

EfficientML.ai Lecture 02: Basics of Neural Networks



Song Han

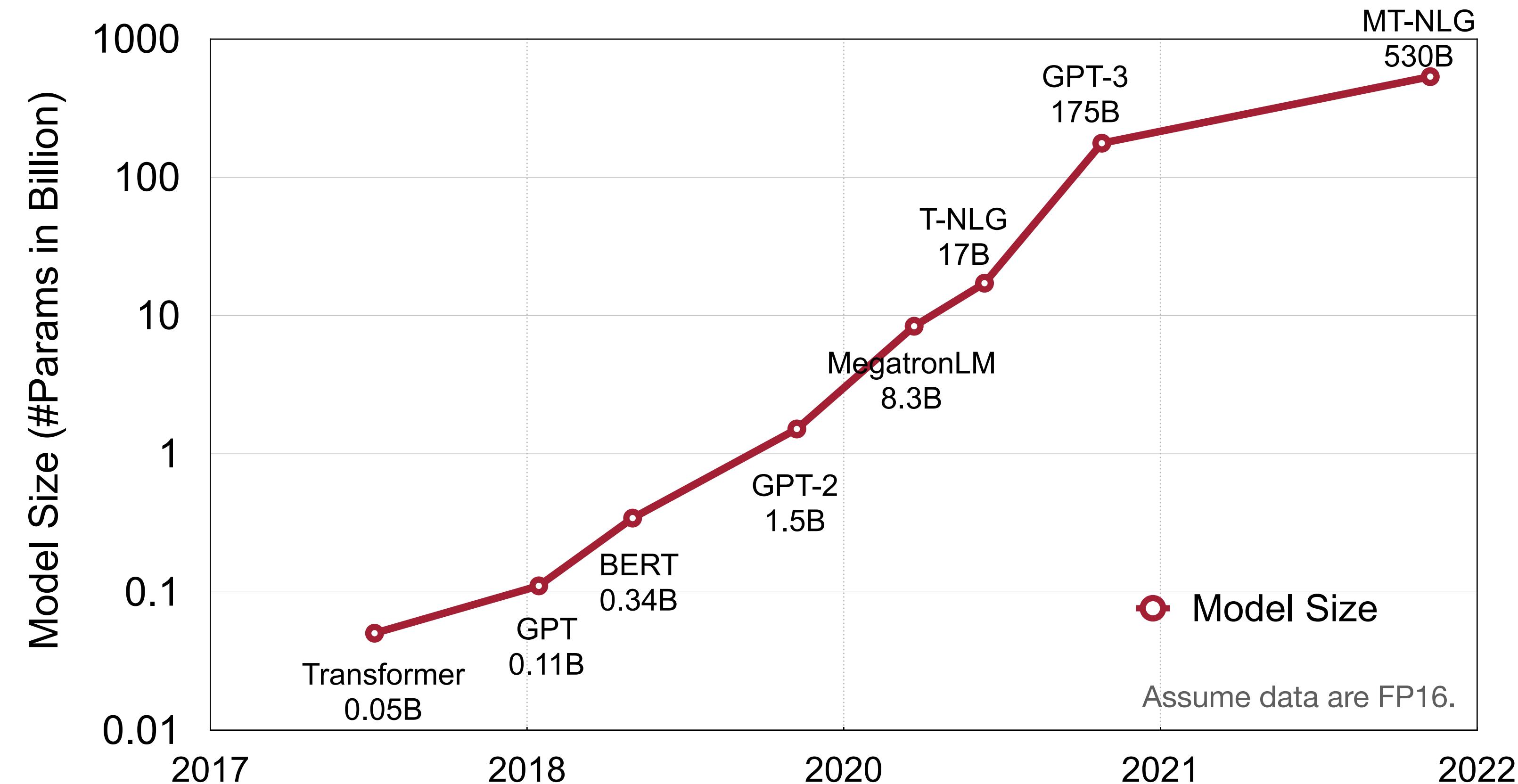
Associate Professor, MIT
Distinguished Scientist, NVIDIA

 @SongHan/MIT



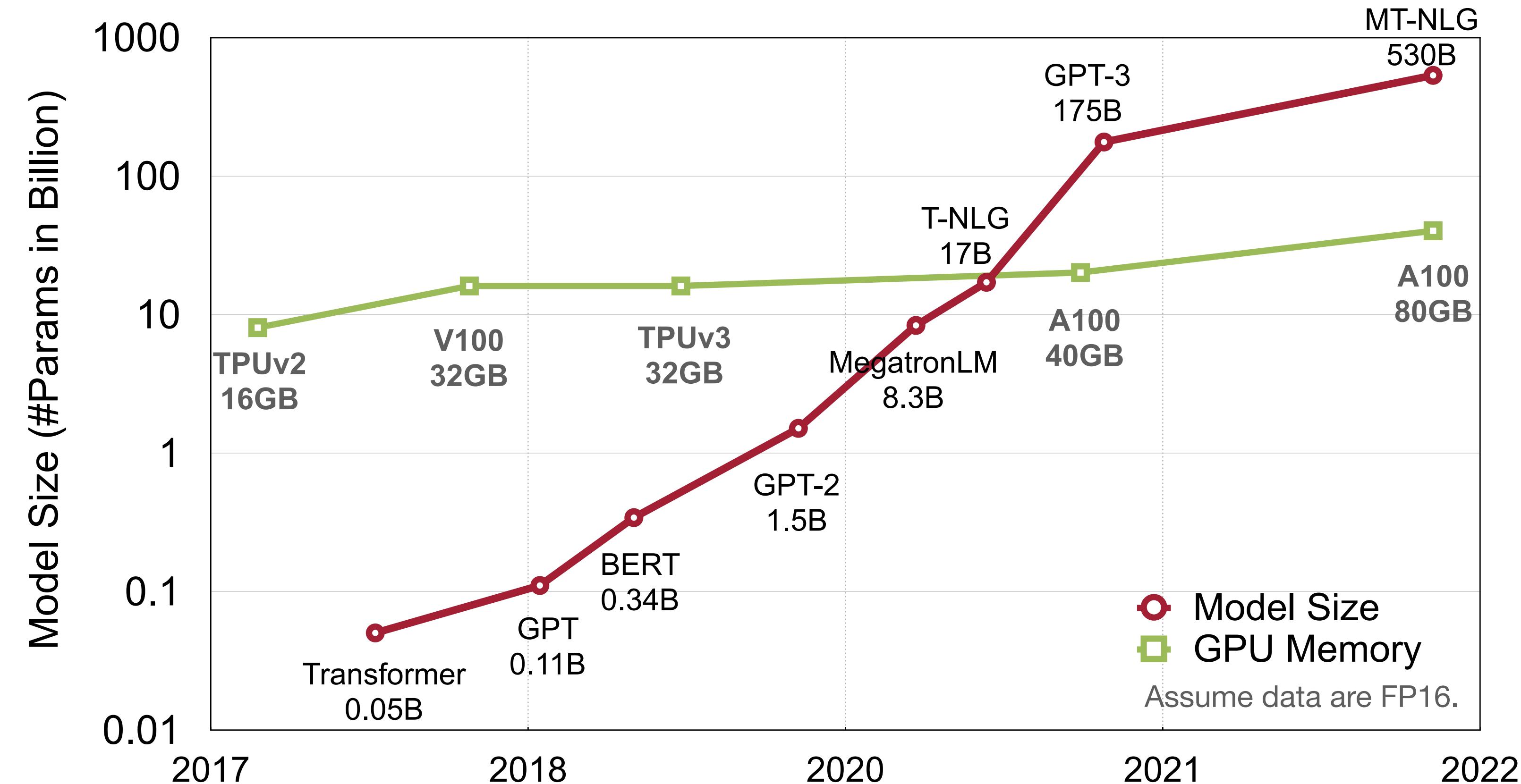
Deep Learning Continues to Scale

The demand of computation grows exponentially



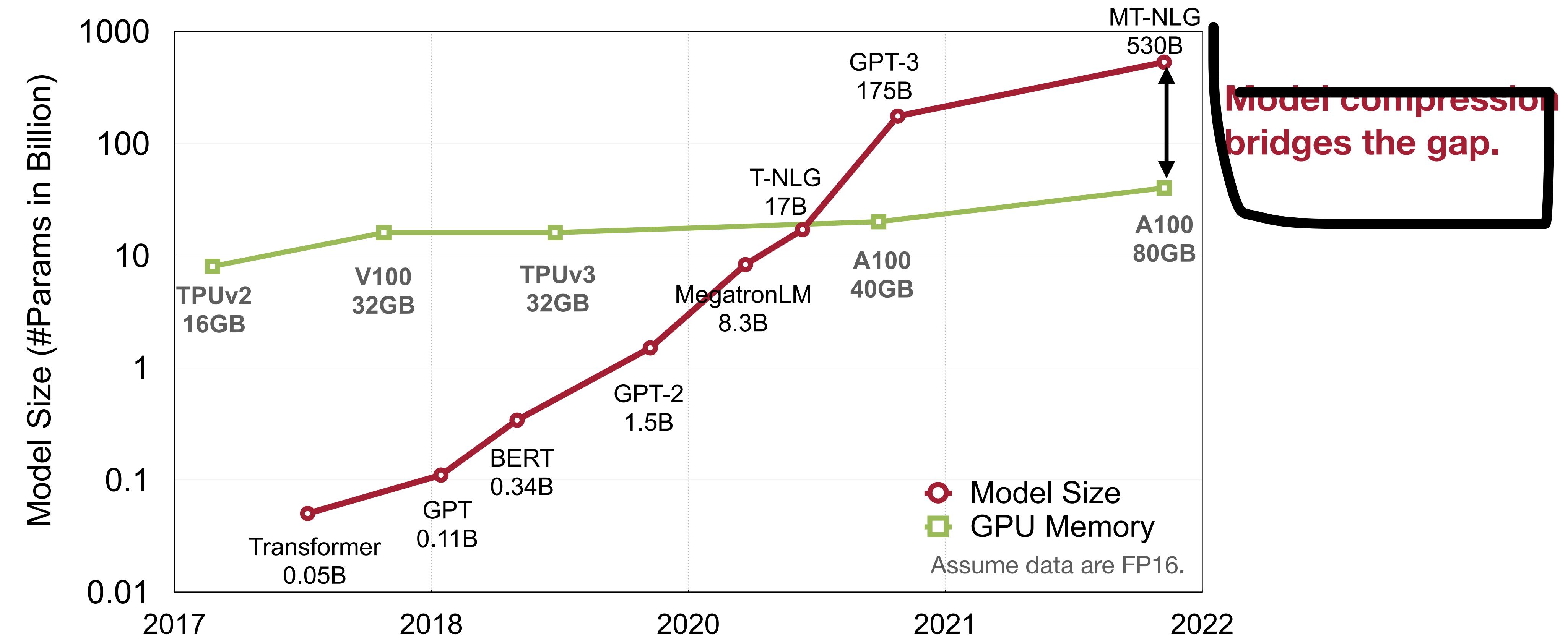
Problem: DL Models Outgrow Hardware

Moore's Law: 2x every 2 years; DL models: 4x every 2 years



Efficient Deep Learning Techniques are Essential

Bridges the Gap between the Supply and Demand of Computation



EfficientViT: Speeds up High-Resolution Computer Vision

Explore websites, people, and locations

Q memory engrams

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A new AI model speeds up high-resolution computer vision, which could improve image quality in video streaming or help autonomous vehicles identify road hazards. The system is “fast enough that we can run it on mobile and cloud devices,” Song Han says.

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EfficientViT: Multi-Scale Linear Attention for High-Resolution Dense Prediction [Cai et al., ICCV 2023]

EfficientViT: Speeds up High-Resolution Computer Vision

EfficientViT enables real-time street scene segmentation on edge

SegFormer
1.6FPS, 82.4mIoU



EfficientViT
21.8FPS, 82.7mIoU



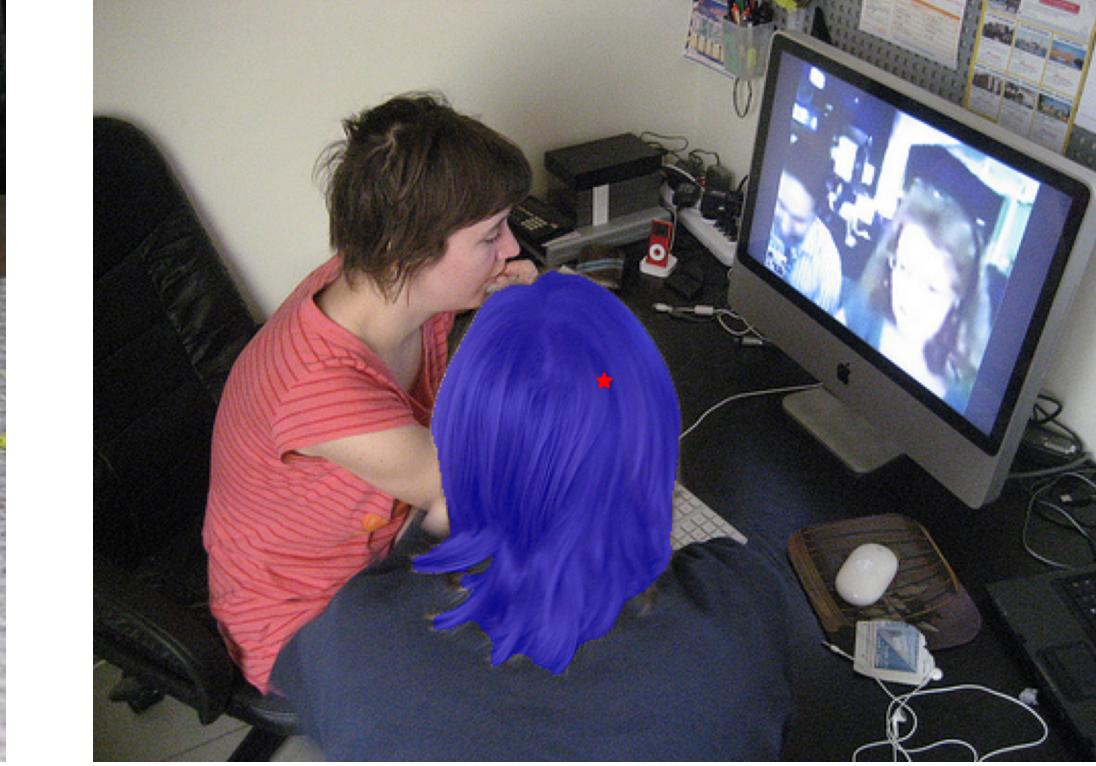
Speed is measured on Nvidia Jetson AGX Orin with TensorRT, fp16, batch size 1.
Performance is measured on the Cityscapes dataset.

Efficient Prompt Segmentation

EfficientViT accelerates Segment Anything by 70 times on GPU

SAM ViT-Huge

12 image/s



EfficientViT

842 image/s



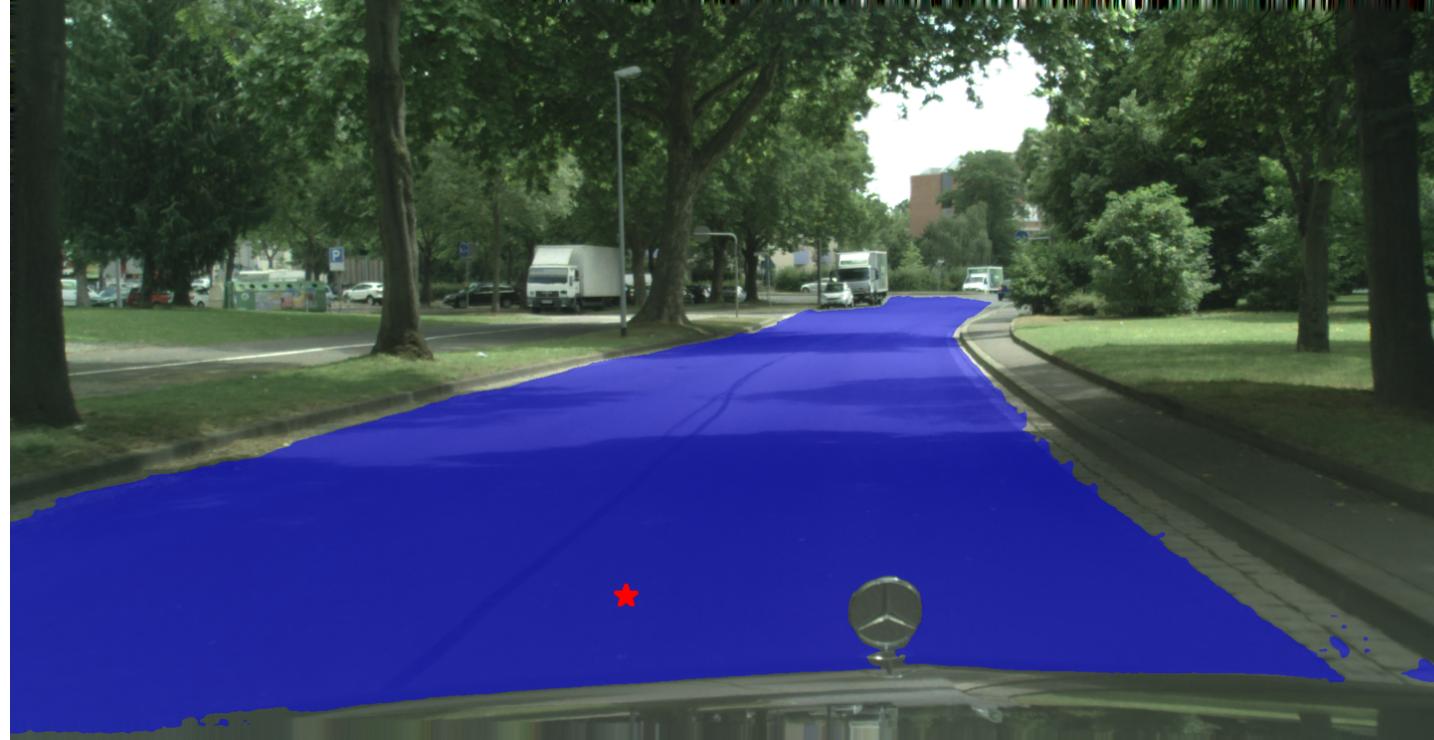
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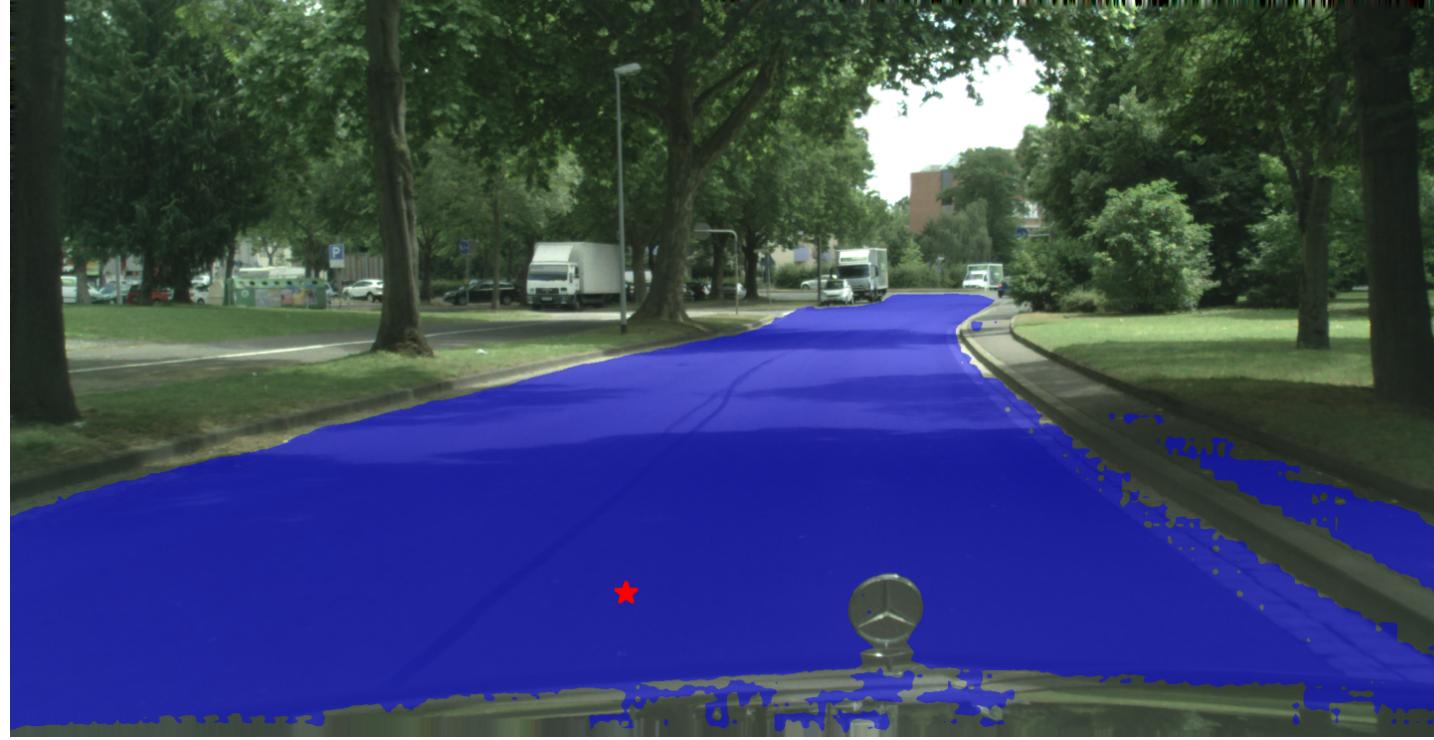
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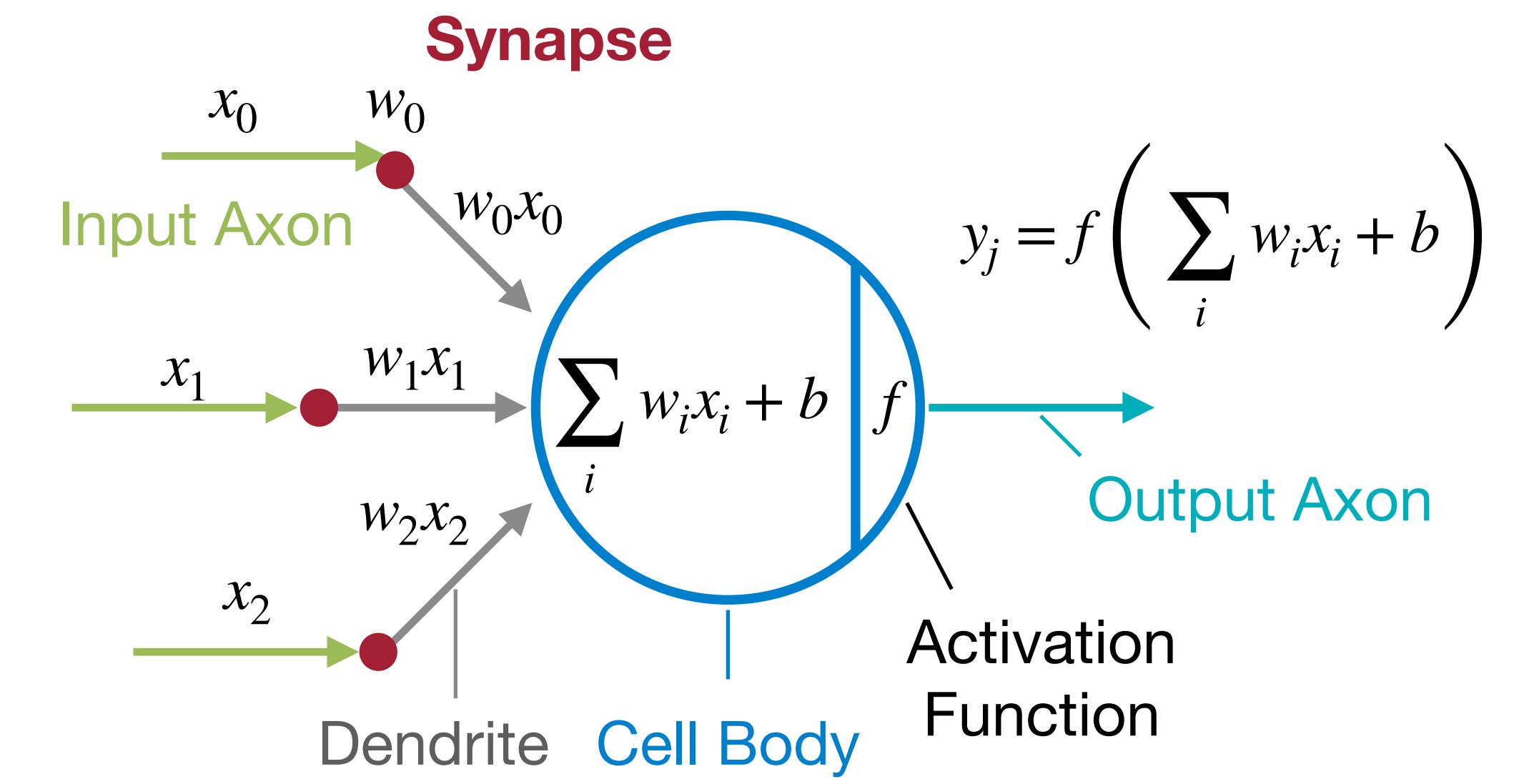
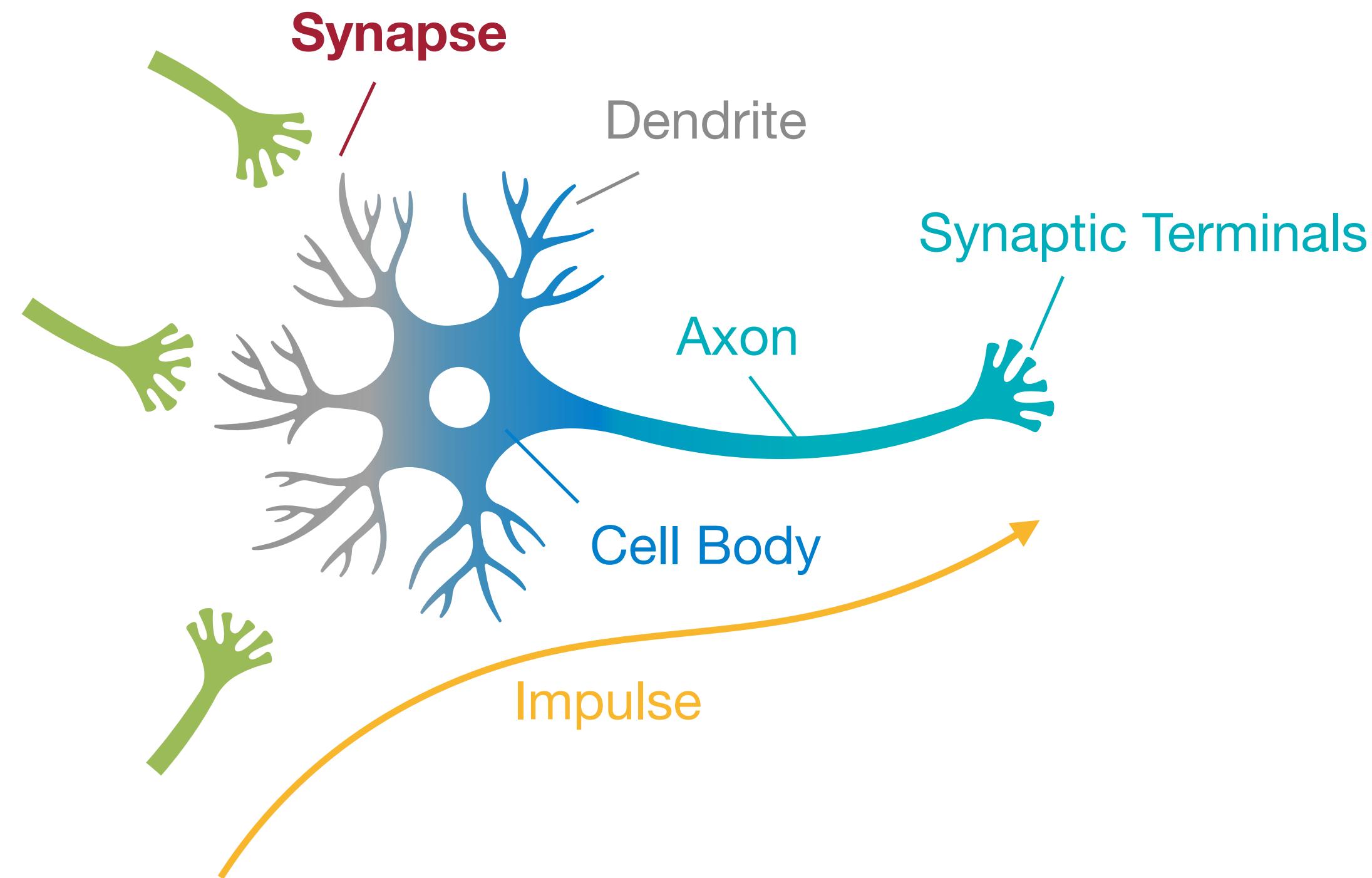
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Lecture Plan

Today we will:

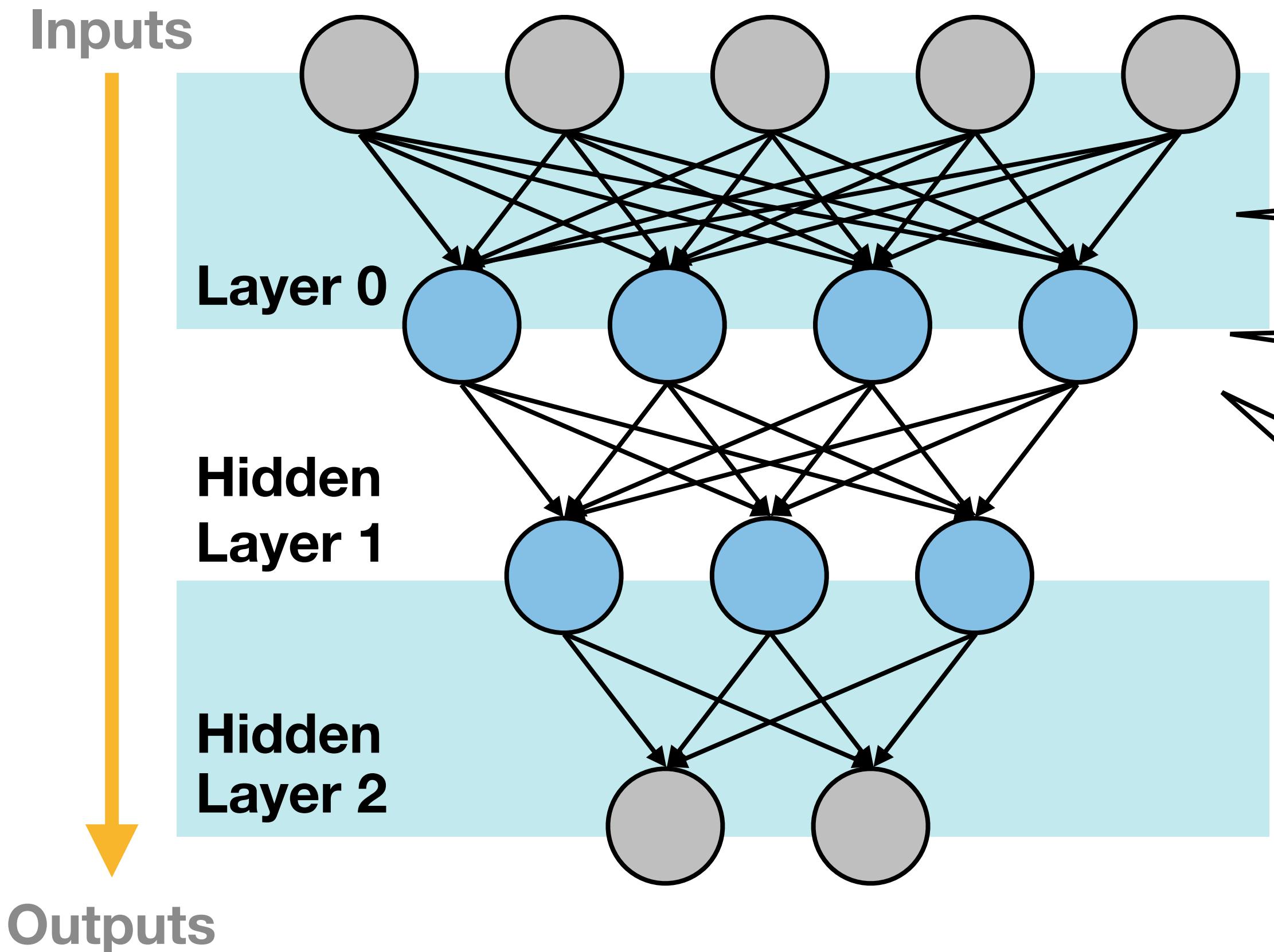
1. Review the **terminology of neural networks**
 - Neuron, Synapses, Activation, Feature, Weight, Parameter, etc
2. Review **popular building blocks** in a neural network
 - Fully-Connected, Convolution, Grouped Convolution, Depthwise Convolution
 - Pooling, Normalization, Transformer
3. Review **convolutional neural networks'** architecture
 - AlexNet, VGG-16, ResNet-50, MobileNetV2
4. Introduce **popular efficiency metrics** for neural networks
 - #Parameters, Model Size, Peak #Activations, MAC, FLOP, FLOPS, OP, OPS, Latency, Throughput
5. Lab 0: Tutorial on PyTorch and lab exercises

Neuron and Synapse

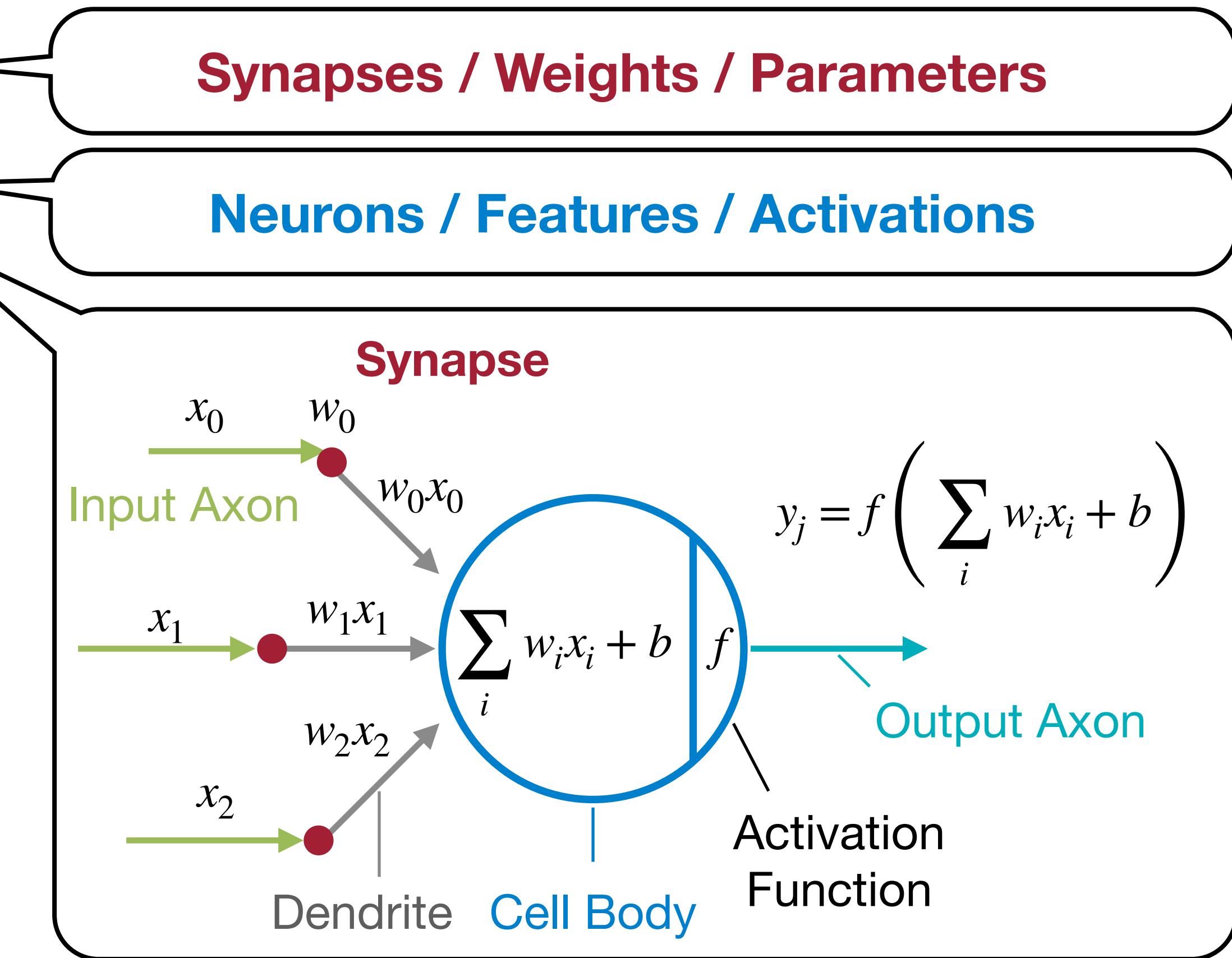


Deep Neural Network

3-Layer Neural Network
With 2 Hidden Layers



The dimensionality of these *hidden* layers determines the **width** of the model.



Popular Neural Network Layers

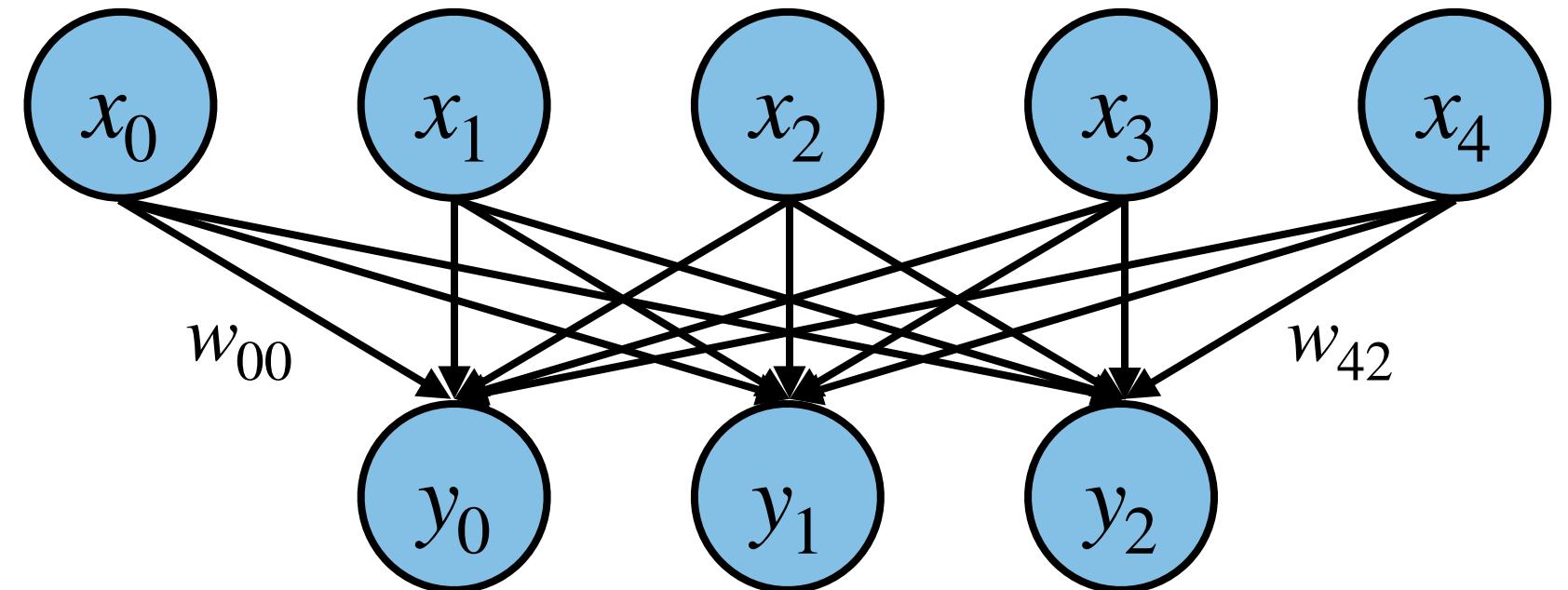
Fully-Connected Layer (Linear Layer)

The output neuron is connected to all input neurons.

- **Shape of Tensors:**

- Input Features \mathbf{X} : $(1, c_i)$
- Output Features \mathbf{Y} : $(1, c_o)$
- Weights \mathbf{W} : (c_o, c_i)
- Bias \mathbf{b} : $(c_o,)$

Notations	
c_i	Input Channels
c_o	Output Channels



$$y_i = \sum_j w_{ij}x_j + b_i$$

$$\begin{matrix} c_i \\ \text{---} \\ \boxed{} \end{matrix} \times \begin{matrix} c_o \\ \text{---} \\ c_i \\ \text{---} \\ \boxed{} \end{matrix} = \begin{matrix} c_o \\ \text{---} \\ \boxed{} \end{matrix}$$

$\mathbf{X} \quad \mathbf{W}^T \quad \mathbf{Y}$

The diagram shows the matrix multiplication for a fully-connected layer. An input vector \mathbf{X} of shape $(1, c_i)$ is multiplied by a weight matrix \mathbf{W}^T of shape (c_o, c_i) to produce an output vector \mathbf{Y} of shape $(1, c_o)$. The result is a scalar value for each output channel.

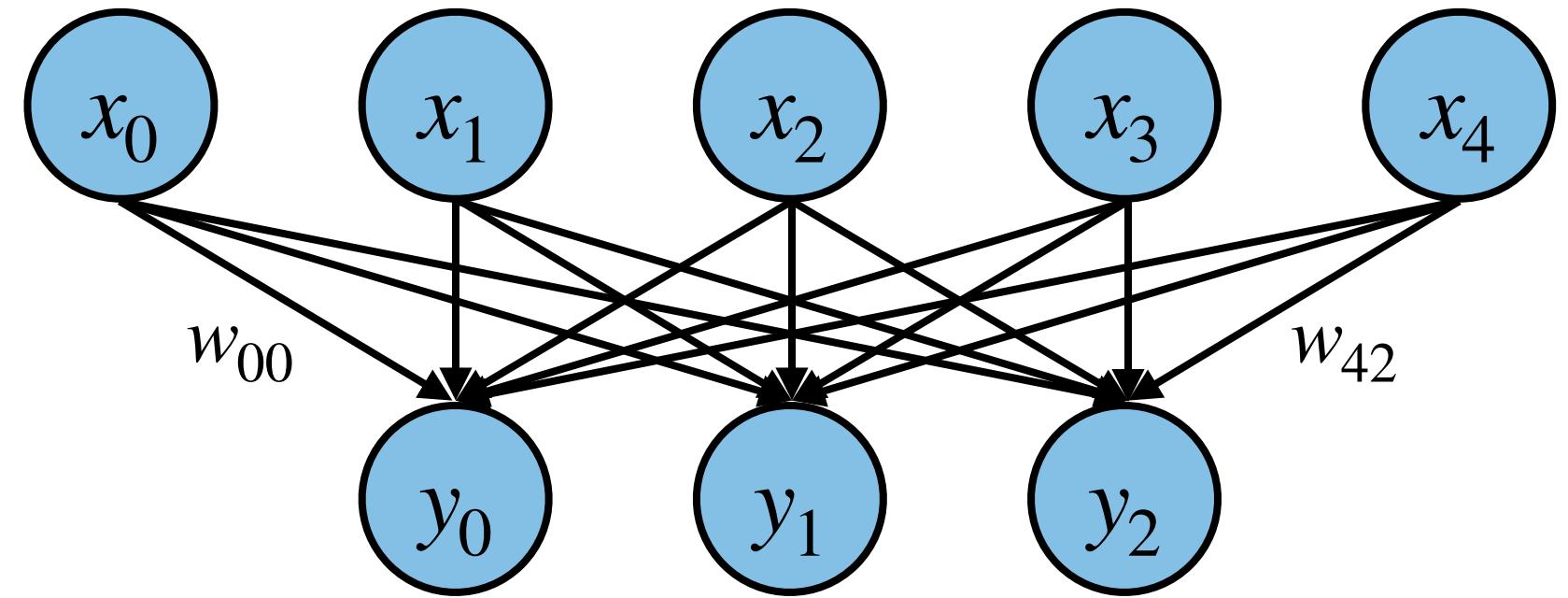
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- **Shape of Tensors:**

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Notations	
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$$y_i = \sum_j w_{ij}x_j + b_i$$

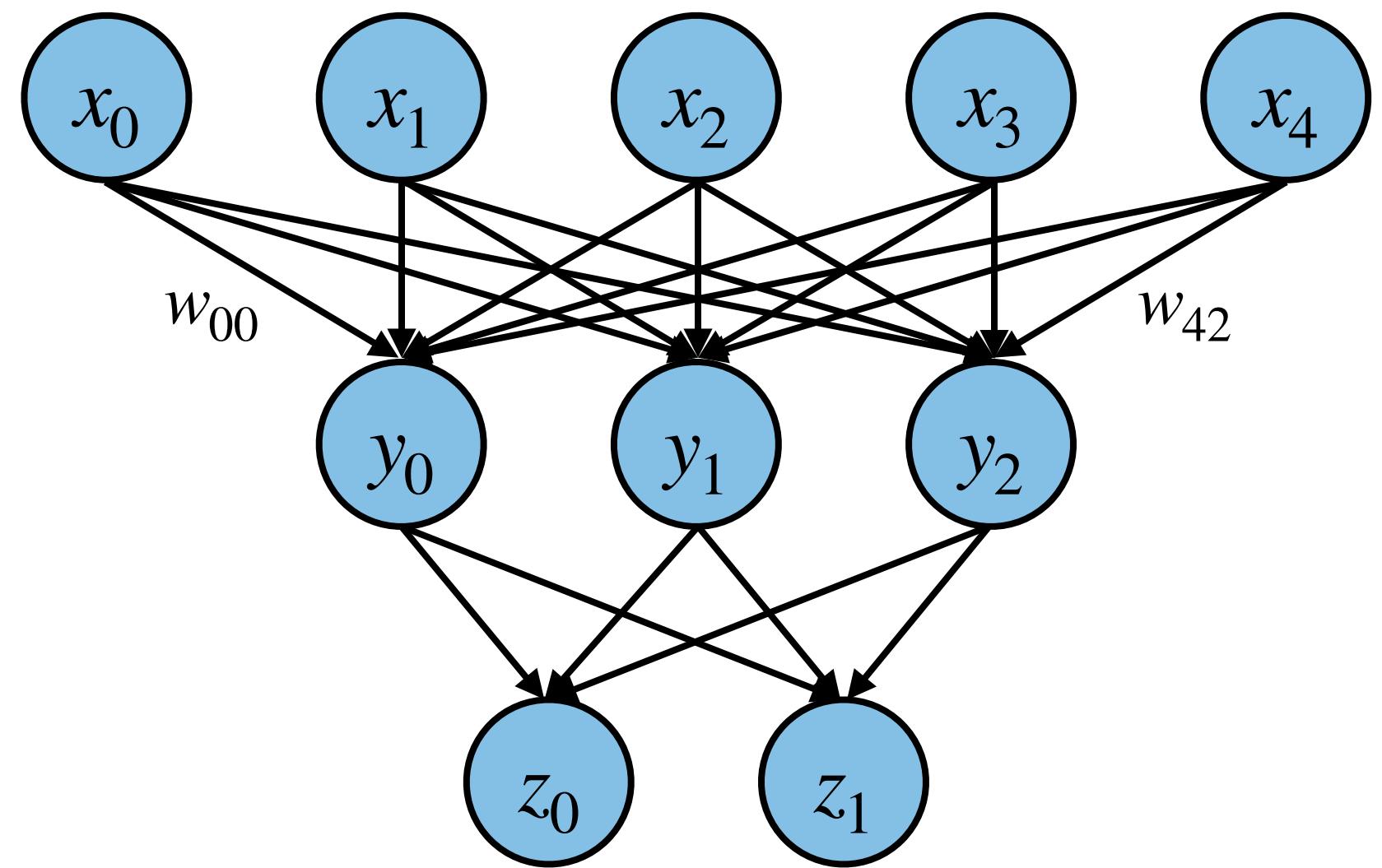
$$\begin{matrix} n & \times & c_i \\ \boxed{} & \times & \boxed{} \\ \mathbf{X} & & \mathbf{W}^T \end{matrix} = \begin{matrix} c_o \\ \boxed{} \\ \mathbf{Y} \end{matrix}$$

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Multilayer Perceptron (MLP)

$$\begin{matrix} n & \times & c_i \\ \boxed{} & \times & \boxed{} \\ \mathbf{X} & & \mathbf{W}^T \end{matrix} = \begin{matrix} c_o \\ \boxed{} \\ \mathbf{Y} \end{matrix}$$

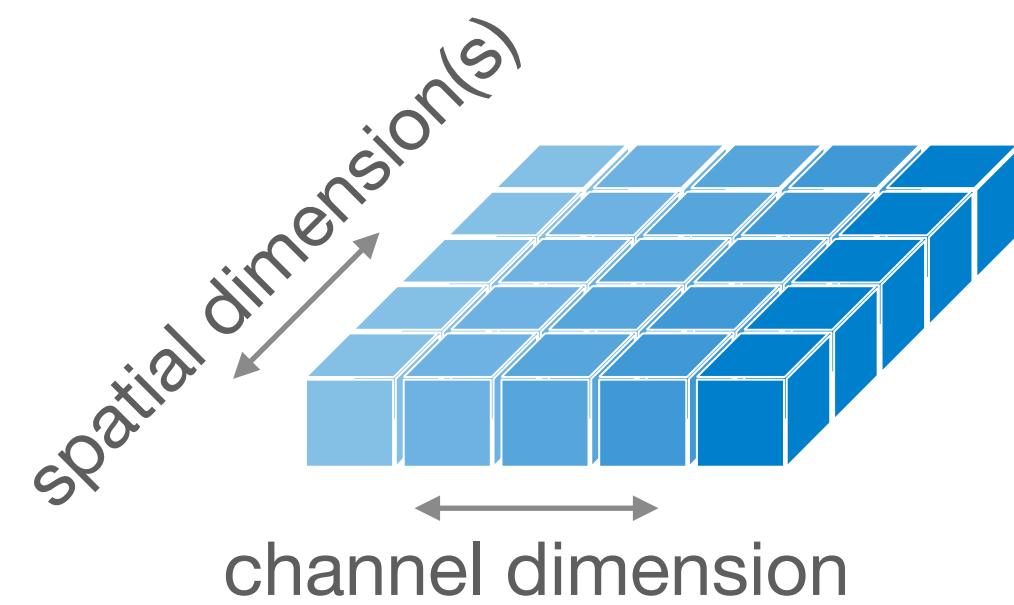
Diagram illustrating the matrix multiplication for a fully-connected layer. An input matrix \mathbf{X} of shape $n \times c_i$ is multiplied by a weight matrix \mathbf{W}^T of shape $c_i \times c_o$ to produce an output matrix \mathbf{Y} of shape $n \times c_o$.

Convolution Layer

The output neuron is connected to input neurons in the receptive field.

- **Shape of Tensors:** 1D Conv
- Input Features \mathbf{X} : (n, c_i) (n, c_i, w_i)
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Notations	
n	Batch Size
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w_i, w_o	Input/Output Width

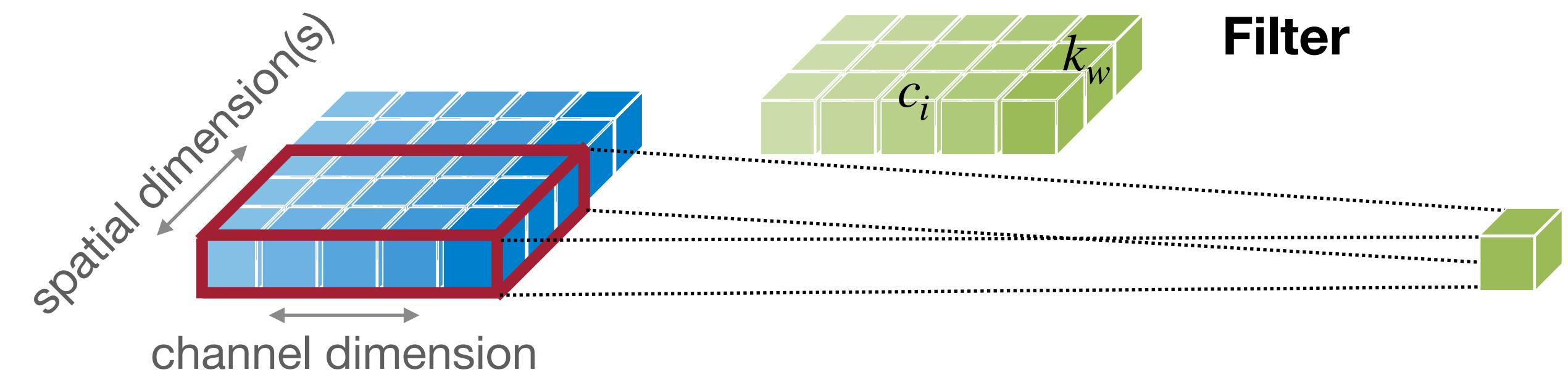


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k_w	Kernel Width

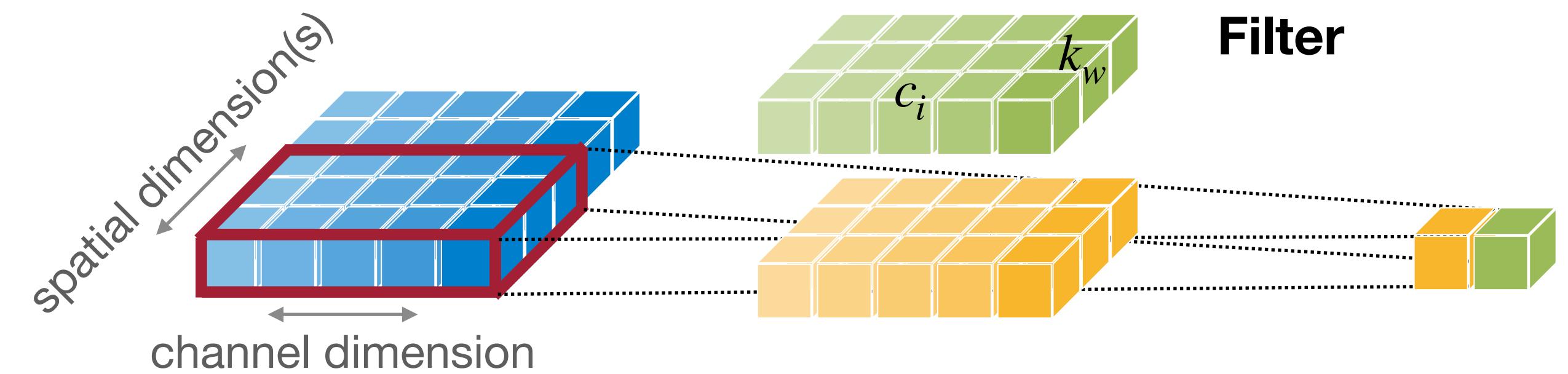


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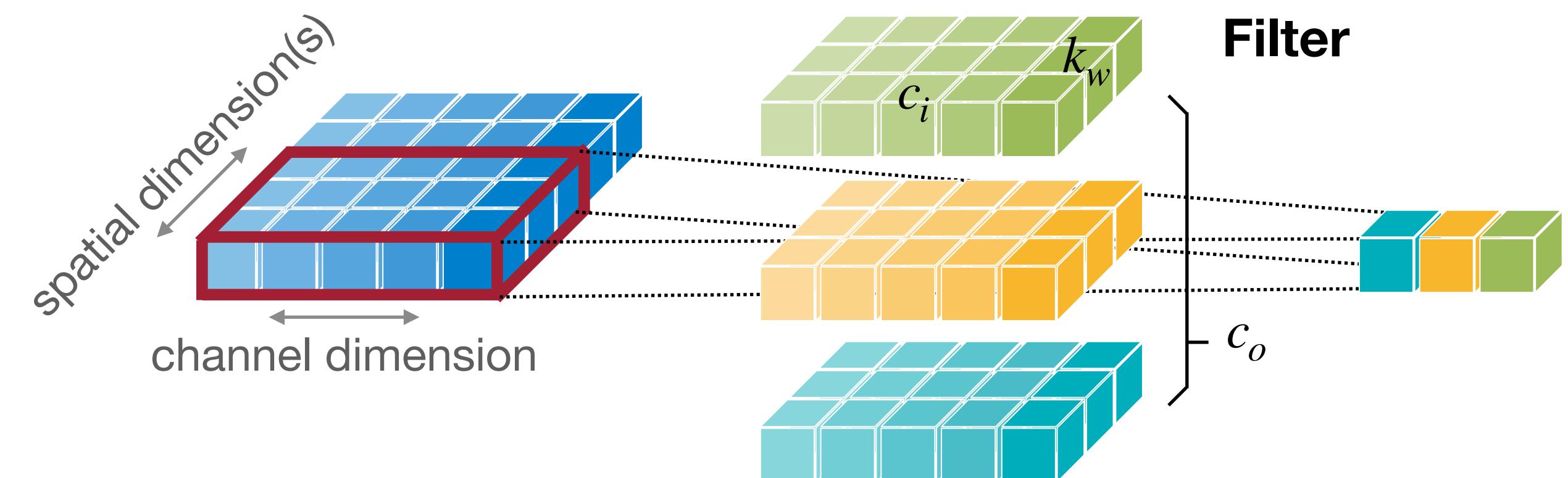


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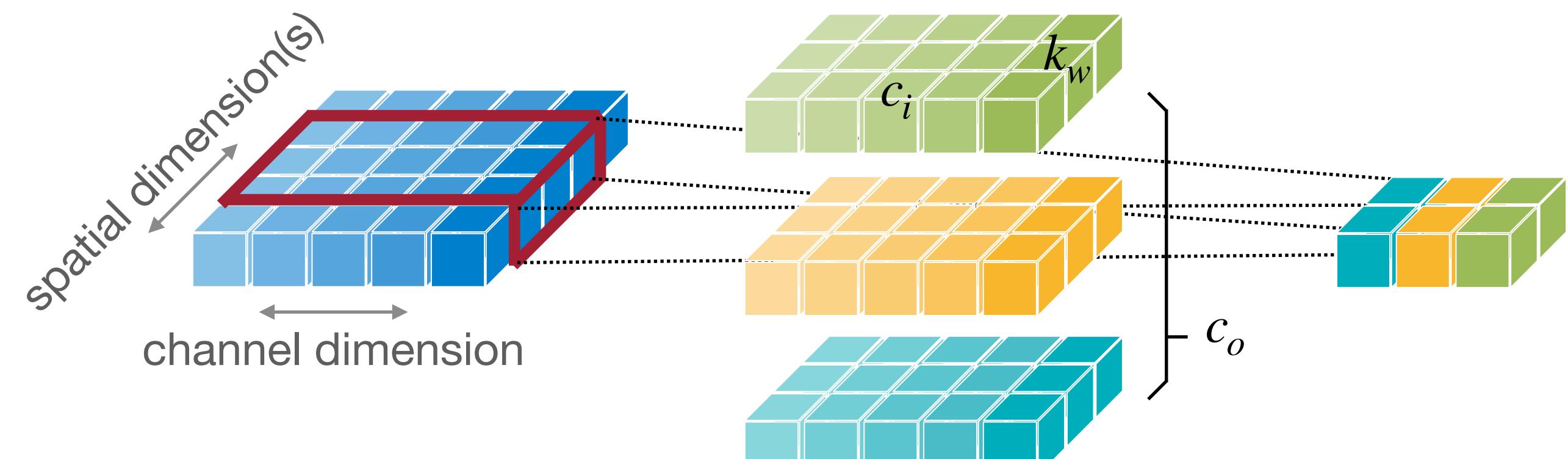


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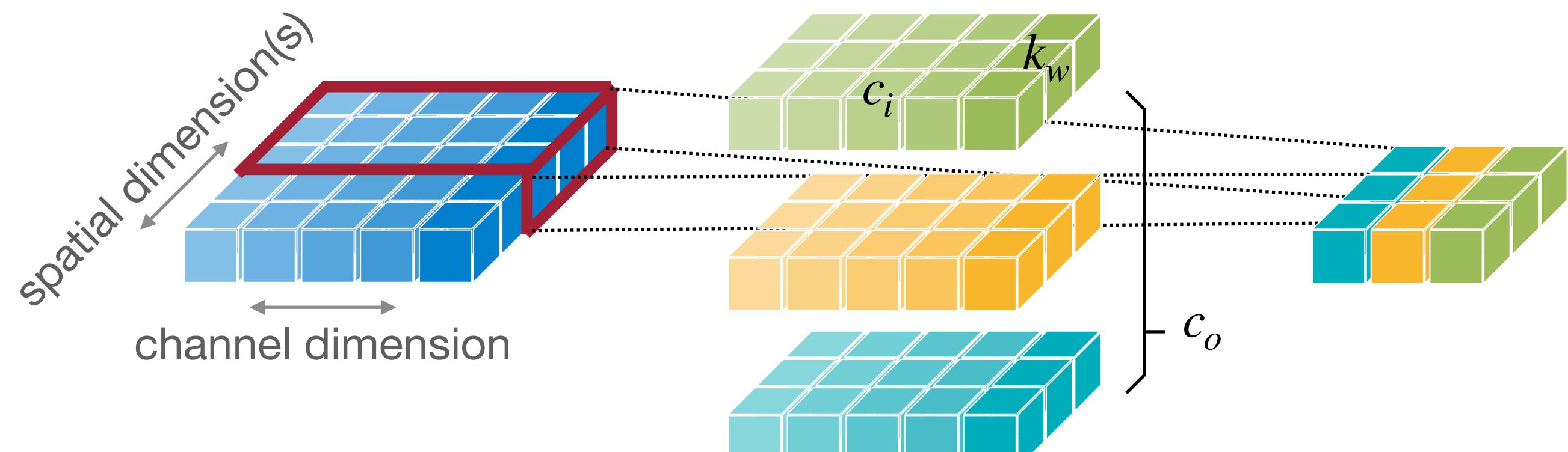
Weight Sharing

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Weight Sharing

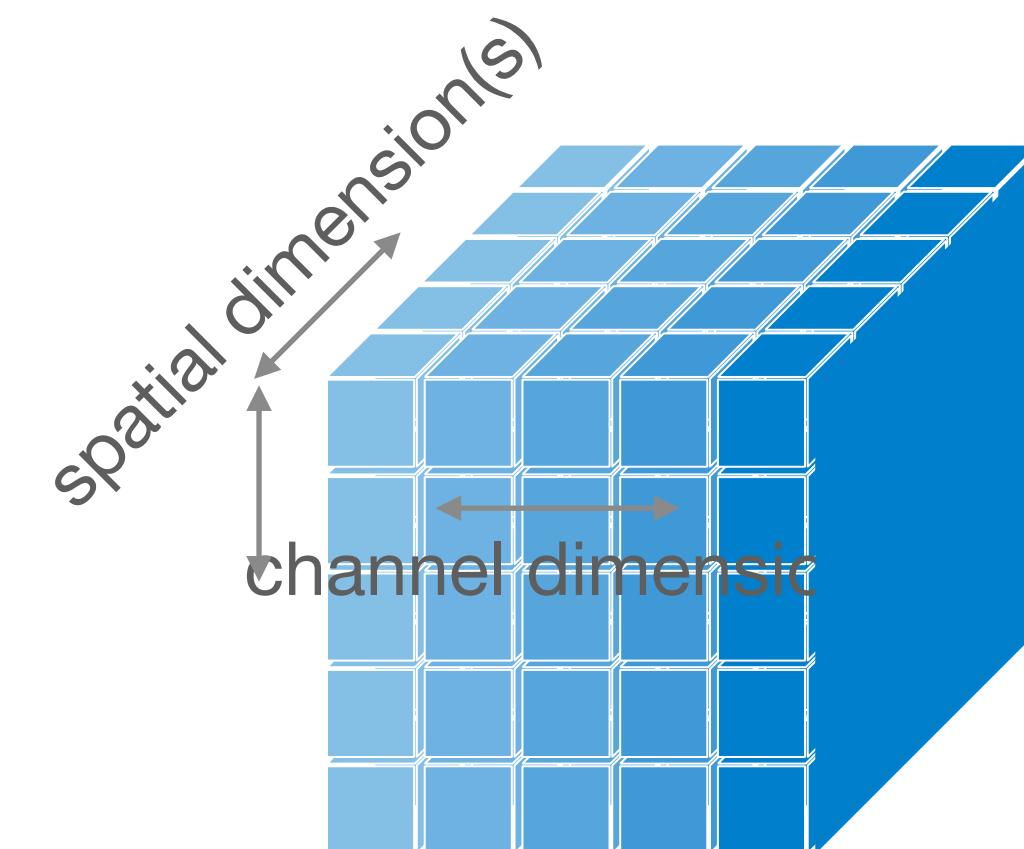
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- **Shape of Tensors:**

- | | 1D Conv | 2D Conv |
|---|-------------------|------------------------|
| • Input Features \mathbf{X} : (n, c_i) | (n, c_i, w_i) | (n, c_i, h_i, w_i) |
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| • Bias \mathbf{b} : $(c_o,)$ | | |

Notations	
n	Batch Size
c_i	Input Channels
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Activation Map / Feature Map

$$h \times w$$

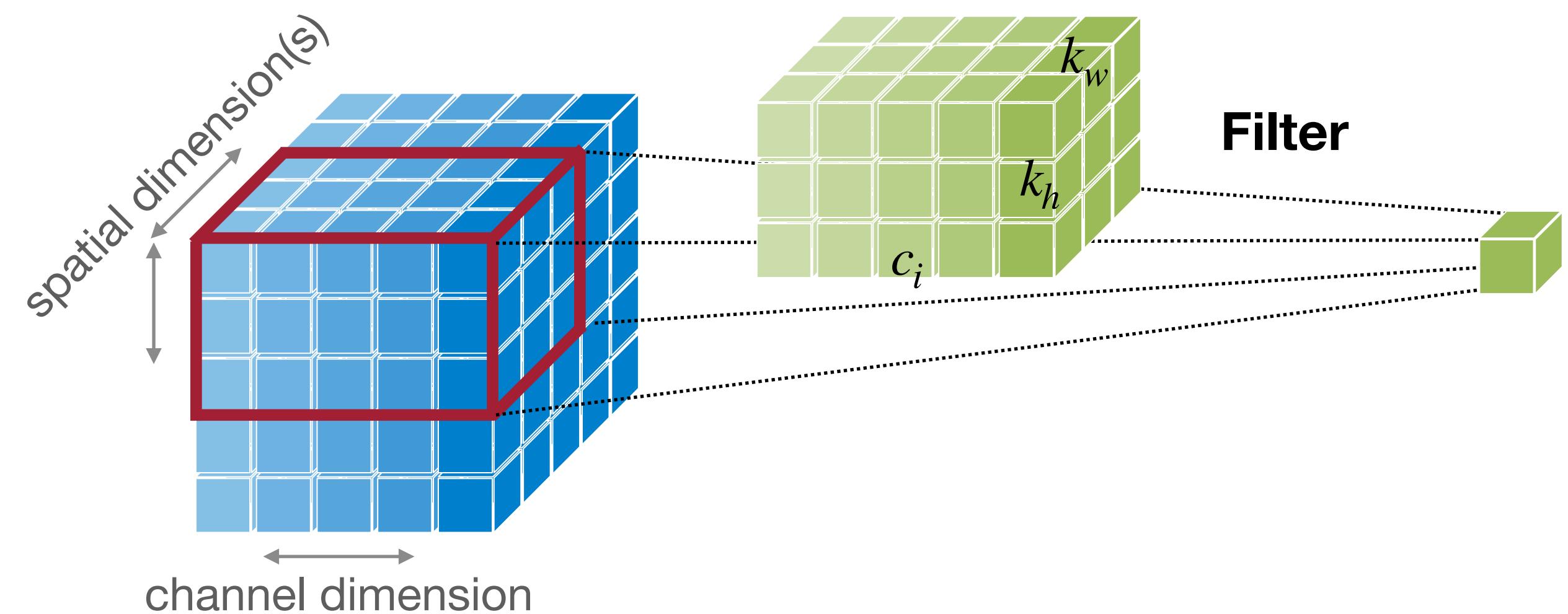
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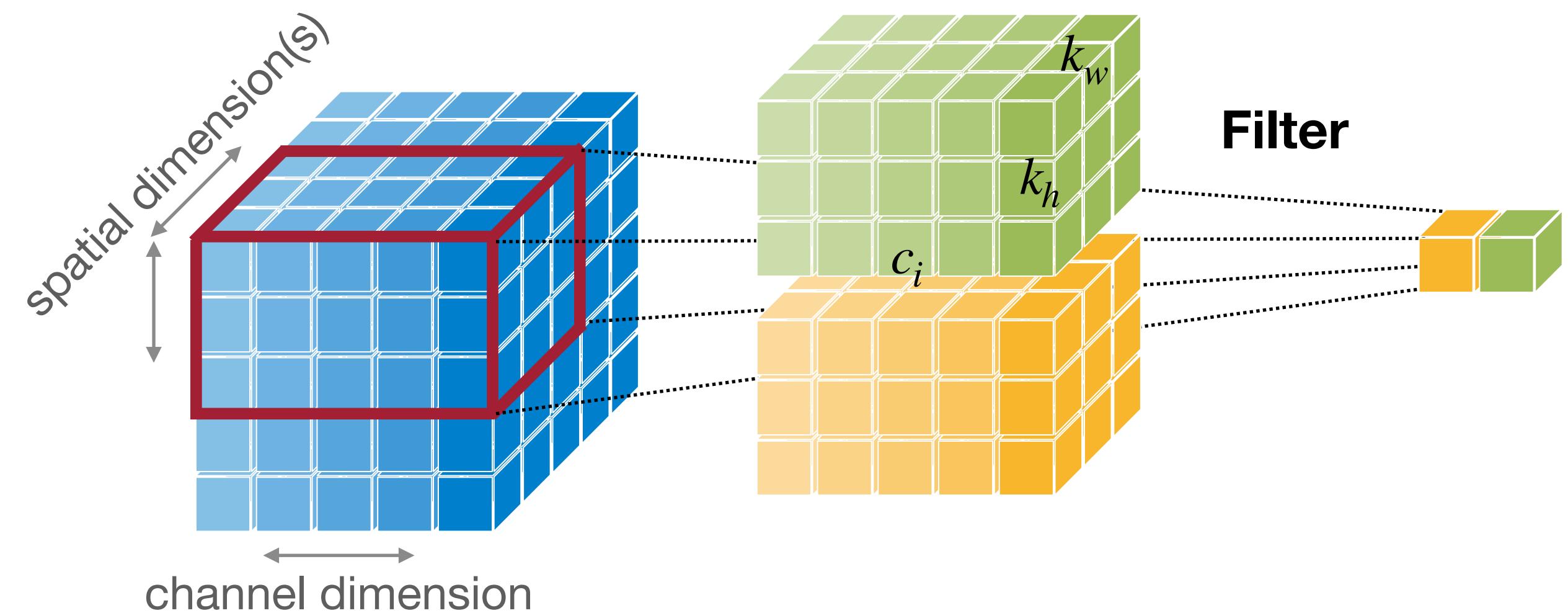
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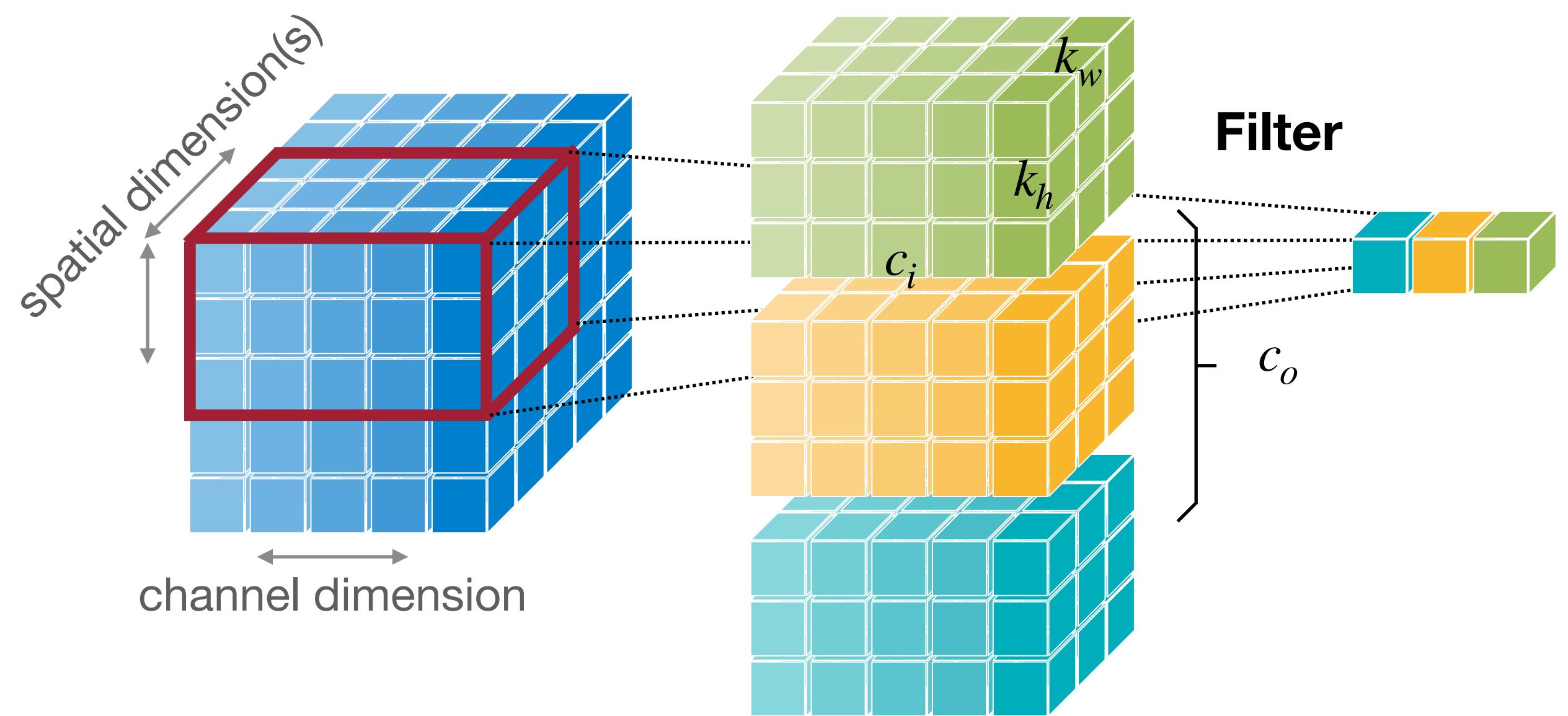
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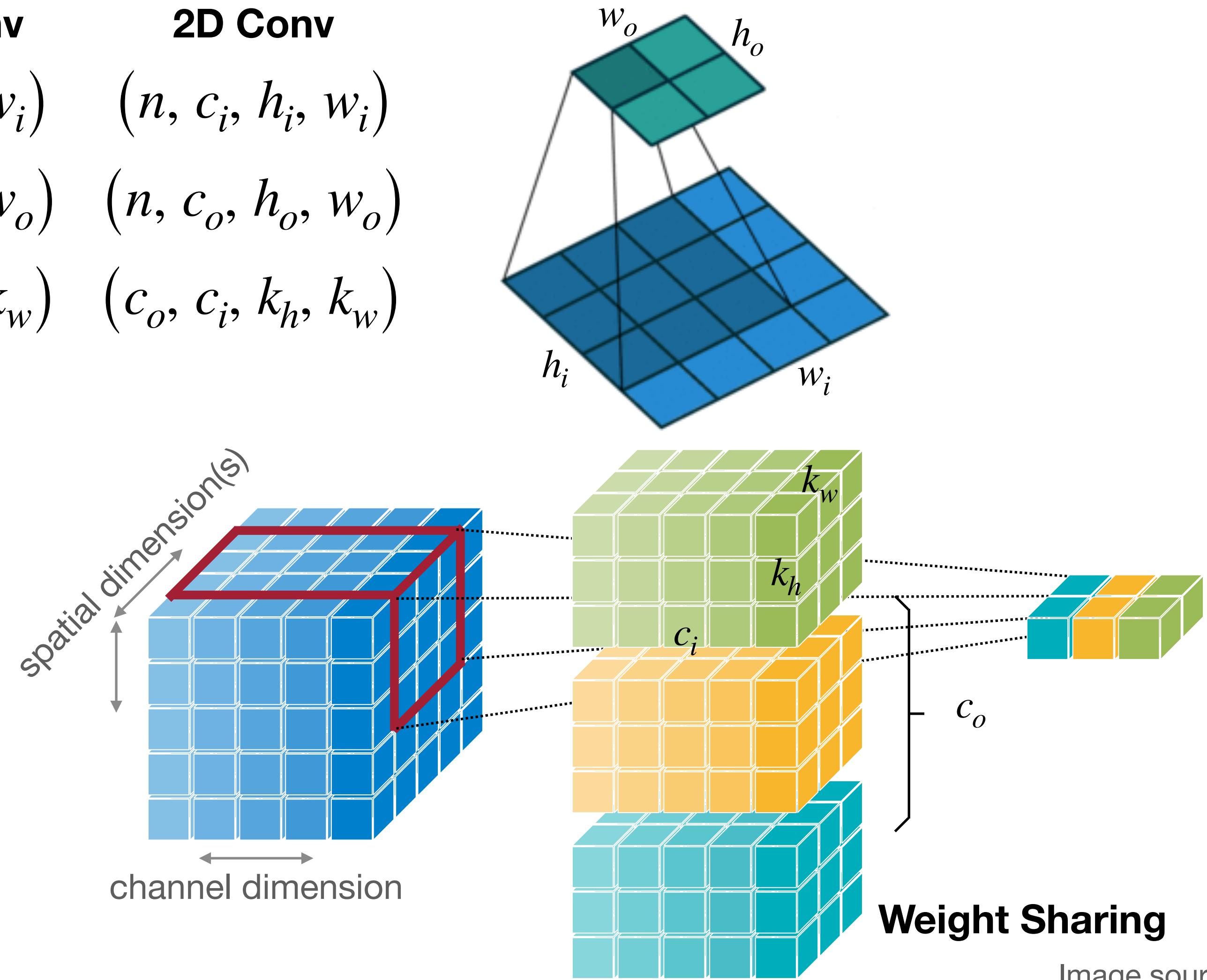


Image source: 1

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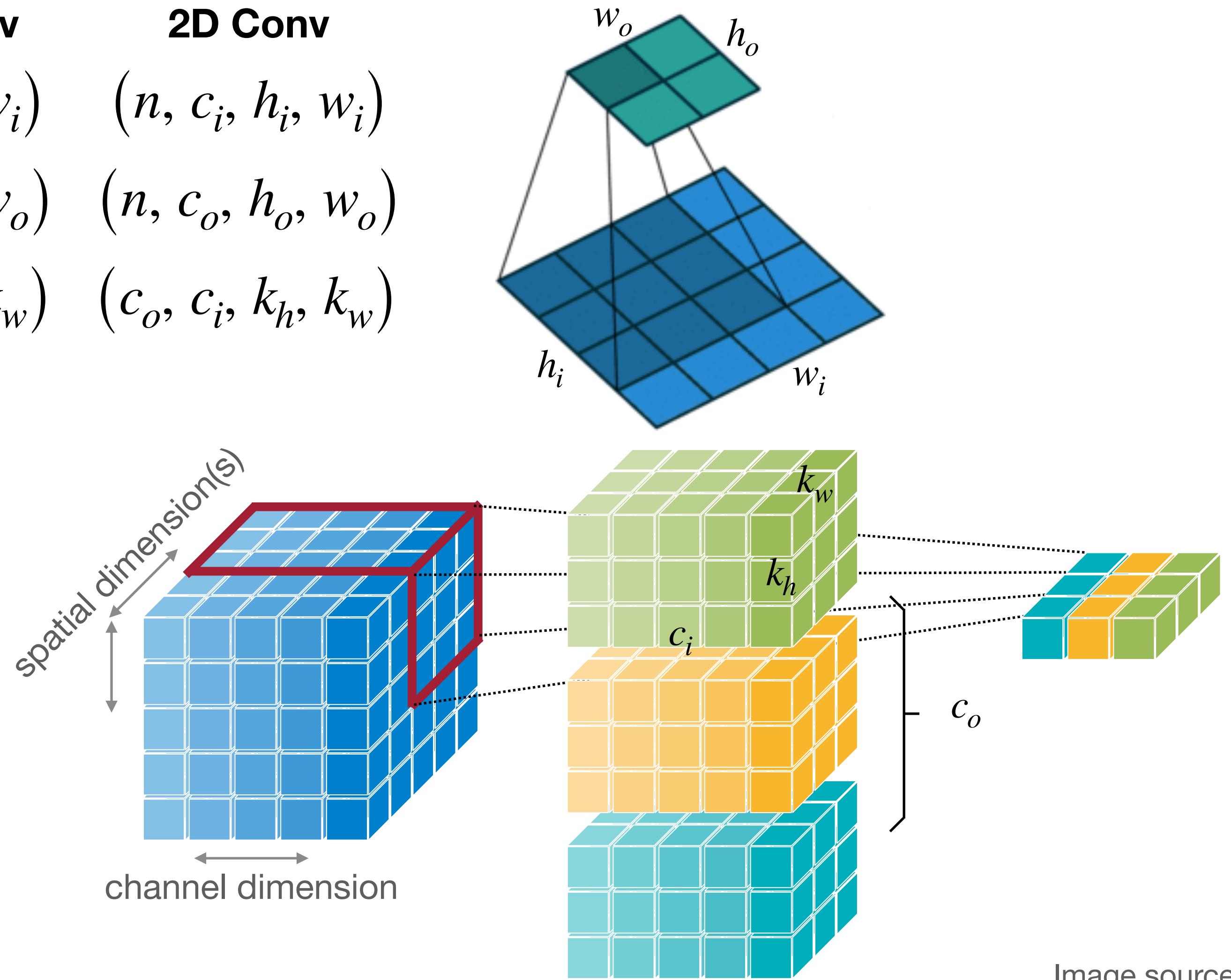


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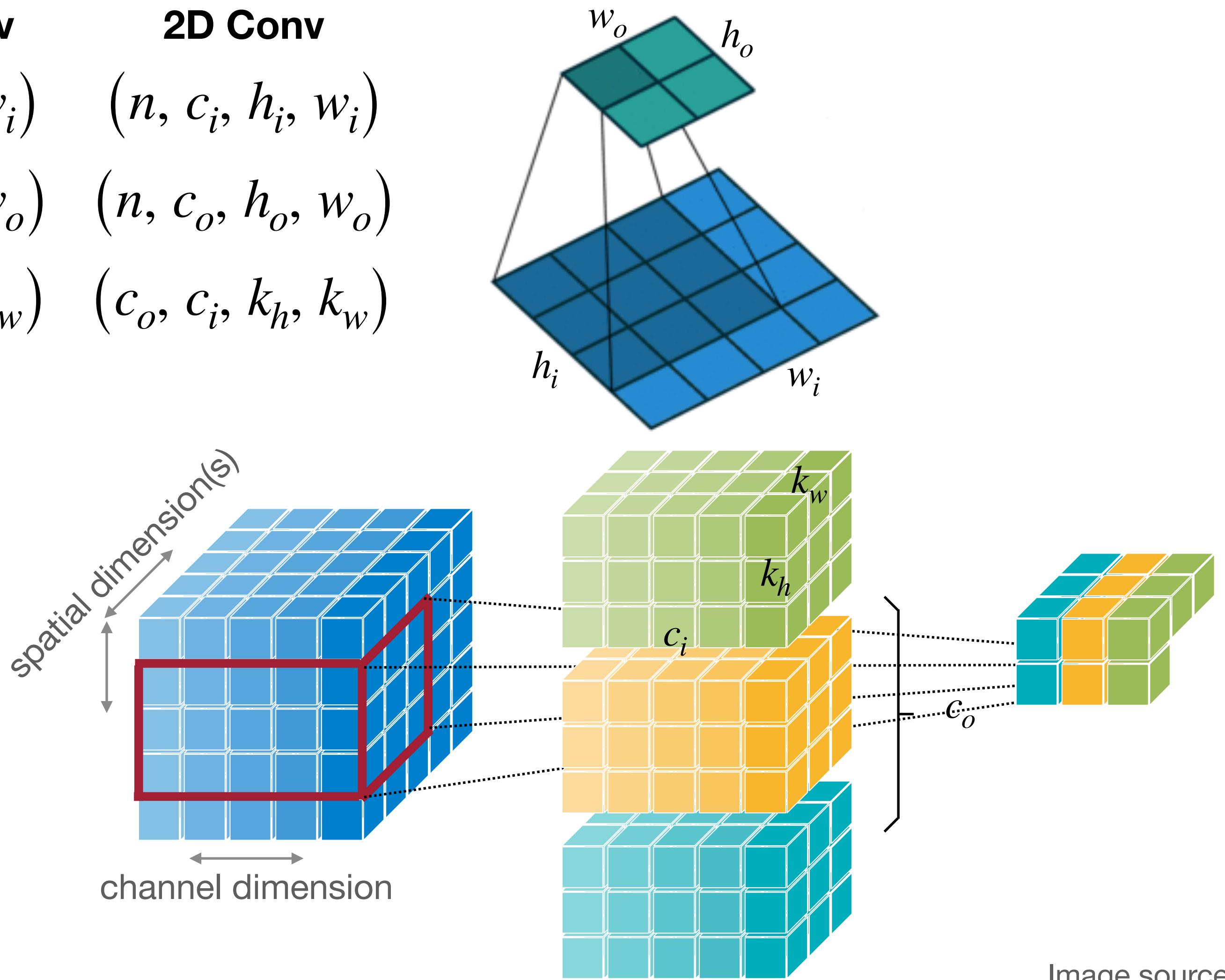


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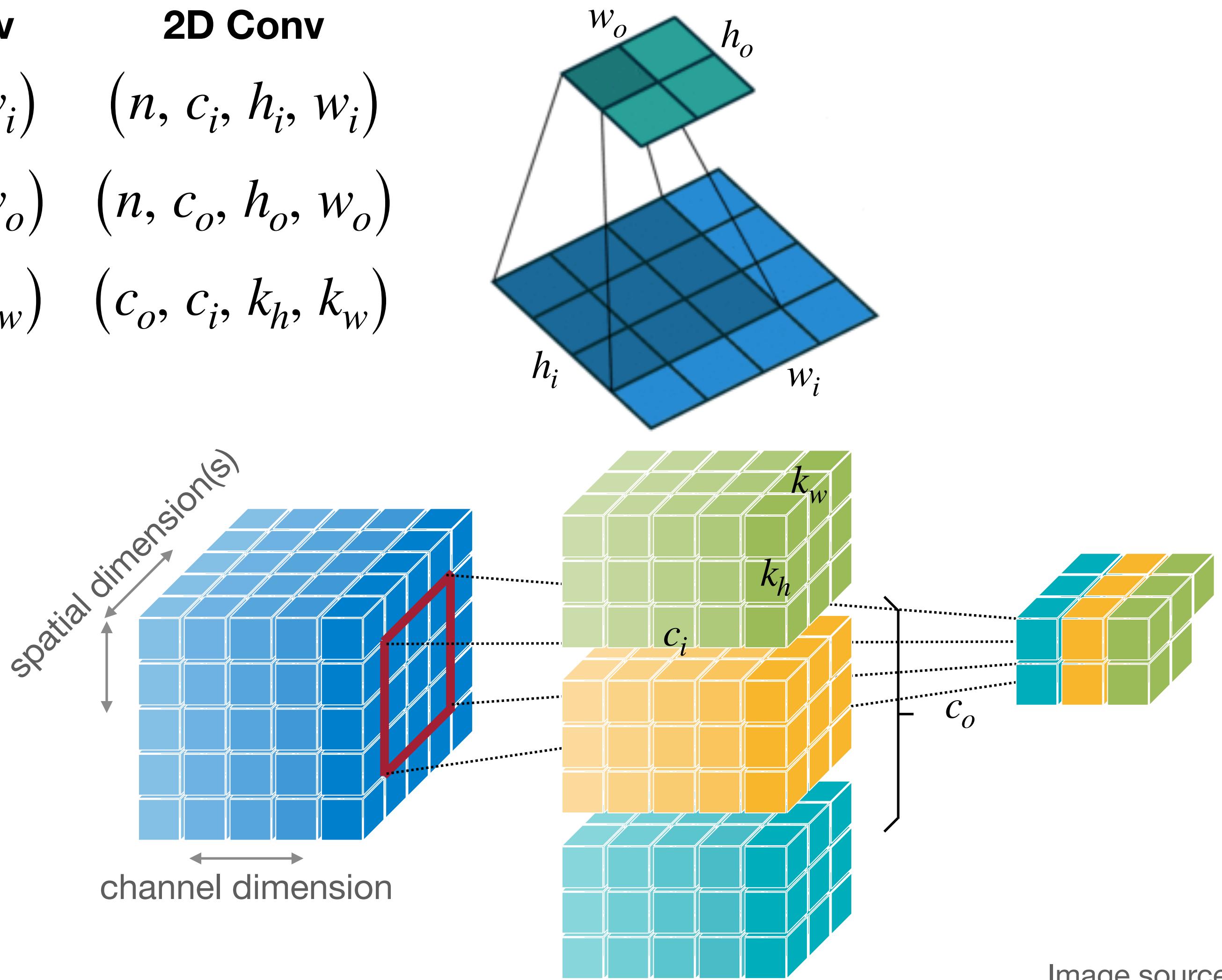


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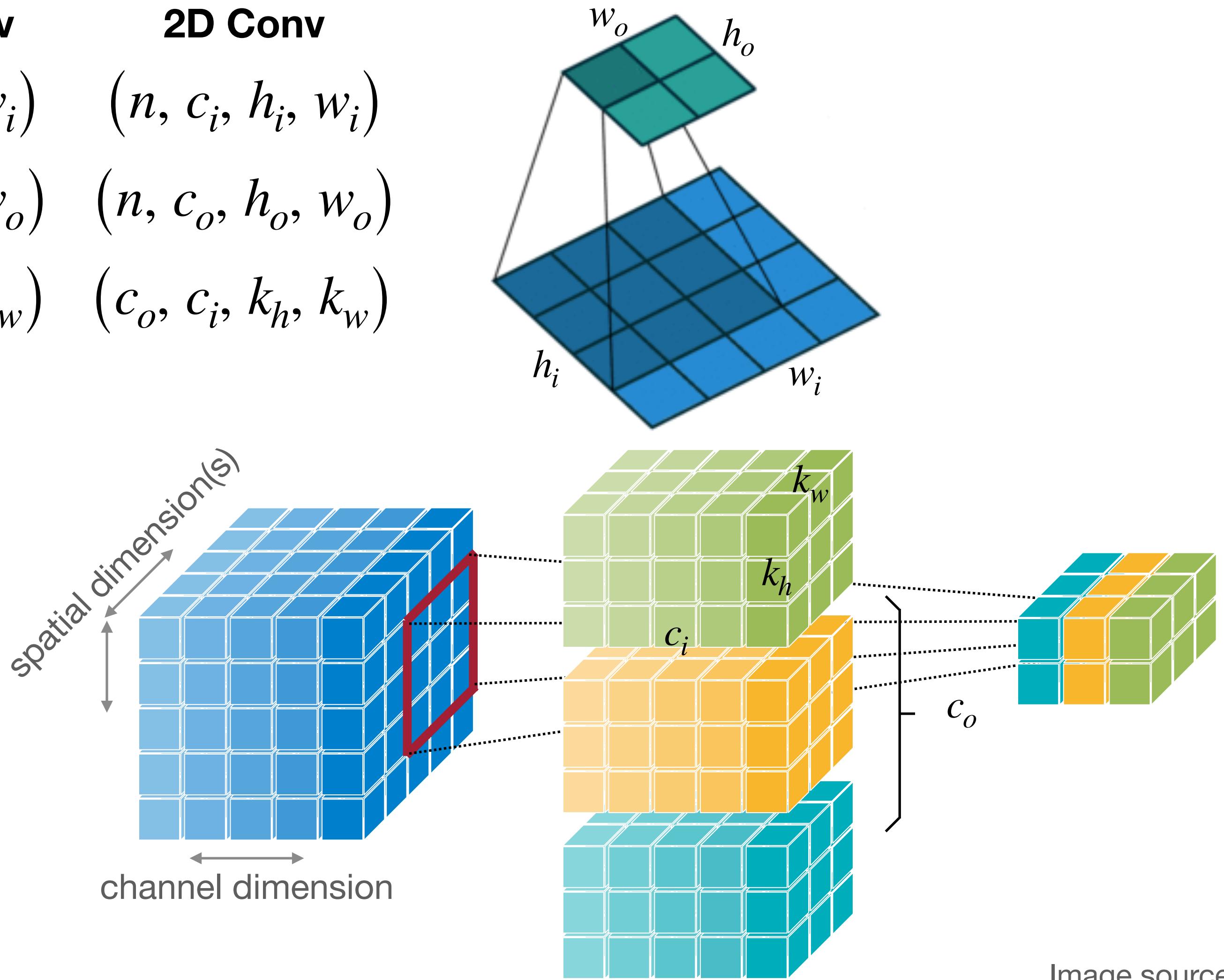


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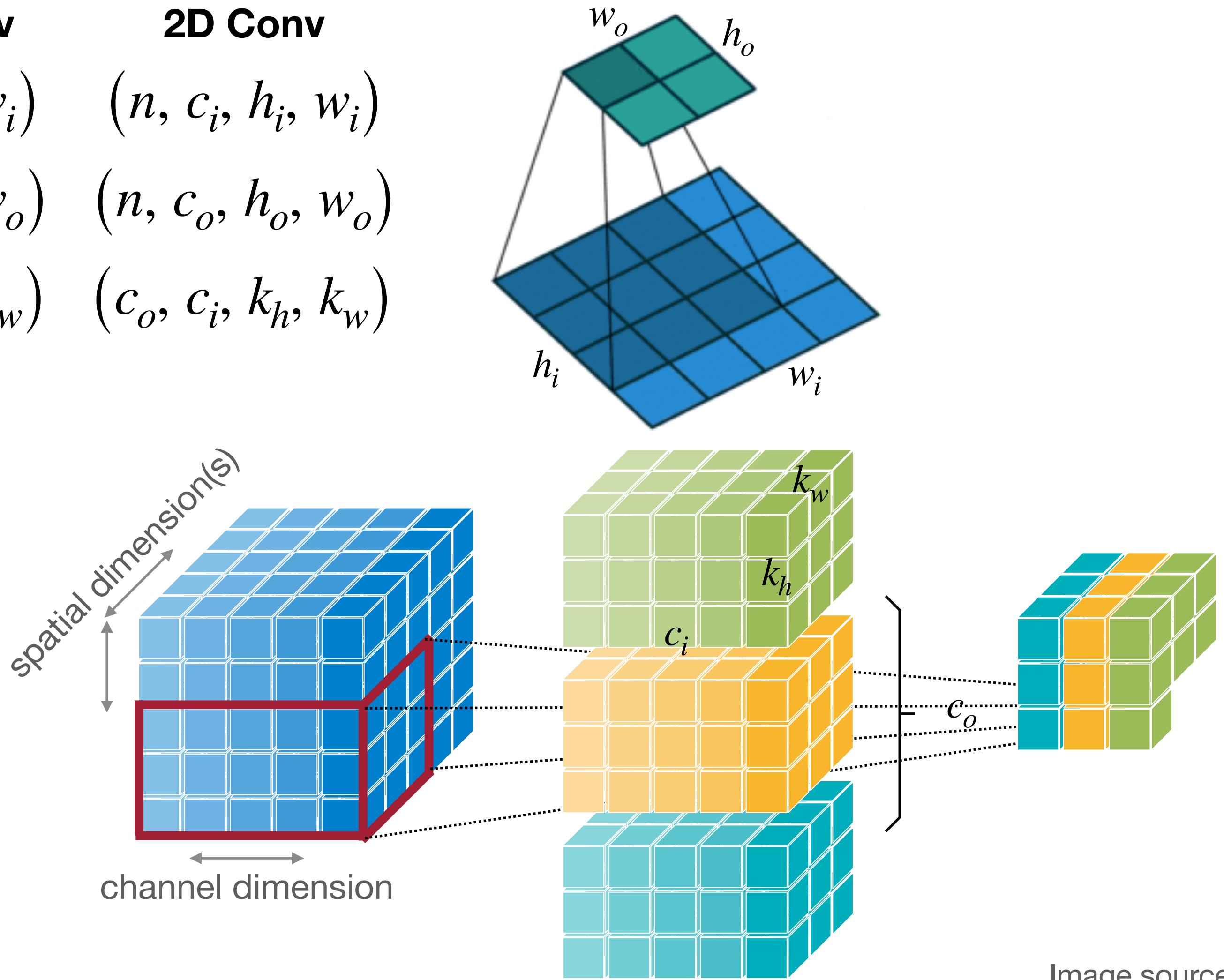


Image source: 1

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- | | | |
|---|-------------------|------------------------|
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| • Output Features \mathbf{Y} : (n, c_o) | (n, c_i, w_i) | (n, c_i, h_i, w_i) |
| • Weights \mathbf{W} : (c_o, c_i) | (c_o, c_i, k_w) | (c_o, c_i, k_h, k_w) |
| • Bias \mathbf{b} : $(c_o,)$ | | |

Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h	Kernel Height
k_w	Kernel Width

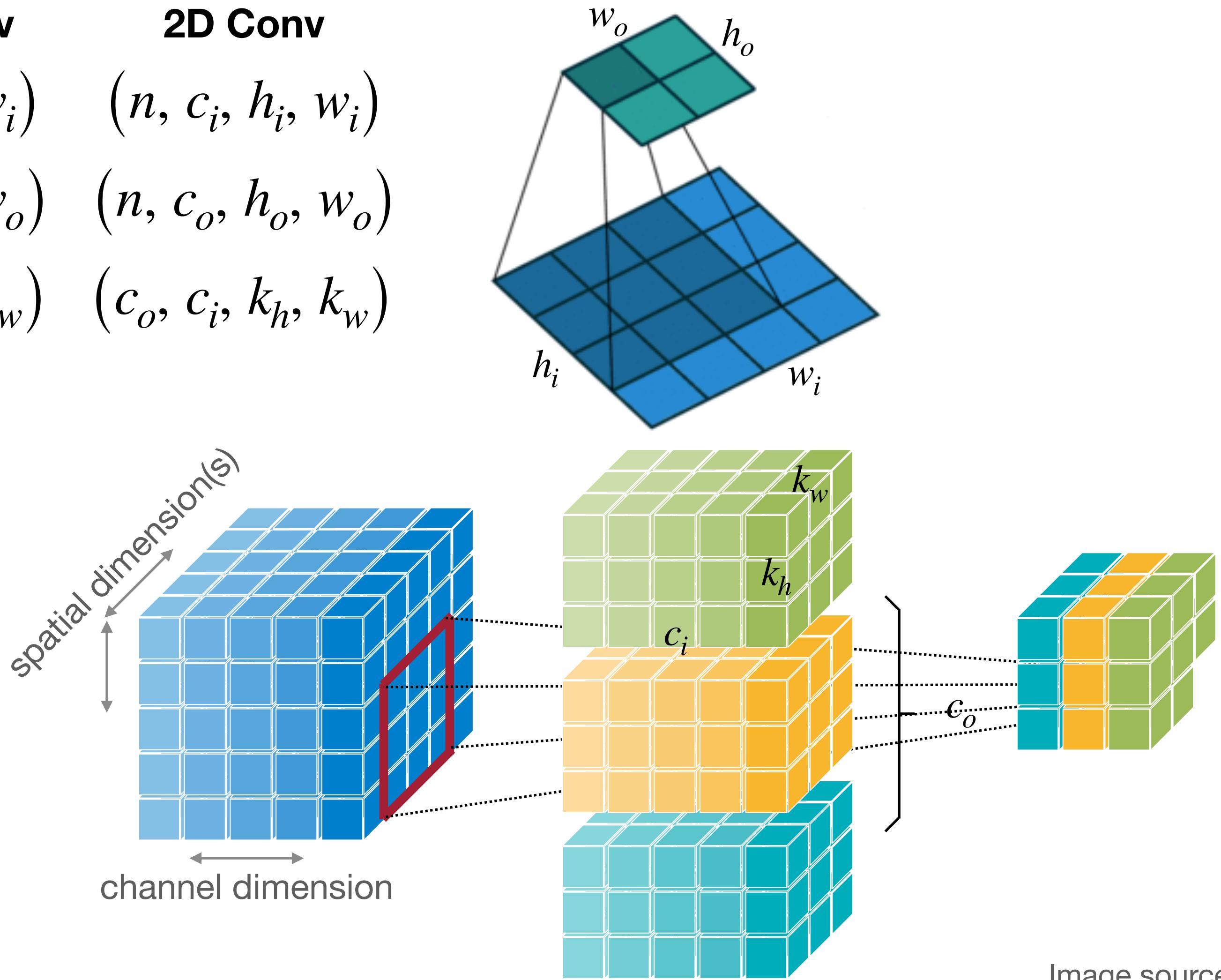


Image source: 1

Convolution Layer

The output neuron is connected to input neurons in the receptive field.

- **Shape of Tensors:**

- Input Features \mathbf{X} : (n, c_i) 1D Conv 2D Conv
 (n, c_i, w_i) (n, c_i, h_i, w_i)
- Output Features \mathbf{Y} : (n, c_o) (n, c_o, w_o) (n, c_o, h_o, w_o)
- Weights \mathbf{W} : (c_o, c_i) (c_o, c_i, k_w) (c_o, c_i, k_h, k_w)
- Bias \mathbf{b} : $(c_o,)$

Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h	Kernel Height
k_w	Kernel Width

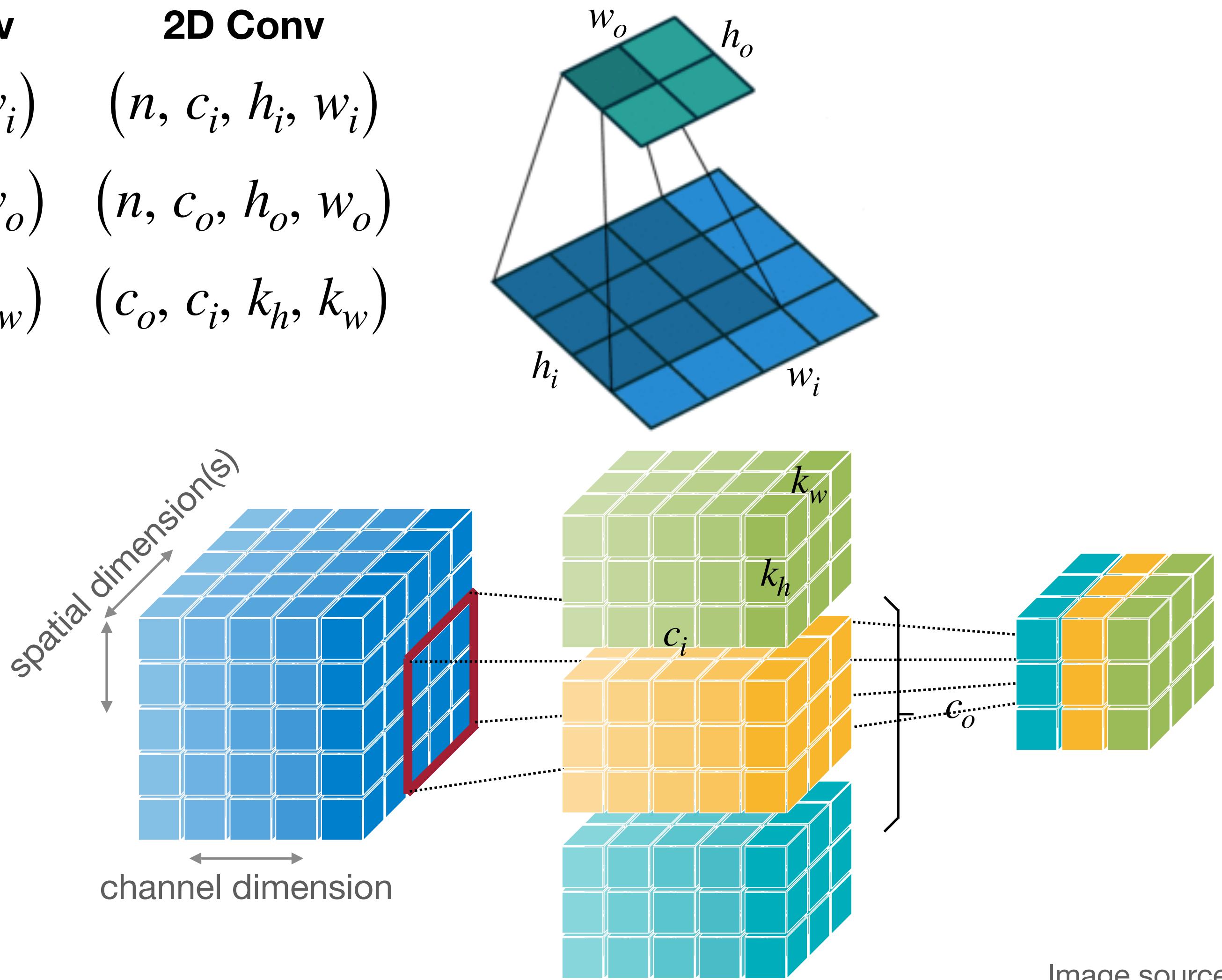


Image source: 1

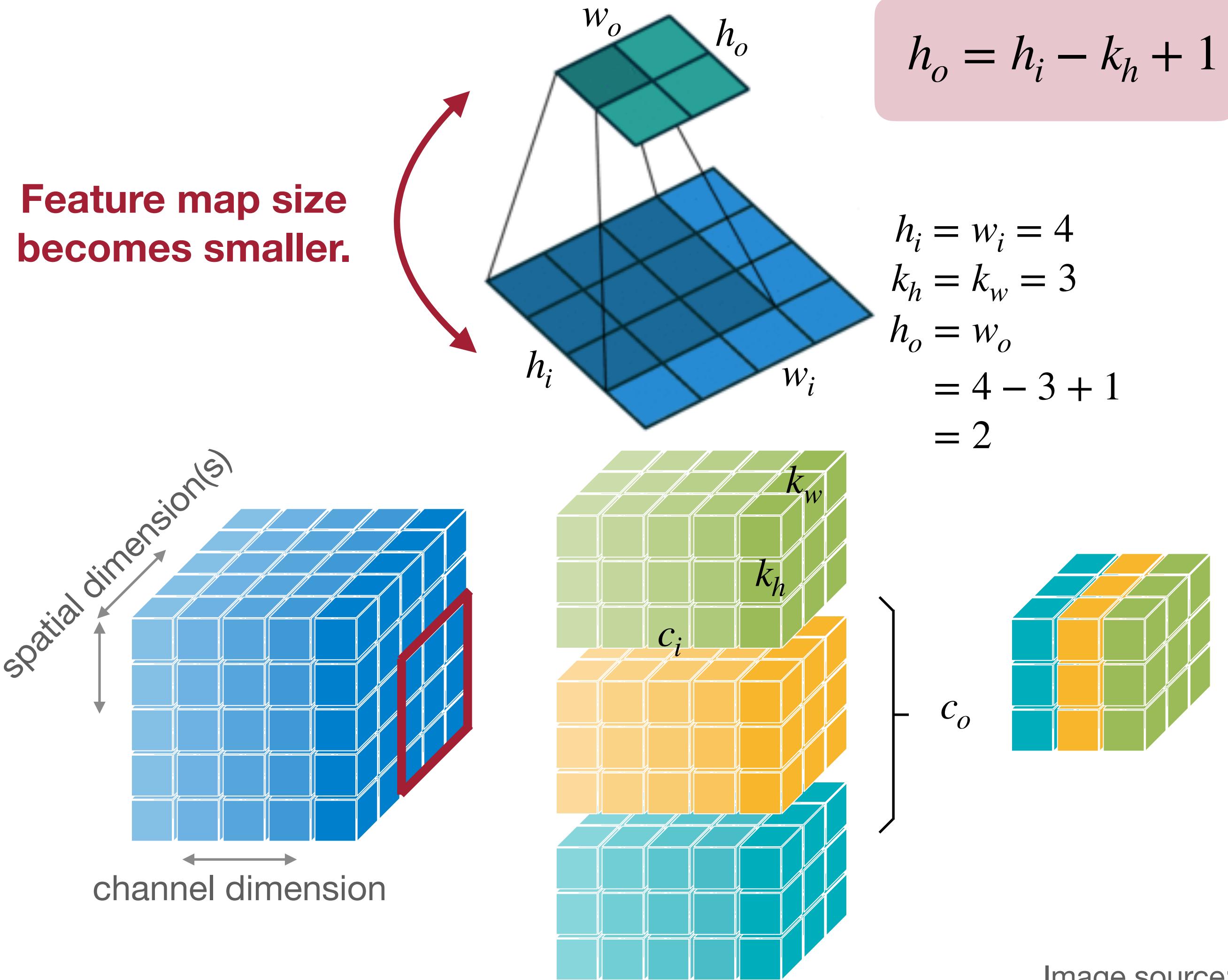
Convolution Layer

The output neuron is connected to input neurons in the receptive field.

- **Shape of Tensors:**

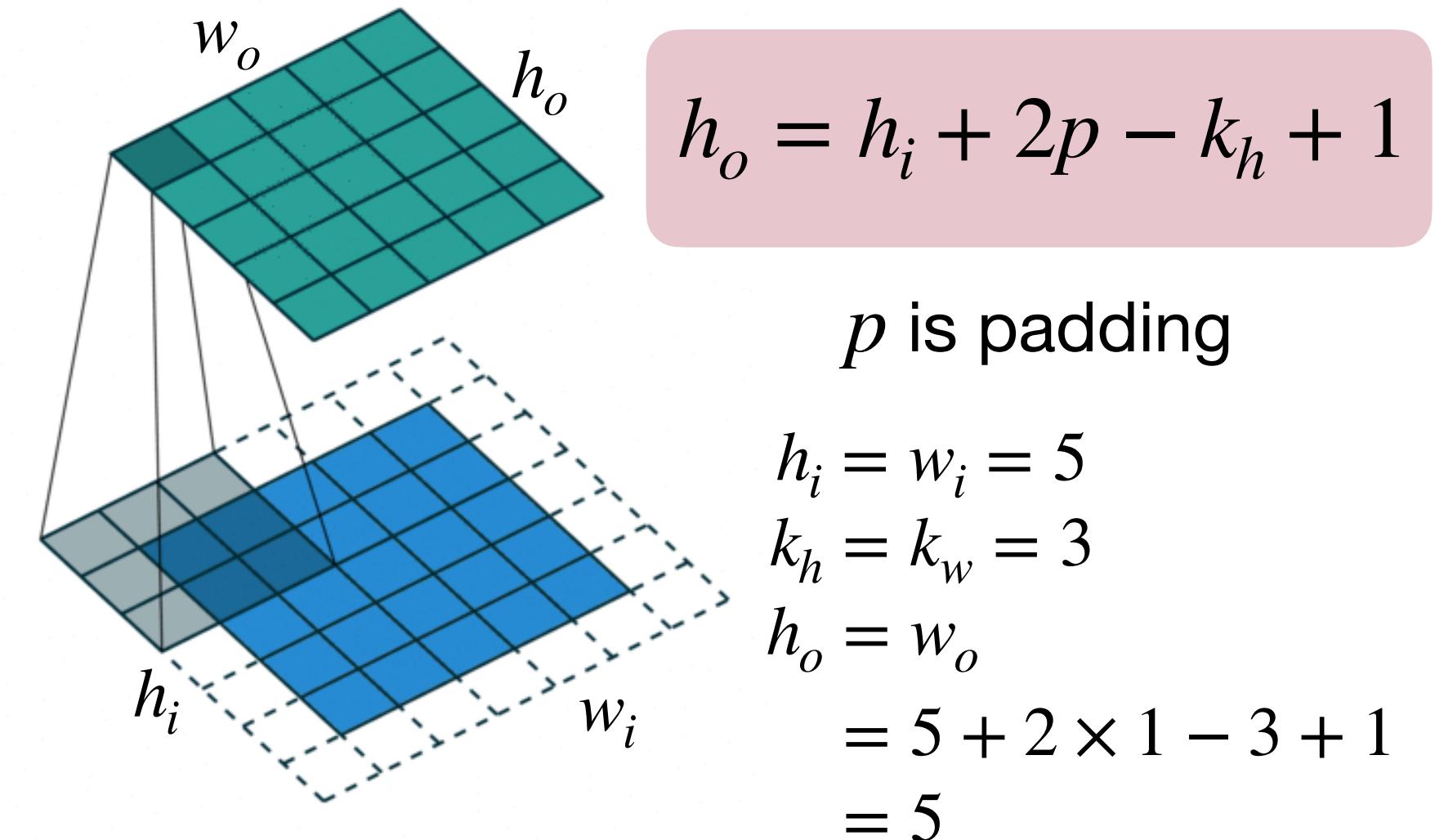
- Input Features \mathbf{X} : (n, c_i, h_i, w_i)
- Output Features \mathbf{Y} : (n, c_o, h_o, w_o)
- Weights \mathbf{W} : (c_o, c_i, k_h, k_w)
- Bias \mathbf{b} : $(c_o,)$

Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h	Kernel Height
k_w	Kernel Width



Convolution Layer: Padding

- Padding can be used to keep the output feature map size the same as input feature map size
 - Zero Padding** pads the input boundaries with zero.
(Default in PyTorch)
 - Other Paddings: Reflection Padding, Replication Padding, Constant Padding



Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h	Kernel Height
k_w	Kernel Width

Zero Padding						
0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	0	1	2	3	0	0
0	0	4	5	6	0	0
0	0	7	8	9	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

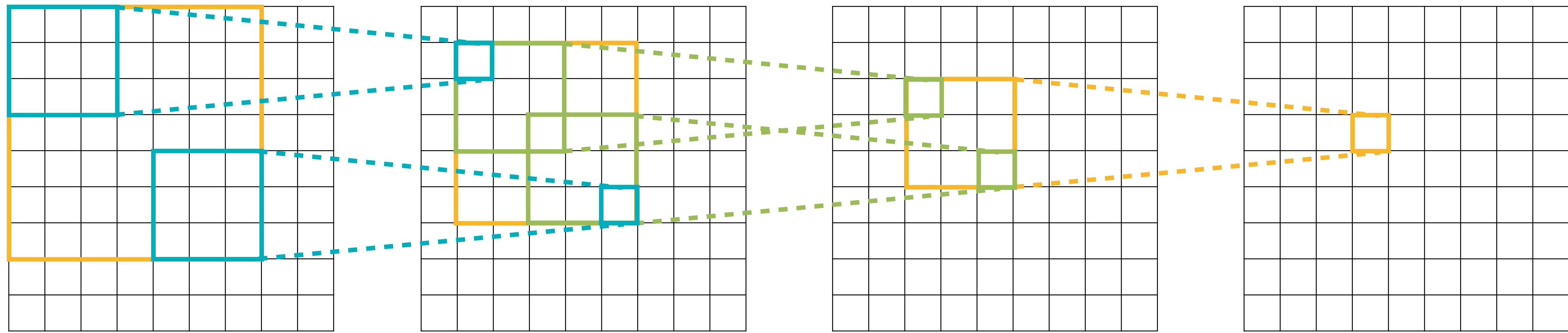
Reflection Padding						
9	8	7	8	9	8	7
6	5	4	5	6	4	5
3	2	1	2	3	2	1
6	5	4	5	6	5	4
9	8	7	8	9	8	7
6	5	4	5	6	5	4
3	2	1	2	3	2	1

Replication Padding						
1	1	1	2	3	3	3
1	1	1	2	3	3	3
1	1	1	2	3	3	3
4	4	4	5	6	6	6
7	7	7	8	9	9	9
7	7	7	8	9	9	9
7	7	7	8	9	9	9

Image source: 1

Convolution Layer: Receptive Field

- In convolution, each output element depends on $k_h \times k_w$ receptive field in the input.
- Each successive convolution adds $k - 1$ to the receptive field size
- With L layers, the receptive field size is $L \cdot (k - 1) + 1$



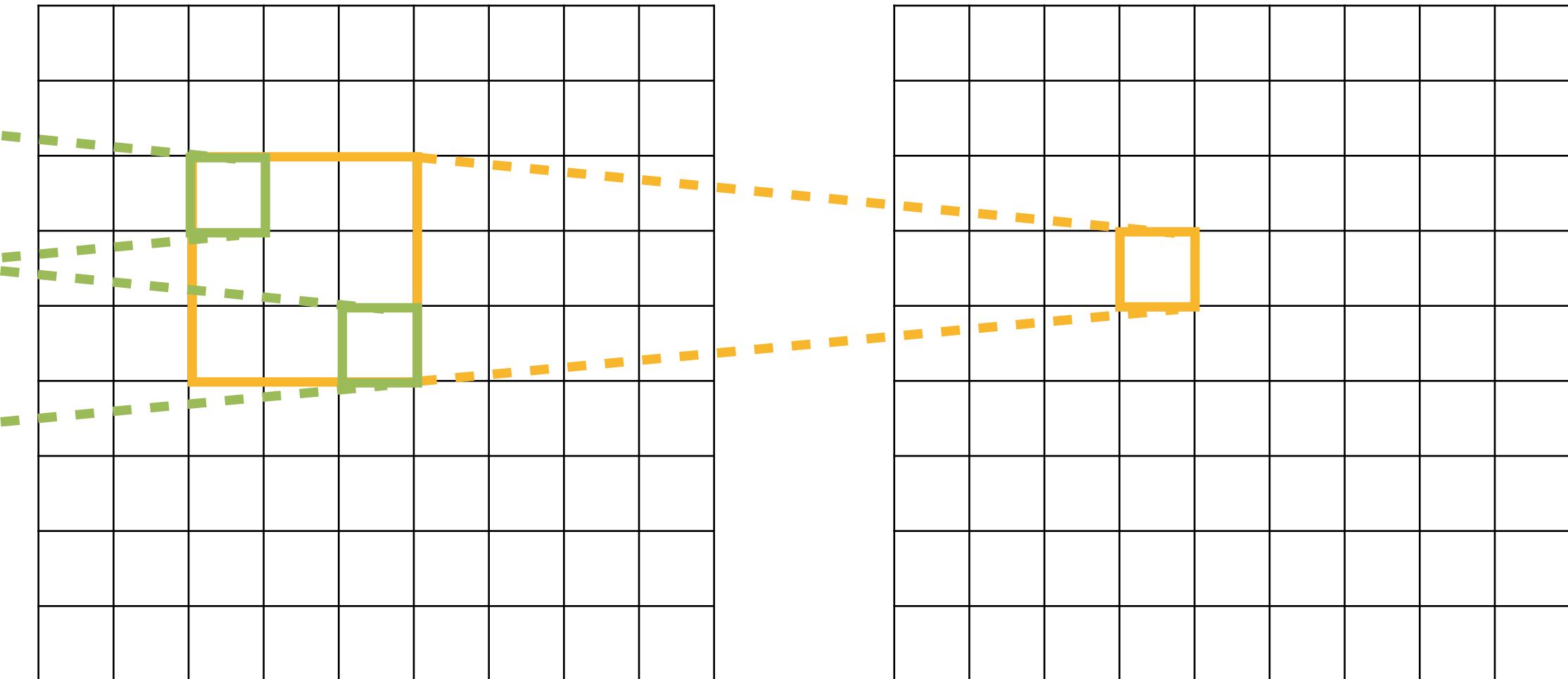
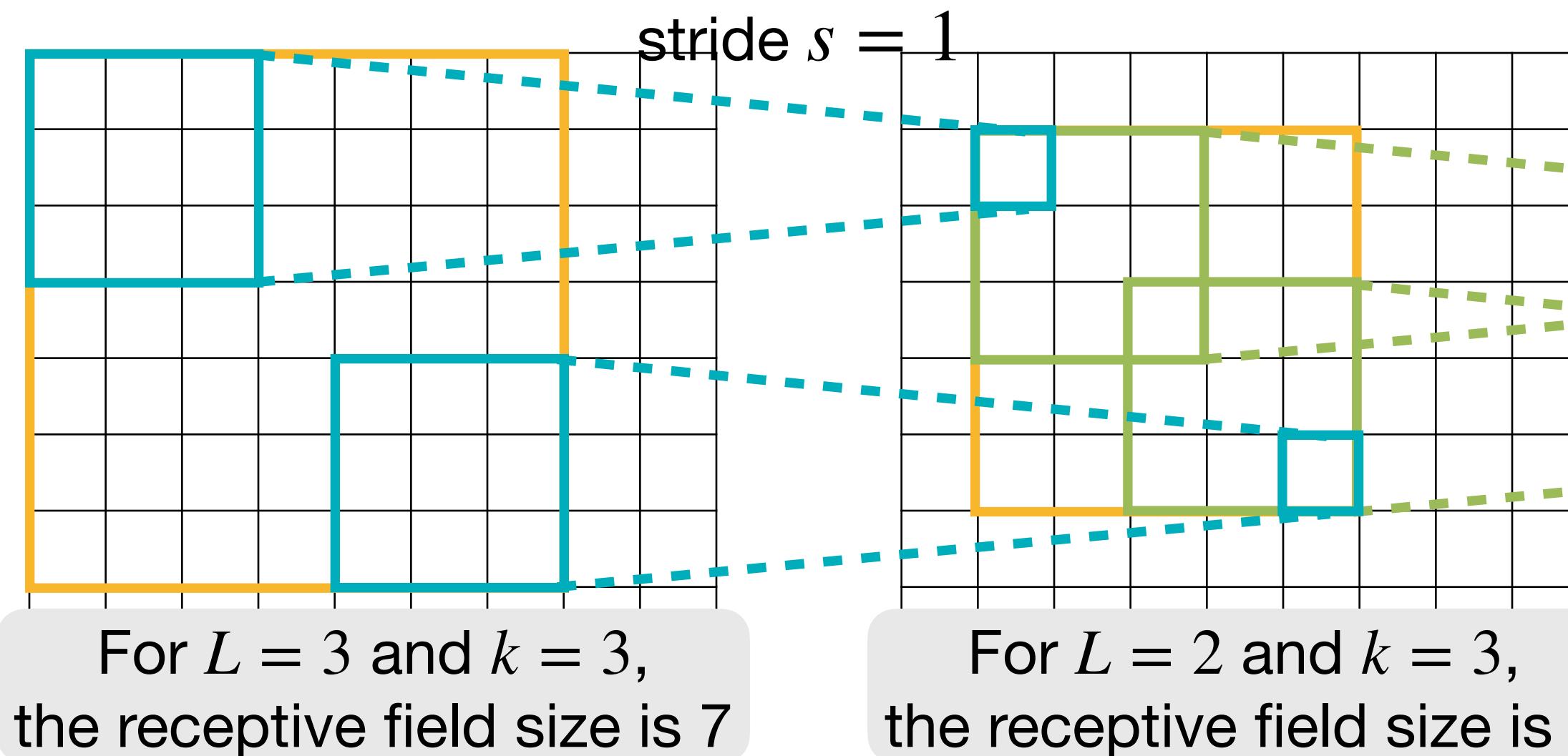
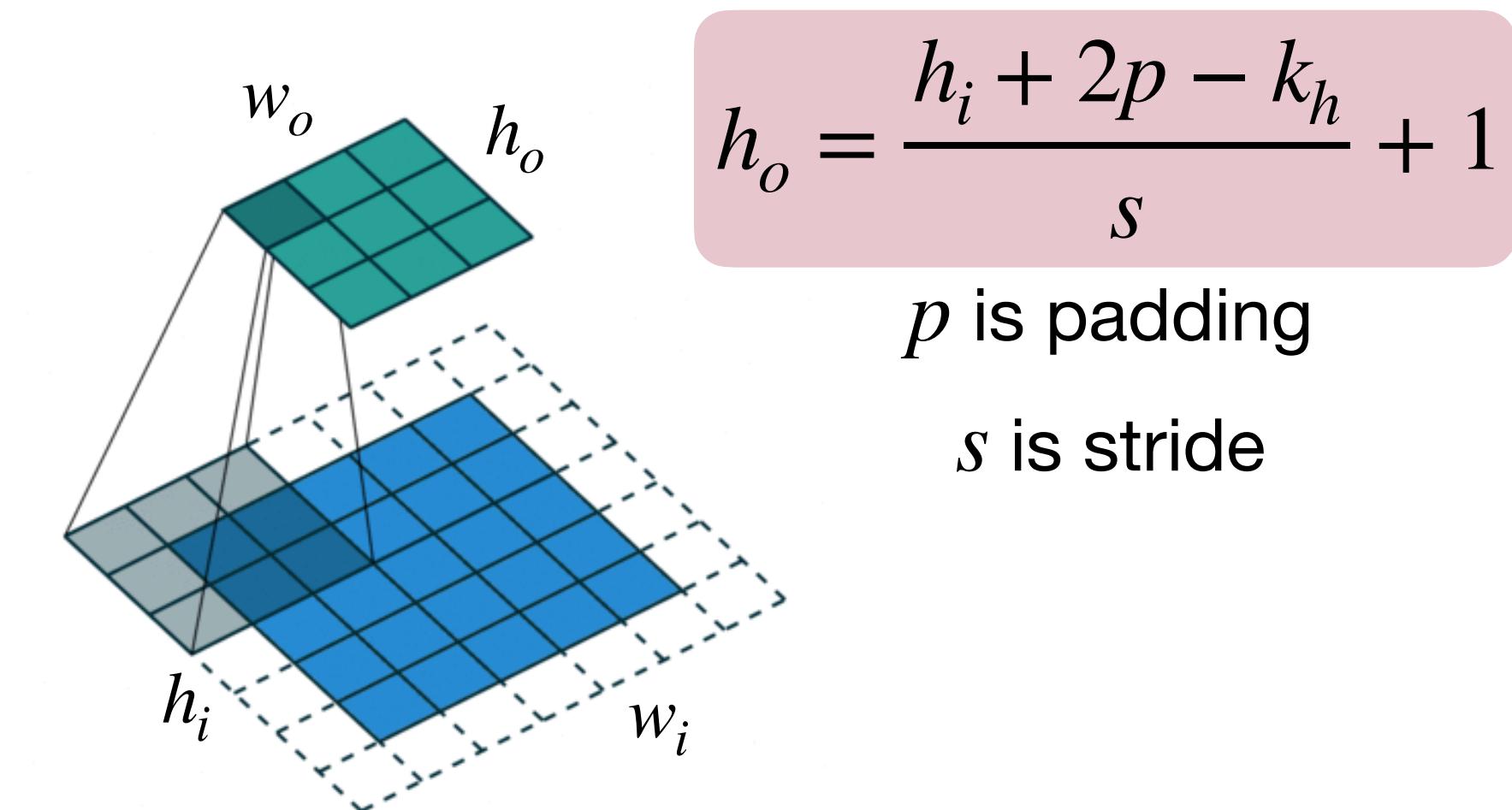
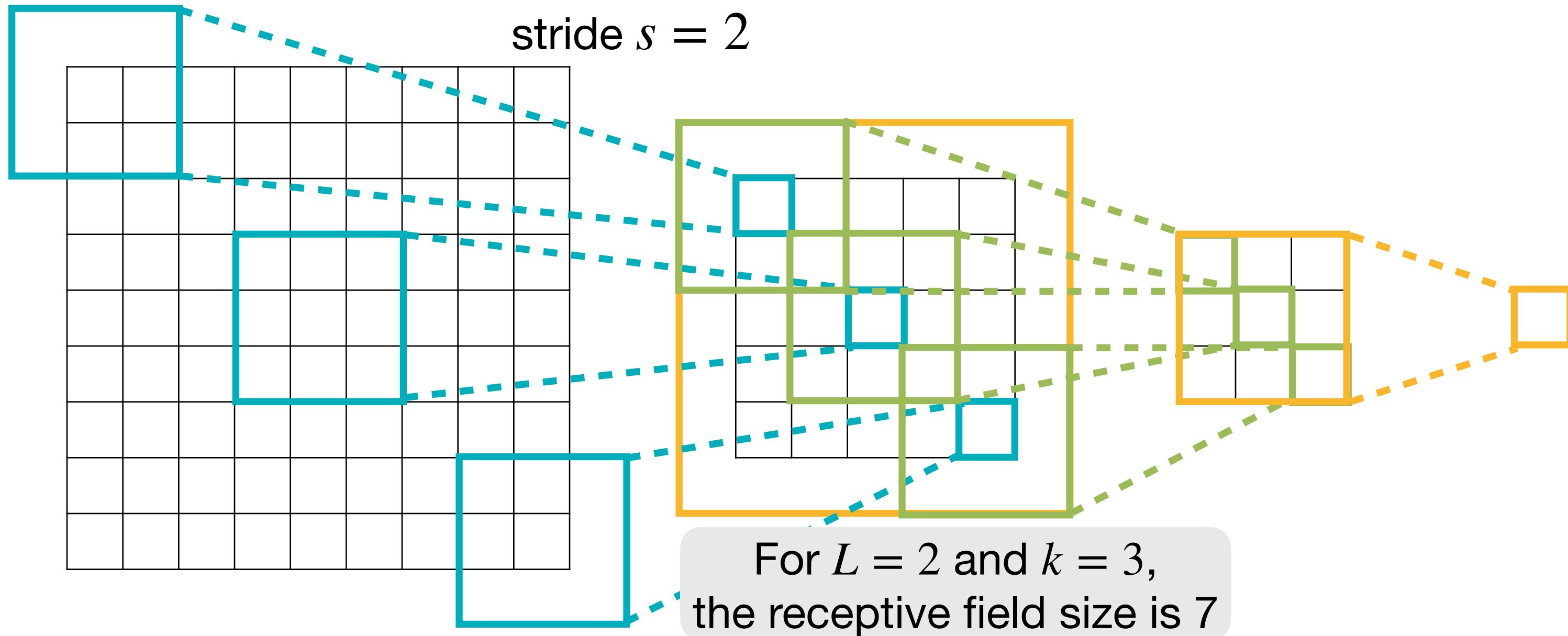
For $L = 2$ and $k = 3$, the receptive field size is 5

For $L = 3$ and $k = 3$, the receptive field size is 7

Problem: For large images, we need many layers for each output to “see” the whole image
Solution: Downsample inside the neural network

Slide Inspiration: [Ruohan Gao](#)

Strided Convolution Layer



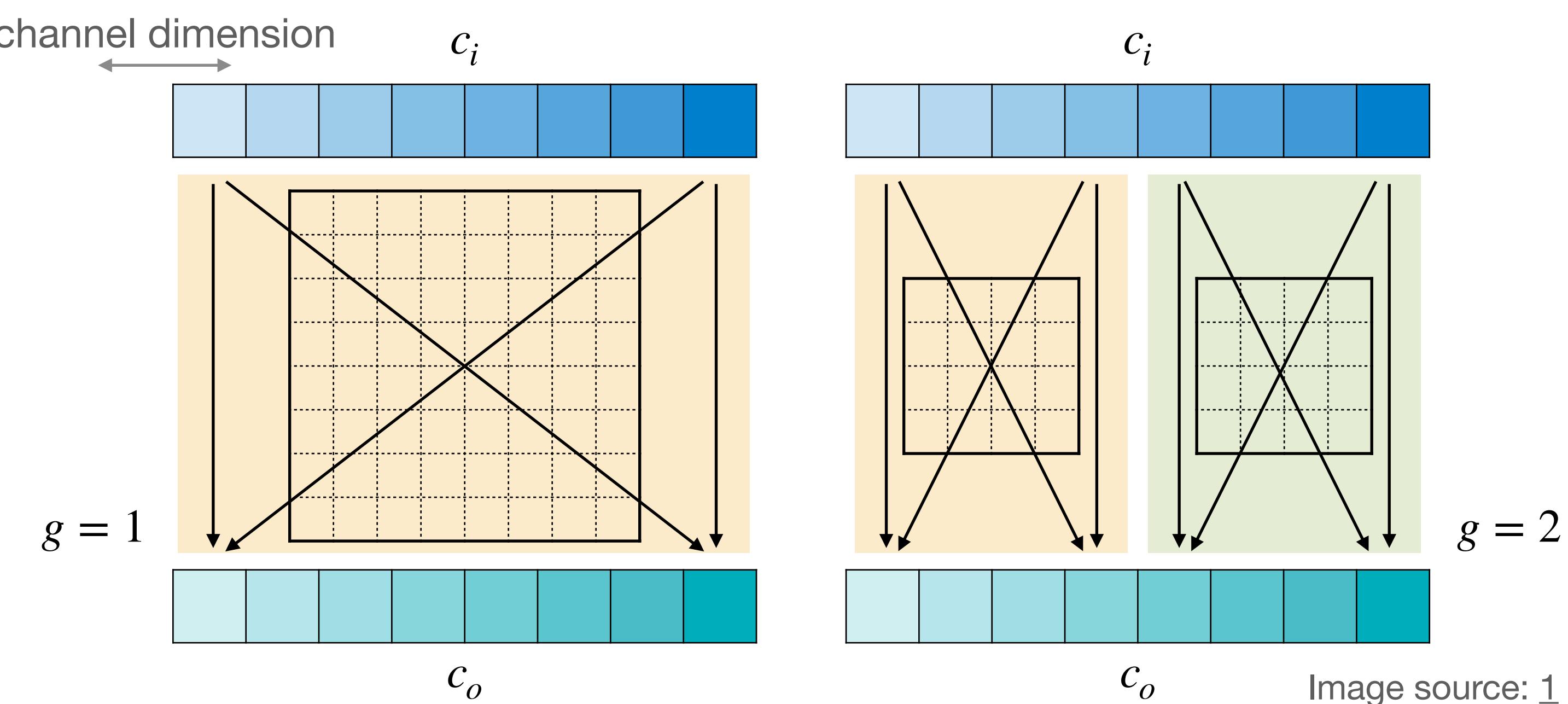
Grouped Convolution Layer

A group of narrower convolutions

- **Shape of Tensors:**

- Input Features $\mathbf{X} : (n, c_i, h_i, w_i)$
- Output Features $\mathbf{Y} : (n, c_o, h_o, w_o)$
- Weights $\mathbf{W} : (c_o, c_i, k_h, k_w) \quad (g \cdot c_o/g, c_i/g, k_h, k_w)$
- Bias $\mathbf{b} : (c_o,)$

Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h	Kernel Height
k_w	Kernel Width
g	Groups



Depthwise Convolution Layer

Independent filter for each channel: $g = c_i = c_o$ in grouped convolution

- **Shape of Tensors:**

- Input Features $\mathbf{X} : (n, c_i, h_i, w_i)$
- Output Features $\mathbf{Y} : (n, c_o, h_o, w_o)$
- Weights $\mathbf{W} : (c_o, c_i, k_h, k_w) \quad (c, k_h, k_w)$
- Bias $\mathbf{b} : (c_o,)$

Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h	Kernel Height
k_w	Kernel Width
g	Groups

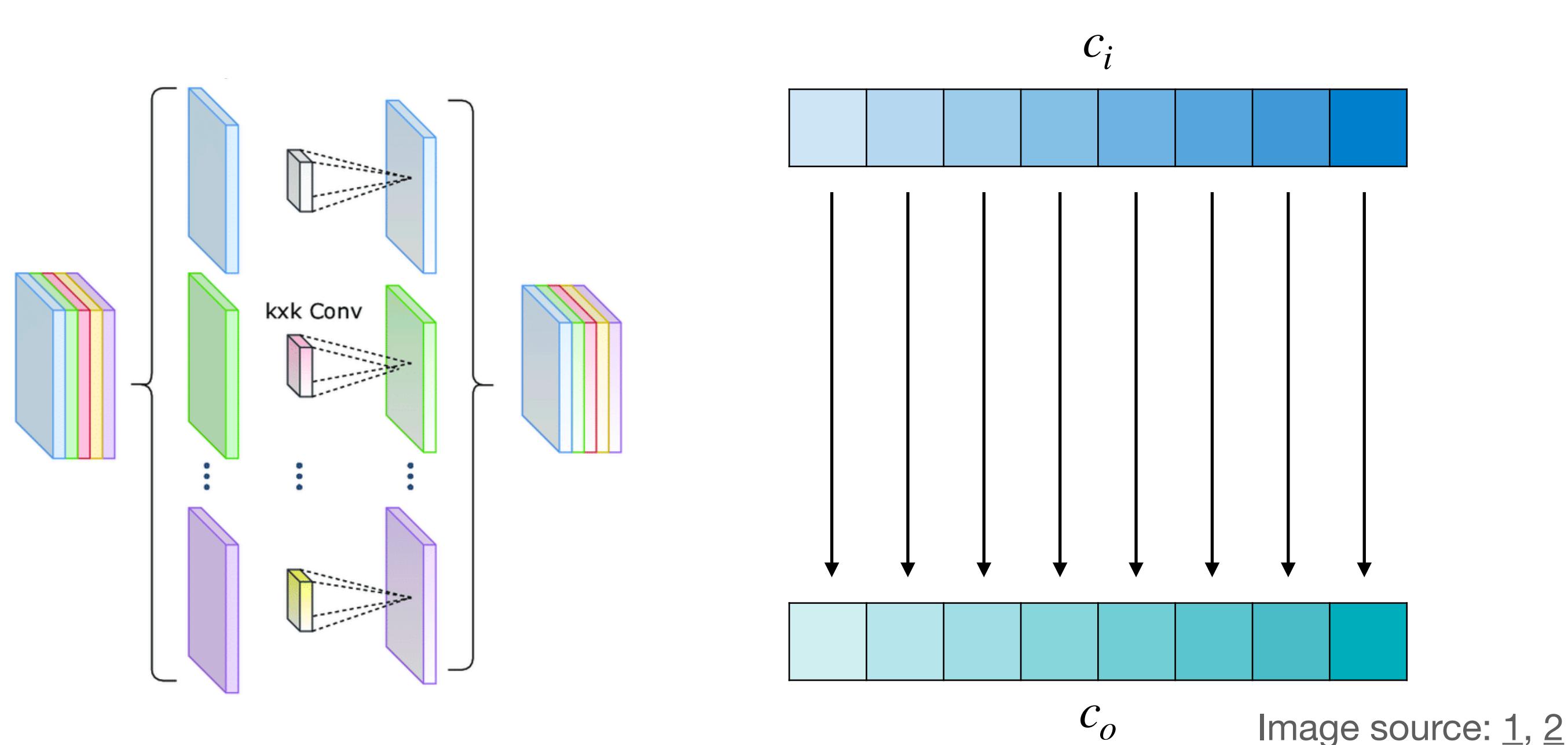
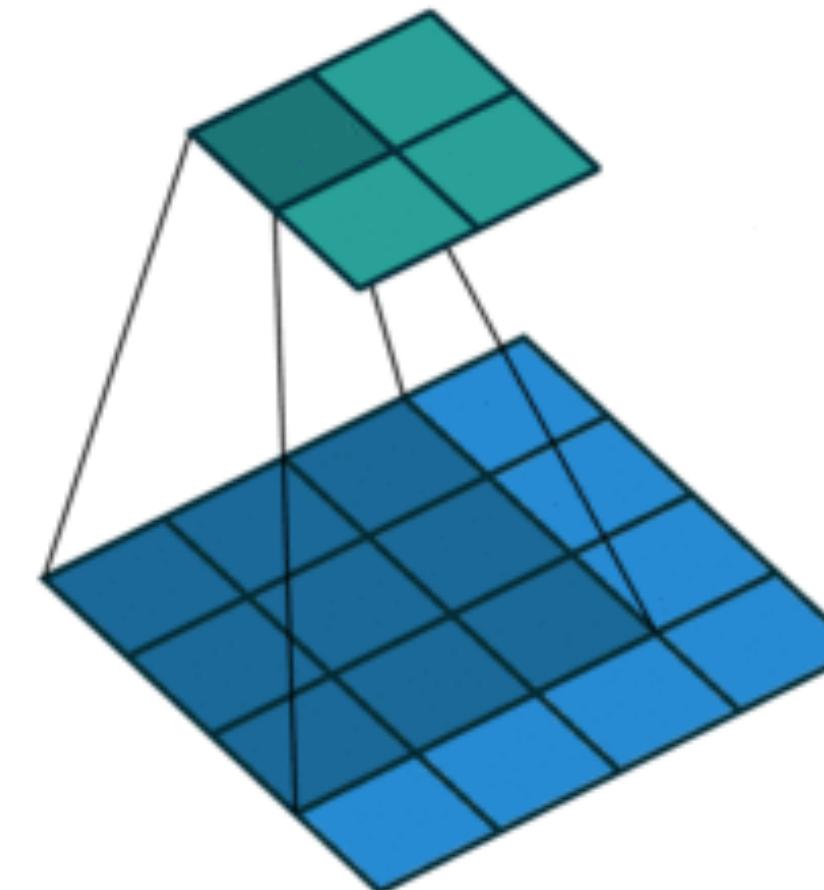


Image source: 1, 2

Pooling Layer

Downsample the feature map to a smaller size

- The output neuron pools the features in the receptive field, similar to convolution.
 - Usually, the stride is the same as the kernel size: $s = k$
- Pooling operates over each channel independently.
- No learnable parameters



stride = kernel size = 2

5	0	1	7
2	1	3	5
0	2	3	1
2	8	1	3

Input Feature Map

Max Pooling

5	7
8	3

Average Pooling

2	4
3	2

Output Feature Map

Slide Inspiration: [Ruohan Gao](#)

Image source: [1](#)

Normalization Layer

Normalizing the features makes optimization faster.

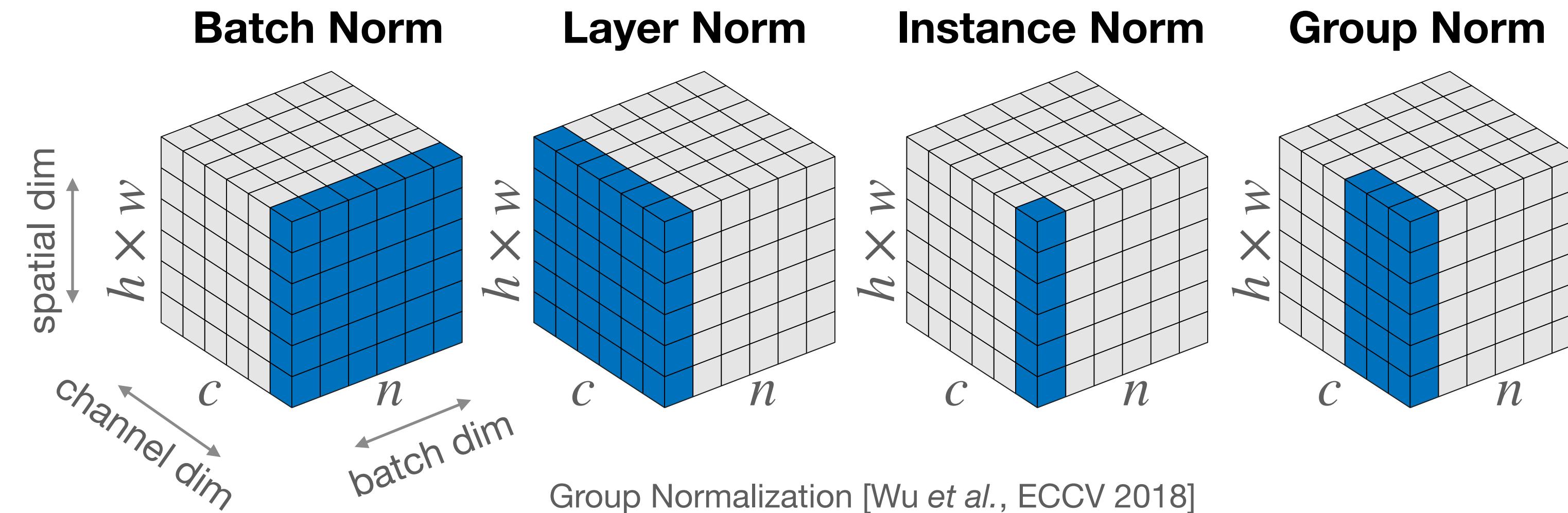
- Normalization layer normalizes the features as follows,

$$\hat{x}_i = \frac{1}{\sigma} (x_i - \mu_i)$$

$$\mu_i = \frac{1}{m} \sum_{k \in \mathcal{S}_i} x_k$$
$$\sigma_i = \sqrt{\frac{1}{m} \sum_{k \in \mathcal{S}_i} (x_k - \mu_i)^2 + \epsilon}$$

- μ_i is the mean, and σ_i is the standard deviation (std) over the set of pixels \mathcal{S}_i .
- Then learns a *per-channel* linear transform (trainable scale γ and shift β) to compensate for the possible lost of representational ability.

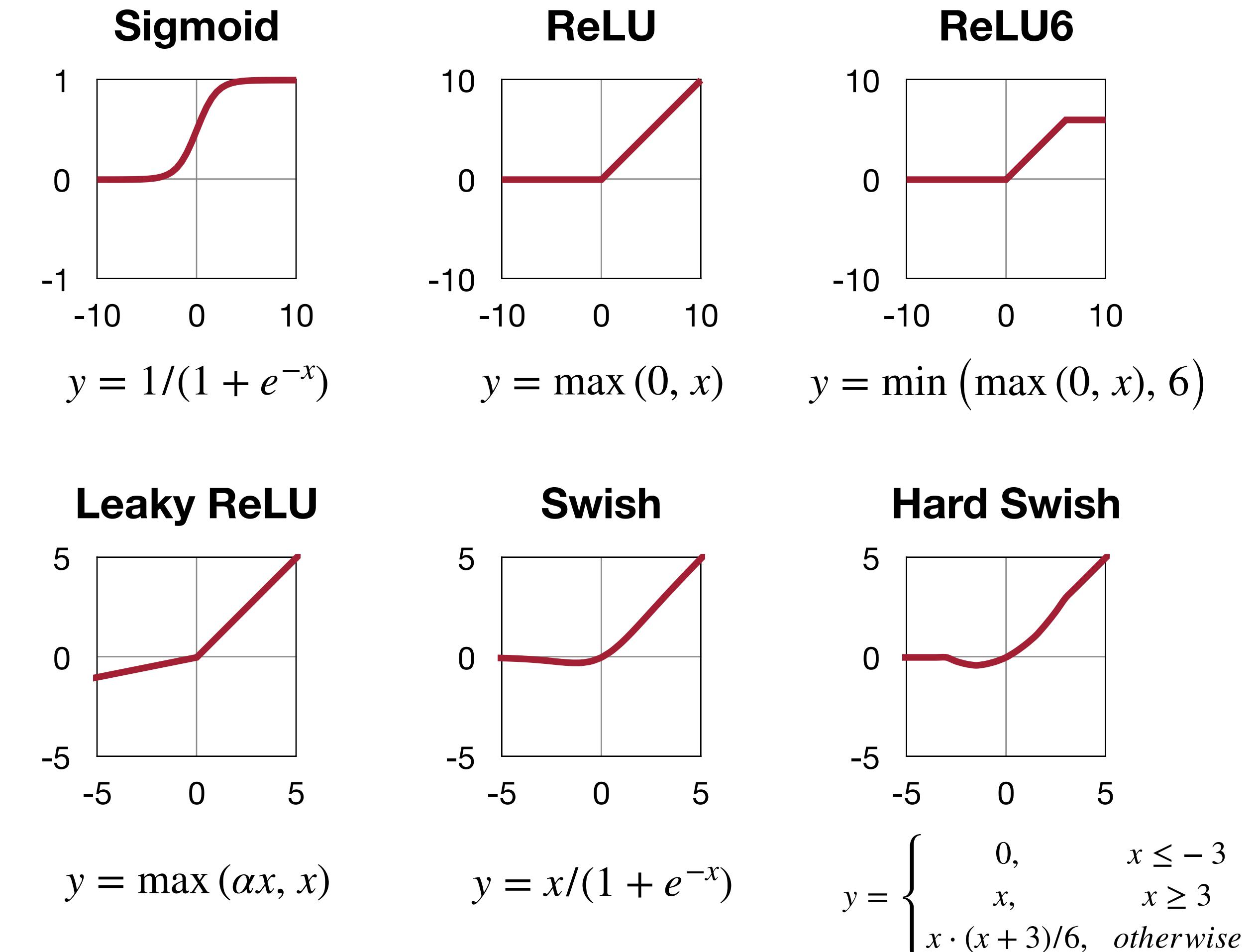
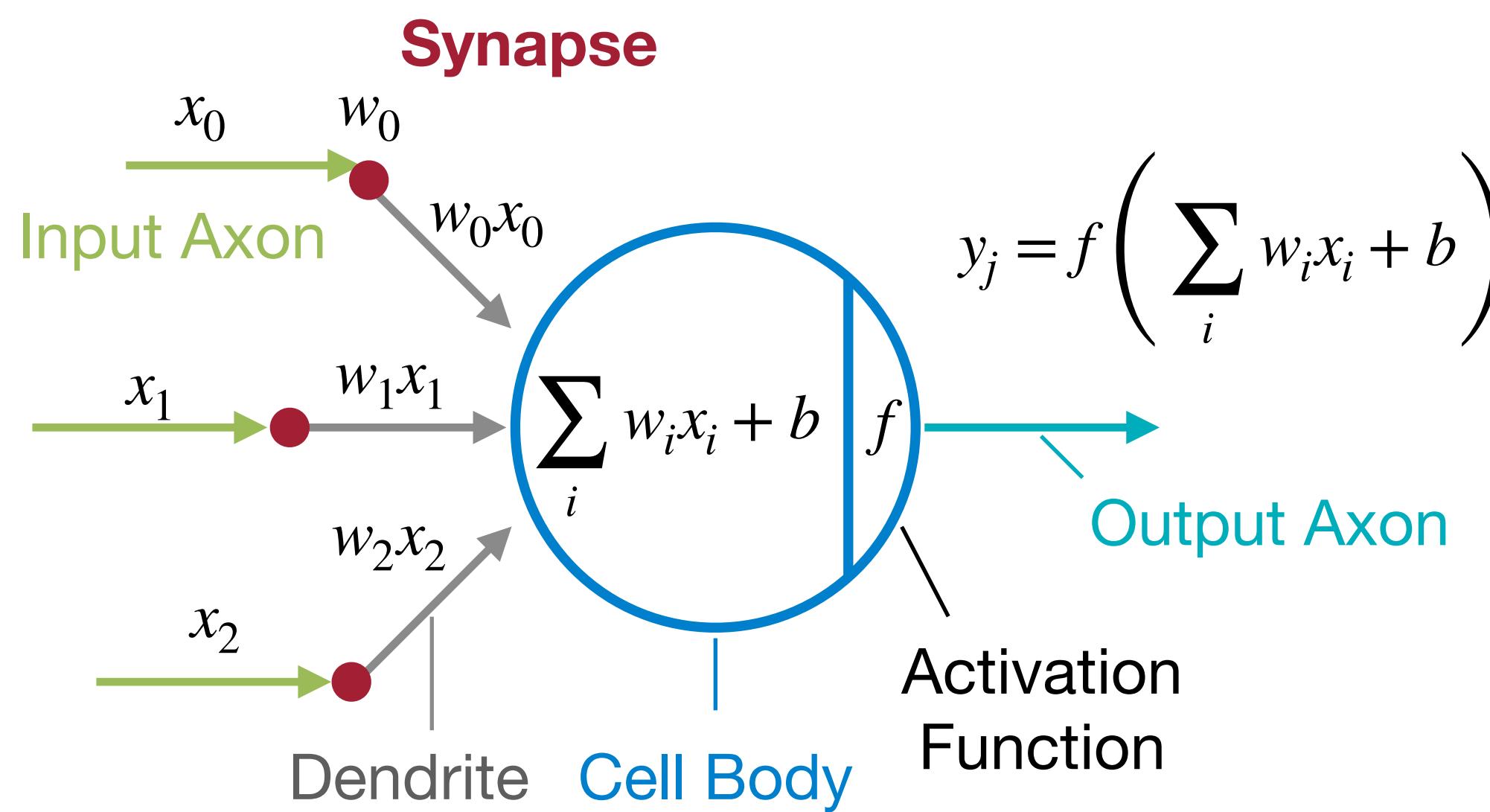
$$y = \gamma_{i_c} \hat{x}_i + \beta_{i_c}$$



Different normalizations use different definitions of the set \mathcal{S}_i (colored in blue)

Activation Function

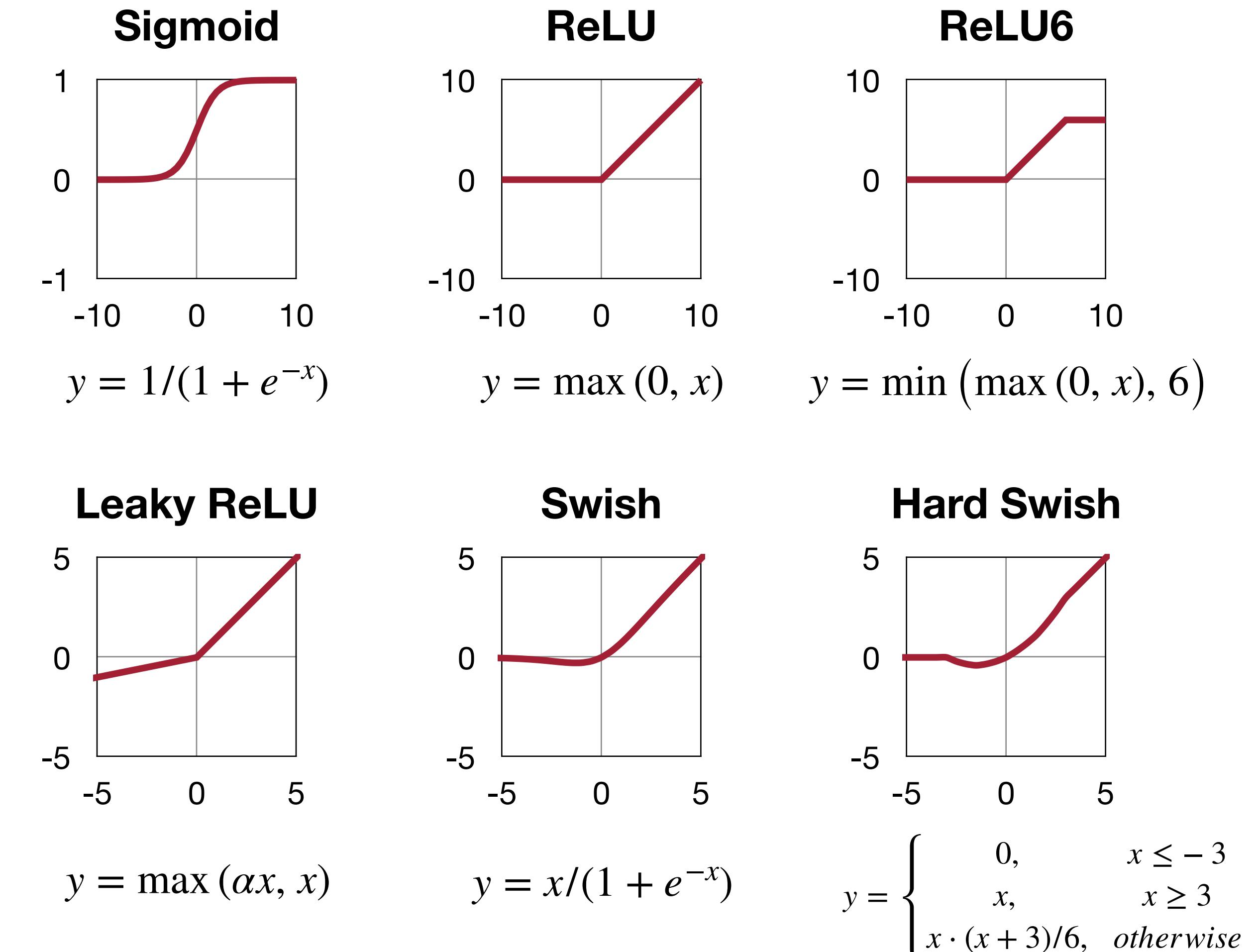
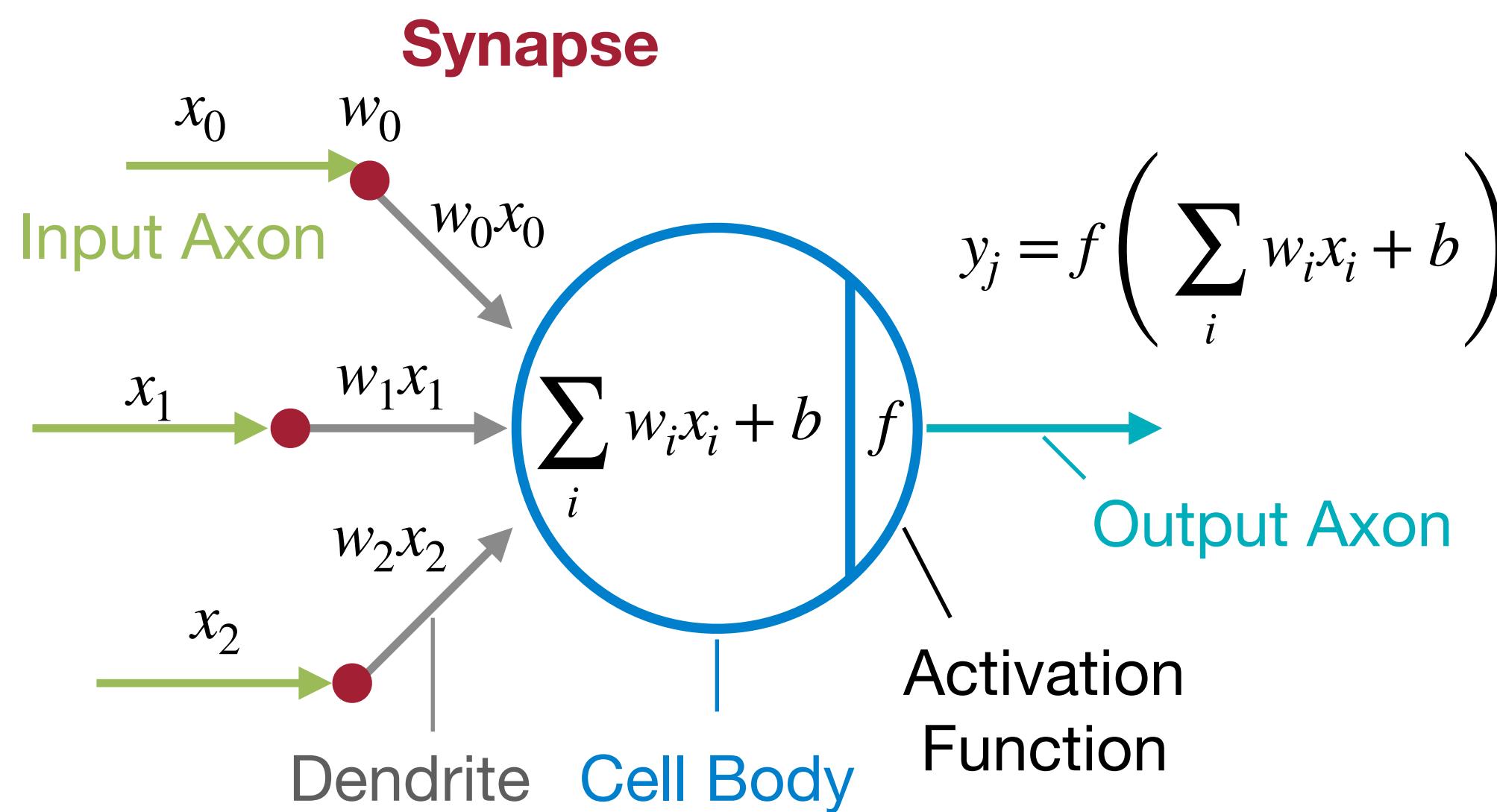
Activation functions are typically non-linear functions



Other Activation Functions: Tanh, GELU, ELU, Mish...

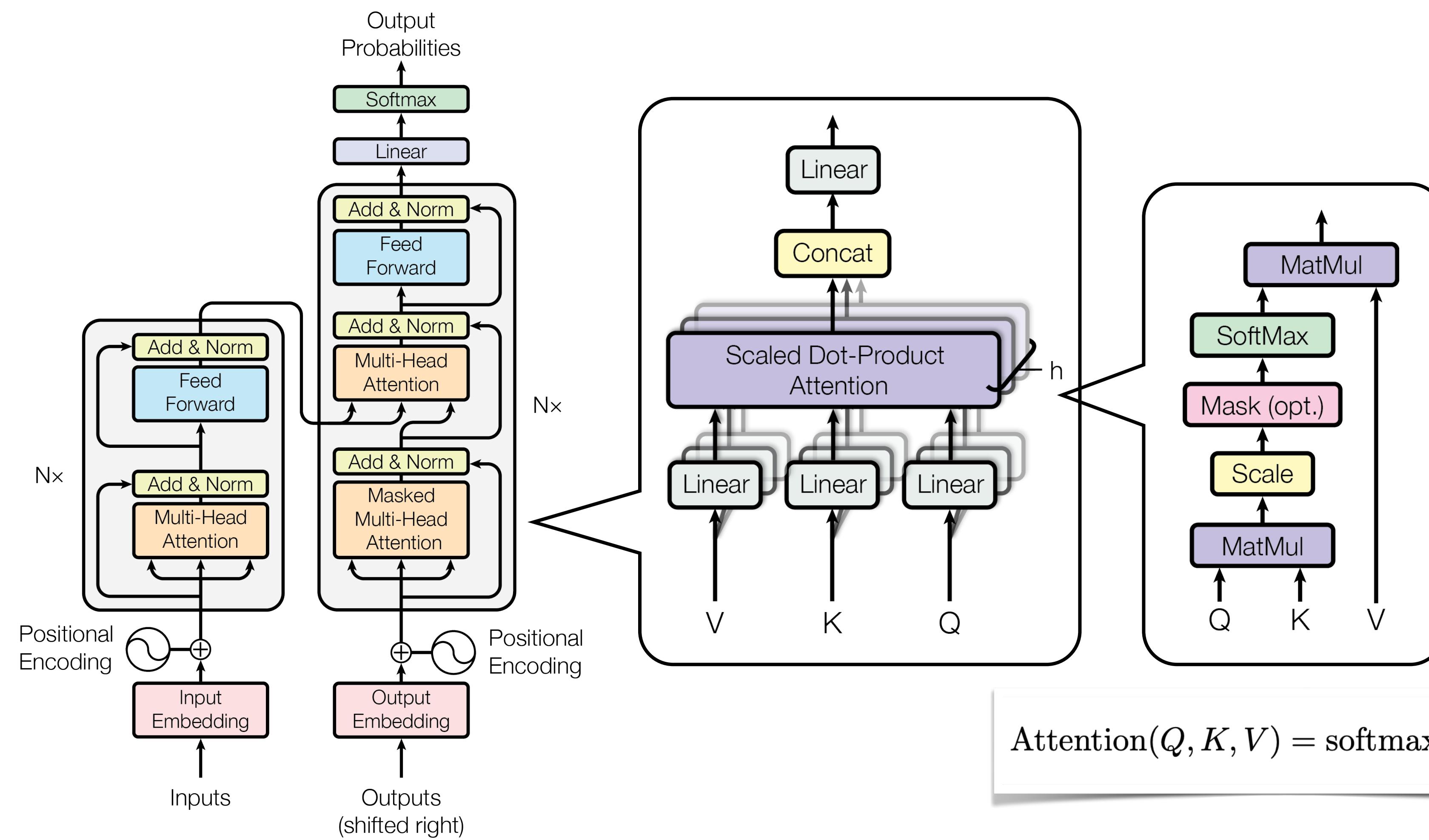
Activation Function

Activation functions are typically non-linear functions



Other Activation Functions: Tanh, GELU, ELU, Mish...

Transformer



Attention is All You Need [Vaswani et al., NeurIPS 2017]

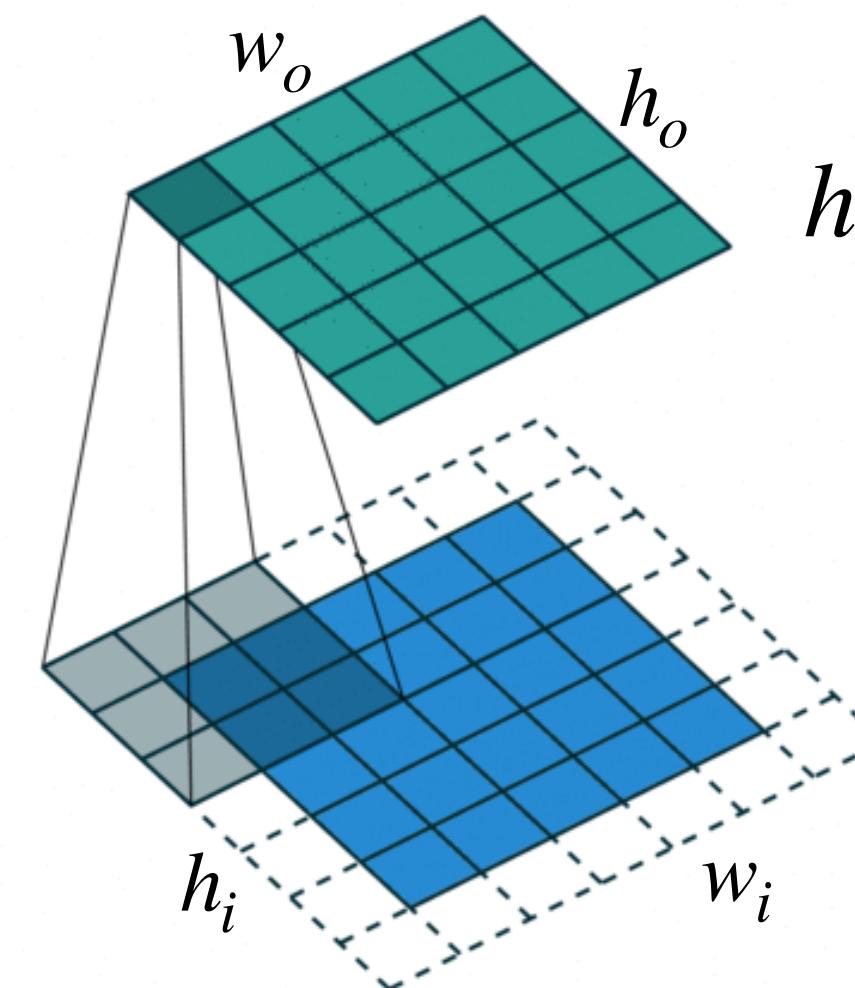
Popular CNN Architectures

AlexNet

AlexNet

	C × H × W	H, W
Image (3×224×224)	3×224×224	
11×11 Conv, channel 96, stride 4, pad 2	96×55×55	$\frac{224 + 2 \times 2 - 11}{4} + 1 = 55$
3×3 MaxPool, stride 2	96×27×27	$\frac{55 + 0 - 3}{2} + 1 = 27$
5×5 Conv, channel 256, pad 2, groups 2	256×27×27	$\frac{27 + 2 \times 2 - 5}{1} + 1 = 27$
3×3 MaxPool, stride 2	256×13×13	$\frac{27 + 0 - 3}{2} + 1 = 13$
3×3 Conv, channel 384, pad 1	384×13×13	$\frac{13 + 2 \times 1 - 3}{1} + 1 = 13$
3×3 Conv, channel 384, pad 1, groups 2	384×13×13	$\frac{13 + 2 \times 1 - 3}{1} + 1 = 13$
3×3 Conv, channel 256, pad 1, groups 2	256×13×13	$\frac{13 + 2 \times 1 - 3}{1} + 1 = 13$
3×3 MaxPool, stride 2	256×6×6	$\frac{13 + 0 - 3}{2} + 1 = 6$
Linear, channel 4096	4096	
Linear, channel 4096	4096	
Linear, channel 1000	1000	

Convolution Layer / Pooling Layer



$$h_o = \frac{h_i + 2p - k_h}{s} + 1$$

p is padding

s is stride

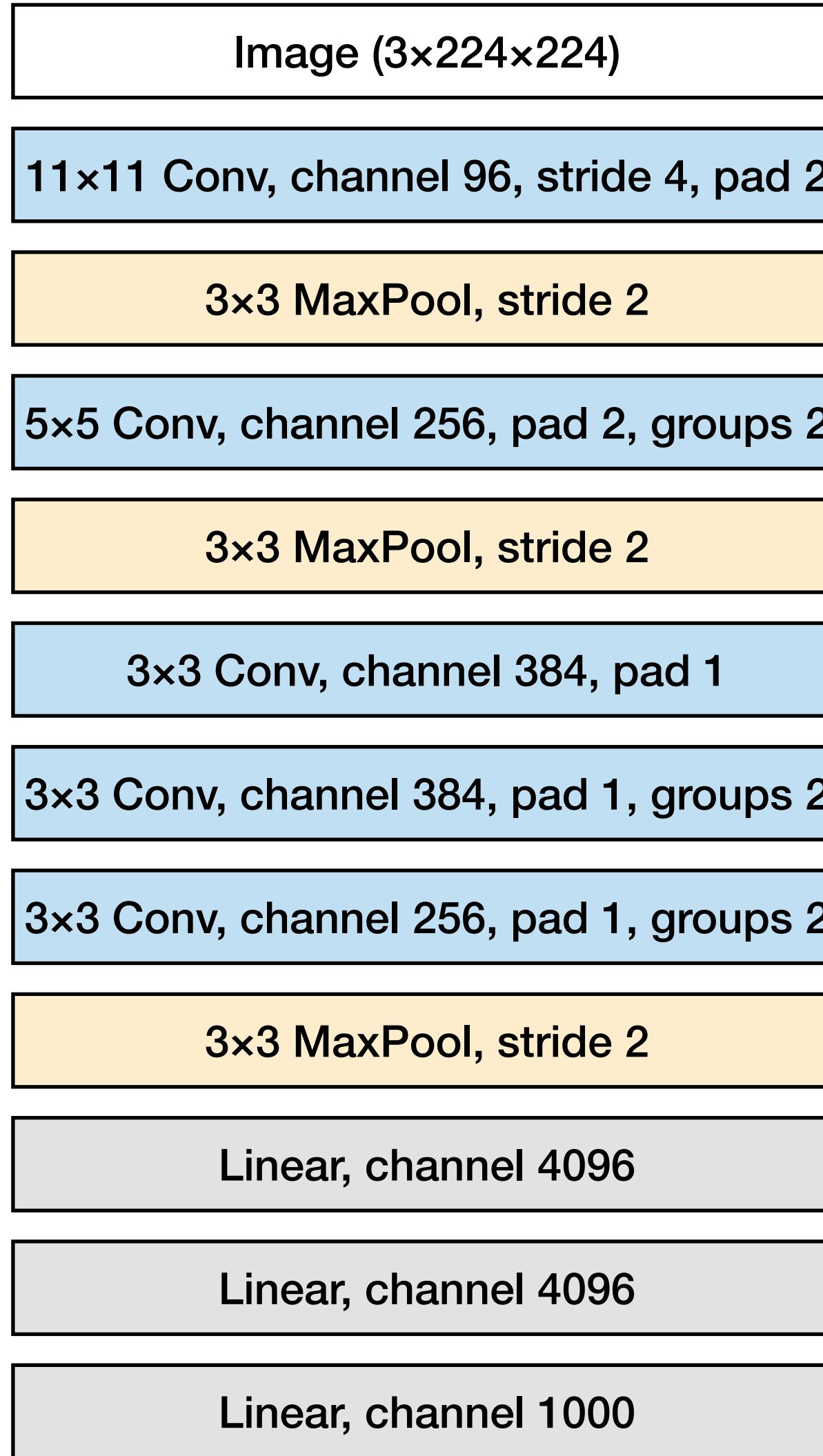
Linear Layer

$$\begin{matrix} c_i \\ n \end{matrix} \times \begin{matrix} c_o \\ c_i \end{matrix} = \begin{matrix} c_o \\ n \end{matrix}$$

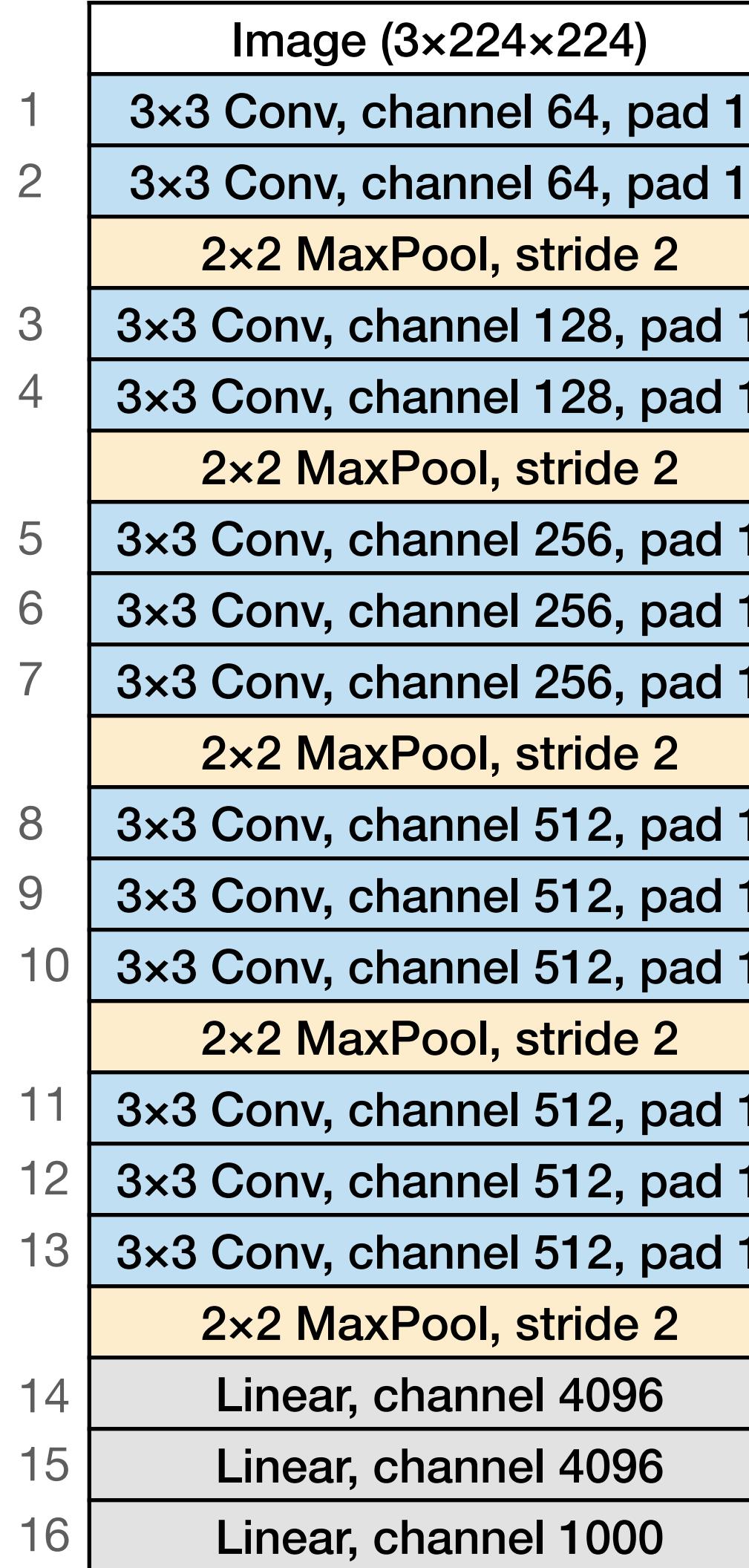
The diagram illustrates the linear layer operation. An input vector X of size $n \times c_i$ is multiplied by a weight matrix W^T of size $c_i \times c_o$ to produce an output vector Y of size $n \times c_o$.

VGG-16

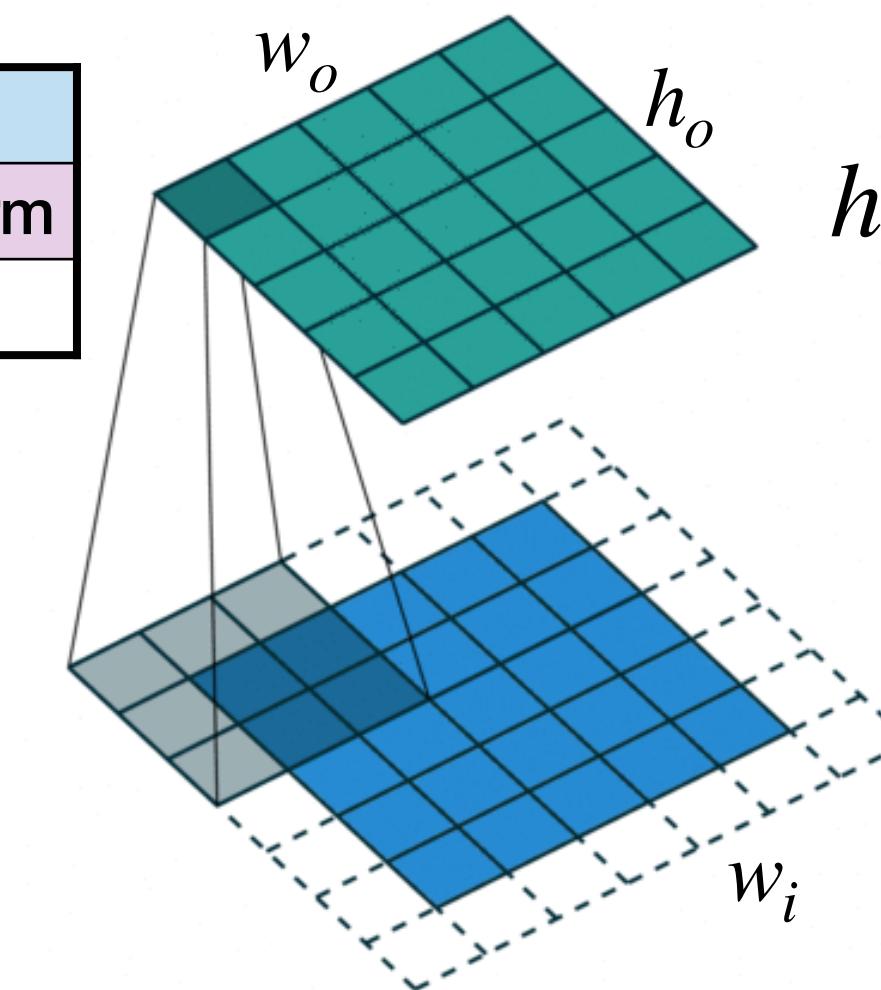
AlexNet



VGG-16



Convolution Layer / Pooling Layer

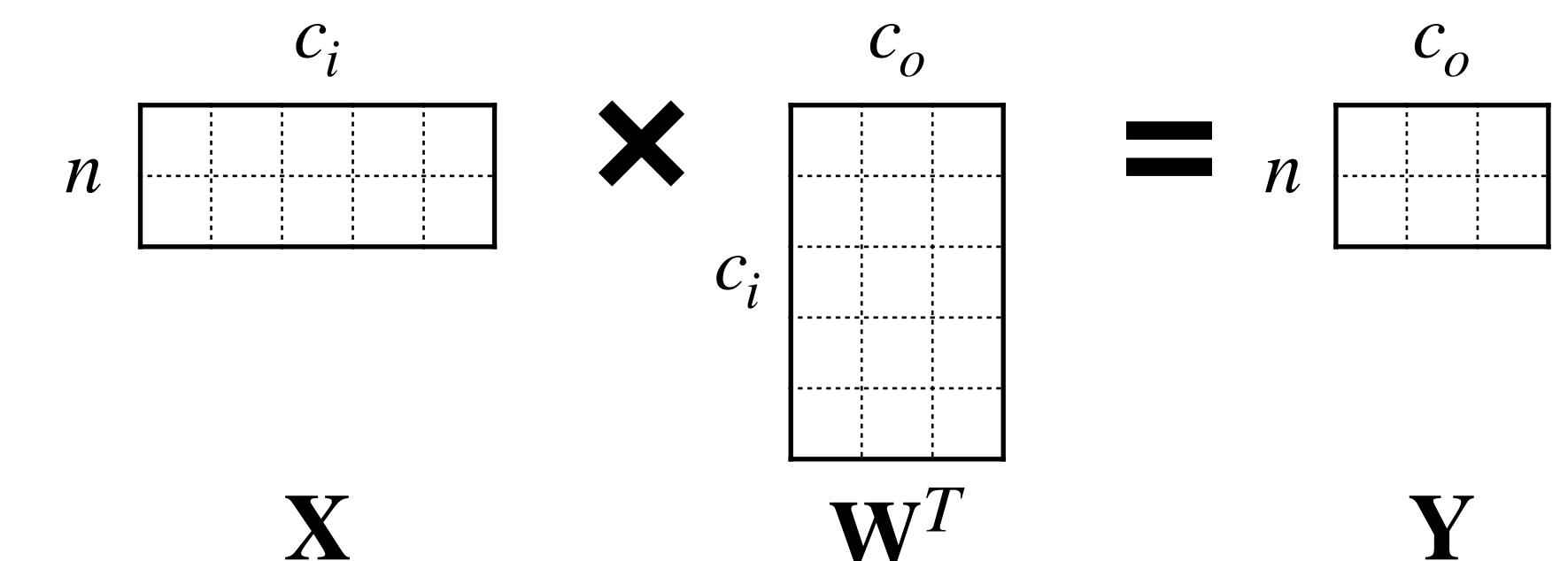


$$h_o = \frac{h_i + 2p - k_h}{s} + 1$$

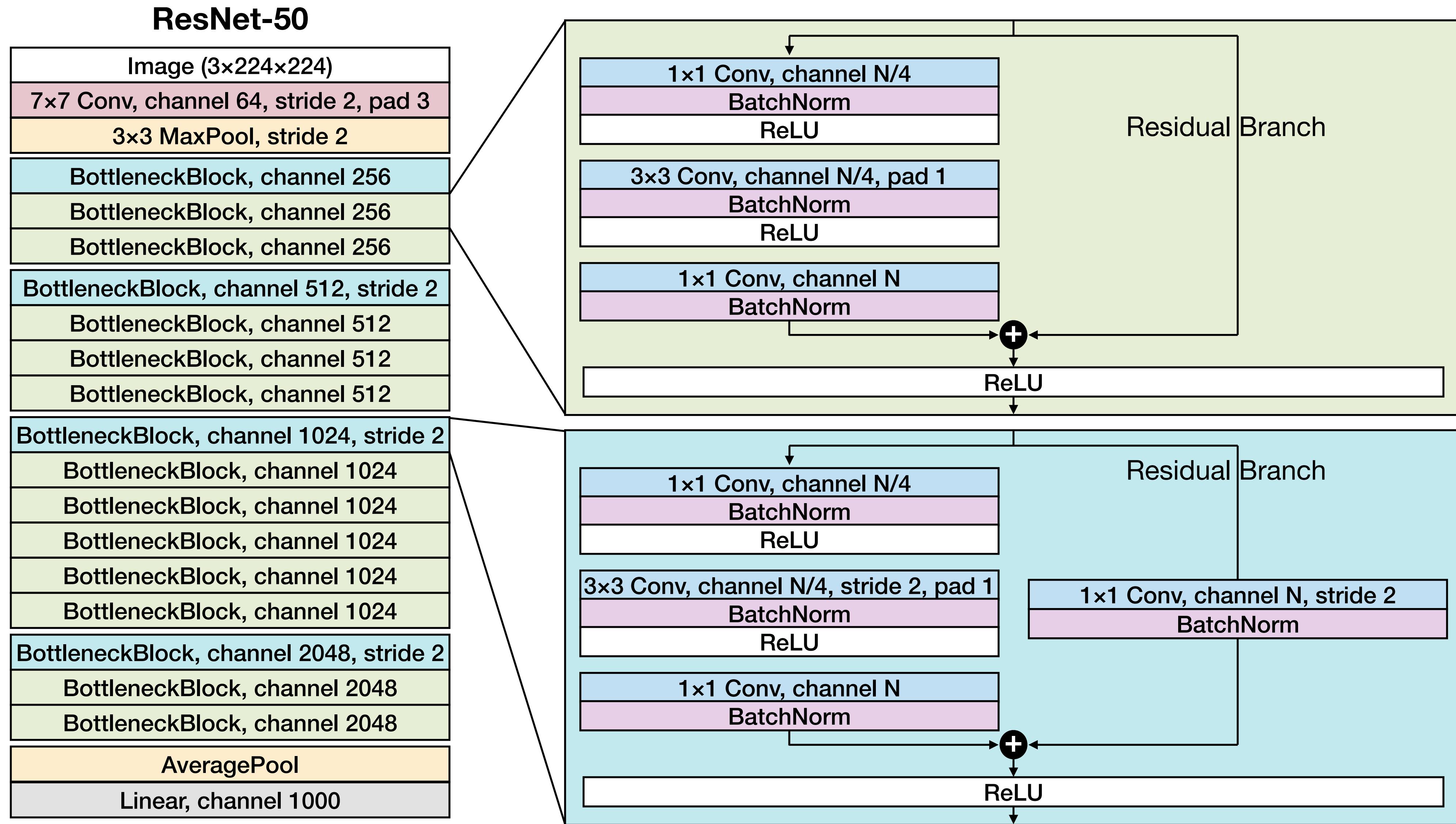
p is padding

s is stride

Linear Layer



ResNet-50



Deep Residual Learning for Image Recognition [He et al., CVPR 2016]

Feature
Channels

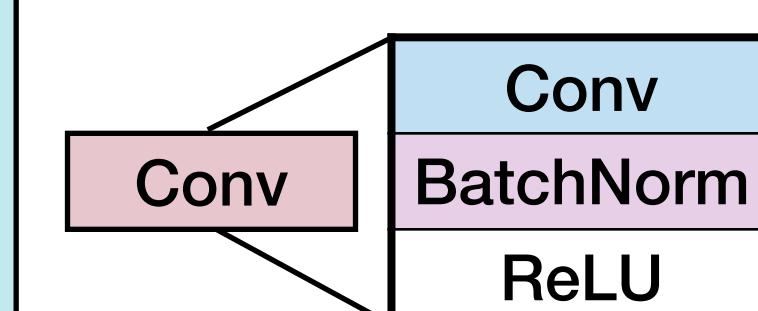
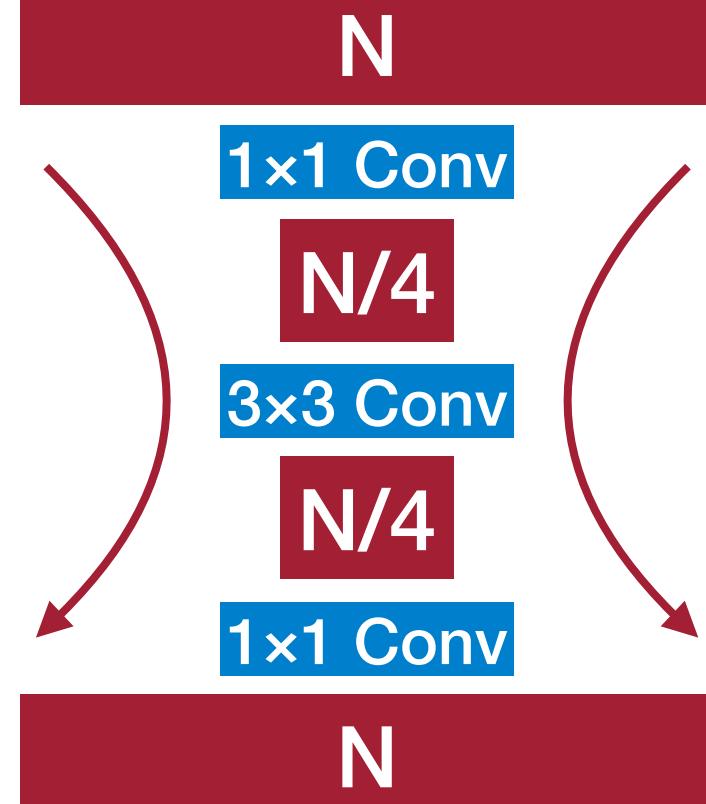
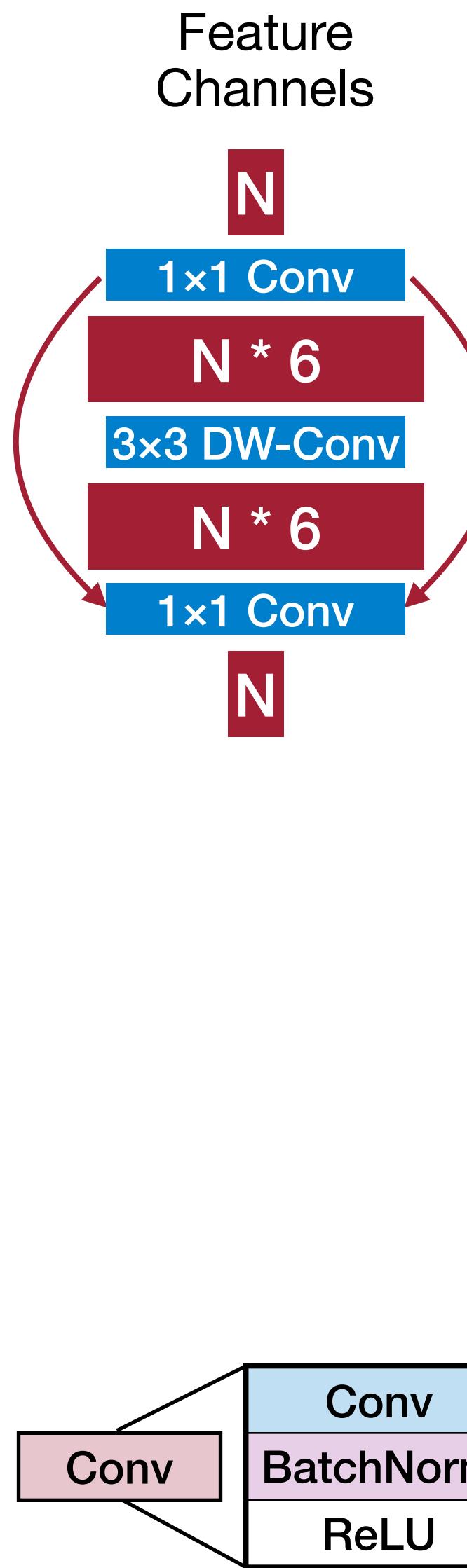
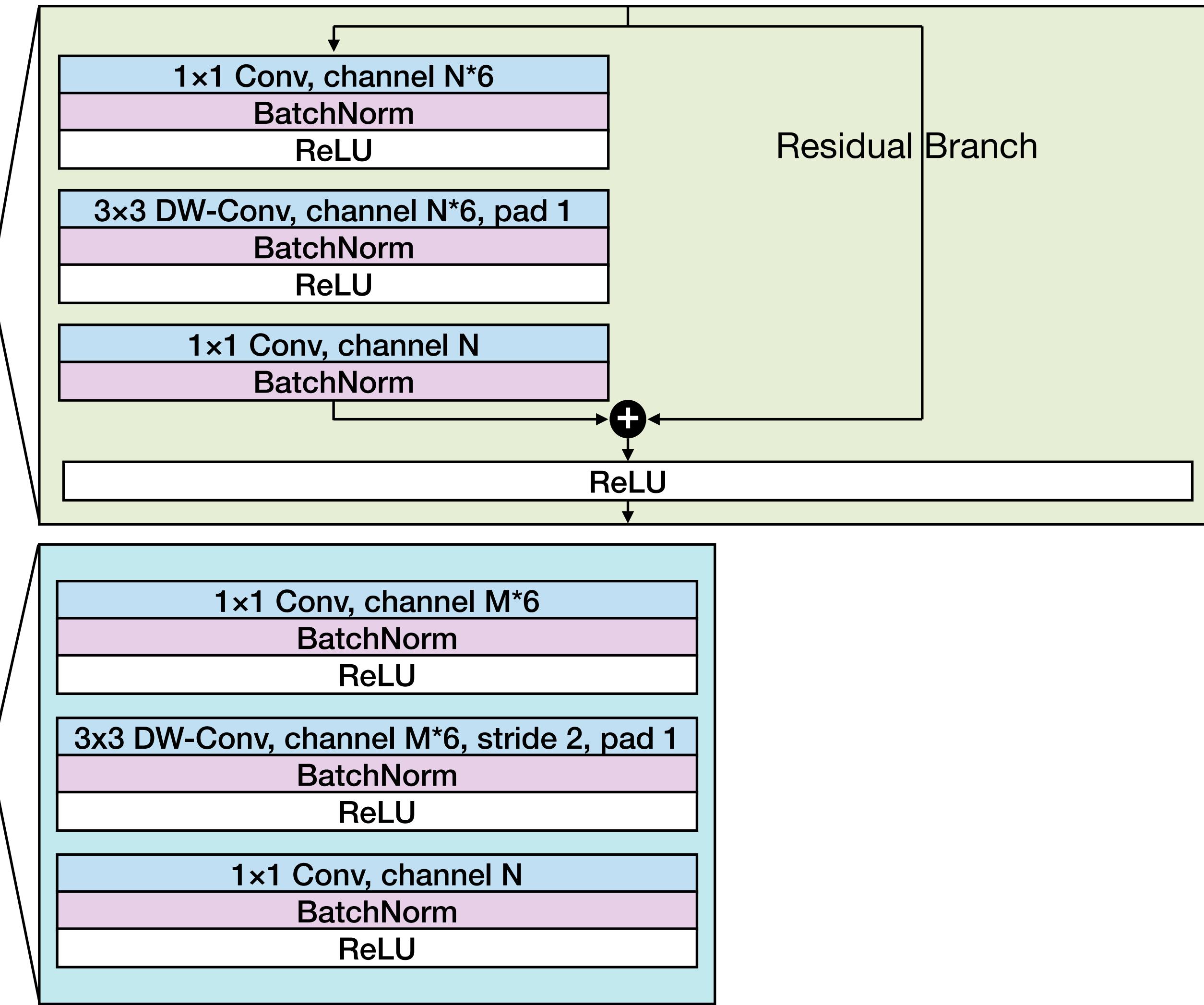
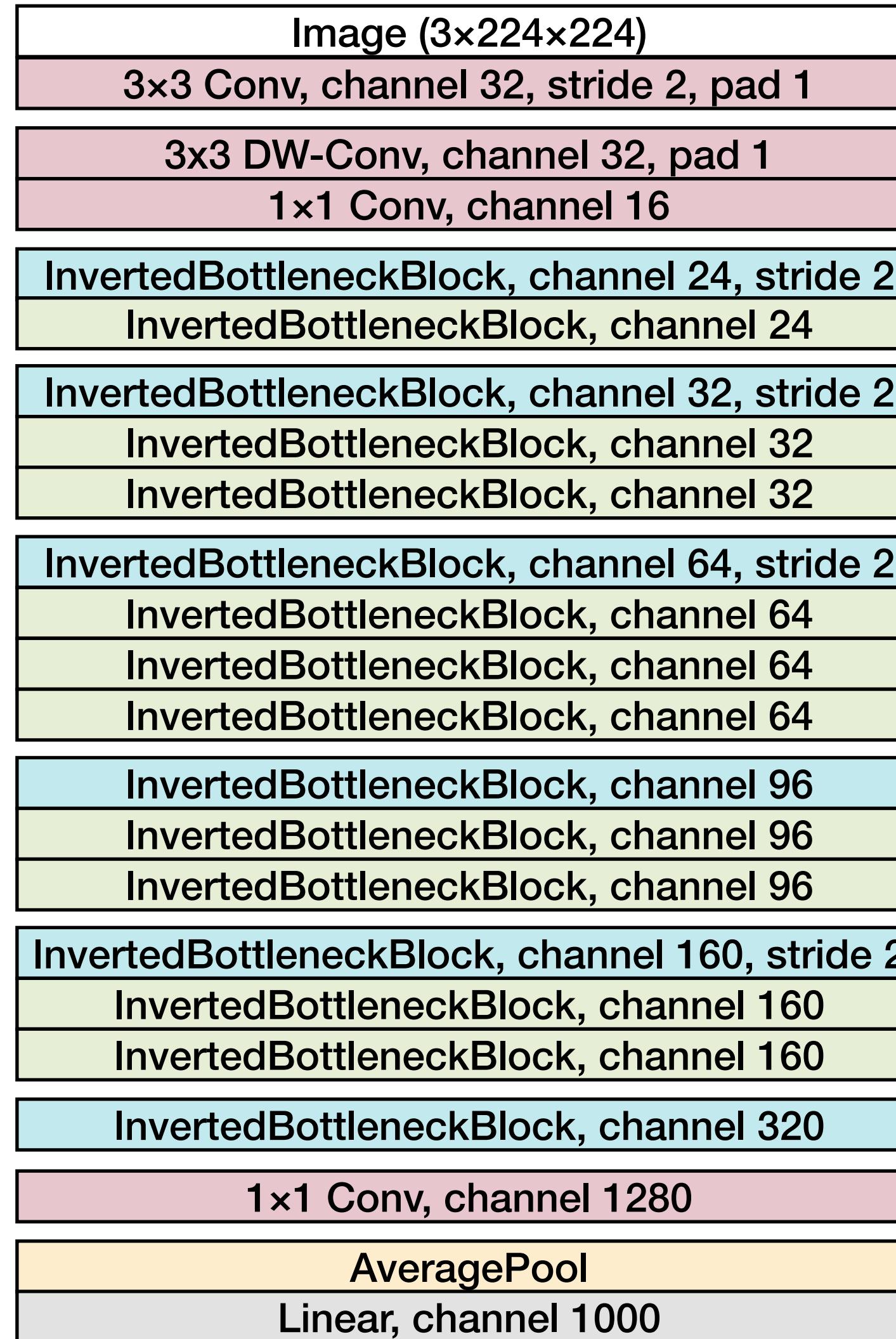


Figure Inspiration: 1

MobileNetV2

MobileNetV2



MobileNetV2: Inverted Residuals and Linear Bottlenecks [Sandler et al., CVPR 2018]

Figure Inspiration: 1

Efficiency Metrics

How should we measure the efficiency of neural networks?

Efficiency of Neural Networks

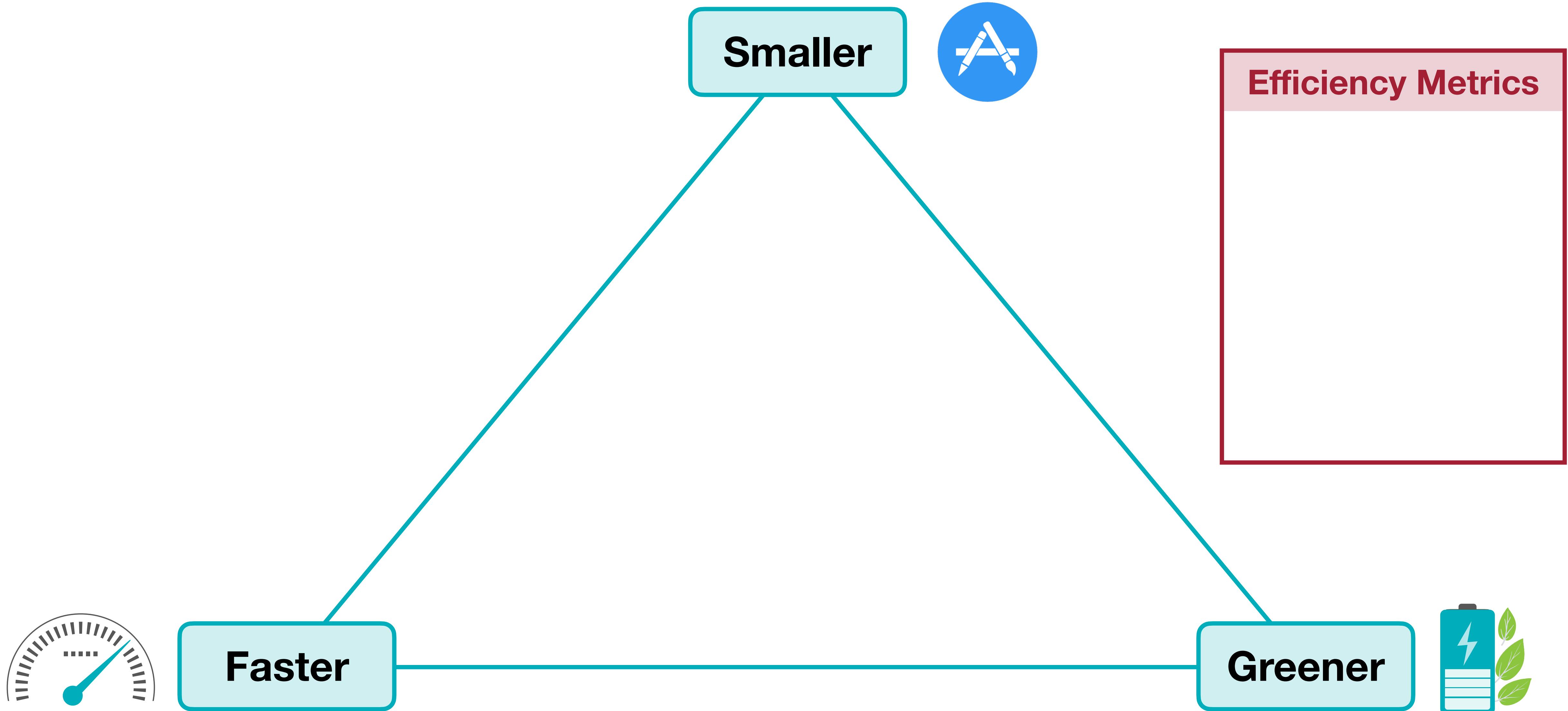


Image source: 1

Efficiency of Neural Networks

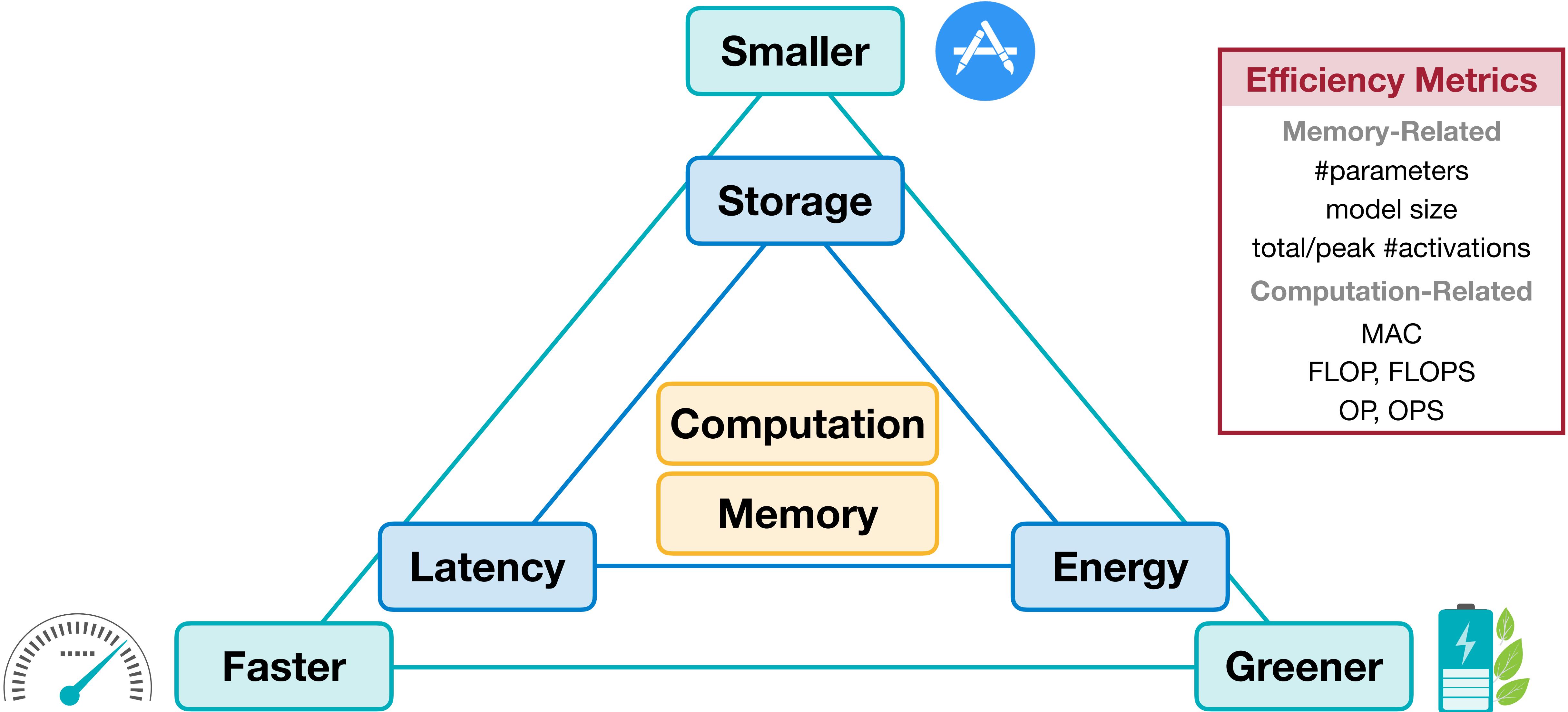


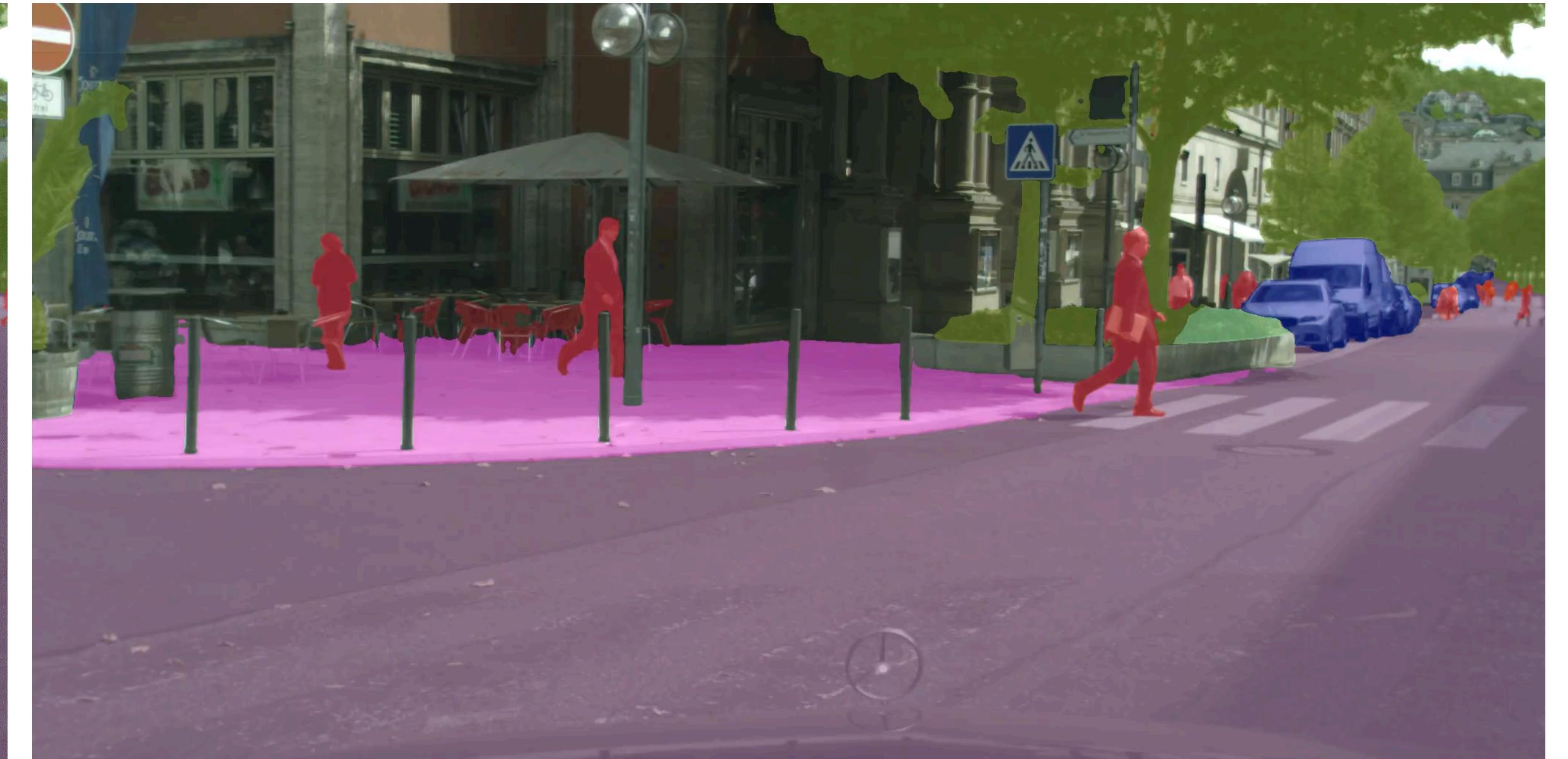
Image source: 1

Latency

Measures the delay for a specific task



High Latency
638ms

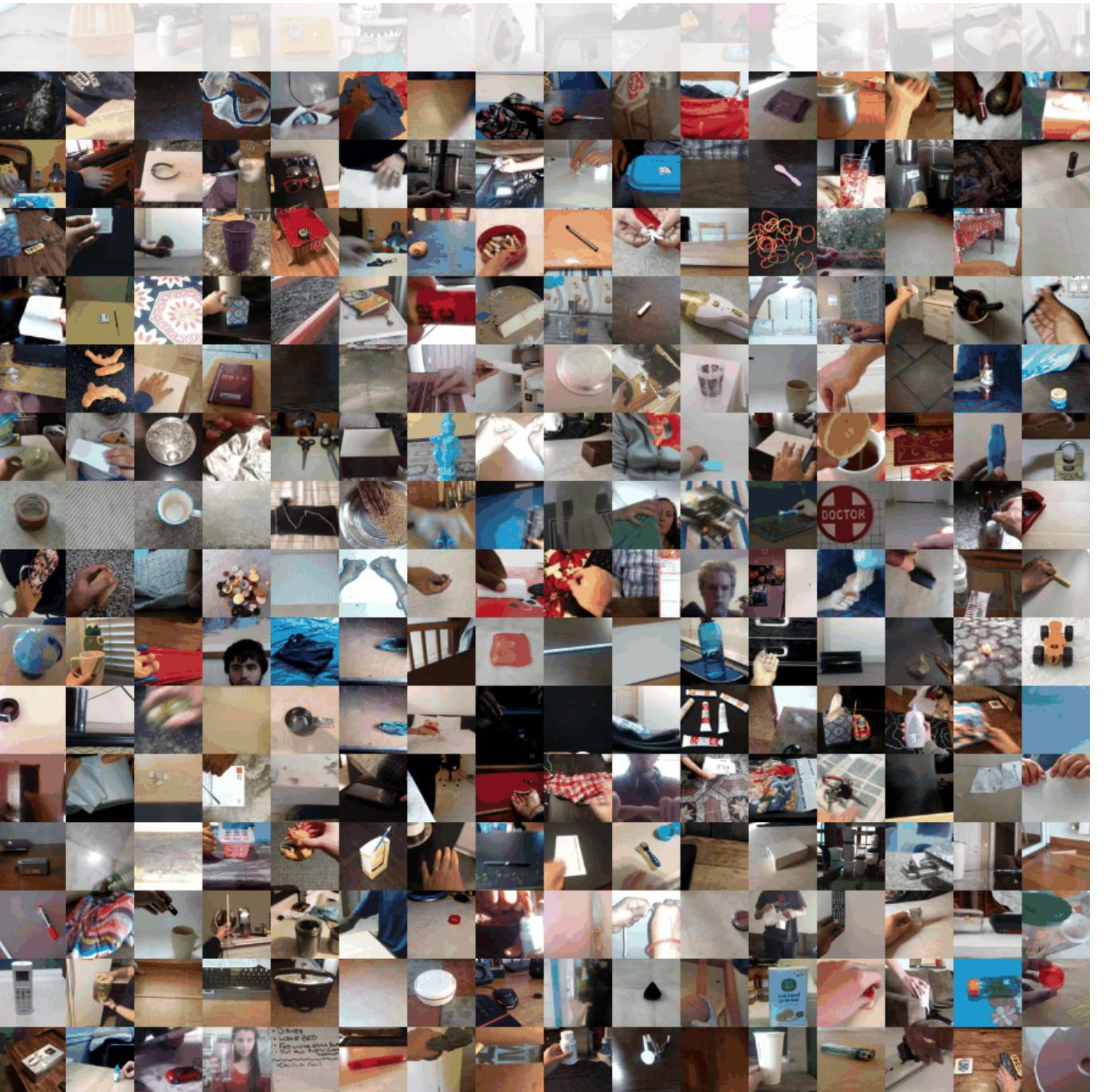


Low Latency
46ms

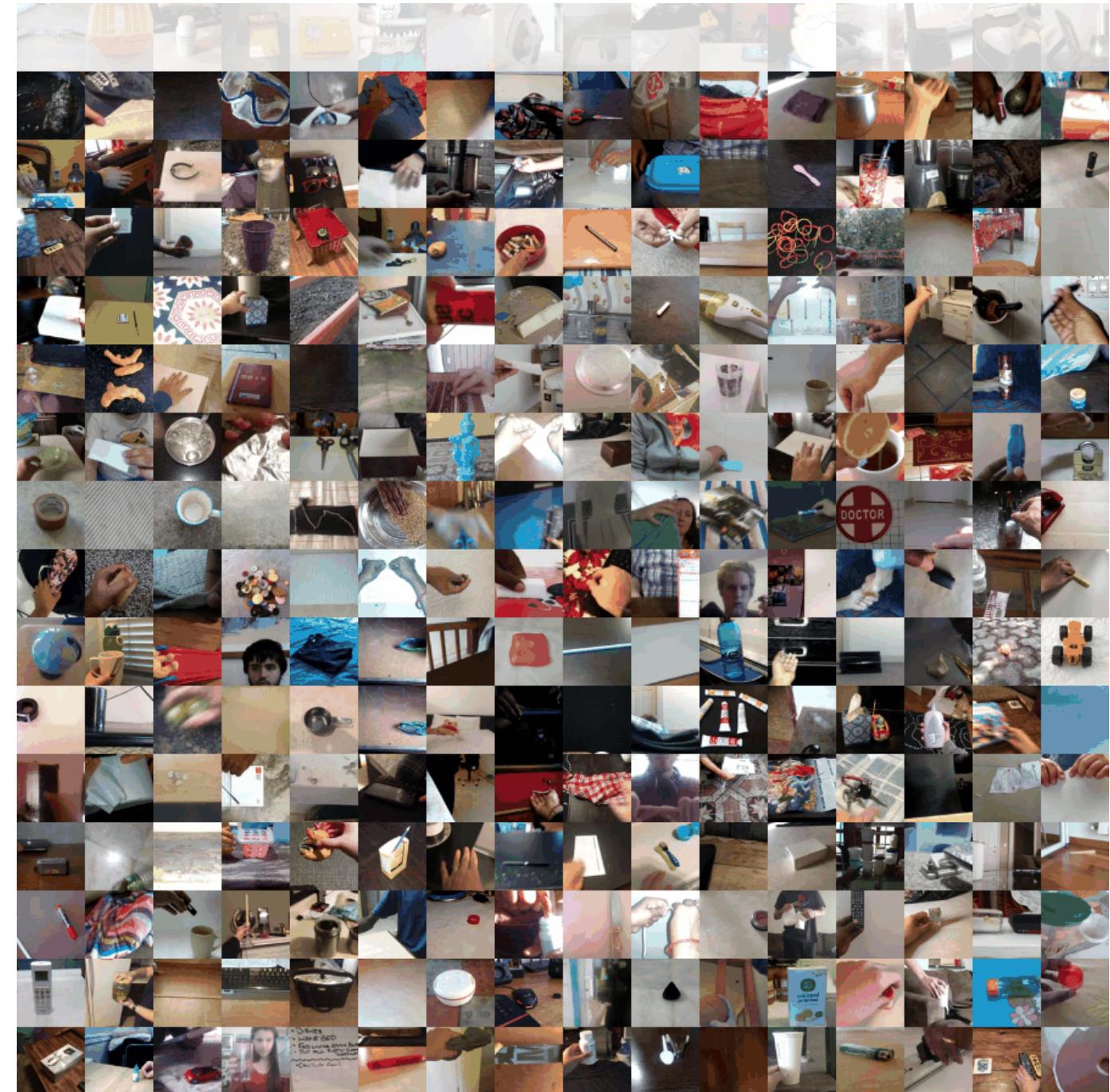
Speed is measured on Nvidia Jetson AGX Orin with TensorRT, fp16, batch size 1.

Throughput

Measures the rate at which data is processed



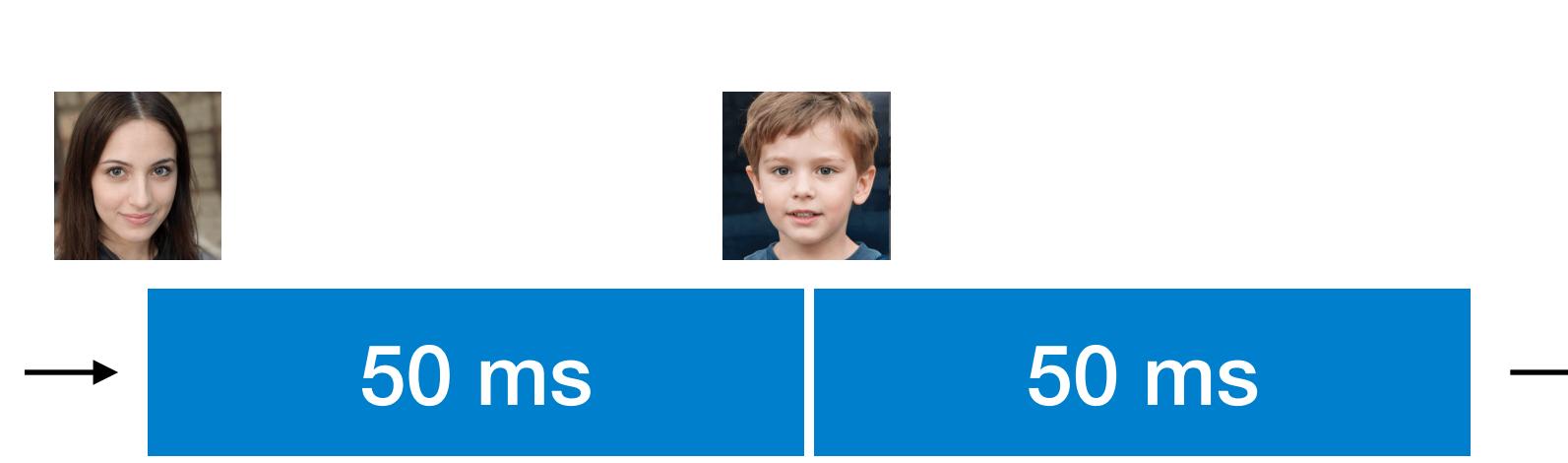
Low Throughput = 6.1 video/s



High Throughput = 77.4 video/s

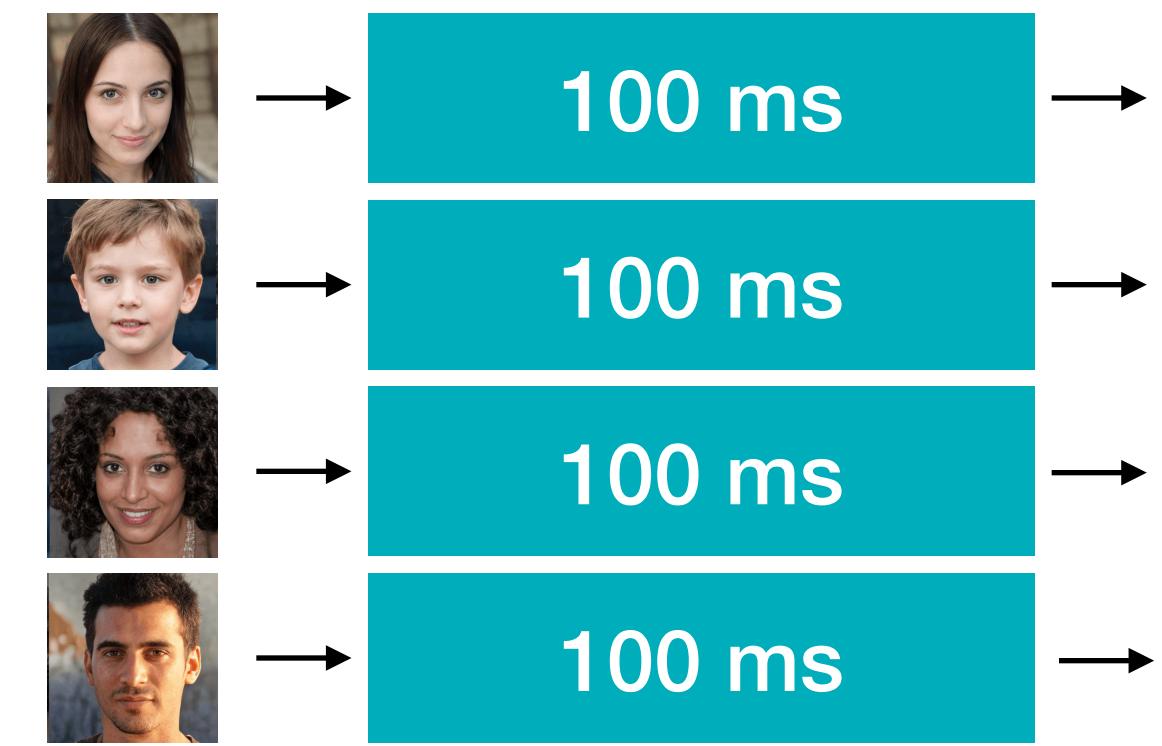
Latency vs. Throughput

- Does higher throughput translate to lower latency? Why?
- Does lower latency translate to higher throughput? Why?



Design 1

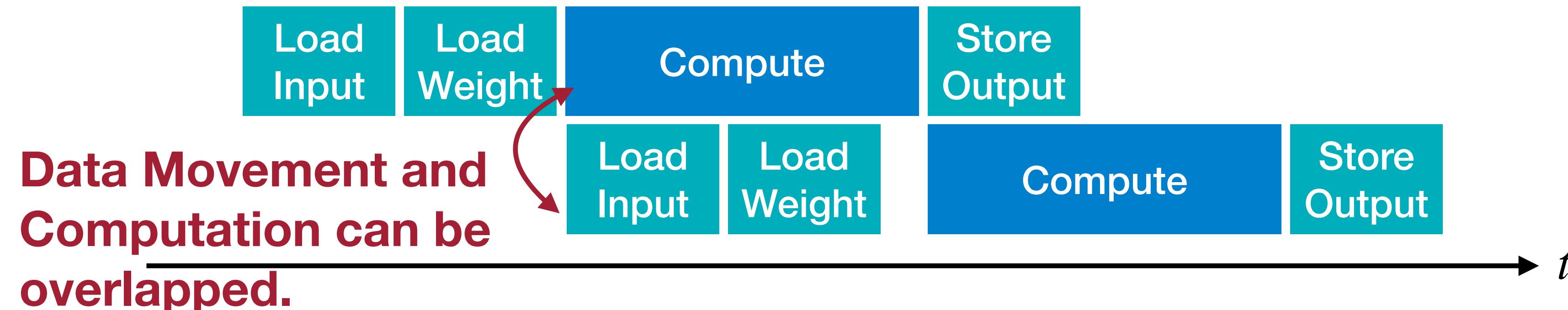
Latency: 50 ms
Throughput: 20 image/s



Design 2

Latency: 100 ms
Throughput: 40 image/s

Latency



$$\text{Latency} \approx \max(T_{\text{computation}}, T_{\text{memory}})$$

$$T_{\text{computation}} \approx \frac{\text{Number of Operations in Neural Network Model}}{\text{Number of Operations that Processor can Process Per Second}}$$

NN Specification

Hardware Specification

$$T_{\text{memory}} \approx T_{\text{data movement of activations}} + T_{\text{data movement of weights}}$$

$$T_{\text{data movement of weights}} \approx \frac{\text{Neural Network Model Size}}{\text{Memory Bandwidth of Processor}}$$

NN Specification

Hardware Specification

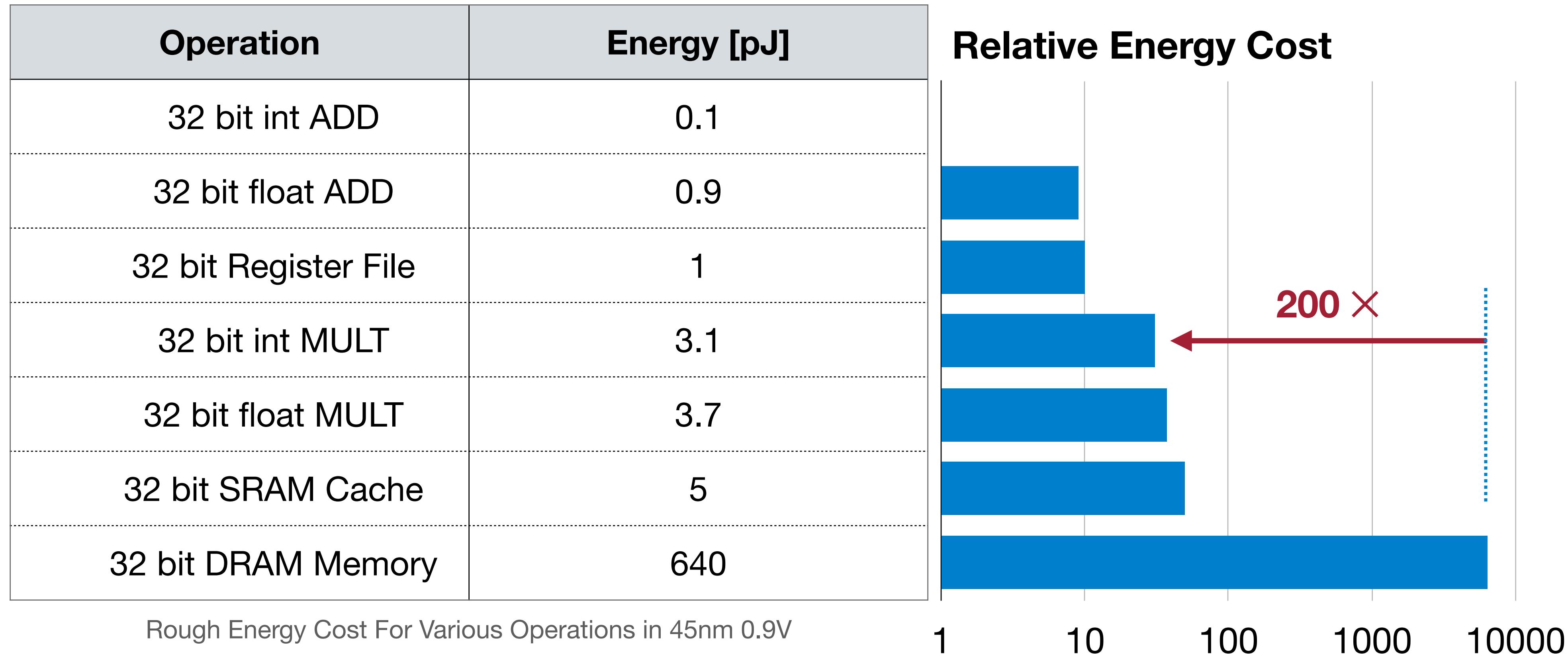
$$T_{\text{data movement of activations}} \approx \frac{\text{Input Activation Size} + \text{Output Activation Size}}{\text{Memory Bandwidth of Processor}}$$

NN Specification

Hardware Specification

Energy Consumption

Data movement → more memory reference → more energy



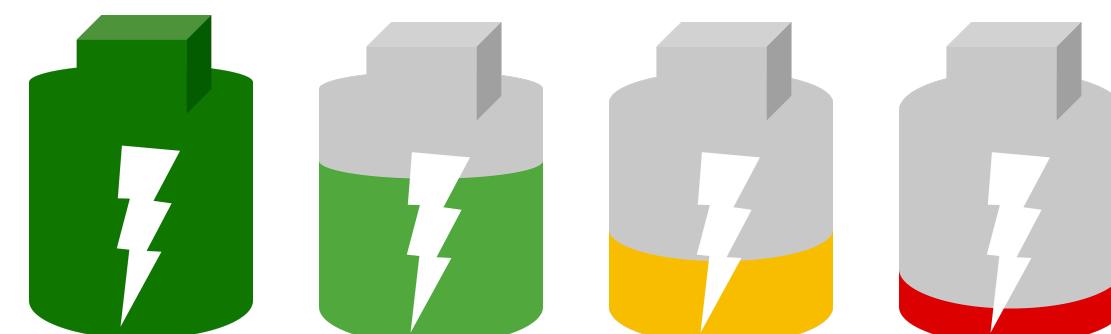
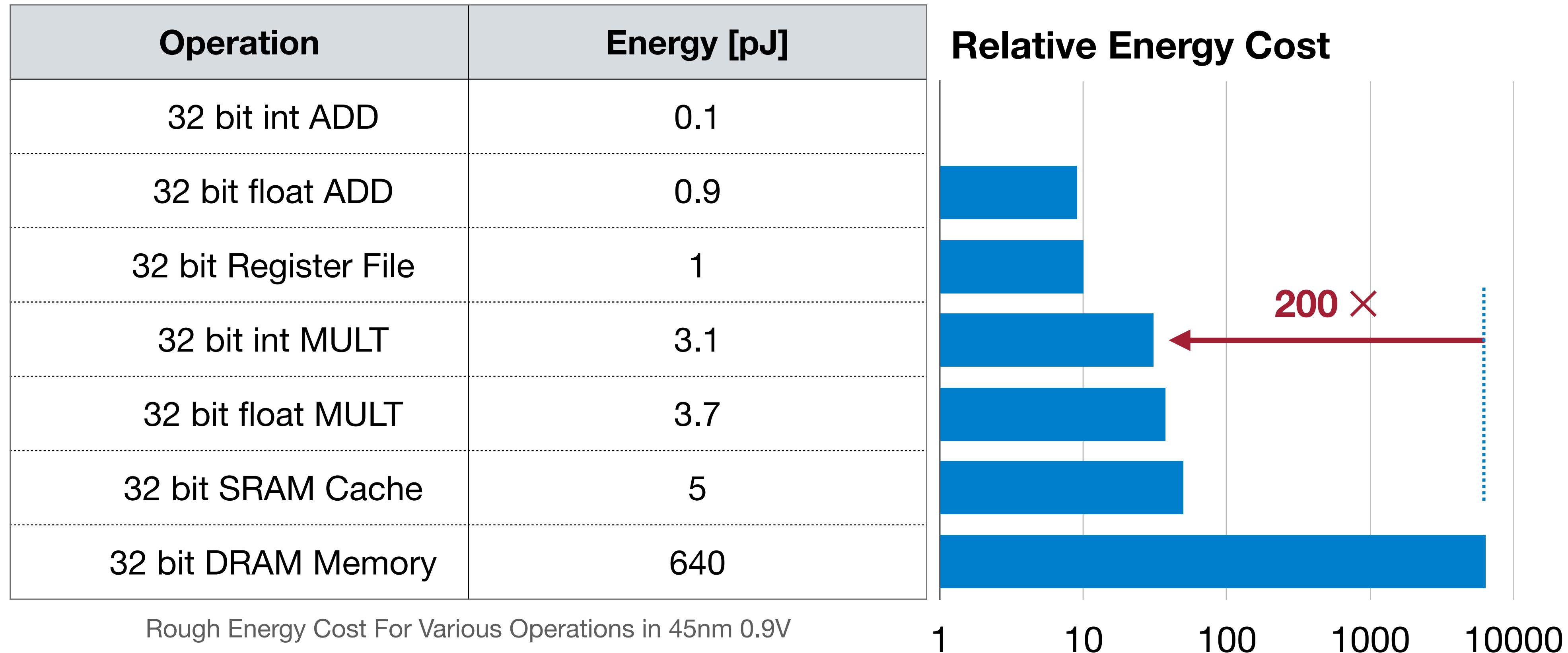
1  = 200 ×+

This image is in the public domain

Computing's Energy Problem (and What We Can Do About it) [Horowitz, M., IEEE ISSCC 2014]

Energy Consumption

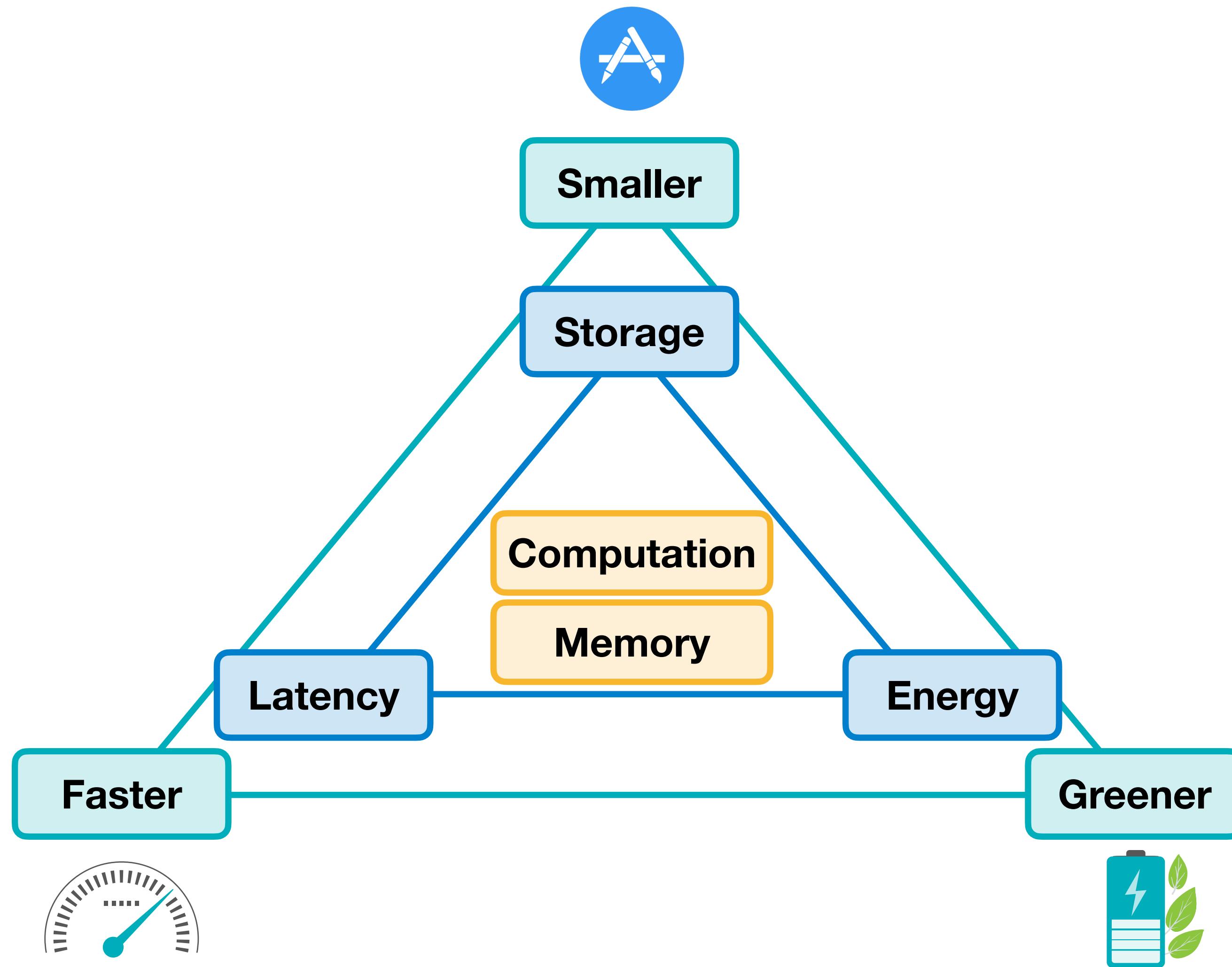
Data movement → more memory reference → more energy



Battery images are in the public domain
[Image 1](#), [Image 2](#), [Image 2](#), [Image 4](#)

Computing's Energy Problem (and What We Can Do About it) [Horowitz, M., IEEE ISSCC 2014]

Efficiency of Neural Networks



Efficiency Metrics

Memory-Related

#parameters

model size

total/peak #activations

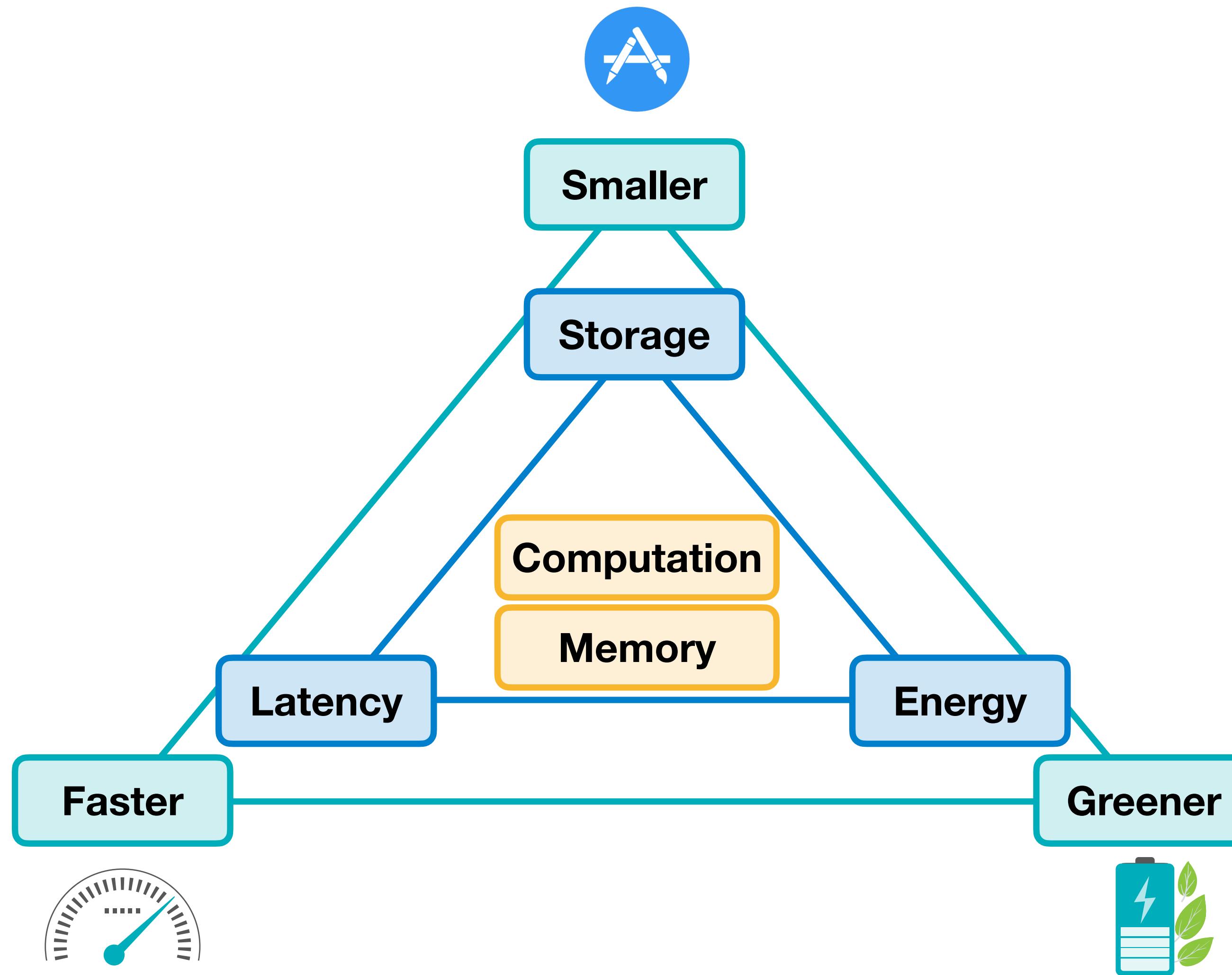
Computation-Related

MAC

FLOP, FLOPS

OP, OPS

Efficiency of Neural Networks



Efficiency Metrics

Memory-Related

#parameters

model size

total/peak #activations

Computation-Related

MAC

FLOP, FLOPS

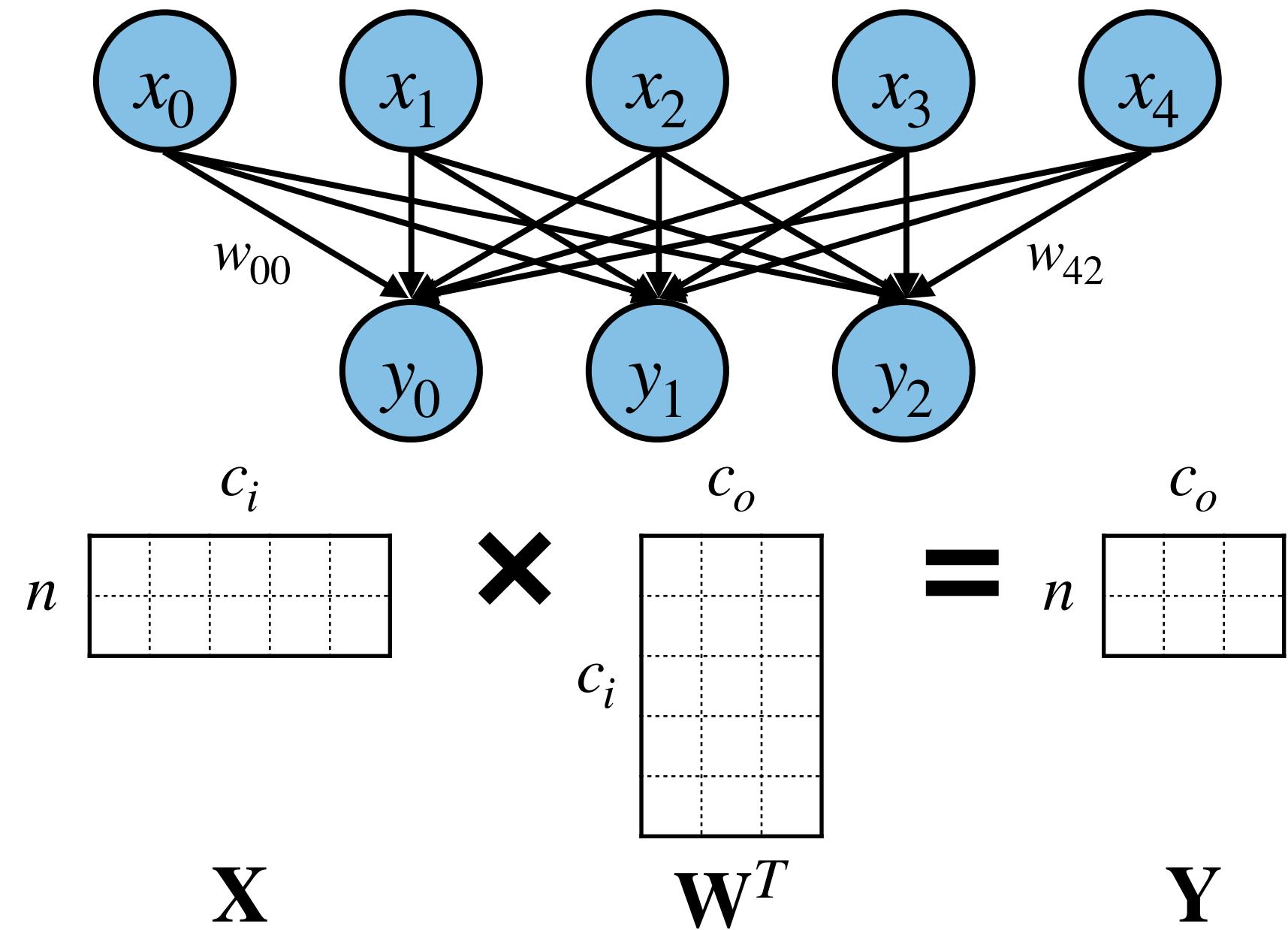
OP, OPS

Number of Parameters (#Parameters)

- #Parameters is the parameter (synapse/weight) count of the given neural network, *i.e.*, the number of elements in the weight tensors.

Number of Parameters (#Parameters)

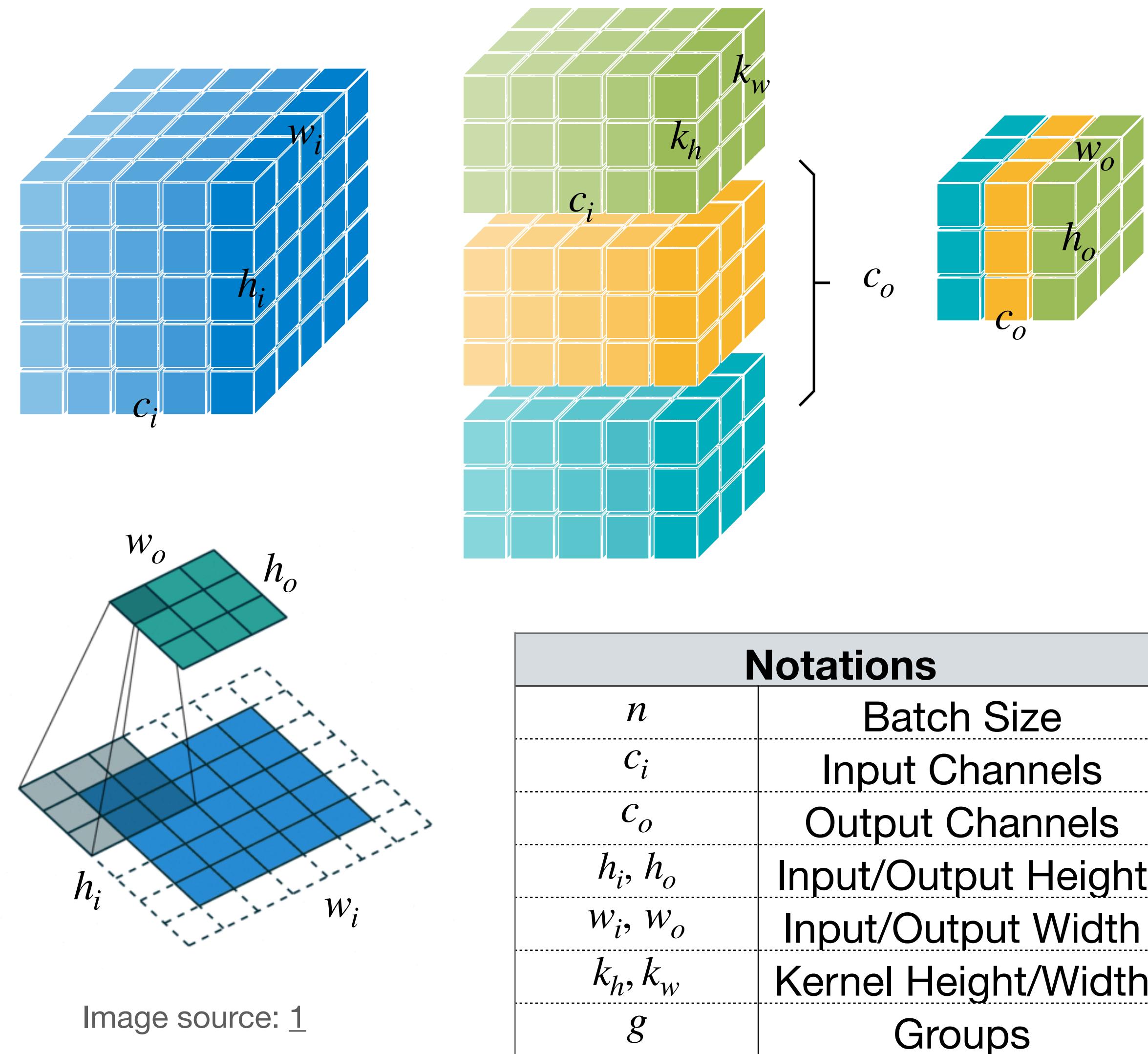
Layer	#Parameters (bias is ignored)
Linear Layer	$c_o \cdot c_i$
Convolution	
Grouped Convolution	
Depthwise Convolution	



Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h, k_w	Kernel Height/Width
g	Groups

Number of Parameters (#Parameters)

Layer	#Parameters (bias is ignored)
Linear Layer	$c_o \cdot c_i$
Convolution	$c_o \cdot c_i \cdot k_h \cdot k_w$
Grouped Convolution	
Depthwise Convolution	



Number of Parameters (#Parameters)

Layer	#Parameters (bias is ignored)
Linear Layer	$c_o \cdot c_i$
Convolution	$c_o \cdot c_i \cdot k_h \cdot k_w$
Grouped Convolution	$c_o/g \cdot c_i/g \cdot k_h \cdot k_w \cdot g$ $= c_o \cdot c_i \cdot k_h \cdot k_w/g$
Depthwise Convolution	

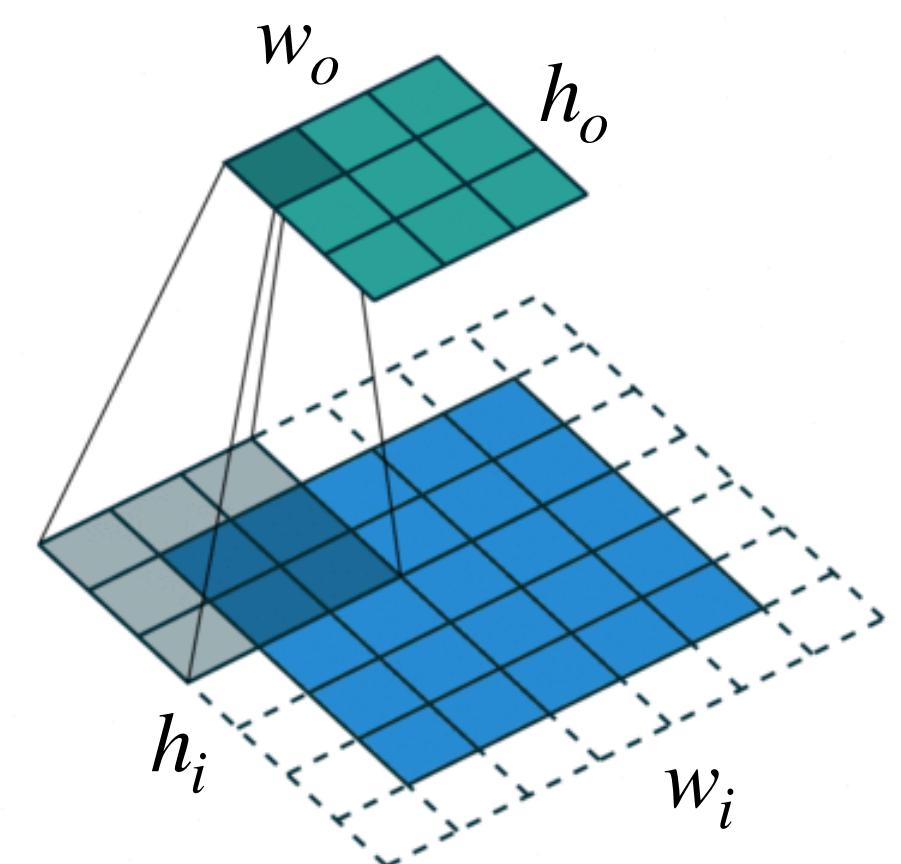
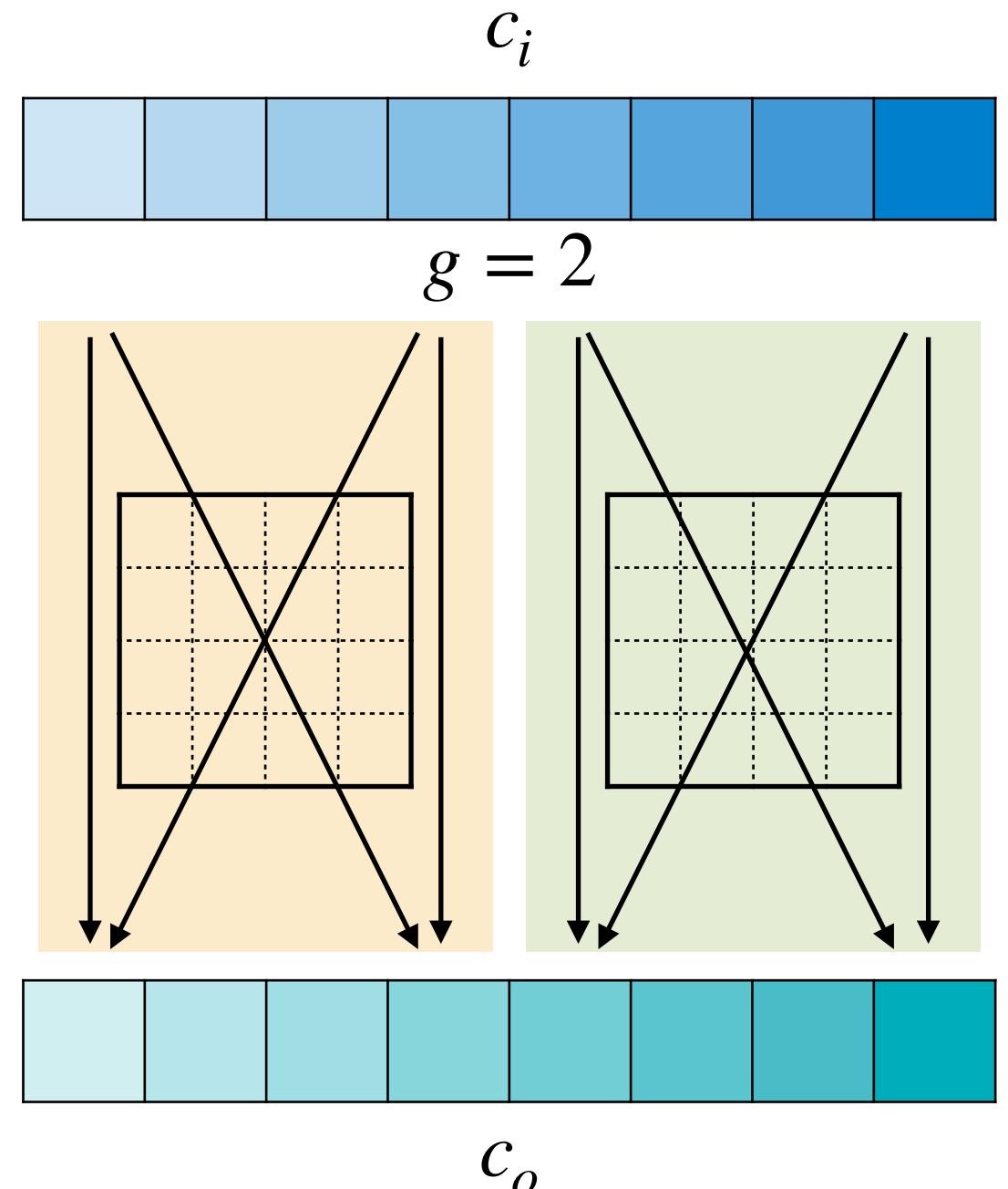


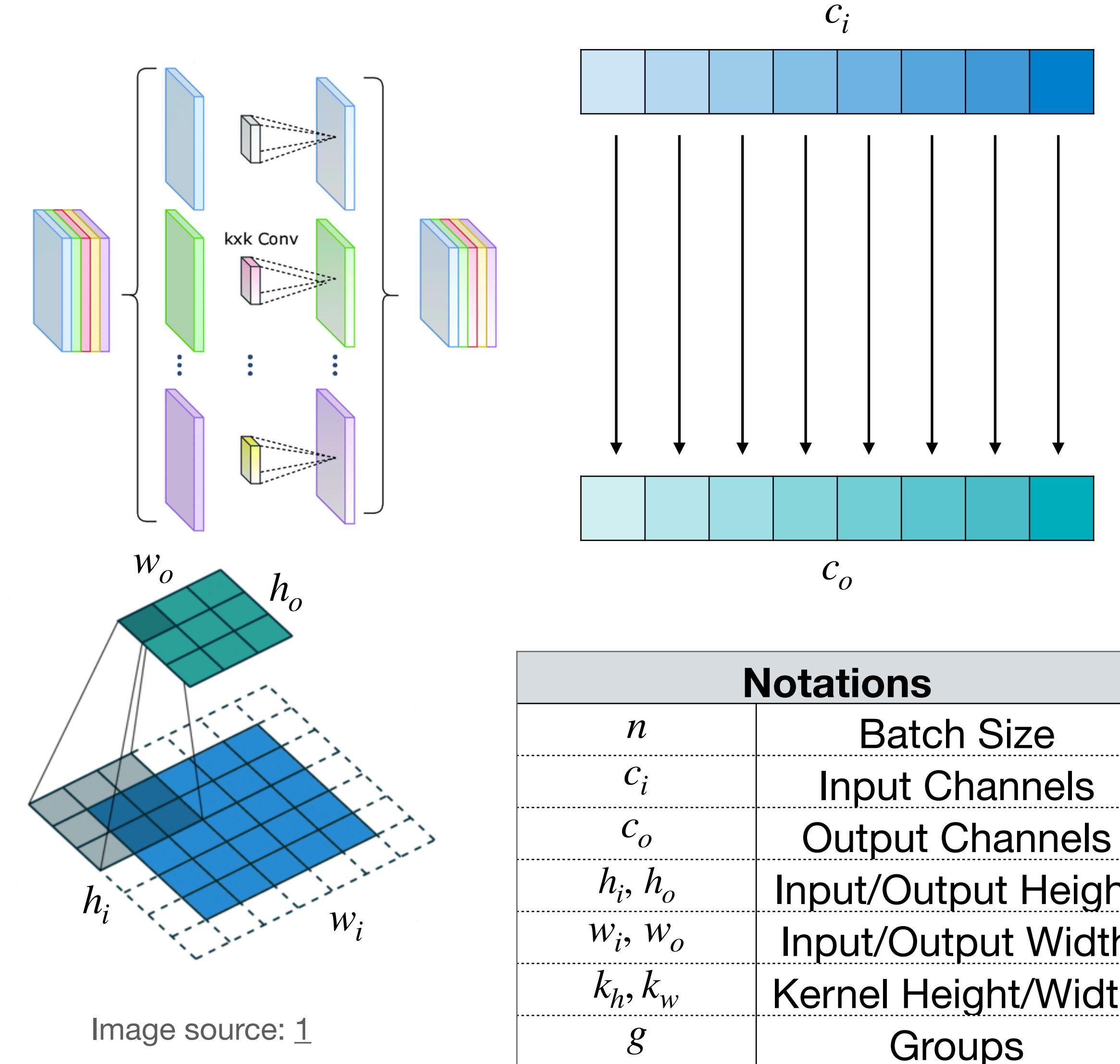
Image source: 1



Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h, k_w	Kernel Height/Width
g	Groups

Number of Parameters (#Parameters)

Layer	#Parameters (bias is ignored)
Linear Layer	$c_o \cdot c_i$
Convolution	$c_o \cdot c_i \cdot k_h \cdot k_w$
Grouped Convolution	$c_o/g \cdot c_i/g \cdot k_h \cdot k_w \cdot g$ $= c_o \cdot c_i \cdot k_h \cdot k_w/g$
Depthwise Convolution	$c_o \cdot k_h \cdot k_w$



AlexNet: #Parameters

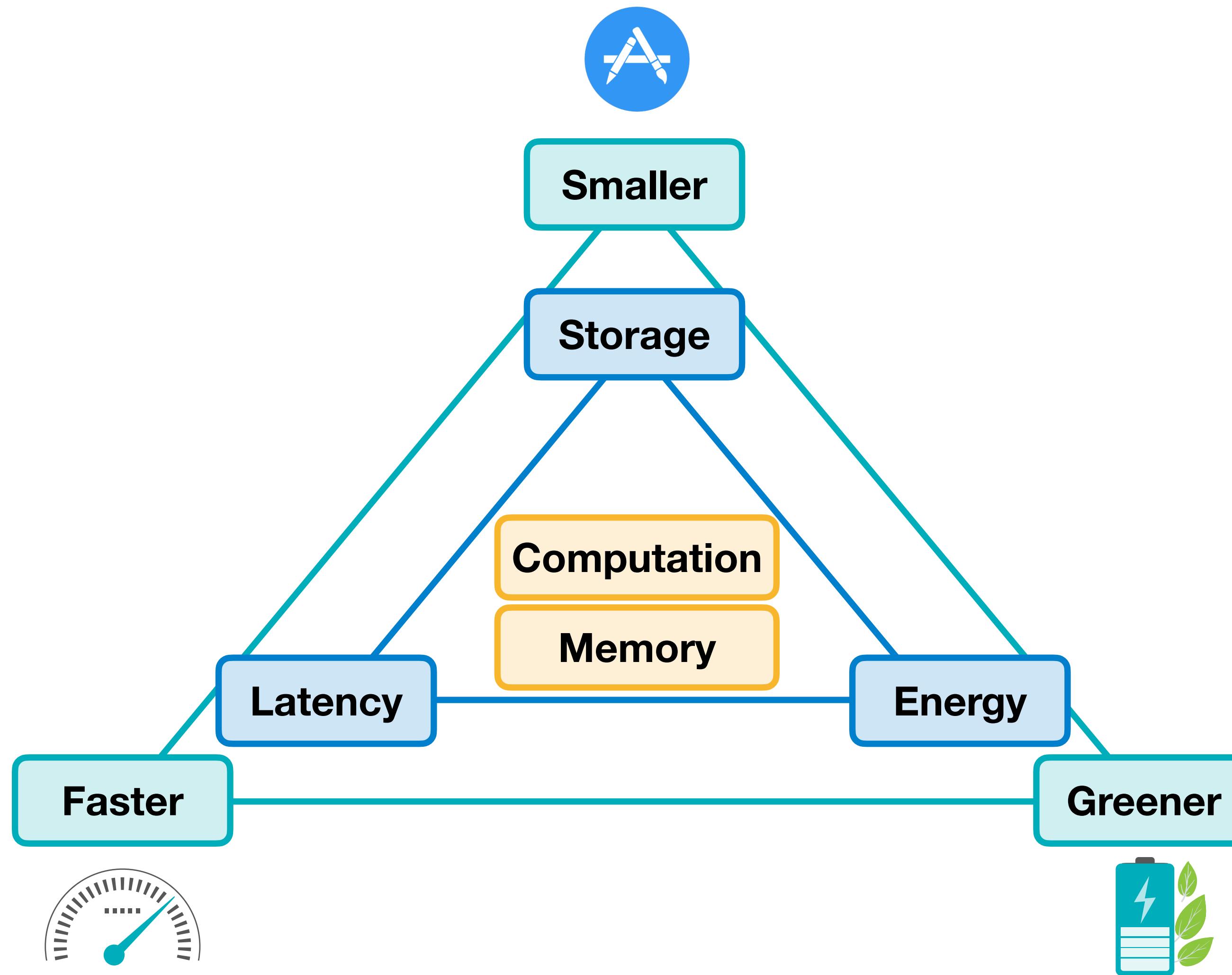
AlexNet	$C \times H \times W$	#Parameters (bias is ignored)
Image (3×224×224)	3×224×224	
11×11 Conv, channel 96, stride 4, pad 2	96×55×55	$96 \times 3 \times 11 \times 11 = 24,848$
3×3 MaxPool, stride 2	96×27×27	
5×5 Conv, channel 256, pad 2, groups 2	256×27×27	$256 \times 96 \times 5 \times 5 / 2 = 307,200$
3×3 MaxPool, stride 2	256×13×13	
3×3 Conv, channel 384, pad 1	384×13×13	$384 \times 256 \times 3 \times 3 = 884,736$
3×3 Conv, channel 384, pad 1, groups 2	384×13×13	$384 \times 384 \times 3 \times 3 / 2 = 663,552$
3×3 Conv, channel 256, pad 1, groups 2	256×13×13	$256 \times 384 \times 3 \times 3 / 2 = 442,368$
3×3 MaxPool, stride 2	256×6×6	
Linear, channel 4096	4096	$4096 \times (256 \times 6 \times 6) = 37,748,736$
Linear, channel 4096	4096	$4096 \times 4096 = 16,777,216$
Linear, channel 1000	1000	$1000 \times 4096 = 4,096,000$

Layer	#Parameters
Linear Layer	$c_o \cdot c_i$
Convolution	$c_o \cdot c_i \cdot k_h \cdot k_w$
Grouped Convolution	$c_o \cdot c_i \cdot k_h \cdot k_w / g$
Depthwise Convolution	$c_o \cdot k_h \cdot k_w$

61M in total

ImageNet Classification with Deep Convolutional Neural Networks [Krizhevsky et al., NeurIPS 2012]

Efficiency of Neural Networks



Efficiency Metrics

Memory-Related

#parameters

model size

total/peak #activations

Computation-Related

MAC

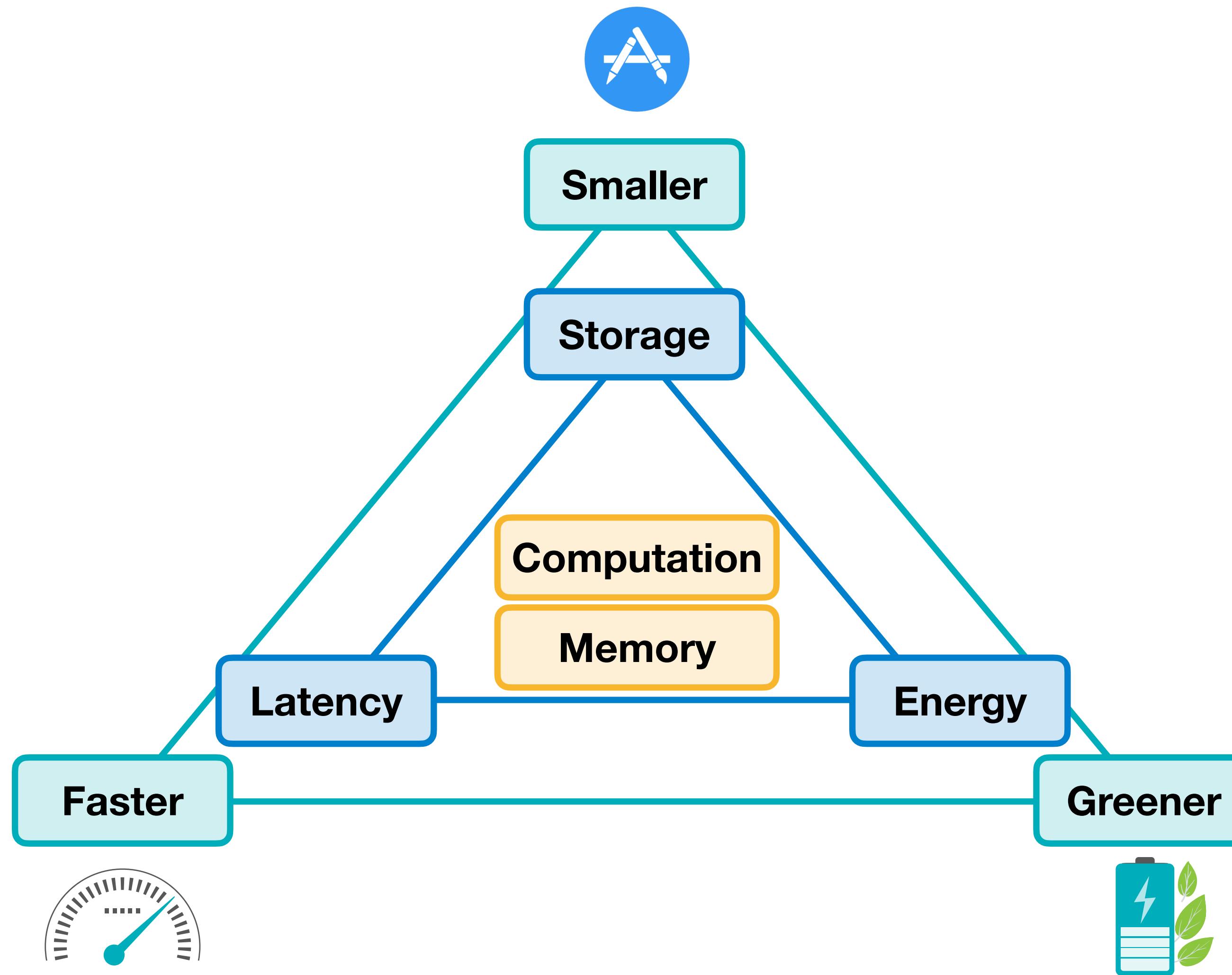
FLOP, FLOPS

OP, OPS

Model Size

- Model size measures the storage for the weights of the given neural network.
 - The common units for model size are: MB (megabyte), KB (kilobyte), bits.
- In general, if the whole neural network uses the same data type (e.g., floating-point),
 - $Model\ Size = \#Parameters \cdot Bit\ Width$
- Example: AlexNet has 61M parameters.
 - If all weights are stored with 32-bit numbers, total storage will be about
 - $61M \times 4\ Bytes\ (32\ bits) = 224\ MB\ (224 \times 10^6\ Bytes)$
 - If all weights are stored with 8-bit numbers, total storage will be about
 - $61M \times 1\ Byte\ (8\ bits) = 61\ MB$

Efficiency of Neural Networks



Efficiency Metrics

Memory-Related

#parameters
model size

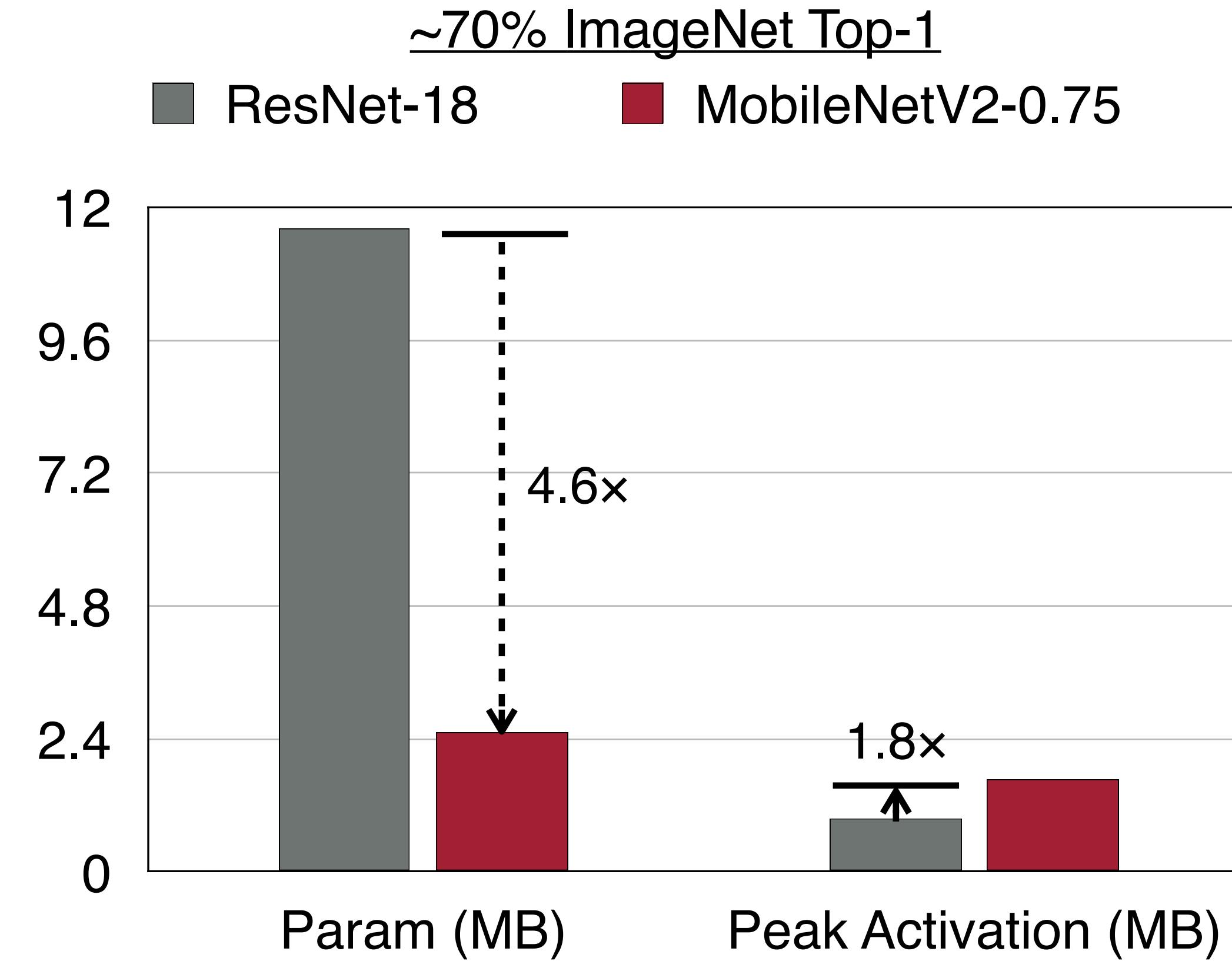
total/peak #activations

Computation-Related

MAC
FLOP, FLOPS
OP, OPS

Number of Activations (#Activations)

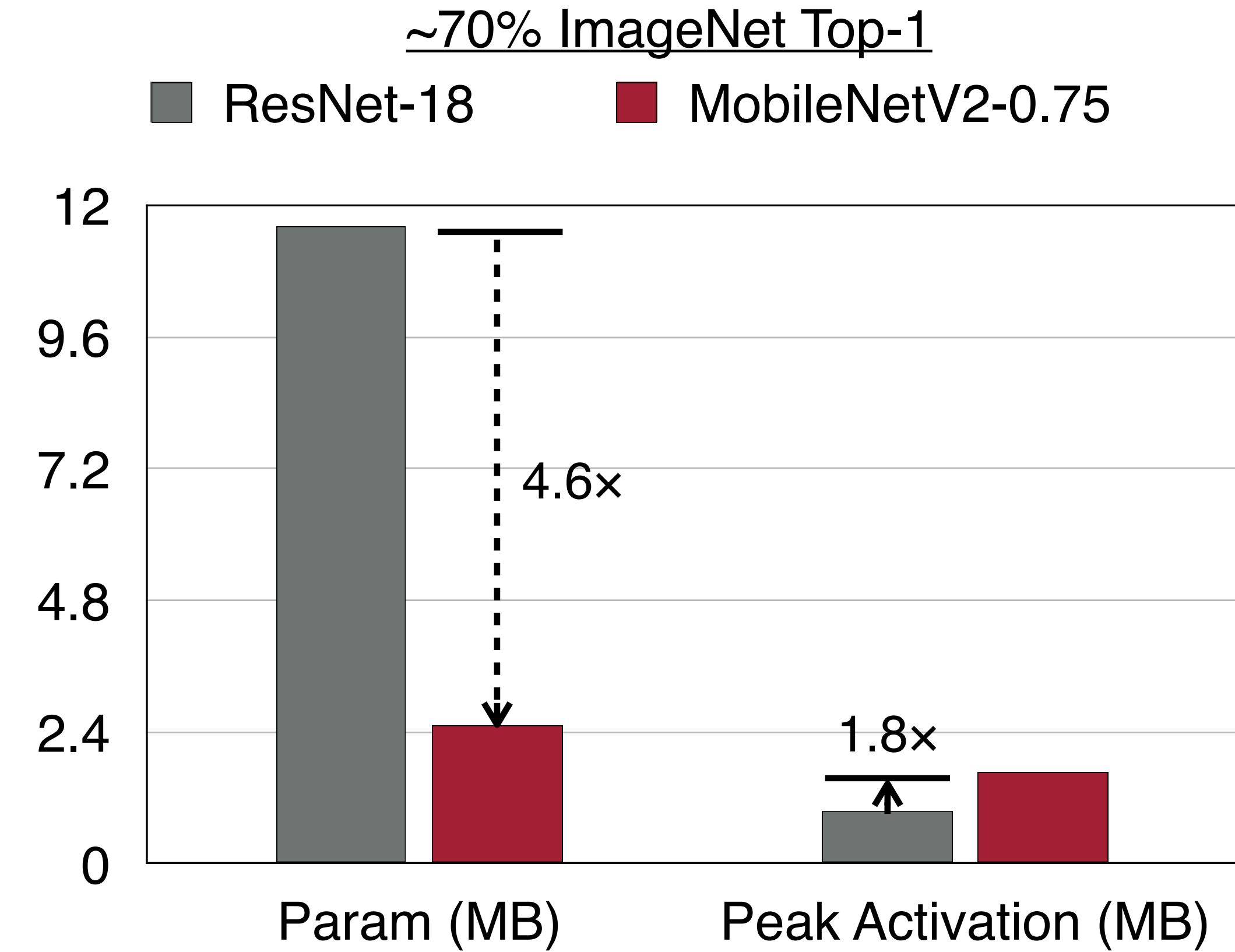
#Activation is the memory bottleneck in inference on IoT, not #Parameters.



* All parameters and activations are Integer numbers (8 bits).

Number of Activations (#Activations)

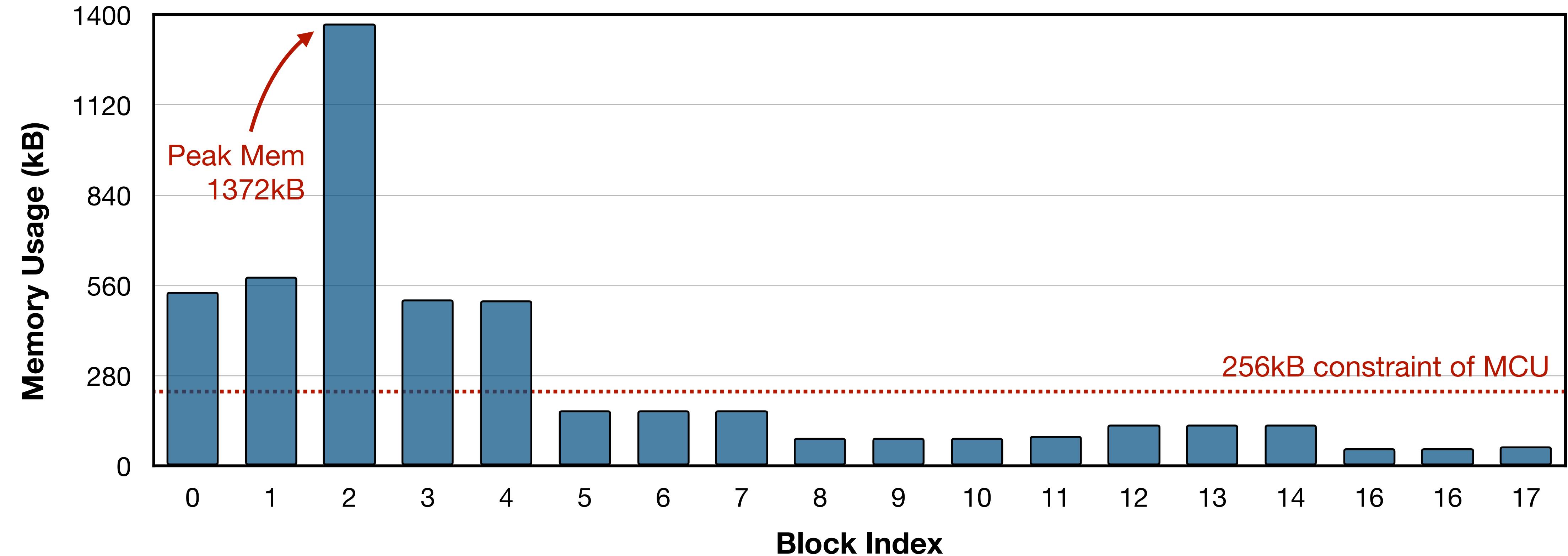
#Activation didn't improve from ResNet to MobileNet-v2



* All parameters and activations are Integer numbers (8 bits).

Number of Activations (#Activations)

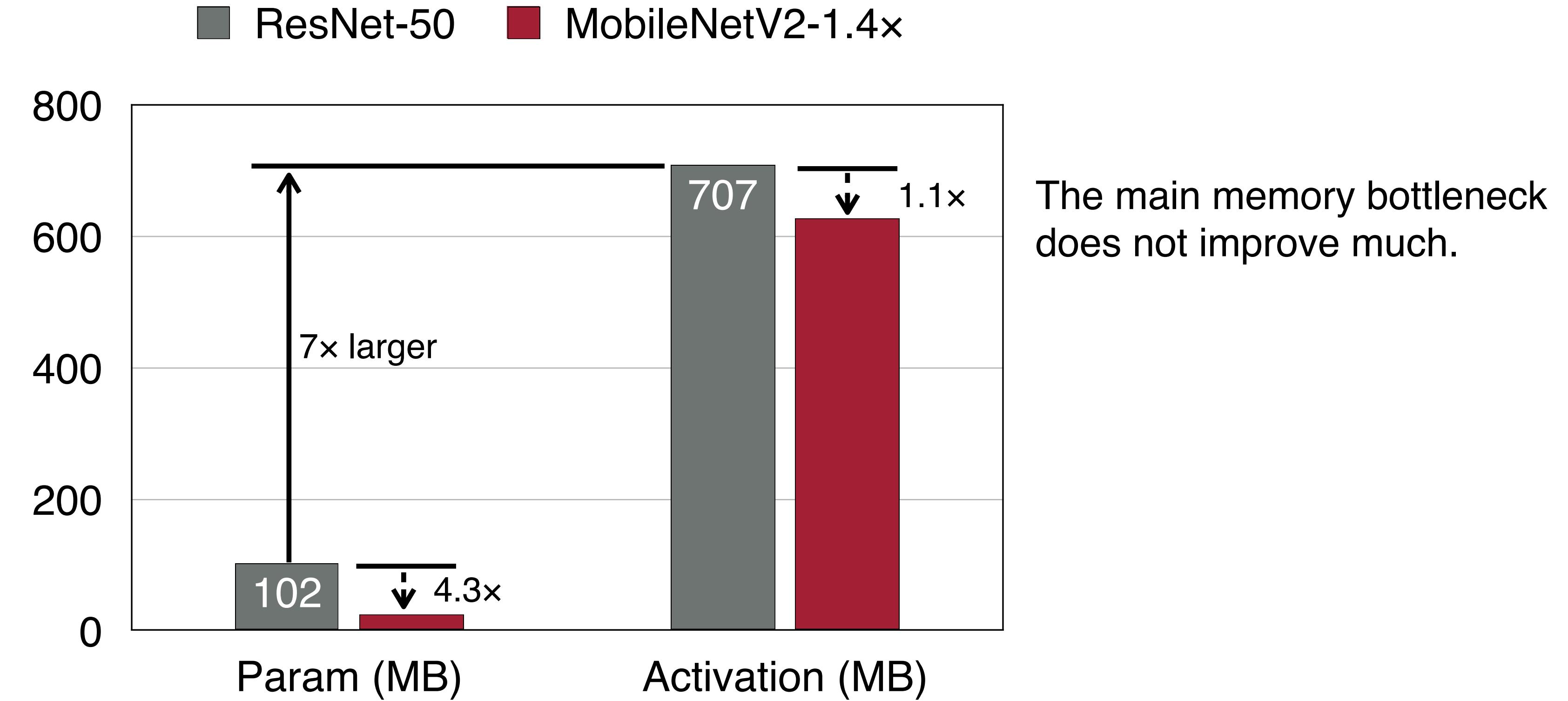
Imbalanced memory distribution of MobileNetV2



MCUNet: Tiny Deep Learning on IoT Devices [Lin et al., NeurIPS 2020]

Number of Activations (#Activations)

#Activation is the memory bottleneck in training, not #Parameters.

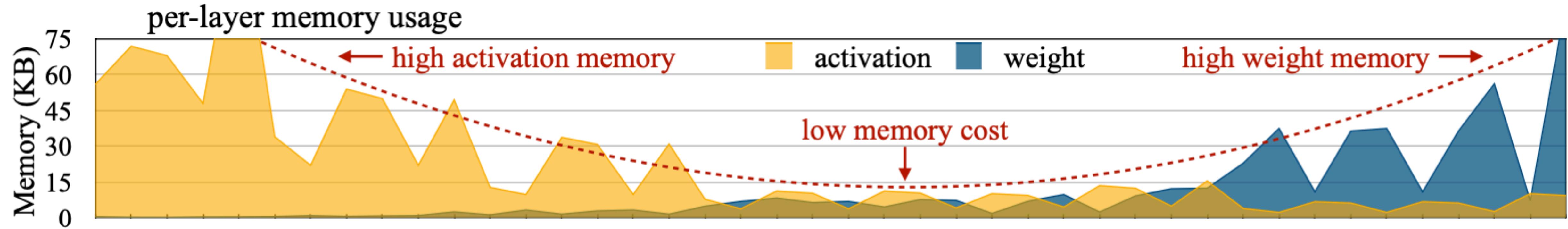


* All parameters and activations are Floating-Point numbers (32 bits).

TinyTL: Reduce Activations, Not Trainable Parameters for Efficient On-Device Learning [Cai et al., NeurIPS 2020]

Number of Activations (#Activations)

Activation and weight memory distribution of MCUNet



MCUNet: Tiny Deep Learning on IoT Devices [Lin et al., NeurIPS 2020]

AlexNet: #Activations

AlexNet	C × H × W
Image (3×224×224)	$3 \times 224 \times 224 = 150,528$
11×11 Conv, channel 96, stride 4, pad 2	$96 \times 55 \times 55 = 290,400$
3×3 MaxPool, stride 2	$96 \times 27 \times 27 = 69,984$
5×5 Conv, channel 256, pad 2, groups 2	$256 \times 27 \times 27 = 186,624$
3×3 MaxPool, stride 2	$256 \times 13 \times 13 = 43,264$
3×3 Conv, channel 384, pad 1	$384 \times 13 \times 13 = 64,896$
3×3 Conv, channel 384, pad 1, groups 2	$384 \times 13 \times 13 = 64,896$
3×3 Conv, channel 256, pad 1, groups 2	$256 \times 13 \times 13 = 43,264$
3×3 MaxPool, stride 2	$256 \times 6 \times 6 = 9,216$
Linear, channel 4096	$4096 = 4,096$
Linear, channel 4096	$4096 = 4,096$
Linear, channel 1000	$1000 = 1,000$

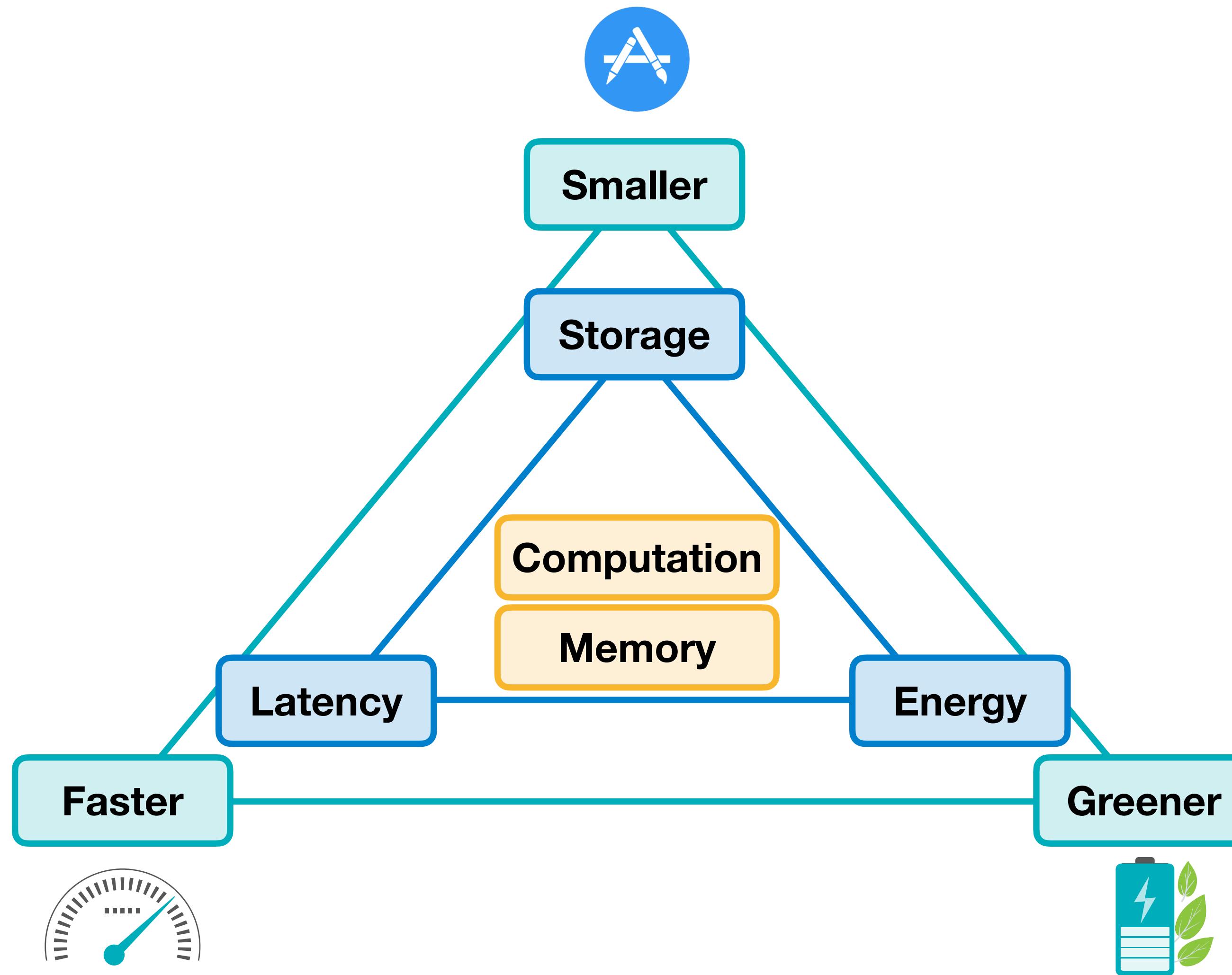
Total #Activation: 932,264

Peak #Activation:

$\approx \#input\ activation + \#output\ activation$

$= 150,528 + 290,400 = 440,928$

Efficiency of Neural Networks



Efficiency Metrics

Memory-Related

#parameters

model size

total/peak #activations

Computation-Related

MAC

FLOP, FLOPS

OP, OPS

Number of Multiply-Accumulate Operations

MAC

- Multiply-Accumulate operation (MAC)

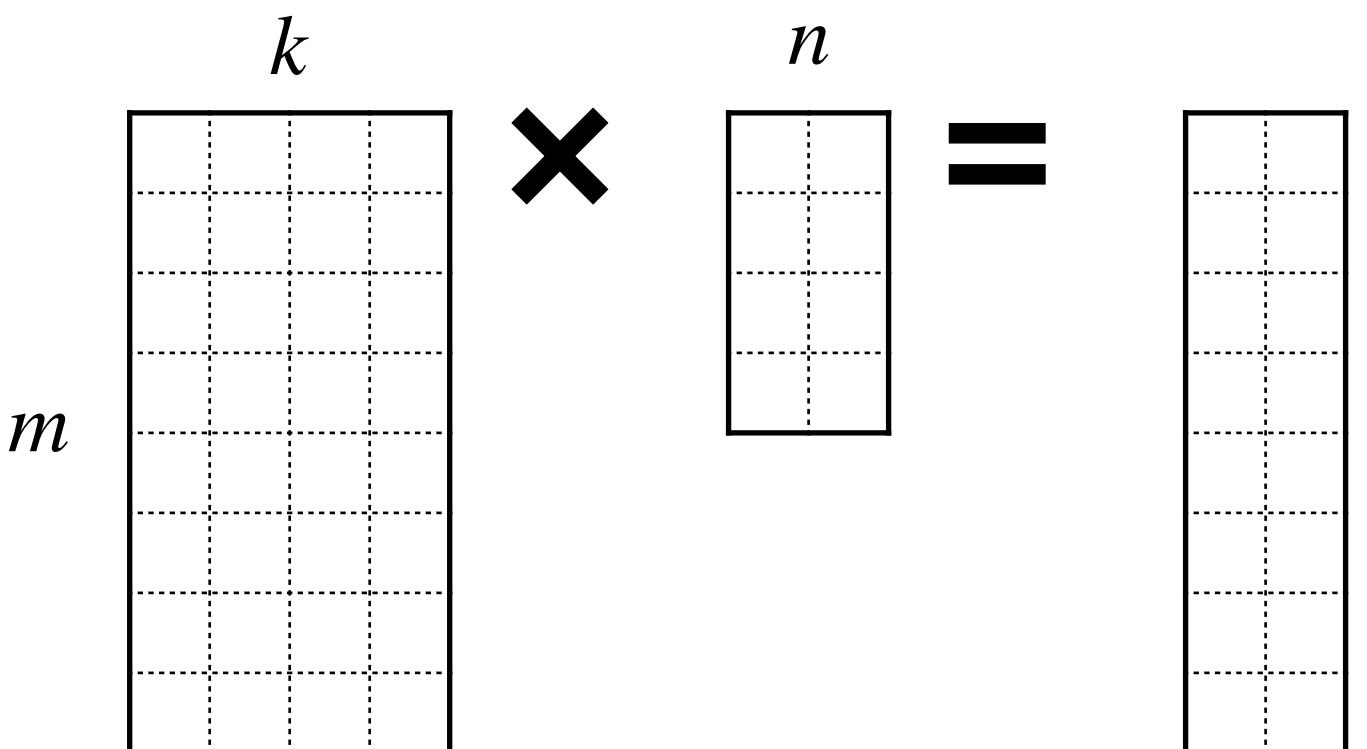
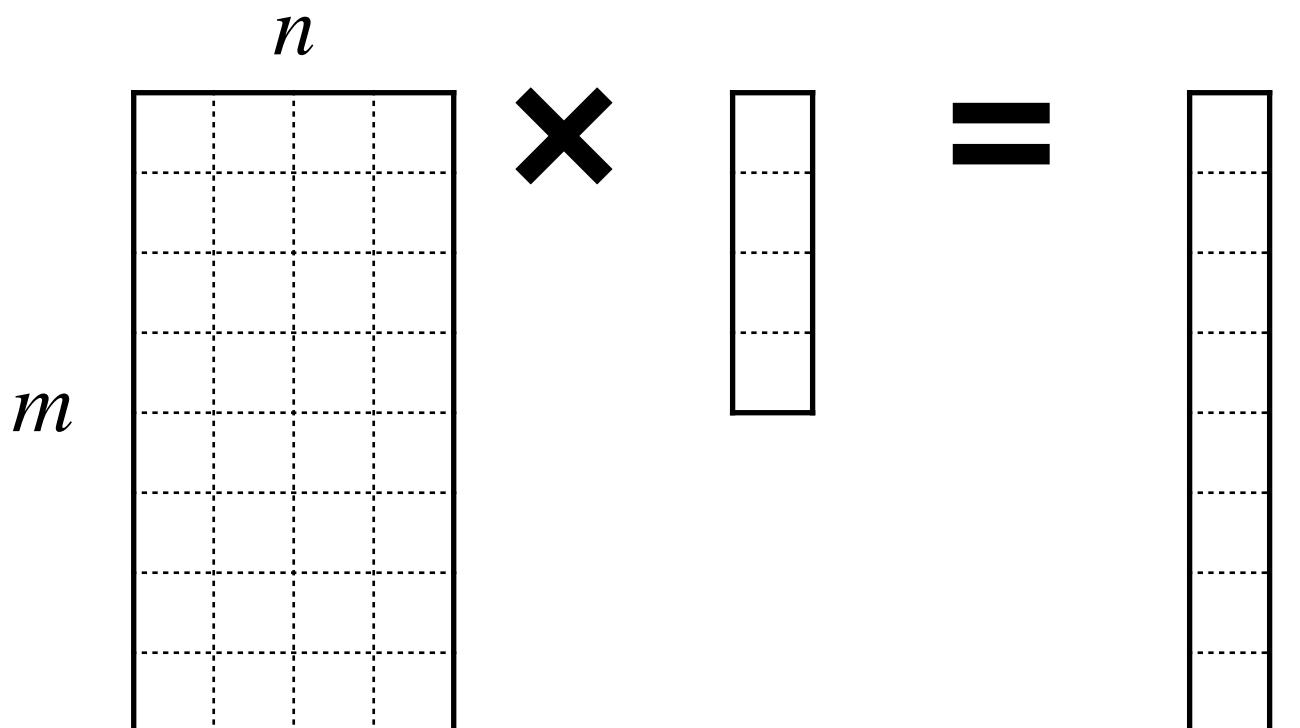
- $a \leftarrow a + b \cdot c$

- Matrix-Vector Multiplication (MV)

- $MACs = m \cdot n$

- General Matrix-Matrix Multiplication (GEMM)

- $MACs = m \cdot n \cdot k$

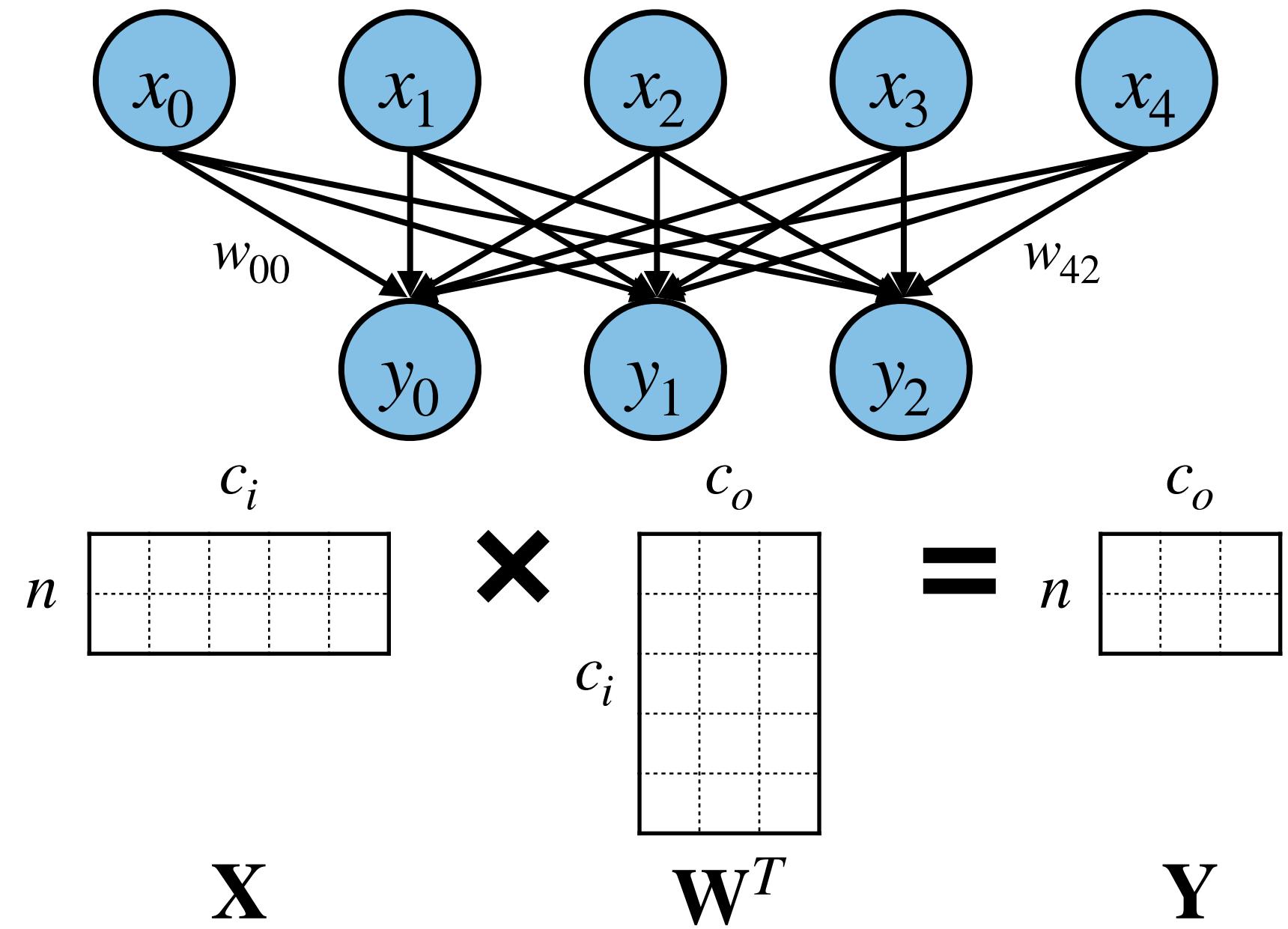


Number of Multiply-Accumulate Operations

MAC

Layer	MACs (batch size n=1)
Linear Layer	$c_o \cdot c_i$
Convolution	
Grouped Convolution	
Depthwise Convolution	

* bias is ignored



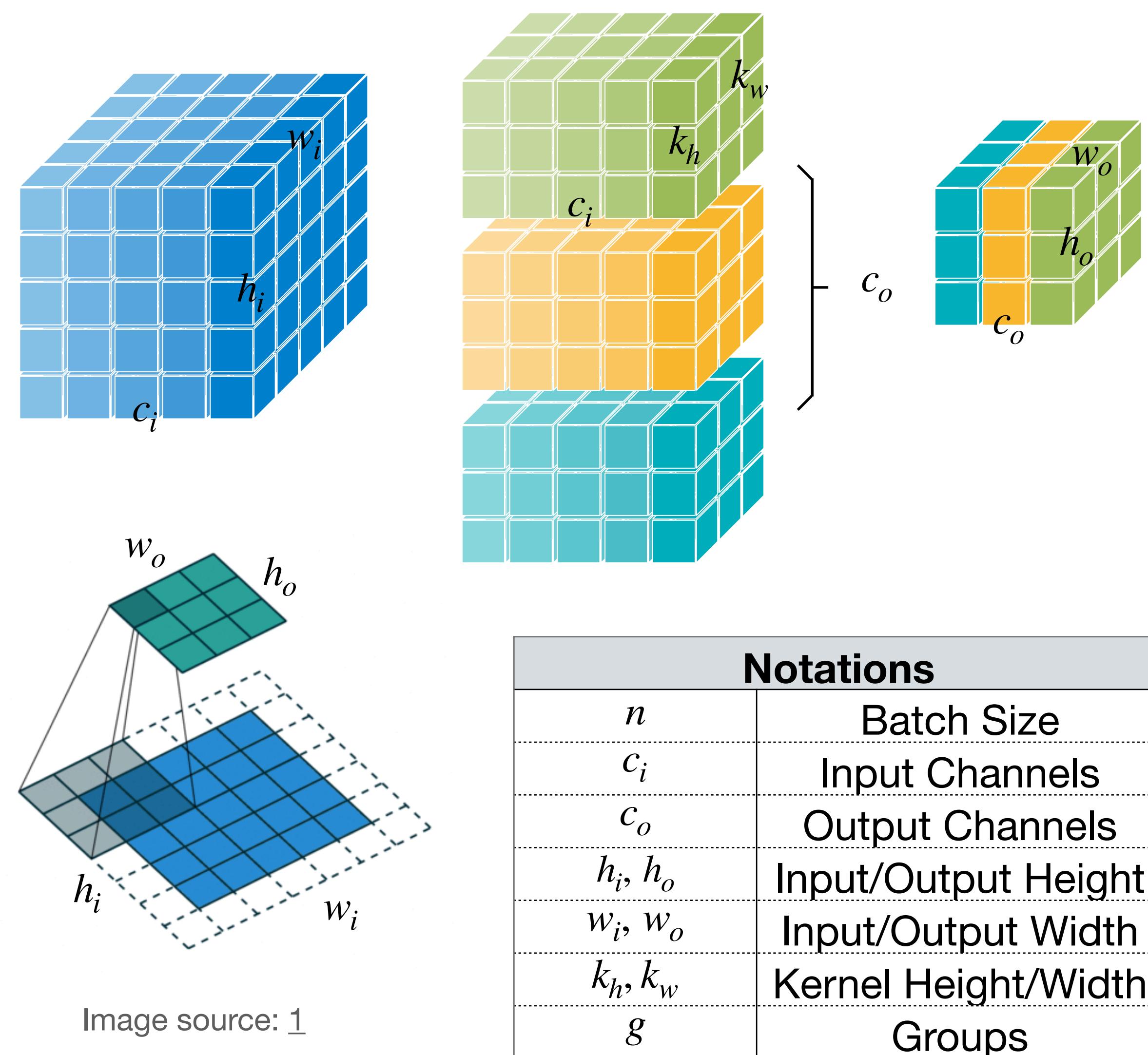
Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h, k_w	Kernel Height/Width
g	Groups

Number of Multiply-Accumulate Operations

MAC

Layer	MACs (batch size n=1)
Linear Layer	$c_o \cdot c_i$
Convolution	$c_i \cdot k_h \cdot k_w \cdot h_o \cdot w_o \cdot c_o$
Grouped Convolution	
Depthwise Convolution	

* bias is ignored



Number of Multiply-Accumulate Operations

MAC

Layer	MACs (batch size n=1)
Linear Layer	$c_o \cdot c_i$
Convolution	$c_i \cdot k_h \cdot k_w \cdot h_o \cdot w_o \cdot c_o$
Grouped Convolution	$c_i/g \cdot k_h \cdot k_w \cdot h_o \cdot w_o \cdot c_o$
Depthwise Convolution	

* bias is ignored

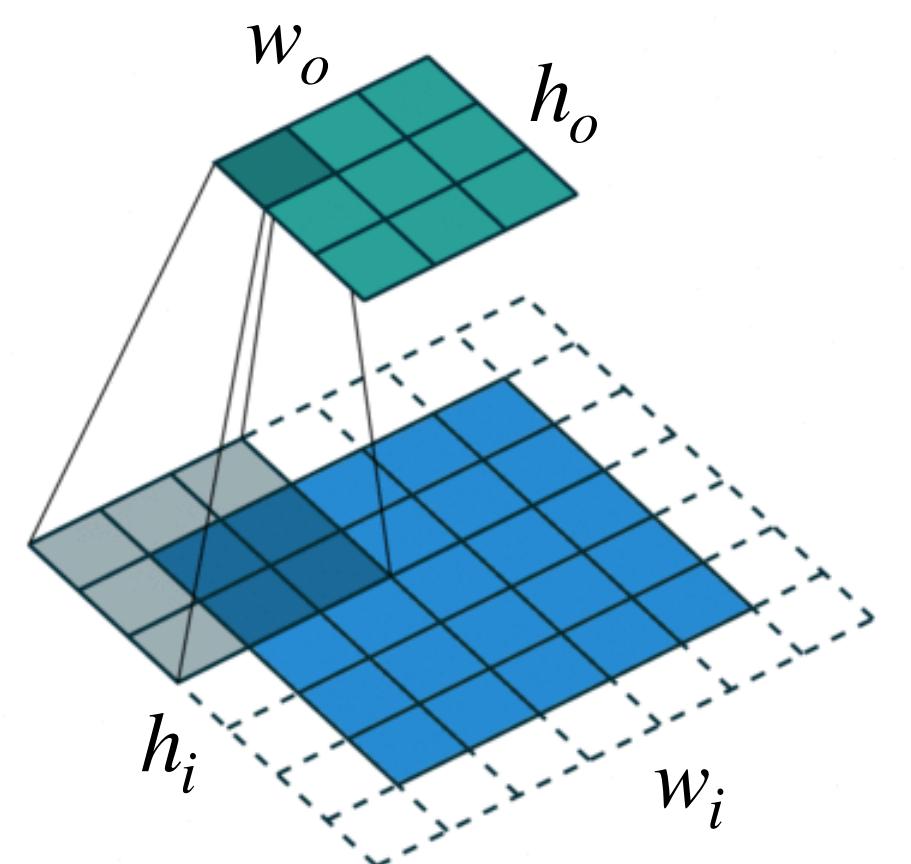
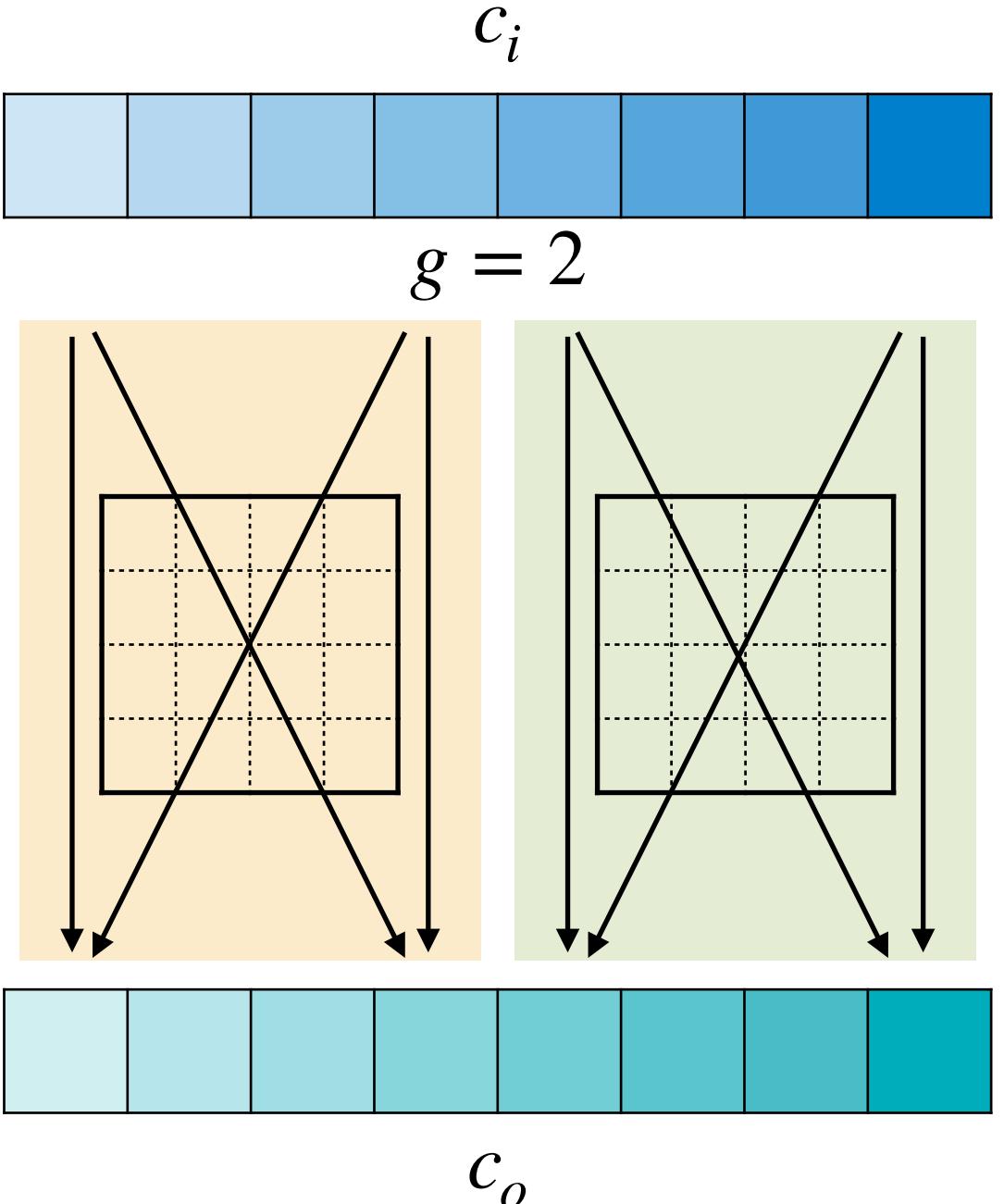


Image source: 1



Notations	
n	Batch Size
c_i	Input Channels
c_o	Output Channels
h_i, h_o	Input/Output Height
w_i, w_o	Input/Output Width
k_h, k_w	Kernel Height/Width
g	Groups

Number of Multiply-Accumulate Operations

MAC

Layer	MACs (batch size n=1)
Linear Layer	$c_o \cdot c_i$
Convolution	$c_i \cdot k_h \cdot k_w \cdot h_o \cdot w_o \cdot c_o$
Grouped Convolution	$c_i/g \cdot k_h \cdot k_w \cdot h_o \cdot w_o \cdot c_o$
Depthwise Convolution	$k_h \cdot k_w \cdot h_o \cdot w_o \cdot c_o$

* bias is ignored

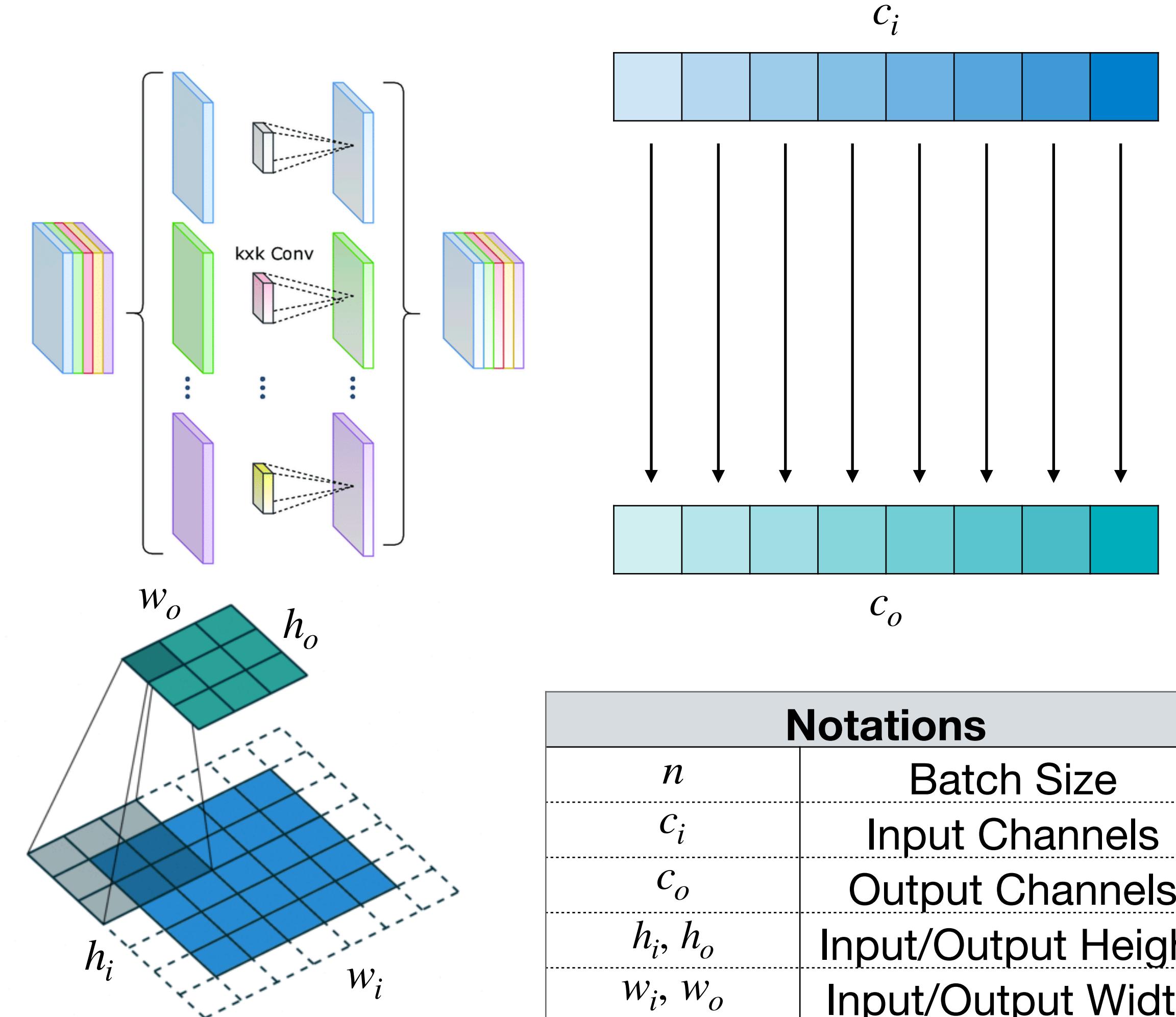


Image source: 1

AlexNet: #MACs

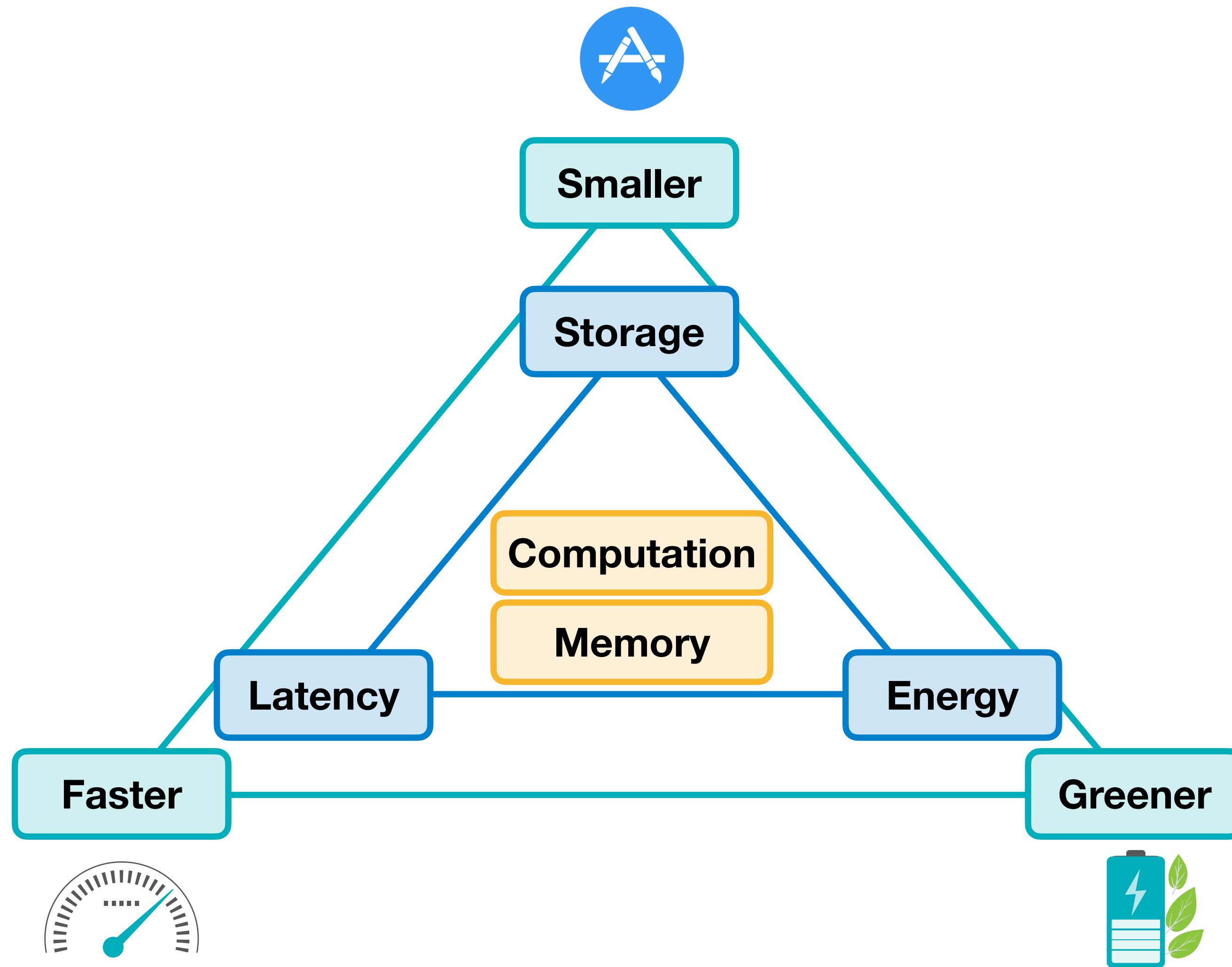
AlexNet	C × H × W	MACs
Image (3×224×224)	3×224×224	
11×11 Conv, channel 96, stride 4, pad 2	96×55×55	$96 \times 3 \times 11 \times 11 \times 55 \times 55 = 105,415,200$
3×3 MaxPool, stride 2	96×27×27	
5×5 Conv, channel 256, pad 2, groups 2	256×27×27	$256 \times 96 \times 5 \times 5 \times 27 \times 27 / 2 = 223,948,800$
3×3 MaxPool, stride 2	256×13×13	
3×3 Conv, channel 384, pad 1	384×13×13	$384 \times 256 \times 3 \times 3 \times 13 \times 13 = 149,520,384$
3×3 Conv, channel 384, pad 1, groups 2	384×13×13	$384 \times 384 \times 3 \times 3 \times 13 \times 13 / 2 = 112,140,288$
3×3 Conv, channel 256, pad 1, groups 2	256×13×13	$256 \times 384 \times 3 \times 3 \times 13 \times 13 / 2 = 74,700,144$
3×3 MaxPool, stride 2	256×6×6	
Linear, channel 4096	4096	$4096 \times (256 \times 6 \times 6) = 37,748,736$
Linear, channel 4096	4096	$4096 \times 4096 = 16,777,216$
Linear, channel 1000	1000	$1000 \times 4096 = 4,096,000$

Layer	MACs (batch size n=1)
Linear Layer	$c_o \cdot c_i$
Convolution	$c_o \cdot c_i \cdot k_h \cdot k_w \cdot h_o \cdot w_o$
Grouped Convolution	$c_o \cdot c_i \cdot k_h \cdot k_w \cdot h_o \cdot w_o / g$
Depthwise Convolution	$c_o \cdot k_h \cdot k_w \cdot h_o \cdot w_o$

724M in total !

ImageNet Classification with Deep Convolutional Neural Networks [Krizhevsky et al., NeurIPS 2012]

Efficiency of Neural Networks



Efficiency Metrics

Memory-Related

#parameters

model size

total/peak #activations

Computation-Related

MAC

FLOP, FLOPS

OP, OPS

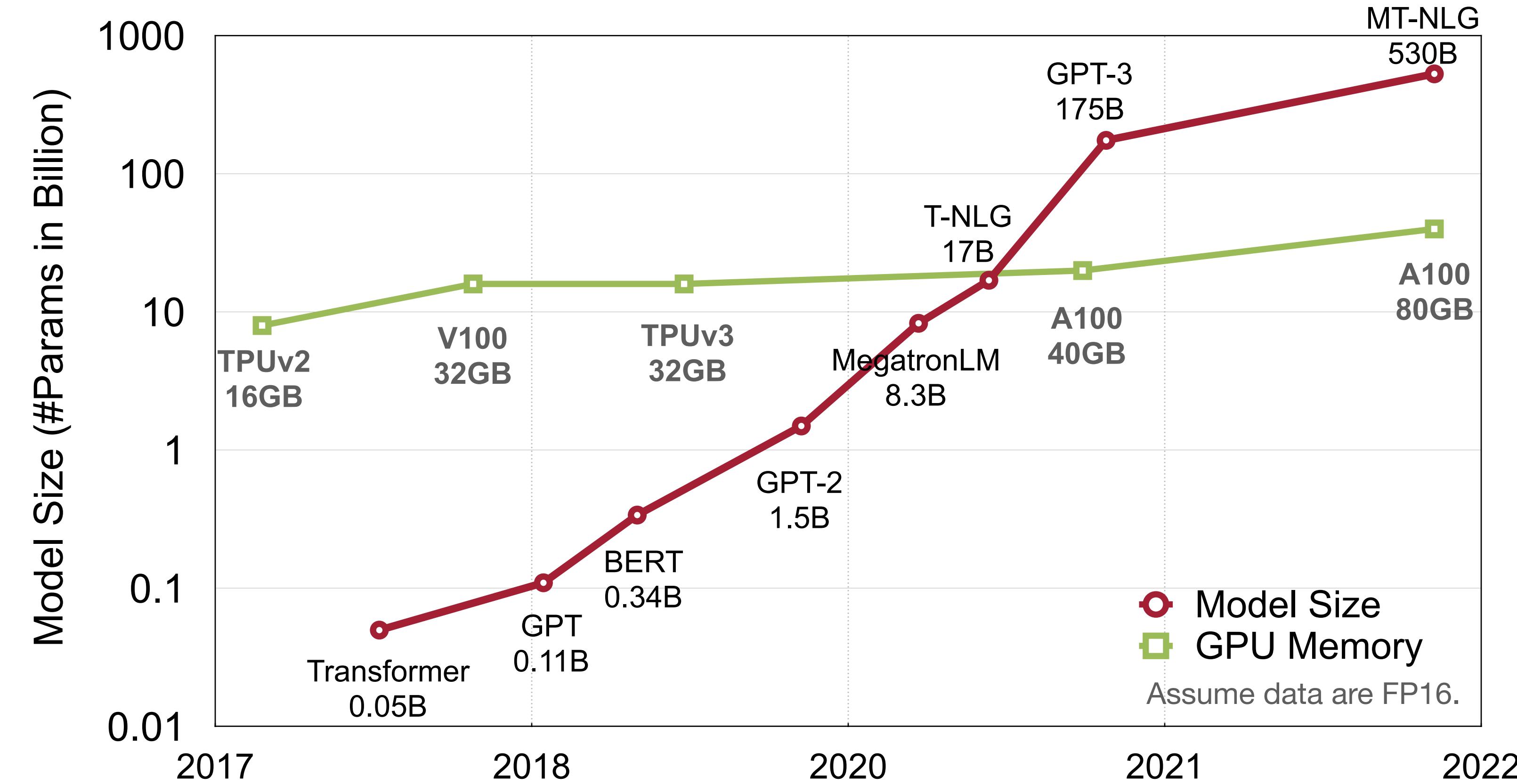
Number of Floating Point Operations (FLOP)

- A multiply is a floating point operation
- An add is a floating point operation
- **One** multiply-accumulate operation is **two** floating point operations (FLOP)
 - Example: AlexNet has 724M MACs, total number of floating point operations will be
 - $724M \times 2 = 1.4G$ FLOPs
- Floating Point Operation Per Second (FLOPS)
 - $FLOPS = \frac{FLOPs}{second}$

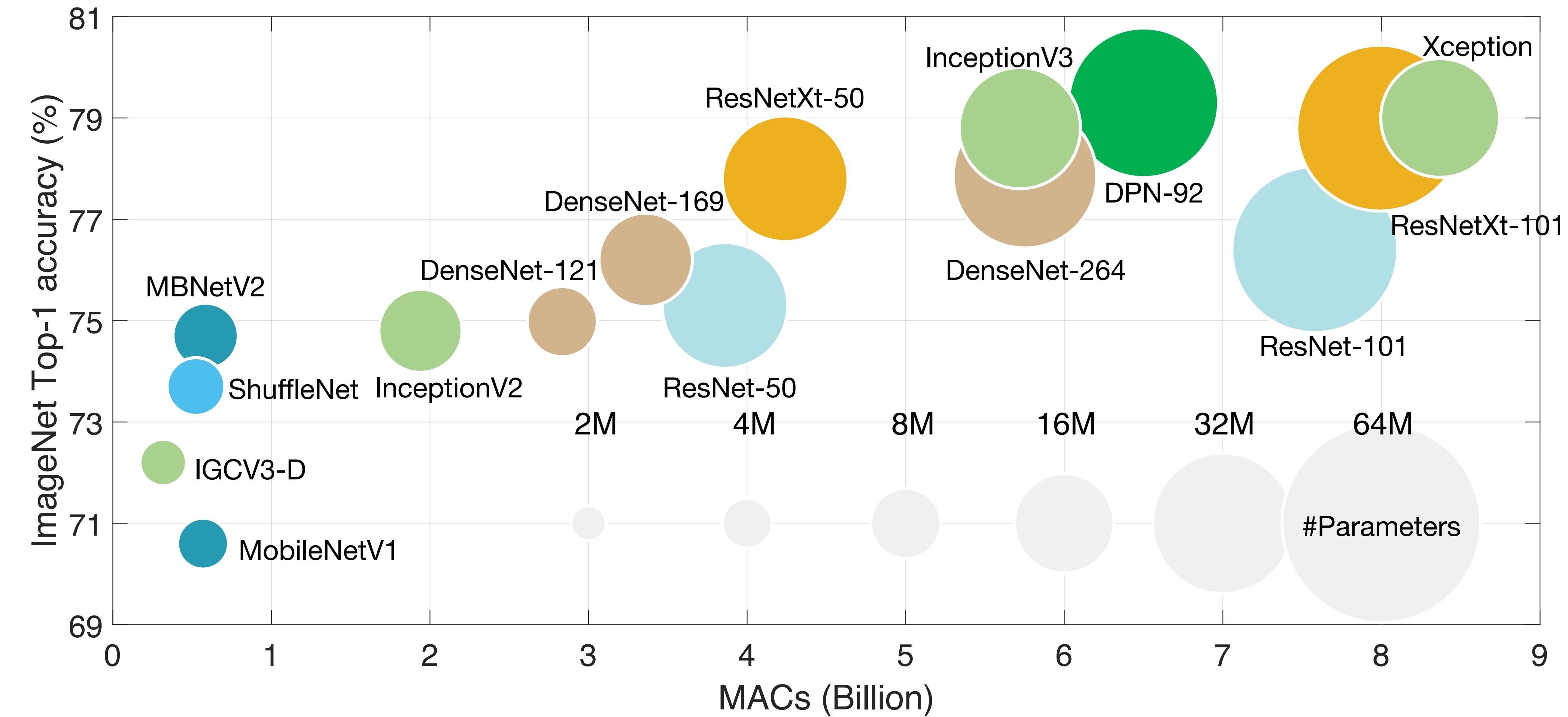
Number of Operations (OP)

- Activations/weights in neural network computing are not always floating point.
- To generalize, number of operations is used to measure the computation amount.
 - Example: AlexNet has 724M MACs, total number of floating point operations will be
 - $724M \times 2 = 1.4G$ OPs
- Similarly, Operation Per Second (OPS)
 - $$OPS = \frac{OPs}{second}$$

Today's AI is too BIG!

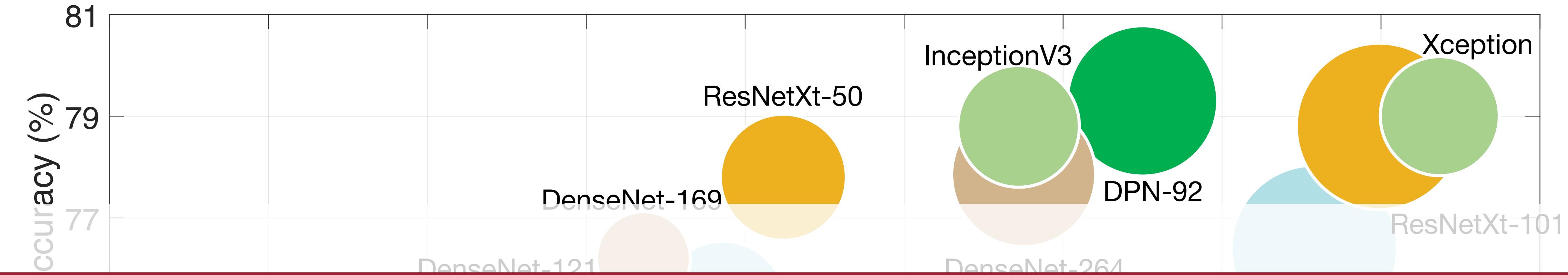


Today's AI is too BIG!

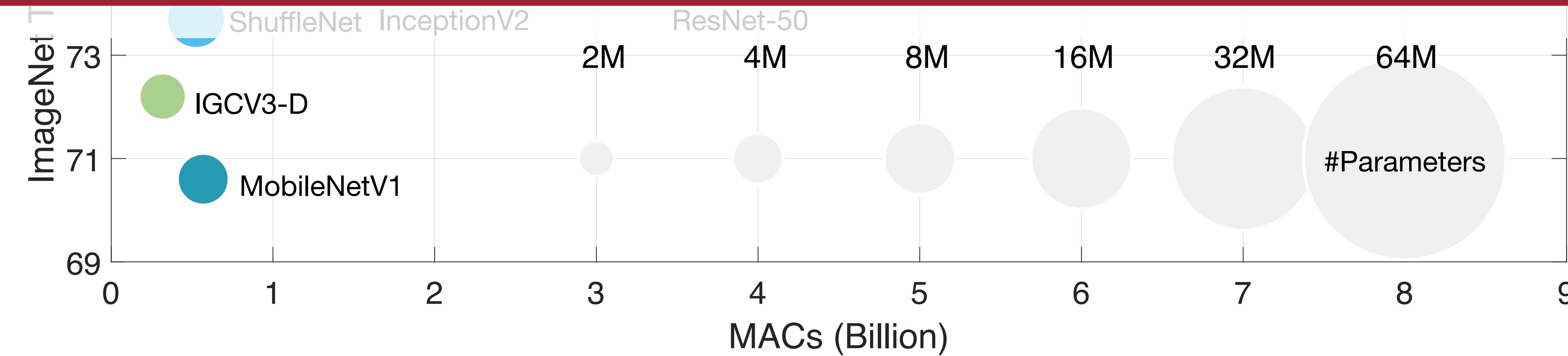


Model Compression and Hardware Acceleration for Neural Networks: A Comprehensive Survey [Deng et al., IEEE 2020]

Today's AI is too BIG!



How should we make deep learning more efficient?



Model Compression and Hardware Acceleration for Neural Networks: A Comprehensive Survey [Deng et al., IEEE 2020]

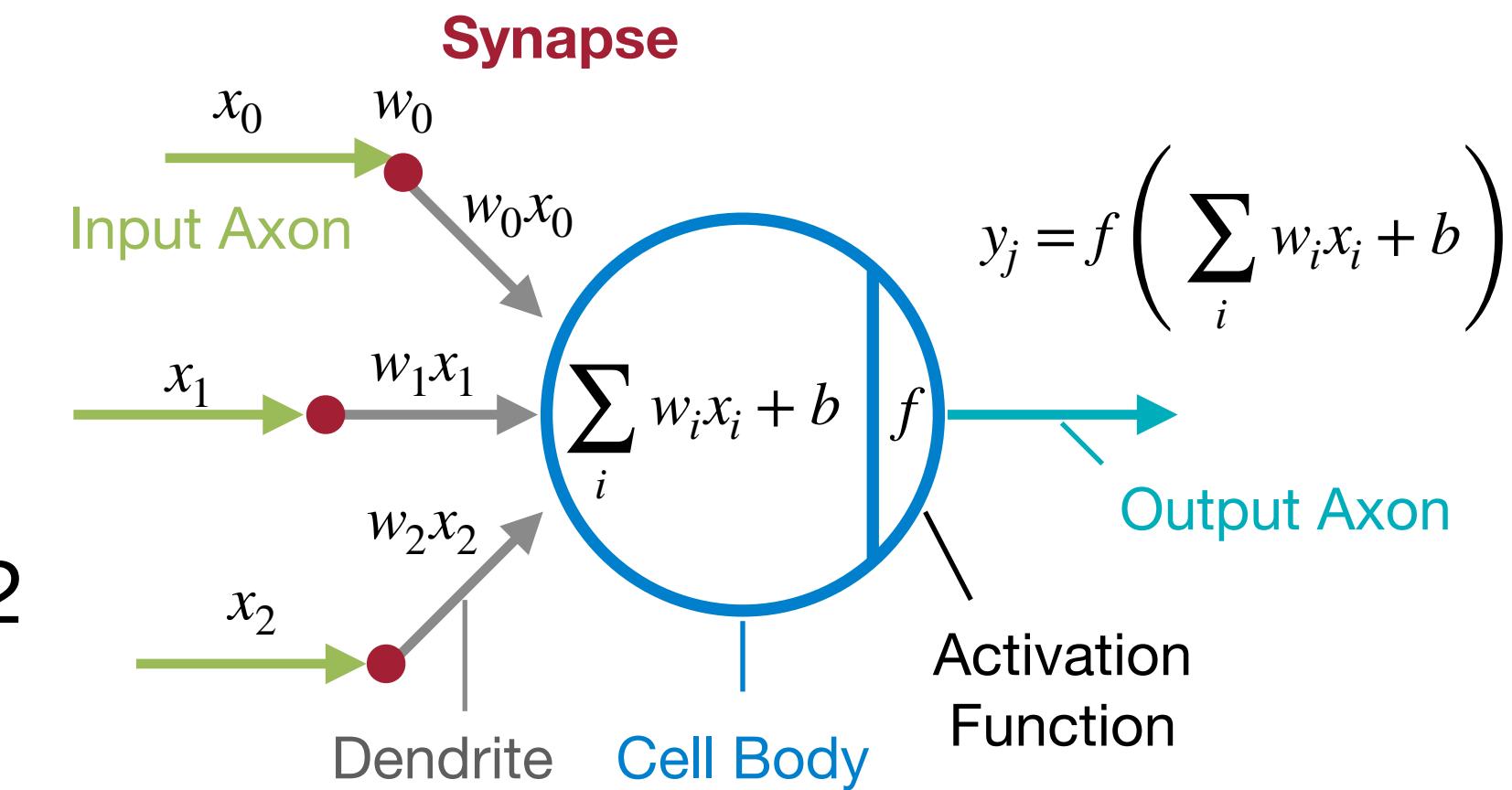
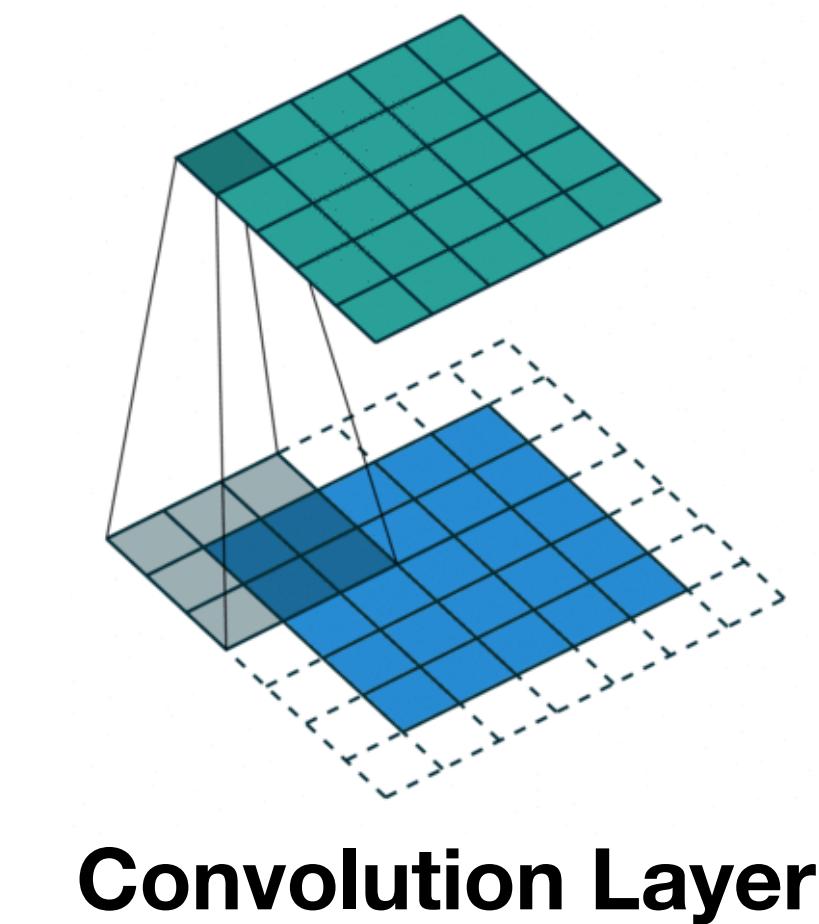
Summary of Today's Lecture

In this lecture, we

- Reviewed the basics of neural networks
 - terminology: neuron output → activation, synapses → weight
 - popular layers: fully-connected, convolution, depthwise convolution, pooling, normalization
 - classic neural networks: AlexNet, VGG-16, ResNet-50, MobileNetV2
- Introduced popular efficiency metrics for neural networks
 - memory cost: #Parameters, Model Size, #Activations
 - computation cost: MACs, FLOP, FLOPS, OP, OPS

$$n \begin{matrix} c_i \\ \boxed{\text{---}} \end{matrix} \times \begin{matrix} c_o \\ \boxed{\text{---}} \end{matrix} = n \begin{matrix} c_o \\ \boxed{\text{---}} \end{matrix}$$

Linear Layer



Layer	MACs (batch size n=1)
Linear Layer	$c_o \cdot c_i$
Convolution	$c_i \cdot k_h \cdot k_w \cdot h_o \cdot w_o \cdot c_o$
Grouped Convolution	$c_i/g \cdot k_h \cdot k_w \cdot h_o \cdot w_o \cdot c_o$
Depthwise Convolution	$k_h \cdot k_w \cdot h_o \cdot w_o \cdot c_o$

Image source: 1

Lab 0: Getting Started

Tutorial on PyTorch and Laboratory Exercises

References

1. Convolution arithmetic [[Github Repo](#)]
2. Image Classification with CNNs [[Stanford CS231n Lecture 5](#)]
3. Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift [[Ioffe et al., ICML 2015](#)]
4. Group Normalization [[Wu et al., ECCV 2018](#)]
5. ImageNet Classification with Deep Convolutional Neural Networks [[Krizhevsky et al., NeurIPS 2012](#)]
6. Very Deep Convolutional Networks for Large-Scale Image Recognition [[Simonyan et al., ICLR 2015](#)]
7. Deep Residual Learning for Image Recognition [[He et al., CVPR 2016](#)]
8. MobileNetV2: Inverted Residuals and Linear Bottlenecks [[Sandler et al., CVPR 2018](#)]
9. Model Compression and Hardware Acceleration for Neural Networks: A Comprehensive Survey [[Deng et al., IEEE 2020](#)]