

data generating model:

$$Y = Cb + E\alpha + G\beta + W\eta + \varepsilon$$

C: clinical factor

$C = (C_1, \dots, C_{q_1})$ ,  $b = (b_1, \dots, b_{q_1})^T$ ,  $q_1=3$ ,  $b$  is generated from unif (1, 2.2)

E: environmental factor

$E = (E_1, \dots, E_{q_2})$ ,  $\alpha = (\alpha_1, \dots, \alpha_{q_2})^T$ ,  $q_2=4$ ,  $\alpha$  is generated from unif (1.2, 2.5)

G: genes

$G = (G_1, \dots, G_P)$ ,  $\beta = (\beta_1, \dots, \beta_P)^T$ ,  $P=100$ , the nonzero  $(\beta_1, \dots, \beta_8)$  is generated from unif(1, 2.5) and other  $\beta$  is 0.

#nonzero: 8

W: GxE interactions

$W = (G_1 \times E_1, \dots, G_1 \times E_{q_2}, \dots, G_p \times E_1, \dots, G_p \times E_{q_2})$ ,  $\eta = (\eta_1, \dots, \eta_{PXq_2})^T$

the nonzero  $(\eta_1, \eta_2, \eta_3), \eta_8, (\eta_9, \eta_{10}), \eta_{16}, (\eta_{17}, \eta_{18}), \eta_{24}, (\eta_{25}, \eta_{26})$  are generated from unif(1.8, 2.5) and other  $\eta$  is 0.

#nonzero: 12

Estimate the coefficients of  $\beta$  and  $\eta$  with marginal model:

$$Y = Cb + E\alpha + X\beta + W'\eta' + \varepsilon$$

$X = G_j$ ,  $W' = (X \times E_1, \dots, X \times E_{q_2})$ ,  $\eta' = (\eta'_1, \dots, \eta'_{q_2})^T$

## Simulation Results

n=200, p=50, error distribution: N(0,1)

### Bayesian Lasso (95% confidence interval)

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	6.033333	0.15	6.55	2.15
sd	1.3138	0.3689	1.6067	1.29

### Bayesian Lasso Spike and Slab (MPM)

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	6.9	1	5.85	0.85
sd	0.8346	0.9882	2.0049	0.8088

### LAD Bayesian Lasso (95% confidence interval)

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	6.95	0.65	10.15	3.05
sd	0.8916	0.6271	1.3795	1.703

### LAD Bayesian Lasso spike and slab (MPM)

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	7.25	1.75	11.25	17.45
sd	0.731	1.672	1.0202	5.1775

## Simulation Results

n=200, p=50, error distribution: t(2)

### Bayesian Lasso (95% confidence interval)

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	5.05	0.15	6.45	2.3
sd	1.776	0.3689	1.395	1.66

### Bayesian Lasso Spike and Slab (MPM)

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	6.35	0.85	5.25	1.05
sd	1.336	0.956	1.738	0.949

### LAD Bayesian Lasso (95% confidence interval)

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	6.7	0.85	9.35	3.9
sd	1.146	0.8916	1.672	2.6

### LAD Bayesian Lasso spike and slab (MPM)

	TP(main)	FP(main)	TP(interaction)	FP(interaction)
mean	6.9	1.8	10.7	19.3
sd	0.97	1.638	0.998	6.17