

# Empirical Methods in Financial Econometrics:Midterm Exam

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October 2, 2019

## Question 0

The stocks I will use for solving this exam:

Stock	Ticker
1	DIS
2	PG
3	SPY

## Question 1

### A

The “t” for the date “September 16, 2008” is 430.

It is impossible to estimate IV for today if it is still in the morning. Because we don’t have enough returns to estimate IV.

### B

The estimate for yesterday’s integrated variance of DIS is  $4.5898 \times 10^{-04}$

The estimate for yesterday’s integrated variance of PG is  $2.2365 \times 10^{-04}$

Interpret: The estimate for integrated variance I used is the truncated variance, which is the sum of the square of the continuous returns. Because we can not get the integrated variance directly, the truncated variance is used to get an asymptotic one.

The estimate for next day’s integrated variance of DIS is  $9.2363 \times 10^{-04}$

The estimate for next day’s integrated variance of PG is  $7.5846 \times 10^{-04}$

Justify: We can see the estimate of next day’s integrated variance is obviously bigger than the estimate of yesterdays’s integrated variance, so it is not wise to use the yesterday’s estimate to forecast the next one.

The reason could be the data of one day is much less than what we need to forecast.

### C

Stock	q	Estimate of $P(r_t^c \leq -q)$		
		Estimate	Lower bound	Upper bound
1	2%	0.1753	0.1268	0.2093
1	4%	0.0309	0.0112	0.0528
2	2%	0.0906	0.0397	0.1308
2	4%	0.0037	$2.2492 \times 10^{-4}$	0.0124

Comment: The width of the confidence interval in DIS is 0.0825 and 0.0416 respectively. The width of the confidence interval in DIS is 0.0911 and 0.0121 respectively. Most of them are around or in the range 0.01-0.06, so I think the estimation accuracy is good.

## D

VaR Estimate and 95% Confidence Interval				
Stock	p	VaR	Lower bound	Upper bound
1	1%	$-9.9679 \times 10^6$	$-1.1502 \times 10^7$	$-8.1495 \times 10^6$
1	5%	$-7.0478 \times 10^6$	$-8.1327 \times 10^6$	$-5.7622 \times 10^6$
2	1%	$-6.9580 \times 10^6$	$-8.2884 \times 10^6$	$-5.3038 \times 10^6$
2	5%	$-4.9197 \times 10^6$	$-5.8604 \times 10^6$	$-3.7501 \times 10^6$

Comment: The width of DIS is 3.3528 million(1%) and 2.3706 million(5%) respectively; The width of PG is 2.9847 million(1%) and 2.1103 million(5%) respectively. At least we can find the range of the loses of each stocks, or the maximum and minimum of the loses of each stocks, so I think my boss could find them helpful by using this information to adjust stock holding.

## Question 2

### A

Summary Statistics of Long-Short Continuous Returns				
Average	Min	5% Percentile	95% Percentile	Max
$-1.5566 \times 10^{-6}$	-0.0357	-0.0022	0.0021	0.0416

### B

Summary Statistics of the Realized Beta				
Average	Min	5% Percentile	95% Percentile	Max
0.3899	-1.3388	-0.2081	0.9650	2.2904

### C

The figure is below:

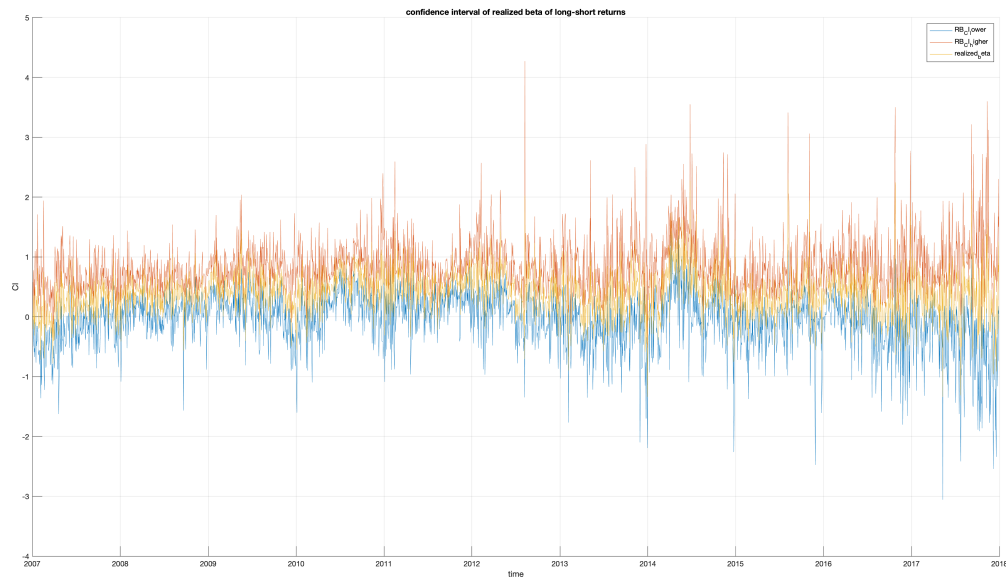


Figure 1: confidence interval of realized beta of long-short returns

Comment: I think the long-short position appears market neutral at least visually, because the realized beta of the long-short portfolio is around 0.

**D**

The figure is below:

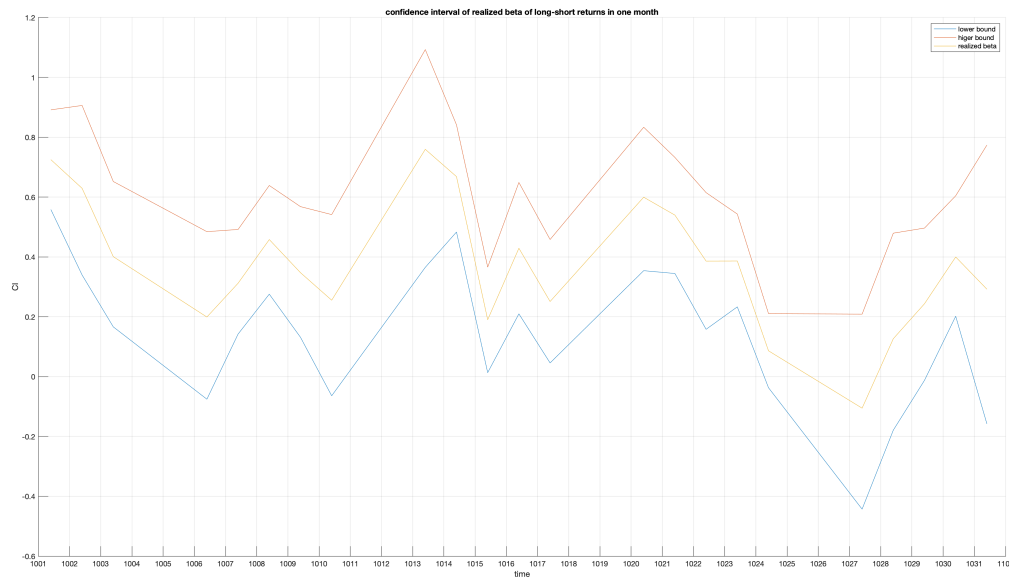


Figure 2: confidence interval of realized beta of long-short returns in one month

Interpret: The trend of the realized beta of long-short returns in one month is fluctuated from 0 to 1. The confidence intervals of the realized beta of long-short returns are good because the plot of the realized beta of long-short returns is under the upper confidence interval and above the lower of confidence interval.

## E

The total number of rejections are 1397.

The percentage of rejections is 50.45%. It is far bigger than 10%, so I think the hedge fund holding long stock 1 and short stock 2 would not be considered market neutral.

## Question 3

### A

Summary Statistics for Continuous Returns					
Stock	Average	Min	5% Percentile	95% Percentile	Max
1	$4.3967 \times 10^{-6}$	-0.0323	-0.0022	0.0022	0.0474
2	$5.4237 \times 10^{-6}$	-0.0254	-0.0015	0.0016	0.0420
SPY	$1.6385 \times 10^{-6}$	-0.0233	-0.0015	0.0015	0.0376

**B**

I detected 116 jumps in the market.

**C**

Summary Statistics of the Realized Beta					
Stock	Average	Min	5% Percentile	95% Percentile	Max
1	0.9312	-1.0811	0.4731	1.3575	-1.0811
2	0.5412	-0.4167	0.1475	0.9690	-0.4167

**D**

The figure is below:

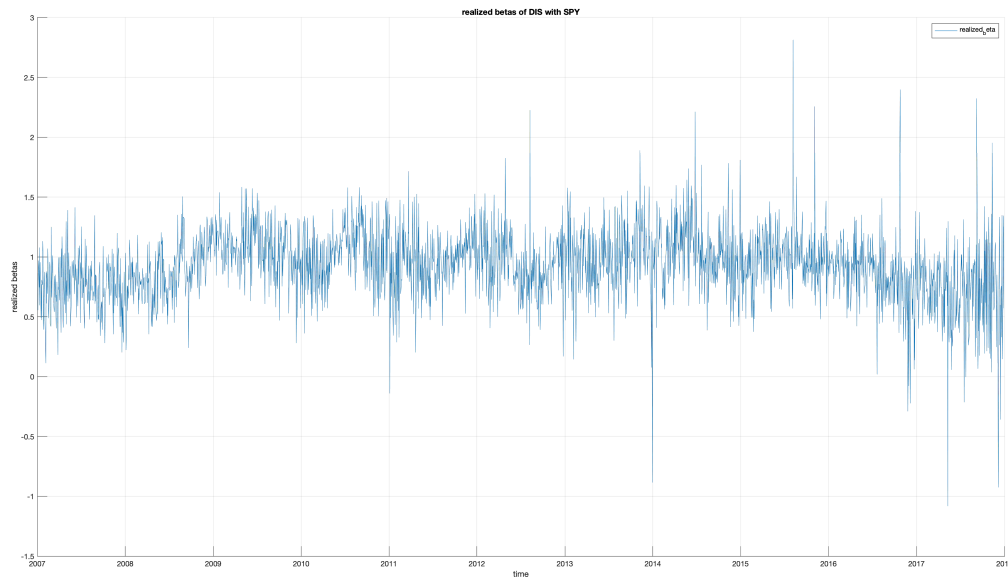


Figure 3: realized betas of DIS with SPY

The figure is below:

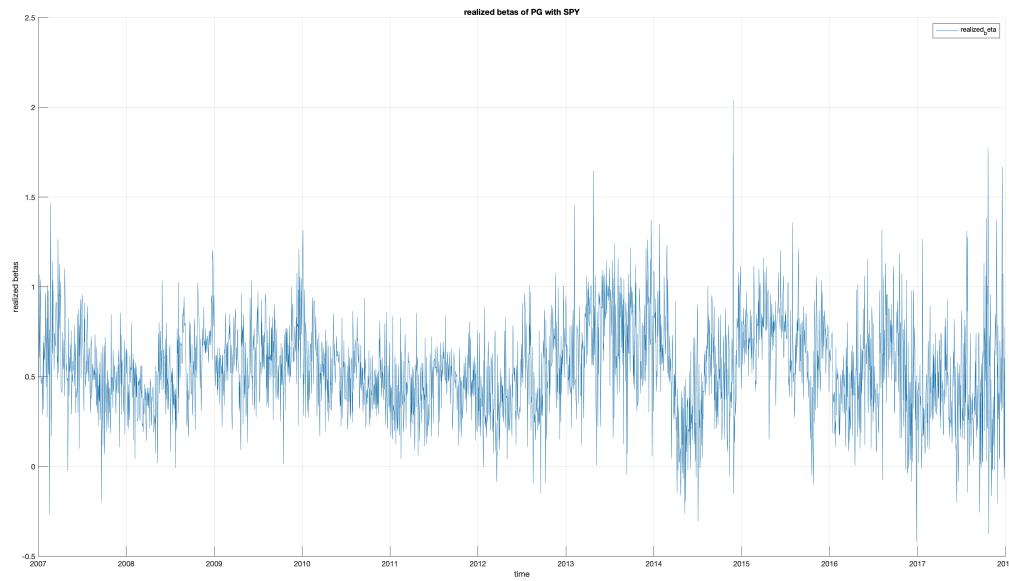


Figure 4: realized betas of PG with SPY

From the plots I can see, the DIS is generally as risky as the market because the  $\beta$  is around 1 ; the PG is generally less risky than the market because the  $\beta$  is below than 1.

**E**

Summary Statistics of the Residual Correlation				
Average	Min	5% Percentile	95% Percentile	Max
0.0196	-0.4993	-0.2476	0.2909	0.5563

**F**

The figure is below:

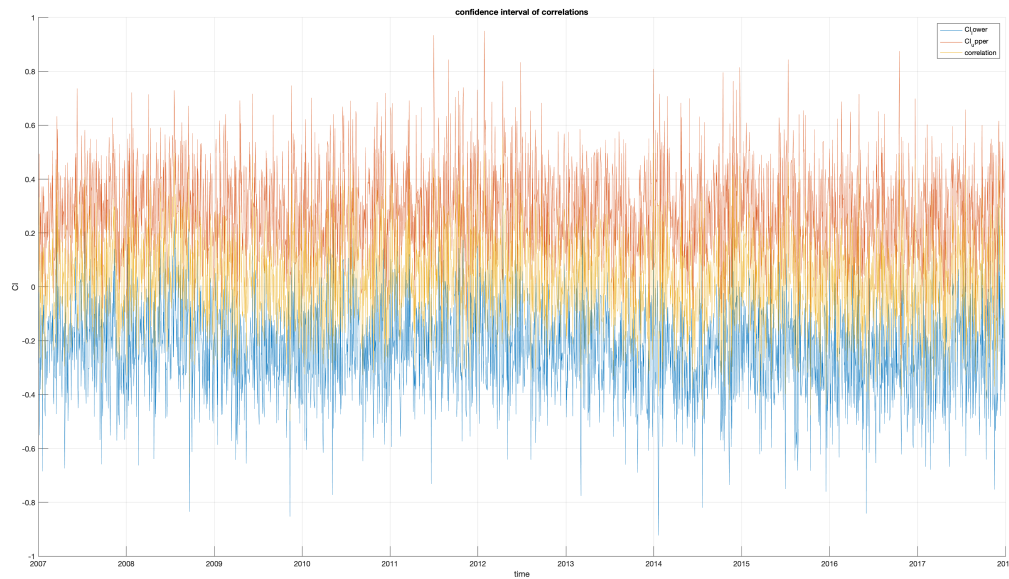


Figure 5: confidence interval of realized correlations

Interpret: The correlation is fluctuated dramatically around 0 from 2007 to 2017. The confidence intervals of the correlation follow the correlation to fluctuate at the same time. The upper and lower limits of the confidence intervals are 1 and -1 respectively.

**G**

The figure is below:



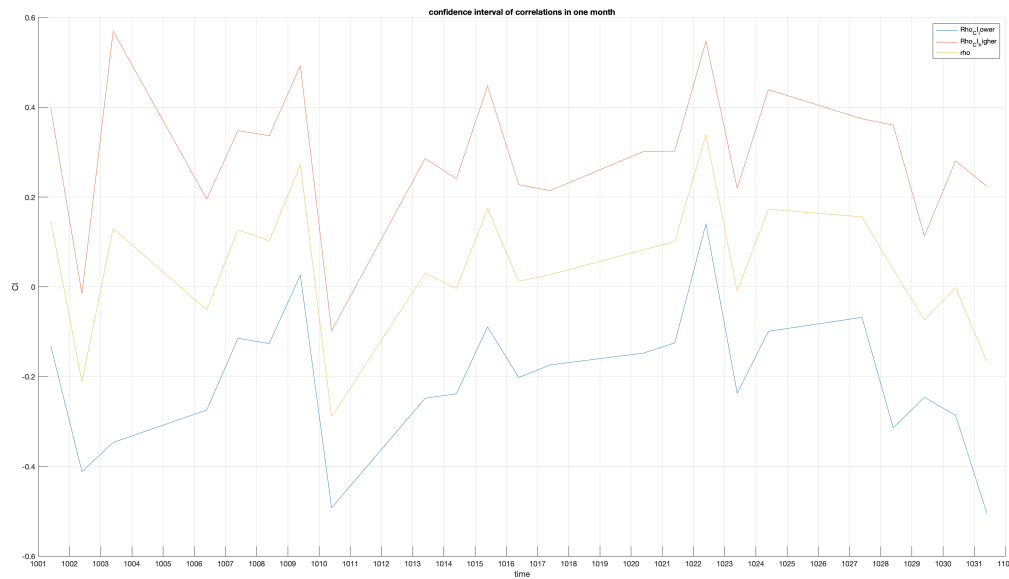


Figure 6: confidence interval of realized correlations in one month

Interpret: We can see the trend more clearly in one month. The correlation is fluctuate around 0 from -0.3 to 0.4. The upper and lower limits of the confidence intervals are 0.6 and -0.6 respectively.

## H

The number of  $p_0$  is 10.9831.

The number of  $p_+$  is 0.7897.

The number of  $p_-$  is 0.4722.

Interpret: The  $p_0$  is 10.9831, which is most of the 11 years, so we do not have enough evidences to reject  $H_0$ , which is the realized correlation is 0.

## Code

The code is below:

Listing 1: q\_1.m

```

1 % A
2 [dates, prices] = load_stock('DIS.csv');
3 [dates_return, deltax] = log_returns(dates, prices);
4 [n, T] = size(deltax);
5

```

```
6 zoom_end_916 = find(dates_return==datenum(2008,9,16,16,00,0))/n;
7 dates_zoom_916 = dates_return(:,zoom_end_916);
8
9 % B
10 zoom_end_915 = find(dates_return==datenum(2008,9,15,16,00,0))/n;
11 dates_zoom_915 = dates_return(:,zoom_end_915);
12
13 deltan = 1/n;
14 deltax_915 = deltax(:,zoom_end_915);
15 tau_915 = tau_f(deltax_915);
16 BV_915 = bipower_var(deltax_915);
17 alpha = 5;
18 cutoff = alpha*deltan^0.49*sqrt(tau_915*BV_915);
19 rc_915 = deltax_915;
20 rc_915(abs(deltax_915)>cutoff)=0;
21
22 TV_915 = sum((rc_915).^2);
23
24 % use the same way on 916
25
26 deltax_916 = deltax(:,zoom_end_916);
27 tau_916 = tau_f(deltax_916);
28 BV_916 = bipower_var(deltax_916);
29 alpha = 5;
30 cutoff = alpha*deltan^0.49*sqrt(tau_916*BV_916);
31 rc_916 = deltax_916;
32 rc_916(abs(deltax_916)>cutoff)=0;
33
34 TV_916 = sum((rc_916).^2);
35
36 % C
37 QIV_915 = 1/(3*deltan)*sum((rc_915).^4);
38 CI_IV_915 = [TV_915-1.96*sqrt(2*deltan*QIV_915),TV_915+1.96*sqrt(2*deltan*
    QIV_915)];
39
40 pd = makedist('Normal','mu',0,'sigma',1);
```

```

41 p_2 = cdf(pd,-0.02/sqrt(TV_915));
42 p_4 = cdf(pd,-0.04/sqrt(TV_915));
43
44 p2_lower = cdf(pd,-0.02/sqrt(CI_IV_915(1,1)));
45 p2_upper = cdf(pd,-0.02/sqrt(CI_IV_915(1,2)));
46 P2_CI = [p2_lower,p2_upper];
47 P2_width = p2_upper - p2_lower;
48
49 p4_lower = cdf(pd,-0.04/sqrt(CI_IV_915(1,1)));
50 p4_upper = cdf(pd,-0.04/sqrt(CI_IV_915(1,2)));
51 P4_CI = [p4_lower,p4_upper];
52 P4_width = p4_upper - p4_lower;
53
54 % D
55 Q_1 = icdf(pd,0.01);
56 Q_5 = icdf(pd,0.05);
57
58 VaR_1 = Q_1*sqrt(TV_915)*200000000;
59 VaR_1_upper = icdf(pd,0.01)*sqrt(CI_IV_915(1,1))*200000000;
60 VaR_1_lower = icdf(pd,0.01)*sqrt(CI_IV_915(1,2))*200000000;
61 VaR_1_CI = [VaR_1_lower,VaR_1_upper];
62
63 VaR_5 = Q_5*sqrt(TV_915)*200000000;
64 VaR_5_upper = icdf(pd,0.05)*sqrt(CI_IV_915(1,1))*200000000;
65 VaR_5_lower = icdf(pd,0.05)*sqrt(CI_IV_915(1,2))*200000000;
66 VaR_5_CI = [VaR_5_lower,VaR_5_upper];

```

Listing 2: q\_2.m

```

1 % A
2 [dates_1, prices_1] = load_stock('DIS.csv');
3 [dates_2, prices_2] = load_stock('PG.csv');
4
5 [dates_return_1,deltax_1] = log_returns(dates_1, prices_1);
6 [dates_return_2,deltax_2] = log_returns(dates_2, prices_2);
7 [n,T] = size(deltax_1);
8 deltan = 1/n;

```

```
9
10 r_long_short = deltax_1-deltax_2;
11
12 tau_r_long_short = tau_f(r_long_short);
13 BV_r_long_short = bipower_var(r_long_short);
14 alpha = 5;
15 cutoff = alpha*deltan^0.49*sqrt(tau_r_long_short*BV_r_long_short);
16 rc_long_short = r_long_short;
17 rc_long_short(abs(r_long_short)>cutoff)=0;
18
19 average_rc_long_short = mean(rc_long_short(:));
20 min_rc_long_short = min(rc_long_short(:));
21 p5_rc_long_short = quantile(rc_long_short(:),0.05);
22 p95_rc_long_short = quantile(rc_long_short(:),0.95);
23 max_rc_long_short = max(rc_long_short(:));
24
25 % B
26 [dates_m, prices_m] = load_stock('SPY.csv');
27 [dates_return_m,deltax_m] = log_returns(dates_m, prices_m);
28 tau_m = tau_f(deltax_m);
29 BV_m = bipower_var(deltax_m);
30 alpha = 5;
31 cutoff = alpha*deltan^0.49*sqrt(tau_m*BV_m);
32 rc_m = deltax_m;
33 rc_m(abs(deltax_m)>cutoff)=0;
34
35 realized_beta = sum((rc_m.*rc_long_short))./sum(rc_m.^2);
36
37 average_realized_beta = mean(realized_beta(:));
38 min_realized_beta = min(realized_beta(:));
39 p5_realized_beta = quantile(realized_beta(:),0.05);
40 p95_realized_beta = quantile(realized_beta(:),0.95);
41 max_realized_beta= max(realized_beta(:));
42
43 % C
44 kn = 11;
```

```
45 M = 7;
46
47 J = 1000;
48 booRB = boost_realized_beta(J,T,n,kn,M,rc_m,rc_long_short);
49
50 RB_CI = ci_f(0.05,mean(booRB),std(booRB));
51
52 f = figure(1);
53 set(f,'units','normalized','outerposition',[0 0 1 1]);
54 plot(dates_m(1,:),RB_CI(1,:))
55 hold on
56 plot(dates_m(1,:),RB_CI(2,:))
57 plot(dates_m(1,:),realized_beta)
58 hold off
59 datetick('x','yyyy');
60 legend('RB_CI_lower','RB_CI_higher','realized_beta');
61 title('confidence interval of realized beta of long-short returns');
62 box off; grid on;
63 xlabel('time');
64 ylabel('CI');
65 print(f,'-dpng','-r200','figures/2C1');
66 close(f);
67
68 % D
69 zoom_start = find(dates_return_1==datenum(2008,10,1,16,0,0))/n;
70 zoom_end = find(dates_return_1==datenum(2008,10,31,16,0,0))/n;
71 realized_beta_zoom = realized_beta(zoom_start:zoom_end);
72 RB_CI_zoom = RB_CI(:,zoom_start:zoom_end);
73 dates_zoom = dates_return_1(1,zoom_start:zoom_end);
74
75
76 f = figure(2);
77 set(f,'units','normalized','outerposition',[0 0 1 1]);
78 plot(dates_zoom(1,:),RB_CI_zoom(1,:))
79 hold on
80 plot(dates_zoom(1,:),RB_CI_zoom(2,:))
```

```

81 plot(dates_zoom(1,:),realized_beta_zoom)
82 hold off
83 legend('lower bound','higer bound','realized beta')
84 % xticks(1:23)
85 % xticklabels
    ({'1','2','3','7','8','9','10','11','14','15','16','17','18','21','22','23','24','25'})
86 datetick('x','mdd');
87 title('confidence interval of realized beta of long-short returns in one
    month');
88 box off; grid on;
89 xlabel('time');
90 ylabel('CI');
91 print(f,'-dpng','-r200','figures/2D1');
92 close(f);
93
94 % E
95 contain_0 = zeros(1,T);
96 for i = 1:T
97     contain_0(i) = RB_CI(1,i)<0 && RB_CI(2,i)>0;
98 end
99
100 sum_contain_0 = sum(contain_0);
101 not_contaion_0 = T - sum_contain_0;
102 p_not_contaion_0 = not_contaion_0/T;

```

Listing 3: q3.m

```

1 % A
2 [dates_1, prices_1] = load_stock('DIS.csv');
3 [dates_2, prices_2] = load_stock('PG.csv');
4 [dates_m, prices_m] = load_stock('SPY.csv');
5
6 [dates_return_1,deltax_1] = log_returns(dates_1, prices_1);
7 [dates_return_2,deltax_2] = log_returns(dates_2, prices_2);
8 [dates_return_m,deltax_m] = log_returns(dates_m, prices_m);
9

```

```
10 [n,T] = size(deltax_1);
11 deltan = 1/n;
12
13 tau_1 = tau_f(deltax_1);
14 tau_2 = tau_f(deltax_2);
15 tau_m = tau_f(deltax_m);
16
17 BV_1 = bipower_var(deltax_1);
18 BV_2 = bipower_var(deltax_2);
19 BV_m = bipower_var(deltax_m);
20
21 alpha = 5;
22 cutoff_1 = alpha*deltan^0.49*sqrt(tau_1*BV_1);
23 cutoff_2 = alpha*deltan^0.49*sqrt(tau_2*BV_2);
24 cutoff_m = alpha*deltan^0.49*sqrt(tau_m*BV_m);
25
26 rc_1 = deltax_1;
27 rc_1(abs(deltax_1)>cutoff_1)=0;
28
29 rc_2 = deltax_2;
30 rc_2(abs(deltax_2)>cutoff_2)=0;
31
32 rc_m = deltax_m;
33 rc_m(abs(deltax_m)>cutoff_2)=0;
34
35 average_1 = mean(rc_1(:));
36 min_1 = min(rc_1(:));
37 p5_1 = quantile(rc_1(:),0.05);
38 p95_1 = quantile(rc_1(:),0.95);
39 max_1 = max(rc_1(:));
40
41 average_2 = mean(rc_2(:));
42 min_2 = min(rc_2(:));
43 p5_2 = quantile(rc_2(:),0.05);
44 p95_2 = quantile(rc_2(:),0.95);
45 max_2 = max(rc_2(:));
```

```
46
47 average_m = mean(rc_m(:));
48 min_m = min(rc_m(:));
49 p5_m = quantile(rc_m(:),0.05);
50 p95_m = quantile(rc_m(:),0.95);
51 max_m = max(rc_m(:));
52
53 % B
54 rd_m = deltax_m;
55 rd_m(abs(deltax_m)<=cutoff_m)=0;
56
57 jumps = sum(rd_m~=0);
58 y = zeros(12,1);
59 [yyyy,mm,dd]= ymd_f('SPY.csv');
60 for i = 1:11
61     y(i+1) = sum(ismember(yyyy,2006+i));
62 end
63 jumps_y = zeros(11,1);
64 for i = 1:11
65     jumps_y(i) = sum(jumps(1,(sum(y(1:i))+1):sum(y(1:i+1))));
66 end
67 sum_jumps_y = sum(jumps_y);
68
69 % C
70 realized_beta_1 = sum((rc_m.*rc_1))./sum(rc_m.^2);
71 realized_beta_2 = sum((rc_m.*rc_2))./sum(rc_m.^2);
72
73 average_rb_1 = mean(realized_beta_1(:));
74 min_rb_1 = min(realized_beta_1(:));
75 p5_rb_1 = quantile(realized_beta_1(:),0.05);
76 p95_rb_1 = quantile(realized_beta_1(:),0.95);
77 max_rb_1 = max(realized_beta_1(:));
78
79 average_rb_2 = mean(realized_beta_2(:));
80 min_rb_2 = min(realized_beta_2(:));
81 p5_rb_2 = quantile(realized_beta_2(:),0.05);
```



```
82 p95_rb_2 = quantile(realized_beta_2(:),0.95);
83 max_rb_2 = max(realized_beta_2(:));
84
85 % D
86 f = figure(3);
87 set(f,'units','normalized','outerposition',[0 0 1 1]);
88 plot(dates_1,realized_beta_1)
89 datetick('x','yyyy');
90 legend('realized_beta');
91 title('realized betas of DIS with SPY');
92 box off; grid on;
93 xlabel('time');
94 ylabel('realized betas');
95 print(f,'-dpng','-r200','figures/3D1');
96 close(f);
97
98 f = figure(4);
99 set(f,'units','normalized','outerposition',[0 0 1 1]);
100 plot(dates_2,realized_beta_2)
101 datetick('x','yyyy');
102 legend('realized_beta');
103 title('realized betas of PG with SPY');
104 box off; grid on;
105 xlabel('time');
106 ylabel('realized betas');
107 print(f,'-dpng','-r200','figures/3D2');
108 close(f);
109
110 % E
111 e_1 = rc_1 - realized_beta_1.*rc_m;
112
113 e_2 = rc_2 - realized_beta_2.*rc_m;
114
115 rho = zeros(1,T);
116 for i = 1:T
117 rho(i) = corr(e_1(:,i),e_2(:,i));
```

```
118 end
119
120 average_rho = mean(rho(:));
121 min_rho = min(rho(:));
122 p5_rho = quantile(rho(:),0.05);
123 p95_rho = quantile(rho(:),0.95);
124 max_rho = max(rho(:));
125
126 % F
127 kn = 11;
128 M = 7;
129
130 J = 1000;
131
132 new_rho = boost_correlation(J,T,n,kn,M,rc_1,rc_2,rc_m);
133
134 CI_new_rho = ci_f(0.05,mean(new_rho),std(new_rho));
135
136 f = figure(5);
137 set(f,'units','normalized','outerposition',[0 0 1 1]);
138 plot(dates_m(1,:),CI_new_rho(1,:))
139 hold on
140 plot(dates_m(1,:),CI_new_rho(2,:))
141 plot(dates_m(1,:),rho)
142 hold off
143 datetick('x','yyyy');
144 legend('CI_lower','CI_upper','correlation');
145 title('confidence interval of correlations');
146 box off; grid on;
147 xlabel('time');
148 ylabel('CI');
149 print(f,'-dpng','-r200','figures/3F');
150 close(f);
151
152 % G
153 zoom_start = find(dates_return_1==datenum(2008,10,1,16,0,0))/n;
```

```
154 zoom_end = find(dates_return_1==datenum(2008,10,31,16,0,0))/n;
155 rho_zoom = rho(zoom_start:zoom_end);
156 CI_new_rho_zoom = CI_new_rho(:,zoom_start:zoom_end);
157 dates_m_zoom = dates_m(1,zoom_start:zoom_end);
158
159 f = figure(6);
160 set(f,'units','normalized','outerposition',[0 0 1 1]);
161 plot(dates_m_zoom(1,:),CI_new_rho_zoom(1,:))
162 hold on
163 plot(dates_m_zoom(1,:),CI_new_rho_zoom(2,:))
164 plot(dates_m_zoom(1,:),rho_zoom)
165 hold off
166 datetick('x','mmdd');
167 legend('Rho_CI_lower','Rho_CI_higher','rho');
168 title('confidence interval of correlations in one month');
169 box off; grid on;
170 xlabel('time');
171 ylabel('CI');
172 print(f,'-dpng','-r200','figures/3G');
173 close(f);
174
175 % H
176 p_1 = (length(find(CI_new_rho(1,:)>0)))/252;
177 p_2 = (length(find(CI_new_rho(2,:)<0)))/252;
178 p_0 = (T-p_1-p_2)/252;
```