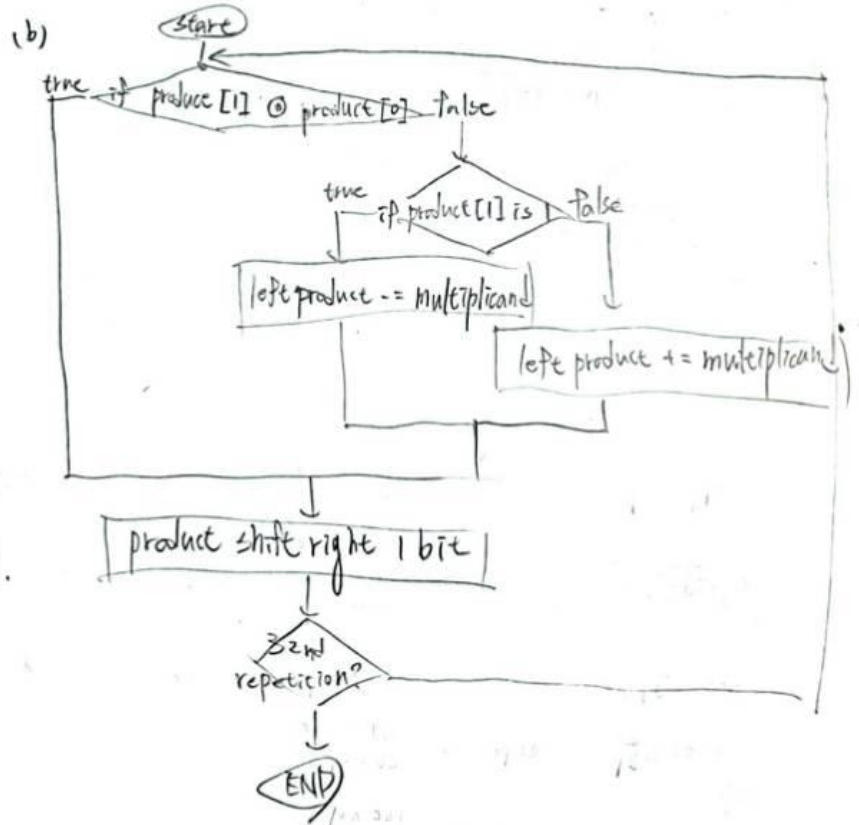
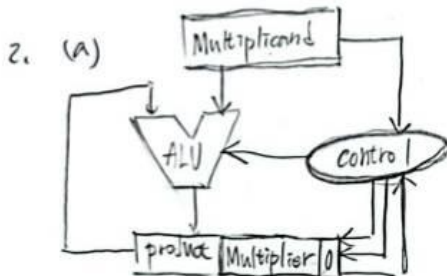


1. $147 = 10010011_{10}$ $28 = 00011100$

Iteration	step	Remainder	Divisor
0	shift left Remainder 1 bit	0000001 00100110	00011100
1	left Remainder \geq Divisor	11100101 00100110	00011100
2	if left Remainder ≤ 0		
3	left Remainder \neq Divisor	00000001 00100110	
4	shift left Remainder 1 bit	00000010 01001100	
5	if not repetition yet		
...			
19	shift left Remainder 1 bit	00100100 11000000	
20	if not repetition yet		
21	left Remainder \geq Divisor	00001000 11000000	
22	if left Remainder ≥ 0		
23	shift left Remainder 1 bit and set 1	00010001 10000001	
24	if not repetition yet		
25	left Remainder \geq Divisor	11101010 10000001	
26	if left Remainder ≤ 0		
27	left Remainder \neq Divisor	00010001 10000001	
28	shift left Remainder 1 bit	00100011 00000010	
29	if not repetition yet		
30	left Remainder \geq Divisor	00000111 00000010	
31	if left Remainder ≥ 0		
32	shift left Remainder 1 bit and set 1	00001110 00000011	
33	if repetition yet		
34	left Remainder shift left 1 bit	00000111 00000011	



(c) in some cases,
Booth's algorithm can achieve
the goal with less computation
than the original multiplication method.

4. (a) $0.3125 = 0.0101_2 \Rightarrow 1.0101 \times 2^{-2}$
 $1.0111 \ 0101000000_2$

(b) $10011000.01 + 0.0101010101$
 $= 1.00110000 \times 2^7 + 1.01010101 \times 2^{-2}$
 $= 1.00110000 \times 2^7 + 0.0000000101010101 \times 2^7$
 $= 1.00110001010101 \times 2^7$

$0 \ 0011 \ 0011000101010101$ $\left\{ \begin{array}{l} \text{Guard} = 0 \\ \text{Round} = 1 \\ \text{Sticky} = 0(0\dots 0) \end{array} \right.$ 捨去

$\Rightarrow 0 \ 0011 \ 00110001010101_2$

(c) $110.0111001 \times 1000.01101$
 $= 1.100111001 \times 2^2 \times 1.00001101 \times 2^3$
 $= 110110.00101100101 \times 2^{(2+3)}$
 $= 1.1011000101100101 \times 2^{(5+5)}$

$0 \ 01010 \ 101100010110010101$ $\left\{ \begin{array}{l} \text{Guard} = 0 \\ \text{Round} = 1 \\ \text{Sticky} = 0(0\dots 0) \end{array} \right.$ 捨去

$\Rightarrow 0 \ 01010 \ 10110001011001_2$

4. (a) $0.3125 = 0.0101_2 \Rightarrow 1.0101 \times 2^{-2}$
 $1 \ 0111 \ 01010 \ 00000 \#$

(b) $10011000.01 + 0.0101010101$
 $= 1.00110000 \times 2^7 + 1.01010101 \times 2^{-2}$
 $= 1.00110000 \times 2^7 + 0.00000000101010101 \times 2^7$
 $= 1.0011000101010101 \times 2^7$

$0 \ 0011 \ 00110001001010101 \ 0$ $\left\{ \begin{array}{l} \text{Guard} = 1 \\ \text{round} = 0 \\ \text{sticky} = 1 \end{array} \right.$

$\Rightarrow 0 \ 0011 \ 0011000101 \#$

(c) $110.0111001 \times 1000.01101$
 $= 1.100111001 \times 2^2 \times 1.00001101 \times 2^3$
 $= 110110.001011100101 \times 2^{(2+3)}$
 $= 1.10110001011100101 \times 2^{(5+5)}$

$0 \ 01010 \ 101100010111001010 \ 0$ $\left\{ \begin{array}{l} \text{Guard} = 1 \\ \text{round} = 1 \\ \text{sticky} = 1 \end{array} \right.$

$\Rightarrow 0 \ 01010 \ 1011000110 \#$