

Feedback Exercise 8

These questions relate to the material in Weeks 16 and 17. These feedback exercises are due by **4pm on Tuesday February 25th, handed in electronically through the course Moodle page**. Late submissions will not be accepted. You must submit your solutions to the feedback exercises through Moodle. Your work must be legible and be in a single PDF file. A PDF scan of your work can be created by scanning your work on any photocopier in the university, for upload to Moodle. **We will not accept or grade photographed work.**

One of the aims of this course is to develop mathematical writing skills. These will be assessed explicitly in the feedback exercises using assessment criteria outlined in **SOLVE: communicating mathematics in writing** (see the course information sheets on Moodle). **These feedback exercises will be graded out of 30 marks, with 15 marks awarded for writing and 15 for mathematics.**

We encourage you to talk to each other about mathematics, and work in groups to understand the material in this course and the exercises. However, your final submitted feedback exercise must be your own work. This means that it is suitable to talk about the problems and get the ideas together, but you should do the final write up alone. You also should not show another student your final submission.

FB1 Find the volume of the solid generated by rotating the region bounded by the curves $y = e^x$, $y = \cos\left(\frac{\pi x^2}{2}\right)$ and $x = 1$ about the y -axis.

FB2 Decide whether the set A of positive integers divisible by 17 and B the set of positive integers divisible by 11 are in bijection.

FB3 Suppose that α, β are disjoint cycles in the symmetric group S_n for $n \geq 9$.

- Let α be a cycle of length 3 and β a cycle of length 9. What is the order of $\alpha\beta$. Is the permutation $\alpha\beta$ even or odd?
- Show that for every positive integer n we have

$$(\alpha\beta)^n = \alpha^n\beta^n.$$