

解: 由题可得: 总传递矩阵为:
$$\begin{bmatrix} 1 & \frac{1}{f_1'} \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -d & 1 \end{bmatrix} \begin{bmatrix} 1 & \frac{1}{f_2'} \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 - \frac{d}{f_1'} & \frac{1}{f_1'} + \frac{1}{f_2'} - \frac{d}{f_1' f_2'} \\ -d & 1 - \frac{d}{f_2'} \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} u_1' \\ y_1' \end{bmatrix} = \begin{bmatrix} 1 - \frac{d}{f_1'} & \frac{1}{f_1'} + \frac{1}{f_2'} - \frac{d}{f_1' f_2'} \\ -d & 1 - \frac{d}{f_2'} \end{bmatrix} \begin{bmatrix} -f_1' \\ y \end{bmatrix}$$

对薄透镜传递矩阵可得:

$$\frac{1}{f} = \frac{1}{f_1'} + \frac{1}{f_2'} - \frac{d}{f_1' f_2'}$$

$$\Rightarrow f = \frac{f_1' f_2'}{f_1' + f_2' - d}$$

$$\Rightarrow f = \frac{f_1' f_2'}{d - f_1' - f_2'}$$

传递矩阵可转化为 $\begin{bmatrix} \beta & \frac{1}{f} \\ 0 & \beta \end{bmatrix}$ 形式

$$\beta = -\frac{1 - (1 - \frac{d}{f_1'})}{1 - (1 - \frac{d}{f_1'})} = -\frac{f_2'}{f_1'} \frac{d}{f_2'} \Rightarrow \beta = -\frac{f_2'}{f_1'}$$

同理其主点位置 $l_H = \frac{f_1' d}{f_2'} = -\frac{f_1' d}{d - f_1' - f_2'}$

$$l_H' = \frac{\frac{d}{f_1'}}{\frac{1}{f_1'} + \frac{1}{f_2'} - \frac{d}{f_1' f_2'}} = -f_2' d / (d - f_1' - f_2')$$

焦点位置: $l_F = \frac{d}{f_2'} - 1 / (\frac{1}{f_1'} + \frac{1}{f_2'} - \frac{d}{f_1' f_2'}) = \frac{f_1' (d - f_2')}{f_1' + f_2' - d}$

$$l_F' = \frac{f_2' (d - f_1')}{f_1' + f_2' - d}$$

节点位置: $l_j = \frac{1 - (1 - \frac{d}{f_2'})}{\frac{1}{f_1'} + \frac{1}{f_2'} - \frac{d}{f_1' f_2'}} = -\frac{f_1' d}{d - f_1' - f_2'}$

$$l_j' = \frac{1 - (1 - \frac{d}{f_1'})}{\frac{1}{f_1'} + \frac{1}{f_2'} - \frac{d}{f_1' f_2'}} = -\frac{f_2' d}{d - f_1' - f_2'}$$

可以看出在 $n = n'$ 即两侧同介质的情况下, 主点与节点重合