面向高可靠通信的资源管理

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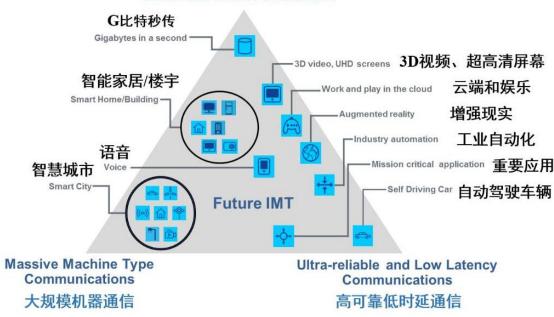
研究背景



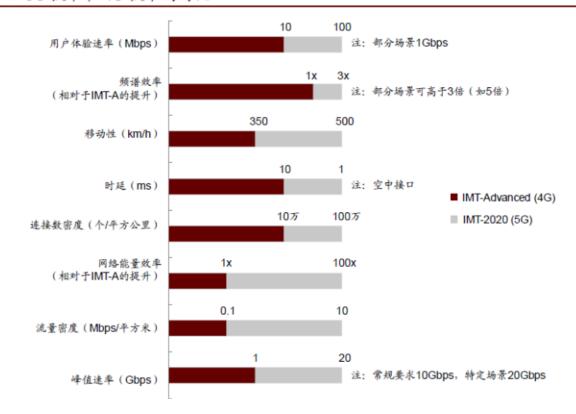
5G应用

增强型移动宽带

Enhanced Mobile Broadband



图表 5G 技术和4G 技术的对比





新型应用

	工业无线 网络需求	现有工业无线网络 (IEEE 802技术体系)	现有5G
时延	闭环时延<2ms	端到端时延百毫秒	端到端时延 几十毫秒
可靠性	高于99.9999%	高于99.99%	高于99.999%
安全性	防止 用户标识信息被截获、篡改	机器数字空间认证信息 易被截获、篡改	用户标识信息 易被截获、 篡改
高速率	峰值速率1Gbps (99.9999%可靠性下)	峰值速率54Mbps (99.99%可靠性下)	峰值速率100Mbps (99.999%可靠性下)
环境感知	物理环境、无线环境	无	无

但现有5G仍无法满足工业级信息交互需求

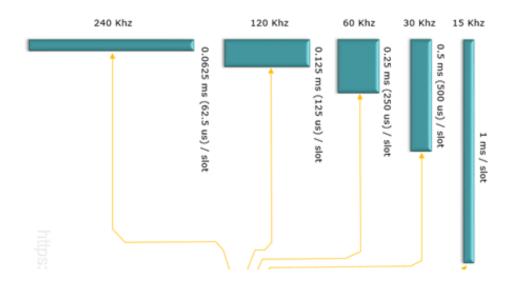


5G超可靠低时延技术

Feature	С	NR
Comm. types	Broadcast	Broadcast, Groupcast,
		Unicast
MCS	Rel. 14: QPSK,	QPSK, 16-QAM,
	16-QAM	64-QAM
	Rel. 15: 64-QAM	
Waveform	SC-FDMA	OFDM
Re-transmissions	Blind	HARQ
Feedback channel	Not Available	PSFCH
Control & data mul-	FDM	TDM
tiplexing		
DMRS	Four/sub-frame	Flexible
Sub-carrier spacing	15 kHz	sub-6 GHz: 15, 30, 60 kHz
		mmWave: 60, 120 kHz
Scheduling interval	one sub-frame	slot, mini-slot or multi-slot
Sidelink modes	Modes 3 & 4	Modes 1 & 2
Sidelink sub-modes	N/A	Modes 2(a), 2(d)

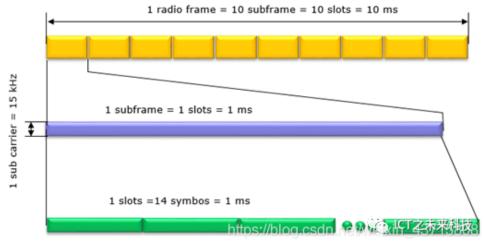
> 关键技术增强

- 灵活的载波间隔
- 时隙,迷你时隙和多时隙调度
- Sidelink反馈信道(PSFCH)

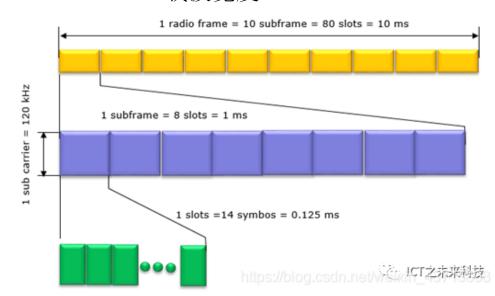




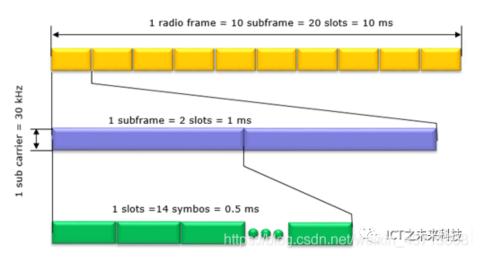
灵活的载波间隔



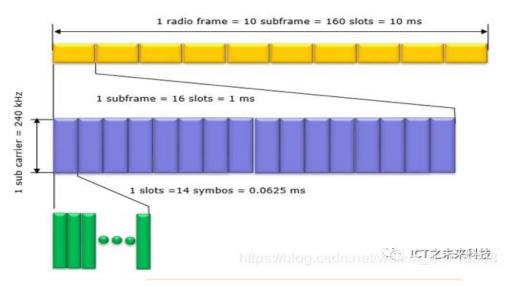
载波宽度15KHz



载波宽度120KHz



载波宽度30KHz



载波宽度240KHz



高可靠通信



越南战争时期的美军

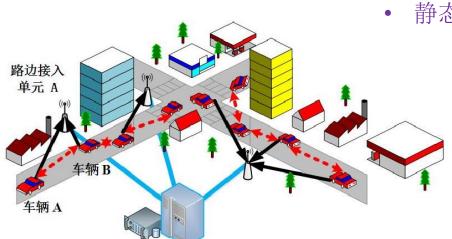
AK74和M16

启示: 严丝合缝的系统VS高可靠的系统



技术挑战

> 车联网



> 工业互联网

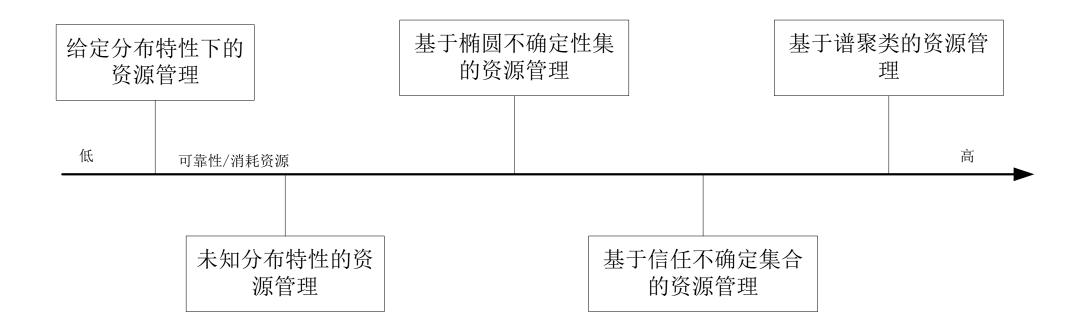


- 动态散射体
- 静态散射体

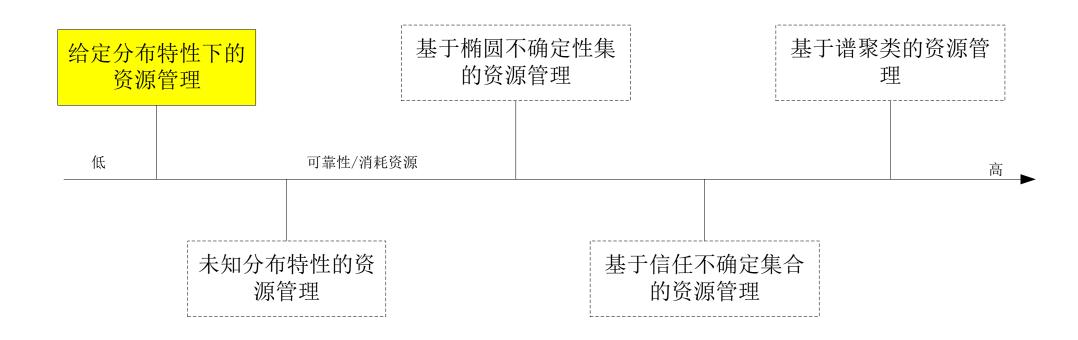
- ▶ 高动态无线信道特点
 - 时间非平稳
 - 深衰落
 - 明显的多普勒效用
 - 不同车流量下信 道的统计特性不 同
 - > 先前系统设计的不足
 - 孤立的存在
 - 和环境缺少交互
 - 自适应性差



面对不可靠信息的资源管理

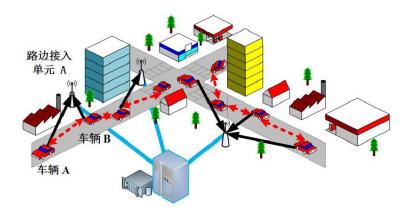


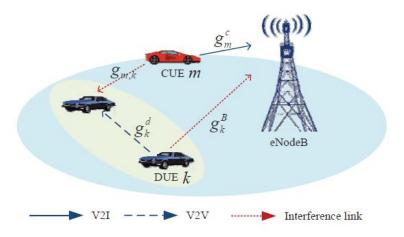






➤ System model





- Channel power gain $g_k^d = h_k^d \beta_k^d \varrho D_k^{-\iota} \triangleq |h_k^d|^2 \alpha_k^d,$
- Small-scale channel gain

$$h = \varepsilon \hat{h} + \sqrt{1 - \varepsilon^2} e.$$

- ϵ is determined by the high dynamic conditions
- SINR

$$\gamma_k^d \!=\! \frac{p_k^d \alpha_k^d \left(\varepsilon^2 |\hat{h}_k^d|^2 \!+\! (1-\varepsilon^2) |e_k^d|^2\right)}{\sigma^2 \!+\! \sum\limits_{m \in \mathcal{M}} \!\! x_{m,k} p_m^c \alpha_{m,k} \left(\varepsilon^2 |\hat{h}_{m,k}|^2 \!+\! (1\!-\!\varepsilon^2) |e_{m,k}|^2\right)},$$



The resource allocation problem

$$\max_{\{x_{m,k}\} \{p_m^c\} \{p_k^d\}} \sum_{m=1}^M B \log_2(1 + \gamma_m^c)$$
s.t.
$$\gamma_m^c \ge \gamma_{min}^c, \forall m \in \mathcal{M},$$

$$\Pr\left\{\gamma_k^d \ge \gamma_{min}^d\right\} \ge 1 - \epsilon, \forall k \in \mathcal{K},$$

$$\sum_{k=1}^K x_{m,k} \le 1, x_{m,k} \in \{0,1\}, \forall m \in \mathcal{M},$$

$$\sum_{m=1}^M x_{m,k} \le 1, \forall k \in \mathcal{K},$$

$$0 \le p_m^c \le P_{max}^c, \forall m \in \mathcal{M}$$

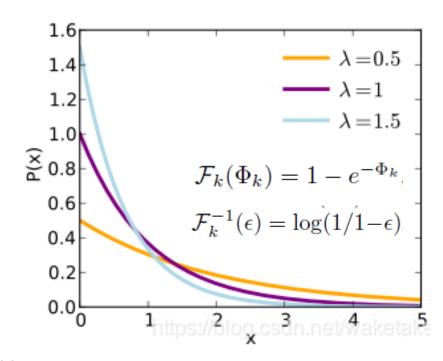
$$0 \le p_k^d \le P_{max}^d, \forall k \in \mathcal{K},$$

Decompose into power allocation subproblem and spectrum allocation subproblem.

$$\begin{split} C_{m,k} &= \max_{\{p_m^c\}\{p_k^d\}} B \log_2 \left(1 + \frac{p_m^c g_m^c}{\sigma^2 + p_k^d g_k^B}\right) \\ \text{s.t.} \quad & \Pr\left\{\frac{\Theta_k^d + \Lambda_k^d X}{\Phi_{m,k} + \Omega_{m,k} Y} \leq \gamma_{min}^d\right\} \leq \epsilon, \\ & \frac{p_m^c g_m^c}{\sigma^2 + p_k^d g_k^B} \geq \gamma_{min}^c, \\ & 0 \leq p_m^c \leq P_{max}^c, 0 \leq p_k^d \leq P_{max}^d, \end{split}$$

where $\Theta_k^d = p_k^d \alpha_k^d \varepsilon^2 |\hat{h}_k^d|^2$, $\Lambda_k^d = p_k^d \alpha_k^d (1 - \varepsilon^2)$, $\Phi_{m,k} = \sigma^2 + p_m^c \alpha_{m,k} \varepsilon^2 |\hat{h}_{m,k}|^2$ and $\Omega_{m,k} = p_m^c \alpha_{m,k} (1 - \varepsilon^2)$. Both $X = |e_k^d|^2$ and $Y = |e_{m,k}|^2$ are exponential random variables with unit mean.





 $\mathcal{F}_k(\cdot)$ is the cumulative distribution function (CDF)

$$\begin{aligned} & \text{outage}_k \ = \mathbb{E}\left[\mathcal{F}_k(\Psi_k)\right] \leq \mathcal{F}_k(\mathbb{E}[\Psi_k]) \\ & = \mathcal{F}_k\left(\frac{\gamma_{min}^d(\Phi_{m,k} + \Omega_{m,k}\mathbb{E}[Y]) - \Theta_k^d}{\Lambda_k^d}\right) = \mathcal{F}_k(\Phi_k), \end{aligned}$$

The QoS requirement can further be given as

$$outage_k \leq \mathcal{F}_k(\Phi_k) \leq \epsilon$$
.

The QoS requirement is

$$\Phi_k \le \mathcal{F}_k^{-1}(\epsilon) \Rightarrow \frac{\Theta_k^d + \Lambda_k^d \mathcal{F}_k^{-1}(\epsilon)}{\Phi_{m,k} + \Omega_{m,k}} \ge \gamma_{min}^d.$$

Obtain the solution

$$\frac{p_k^d \hat{g}_k^d}{\sigma^2 + p_m^c \hat{g}_{m,k}} \ge \gamma_{min}^d,$$



V2I QoS Constraint

$$\frac{p_m^c g_m^c}{\sigma^2 + p_k^d g_k^B} \ge \gamma_{min}^c,$$

V2V QoS Constraint

$$\frac{p_k^d \hat{g}_k^d}{\sigma^2 + p_m^c \hat{g}_{m,k}} \ge \gamma_{min}^d$$

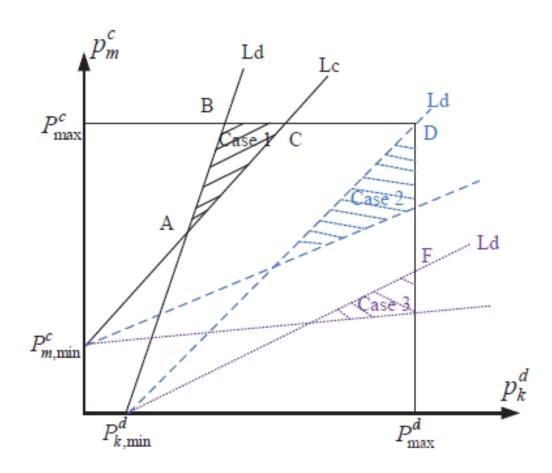
The optimal solution can be obtained

$$(p_m^{c,*}, p_k^{d,*}) = \underset{(p_m^c, p_k^d) \in \Omega}{\arg\max} \left\{ \log_2 \left(1 + \frac{p_m^c g_m^c}{\sigma^2 + p_k^d g_k^B} \right) \right\}$$

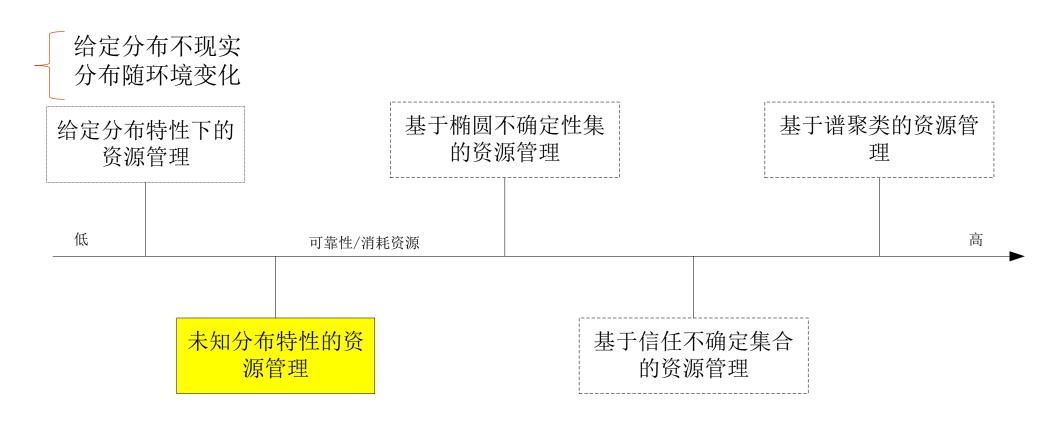
where

$$\Omega = \begin{cases} \{(P^{d}_{c,max}, P^{c}_{max})\}, \text{if} \frac{P^{d}_{max}\hat{g}^{d}_{k}}{P^{c}_{max}\hat{g}_{m,k} + \sigma^{2}} > \gamma^{d}_{min} \\ \{(P^{d}_{max}, P^{c}_{max})\}, \quad \text{if} \frac{P^{d}_{max}\hat{g}^{d}_{k}}{P^{c}_{max}\hat{g}_{m,k} + \sigma^{2}} = \gamma^{d}_{min} \\ \{(P^{d}_{max}, P^{c}_{d,max})\}, \text{if} \frac{P^{d}_{max}\hat{g}^{d}_{m,k} + \sigma^{2}}{P^{c}_{max}\hat{g}_{m,k} + \sigma^{2}} < \gamma^{d}_{min} \end{cases}$$

Feasible region of power control problem









Collect multiple samples of the uncertain CSI

$$\mathcal{D} = \{\xi_1, \xi_2, \cdots, \xi_N\}$$

The first-order moment of uncertain CSI

$$\bar{\mathbf{g}} = \frac{1}{N} \sum_{k=1}^{N} \xi_k.$$

The second-order moment

$$\Sigma = \frac{1}{N-1} \left[\sum_{i=1}^{N-1} \xi_i \xi_i^T - \frac{1}{N-1} \left(\sum_{i=1}^{N} \xi_i \right) \left(\sum_{i=1}^{N} \xi_i \right)^T \right]$$

The QoS constraint reformulated as distributionally robust constraint

$$\inf_{\mathbb{P}\in\mathcal{P}_{\mathcal{G}}} \mathbb{P}\left(\frac{p_k^d g_k^d}{\sigma^2 + p_m^c g_{m,k}} \ge \gamma_{min}^d\right) \ge 1 - \epsilon.$$

Deterministic Optimization

$$\inf_{\mathbf{x}} f(\mathbf{x}, \boldsymbol{\xi})$$

s.t. $\mathbf{x} \in X$

Stochastic Programming

$$\inf_{\mathbf{x}} \, \mathbb{E}_{\mathbb{P}} \{ f(\mathbf{x}, \boldsymbol{\xi}) \}$$

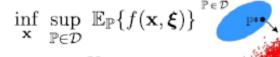
s.t. $\mathbf{x} \in X$



Robust Optimization

$$\inf_{\mathbf{x}} \sup_{\boldsymbol{\xi} \in U} f(\mathbf{x}, \boldsymbol{\xi})$$

DR Optimization



s.t. $\mathbf{x} \in X$



The feasible set of chance constraint

$$\left\{p_m^c, p_k^d \in \mathbb{R}^+ : \inf_{\mathbb{P} \in \mathcal{P}_{\mathcal{G}}} \mathbb{P}\left(\frac{p_k^d g_k^d}{\sigma^2 + p_m^c g_{m,k}} \! \geq \! \gamma_{min}^d\right) \! \geq \! 1 - \epsilon\right\}$$



(CVaR) conditional expectation for evaluating the loss above the $(1 - \epsilon)$ -quantile of the loss distribution.

$$\mathbb{P}\text{-CVaR}(L(\mathbf{g})) = \inf_{\beta \in \mathbb{R}} \left\{ \beta + \frac{1}{\epsilon} \mathbb{E}_{\mathbb{P}} \left[(L(\mathbf{g}) - \beta)^+ \right] \right\}$$

Define the loss function as
$$\left(\frac{p_k^d g_k^d}{\sigma^2 + p_m^c g_{m,k}} \! \ge \! \gamma_{min}^d \right)$$

$$L(\mathbf{g}) = \sigma^2 \gamma_{min}^d + \gamma_{min}^d p_m^c g_{m,k} - p_k^d g_k^d.$$

The solution can be obtained

$$\sup_{\mathbb{P}\in\mathcal{P}_{\mathcal{G}}} \mathbb{P}\text{-CVaR}_{\epsilon} \left(L(\mathbf{g})\right) \leq 0 \Rightarrow$$

$$\inf_{\mathbb{P}\in\mathcal{P}_{\mathcal{G}}} \mathbb{P} \left(\frac{p_k^d g_k^d}{\sigma^2 + p_m^c g_{m,k}} \geq \gamma_{min}^d\right) \geq 1 - \epsilon.$$

$$\sup_{\mathbb{P}\in\mathcal{P}_{\mathcal{G}}}\mathbb{P}\text{-CVaR}_{\epsilon}\left(L(\mathbf{g})\right)$$

$$= \sup_{\mathbb{P} \in \mathcal{P}_{\mathcal{G}}} \inf_{\beta \in \mathbb{R}} \left\{ \beta + \frac{1}{\epsilon} \mathbb{E}_{\mathbb{P}} \left[(L(\mathbf{g}) - \beta)^{+} \right] \right\}$$
$$= \inf_{\beta \in \mathbb{R}} \left\{ \beta + \frac{1}{\epsilon} \sup_{\mathbb{P} \in \mathcal{P}_{\mathcal{G}}} \mathbb{E}_{\mathbb{P}} \left[(L(\mathbf{g}) - \beta)^{+} \right] \right\},$$

Lemma 1: Suppose that $f: \mathbb{R}^2 \to \mathbb{R}$ is a measurable function and define the worst-case expectation as $\varpi = \sup_{\mathbb{P} \in \mathcal{P}} \mathbb{E}_{\mathbb{P}} [(f(\mathbf{g}))^+]$, where \mathcal{P} represents the usual set of all probability distributions on \mathbb{R}^2 with given mean \bar{g} and covariance matrix Σ . Then

$$arpi = \inf_{\mathbf{M} \in \mathbb{S}^3} \left\{ \langle \Omega, \mathbf{M}
angle : \mathbf{M} \succeq \mathbf{0}, \left[\mathbf{g}^T \ \mathbf{1}
ight] \mathbf{M} \left[\mathbf{g}^T \ \mathbf{1}
ight]^T \geq f(\mathbf{g}), orall \mathbf{g} \in \mathbb{R}^2
ight\}$$

where

$$\Omega = \left[egin{array}{cc} \Sigma + ar{\mathbf{g}}ar{\mathbf{g}}^T & ar{\mathbf{g}} \ ar{\mathbf{g}}^T & 1 \end{array}
ight]$$

is the second-order moment matrix of g.



The CVaR is computed as

$$\begin{split} \sup_{\mathbb{P} \in \mathcal{P}_{\mathcal{G}}} \mathbb{P}\text{-CVaR}_{\epsilon} \; (L(\mathbf{g})) &= \min_{\beta, \mathbf{M}} \beta + \frac{1}{\epsilon} \text{Tr}(\Omega^T \mathbf{M}) \\ \text{s.t.} \beta \in \mathbb{R}, \mathbf{M} \in \mathbb{S}^3, \mathbf{M} - \Phi \succeq \mathbf{0}, \end{split}$$

The power allocation problem can be reformulated as the following optimization problem

$$C_{m,k} = \max_{\{p_m^c\}, \{p_k^d\}, \beta, \mathbf{M}} B \log_2 \left(1 + \frac{p_m^c g_m^c}{\sigma^2 + p_k^d g_k^B} \right)$$
s.t.
$$\beta + \frac{1}{\epsilon} \text{Tr}(\mathbf{\Omega}^T \mathbf{M}) \le 0,$$

$$\beta \in \mathbb{R}, \mathbf{M} \in \mathbb{S}^3, \mathbf{M} - \Phi \succeq 0,$$
(7d).

Algorithm 2 Bisection Search for Solving Problem (37)

```
Set termination threshold 0 < \zeta < 1;
Set p_{k,min}^d = 0 and p_{k,max}^d = P_{max}^d;
while p_k^d < P_{max}^d - \zeta do
   set p_k^d = (p_{k,min}^d + p_{k,max}^d)/2; Solve (38) to obtain p_m^c;
   \begin{array}{l} \text{if } p_m^c > P_{max}^c + \zeta \text{ then} \\ p_{k,max}^d = p_k^d \end{array}
   else if p_m^c < P_{max}^c - \zeta then
   else if P_{max}^c - \zeta < p_m^c < P_{max}^c + \zeta then
       break
   end if
end while
```

Output the optimal transmit powers $p_m^{c,*}$ and $p_k^{d,*}$.

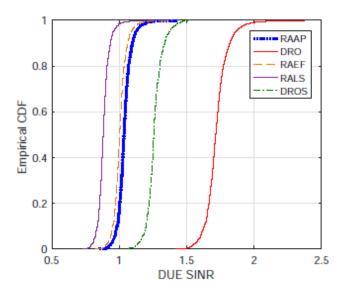


Fig. 4. V2V feasibility probability under the target SINR, assuming $\gamma^c=2$, $\gamma^d=1$, vehicle speed v=100km/h and $P^c_{max}=P^d_{max}=30$ dBm.



Collect multiple samples of the uncertain CSI

$$\mathcal{D} = \{\boldsymbol{\xi}_1, \boldsymbol{\xi}_2, \cdots, \boldsymbol{\xi}_N\}$$

The support *s* > 0 can be estimated as

$$s = \max_{1 \le i \le N} (\boldsymbol{\xi}_i - \bar{\mathbf{g}})^T \boldsymbol{\Sigma}^{-1} (\boldsymbol{\xi}_i - \bar{\mathbf{g}}).$$

Rewrite the uncertainty set *S* as the following semi-infinite constraint

$$(\mathbf{g} - \bar{\mathbf{g}})^T \mathbf{\Sigma}^{-1} (\mathbf{g} - \bar{\mathbf{g}}) \le s \Leftrightarrow$$

$$\begin{bmatrix} \mathbf{g} \\ 1 \end{bmatrix}^T \begin{bmatrix} \mathbf{\Sigma}^{-1} & -\mathbf{\Sigma}^{-1} \bar{\mathbf{g}} \\ -\bar{\mathbf{g}}^T \mathbf{\Sigma}^{-1} & \bar{\mathbf{g}}^T \mathbf{\Sigma}^{-1} \bar{\mathbf{g}} - s \end{bmatrix} \begin{bmatrix} \mathbf{g} \\ 1 \end{bmatrix} \le 0.$$

Lemma 2. Suppose $f_i(\mathbf{g}) = \mathbf{g}^T \mathbf{A}_i \mathbf{g}$ with $\mathbf{A}_i \in \mathbb{S}^3$ be quadratic functions of $\mathbf{g} \in \mathbb{R}^3$ for $i = 0, \dots, p$. Then, $f_0(\mathbf{g}) \geq 0$ for all \mathbf{g} with $f_i(\mathbf{g}) \leq 0, i = 1, \dots p$ if there exists constants $\tau_i \geq 0$ such that

$$\mathbf{A}_0 + \sum_{i=1}^p \tau_i \mathbf{A}_i \succeq \mathbf{0}. \tag{44}$$

QoS constraint condition

$$\begin{split} \sup_{\mathbb{P} \in \mathcal{P}_{\mathcal{G}}} \mathbb{P}\text{-CVaR}_{\epsilon} \ (L(\mathbf{g})) &= \min_{\beta, \mathbf{M}} \beta + \frac{1}{\epsilon} \mathrm{Tr}(\Omega^T \mathbf{M}) \\ \mathrm{s.t.} \beta \in \mathbb{R}, \mathbf{M} \in \mathbb{S}^3, \mathbf{M} - \Phi \succeq \mathbf{0}, \end{split}$$

The QoS constraint is transformed into

$$\begin{split} \sup_{\mathbb{P} \in \mathcal{P}_{\mathcal{G}}} \mathbb{P}\text{-CVaR}_{\epsilon}(L(\mathbf{g})) &= \min_{\beta, \mathbf{M}, \tau^{1}, \tau^{0}} \beta + \frac{1}{\epsilon} \text{Tr}(\mathbf{\Omega}^{T} \mathbf{M}) \\ \text{s.t. } \beta \in \mathbb{R}, \mathbf{M} \in \mathbb{S}^{3}, \\ \mathbf{M} + \tau^{1} \mathbf{W} - \mathbf{\Phi} \succeq \mathbf{0}, \\ \mathbf{M} + \tau^{0} \mathbf{W} \succeq \mathbf{0}, \tau^{1}, \tau^{0} \geq 0, \end{split}$$

The power control problem

$$C_{m,k} = \max_{\{p_{pm}^c\}, \{p_k^d\}, \beta, \mathbf{M}, \tau^1, \tau^0} B \log_2 \left(1 + \frac{p_m^c g_m^c}{\sigma^2 + p_k^d g_k^B} \right)$$
s.t.
$$\beta + \frac{1}{\epsilon} \text{Tr}(\mathbf{\Omega}^T \mathbf{M}) \le 0,$$

$$\beta \in \mathbb{R}, \mathbf{M} \in \mathbb{S}^3,$$

$$\mathbf{M} + \tau^1 \mathbf{W} - \mathbf{\Phi} \succeq \mathbf{0},$$

$$\mathbf{M} + \tau^0 \mathbf{W} \succeq \mathbf{0}, \tau^1, \tau^0 \ge 0,$$



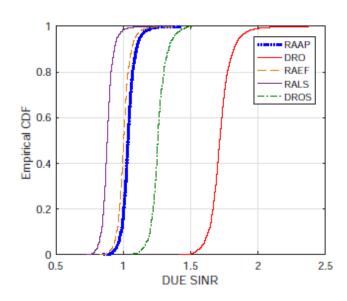


Fig. 4. V2V feasibility probability under the target SINR, assuming $\gamma^c=2$, $\gamma^d=1$, vehicle speed v=100km/h and $P^c_{max}=P^d_{max}=30$ dBm.

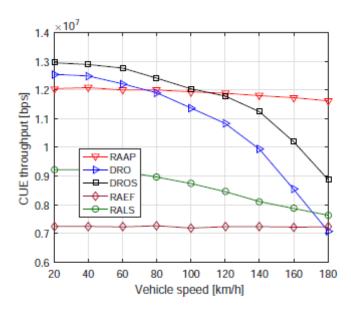


Fig. 9. CUE throughput versus the vehicle speed, assuming $\gamma^c=2,$ $\gamma^d=1$ and $P^c_{max}=P^d_{max}=30$ dBm.

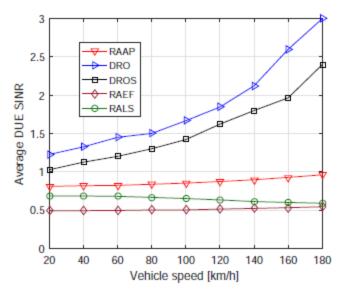
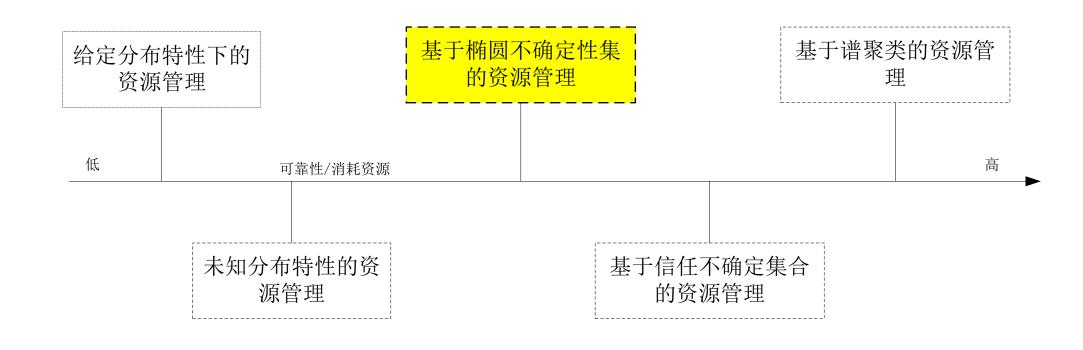


Fig. 10. Average DUE SINR versus the vehicle speed, assuming $\gamma^c=2$, $\gamma^d=1$ and $P^c_{max}=P^d_{max}=30$ dBm.

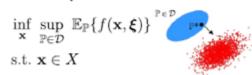




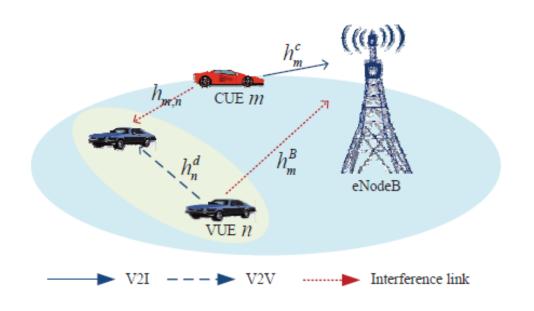
Robust Optimization

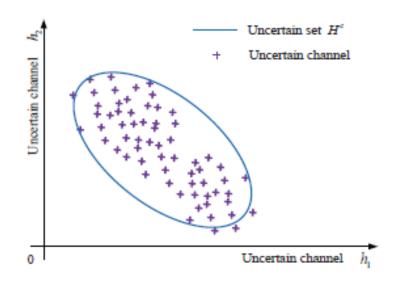
 $\inf_{\mathbf{x}} \sup_{\boldsymbol{\xi} \in U} f(\mathbf{x}, \boldsymbol{\xi})$ s.t. $\mathbf{x} \in X$

DR Optimization









Ultra-reliable communications constraint

$$\Pr\left\{\gamma_n^d \ge \gamma_{req}^d\right\} \ge 1 - \epsilon,$$

We use ellipsoid sets to model the uncertainties of the channel realizations

$$\mathcal{H}^c = \{\mathbf{h}^c : \mathbf{h}^c = \bar{\mathbf{h}}^c + \mathbf{B}^c \mathbf{u}, \mathbf{u}^T \mathbf{u} \le 1\},$$

$$\mathcal{H}^c = \{\mathbf{h}^c : (\mathbf{h}^c - \bar{\mathbf{h}}^c)^T \mathbf{\Sigma}^{-1} (\mathbf{h}^c - \bar{\mathbf{h}}^c) \le s_c\},$$



Collect multiple samples of the uncertain CSI

$$\mathcal{D} = \{\xi_1, \xi_2, \cdots, \xi_N\}$$

1) Shape Learning

The center is

$$\bar{\mathbf{h}}^c = \frac{1}{D_1} \sum_{k=1}^{D_1} \boldsymbol{\xi}_k,$$

The correlation between each element is

$$oldsymbol{\Sigma} = \left[egin{array}{ccc} oldsymbol{\Sigma}_1 & & & & \ & \ddots & & \ & & oldsymbol{\Sigma}_M \end{array}
ight]$$

$$\Sigma_{m}^{i,j} = \frac{1}{D_{1}} \sum_{k=1}^{D_{1}} (\boldsymbol{\xi}_{k}^{2(m-1)+i} - \bar{\mathbf{h}}_{2(m-1)+i}^{c})^{T} (\boldsymbol{\xi}_{k}^{2(m-1)+j} - \bar{\mathbf{h}}_{2(m-1)+j}^{c})$$

2) Size Calibration:

$$t(\boldsymbol{\xi}) = (\boldsymbol{\xi} - \bar{\mathbf{h}}^c)^T \boldsymbol{\Sigma}^{-1} (\boldsymbol{\xi} - \bar{\mathbf{h}}^c)$$

Then, the $k* = \lceil (1-\delta)D2 \rceil$ -th values $t(1) \le \cdots \le t(D-D1)$ in ascending order is the upper bound of $(1-\delta)$ -quantile

$$\mathcal{H}^c = \{\mathbf{h}^c : \mathbf{h}^c = \bar{\mathbf{h}}^c + \mathbf{B}^c \mathbf{u}, \mathbf{u}^T \mathbf{u} \le 1\},\$$

The QoS constraint can be computed as

min
$$\mathbf{p}^c \mathbf{h}^c \ge \sigma^c$$
,
s.t. $\mathbf{h}^c = \bar{\mathbf{h}}^c + \mathbf{B}^c \mathbf{u}, \mathbf{u}^T \mathbf{u} \le 1$,

The robust counterpart is

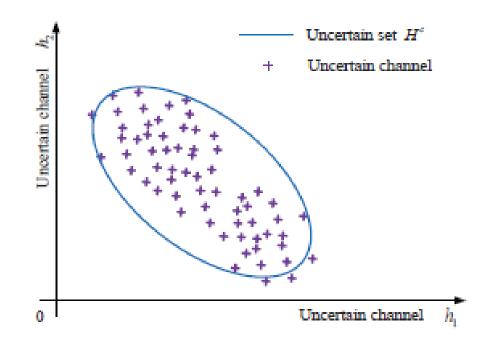
$$\mathbf{p}^{d}\mathbf{h}^{d} \geq \boldsymbol{\sigma}, \mathbf{h}^{d} = \bar{\mathbf{h}}^{d} + \mathbf{B}^{d}\mathbf{u}, \mathbf{u}^{T}\mathbf{u} \leq 1$$

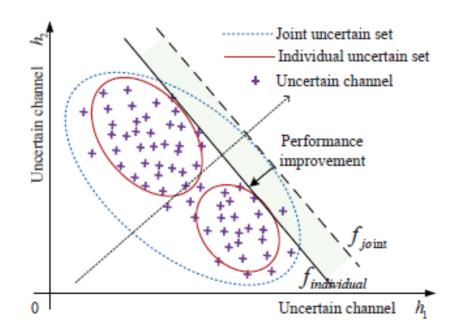
$$\Leftrightarrow \inf_{\|\mathbf{u}\| \leq 1} \mathbf{p}^{d}(\bar{\mathbf{h}}^{d} + \mathbf{B}^{d}\mathbf{u}) = \mathbf{p}^{d}\bar{\mathbf{h}}^{d} - \|\mathbf{p}^{d}\mathbf{B}^{d}\|.$$



The robust counterpart is

$$\begin{aligned} & \min \quad w_1 \sum_m p_m^c + w_2 \sum_n p_n^d \\ & \text{s.t.} \quad \mathbf{p}^c \bar{\mathbf{h}}^c - \|\mathbf{p}^c \mathbf{B}^c\| \geq \sigma^c, \\ & \mathbf{p}^d \bar{\mathbf{h}}^d - \|\mathbf{p}^d \mathbf{B}^d\| \geq \sigma^d, \\ & (4\mathbf{d}), (4\mathbf{e}), \end{aligned}$$







Collect multiple samples of the uncertain CSI

$$\mathcal{D} = \{\boldsymbol{\xi}_1, \boldsymbol{\xi}_2, \cdots, \boldsymbol{\xi}_N\}$$

1) Shape Learning

The center is

$$ar{\eta}_m^c = rac{1}{D_1} \sum_{k=1}^{D_1} \xi_k^m \quad ext{and} \quad ar{arphi}_n^d = rac{1}{T_1} \sum_{k=1}^{T_1} m{ heta}_k^n,$$

The correlation between each element is

$$\mathbf{\Sigma}_m = \left[egin{array}{ccc} \Sigma^{1,1} & \Sigma^{1,2} \ \Sigma^{2,1} & \Sigma^{2,2} \end{array}
ight], \mathbf{\Lambda}_n = \left[egin{array}{ccc} \Lambda^{1,1} & \Lambda^{1,2} \ \Lambda^{2,1} & \Lambda^{2,2} \end{array}
ight],$$

2) Size Calibration:

$$t_{\boldsymbol{\xi}}(\boldsymbol{\xi}) = \max_{m=1,\cdots,M} (\boldsymbol{\xi}_m - \bar{\boldsymbol{\eta}}_m^c)^T \boldsymbol{\Sigma}_m^{-1} (\boldsymbol{\xi}_m - \bar{\boldsymbol{\eta}}_m^c),$$

Robust optimization problem

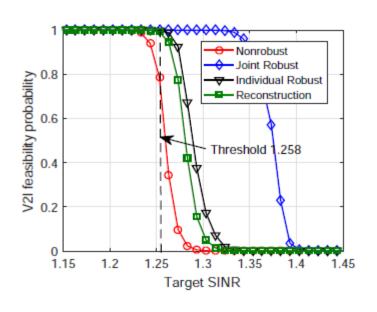
min
$$w_1 p_m^c + w_2 p_n^d$$

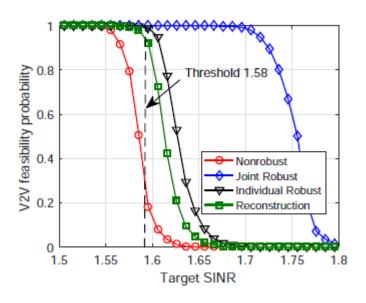
s.t. $\mathbf{p}_m^c \boldsymbol{\eta}_m^c \ge \sigma^2, \boldsymbol{\eta}_m^c = \bar{\boldsymbol{\eta}}_m^c + \mathbf{B}_m^c \boldsymbol{\mu}, \boldsymbol{\mu}^T \boldsymbol{\mu} \le 1,$
 $\mathbf{p}_n^d \boldsymbol{\varphi}_n^d \ge \sigma^2, \boldsymbol{\varphi}_n^d = \bar{\boldsymbol{\varphi}}_n^d + \mathbf{B}_n^d \boldsymbol{\mu}, \boldsymbol{\mu}^T \boldsymbol{\mu} \le 1,$
(29d), (29e).

The robust counterpart can be written as

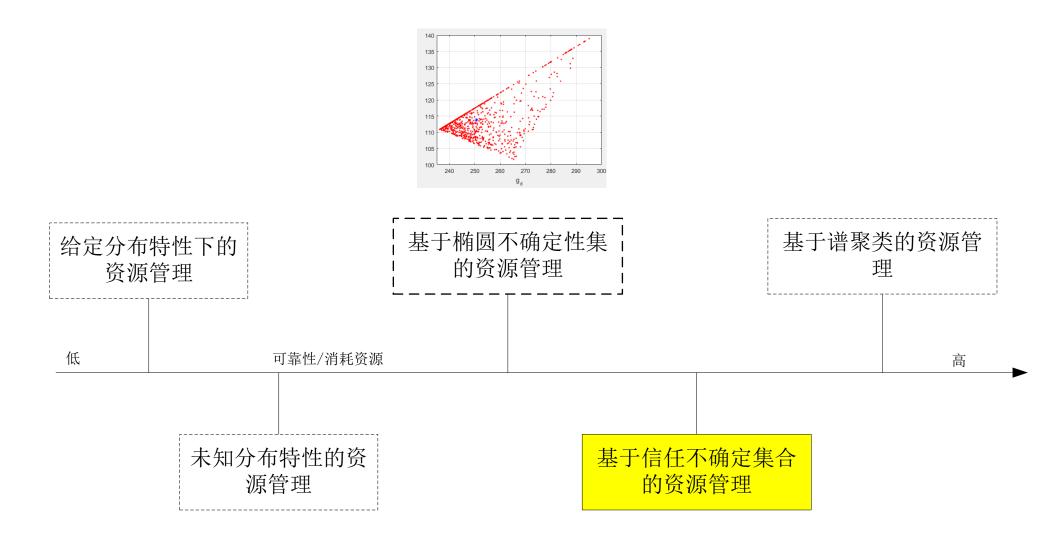
min
$$w_1 p_m^c + w_2 p_n^d$$

s.t. $\mathbf{p}_m^c \bar{\eta}_m^c - \|\mathbf{p}_m^c \mathbf{B}_m^c\| \ge \sigma^2$,
 $\mathbf{p}_n^d \bar{\varphi}_n^d - \|\mathbf{p}_n^d \mathbf{B}_n^d\| \ge \sigma^2$,
(29d), (29e).











基于信任不确定集的资源管理

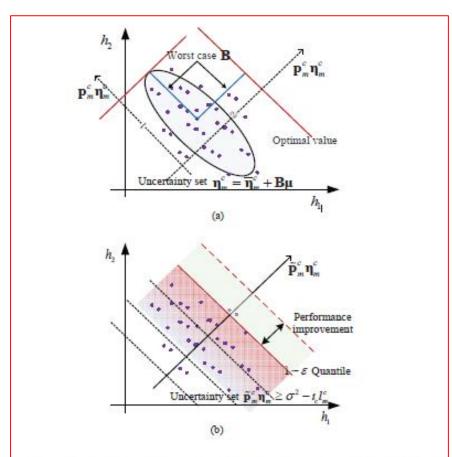


Fig. 4. Performance improvement through reconstructing the ellipsoid set as an affine set. $\mathbf{p}_m^c \eta_m^c$ is the possible increasing direction of the network performance. B indicates the worst case of CSI error. $\tilde{\mathbf{p}}_m^c \eta_m^c$ is the reliable increasing direction of the network performance. $\tilde{\mathbf{p}}_m^c \eta_m^c \geq \sigma^2 - \iota_c l_m^c$ is the uncertainty set constructed along the reliable increasing direction.

The QoS constraint

$$\gamma_m^c \geq \gamma_{req}^c \Rightarrow \frac{p_m^c h_m^c}{\gamma_{req}^c} - p_n^d h_n^B \geq \sigma^2, \forall m. \quad \mathcal{H}_m^c = \{\eta_m^c | \tilde{\mathbf{p}}_m^c \eta_m^c \geq \sigma^2 - \iota_c l_m^c \},$$

The values is calibrated by letting

$$t_{\boldsymbol{\xi}}(\boldsymbol{\xi}) = \max_{m=1,\dots,M} \left\{ \left(\sigma^2 - \tilde{\mathbf{p}}_m^c \boldsymbol{\xi}_m \right) / l_m^c \right\},\,$$

Robust counterpart

$$\begin{array}{lll} \min \limits_{\boldsymbol{\varphi}_n^d} & \mathbf{p}_n^d \boldsymbol{\varphi}_n^d & \max & y_n^d (\sigma^2 - \iota_d l_n^d) \\ \mathrm{s.t.} & \tilde{\mathbf{p}}_n^d \boldsymbol{\varphi}_n^d \geq \sigma^2 - \iota_d l_n^d. & \mathrm{s.t.} & y_n^d \tilde{\mathbf{p}}_n^d \leq \mathbf{p}_n^d, y_n^d \geq 0 \end{array}$$

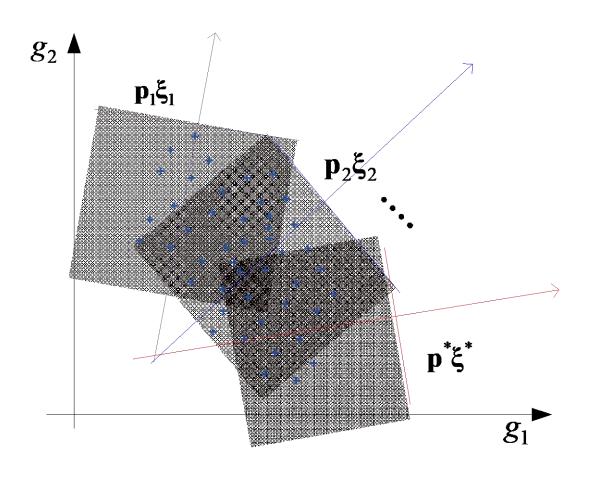
Robust problem

min
$$w_1 p_m^c + w_2 p_n^d$$

s.t. $y_m^c (\sigma^2 - \iota_c l_m^c) \ge \sigma^2$,
 $y_m^c \tilde{\mathbf{p}}_m^c \le \mathbf{p}_m^c, y_m^c \ge 0$,
 $y_n^d (\sigma^2 - \iota_d l_n^d) \ge \sigma^2$,
 $y_n^d \tilde{\mathbf{p}}_n^d \le \mathbf{p}_n^d, y_n^d \ge 0$,



基于信任不确定集的资源管理



The values is calibrated by letting

$$t_{\xi}(\xi) = \max_{m=1,\dots,M} \left\{ \left(\sigma^2 - \tilde{\mathbf{p}}_m^c \xi_m \right) / l_m^c \right\},\,$$

Robust counterpart

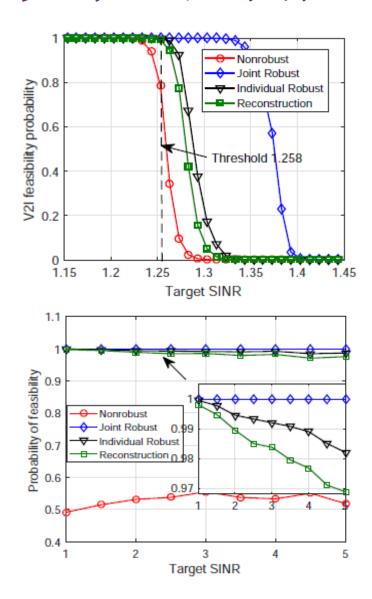
$$\begin{array}{lll} \min \limits_{\boldsymbol{\varphi}_n^d} & \mathbf{p}_n^d \boldsymbol{\varphi}_n^d & \max & y_n^d (\sigma^2 - \iota_d l_n^d) \\ \mathrm{s.t.} & \tilde{\mathbf{p}}_n^d \boldsymbol{\varphi}_n^d \geq \sigma^2 - \iota_d l_n^d. & \mathrm{s.t.} & y_n^d \tilde{\mathbf{p}}_n^d \leq \mathbf{p}_n^d, y_n^d \geq 0 \end{array}$$

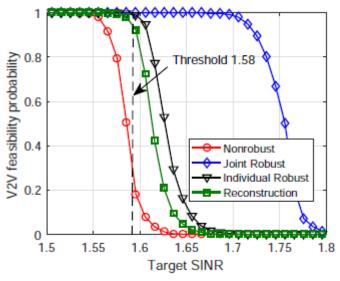
Robust problem

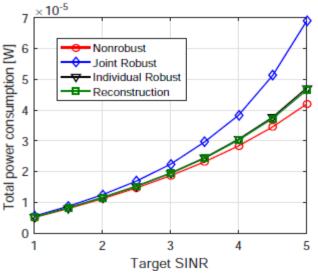
$$\begin{aligned} & \min \quad w_1 p_m^c + w_2 p_n^d \\ & \text{s.t.} \quad y_m^c (\sigma^2 - \iota_c l_m^c) \geq \sigma^2, \\ & y_m^c \tilde{\mathbf{p}}_m^c \leq \mathbf{p}_m^c, y_m^c \geq 0, \\ & y_n^d (\sigma^2 - \iota_d l_n^d) \geq \sigma^2, \\ & y_n^d \tilde{\mathbf{p}}_n^d \leq \mathbf{p}_n^d, y_n^d \geq 0, \end{aligned}$$



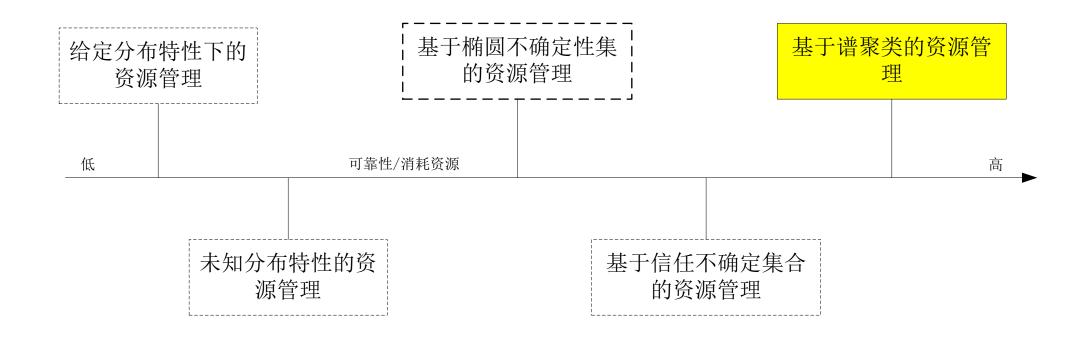
基于信任不确定集的资源管理



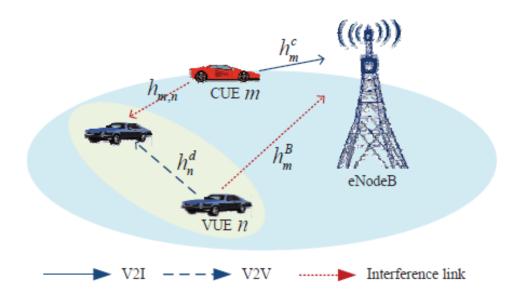












• Channel power gain

$$g_k^d = h_k^d \beta_k^d \varrho D_k^{-\iota} \triangleq |h_k^d|^2 \alpha_k^d,$$

• Small-scale channel gain

$$h = \varepsilon \hat{h} + \sqrt{1 - \varepsilon^2} e.$$

• SINR

$$\gamma_k^d = \frac{p_k^d \alpha_k^d \left(\varepsilon^2 |\hat{h}_k^d|^2 + (1 - \varepsilon^2) |e_k^d|^2 \right)}{\sigma^2 + \sum\limits_{m \in \mathcal{M}} x_{m,k} p_m^c \alpha_{m,k} \left(\varepsilon^2 |\hat{h}_{m,k}|^2 + (1 - \varepsilon^2) |e_{m,k}|^2 \right)},$$

• QoS requirements

$$\Pr\left\{\gamma_d \ge \gamma_{min}^d\right\} \ge \Pr\left\{\mathbf{g} \in \mathcal{G}\right\} \ge 1 - \epsilon,$$

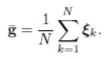


Symmetrical-geometry-based learning approach

> Polytope Model

$$\mathcal{P} = \{ \mathbf{g} | | g_d - \bar{g}_d | + | g_{c,d} - \bar{g}_{c,d} | \le \Gamma \},$$

1) Shape Learning:





2) Size Calibration:

$$t_p(\xi) = |\xi(1) - \bar{g}_d| + |\xi(2) - \bar{g}_{c,d}|$$

QoS constraint computed as

$$\begin{aligned} & \min \quad & \mathbf{p}^T \mathbf{g} \\ & \text{s.t.} \quad & \mathbf{M}_p(\mathbf{g} - \bar{\mathbf{g}}) \leq \mathbf{\Gamma}. \end{aligned}$$

Lagrange dual as

max
$$-(\mathbf{\Gamma} + \mathbf{M}_p \bar{\mathbf{g}})^T \mathbf{x}$$

s.t. $-\mathbf{M}_p^T \mathbf{x} \leq \mathbf{p}, \mathbf{x} \geq 0$,

Robust counterpart

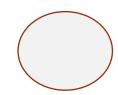
$$\begin{cases} -(\mathbf{\Gamma} + \mathbf{M}_p \bar{\mathbf{g}})^T \mathbf{x} \ge \gamma_{min}^d, \\ -\mathbf{M}_p^T \mathbf{x} \le \mathbf{p}, \mathbf{x} \ge 0. \end{cases}$$

Ellipsoidal

$$\mathcal{E} = \{ \mathbf{g} : (\mathbf{g} - \bar{\mathbf{g}})^T (\mathbf{g} - \bar{\mathbf{g}}) \le \Lambda \},$$

1) Shape Learning:

$$\bar{\mathbf{g}} = \frac{1}{N} \sum_{k=1}^{N} \boldsymbol{\xi}_k.$$



2) Size Calibration:

$$t_e(\boldsymbol{\xi}) = (\boldsymbol{\xi} - \bar{\mathbf{g}})^T (\boldsymbol{\xi} - \bar{\mathbf{g}})$$

QoS constraint computed as

$$\begin{aligned} & \min \quad & \mathbf{p}^T \mathbf{g} \\ & \text{s.t.} \quad & \mathbf{g} = \bar{\mathbf{g}} + \zeta \mathbf{u}, \mathbf{u}^T \mathbf{u} \leq 1. \end{aligned}$$

Since

$$\inf_{\|\mathbf{u}\| \le 1} \mathbf{p}^T (\bar{\mathbf{g}} + \zeta \mathbf{u}) = \mathbf{p}^T \bar{\mathbf{g}} - \zeta \| \mathbf{p}^T \|,$$

Robust counterpart

$$\mathbf{p}^T \bar{\mathbf{g}} - \zeta \|\mathbf{p}^T\| \ge \gamma_{min}^d,$$

> Box Uncertainty Set

$$\mathcal{B} = \{\mid \mathbf{g}(i) - \bar{\mathbf{g}}(i) \mid \leq \Psi, i = 1, 2\},\$$

1) Shape Learning:

$$\bar{\mathbf{g}} = \frac{1}{N} \sum_{k=1}^{N} \boldsymbol{\xi}_k.$$

2) Size Calibration:

$$t_b(\boldsymbol{\xi}_i) = \max_{i=1,2} |\boldsymbol{\xi}_i - \bar{\mathbf{g}}_i|$$

QoS constraint computed as

min
$$\mathbf{p}^T \mathbf{g}$$

s.t. $\mathbf{M}_b(\mathbf{g} - \bar{\mathbf{g}}) \leq \mathbf{\Psi}$.

Lagrange dual as

max
$$-(\boldsymbol{\Psi} + \mathbf{M}_b \bar{\mathbf{g}})^T \mathbf{y}$$

s.t. $-\mathbf{M}_b^T \mathbf{y} \leq \mathbf{p}, \mathbf{y} \geq 0$,

Robust counterpart

$$\begin{cases} -(\mathbf{\Psi} + \mathbf{M}_b \bar{\mathbf{g}})^T \mathbf{y} \ge \gamma_{min}^d \\ -\mathbf{M}_b^T \mathbf{y} \le \mathbf{p}, \mathbf{y} \ge 0. \end{cases}$$



> 功率分配问题

$$\max_{\mathbf{p}_{e}, \mathbf{p}_{d}} \quad B \log_{2} \left(1 + \frac{p_{e}g_{e}}{\sigma^{2} + p_{d}g_{d,B}} \right)$$
s.t.
$$\begin{cases} -(\Gamma + \mathbf{M}_{p}\bar{\mathbf{g}})^{T}\mathbf{x} \geq \gamma_{min}^{d}, \\ -\mathbf{M}_{p}^{T}\mathbf{x} \leq \mathbf{p}, \mathbf{x} \geq 0. \end{cases}$$

$$\mathbf{p}^{T}\bar{\mathbf{g}} - \zeta \|\mathbf{p}^{T}\| \geq \gamma_{min}^{d},$$

$$\begin{cases} -(\Psi + \mathbf{M}_{b}\bar{\mathbf{g}})^{T}\mathbf{y} \geq \gamma_{min}^{d}, \\ -\mathbf{M}_{b}^{T}\mathbf{y} \leq \mathbf{p}, \mathbf{y} \geq 0. \end{cases}$$

Algorithm 1 Bisection Search-Based Power Allocation

```
Set termination threshold 0 < \zeta < 1;

Set p_{k,min}^d = 0 and p_{k,max}^d = P_{max}^d;

while p_k^d < P_{max}^d - \zeta do

set p_k^d = (p_{k,min}^d + p_{k,max}^d)/2; Solve (30) to obtain p_m^c;

if p_m^c > P_{max}^c + \zeta then

p_{k,max}^d = p_k^d

else if p_m^c < P_{max}^c - \zeta then

p_{k,min}^d = p_k^d

else if P_{max}^c - \zeta < p_m^c < P_{max}^c + \zeta then

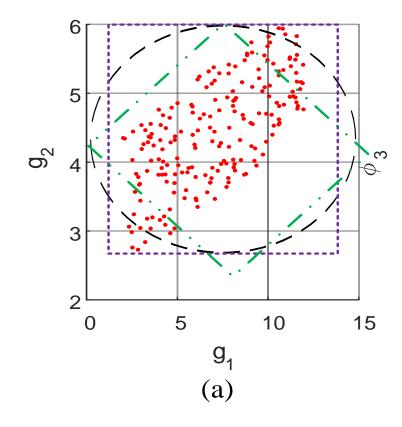
break

end if

end while

Output the optimal transmit powers p_m^{c,*} and p_k^{d,*}.
```

▶ 学习到的不确定性集合





- Use SVC to cover the uncertain CSI in high-dimensional space
 - Define nonlinear mapping

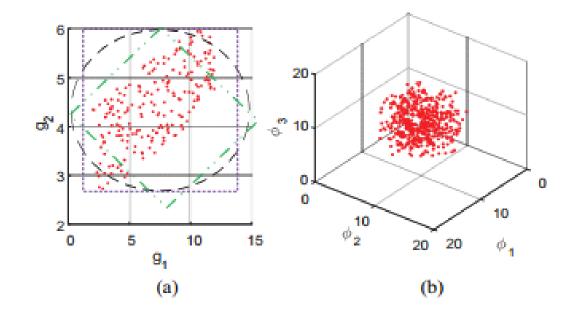
$$\phi(\boldsymbol{\xi}_i) : \mathbb{R}^2 \stackrel{\cdot}{\mapsto} \mathbb{R}^K$$

to map the CSI samples into a high-dimensional features

 seek the smallest sphere to enclose the CSI samples in high-dimensional features space

$$\min_{\substack{R, \rho, \{\psi_i\}}} R^2 + C \sum_{i=1}^{N} \psi_i$$
s.t. $\|\phi(\xi_i) - \rho\|^2 \le R^2 + \psi_i, i = 1, \dots, N,$

$$\psi_i \ge 0, i = 1, \dots, N,$$



set $C = 1/(\epsilon N)$ to control the sphere covering the CSI samples with $(1 - \epsilon) \times 100\%$ confidence.



> The dual problem is formulated as

$$\min_{\lambda} \sum_{i=1}^{N} \sum_{j=1}^{N} \lambda_i \lambda_j K(\boldsymbol{\xi}_i, \boldsymbol{\xi}_j) - \sum_{i=1}^{N} \lambda_i K(\boldsymbol{\xi}_i, \boldsymbol{\xi}_i)$$
s.t. $0 \le \lambda_i \le C, i = 1, \dots, N,$

$$\sum_{i=1}^{N} \lambda_i = 1,$$

KKT conditions

$$\begin{cases} \frac{\partial L}{\partial R} = 0 \to \sum_{i=1}^{N} \lambda_i = 1, \\ \frac{\partial L}{\partial \rho} = 0 \to \rho = \sum_{i=1}^{N} \lambda_i \phi(\xi_i), \\ \frac{\partial L}{\partial \psi_i} \to \lambda_i + \eta_i = C. \end{cases}$$

Obtain the following desirable geometric interpretations

$$\begin{cases} \|\phi(\xi_i) - \rho\|^2 < R^2 \to \lambda_i = 0, \eta_i = C, \\ \|\phi(\xi_i) - \rho\|^2 = R^2 \to 0 < \lambda_i < C, 0 < \eta_i < C, \\ \|\phi(\xi_i) - \rho\|^2 > R^2 \to \lambda_i = C, \eta_i = 0. \end{cases}$$

We give definitions of all support vectors and boundary support vectors

$$\mathcal{F} = \{i \mid \lambda_i > 0, \forall i\} \text{ and } \mathcal{B}_v = \{i \mid 0 < \lambda_i < C, \forall i\}$$

The radius of the sphere

$$R^{2} = \|\phi(\xi_{l}) - \rho\|^{2} = \|\phi(\xi_{l}) - \sum_{i=1}^{N} \lambda_{i} \phi(\xi_{i})\|^{2}$$
$$= K(\xi_{l}, \xi_{l}) - 2 \sum_{i=1}^{N} \lambda_{i} K(\xi_{l}, \xi_{i}) + \sum_{i=1}^{N} \sum_{i=1}^{N} \lambda_{i} \lambda_{j} K(\xi_{l}, \xi_{i})$$

The feasible set of uncertain CSI

$$S_{\epsilon}(\mathcal{N}) = \left\{ \mathbf{g} \mid K(\mathbf{g}, \mathbf{g}) - 2 \sum_{i=1}^{N} \lambda_{i} K(\mathbf{g}, \boldsymbol{\xi}_{i}) + \sum_{i=1}^{N} \sum_{j=1}^{N} \lambda_{i} \lambda_{j} K(\boldsymbol{\xi}_{i}, \boldsymbol{\xi}_{j}) \leq R^{2} \right\}$$

The kernel function plays a key role



Commonly used functions

Gaussian kernel:

$$K(\xi_i, \xi_j) = \exp(-q \|\xi_i - \xi_j\|^2)$$

Sigmoid kernel:

$$K(\boldsymbol{\xi}_i, \boldsymbol{\xi}_j) = \tanh(a \cdot \boldsymbol{\xi}_i^T \cdot \boldsymbol{\xi}_j + r)$$

Polynomial kernel:

$$K(\boldsymbol{\xi}_i,\boldsymbol{\xi}_j) = (\boldsymbol{\xi}_i^T \cdot \boldsymbol{\xi}_j + 1)^d$$

inevitably complicate the application in power allocation.

$$S_{\epsilon}(\mathcal{N}) = \left\{ \mathbf{g} \mid K(\mathbf{g}, \mathbf{g}) - 2 \sum_{i=1}^{N} \lambda_{i} K(\mathbf{g}, \boldsymbol{\xi}_{i}) + \sum_{i=1}^{N} \sum_{j=1}^{N} \lambda_{i} \lambda_{j} K(\boldsymbol{\xi}_{i}, \boldsymbol{\xi}_{j}) \leq R^{2} \right\}$$

Proposed kernel functions

$$K(\xi_i, \xi_j) = \sum_{k=1}^{2} \Xi_k - \|\mathbf{Q}(\xi_i - \xi_j)\|_1,$$

Q can be constructed as $Q = \Sigma^{-\frac{1}{2}}$,

$$\Sigma = \frac{1}{N-1} \left[\sum_{i=1}^{N-1} \xi_i \xi_i^T - \frac{1}{N-1} \left(\sum_{i=1}^{N} \xi_i \right) \left(\sum_{i=1}^{N} \xi_i \right)^T \right].$$

 Ξ_k is chosen as

$$\Pi_k > \max_{1 \le i \le N} \mathbf{q}_k^T \boldsymbol{\xi}_i - \min_{1 \le i \le N} \mathbf{q}_k^T \boldsymbol{\xi}_i.$$

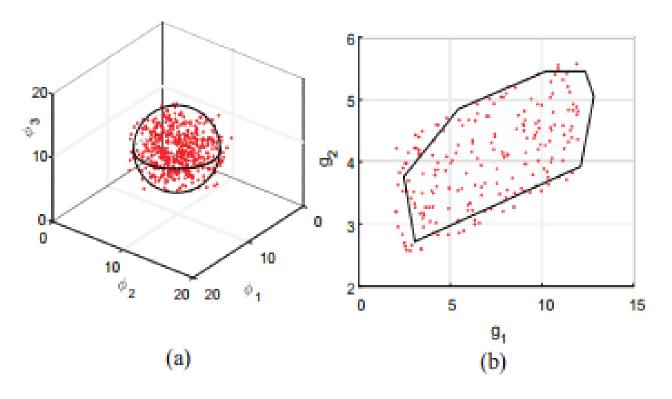


➤ The explicit expression of data-driven uncertainty set is represented as

$$S_{\epsilon}(\mathcal{N}) = \left\{ \mathbf{g} \left| \sum_{i \in \mathcal{F}} \lambda_{i} \| \mathbf{Q}(\mathbf{g} - \boldsymbol{\xi}_{i}) \|_{1} \leq \sum_{i \in \mathcal{F}} \lambda_{i} \| \mathbf{Q}(\boldsymbol{\xi}_{l} - \boldsymbol{\xi}_{i}) \|_{1}, l \in \mathcal{B}_{v} \right\} \right\}$$

let
$$\varrho = \sum_{i \in \mathcal{F}} \lambda_i \|\mathbf{\tilde{Q}}(\boldsymbol{\xi}_l - \boldsymbol{\xi}_i)\|_1, l \in \mathcal{B}_v$$

$$S_{\epsilon}(\mathcal{N}) = \left\{ \mathbf{g} \middle| \begin{array}{c} \exists \mathbf{v}_{i}, i \in \mathcal{F} \text{ s.t.} \\ \sum_{i \in \mathcal{F}} (\lambda_{i} \cdot \mathbf{v}_{i}^{T} \mathbf{1}_{2 \times 1}) \leq \varrho \\ -\mathbf{v}_{i} \leq \mathbf{Q}(\mathbf{g} - \boldsymbol{\xi}_{i}) \leq \mathbf{v}_{i}, i \in \mathcal{F} \end{array} \right\}.$$





The chance QoS constraint

$$\begin{aligned} & \min_{\mathbf{g}, \{\mathbf{v}_i\}} & \mathbf{p}^T \mathbf{g} \\ & \text{s.t.} & & \sum_{i \in \mathcal{F}} (\lambda_i \cdot \mathbf{v}_i^T \mathbf{1}_{2 \times 1}) \leq \varrho, \\ & & -\mathbf{v}_i \leq \mathbf{Q} (\mathbf{g} - \boldsymbol{\xi}_i) \leq \mathbf{v}_i, i \in \mathcal{F}. \end{aligned}$$

Dual problem

$$\begin{aligned} \max_{\kappa, \{\varphi_i\}, \{\omega_i\}} & & \sum_{i \in \mathcal{F}} (\omega_i - \varphi_i)^T \mathbf{Q} \boldsymbol{\xi}_i - \varrho \kappa \\ \text{s.t.} & & \sum_{i \in F} (\omega_i - \varphi_i)^T \mathbf{Q} - \mathbf{p} = \mathbf{0}, \\ & & \omega_i + \varphi_i - \lambda_i \cdot \kappa \cdot \mathbf{1} = \mathbf{0}, \forall i \in \mathcal{F}, \\ & & \kappa \geq 0, \varphi_i, \omega_i \in \mathbb{R}_+^2. \end{aligned}$$

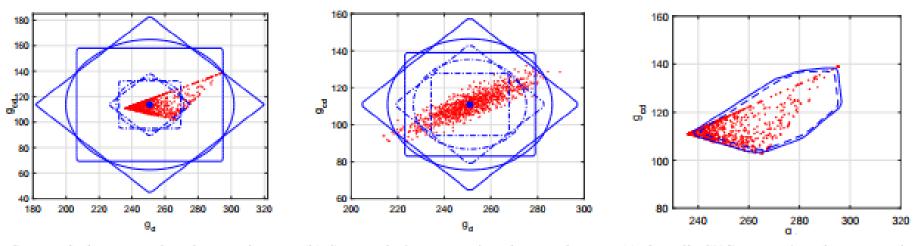
➤ The intractable chance constraint can be replaced by the following linear constraint

$$\begin{cases} \sum_{i \in \mathcal{F}} (\omega_i - \varphi_i)^T \mathbf{Q} \boldsymbol{\xi}_i - \varrho \kappa \geq \gamma_{min}^d, \\ \sum_{i \in \mathcal{F}} (\omega_i - \varphi_i)^T \mathbf{Q} - \mathbf{p} = \mathbf{0}, \\ \omega_i + \varphi_i - \lambda_i \cdot \kappa \cdot \mathbf{1} = \mathbf{0}, \forall i \in \mathcal{F}, \\ \kappa \geq 0, \varphi_i, \omega_i \in \mathbb{R}_+^2. \end{cases}$$

The power allocation problem

$$\max_{p_{e},p_{d}} B \log_{2} \left(1 + \frac{p_{c}g_{c}}{\sigma^{2} + p_{d}g_{d,B}} \right)$$
s.t.
$$\begin{cases} \sum_{i \in \mathcal{F}} (\omega_{i} - \varphi_{i})^{T} \mathbf{Q} \xi_{i} - \varrho \kappa \geq \gamma_{min}^{d}, \\ \sum_{i \in \mathcal{F}} (\omega_{i} - \varphi_{i})^{T} \mathbf{Q} - \mathbf{p} = \mathbf{0}, \\ \omega_{i} + \varphi_{i} - \lambda_{i} \cdot \kappa \cdot \mathbf{1} = \mathbf{0}, \forall i \in \mathcal{F}, \\ \kappa \geq 0, \varphi_{i}, \omega_{i} \in \mathbb{R}_{+}^{2}. \end{cases}$$





(a) Symmetrical-geometry-based uncertainty set (b) Symmetrical-geometry-based uncertainty set (c) Quantile-SVC approach under truncated exponential.

under gaussian.

ponential.

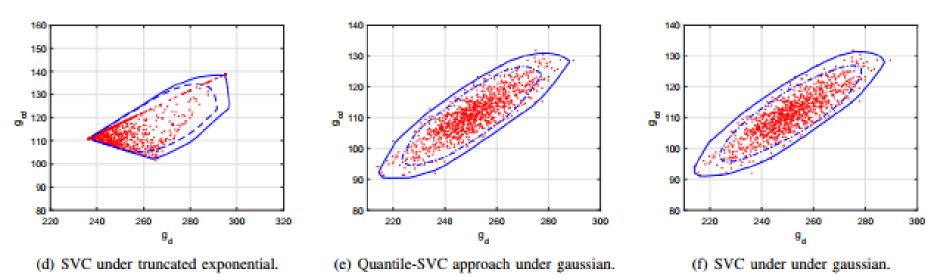


Fig. 4. Learning results of the uncertainty sets, where the solid line and the dotted line correspond to $\epsilon = 0.01$ and $\epsilon = 0.05$ respectively



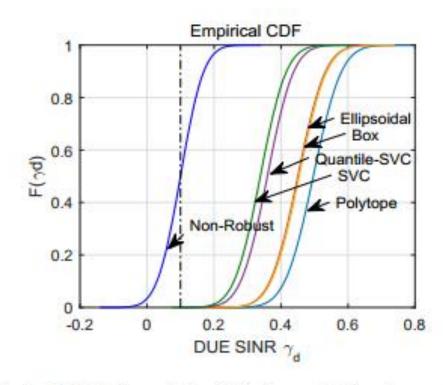


Fig. 7. DUE SINR cumulative distributions under Gaussian uncertainties, assuming $P^c_{max} = P^d_{max} = 20 \text{dBm}$, QoS requirements $\gamma^c_{min} = 5$, $\gamma^d_{min} = 0.1$ and outage probability $\epsilon = 0.05$.

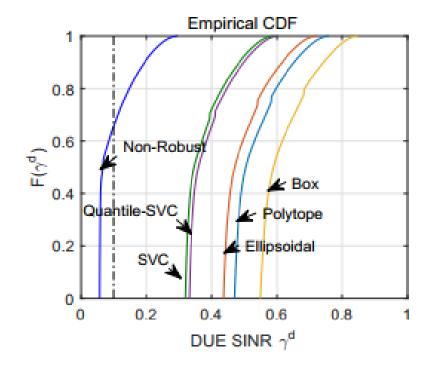


Fig. 8. DUE SINR cumulative distributions under exponential uncertainties, assuming $P^c_{max} = P^d_{max} = 20 \text{dBm}$, QoS requirements $\gamma^c_{min} = 5$, $\gamma^d_{min} = 0.1$ and outage probability $\epsilon = 0.05$.



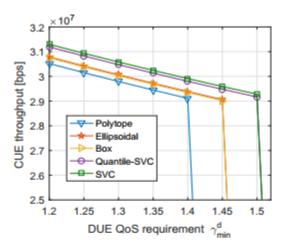


Fig. 11. CUE throughput versus DUE QoS requirement, assuming $P^c_{max} = P^d_{max} = 20$ dBm, CUE QoS requirement $\gamma^c_{min} = 5$ and outage probability $\epsilon = 0.05$.

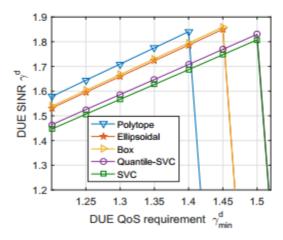


Fig. 12. DUE SINR versus DUE QoS requirement, assuming $P^c_{max}=P^d_{max}=20$ dBm, CUE QoS requirement $\gamma^c_{min}=5$ and outage probability $\epsilon=0.05$.

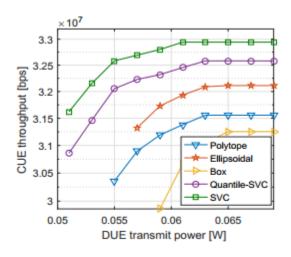


Fig. 13. CUE throughput versus DUE transmit power, assuming $P^c_{max}=20$ dBm, CUE QoS requirement $\gamma^c_{min}=5$, DUE QoS requirement $\gamma^c_{min}=1$ and outage probability $\epsilon=0.05$.

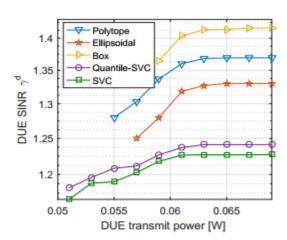


Fig. 14. DUE SINR versus DUE transmit power, assuming $P^c_{max}=20 {\rm dBm}$, CUE QoS requirement $\gamma^c_{min}=5$, DUE QoS requirement $\gamma^c_{min}=1$ and outage probability $\epsilon=0.05$.

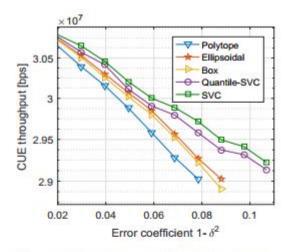


Fig. 15. CUE throughput versus channel estimation error coefficient, assuming $P^c_{max} = P^d_{max} = 20 \text{dBm}$, CUE QoS requirement $\gamma^c_{min} = 5$, DUE QoS requirement $\gamma^c_{min} = 1.5$ and outage probability $\epsilon = 0.05$.

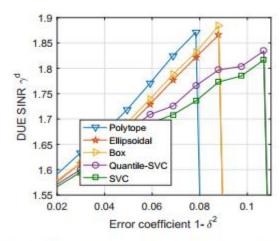


Fig. 16. DUE SINR versus channel estimation error coefficient, assuming $P_{max}^c = P_{max}^d = 20 \text{dBm}$, CUE QoS requirement $\gamma_{min}^c = 5$, DUE QoS requirement $\gamma_{min}^c = 1.5$ and outage probability $\epsilon = 0.05$.



谢谢

