

# Regression, EDA about medical cost

Roysen

12/11/2020

```
library(tidyverse)
library(forcats)
library(ggthemes)
library(broom.mixed)
library(corrplot)
library(modelr)
library(lme4)
library(patchwork)
library(broom)
```

## 读取数据

```
insurance <- read_csv("~/workspace/insurance.csv")
insurance
```

```
## # A tibble: 1,338 x 7
##   age sex    bmi children smoker region    charges
##   <dbl> <chr> <dbl>    <dbl> <chr>  <chr>    <dbl>
## 1    19 female  27.9         0 yes    southwest 16885.
## 2    18 male    33.8         1 no     southeast  1726.
## 3    28 male    33          3 no     southeast  4449.
## 4    33 male    22.7         0 no     northwest 21984.
## 5    32 male    28.9         0 no     northwest  3867.
## 6    31 female  25.7         0 no     southeast  3757.
## 7    46 female  33.4         1 no     southeast  8241.
## 8    37 female  27.7         3 no     northwest  7282.
## 9    37 male    29.8         2 no     northeast  6406.
## 10   60 female  25.8         0 no     northwest 28923.
## # ... with 1,328 more rows
```

序号	变量	注释
1	age	年龄
2	sex	性别
3	bmi	身体质量指数，成人标准值（18.5-23.9），算法： $\text{kg}/(\text{m}^2)$
4	children	小孩数量
5	smoker	是否吸烟
6	region	地区
7	charges	投保费用

数据集有1338行（观测值），7个变量，3个字符型向量，4个数字型向量。

该数据集主要是针对医疗费用支出收集的相关数据，自变量包括用户的年龄、性别、身体质量指数、小孩数量、是否吸烟、地区。属于回归分析的范畴。

### ##检查缺失值

```
insurance %>%
  summarise_all(
    ~ sum(is.na(.))
  )
```

```
## # A tibble: 1 x 7
##   age    sex    bmi children smoker region charges
##   <int> <int> <int>    <int>  <int>  <int>    <int>
## 1     0     0     0        0     0     0        0
```

各个变量均没有缺失值。#数据概览

```
summary(insurance)
```

```
##           age           sex           bmi           children
##  Min.   :18.00  Length:1338  Min.    :15.96  Min.     :0.000
##  1st Qu.:27.00  Class  :character  1st Qu.:26.30  1st Qu.:0.000
##  Median :39.00  Mode   :character  Median :30.40  Median :1.000
##  Mean    :39.21                Mean    :30.66  Mean    :1.095
##  3rd Qu.:51.00                3rd Qu.:34.69  3rd Qu.:2.000
##  Max.    :64.00                Max.    :53.13  Max.    :5.000
##           smoker           region           charges
##  Length:1338  Length:1338  Min.    : 1122
##  Class  :character  Class :character  1st Qu.: 4740
##  Mode   :character  Mode   :character  Median : 9382
##                                     Mean    :13270
##                                     3rd Qu.:16640
##                                     Max.    :63770
```

##将sex、smoker、region变量转换为因子，并保留在insu\_df数据框

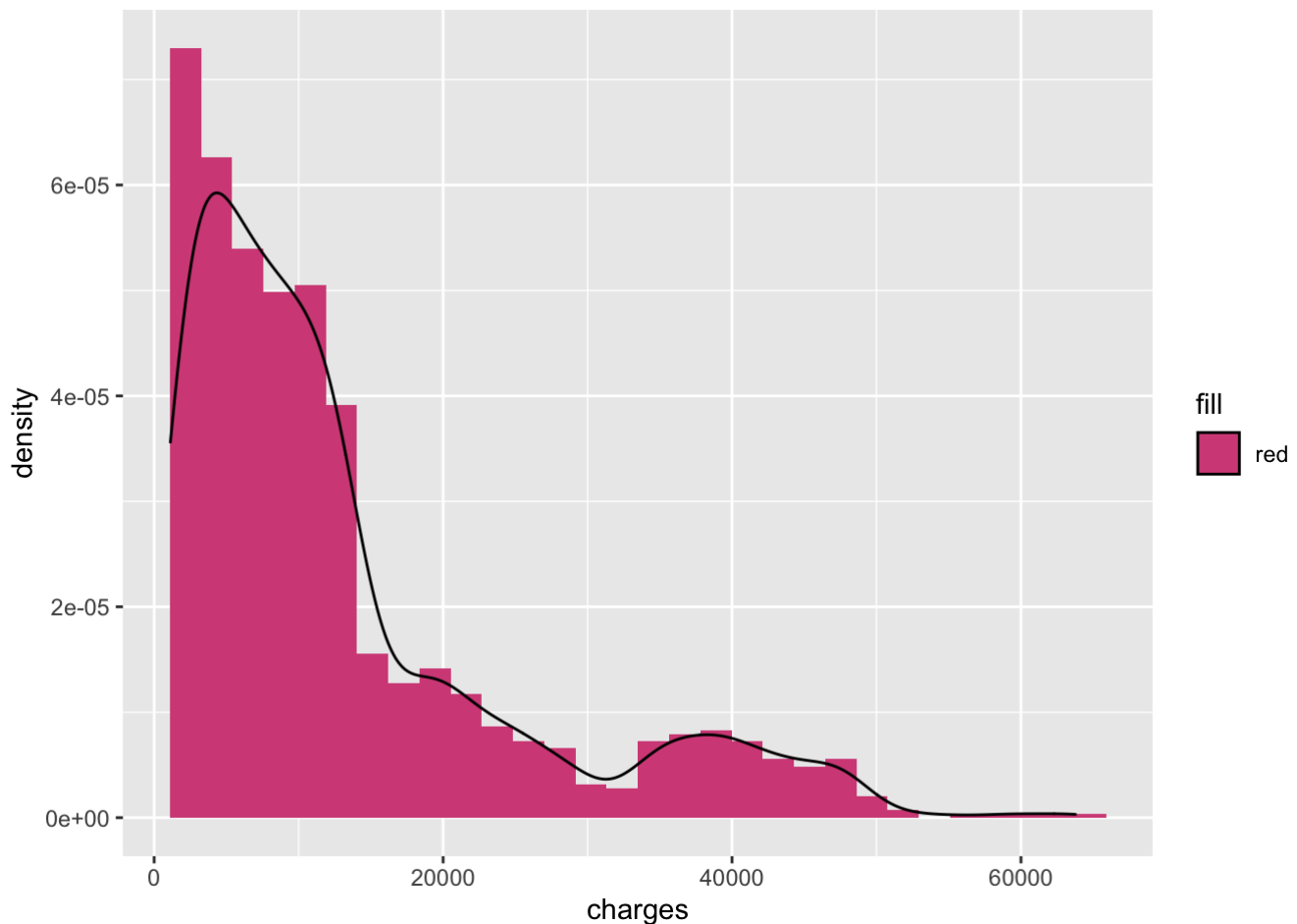
```
insu_df <- insurance %>%
  mutate(sex = factor(sex),
         smoker = factor(smoker),
         region = factor(region)
  )
insu_df
```

```
## # A tibble: 1,338 x 7
##   age sex    bmi children smoker region    charges
##   <dbl> <fct> <dbl>    <dbl> <fct>  <fct>    <dbl>
## 1    19 female  27.9        0 yes    southwest 16885.
## 2    18 male   33.8        1 no     southeast  1726.
## 3    28 male   33         3 no     southeast  4449.
## 4    33 male  22.7        0 no     northwest 21984.
## 5    32 male  28.9        0 no     northwest  3867.
## 6    31 female 25.7        0 no     southeast  3757.
## 7    46 female 33.4        1 no     southeast  8241.
## 8    37 female 27.7        3 no     northwest  7282.
## 9    37 male  29.8        2 no     northeast  6406.
## 10   60 female 25.8        0 no     northwest 28923.
## # ... with 1,328 more rows
```

#变量简单统计 #insurance变量分布图

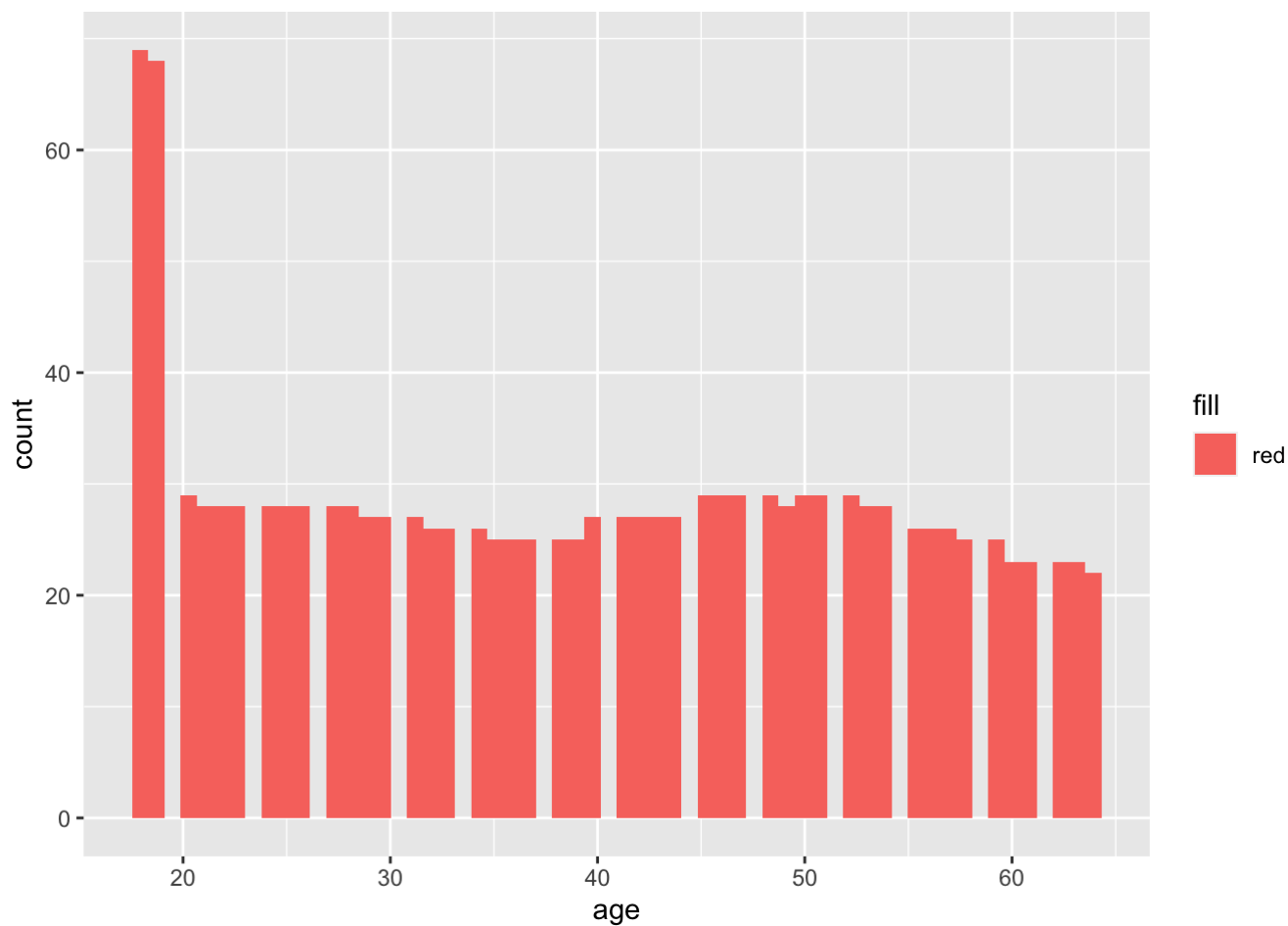
```
insurance %>%
  ggplot(aes(x = charges, y = stat(density)))+
    geom_histogram(aes(fill = "red"))+
    scale_fill_manual(values = c("#d45087"))+
    geom_density()
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

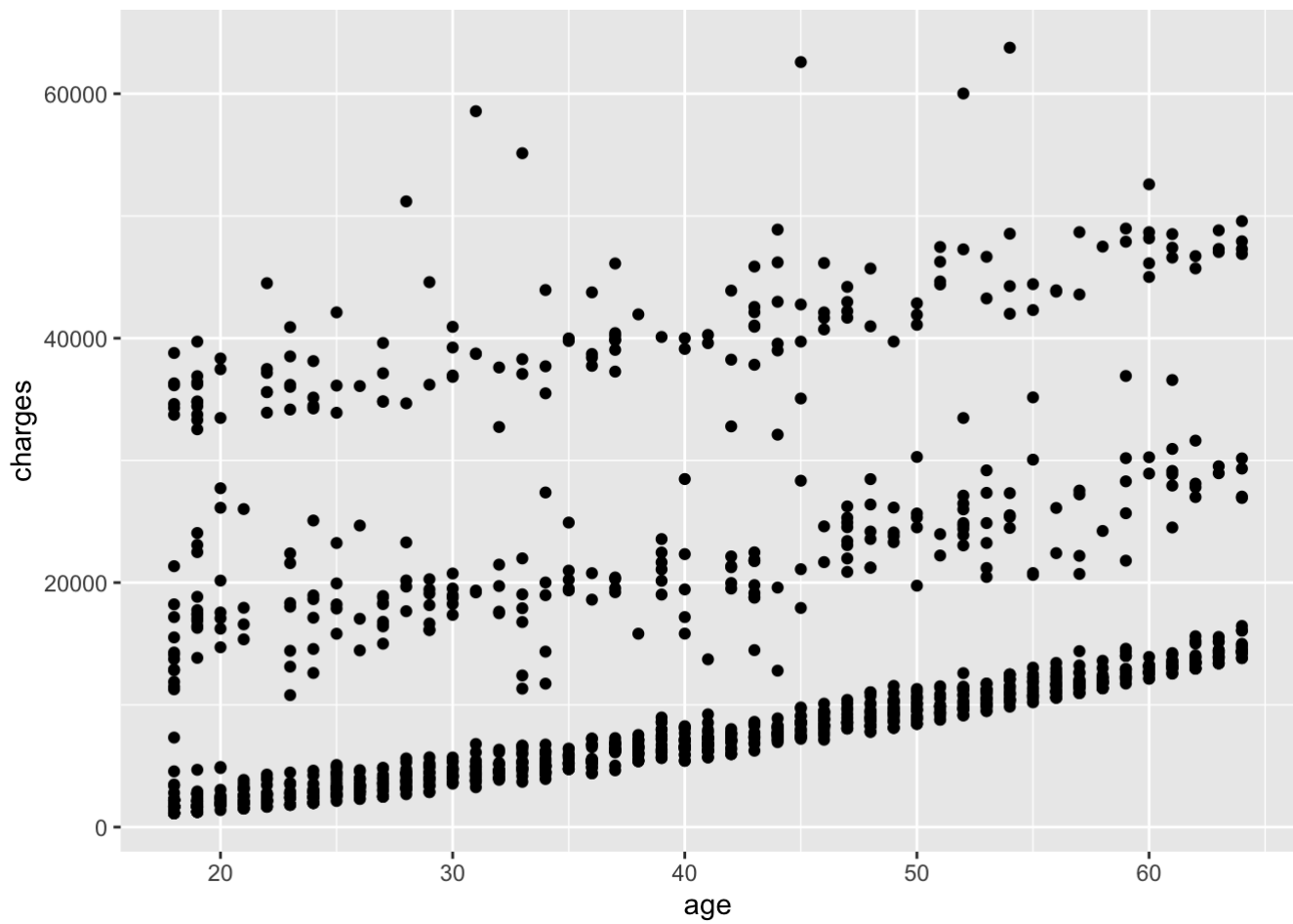


## ##年龄因素

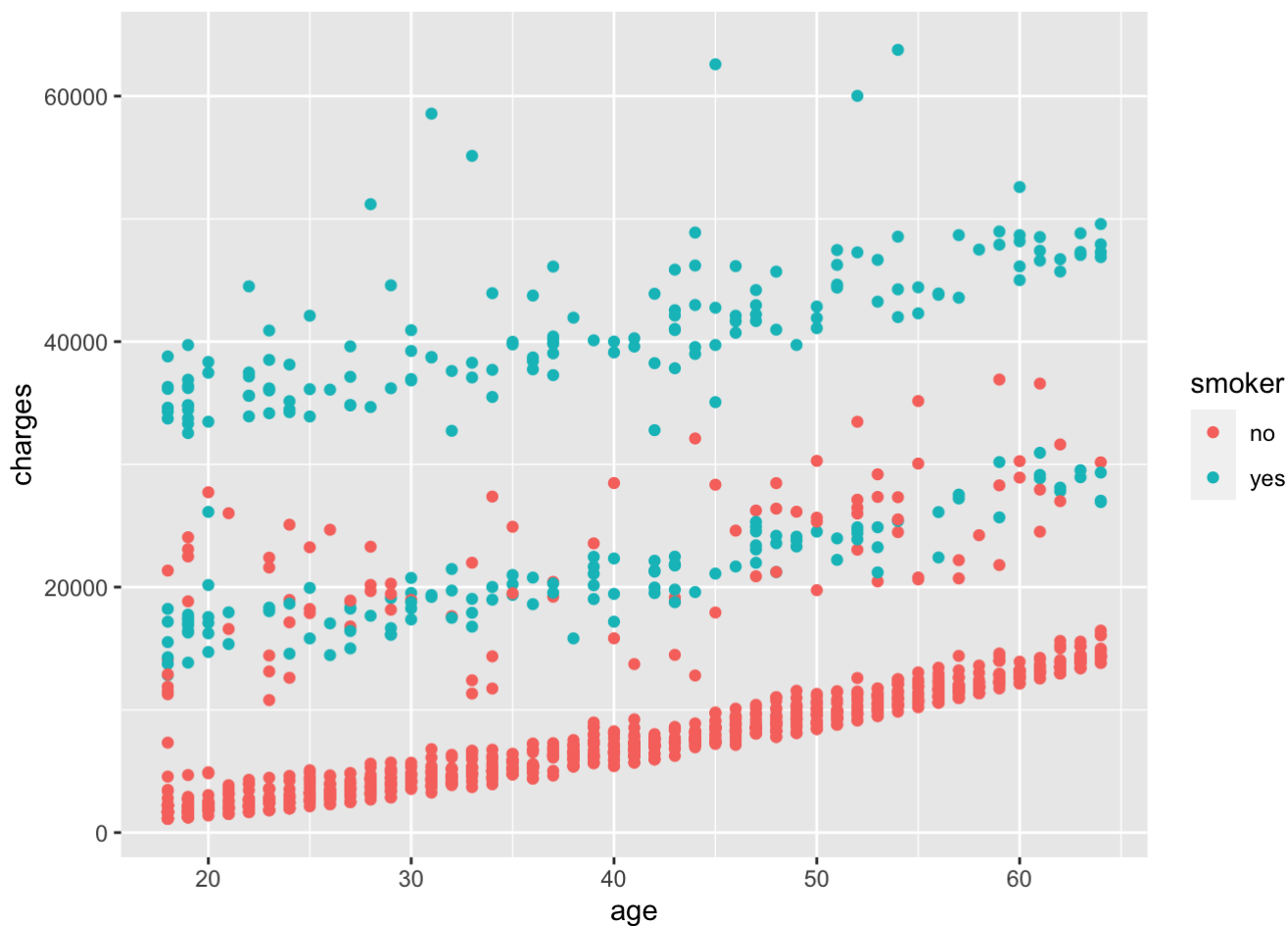
```
insu_df %>%  
  ggplot(aes(age, fill = "red"))+  
  geom_histogram(bins = 60)
```



```
insu_df %>%  
  ggplot(aes(age, charges))+  
  geom_point()
```



```
insu_df %>%  
  ggplot(aes(age, charges, color = smoker))+  
  geom_point()
```



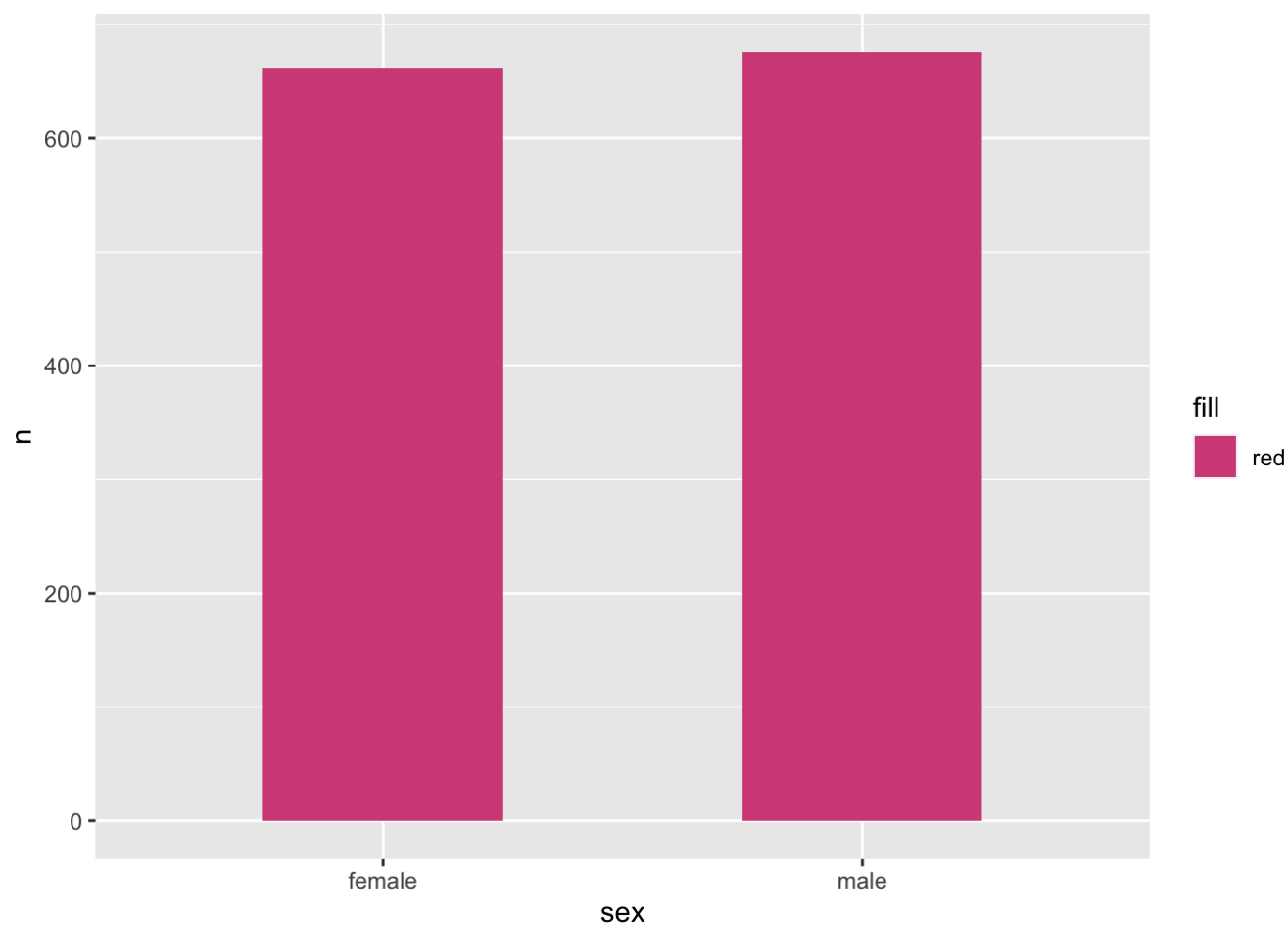
20岁以下的用户占比最高，年龄和保险支出费用呈线性关系，但是这种关系应该收到其他因素的影响，表现为三层线性关系。经分析年龄和保险支出费用中需加入smoker这个因素，可能包含着交互效应以及多层模型。图形表明：

医疗支出费用随着年龄增加而增加，

抽烟群体的保险支出费用比非抽烟人群的保险支出费用要高，都成线性增长趋势。

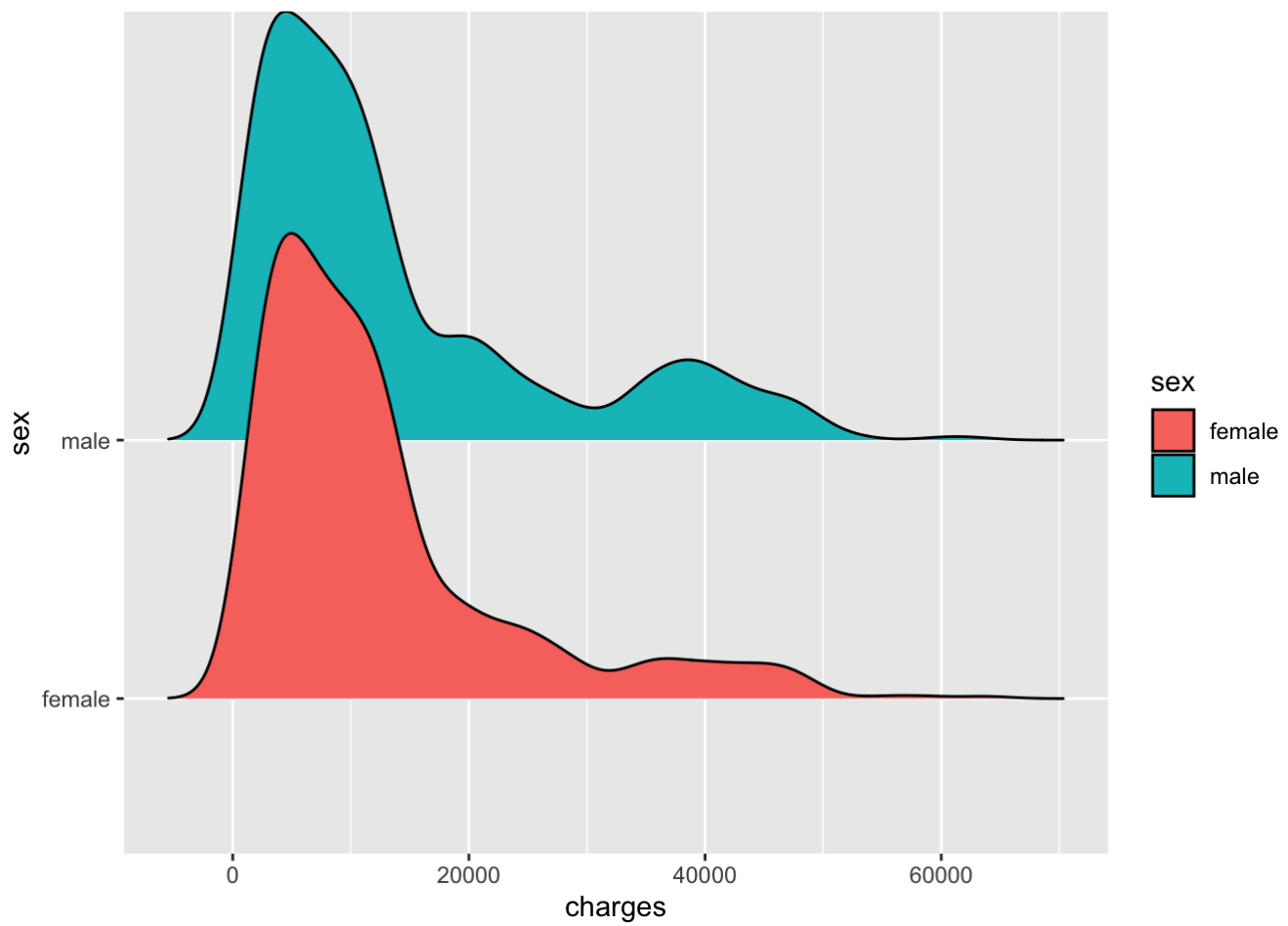
##性别因素

```
insu_df %>%
  count(sex) %>%
  ggplot(aes(sex, n))+
  geom_col( aes(fill = "red", width = 0.5))+
  scale_fill_manual(values = c("#d45087"))
```



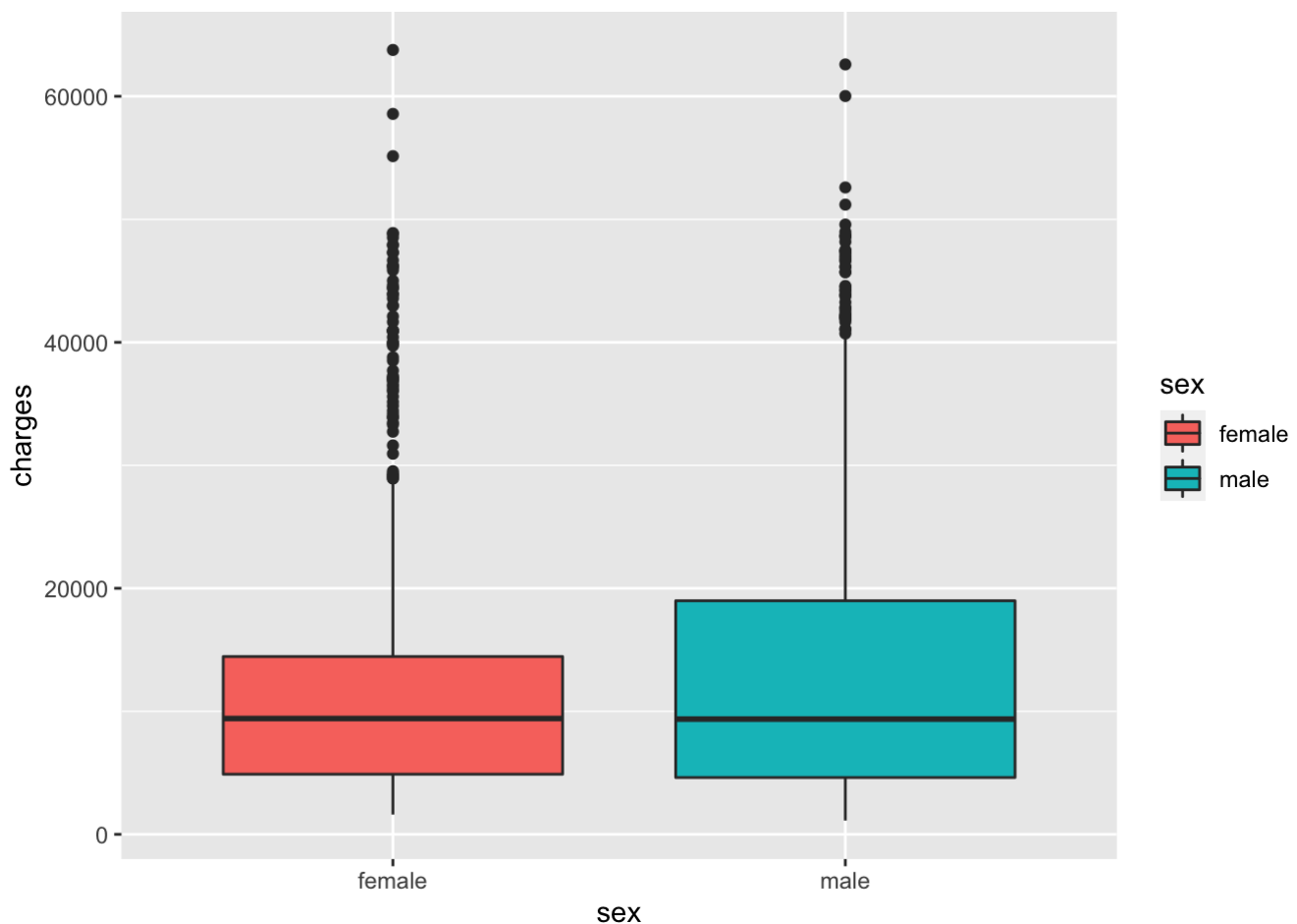
```
insu_df %>%  
ggplot(aes(charges, sex, fill = sex)) +  
  ggribes::geom_density_ridges()
```

```
## Picking joint bandwidth of 2190
```



```
insu_df %>%  
ggplot(aes(sex, charges, fill = sex))+  
  geom_boxplot()
```



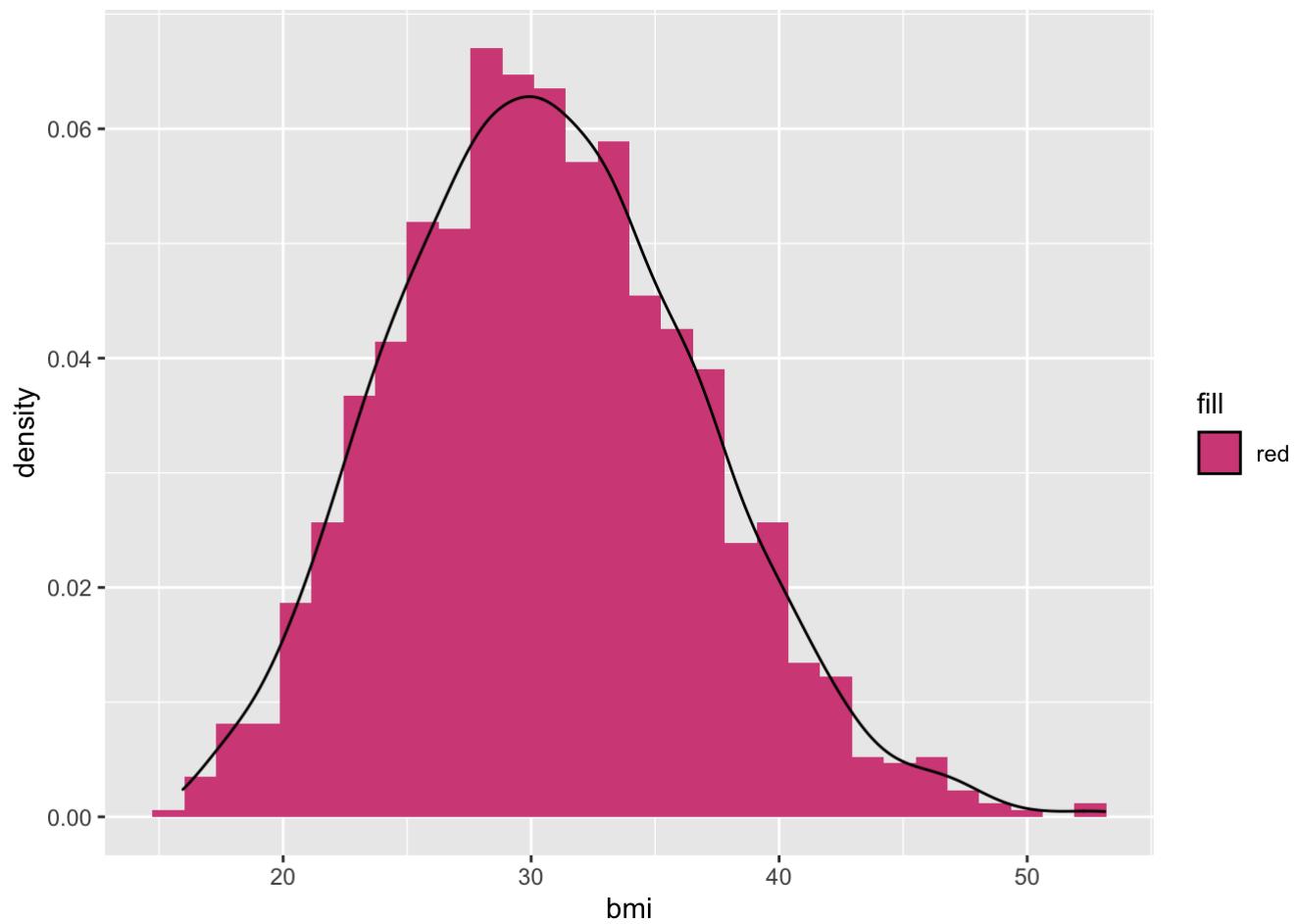


性别因素，女性医疗费用支出费用集中在（500-1500美元），男性集中在（500-2000美元）。女性保险支出费用在（15000-30000美元）和男性支出费用在（20000-40000美元），为正常的波动范围，男性的波动幅度更大些。女性30000美元以上和男性40000以上为各自组内的异常值，表明这一部分用户群相对是少数。在异常值的部分，女性用户的波动范围很大（30000-65000美元），可能是什么原因呢？也许需要进行问卷调研。共同点：医疗费用支出有着大致相同的曲线，分别都有两个高峰。原因同需探究。

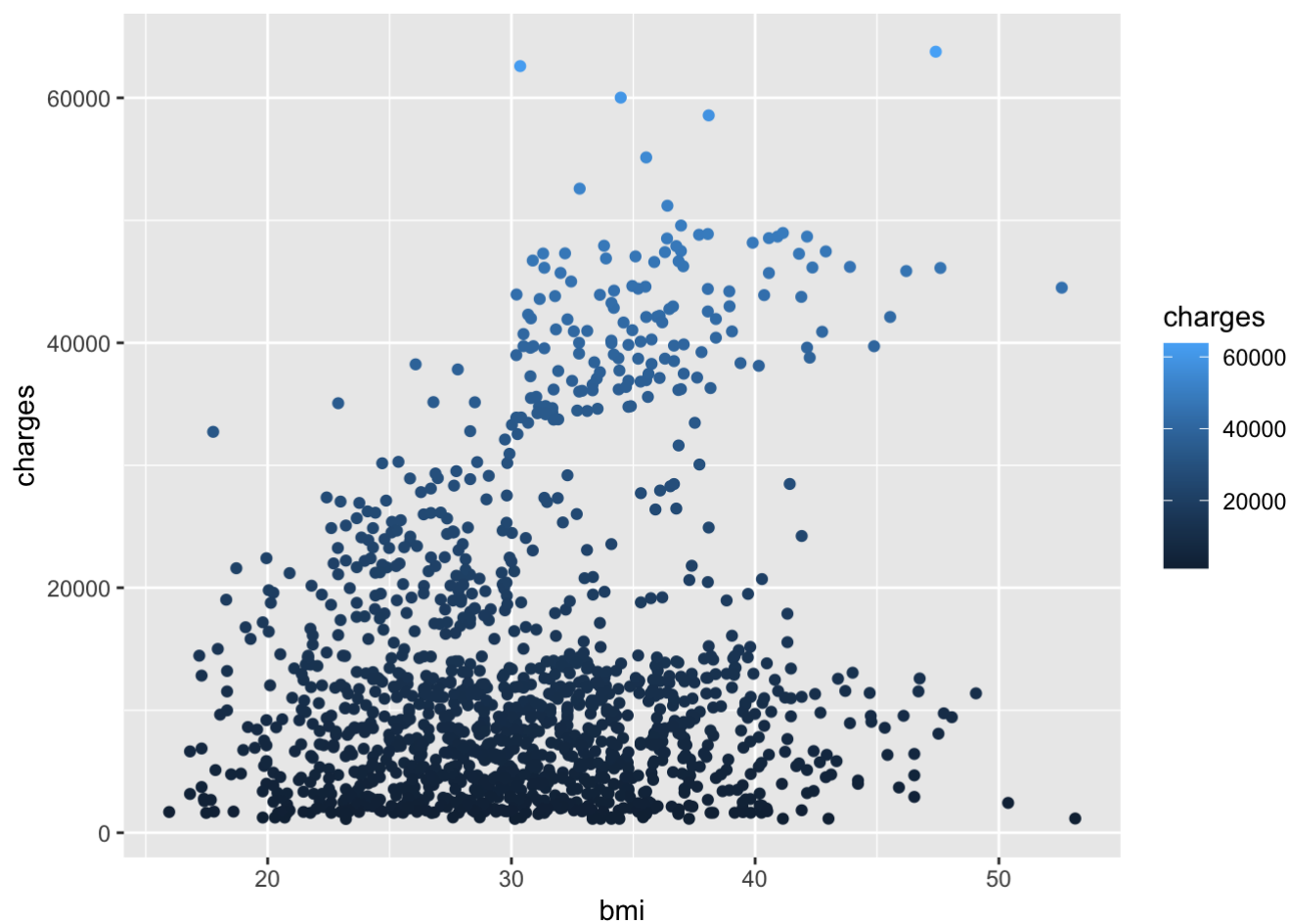
### ##bmi因素

```
insu_df %>%
  ggplot(aes(x = bmi, y = stat(density)))+
    geom_histogram( aes(fill = "red"))+
    scale_fill_manual(values = c("#d45087"))+
    geom_density()
```

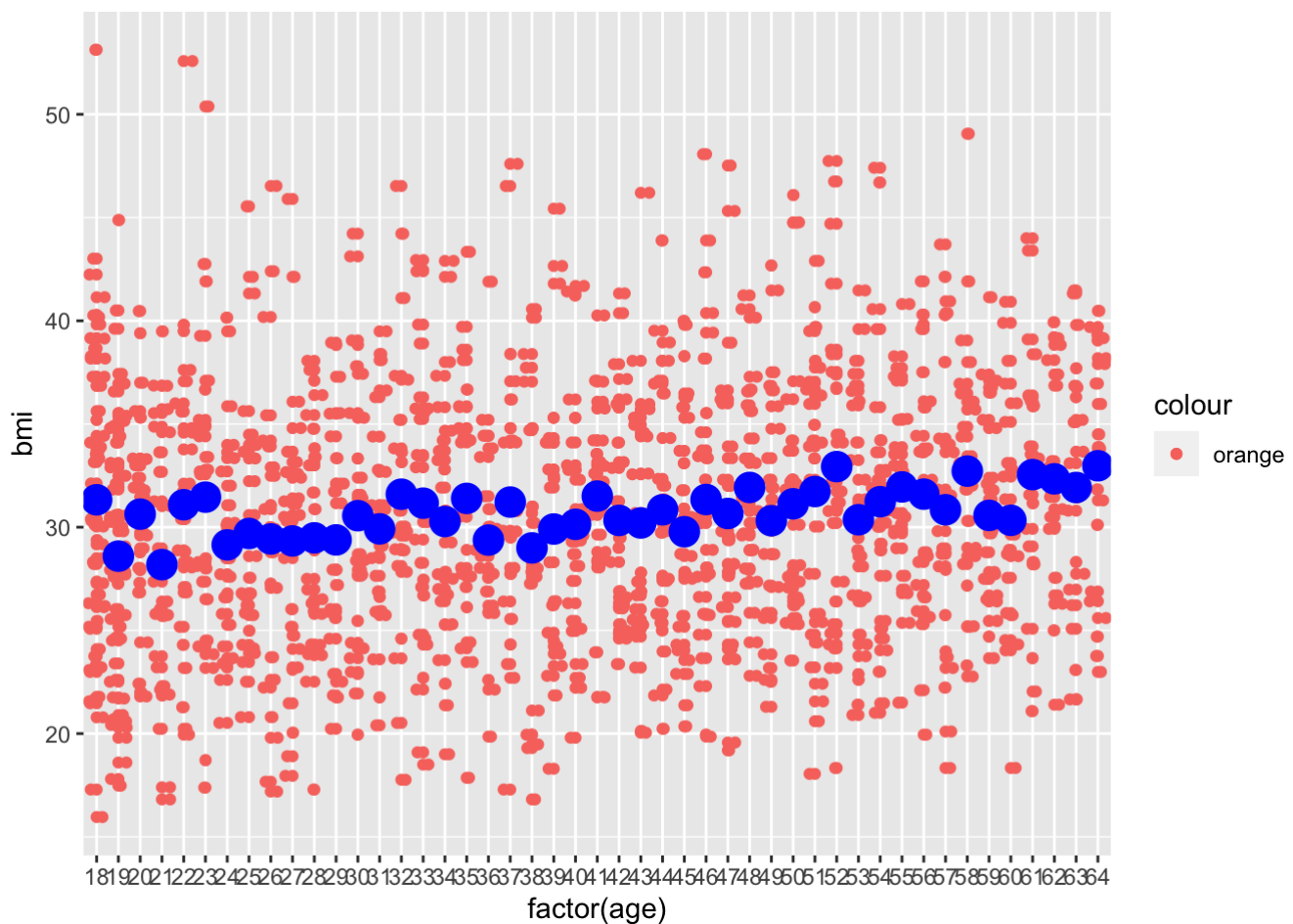
```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
insu_df %>%  
ggplot(aes(x = bmi, charges, color = charges))+  
  geom_point()
```



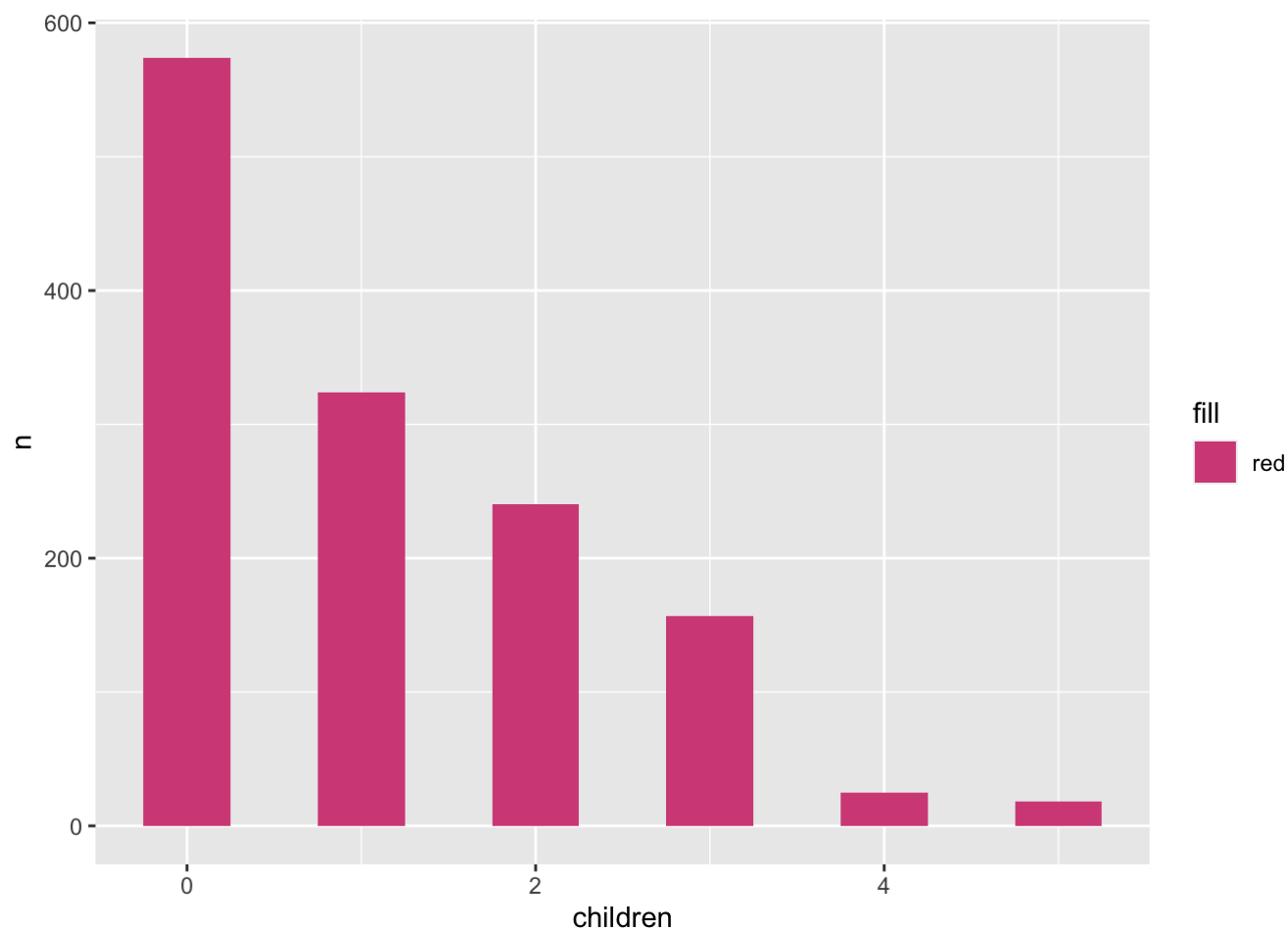
```
insu_df %>%  
ggplot(aes(factor(age), bmi, color = "orange"))+  
  geom_point()+  
  geom_jitter()+  
  stat_summary(fun.y = mean, colour = "blue", geom = "point", size = 5)
```



用户各个年龄段的平均bmi为30，bmi范围集中（25-35），在大致来说当bmi超过30，即身体明显处于肥胖状态时，保险支出费用有极大值，费用超过了30000美元。同时，各个年龄段肥胖人数的比例都接近50%，这是一个不好的现象。

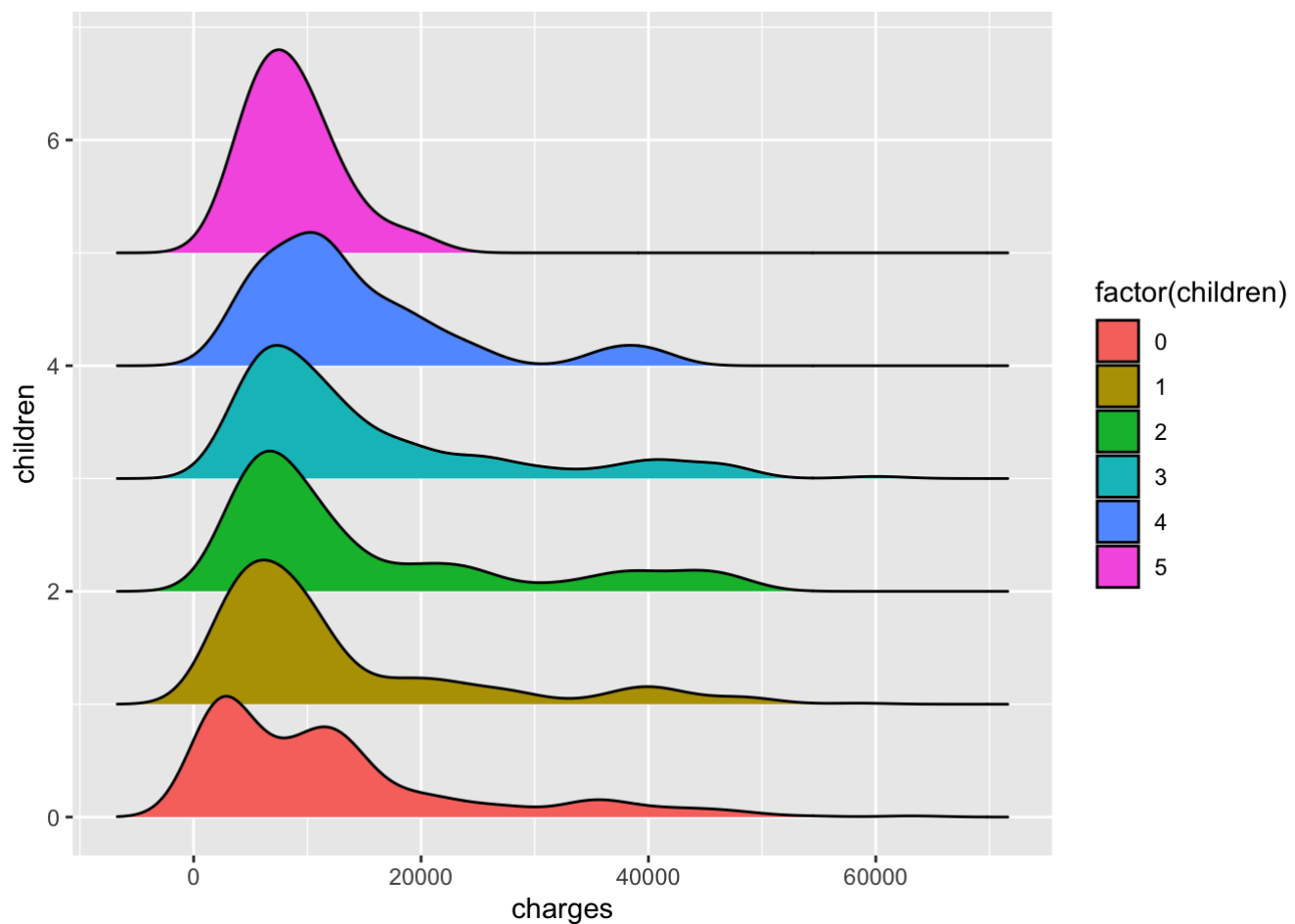
##儿童个数因素

```
insurance %>%
  count(children) %>%
  ggplot(aes(children, n))+
  geom_col( aes(fill = "red", width = 0.5))+
  scale_fill_manual(values = c("#d45087"))
```

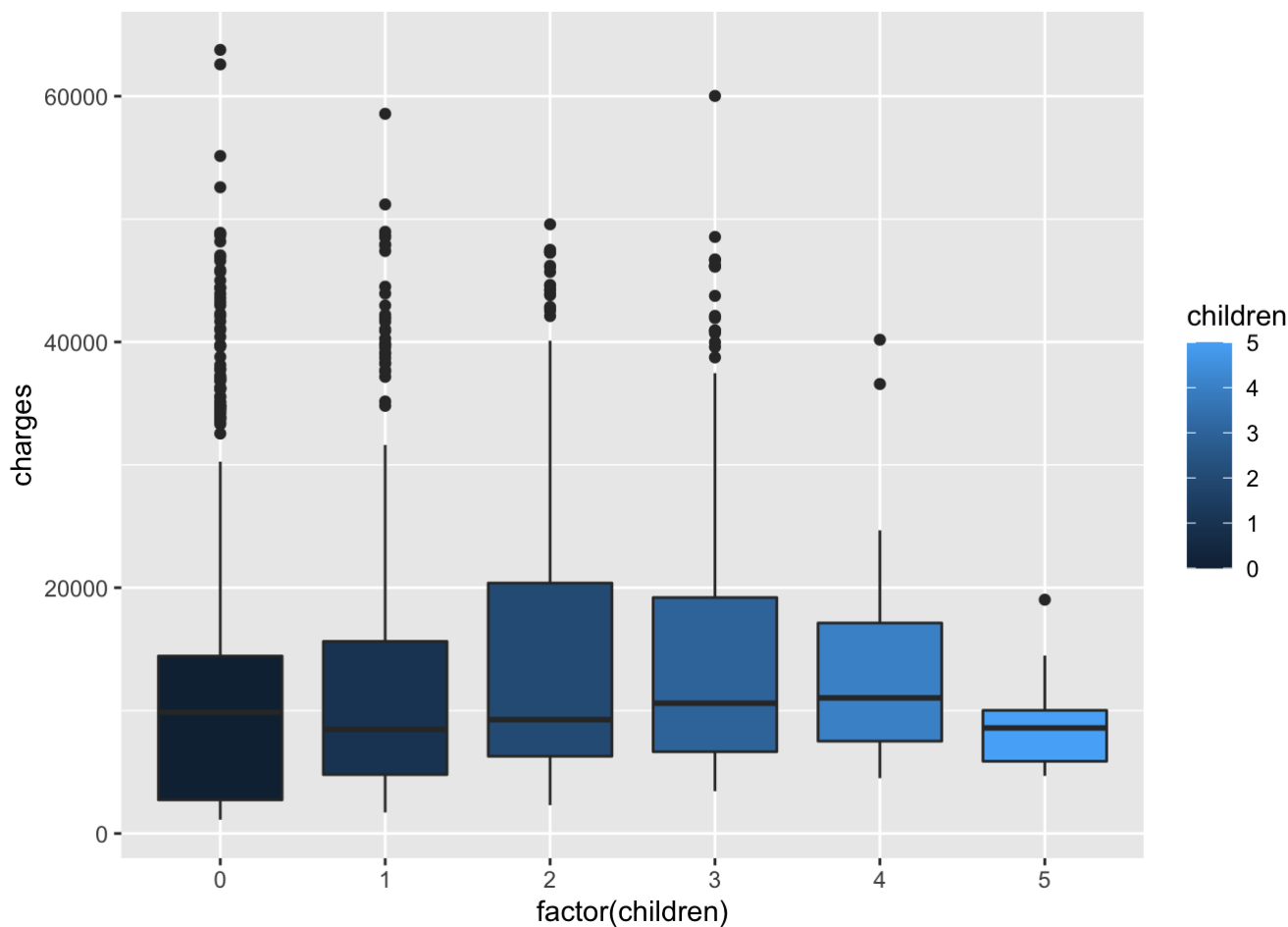


```
insurance %>%  
  ggplot(aes(charges, children))+  
  ggribes::geom_density_ridges(aes(fill = factor(children)))
```

```
## Picking joint bandwidth of 2610
```



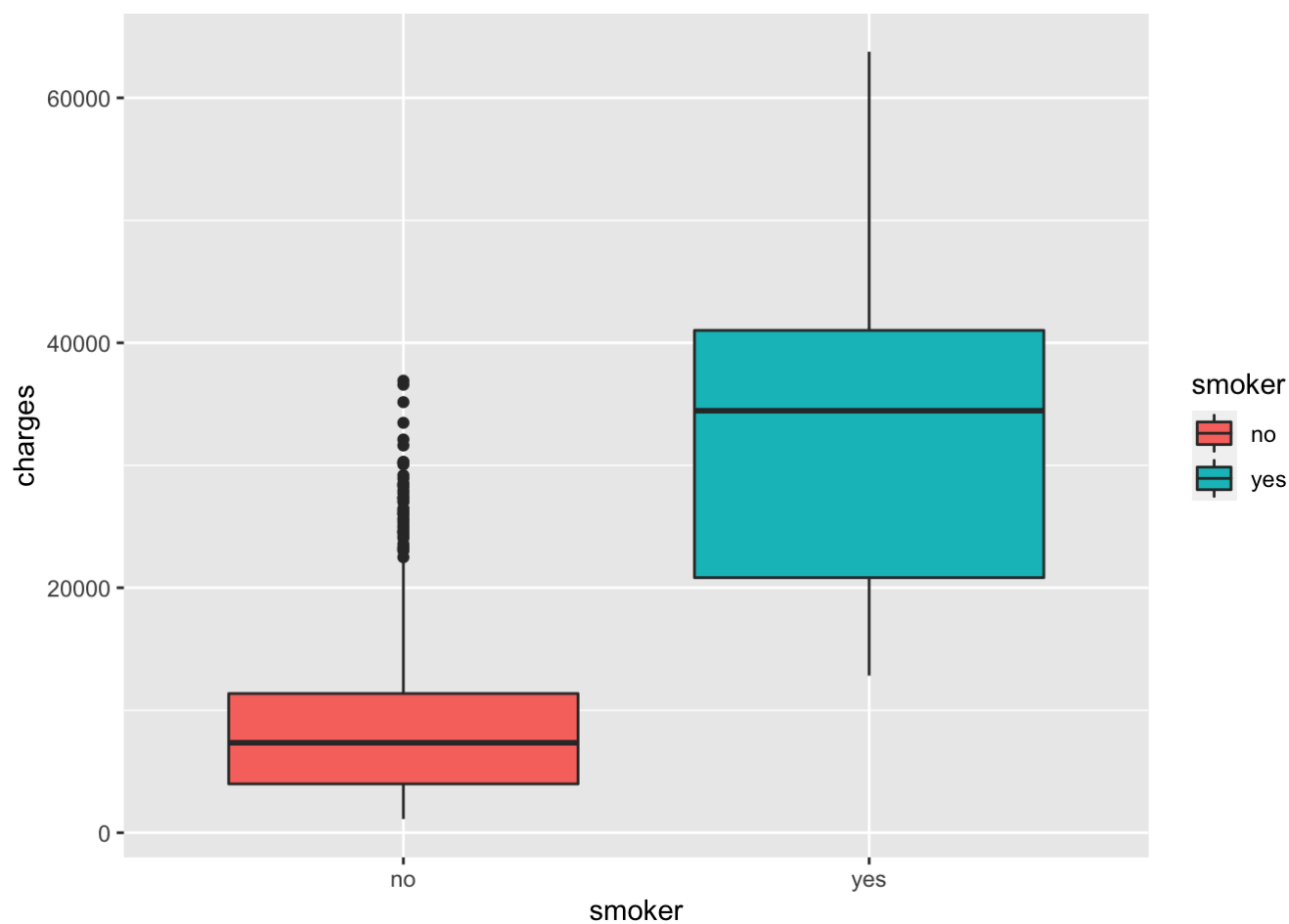
```
insurance %>%  
  ggplot(aes(factor(children), charges, fill = children))+  
  geom_boxplot()
```



儿童医保支出费用平均1000美元，同男女性别上并无差异，集中在20000美元以下，对于小于等于3个的儿童用户，支出费用极大值广泛存在。孩子多了各项支出也相应多了。

#smoker因素

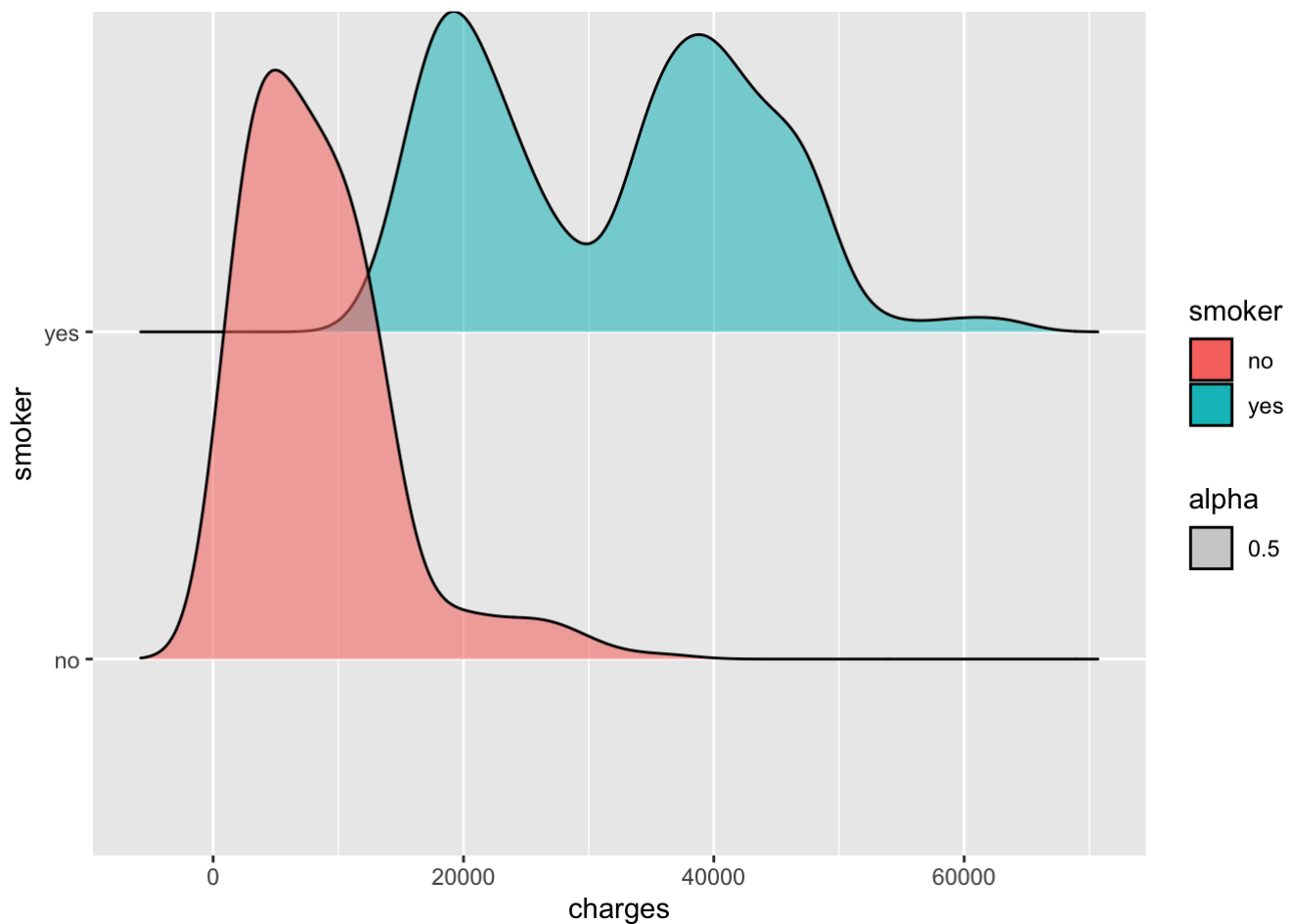
```
insurance %>%  
  ggplot(aes(smoker, charges, fill = smoker)) +  
  geom_boxplot()
```



```
insurance %>%  
  ggplot(aes(charges, smoker, fill = smoker, alpha = 0.5))+  
  ggribges::geom_density_ridges()
```

```
## Picking joint bandwidth of 2300
```

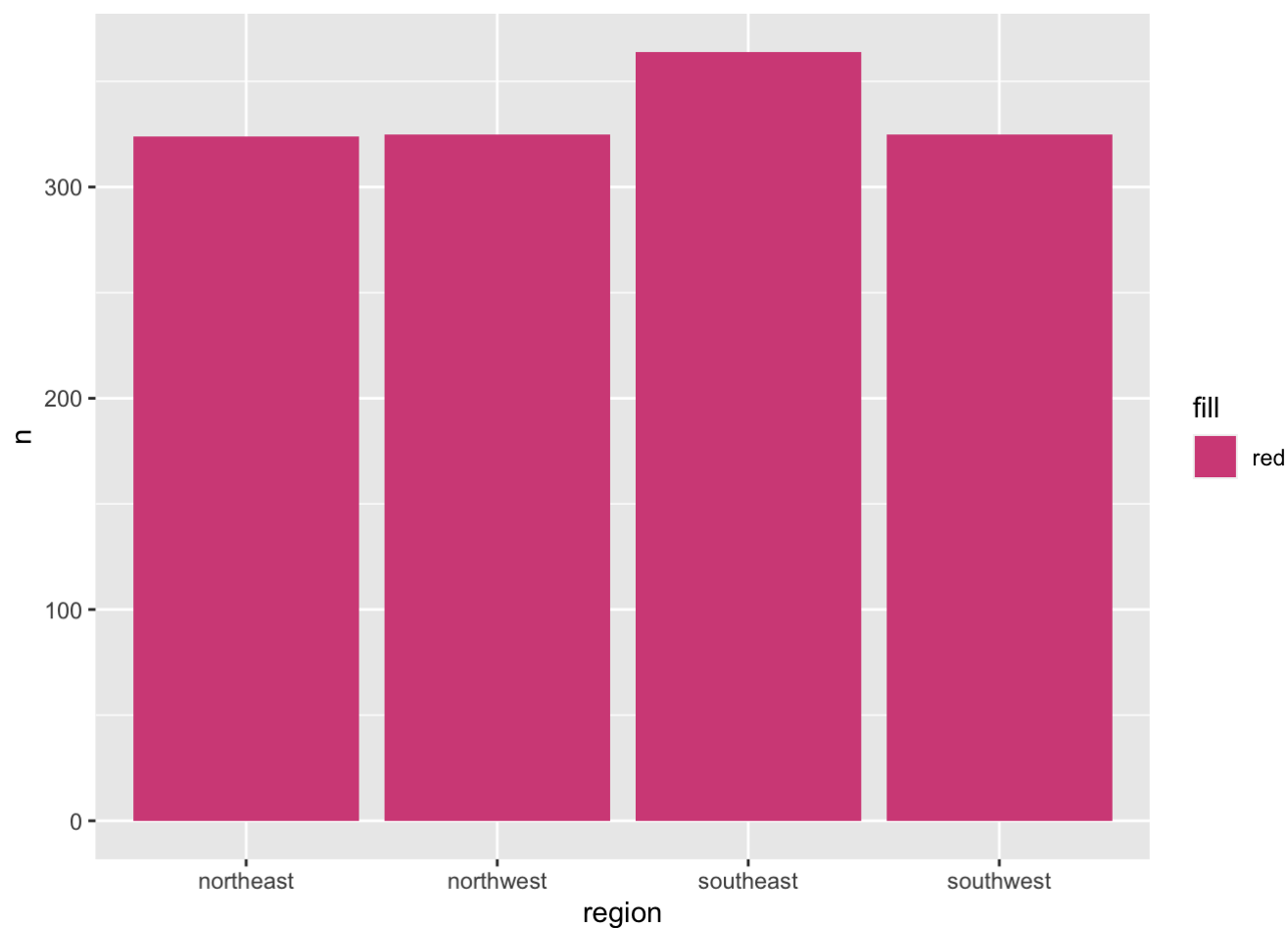




在正常的波动范围内，吸烟用户的保险支出费用远高于非吸烟用户，吸烟用户在支出费用为30000美金左右呈现山谷状，是什么因素导致这一情况呢？需要对吸烟群体进行划分分析，也许和年龄、收入等有关。

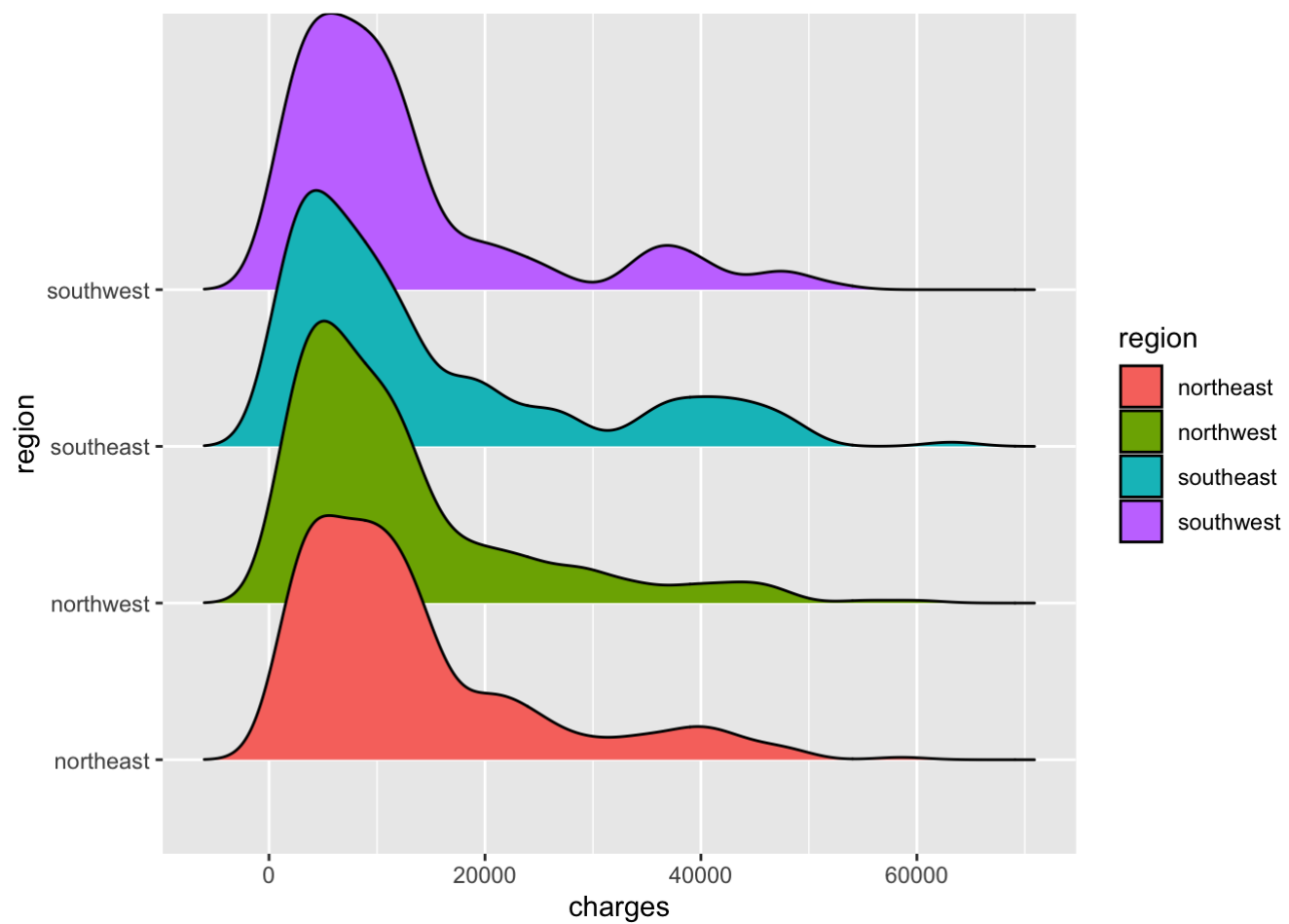
#地区因素

```
insurance %>%  
  count(region) %>%  
  ggplot(aes(region, n, fill = "red"))+  
  geom_col()+  
  scale_fill_manual(values = c("#d45087"))
```

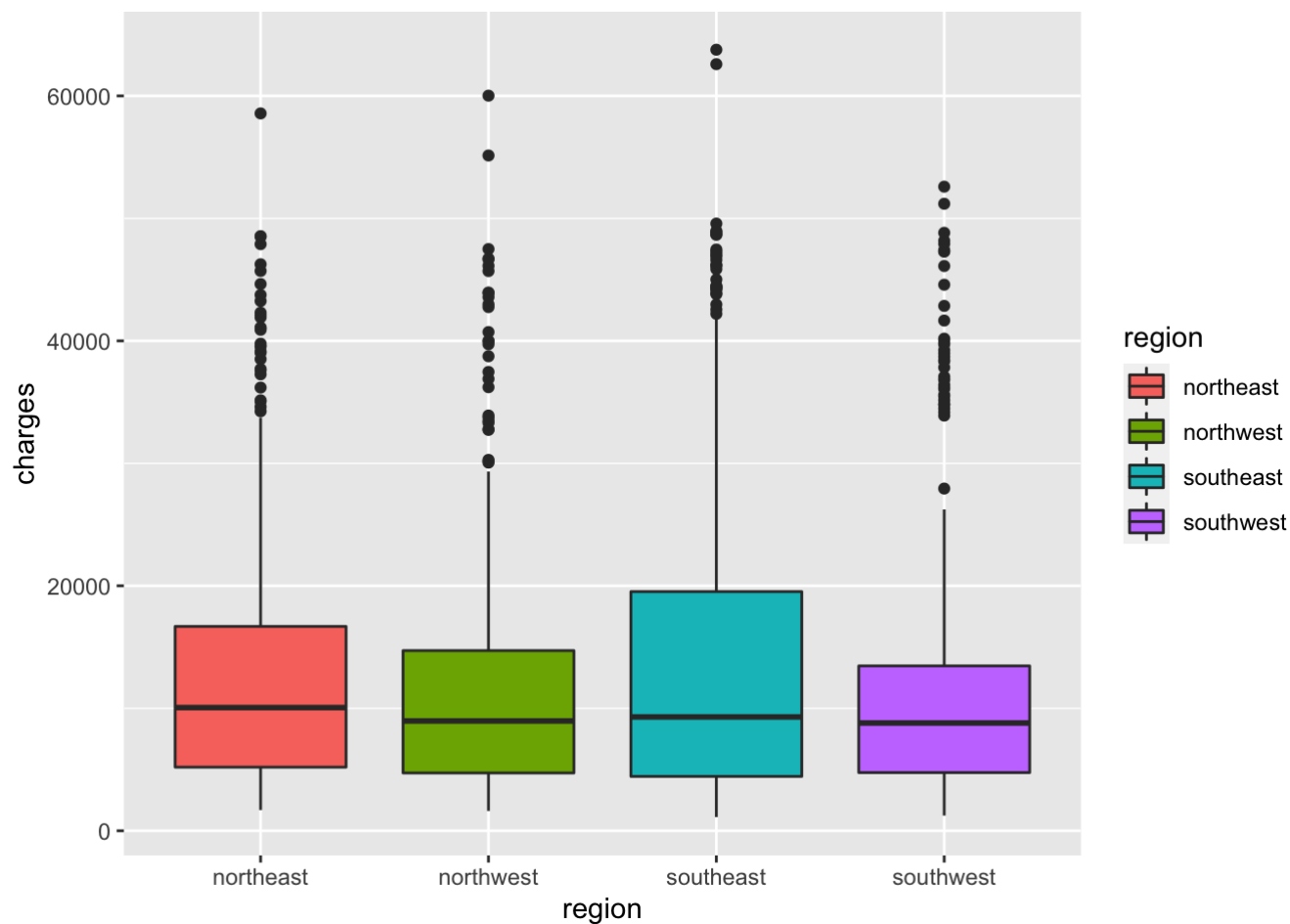


```
insurance %>%  
  ggplot(aes(charges, region, fill = region))+  
  ggribes::geom_density_ridges()
```

```
## Picking joint bandwidth of 2370
```



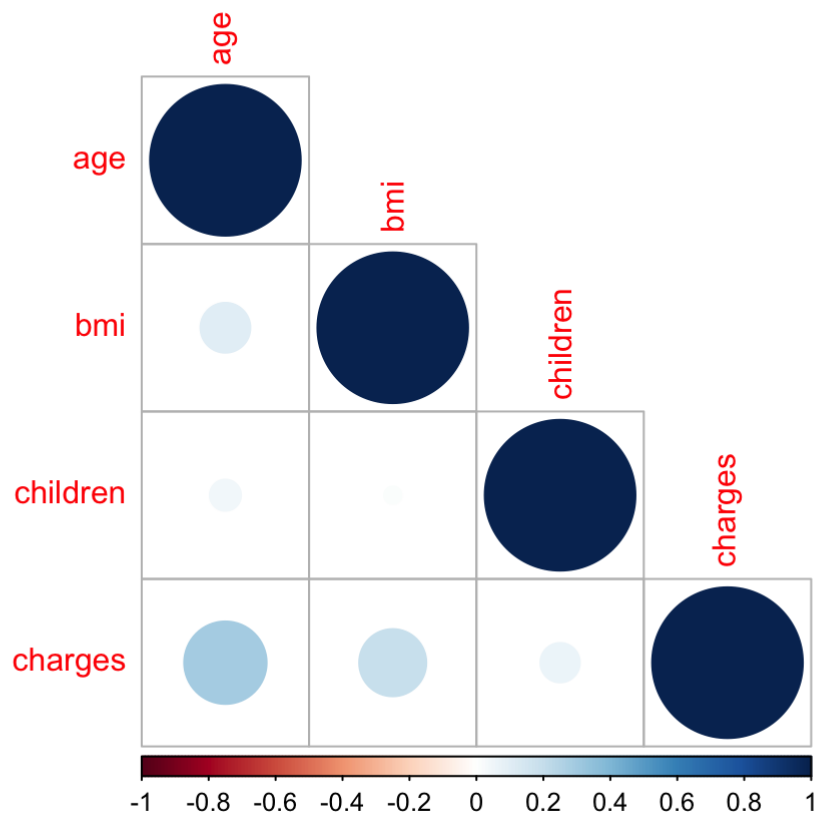
```
insurance %>%  
  ggplot(aes(region, charges, fill = region))+  
  geom_boxplot()
```



地区上，东南部医疗保险支出费用的极值要更高于其他地区，可能是因为地处美国的政治、经济、文化、中心-纽约及其周边。

#相关系数矩阵

```
insurance %>%
  select(-sex, -smoker, -region) %>%
  cor() %>%
  corrplot::corrplot(type = "lower")
```



charges同age、bmi、children都呈现正相关，同age的相关性要强一些。

##model

```
fit <- insu_df %>%  
  mutate_at(vars(age, bmi, children, charges), scale) %>%  
  lm(charges ~ age+bmi+children, data = .)  
summary(fit)
```

```
##
## Call:
## lm(formula = charges ~ age + bmi + children, data = .)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.1465 -0.5775 -0.4205  0.5884  4.0155
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.732e-17  2.567e-02   0.000   1.0000
## age         2.784e-01  2.586e-02  10.767 < 2e-16 ***
## bmi         1.672e-01  2.584e-02   6.472 1.35e-10 ***
## children    5.404e-02  2.571e-02   2.102  0.0357 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9391 on 1334 degrees of freedom
## Multiple R-squared:  0.1201, Adjusted R-squared:  0.1181
## F-statistic: 60.69 on 3 and 1334 DF,  p-value: < 2.2e-16
```

```
broom::tidy(fit)
```

```
## # A tibble: 4 x 5
##   term          estimate std.error statistic  p.value
##   <chr>          <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept) 2.73e-17    0.0257  1.06e-15 1.00e+ 0
## 2 age         2.78e- 1    0.0259  1.08e+ 1 5.53e-26
## 3 bmi         1.67e- 1    0.0258  6.47e+ 0 1.35e-10
## 4 children    5.40e- 2    0.0257  2.10e+ 0 3.57e- 2
```

在显著水平为0.1%的情况下，age和bmi相对更重要，children数量的重要性相对弱一些。

```
mod2 <- lm(charges ~ age + smoker, data = insu_df)
mod2
```

```
##
## Call:
## lm(formula = charges ~ age + smoker, data = insu_df)
##
## Coefficients:
## (Intercept)          age      smokeryes
##      -2391.6         274.9        23855.3
```

```
broom::tidy(mod2)
```

```
## # A tibble: 3 x 5
##   term          estimate std.error statistic  p.value
##   <chr>         <dbl>    <dbl>    <dbl>    <dbl>
## 1 (Intercept)   -2392.    528.    -4.53 6.52e- 6
## 2 age           275.    12.5    22.1 2.91e-92
## 3 smokeryes     23855.   433.    55.0 0.
```

## #多重线性

```
mod3 <- lmer(charges ~ age + (1 + age | smoker), data = insu_df)
```

```
## boundary (singular) fit: see ?isSingular
```

```
mod3
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: charges ~ age + (1 + age | smoker)
## Data: insu_df
## REML criterion at convergence: 27234.39
## Random effects:
## Groups Name Std.Dev. Corr
## smoker (Intercept) 9963.72
## age 18.18 1.00
## Residual 6396.79
## Number of obs: 1338, groups: smoker, 2
## Fixed Effects:
## (Intercept) age
## 9066 287
## optimizer (nloptwrap) convergence code: 0 (OK) ; 0 optimizer warnings; 1 lme4 warning
s
```

```
broom.mixed::tidy(mod3, effects = "fixed")
```

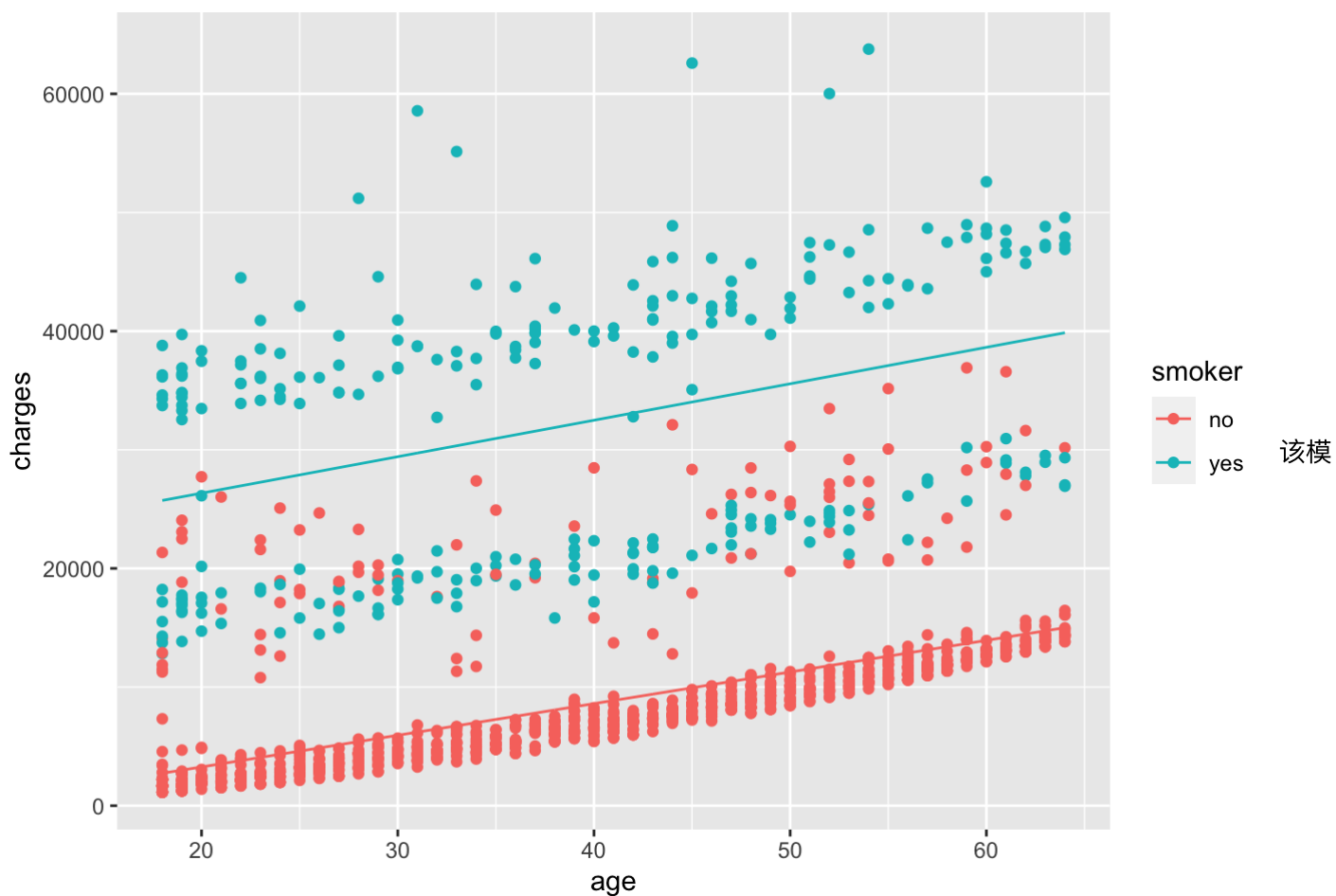
```
## # A tibble: 2 x 5
##   effect term          estimate std.error statistic
##   <chr> <chr>         <dbl>    <dbl>    <dbl>
## 1 fixed (Intercept)   9066.    7065.     1.28
## 2 fixed age           287.    17.9    16.0
```

```
broom.mixed::tidy(mod3, effects = "ran_vals")
```

```
## # A tibble: 4 x 6
##   effect   group level term      estimate std.error
##   <chr>    <chr> <chr> <chr>      <dbl>     <dbl>
## 1 ran_vals smoker no    (Intercept) -11132.    183.
## 2 ran_vals smoker yes   (Intercept)  11132.    361.
## 3 ran_vals smoker no    age        -20.3     0.334
## 4 ran_vals smoker yes   age         20.3     0.658
```

#以somoker为分组对age变量做多重线性模型的可视化

```
insu_df %>%
  add_predictions(mod3) %>%
  ggplot(aes( age, charges, color = smoker)) +
  geom_point() +
  geom_line(aes(x = age, y = pred))
```



型对不抽烟的用户拟合的还是比较好的，但是对于吸烟的用户拟合直线明显感觉有些粗旷。或许与吸烟的量以及其他因素有关，导致该模型拟合的绿色直线，有些不够好。

```
mod4 <- lmer(charges ~ age + (1 + age | sex), data = insu_df)
```

```
## boundary (singular) fit: see ?isSingular
```

```
mod4
```



```
## Linear mixed model fit by REML ['lmerMod']
## Formula: charges ~ age + (1 + age | sex)
## Data: insu_df
## REML criterion at convergence: 28805.38
## Random effects:
## Groups      Name                Std.Dev.  Corr
## sex         (Intercept)         908.156
##              age                 2.365  1.00
## Residual                    11538.881
## Number of obs: 1338, groups: sex, 2
## Fixed Effects:
## (Intercept)              age
##      3122.8             258.7
## optimizer (nloptwrap) convergence code: 0 (OK) ; 0 optimizer warnings; 1 lme4 warning
s
```

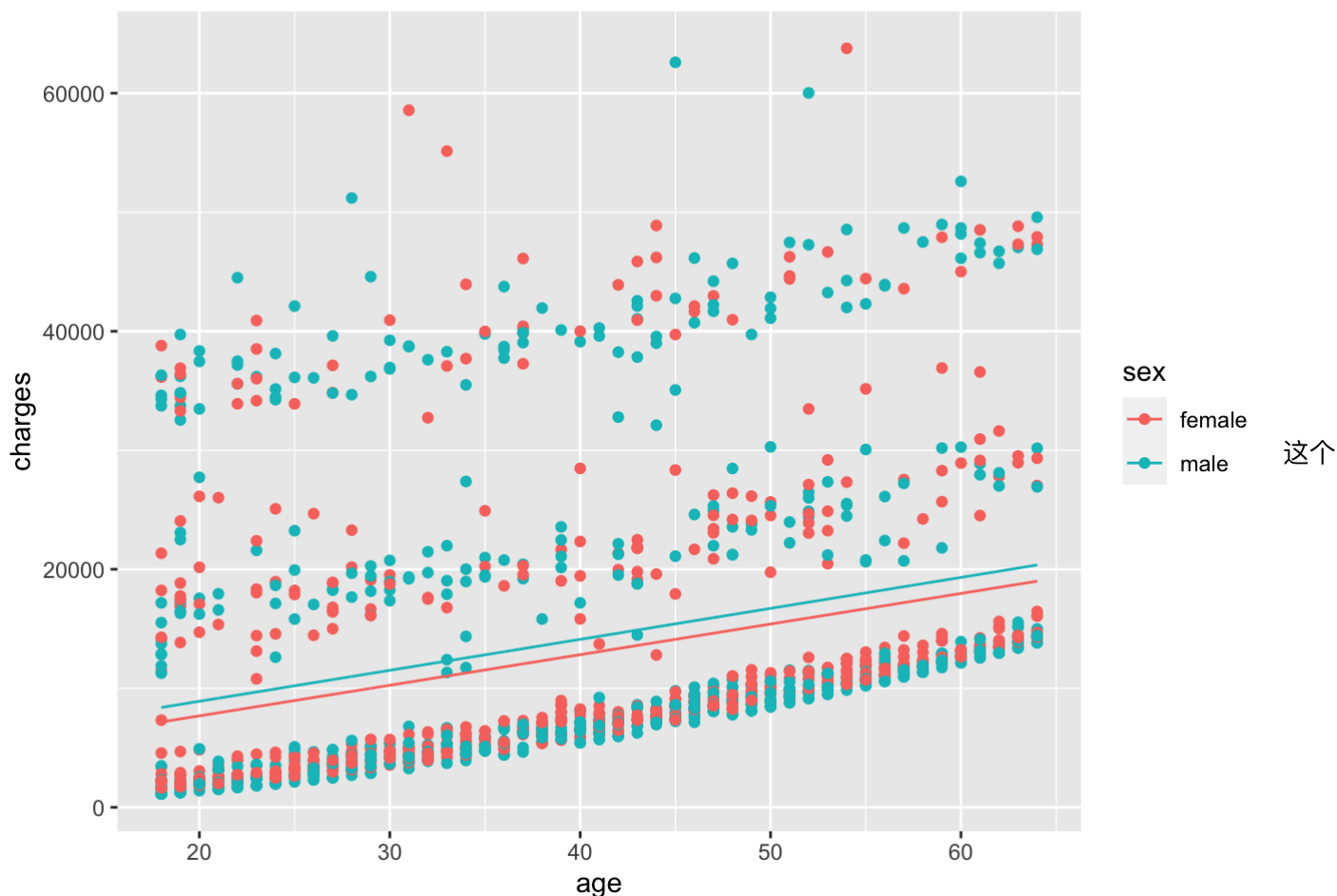
```
broom.mixed::tidy(mod4, effects = "fixed")
```

```
## # A tibble: 2 x 5
##   effect term          estimate std.error statistic
##   <chr>  <chr>          <dbl>    <dbl>    <dbl>
## 1 fixed  (Intercept)    3123.    1135.      2.75
## 2 fixed  age           259.     22.5     11.5
```

```
broom.mixed::tidy(mod4, effects = "ran_vals")
```

```
## # A tibble: 4 x 6
##   effect  group level term          estimate std.error
##   <chr>   <chr> <chr>  <chr>          <dbl>    <dbl>
## 1 ran_vals sex   female (Intercept) -582.    371.
## 2 ran_vals sex   male   (Intercept)  582.    368.
## 3 ran_vals sex   female age        -1.52    0.966
## 4 ran_vals sex   male   age         1.52    0.959
```

```
insu_df %>%
  add_predictions(mod4) %>%
  ggplot(aes( age, charges, color = sex)) +
  geom_point() +
  geom_line(aes(x = age, y = pred))
```



模型的评价能力太不合适了。

```
mod5 <- lmer(charges ~ bmi + (1 + bmi | smoker), data = insu_df)
```

```
## boundary (singular) fit: see ?isSingular
```

```
mod5
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: charges ~ bmi + (1 + bmi | smoker)
## Data: insu_df
## REML criterion at convergence: 27132.37
## Random effects:
## Groups Name Std.Dev. Corr
## smoker (Intercept) 13479.9
## bmi 982.6 -1.00
## Residual 6158.5
## Number of obs: 1338, groups: smoker, 2
## Fixed Effects:
## (Intercept) bmi
## -3652.3 778.1
## optimizer (nloptwrap) convergence code: 0 (OK) ; 0 optimizer warnings; 1 lme4 warning
s
```

```
broom.mixed::tidy(mod5, effects = "fixed")
```

```
## # A tibble: 2 x 5
##   effect term          estimate std.error statistic
##   <chr>  <chr>          <dbl>    <dbl>    <dbl>
## 1 fixed  (Intercept)    -3652.    9571.    -0.382
## 2 fixed  bmi              778.     695.     1.12
```

```
broom.mixed::tidy(mod5, effects = "ran_vals")
```

```
## # A tibble: 4 x 6
##   effect  group level term          estimate std.error
##   <chr>   <chr> <chr> <chr>          <dbl>    <dbl>
## 1 ran_vals smoker no      (Intercept)    9530.    144.
## 2 ran_vals smoker yes    (Intercept)   -9530.    282.
## 3 ran_vals smoker no      bmi           -695.    10.5
## 4 ran_vals smoker yes    bmi            695.    20.5
```

该模型以不吸烟组作为参数对照，吸烟人群的bmi每增加一个单位，医疗费用支出增加982.6。

#模型5可视化。

```
insu_df %>%
  add_predictions(mod5) %>%
  ggplot(aes( bmi, charges, color = smoker)) +
  geom_point() +
  geom_line(aes(x = bmi, y = pred))
```



这个模型的解释能力很好，从健康的角度考虑，吸烟与否和肥胖状况确实是健康的两大杀手，对于二者均沾的人来说，健康程度要差一些，在医疗费用的支出上高一些的可能性是合理的。从数据上看，这样的数据分布，表明这一数据集中的用户明显可以分为两类人，中间还有一些交叉的用户。

##结论 1.美国居民医疗费用支出集中分布在200-1500美元。 2.20岁以下的儿童是医疗费用支出的人数是最多的，其他年龄段人数上差异不大，性别和地区上差异不大。不同的肥胖指数与是否吸烟人群在医疗费用上差异变化很大。 3.从模型上看，医疗费用支出同bmi、smoker、age这三个变量表现出较高的相关性，但这种相关性不是固定的单独线性关系，而是多重线性关系，从图形拟合中能得到验证。 4.形象的说这三个因素相互作用影响到了医疗费用支出的金额，医疗费用的变化收到多重因素的影响。从常识来看，一个人随着年龄的增加+肥胖严重+吸烟，那么健康问题将会非常突出，高血压、心脏病、肺病等疾病患病的概率将会大大增加，医疗费用的支出也将会大大增加。