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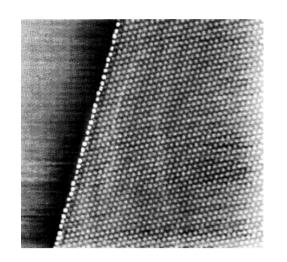
# Magic-angle twisted 2D materials

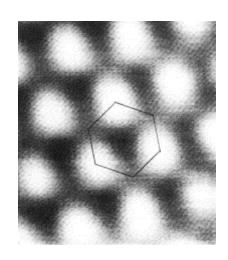
Group Member: 王杏 林益浩 王昊 杜思敬 赵天伦 李科卫 王继鹏

- Moire Pattern & Twistronics
- Moire band and Magic angle
- Experiments
- Summary

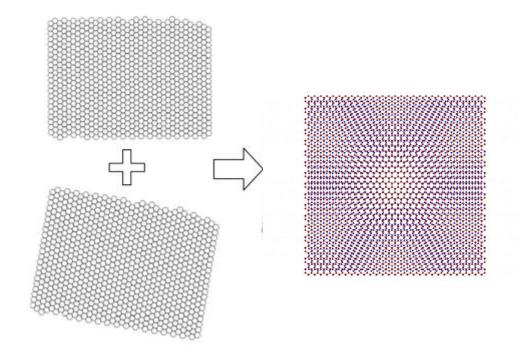
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### Moire Pattern



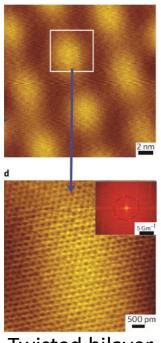


$$D = d/[2\sin(\theta/2)]$$

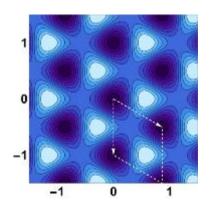


2005 Pong, W.-T., Durkan, C. J. Phys. D:Appl. Phys. 38(21), pp. R329-R355

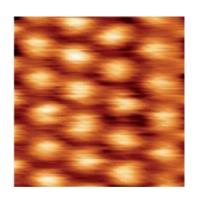
#### Twisted 2D materials & Twistronics



Twisted bilayer graphene



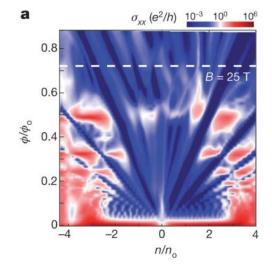
WS2/MoS2 heterobilayers



Bilayer graphene on h-BN

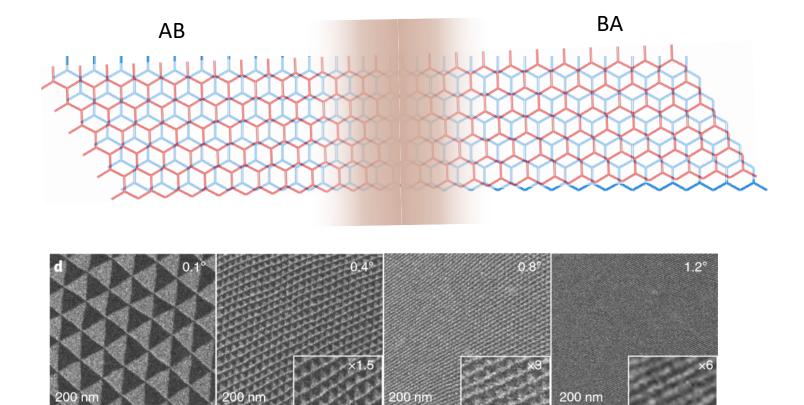
#### **Novel Physical Properties:**

- Unconventional superconductivity
- Moire excitons
- Hofstadter's butterfly
- ...



2010 Li, G.et.al. Nat. Phys. 6(2), pp. 109-113 2018 Wu, F. et.al. PRB 97(3),035306 2013 Ponomarenko, L.A.et.al. Nature 497(7451), pp. 594-597 2013 Dean, C.R. et.al. Nature. 497(7451), pp. 598-602

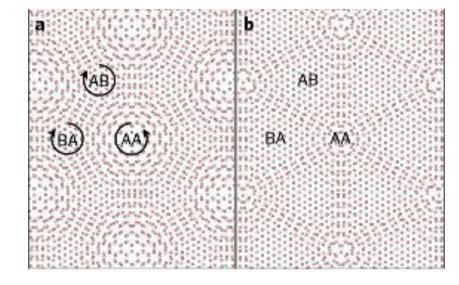
# Twisted bilayer graphene(TBG)



2019 Yoo, H.et.al. Nat. Mat. 18(5), pp. 448-453

Atomic and electronic reconstruction at the van der Waals interface in twisted bilayer graphene

Formation of the "commensurate domains"

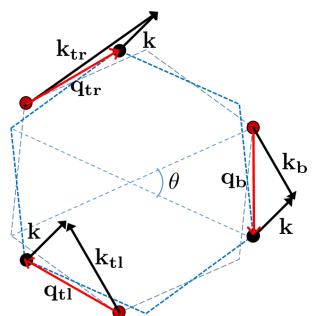


- Moire Pattern & Twistronics
- Moire band and Magic angle
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- Summary

### Moire band

#### Problem:

- Breakdown of Bloch electron picture due to Incommensurate structure
- Solution: Notion of Moire band
- 2011 Bistritzer, R.et.al. PNAS. Moiré bands in twisted double-layer graphene



$$H = \begin{pmatrix} h(-\theta/2) & T(\mathbf{r}) \\ T^{\dagger}(\mathbf{r}) & h(\theta/2) \end{pmatrix}$$

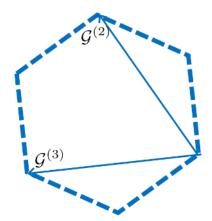
Layers' Dirac cone:

$$h = iv\sigma \cdot \nabla$$

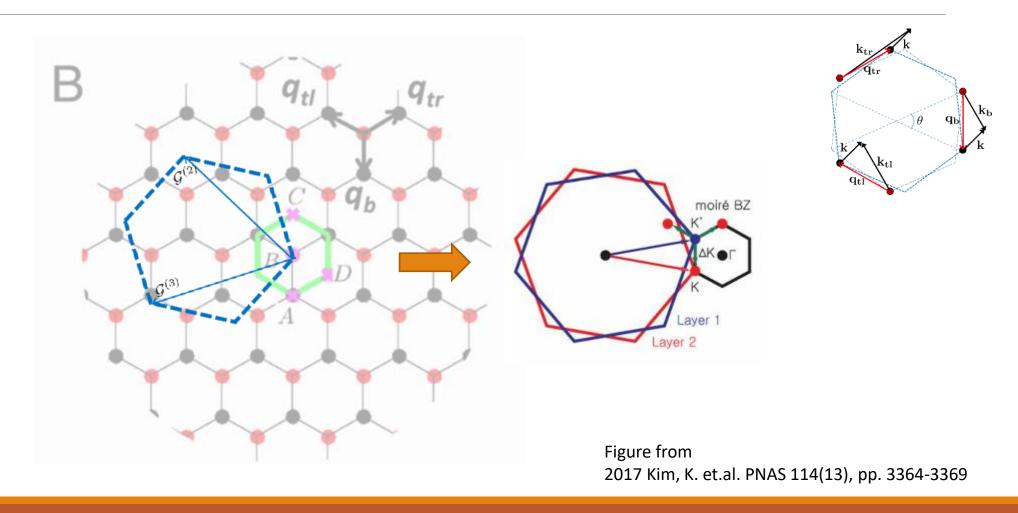
Three types of interlayer hopping:

$$T(\mathbf{r}) = w \sum_{\cdot} e^{-i\mathbf{q}_j \cdot \mathbf{r}} T_j$$
  $\qquad w \sim \text{vdW interaction strength}$ 

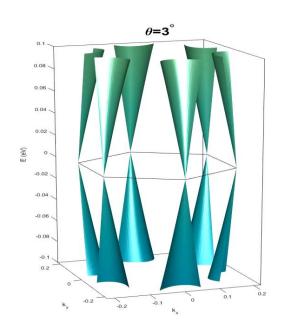
$$T_1=\left(egin{array}{cc} 1 & 1 \ 1 & 1 \end{array}
ight), T_2=\left(egin{array}{cc} e^{-i\phi} & j \ e^{i\phi} & e^{-i\phi} \end{array}
ight), T_3=\left(egin{array}{cc} e^{i\phi} & 1 \ e^{-i\phi} & e^{i\phi} \end{array}
ight) \;\; ext{where} \;\; \phi=2\pi/3$$

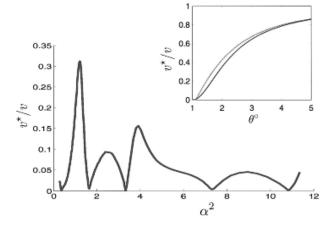


## Moire band

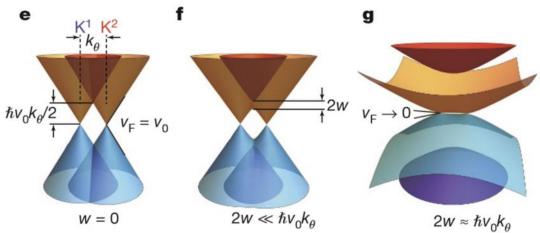


# Emergence of "Magic angle"





Calculated Fermi velocity of Moire Dirac cone  $\alpha = w/vk_{\theta}$ 



List of "magic angle"  $\theta \approx 1.05^\circ$  ,  $0.5^\circ$  ,  $0.35^\circ$  ,  $0.24^\circ$  ,  $0.2^\circ$ 

When kinetic energy ~ interlayer vdW interaction

2011 Bistritzer, R.et.al. PNAS. 108(30), pp. 12233-12237

2018 Cao, Y. Nature 556(7699), pp. 80-84

nature > articles > article

Published: 05 March 2018

# Unconventional superconductivity in magic-angle graphene superlattices

Yuan Cao 🗁, Valla Fatemi, Shiang Fang, Kenji Watanabe, Takashi Taniguchi, Efthimios Kaxiras & Pablo Jarillo-Herrero 🖼

*Nature* **556**, 43–50(2018) Cite this article

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nature > letters > article

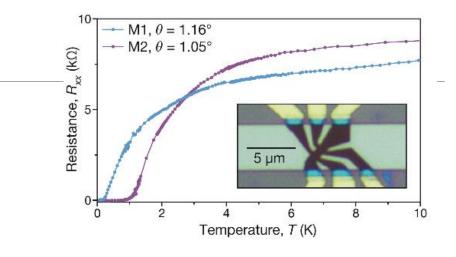
Published: 05 March 2018

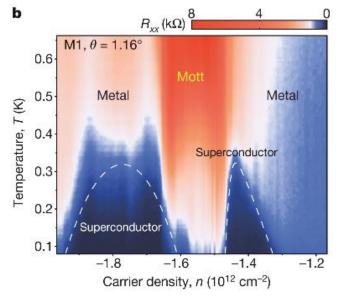
# Correlated insulator behaviour at half-filling in magicangle graphene superlattices

Yuan Cao, Valla Fatemi, Ahmet Demir, Shiang Fang, Spencer L. Tomarken, Jason Y. Luo, Javier D. Sanchez-Yamagishi, Kenji Watanabe, Takashi Taniguchi, Efthimios Kaxiras, Ray C. Ashoori & Pablo Jarillo-Herrero

Nature **556**, 80–84(2018) | Cite this article

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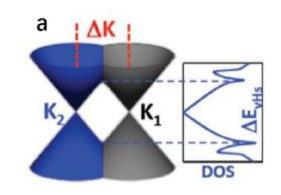




- Moire Pattern & Twistronics
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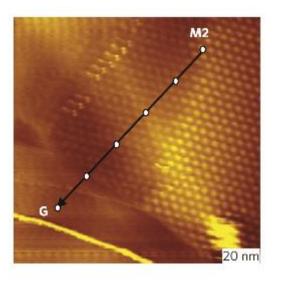
# Van Hove singularity

The integrand of the density of states is divergent.

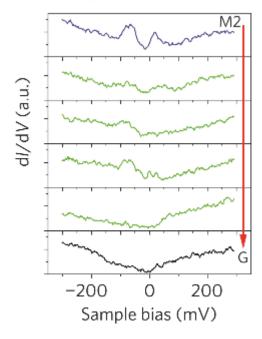


$$g(E) = rac{L^3}{(2\pi)^3} \iint rac{dk_x' \, dk_y'}{|ec
abla E|}$$

# Topography near the boundary of the pattern



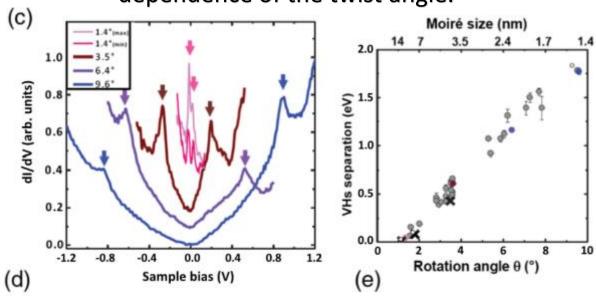
# Spatial dependence of tunneling spectra along a line



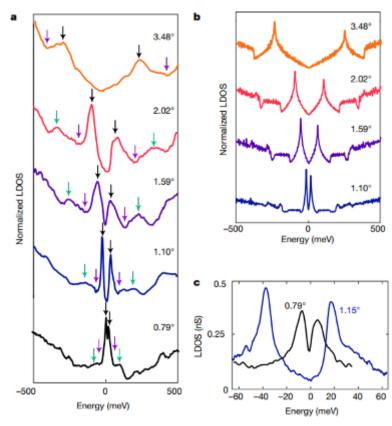
Li, G.; Luican, A.; Lopes dos Santos, J.M.B.; Castro Neto, A.H.; Reina, A.; Kong, J.; Andrei, E.Y. Observation of Van Hove singularities in twisted graphene layers. Nat. Phys. 2010, 6, 109–113.

# Van Hove singularity

The Van Hove singularity is in dependence of the twist angle.



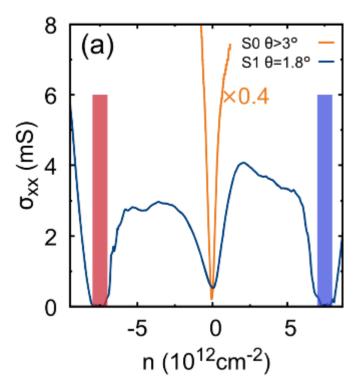
$$\Delta E_{\rm vHs} = 2\hbar v_F \Gamma K \sin(\theta/2) - 2t_{\theta}$$

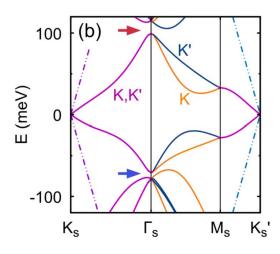


Choi, Y., Kemmer, J., Peng, Y. *et al.* Electronic correlations in twisted bilayer graphene near the magic angle. *Nat. Phys.* **15**, 1174–1180 (2019).

# Mott insulator & Superconductivity

The conductance of different twist angles.



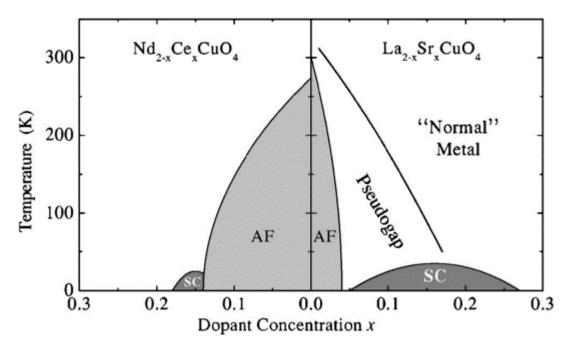


 $n = 7.5 \times 10^{12} \ cm^{-2}$ , is 4 times of the mini Brillouin zone area

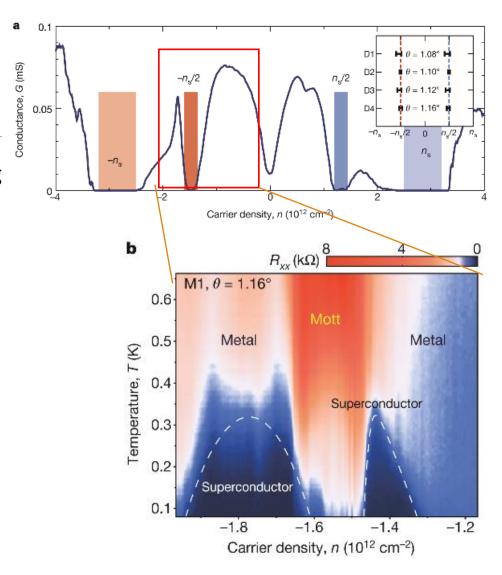
$$A_{\rm SL} = 4/n = 53.3 \text{ nm}^2$$
  $\Rightarrow \theta = 1.8^{\circ}$ 

### Mott insulator & Superconductivity

Schematic phase diagram of high-Tc superconductors showing hole doping right side and electron doping left side.

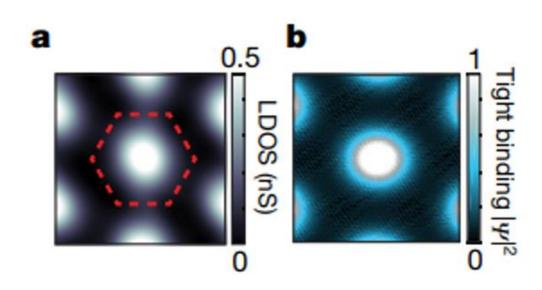


#### Measured conductance G of magic-angle TBG device.

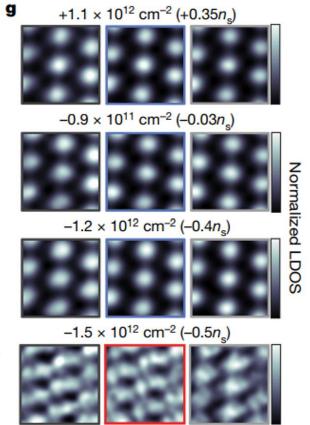


Cao, Y.; et al. Correlated insulator behaviour at half-filling in magic-angle graphene superlattices. Nature 2018, 556, 80–84 Cao, Y.; Jarillo-Herrero, P. ;et al, Unconventional superconductivity in magic-angle graphene superlattices. Nature 2018, 556, 43–50

## Mott insulator & Superconductivity



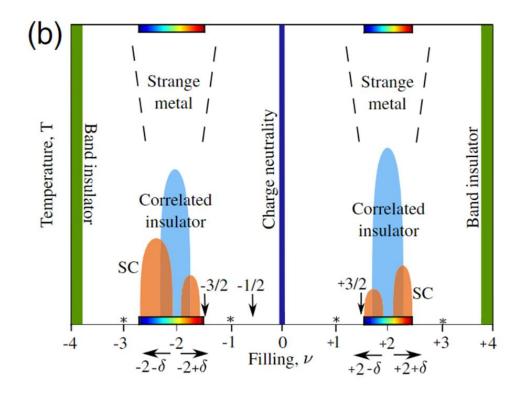
C3-Symmetry breaking when the Fermi level attaches the half filling.



### Summary

- Van Hove singularity
- Superconductor
- CDW
- Magnetism
- Strange metal
- ●...

- Twistronics
- Multilayer twistronics



2020 Cao, Y. et.al. PRL 124(7),076801

Thank you for attention