , and $50 \times |\mathcal{D}^0|$ indicates local model predicts 50 times on each sample of \mathcal{D}^0 with different augmentation seeds.

in the following experiments.

Chest X-Ray Image Classification

Although mainstream FL methods experiment exclusively with private data from the same dataset (domain), this is typically not realistic in practical applications. For example, data acquired at different hospitals may come from different sources. We thus consider a more general heterogeneous setting where the private data at different local nodes and the unlabeled public data all come from different domains.

Method	Private data \mathcal{D}^k	Test	$K = 3$	$K = 5$
			$K = 2$	$K = 6$
FedKD	CXR14	CXR14	75.02	74.80
	Xpert	Xpert	82.41	82.35
FedMD	CXR14+Xpert	CXR14	78.19	73.79
	CXR14+Xpert	Xpert	78.01	77.97
FedKD	CXR14+Xpert	CXR14	79.03	76.13
	CXR14+Xpert	Xpert	79.77	80.91

Table 3: Multi-label classification experiments on chest-x-ray images with single/cross domain private data. We report the test mAUC (%) on NIH CXR14 and CheXpert over 12 and 8 classes respectively.

Here we implement multi-label classification on chest-x-ray images, using the NIH CXR14 (Wang et al. 2017) and CheXpert (Irvin et al. 2019) datasets to represent different domains for private data. We ignore ambiguous categories (Effusion, Pleural Effusion, Pleural Other and Support Device), remaining a total of 14 annotation classes, of which NIH CXR14 has annotations for 12 classes and CheXpert for 8 classes, with 6 overlapping classes. So there are totally 86,524 images come from NIH CXR14 and 64,346 images come from CheXpert dataset. For each dataset, we randomly sample 90% for training and the rest 10% for validation. We use 26,684 images from the RSNA Pneumonia Detection Challenge (Kaggle 2018) without using their labels as public data.

In the setting with cross-domain private data (two datasets as private data), each dataset is distributed to $K_d = K/2$ local nodes when there is a total of K local nodes. For local training, we use a batch size of 32, same data augmentation strategies as in prior work (Ye et al. 2020), and train each local node individually with SGD and CosineAnnealing, decreasing the learning rate from 1e-2 to 1e-4 in ten epochs. For distillation, we use SGD and a constant learning rate of 1e-3 and 30 epochs.

In Table 3, we first study the hyper-parameters K with $\alpha=1$, $S=200$, $\gamma=1$ and local data from a single dataset (domain). It shows larger numbers of locals K negatively affects the distillation performance. Table 3 also shows cross-domain, cross-site evaluations using both datasets as private data, with a total of K local nodes ($K_d=K/2$ for each dataset, and each node hosts data from only one of the datasets). When comparing with the distillation-based FL work FedMD (Li and Wang 2019) under the same cross-domain scenario, FedKD outperforms FedMD by a significant margin on both test datasets. More importantly, our FedKD provides a stronger privacy guarantee with noise perturbation.

Street Scenes Segmentation

Cityscapes (Cordts et al. 2016) is a semantic segmentation dataset of urban street scenes collected from Germany, France, and Switzerland. We stratify the training data based on the origins (e.g., three countries) as private data and

Method	\mathcal{D}^1	\mathcal{D}^2	\mathcal{D}^3	mIoU(%)	Pixel Acc(%)
PATE	CS_Germany	CS_Swiss	CS_France	64.48	93.97
FedKD	CS_Germany	CS_Swiss	CS_France	70.31	94.77
	CS_Germany	CS_Swiss	CamVid	69.31	93.98
	CS_Germany	CS_Swiss	GTA5	66.79	93.71
	CS_Germany	CamVid	GTA5	63.69	93.01

Table 4: Study on street scenes segmentation with varying local training data \mathcal{D}^k with $K=3$.

Method	Privacy		Average Dice(%) \uparrow	Communication Efficiency	
	NO shared Param.	Noise perturb.		Bandwidth(GB) \downarrow	One-shot
FedMD (Li et al. 2019)	✓	✗	75.71 84.33	2154.84 64.37	✗
FedKD	✓	✓	77.80	13.36	✓

Table 5: Comparisons on BraTS. We compare privacy guarantee, average Dice score over voxel-level annotations of “whole tumour”, “tumour core”, and “enhancing tumour”, and other communication efficiency attributes.

use 1,525 unlabeled test images as public data. We test 19 classes on the validation dataset of cityscapes which contains 500 images. We use PSPNet (Zhao et al. 2017) with ResNet101 (He et al. 2016), with the backbone pretrained on ImageNet (Deng et al. 2009), and follow the training strategy in (Liu et al. 2019). Although public data and the training data of each local client are collected from different sites, we further experiment with the under-explored larger domain gaps among the local training data.

In Table 4, we experiment with local data with different degree of domain gap. With the same locally trained models, our FedAD demonstrates superior performance on both mIoU and pixel accuracy compared with another privacy preserving method PATE.

Brain Tumor Segmentation

The BraTS 2018 dataset (Bakas et al. 2018) contains multi-parametric pre-operative MRI scans of 285 subjects with brain tumors. Each subject was scanned under the T1-weighted, T1-weighted with contrast enhancement, T2-weighted, and T2 fluid-attenuated inversion recovery (T2-FLAIR) modalities. For consistency, we follow the same experimental protocol as prior work (Li et al. 2019), using 242 subjects for the training set and 43 subjects for held-out test set. According to the originating institution, the training set is stratified into three federated local clients. We use the unlabeled validation set of the BraTS 2020 dataset (Menze et al. 2014) as the public data comprising 125 subjects, independent of either private dataset.

We use the same model structure as (Li et al. 2019) and the same training strategy as (Myronenko 2018). The local training takes 20,000 iterations, with local-to-central distillation taking 5,000 iterations. Table 5 compares the segmentation performance and other utilities. One can note that our FedKD substantially outperforms the competing methods with the best privacy/performance trade-offs.

		FedAvg	FedDF	FedKD	Standalone	Centralized
AG News	Accuracy (%) \uparrow Bandwidth(MB) \downarrow	91.98 10217	92.57 10235	92.58 36.6	86.30 \pm 5.21	93.11
SST2	Accuracy (%) \uparrow Bandwidth(MB) \downarrow	87.13 10217	88.51 10221	91.50 10.3	74.80 \pm 5.05	90.07
Privacy (NO shared Param.)		✗	✗	✓	-	-

Table 6: Comparisons on AG News and SST2 datasets with $K=10$ under the same experiment setting. *Standalone*: mean \pm std of local models trained with individual private data. *Centralized*: centralized training all local private data.

Text classification tasks

We evaluate our framework on two text classification datasets: AG News (Zhang, Zhao, and LeCun 2015) and SST2 (Socher et al. 2013). Following FedDF (Lin et al. 2020), we use pre-trained DistilBERT (Sanh et al. 2019) as the transformer language model. Local training and distillation takes 100 and 20 epochs, respectively, and the training strategy is the same as FedDF. From Table 6, we can note that our method gives the best performance on both datasets. On bot AG News and SST2 dataset, our proposed framework achieves superior accuracy and substantially lower communication bandwidth compared to the prior arts. More importantly, our method does not share parameters/gradients of local models during communication, which offers much stronger privacy guarantee compared to the prior arts.

Conclusions

In this work, we propose a novel distillation-based federated learning framework, namely FedKD, which can preserve local data privacy by learning with only unlabeled and domain robust public data. To comprehensively address the communication bottleneck, we employ a one-shot and one-way (offline) knowledge distillation process with an efficient ensemble scheme. Extensive experiments on both classification and segmentation tasks using cross-domain and heterogeneous data distributions demonstrate the efficacy of FedKD with better privacy guarantee compared to prior arts. Given the increasing importance of privacy, we believe our proposed FL method will be a practical solution to facilitate privacy-preserving decentralized learning across multiple sites in real-world scenarios, especially for medical applications where leveraging valuable local data at different hospitals without exposing proprietary data to privacy risks is essential.

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