

From User's View

Tensor a multi-dimension float-value array. For a Tensor with shape $\langle a, b, c \rangle$, where a, b , and c are all positive integers, there are in total of abc number of elements, called **size**, in it. The length of the shape is called **rank**. It is also the number of dimensions. Scalar is viewed as a Tensor with shape $\langle 1 \rangle$, i.e., rank 1.

This leads to the following definition:

```
typedef struct {
    mlvm_uint_t rank; /* Must be positive (non-zero). */
    mlvm_uint_t* shape; /* Length is 'rank' above. */
    mlvm_size_t size; /* Total number of elements. */
    double* value; /* The value buffer. */
} tensor_t;
```

From Intermediate Representation's View

There are two new concepts.

value mode The first one is ownership, called **value-mode**, which is an internal field. It represents whether the current Tensor owns its value buffer.

stride The second one is **stride**, with type `mlvm_size_t*`. It is an array with same length as **shape**. For **stride**[i], it represents the offset difference between the dimension increment at dimension **shape**[i].

tranpose For a Tensor with shape $\langle a, b, c \rangle$ and stride $\{bc, c, 1\}$, *tranpose*(1, 2, 0) produces a new Tensor with shape $\langle b, c, a \rangle$. With **stride** property, we could re-use the same value buffer, saving the copy cost, and represent the new Tensor as: shape $\langle b, c, a \rangle$ and stride $\{c, 1, bc\}$.

broadcast For a Tensor with shape $\langle a, 1 \rangle$ and stride $\{1, 1\}$, *broadcasting* to $\langle a, b \rangle$ is cost free as we just need a new Tensor with shape $\langle a, b \rangle$ and stride $\{1, 0\}$. Similarly, *broadcasting* a Tensor with shape $\langle 1, b \rangle$ to new shape $\langle a, b \rangle$ can be represented as shape $\langle a, b \rangle$ and stride $\{0, 1\}$.

constant If all above make sense, a **zeros** tensor with shape $\langle a, b \rangle$ is simply *broadcasting* a scalar 0 to $\langle a, b \rangle$, i.e., stride $\{0, 0\}$. So is a **ones** tensor.

data access This would be a big *disadvantage*. Locality is bad for arbitrary stride. Iterating the data value is also quite complicated.

reshape This would be another *disadvantage*. *Reshaping* a Tensor with arbitrary stride is not always cost-free. For example, *reshaping* a Tensor with shape $\langle a, b \rangle$ and stride $\{1, 0\}$ to $\langle ab \rangle$ needs a value buffer copy.