

# Sensors

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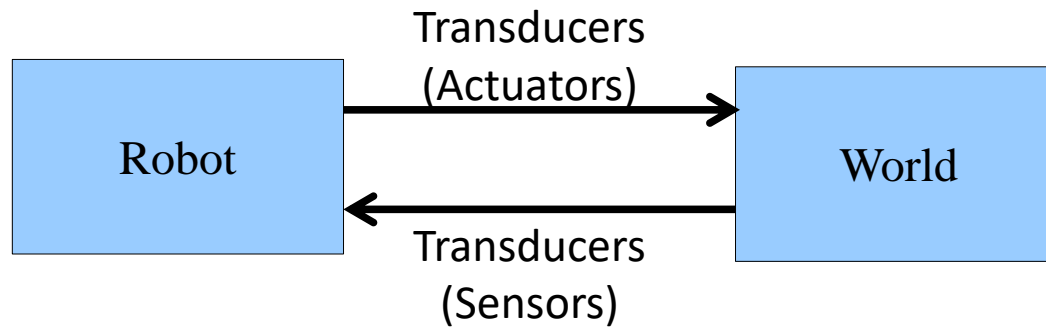
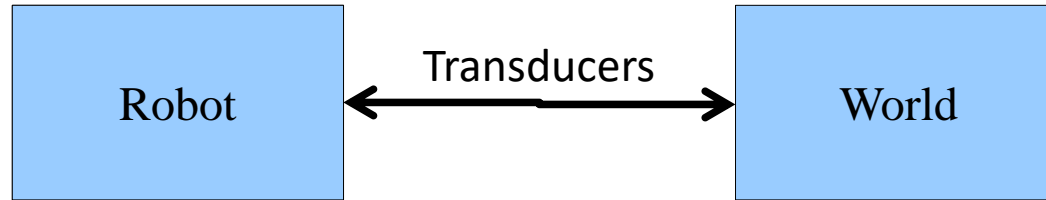
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*Also, a very special Thank You to: **Prof. Nuno Lau, IEETA, U. Aveiro***



# Robot & World



# The Perception Problem

# The Perception Problem

- **What does a robot needs to sense**
  - Depends on what the robot needs to do
  - Animals have evolved sensors that suited to their environment and position in the ecosystem
    - ⇒ A good robot designer should follow similar principles
- **Two possible questions:**
  - Given a sensory reading, what was the world like when the reading was taken?
  - Given a sensory reading, what should I do?

# The Perception Problem

- **The first question**
  - Focused on world representation
  - Perception is considered in isolation
- **The second question**
  - Perception without the context of action is meaningless
  - Systemic view of the robot design
    - Task to perform
    - Best suited sensors
    - Most suited mechanical design

# Some current sensing methods

- **Action oriented perception**
  - Direct link between perception and action
- **Expectation-based perception**
  - Sensor interpretation constraining based on world knowledge
- **Task-driven attention**
  - Direct perception where information is needed or likely to be provided (focus-of-attention)
- **Perceptual classes**
  - Partition world in manageable categories

# What is a sensor?

Sensors:

- Are transducers (change physical properties)
- Map physical attribute(s) to a [quantitative] measure(s)
- Produce results, measurements over time
- Constitute the perceptual system of the robot (perception after measurement)
- Sensor “chain” (perception chain likely hardware + software)
- Transducer + electronics + ADC + software

# Human sensing

Sense	Physical attribute	Organ
Vision	EM waves	eyes
Audition	Pressure waves	Ears
Gustation	Chemical properties	Tongue
Olfaction	Chemical properties	Nose
Tact	Contact pressure/texture	Skin

- Humans can also sense other things like temperature, pain, equilibrium, own body
- Several animals have still other types of sensor capabilities



# Robot sensors

- **Proximity**
  - Infrared, Sonar, laser, optical, capacitive, inductive
- **Position**
  - Potentiometer, switch, buttons, encoder
- **Heading**
  - Compass, gyroscope
- **Temperature**
  - Thermocouple
- **Sound**
  - Microphone
- **Force, Pressure**
  - Piezoelectric, variable resistance
- **Battery, Current**
  - Thermocouple
- **Chemical**
  - Several
- **Magnetic field**
  - magnetometer
- **Vision**
  - Camera
- **Etc...**

# Levels of sensing

- **Attribute to be measured**
- **Physical principle of transduction**
  - Determines many of the characteristics of the sensor
- **Hardware**
  - Electronics
- **Software**
  - Signal processing
  - Computation
  - Sensor fusion

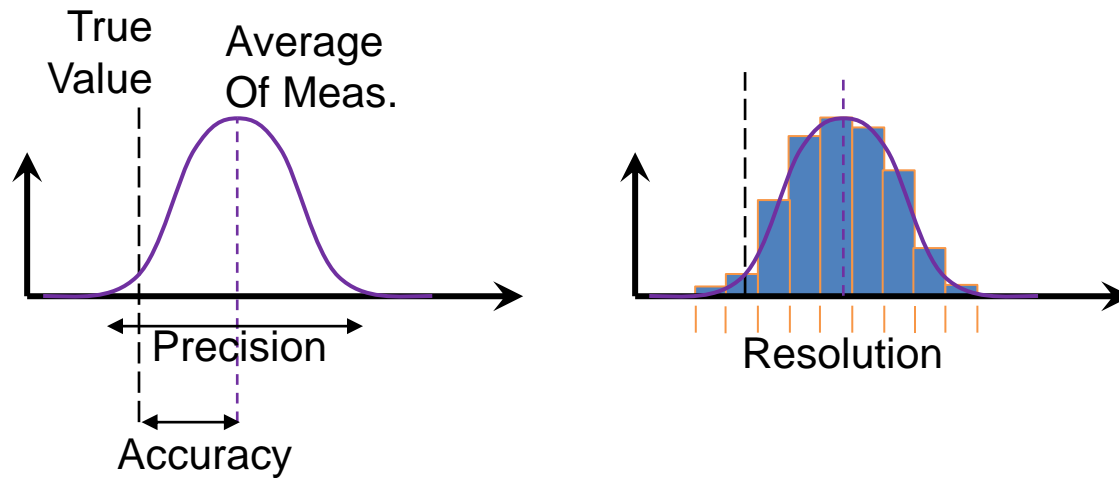
# Levels of sensing

- **Attribute to be measured**
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# Sensor Characteristics

- Field of view and Range
- Accuracy, repeatability and resolution
- Responsiveness in the target domain
- Power consumption
- Hardware reliability
- Size
- Computational complexity
- Interpretation reliability

# Accuracy...



High Accuracy AND  
High Repeatability



Low Accuracy BUT  
High Repeatability



Medium Accuracy AND  
Medium Repeatability



Low Accuracy AND  
Low Repeatability

<https://www.pi-usa.us/en/tech-blog/the-difference-between-position-accuracy-and-repeatability-and-methods-to-reduce-position-errors/>

Optional viewing: <https://www.youtube.com/watch?v=-Lit-lusMZk>

# Sensor errors

- **Systematic errors**

- Always push the measured value in the same direction
- Can be reduced by sensor calibration
- Ex: temperature in sonar, wheel radius in odometry
- Note: Interference is different, some interferences can be measured and corrected by sensor fusion like techniques

- **Non systematic errors**

- Have a more random behavior
- Cannot be predicted or eliminated by calibration

**≠ Interference** (external influence)

# Classification of sensors

- **Passive sensors**

- Rely on environment to provide the medium for observation
- Ex: Camera, thermocouple, microphone
- Less energy
- Reduced Signal to Noise ratio

- **Active sensors**

- Emits form of energy and measures the impact
- Ex: sonars. X-ray
- Restricted environments

# Classification of sensors

- **Proprioceptive**
  - Measure values internally to the system
  - Ex: motor speed, battery status, joint angle, etc.
- **Exteroceptive**
  - Information from the robots external environment
  - Generally considering the robots frame of reference
  - Depend on something external

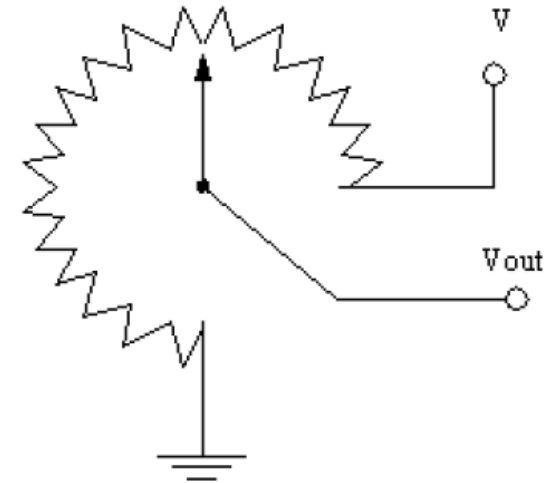


# Proprioceptive sensors

- Potentiometers
- Encoders
- Inertial navigation system
- Compass
- Gyroscopes
- Battery sensors

# Potentiometer

- **Physical principle:**  
Linear tension variation at the output of a variable resistance
- **Can be used to detect angular or linear position**
  - Joint angle, servomotor, etc



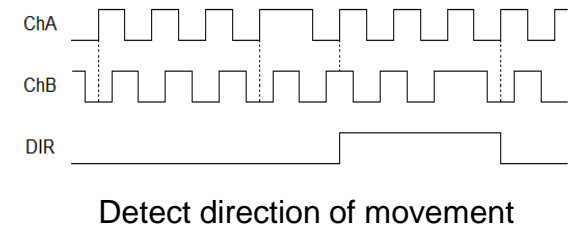
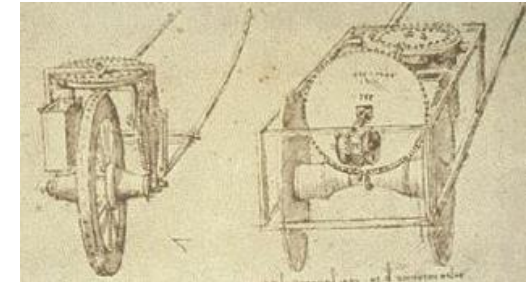
# Encoders / Odometry

- **Physical principle**

Record the wheel traversed distance

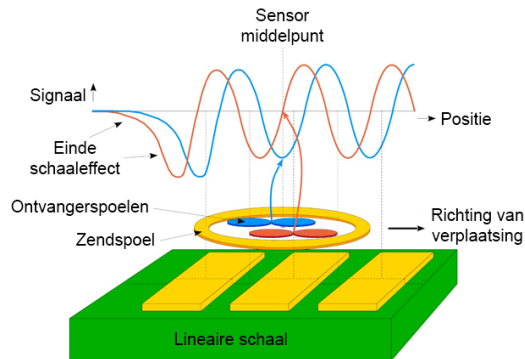
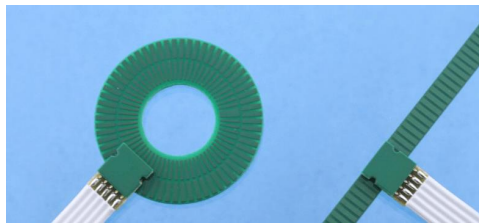
- **Wheel traversed distance is used to estimate robot position and orientation**

$$v = \frac{v_1 + v_2}{2}$$
$$\omega = \frac{v_1 - v_2}{b}$$



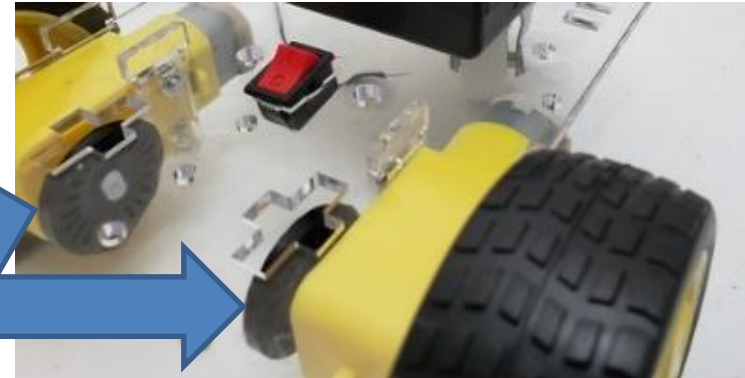
# Encoders / Odometry

Magnetic version  
of an encoder:  
(Rotary or linear)

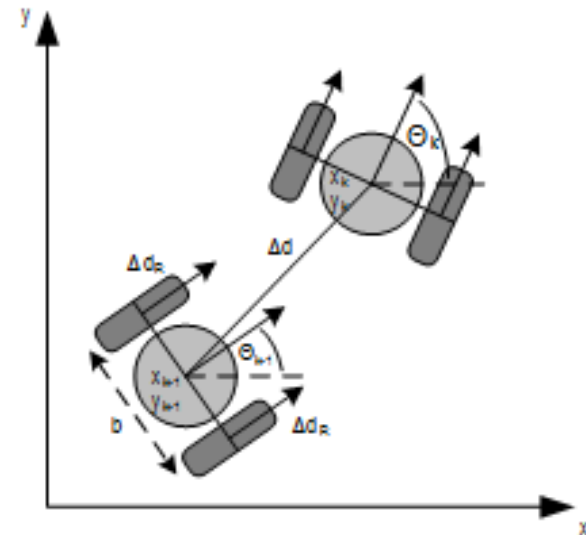


<https://e.sentech.nl/en/news/inductive-encoder-accurately-measure-displacement-in-harsh-conditions>

The two encoder wheels,  
one for each motor,  
beneath transparent  
floor of the robot



<https://automaticaddison.com/how-to-make-an-autonomous-wheeled-robot-using-ros/>



<https://hackaday.io/project/158496-imcoders/log/147068-robot-odometry>

# GPS/DGPS

- **Physical principle**

Triangulation over the distance to several satellites

- **Estimates longitude, latitude and altitude**

- Resolution: 10-15m

- **DGPS (Differential GPS)**

- Extra GPS receivers at known locations are used to reduce errors
  - Resolution: few centimeters

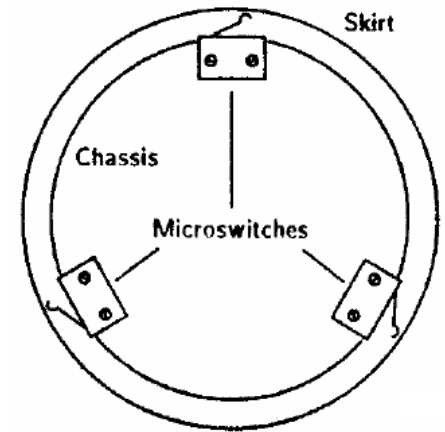


# Proximity sensors

- Bumper
- Infrared
- Sonar
- Laser Range Finder

# Bumper

- **Physical principle**  
Direct contact closes (or opens)  
a circuit
- **Used to detect collisions**
- **Binary value**
- **Reliable but the collision is eminent**



# Infrared sensor

- **Physical principle**

Na IR emitter/receiver is used to detect distance or as a barrier

- **Used to estimate distance , presence of objects or color**

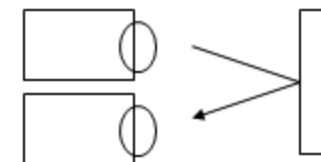
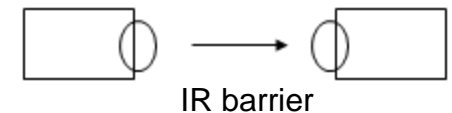
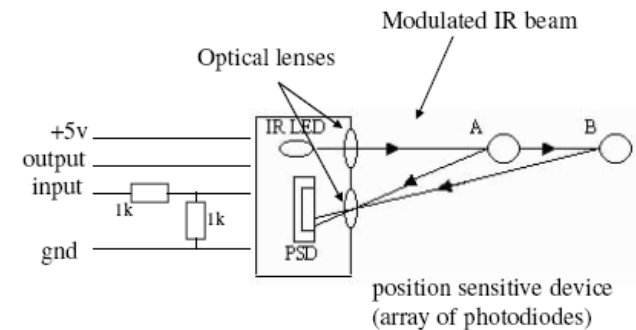
- Some dark surfaces do not reflect IR

- **Several technologies**

- **Range: from <10cm to ~1m**

- **Narrow field of view**

- **Cheap**





# Sonar

- **Physical principle**

Emit US chirp, time until echo is received is used to estimate distance

- **Time until echo is proportional to the distance until closest obstacle**

- Speed of sound changes with temperature and pressure

- **Range: few centimeters to ~10m**

- **Field of view ~30°**

- **Cheap (but not as cheap as IR)**

- **Fast (depends on range)**

- **Ring of sonars**

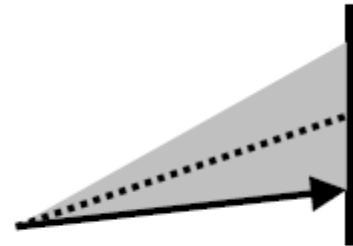


# Sonar problems

- **Foreshortening**

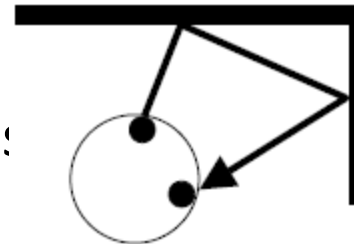
- **Crosstalk**

- Receiver may detect echoes from objects in the ring



- **Specular reflection**

- Wave is reflected when angle is



# Laser range finder

- **Physical principle**

Similar to sonar but uses laser instead of sound

- **Time of flight is used to estimate distance**
- **Range: 2m until ~500m**
- **Resolution: 1 cm**
- **Field of view: 100°-180°**
- **Much more accurate than sonar**
- **Also more expensive**



# Vision

Pinhole camera

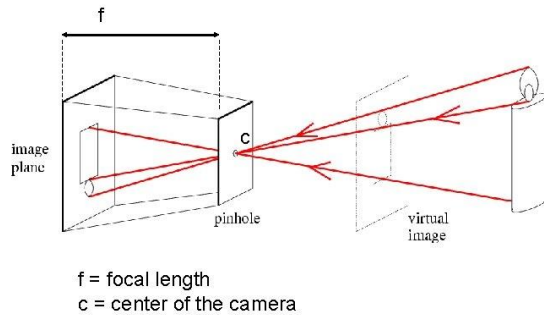
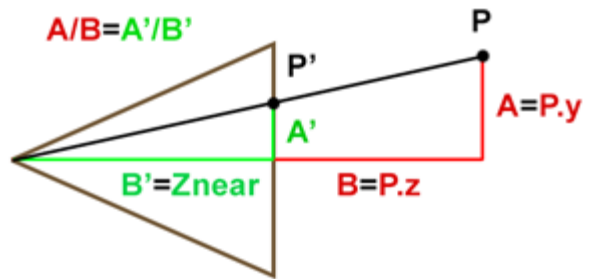


Figure from Forsyth

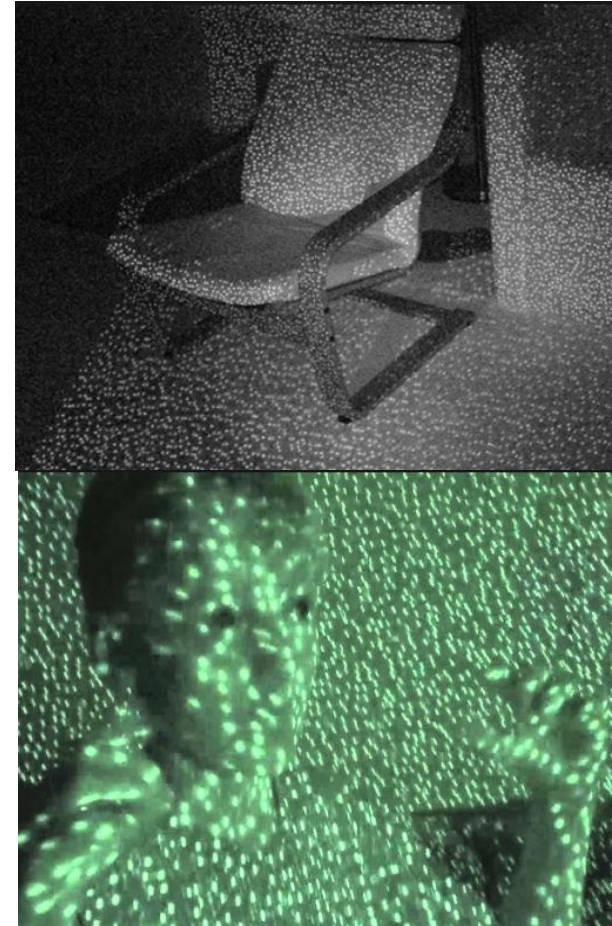
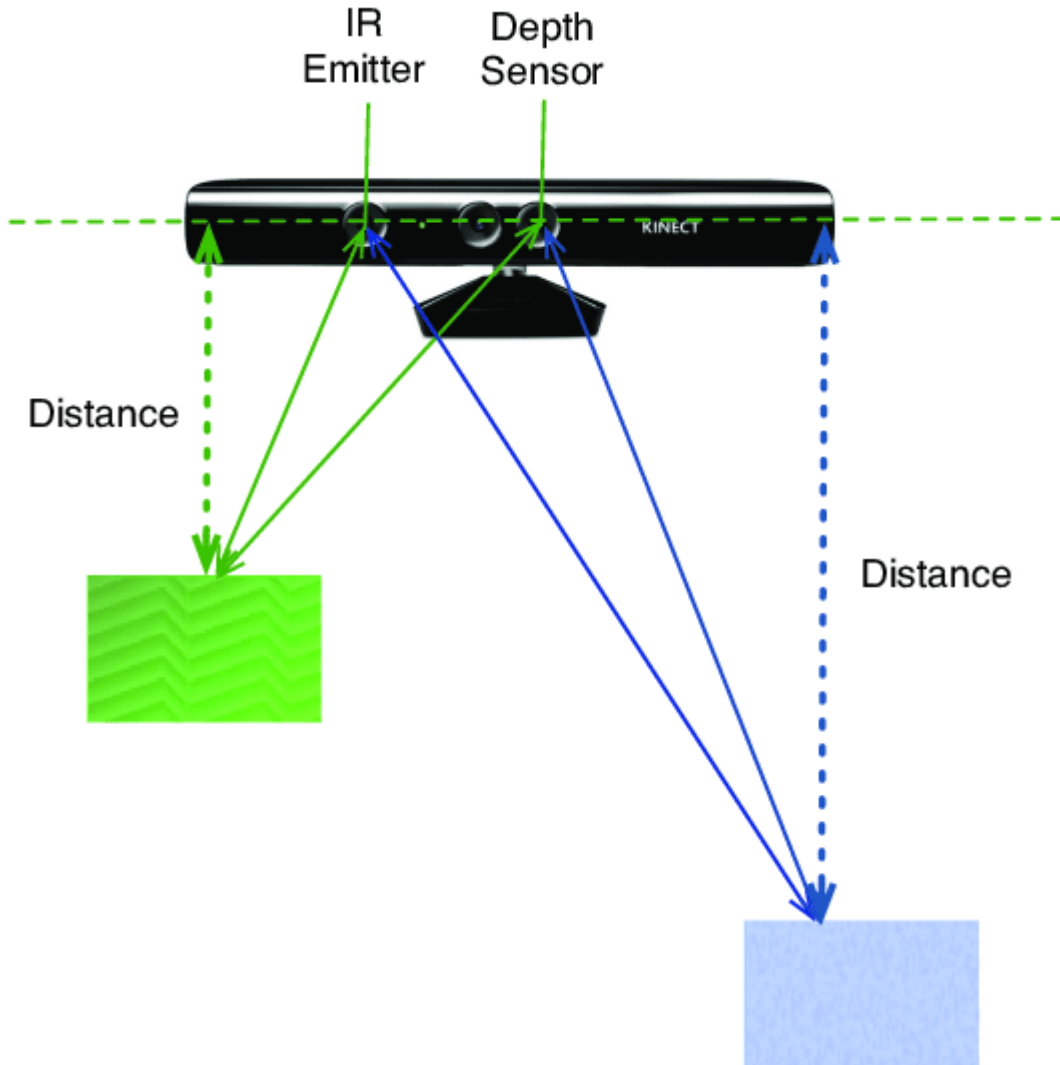


© www.scratchapixel.com

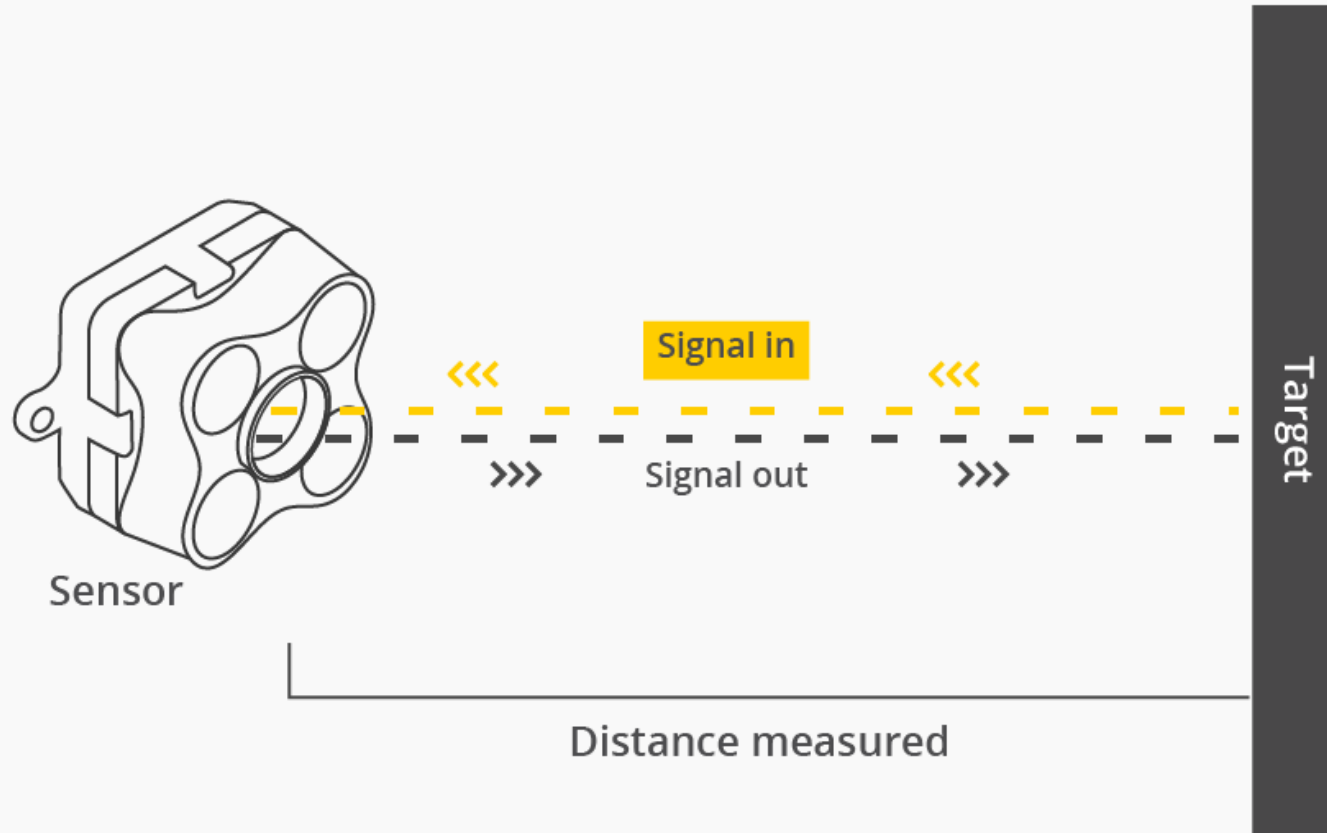
<https://slidetodoc.com/pinhole-camera-model-computational-photography-derek-hoim-university/>

<https://www.scratchapixel.com/lessons/3d-basic-rendering/3d-viewing-pinhole-camera/how-pinhole-camera-works-part-2>

# Depth Sensing

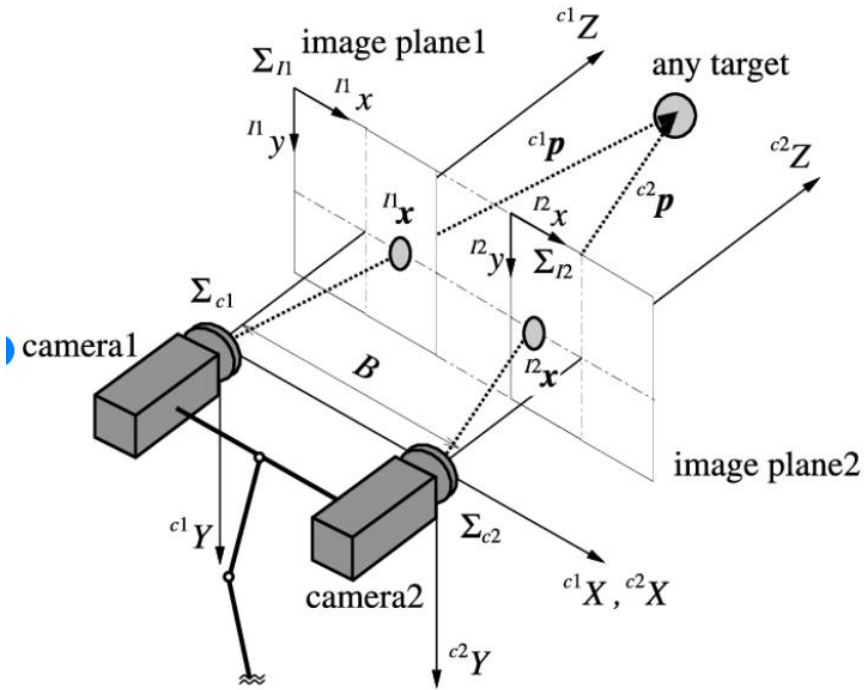


# Depth Sensing





# Stereo Vision



<https://www.stereolabs.com/zed-2i/>

<https://www.stereolabs.com/solutions/robotics/>

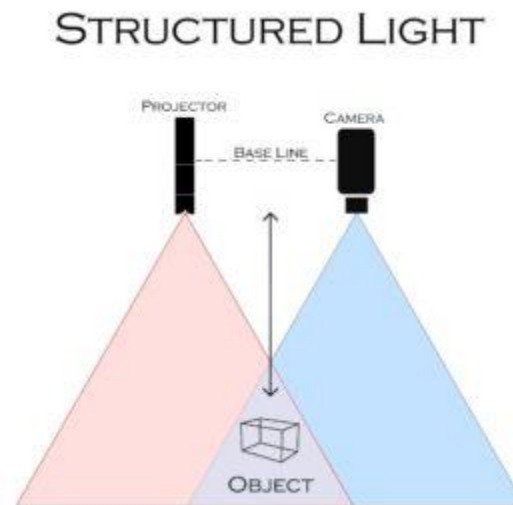
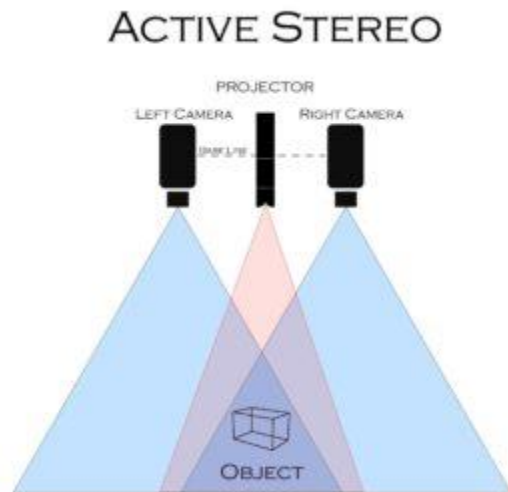
Visual tracking of unknown moving object by adaptive binocular visual servoing 1999

DOI:[10.1109/MFI.1999.815998](https://doi.org/10.1109/MFI.1999.815998)

• [IEEE Xplore](https://ieeexplore.ieee.org/abstract/document/815998)

• Conference: Multisensor Fusion and Integration for Intelligent Systems,

# Active Stereo

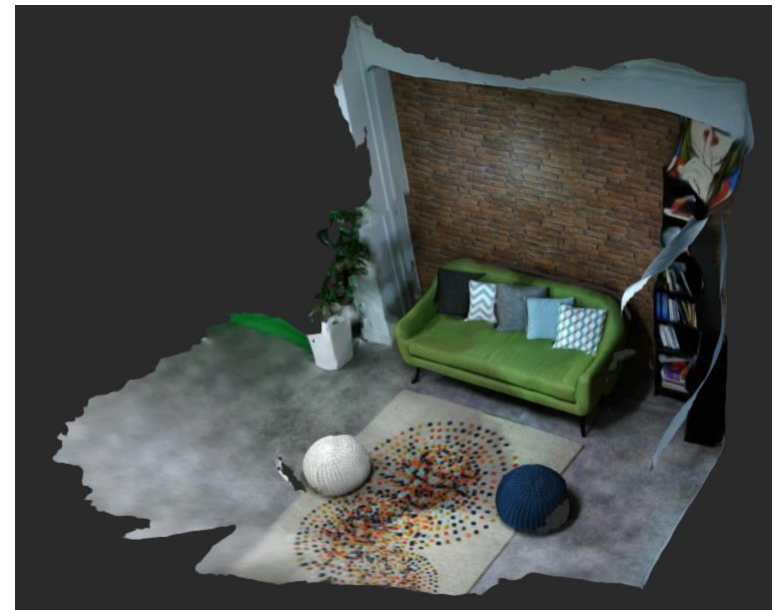


<https://www.osela.com/depth-sensing/>

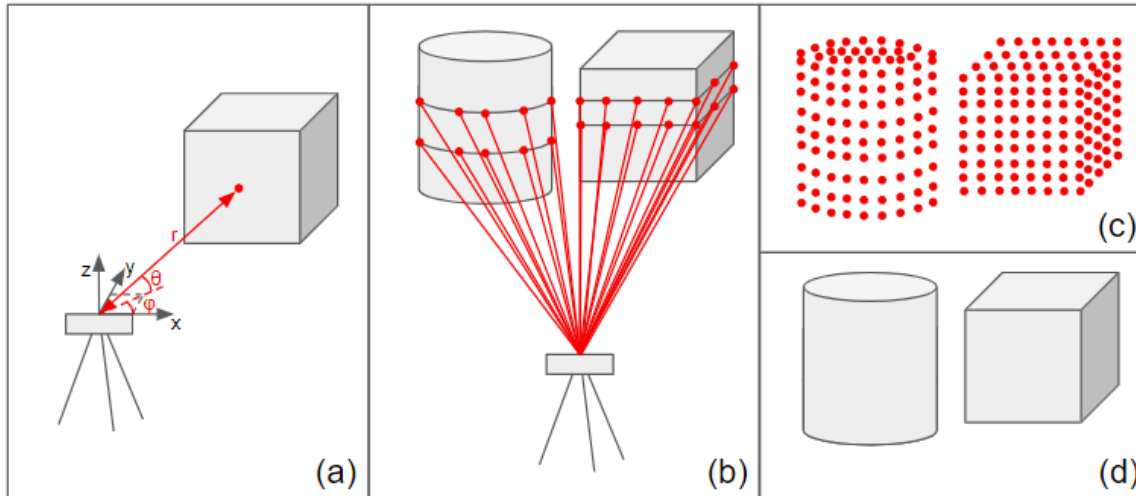


# RGBD

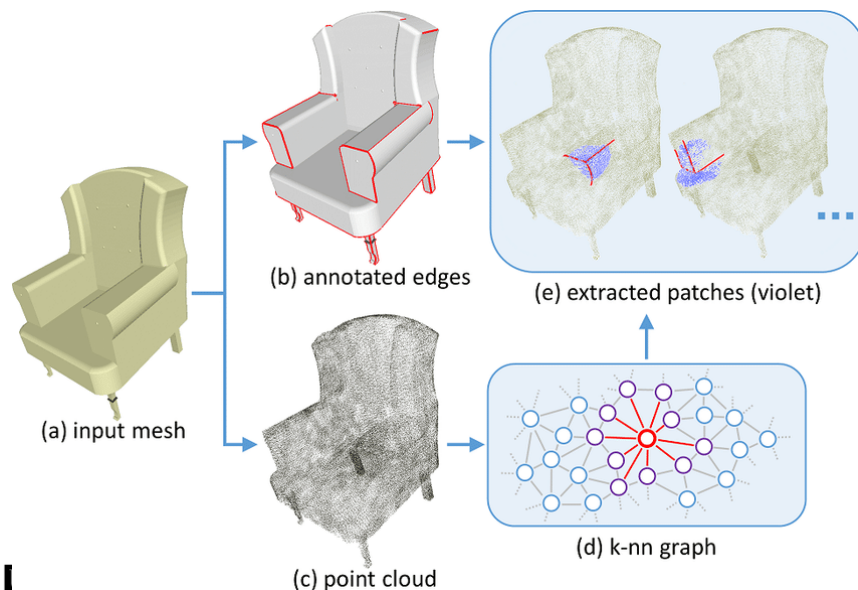
- <https://p3d.in/ifOvj> (interactive!)



# RGBD – Point Cloud



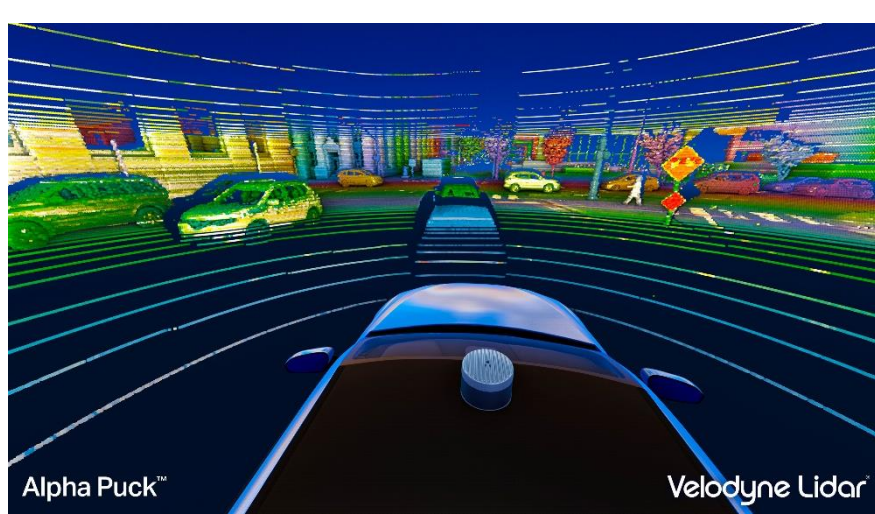
<https://blog.bricsys.com/point-clouds-whats-the-point/>



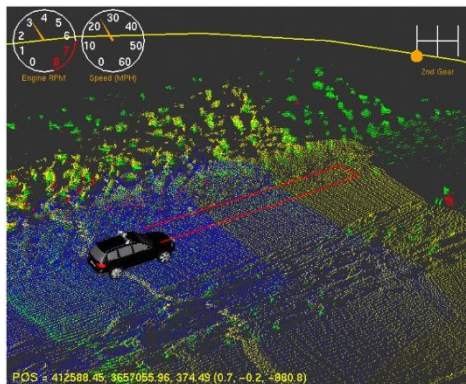
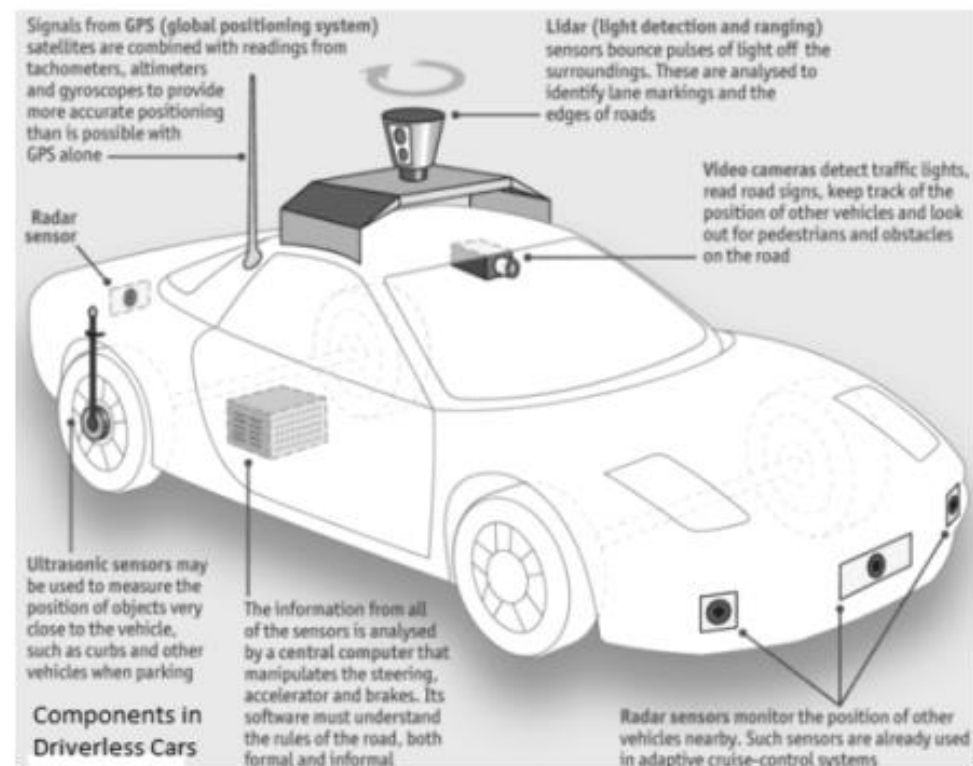
Yu, Lequan & Li, Xianzhi & Fu, Chi-Wing & Cohen-Or, Daniel & Heng, Pheng-Ann. (2018). EC-Net: an Edge-aware Point set Consolidation Network.

[https://www.researchgate.net/publication/326459389\\_EC-Net\\_an\\_Edge-aware\\_Point\\_set\\_Consolidation\\_Network](https://www.researchgate.net/publication/326459389_EC-Net_an_Edge-aware_Point_set_Consolidation_Network)

# Automotive Sensors / LIDAR



<https://www.roboticsbusinessreview.com/unmanned/unmanned-ground/velodyne-touts-latest-lidar-advances-autonomous-vehicle-partnerships/>



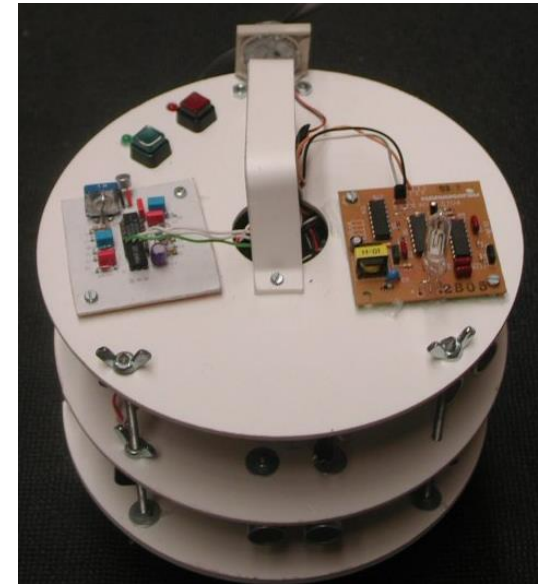
Thrun et al.

Thakurdesai, Hrishikesh & Aghav, Jagannath. (2021). Autonomous Cars: Technical Challenges and a Solution to Blind Spot.

Components of Driver-less Car  
(Source: The Economist,  
How does a self-driving car work )

# Fire detection sensors

- **Physical principle**  
Detect flame by sensing ultraviolet light
- **Flame detector, fire alarms, fire fighting competitions, etc**
- **Can detect a flame from a cigarette lighter from a distance of more than 5m**





# Compass

- **Physical principle**

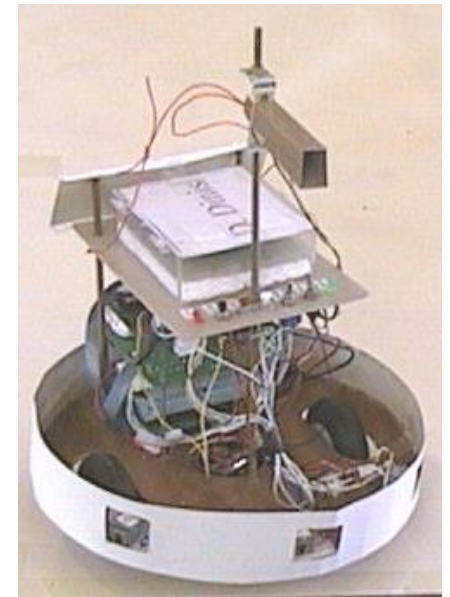
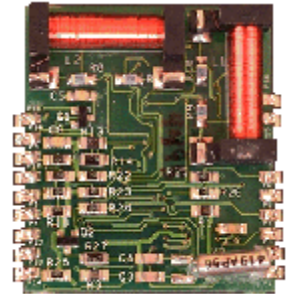
Detection of Earth magnetic field

- **Used to detect robot orientation**

- **Together with velocity information can be used for dead reckoning**

- **Resolution 1º, Accuracy 2º**

- **Sensitive to other magnetic fields of metal in the environment**



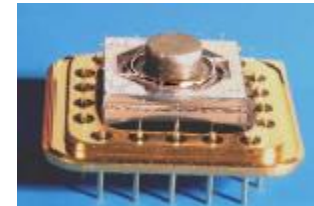
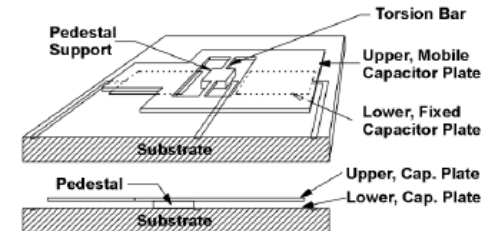
# Inertial sensors

- **Accelerometer**

- Measures the linear acceleration of the robot
- Second integration to obtain displacement

- **Gyroscope**

- Measures the angular motion of the robot
- Not influenced by gravity
- Integration gives angular displacement



# Multisensor fusion

- **Redundant**
  - Several sensors return the same percept
- **Complementary**
  - Provide disjoint types of information about percept
- **Coordinated**
  - Sequence of sensors
  - Focus-of-attention

# Redundant Multisensor fusion

- **Mean of several measures**
  - Considering a normal distribution:

The mean of N measures as a reduced covariance

$$M \sim N(\mu, \sigma^2)$$

$$Mean = 1/N \sum_{n=1}^N M_i$$

$$Mean \sim N\left(\mu, \sigma^2/N\right)$$



# Sensor Fusion

- **Kalman filter**

- Integration of measures over time
- Markovian assumption
- Considers physics model and action model

- Predict step

$$x_t = Px_{t-1} + Cu_t + q \quad \begin{matrix} q & N(0, Q) \\ r & N(0, R) \end{matrix}$$

$$z_t = Hx_t + r \quad N(\hat{x}_{t-1}, \Sigma_{t-1})$$

- Information

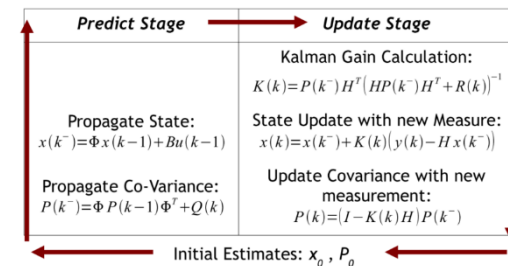
$$\bar{x}_t = P\hat{x}_{t-1} + Cu_t$$

$$\bar{\Sigma}_t = P\Sigma_{t-1}P^T + Q$$

$$K_t = \bar{\Sigma}_t H^T (H \bar{\Sigma}_t H^T + R)^{-1}$$

$$\Sigma_t = (I - K_t H) \bar{\Sigma}_t$$

$$\hat{x}_t = \bar{x}_t + K_t (z_t - H \bar{x}_t)$$



# EKF

$$\begin{cases} \frac{dx(t)}{dt} = Ax(t) + Bu(t) \\ y(t) = Cx(t) \end{cases}$$

$$x = [x_1 \ x_2 \cdots x_m]^T \quad \dim(A) = m \times m$$

$$u = [u_1 \ u_2 \cdots u_p]^T \quad \dim(B) = p \times m$$

$$y = [y_1 \ y_2 \cdots y_q]^T \quad \dim(C) = m \times q$$

$$\begin{cases} x(k) = \Phi x(k-1) + Gu(k-1) \\ y(k) = Hx(k) \end{cases}$$

$$\Delta t_k = t_k - t_{k-1}$$

$$\Phi(k) = e^{A \Delta t_k}$$

$$G = \int_{t_{k-1}}^{t_k} e^{A \Delta t_k} B dt$$

$$H = C$$

# EKF

$$\begin{cases} x(k) &= \Phi x(k-1) + Gu(k-1) + w(k-1) \\ y(t) &= Hx(k) + v(k-1) \end{cases}$$

$$R_w(k, i) = \begin{cases} Q(k) & \text{se } i=k \\ 0 & \text{se } i \neq k \end{cases}$$

$$E(w(k)v(i)^T) = 0, \forall k, i$$

$$E(x(0)) = X_0$$

$$R_v(k, i) = \begin{cases} R(k) & \text{se } i=k \\ 0 & \text{se } i \neq k \end{cases}$$

$$\begin{aligned} P(w) &\sim N(0, Q) \\ P(v) &\sim N(0, R) \end{aligned}$$

$$\text{cov}(x(0)) = P_0$$

Kalman Filter always keeps track of **averages** and **covariances** !

$$P \Rightarrow \sigma^2 = \begin{bmatrix} \text{cov}(y_1, y_1) & \text{cov}(y_1, y_2) & \cdots & \text{cov}(y_1, y_n) \\ \text{cov}(y_2, y_1) & \text{cov}(y_2, y_2) & \cdots & \text{cov}(y_2, y_n) \\ \vdots & \vdots & \ddots & \vdots \\ \text{cov}(y_n, y_1) & \text{cov}(y_n, y_2) & \cdots & \text{cov}(y_n, y_n) \end{bmatrix}$$

# EKF

```
Initial(State, Covariance)
```

```
Cycle:
```

```
    Propagate (Stat,Covar,SysModel,Inputs)
```

```
    Cycle Meas(i):
```

```
        If Valid(Meas(i)) then
```

```
            Update (Stat,Covar,MeasModel(i),Meas(i))
```

*This is an abuse => no guarantees!*

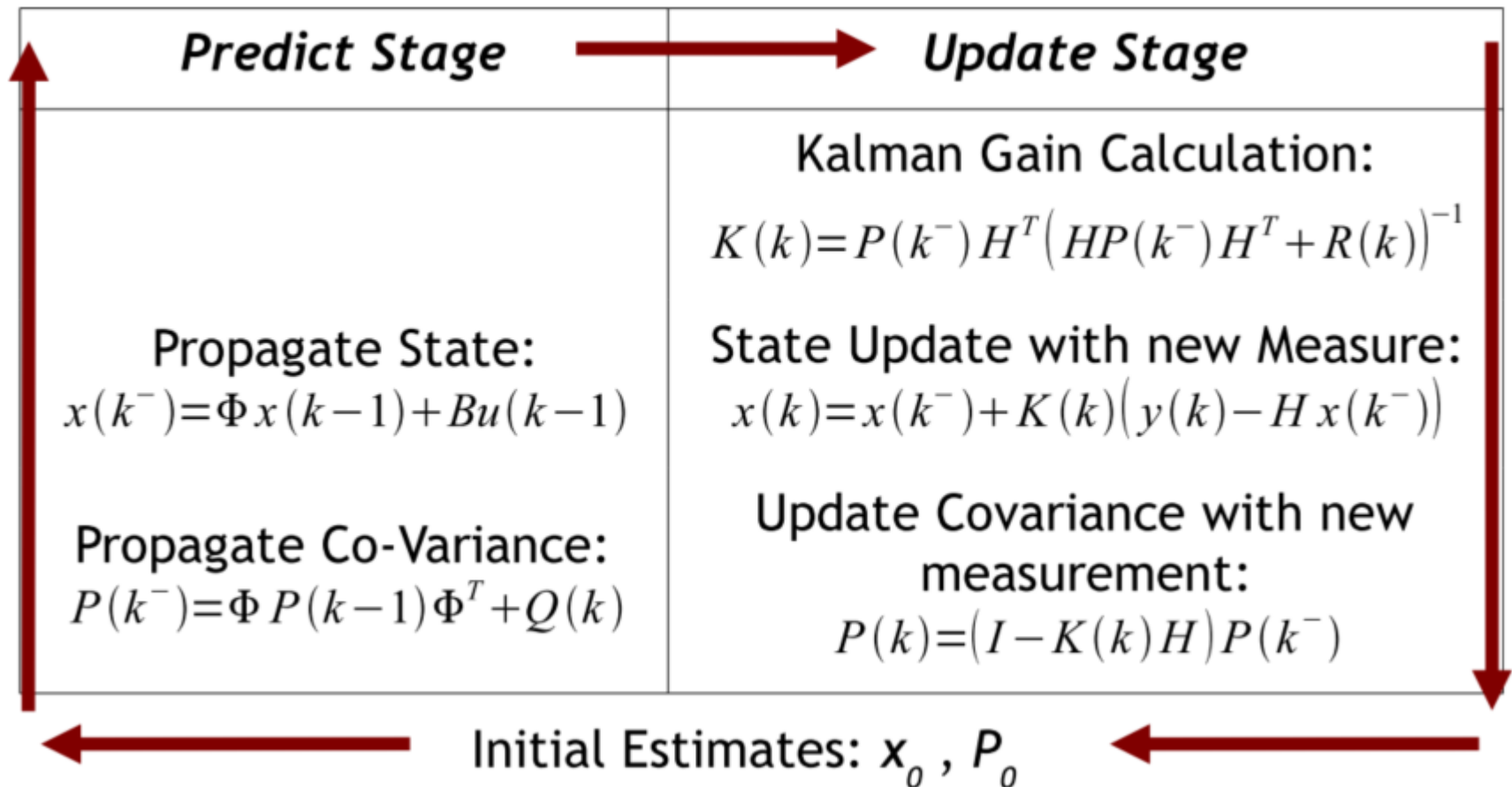
# EKF

$$\frac{dX(t)}{dt} = f(X(t), u(t_k), t), \quad t \in ]t_{k-1}, t_k] \quad A_k = \left. \frac{\partial f}{\partial x} \right|_{\substack{x=x(t_k) \\ u=u(t_k) \\ t=t_k}} \quad A(k) = \exp(A_k(t_k - t_{k-1}))$$

$$\begin{aligned} x(k) &\approx \tilde{x}(k) + A(x(k-1) - \hat{x}(k)) + W w(k-1) \\ y(k) &\approx \tilde{y}(k) + h(x(k) - \tilde{x}(k)) + V v(k) \end{aligned}$$

$$A = \frac{\partial f}{\partial x} = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} & \frac{\partial f_1}{\partial x_2} & \dots & \frac{\partial f_1}{\partial x_n} \\ \frac{\partial f_2}{\partial x_1} & \frac{\partial f_2}{\partial x_2} & \dots & \frac{\partial f_2}{\partial x_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial f_n}{\partial x_1} & \frac{\partial f_n}{\partial x_2} & \dots & \frac{\partial f_n}{\partial x_n} \end{bmatrix} \quad H = \frac{\partial h}{\partial x} = \begin{bmatrix} \frac{\partial h_1}{\partial x_1} & \frac{\partial h_1}{\partial x_2} & \dots & \frac{\partial h_1}{\partial x_n} \\ \frac{\partial h_2}{\partial x_1} & \frac{\partial h_2}{\partial x_2} & \dots & \frac{\partial h_2}{\partial x_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial h_q}{\partial x_1} & \frac{\partial h_q}{\partial x_2} & \dots & \frac{\partial h_q}{\partial x_n} \end{bmatrix} \quad W = \frac{\partial f}{\partial w} = \begin{bmatrix} \frac{\partial f_1}{\partial w_1} & \frac{\partial f_1}{\partial w_2} & \dots & \frac{\partial f_1}{\partial w_n} \\ \frac{\partial f_2}{\partial w_1} & \frac{\partial f_2}{\partial w_2} & \dots & \frac{\partial f_2}{\partial w_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial f_n}{\partial w_1} & \frac{\partial f_n}{\partial w_2} & \dots & \frac{\partial f_n}{\partial w_n} \end{bmatrix} \quad V = \frac{\partial h}{\partial v} = \begin{bmatrix} \frac{\partial h_1}{\partial v_1} & \frac{\partial h_1}{\partial v_2} & \dots & \frac{\partial h_1}{\partial v_n} \\ \frac{\partial h_2}{\partial v_1} & \frac{\partial h_2}{\partial v_2} & \dots & \frac{\partial h_2}{\partial v_n} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial h_q}{\partial v_1} & \frac{\partial h_q}{\partial v_2} & \dots & \frac{\partial h_q}{\partial v_n} \end{bmatrix}$$

# EKF



# EKF – Trouble

EKF offer no theoretical guarantees

- Not Optimal

- May not converge

- Expect troubles with periodical functions such as trigonometrical

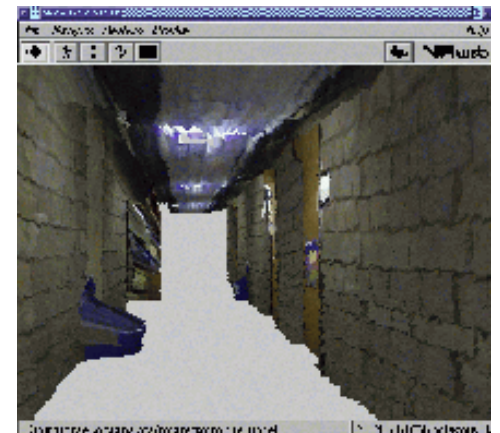
Should:

- Design and implement VERY carefully

- Test thouroughly

# Complementary Multisensor fusion

- **Example: Mercator Project**
  - The robot
    - 2 Laser ranger finders
    - 1 omnicam
  - Laser ranger finders are used to detect distance to walls and obstacles
  - Output of omnicam is used to apply textures to the model





# Sensors

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