

data generating model:

$$Y = Cb + E\alpha + G\beta + W\eta + \varepsilon$$

C: clinical factor

$C = (C_1, \dots, C_{q_1})$, $b = (b_1, \dots, b_{q_1})^T$, $q_1=3$, b is generated from unif (1, 2.2)

E: environmental factor

$E = (E_1, \dots, E_{q_2})$, $\alpha = (\alpha_1, \dots, \alpha_{q_2})^T$, $q_2=4$, α is generated from unif (1.2, 2.5)

E have 2 continuous variables and 2 discrete variables.

G: genes

$G = (G_1, \dots, G_P)$, $\beta = (\beta_1, \dots, \beta_P)^T$, $P=100$, the nonzero $(\beta_1, \dots, \beta_8)$ is generated from unif(1, 2.5) and other β is 0.

#nonzero: 8

W: GxE interactions

$W = (G_1 \times E_1, \dots, G_1 \times E_{q_2}, \dots, G_P \times E_1, \dots, G_P \times E_{q_2}, \dots)$, $\eta = (\eta_1, \dots, \eta_{PXq_2})^T$

the nonzero $\eta_1, \eta_{10}, \eta_{19}, \eta_{32}, \eta_{57}, \eta_{70}, \eta_{96}, \eta_{97}, \eta_{138}, \eta_{144}, \eta_{157}, \eta_{170}$ are generated from unif(1.8, 2.5) and other η is 0.

#nonzero: 12

Estimate the coefficients of β and η with marginal model:

$$Y = Cb + E\alpha + X\beta + W'\eta' + \varepsilon$$

$X = G_j$, $W' = (X \times E_1, \dots, X \times E_{q_2})$, $\eta' = (\eta'_1, \dots, \eta'_{q_2})^T$

Simulation Results

n=300, p=200, error distribution: N(0,1)

Bayesian Lasso

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	8	192	12	788
sd	0	0	0	0

Bayesian Lasso Spike and Slab

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	8	3.67	6.37	13.6
sd	0	2.09	1.73	5.89

LAD Bayesian Lasso

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	8	192	12	788
sd	0	0	0	0

LAD Bayesian Lasso spike and slab

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	8	27.53	9.83	103.2
sd	0	7.27	1.48	19.1