

# project\_8 report

November 9, 2019

## 1 Empirical Method in Financial Econometrics: Project 8

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### 1.2 Exercise 1

#### 1.2.1 A

```
[86]: prices = [142.19,142.27,142.29,142.62,142.70,142.64,142.61,142.62,142.63,142.  
    ↳67,142.62,142.50,142.45,142.57,142.54,142.32,142.17,142.03,141.85,141.30,141.  
    ↳36,141.01,140.78,140.96,141.16,141.38]
```

```
[87]: len_prices = len(prices)
```

```
[88]: print(len_prices)
```

26

```
[89]: freq_prices = (5*78/len_prices)
```

```
[90]: print(freq_prices)
```

15.0

The sampling frequency of the prices above is every 15-minutes 1 observation.

#### 1.2.2 B

```
[200]: import math  
log_returns = []  
for i in range(1,len(prices)):  
    log_returns.append(math.log(prices[i]) - math.log(prices[i-1]))
```

#### 1.2.3 C

```
[92]: import statistics as stat  
average_return = stat.mean(log_returns)  
print(average_return)
```

-0.00022851562661898583

```
[93]: standard_deviation = stat.stdev(log_returns)
      print(standard_deviation)
```

0.0013378543298329293

The average return is about -0.0002285; and the standard deviation of the returns is 0.0013379.

#### 1.2.4 D

```
[94]: def realized_variance(log_returns):
      rv = 0
      for r in log_returns:
          rv += r**2
      return rv
```

```
[95]: RV = realized_variance(log_returns)
      annulized_RV = 100*math.sqrt(252*RV)
      print(RV)
      print(annulized_RV)
```

4.426198577869189e-05

10.561259591653997

The annulized value is 10.56125959%.

#### 1.2.5 E

```
[96]: print(0.1 + 0.2 == 0.3)
```

False

```
[97]: print(sum([0.1,0.2]) == 0.3)
```

False

```
[98]: print(0.1 + 0.2)
```

0.30000000000000004

```
[99]: print(sum([0.1,0.2]))
```

0.30000000000000004

Because as we can see, the original equations are wrong, like  $0.1+0.2$  is not exactly equal to 3. This situation can be find in other programming tools like C, C++, Java and so on The reason is that binary can't accurately describe decimal fractions, so there is an error in the operation of float. I think this issue could not affect the computation of the realized variance, because the space for float is enough.

### 1.2.6 F

sum function: Return the sum of a 'start' value (default: 0) plus an iterable of numbers. When the iterable is empty, return the start value. This function is intended specifically for use with numeric values and may reject non-numeric types.

fsum function: Return an accurate floating point sum of values in the iterable seq. Assumes IEEE-754 floating point arithmetic.

```
[100]: r = []
for i in range(0, len(log_returns)):
    r.append(log_returns[i]**2)
    RV = math.fsum(r)
annulized_RV = 100*math.sqrt(252*RV)
print(annulized_RV)
```

10.561259591653997

Compared to the two results, I think they are same.

### 1.2.7 G

```
[101]: b = []
for i in range(1, len(log_returns)):
    b.append(abs(log_returns[i])*abs(log_returns[i-1]))
    BV = math.fsum(b) * math.pi/2
annulized_BV = 100*math.sqrt(252*BV)
print(annulized_BV)
```

9.997816709510156

The annulized value is 9.9978167%.

## 1.3 Excercise 2 - DIS

### 1.3.1 A

```
[167]: import os
os.getcwd()
os.chdir("/Users/zhouxijie/python/project_8/data/")
```

```
[168]: import csv
with open("DIS.csv", "r") as data:
    content = data.read()
```

```
[169]: data_lines = content.split("\n")
```

```
[170]: dates, times, prices = [], [], []
for line in data_lines:
    if line:
```

```

date, time, price = line.split(',')
dates.append(int(date))
times.append(int(time))
prices.append(float(price))

```

### 1.3.2 B

```

[171]: N = dates.count(dates[0])
      T = len(dates)//dates.count(dates[0])
      print(N)
      print(T)

```

78  
2769

There are 78 observations available each day and 2769 days available in the sample.

### 1.3.3 C

```

[172]: new_list = [prices[i:i+N] for i in range(0, len(prices), N)]

```

### 1.3.4 D

```

[173]: log_prices = [math.log(price) for price in prices]
      log_list = [log_prices[i:i+N] for i in range(0, len(log_prices), N)]
      log_returns = []
      for i in range(len(log_list)):
          log_returns.append([log_list[i][j+1] - log_list[i][j] for j in
      ↪range(len(log_list[0])-1)])

```

### 1.3.5 E

```

[199]: RV_new = [realized_variance(rlist) for rlist in log_returns]

```

### 1.3.6 F

```

[175]: average_rv = stat.mean(RV_new)
      annulized_av_rv = 100*math.sqrt(252*average_rv)
      print(annulized_av_rv)

```

21.778821985923436

```

[176]: median_rv = stat.median(RV_new)
      annulized_md_rv = 100*math.sqrt(252*median_rv)
      print(annulized_md_rv)

```

15.019035530425818

The average of the realized variance is 21.78%; the median of the realized variance is 15.02%.

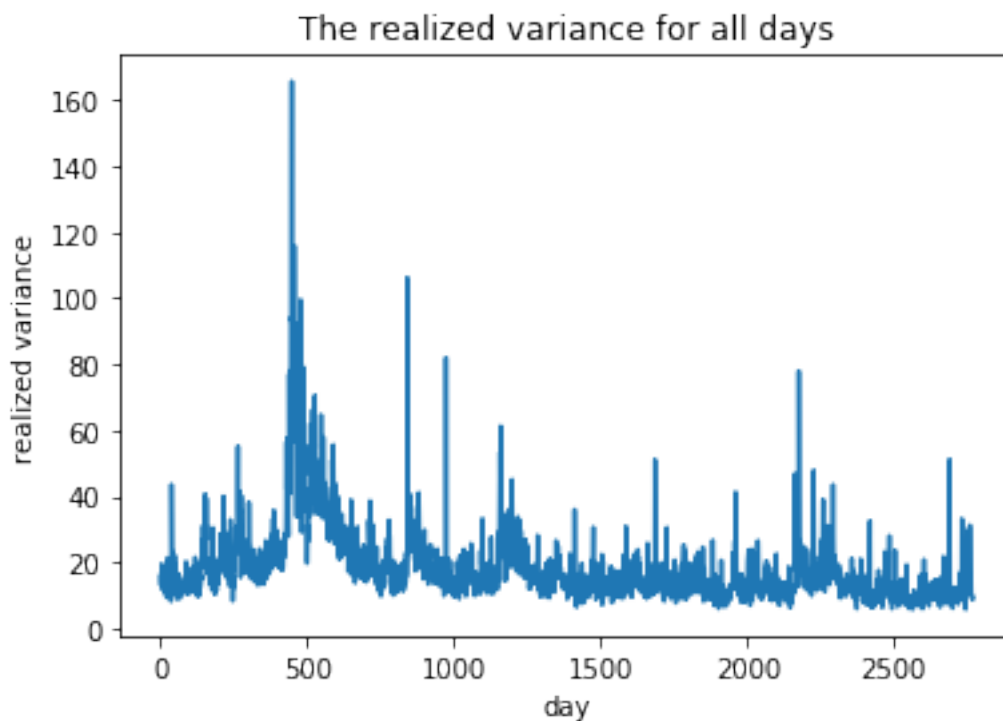
## 1.4 Exercise 3 - DIS

### 1.4.1 A

```
[177]: import matplotlib.pyplot as plt
```

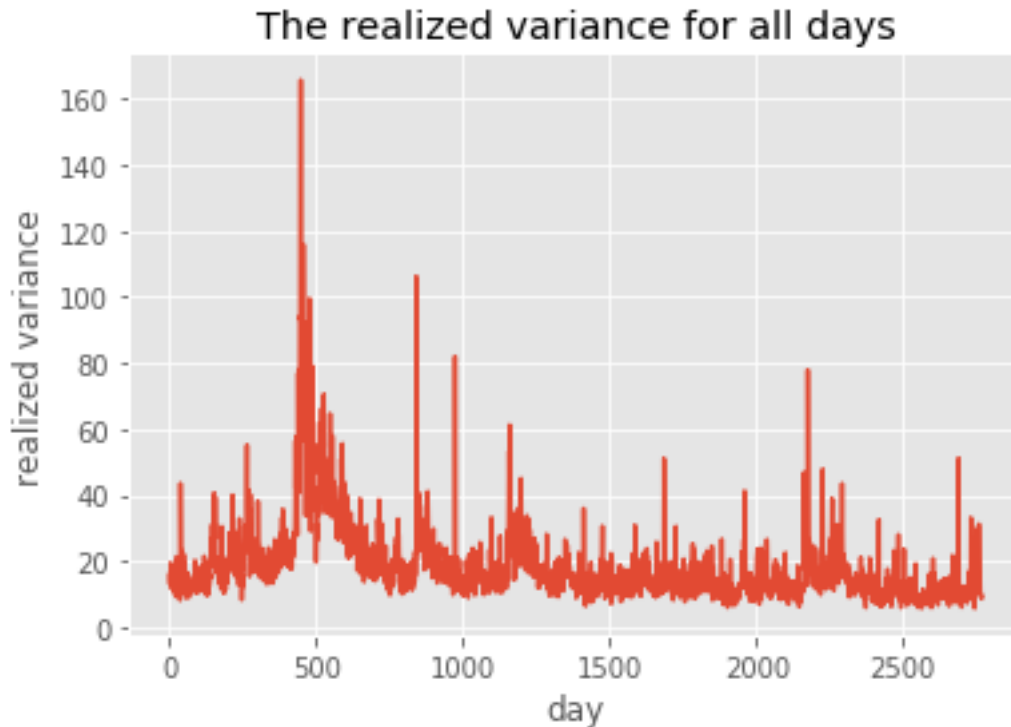
```
[178]: plt.plot([math.sqrt(rv*252)*100 for rv in RV_new])  
plt.xlabel('day')  
plt.ylabel('realized variance')  
plt.title('The realized variance for all days')
```

```
[178]: Text(0.5, 1.0, 'The realized variance for all days')
```



### 1.4.2 B

```
[179]: with plt.style.context("ggplot"):  
plt.plot([math.sqrt(rv*252)*100 for rv in RV_new])  
plt.xlabel('day')  
plt.ylabel('realized variance')  
plt.title('The realized variance for all days')
```



#### 1.4.3 C

```
[180]: from datetime import datetime
print(datetime(2017, 11, 20))
print(datetime.strptime('20171120 0927', '%Y%m%d %H%M'))
```

```
2017-11-20 00:00:00
2017-11-20 09:27:00
```

When using the method `strptime`, the format for `%H` is from 01 to 12, so we need to type '09' other than '9' for python to recognize this format. `%Y` means year, `%m` means month, `%d` means day, `%M` means minute.

#### 1.4.4 D

```
[181]: zipped = list(zip(dates, times))
dt = []
for time in zipped:
    if time[1]//1000 < 1:
        dt.append([str(time[0]) + " " + '0' + str(time[1])])
    else:
        dt.append([str(time[0]) + ' ' + str(time[1])])
print(dt[0])
```

```
['20070103 0935']
```

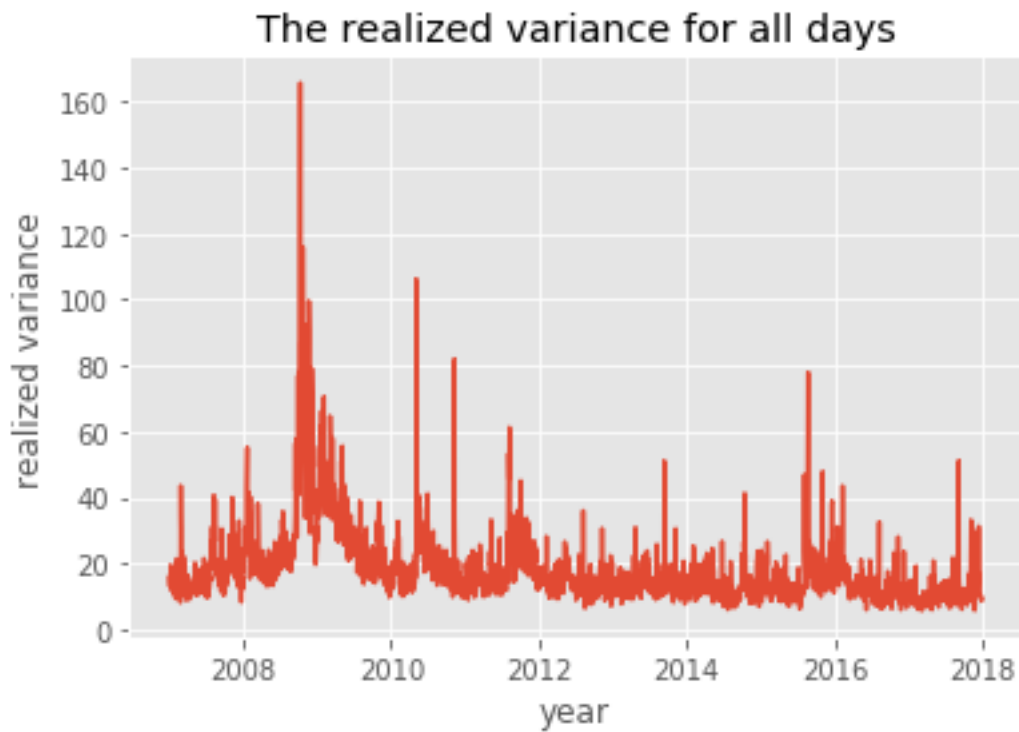
#### 1.4.5 E

```
[182]: format_dt = [datetime.strptime(str(dt[0]), '%Y%m%d %H%M') for dt in dt]
```

```
[183]: dts = []
for t in range(0, len(dt)):
    subdt = []
    for i in range(0, len(dt[t])):
        time = datetime.strptime(dt[t][i], '%Y%m%d %H%M')
        subdt.append(time)
    dts.append(subdt)
```

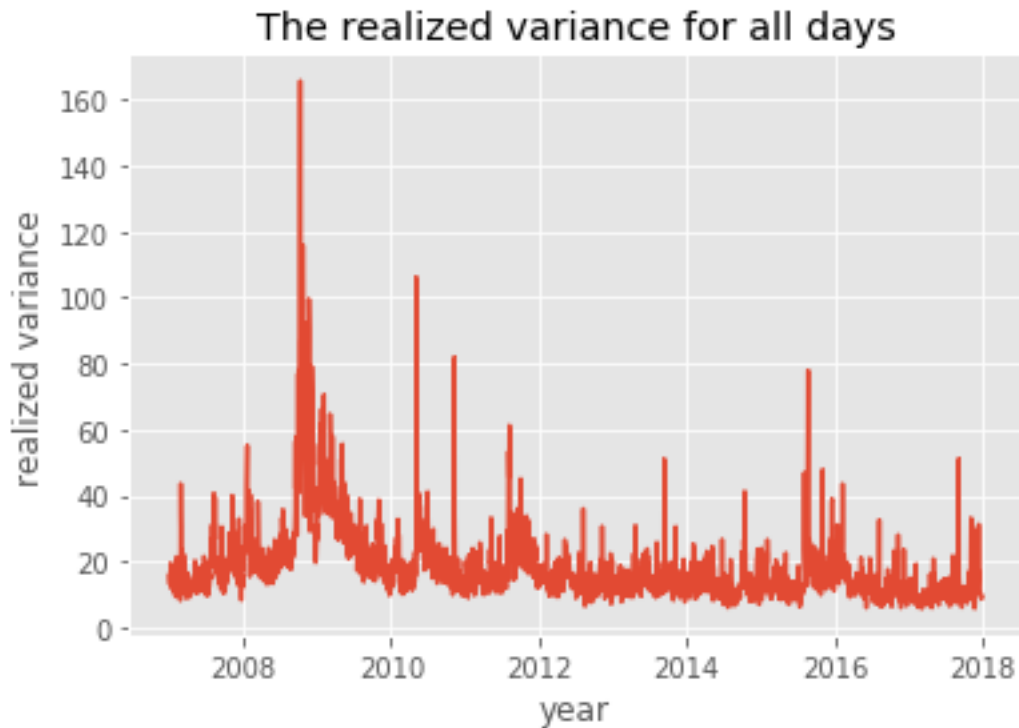
#### 1.4.6 F

```
[184]: with plt.style.context("ggplot"):
    dtx = [datetime.strptime(str(dates[i]), '%Y%m%d') for i in range(0,
    ↪len(dates), N)]
    plt.plot(dtx, [math.sqrt(rv*252)*100 for rv in RV_new])
    plt.xlabel('year')
    plt.ylabel('realized variance')
    plt.title('The realized variance for all days')
```



### 1.4.7 G

```
[185]: with plt.style.context("ggplot"):
        dtx = [datetime.strptime(str(dates[i]), '%Y%m%d') for i in range(0,
        ↪len(dates), N)]
        plt.plot(dtx, [math.sqrt(rv*252)*100 for rv in RV_new])
        plt.xlabel('year')
        plt.ylabel('realized variance')
        plt.title('The realized variance for all days')
```



## 1.5 Exercise 2 - PG

### 1.5.1 A

```
[186]: import os
        os.getcwd()
        os.chdir("/Users/zhouxijie/python/project_8/data/")
        import csv
        with open("PG.csv", "r") as data:
            content = data.read()
        data_lines = content.split("\n")
        dates, times, prices = [], [], []
        for line in data_lines:
            if line:
```



```

date, time, price = line.split(',')
dates.append(int(date))
times.append(int(time))
prices.append(float(price))

```

### 1.5.2 B

```

[187]: N = dates.count(dates[0])
      T = len(dates)//dates.count(dates[0])
      print(N)
      print(T)

```

78  
2769

There are 78 observations available each day and 2769 days available in the sample.

### 1.5.3 C

```

[188]: new_list = [prices[i:i+N] for i in range(0, len(prices), N)]

```

### 1.5.4 D

```

[189]: log_prices = [math.log(price) for price in prices]
      log_list = [log_prices[i:i+N] for i in range(0, len(log_prices), N)]
      log_returns = []
      for i in range(len(log_list)):
          log_returns.append([log_list[i][j+1] - log_list[i][j] for j in
      ↪range(len(log_list[0])-1)])

```

### 1.5.5 E

```

[190]: RV_new = [realized_variance(rlist) for rlist in log_returns]

```

### 1.5.6 F

```

[191]: average_rv = stat.mean(RV_new)
      annulized_av_rv = 100*math.sqrt(252*average_rv)
      print(annulized_av_rv)
      median_rv = stat.median(RV_new)
      annulized_md_rv = 100*math.sqrt(252*median_rv)
      print(annulized_md_rv)

```

15.624203800306113  
11.364598799912011

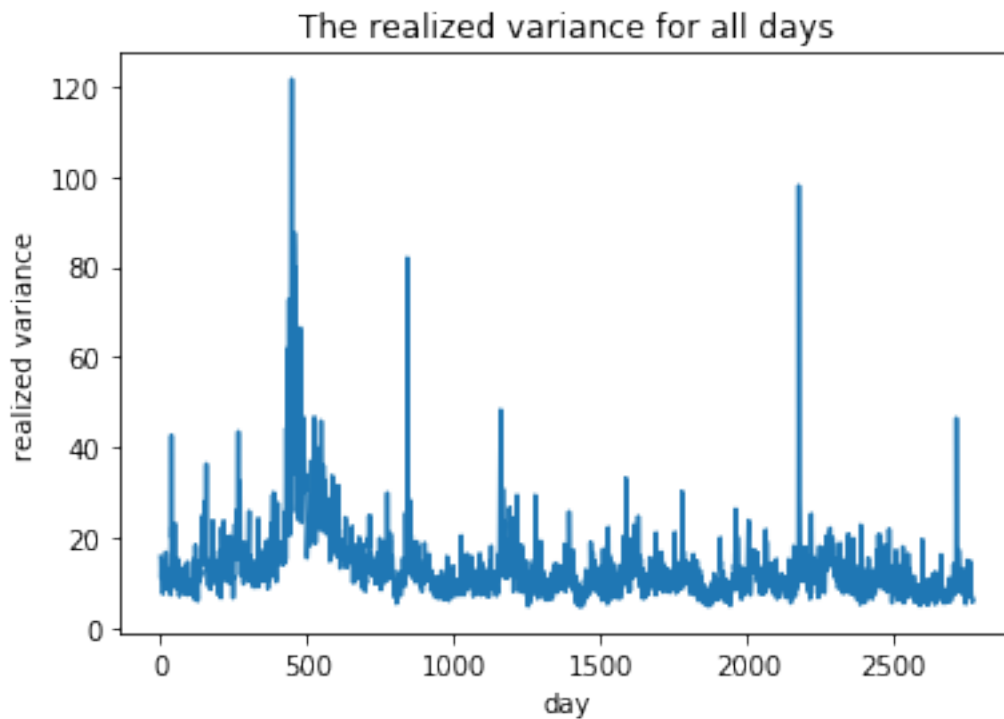
The average of the realized variance is 15.62%; the median of the realized variance is 11.36%.

## 1.6 Exercise 3 - PG

### 1.6.1 A

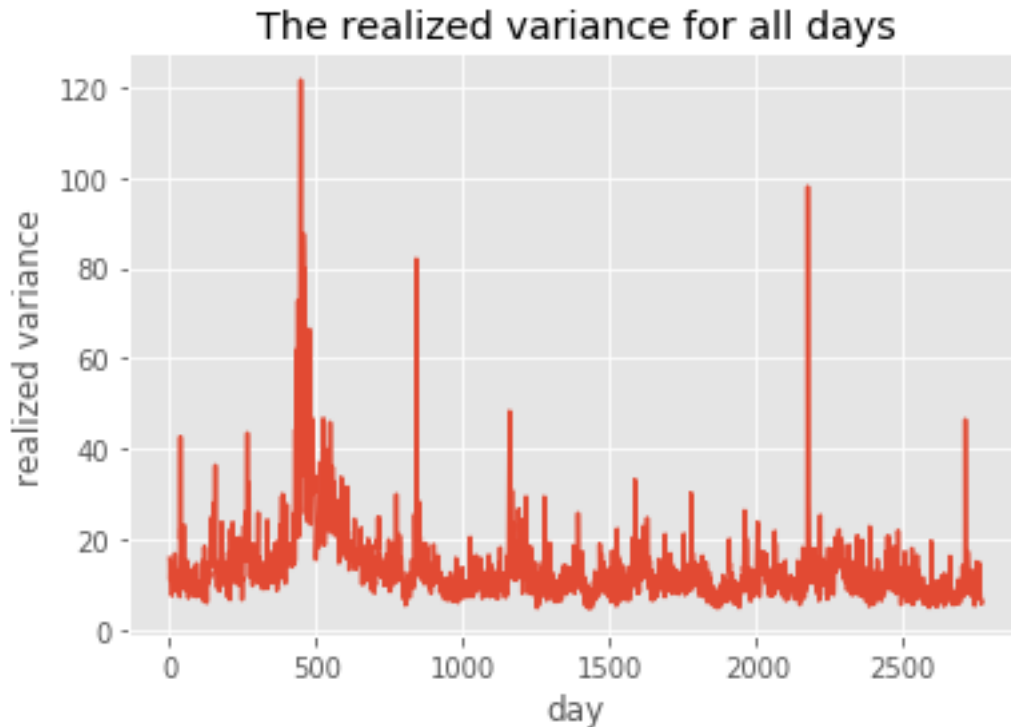
```
[192]: import matplotlib.pyplot as plt
plt.plot([math.sqrt(rv*252)*100 for rv in RV_new])
plt.xlabel('day')
plt.ylabel('realized variance')
plt.title('The realized variance for all days')
```

```
[192]: Text(0.5, 1.0, 'The realized variance for all days')
```



### 1.6.2 B

```
[193]: with plt.style.context("ggplot"):
plt.plot([math.sqrt(rv*252)*100 for rv in RV_new])
plt.xlabel('day')
plt.ylabel('realized variance')
plt.title('The realized variance for all days')
```



### 1.6.3 C

```
[194]: from datetime import datetime
print(datetime(2017, 11, 20))
print(datetime.strptime('20171120 0927', '%Y%m%d %H%M'))
```

2017-11-20 00:00:00

2017-11-20 09:27:00

When using the method `strptime`, the format for `%H` is from 01 to 12, so we need to type '09' other than '9' for python to recognize this format. `%Y` means year, `%m` means month, `%d` means day, `%M` means minute.

### 1.6.4 D

```
[195]: zipped = list(zip(dates, times))
dt = []
for time in zipped:
    if time[1]//1000 < 1:
        dt.append([str(time[0]) + " " + '0' + str(time[1])])
    else:
        dt.append([str(time[0]) + ' ' + str(time[1])])
print(dt[0])
```

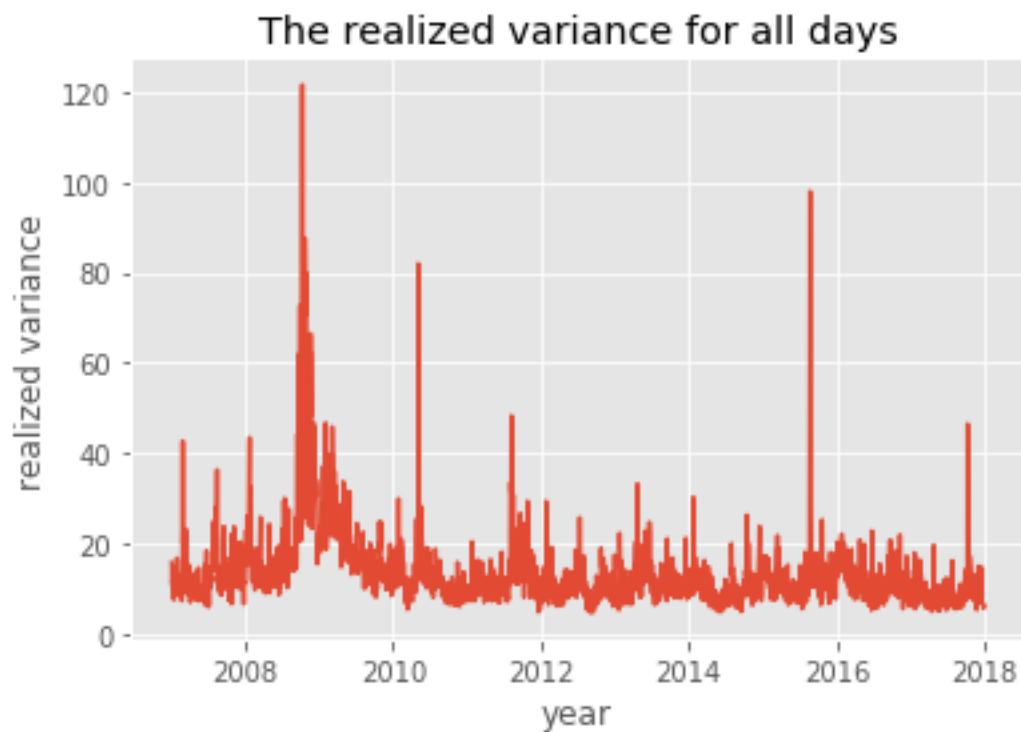
```
['20070103 0935']
```

### 1.6.5 E

```
[196]: format_dt = [datetime.strptime(str(dt[0]), '%Y%m%d %H%M') for dt in dt]
      dts = []
      for t in range(0, len(dt)):
          subdt = []
          for i in range(0, len(dt[t])):
              time = datetime.strptime(dt[t][i], '%Y%m%d %H%M')
              subdt.append(time)
          dts.append(subdt)
```

### 1.6.6 F

```
[197]: with plt.style.context("ggplot"):
      dtx = [datetime.strptime(str(dates[i]), '%Y%m%d') for i in range(0,
      →len(dates), N)]
      plt.plot(dtx, [math.sqrt(rv*252)*100 for rv in RV_new])
      plt.xlabel('year')
      plt.ylabel('realized variance')
      plt.title('The realized variance for all days')
```



### 1.6.7 G

```
[198]: with plt.style.context("ggplot"):  
        dtx = [datetime.strptime(str(dates[i]), '%Y%m%d') for i in range(0,   
→len(dates), N)]  
        plt.plot(dtx, [math.sqrt(rv*252)*100 for rv in RV_new])  
        plt.xlabel('year')  
        plt.ylabel('realized variance')  
        plt.title('The realized variance for all days')
```

