

CSC380: Principles of Data Science

Data Analysis, Collection, and Visualization 1

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Announcements

HW01 is out (due next Friday, Sep 5 by 11:59pm)

Lecture participation <u>self-report form</u> in course website

Office hours start tomorrow.

Today's plan

- Basic data processing using Pandas
- Descriptive statistics using Pandas

Basic data visualization





Pandas

Pandas

Open source library for data handling and manipulation in high-performance environments.



Installation If you are using Anaconda package manager,

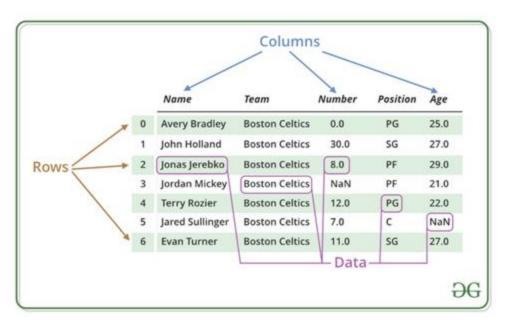
```
conda install pandas
```

Or if you are using PyPi (pip) package manager,

```
pip install pandas
```

See Pandas documentation for more detailed instructions https://pandas.pydata.org/docs/getting started/install.html

Primary data structure : Essentially a table



Q: how is it different from an array?

```
array([[30, 32, 35],
[40, 42, 45],
[50, 52, 55]])
```

- Dataframes' elements' data types can be mixed; an array usually store elements of same type
- Dataframes' rows and are labeled with indices; array indices are usually integers

DataFrame Example

Create and print an entire DataFrame



DataFrame Example

Can create *named columns* using dictionary

```
Name Age
import pandas as pd
# intialise data of lists.
                                                                    20
                                                            Tom
data = {'Name':['Tom', 'nick', 'krish', 'jack'],
        'Age':[20, 21, 19, 18]}
                                                            nick
                                                                    21
# Create DataFrame
                                                            krish
                                                                    19
df = pd.DataFrame(data)
                                                                    18
                                                            jack
# Print the output.
print(df)
```

all data must have the same length

DataFrame: Selecting Columns

Select columns to print by name

```
# Import pandas package
import pandas as pd
                                                                         Name Qualification
# Define a dictionary containing employee data
data = {'Name':['Jai', 'Princi', 'Gaurav', 'Anuj'],
                                                                            Jai
                                                                    0
                                                                                         Msc
        'Age':[27, 24, 22, 32],
        'Address':['Delhi', 'Kanpur', 'Allahabad', 'Kannauj'],
                                                                         Princi
                                                                                          MA
        'Qualification':['Msc', 'MA', 'MCA', 'Phd']}
                                                                    2 Gaurav
                                                                                        MCA
# Convert the dictionary into DataFrame
df = pd.DataFrame(data)
                                                                    3
                                                                          Anuj
                                                                                         Phd
# select two columns
```

print(df[['Name', 'Qualification']])

access columns by name, not the column index!

DataFrame: Selecting Columns

```
pandas.Series
        import pandas as pd
        data = {'Name': ['tom', 'nick'], 'Age': [10,20]}
                                                                                       class pandas.Series(data=None, index=None, dtype=None, name=None, copy=False,
        df = pd.DataFrame(data)
                                                                                       fastpath=False)
                                                                                                                                                            [source]
                                                                                           One-dimensional ndarray with axis labels (including time series).
        df[['Name']]
                                                                                          Labels need not be unique but must be a hashable type. The object supports both integer- and label-
                                                                                          based indexing and provides a host of methods for performing operations involving the index. Statistical
[36]:
            Name
                                                                                           methods from ndarray have been overridden to automatically exclude missing data (currently
                                                                                           represented as NaN).
              tom
              nick
        df['Name']
                                                                                              still a DataFrame
                tom
               nick
        Name: Name, dtype: object
                                                                                                       essentially, a DataFrame's single
        type(df[['Name']]), type(df['Name']
[38]:
                                                                                                       row or column
        (pandas.core.frame.DataFrame, pandas.core.series.Series)
```

DataFrame : Selecting Rows

Use df.loc to access certain rows

```
import pandas as pd
import numpy as np
# Define a dictionary containing employee data
data = {'Name':['Jai', 'Princi', 'Gaurav', 'Anuj'],
        'Age':[27, 24, 22, 32],
        'Address':['Delhi', 'Kanpur', 'Allahabad', 'Kannauj'],
        'Qualification':['Msc', 'MA', 'MCA', 'Phd']}
                                                                         Output
# Convert the dictionary into DataFrame
df = pd.DataFrame(data)
                                                                           Address Qualification
                                                              Name
                                                                    Age
                                                            Princi
                                                                            Kanpur
                                                                                               MA
# Print rows 1 & 2
                                                                      22 Allahabad
                                                            Gaurav
                                                                                              MCA
row = df.loc[1:2]
                                                                      (still a DataFrame)
print (row)
```

1:2 includes 2! This is different from Python array indexing

DataFrame : Selecting Rows

```
[6]: import pandas as pd
      data = {'Name': ['tom', 'nick'], 'Age': [10,20]}
      df = pd.DataFrame(data)
[19]: df.loc[1:1]
[19]:
        Name Age
         nick
               20
[20]: df.loc[1]
[20]: Name
              nick
                20
      Age
      Name: 1, dtype: object
[21]: type(df.loc[1:1]), type(df.loc[1])
     (pandas.core.frame.DataFrame, pandas.core.series.Series)
```

- df.loc[1:1] is DataFrame object
- df.loc[1] is a series

DataFrame : Selecting Rows

head() and tail() select rows from beginning / end

handy when we would like to get a sense of what a big table looks like

```
import pandas as pd
import numpy as np
# Define a dictionary containing employee data
data = {'Name':['Jai', 'Princi', 'Gaurav', 'Anuj'],
        'Age':[27, 24, 22, 32],
        'Address':['Delhi', 'Kanpur', 'Allahabad', 'Kannauj'],
                                                                         Output
        'Qualification':['Msc', 'MA', 'MCA', 'Phd']}
                                                                Name
                                                                      Age Address Qualification
# Convert the dictionary into DataFrame
                                                                            Delhi
                                                                 Jai
                                                                     27
                                                                                            Msc
df = pd.DataFrame (data)
                                                           1 Princi
                                                                       24 Kanpur
                                                                                             MA
# Print first / last rows
                                                                       Age Address Qualification
                                                                 Name
first2 = df.head(2)
                                                           2 Gaurav
                                                                       22 Allahabad
                                                                                               MCA
last2 = df.tail(2)
                                                                       32
                                                                Anuj
                                                                             Kannauj
                                                                                               Phd
print (first2)
print('\n', last2)
```

Reading Data from Files

Easy reading / writing of standard formats

```
Output
                                                          index |
df = pd.read json("data.json")
print (df)
                                                                                Pulse Maxpulse
                                                                     Duration
                                                                                                 Calories
df.to csv("data.csv", index=False)
df csv = pd.read csv("data.csv")
                                                                                  110
                                                                                            130
                                                                                                    409.1
                                                                                 117
                                                                                            145
                                                                                                    479.0
print(df csv.head(2))
                                                                                            135
                                                                                                    340.0
                                                                                 103
                                                                            45
                                                                                 109
                                                                                            175
                                                                                                    282.4
Json format: e.g. X(twitter) API
                                                                                 117
                                                                                            148
                                                                                                    406.0
                                                                                            . . .
                                                                                                       . . .
                                                                164
                                                                                 105
                                                                                            140
                                                                                                    290.8
                                                                           60
            "fruits": ["apple", "banana", "cherry"],
                                                                165
                                                                                 110
                                                                                            145
                                                                                                    300.4
                                                                166
                                                                           60
                                                                                 115
                                                                                            145
                                                                                                    310.2
            "numbers": [1, 2, 3, 4],
                                                                167
                                                                           75
                                                                                  120
                                                                                                    320.4
                                                                                            150
            "mixed": [true, "hello", null]
                                                                           75
                                                                168
                                                                                 125
                                                                                            150
                                                                                                    330.4
                                                                [169 rows x 4 columns]
                                                                   Duration Pulse Maxpulse Calories
 CSV format (comma separated values)
                                                                         60
                                                                                110
                                                                                          130
                                                                                                  409.1
                                                                         60
                                                                               117
                                                                                          145
                                                                                                  479.0
           Name, Age, City
```

Alice,25,New York Bob,30,San Francisco Charlie,22,Chicago

Data Type Conversions

Working with DataFrames outside of Pandas can be tricky

```
df['Duration']
```

Q: is this a DataFrame object or Series object?

A: a Series object

We can easily convert a Series to builtin types, e.g., a list.

```
60
        60
        60
        45
        45
        . .
164
        60
165
        60
166
        60
167
        75
168
        75
Name: Duration, Length: 169, dtype: int64
```

Data Type Conversions

Or, to a numpy array

```
[6]: import pandas as pd
      data = {'Name': ['tom', 'nick'], 'Age': [10,20]}
      df = pd.DataFrame(data)
[29]: df
[29]:
         Name Age
          tom
          nick
               20
[31]: df.to_numpy()
[31]: array([['tom', 10],
             ['nick', 20]], dtype=object)
[40]: df['Name'].to_numpy()
[40]: array(['tom', 'nick'], dtype=object)
```

to_numpy(): can take Series and DataFrame objects as input

Numpy: Python library for scientific computing

Descriptive Statistics (using Pandas)

Descriptive Statistics Overview

- Given a data array, oftentimes useful to summarize it using some of its key features
 - Range
 - Histogram
 - Mean
 - Median
 - Mode

Range

- Difference between highest (maximum) and lowest (minimum) values
- [min, max] is called the range interval

Example what is the range of the following dataset? 4, 7, 2, 9, 12

Max: 12

Min: 2

=> Range interval = [2, 12], Range = 12 - 2 = 10

Histogram

Split the *range interval* into equally-sized bins and report counts in each bin.

Example Taking the ages of the presidents of the United States at the time of their inauguration (in total 44 points) 57,61,57,57,58,57,61,54,68,51, ... 47,70

Bins: (40, 45], (45, 50], (50, 55], (55, 60], (60, 65], (65, 70]

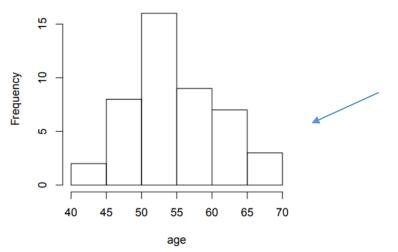
Histogram

Counts in different bins

(40, 45]	(45, 50]	(50, 55]	(55, 60]	(60, 65]	(65, 70]
2	8	16	9	7	3

We can also visualize the histogram using a bar plot:

Histogram of age



Histogram can show the "spread" of data

Mean

- Average of the data $x_1, ..., x_n$
- In formula:

$$\bar{x} = \frac{1}{n}(x_1 + \dots + x_n) =: \frac{1}{n} \sum_{i=1}^{n} x_i$$

Example heights of 3 students are 1.71, 1.84, 1.64 (m)

their average height $\bar{x} = \frac{1}{3}(1.71+1.84+1.63) = 1.73$ (m)

For data x_1, x_2, \ldots, x_N sort the data,

$$x_{(1)}, x_{(2)}, \ldots, x_{(n)}$$

- Notation $x_{(i)}$ means the i-th *lowest* value, e.g. $x_{(i-1)} \le x_{(i)} \le x_{(i+1)}$
- $x_{(1)}, x_{(2)}, \ldots, x_{(n)}$ are called *order statistics* not summary info, but rather a transformation

If n is **odd** then find the middle datapoint,

$$median(x_1,...,x_n) = x_{((n+1)/2)}$$

If n is even then average between both middle datapoints,

median
$$(x_1, \dots, x_n) = \frac{1}{2} (x_{(n/2)} + x_{(n/2+1)})$$

4.5

What is the median of the following data?

1, 2, 3, 4, 5, 6, 8, 9

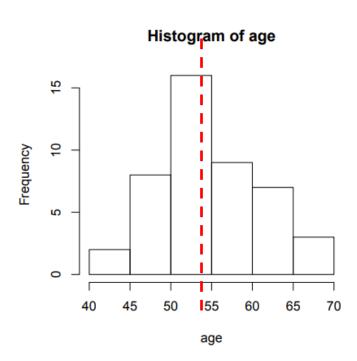
What is the median of the following data?

1, 2, 3, 4, 5, 6, 8, 100 **4.5**

Median is *robust* to outliers

Median

 Roughly speaking, median is the point where half of the population is below it and half of the population is above it



Mode

Value of highest number of appearances

Example what is the mode of the following dataset? 1,1,2,3,7,8,8,8,9

Count of 8: 3

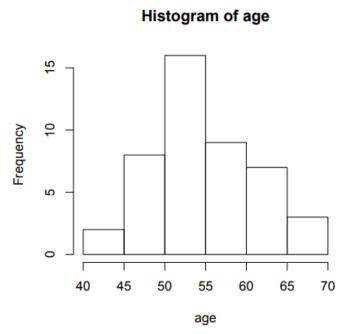
Count of 1: 2

Counts of other numbers: 1

=> Mode = 8

Mode

Roughly speaking, mode is the location of the histogram with the tallest bar



Summary Statistics in Pandas

Compute summary statistics on Pandas Series

```
print('Min: ', df['Duration'].min())
print('Max: ', df['Duration'].max())
print('Median: ', df['Duration'].median())

Min: 15
Max: 300
Median: 60.0
```

Can also count occurrences of unique values,

```
bf['Duration'].value_counts()
```

```
60
       79
       35
       16
90
150
120
180
15
75
160
210
270
25
300
80
Name: Duration, dtype: int64
```

```
s = df['Duration'].value_counts()
s[60]=79.
```

Summary Statistics

Compute summary statistics on each column of Dataframe



Many database operations are available

- You can specify index, which can speed up some operations
- You can do 'join'
- You can do 'where' clause to filter the data
- You can do 'group by'

More on Pandas

| pandas

Q. Search the docs ...

Installation

Package overview

handle?

Getting started tutorials

What kind of data does pandas

How do I read and write tabular data?

How do I select a subset of a

DataFrame ?

How to create plots in pandas?

How to create new columns derived from existing columns?

How to calculate summary statistics?

How to reshape the layout of tables?

How to combine data from multiple tables?

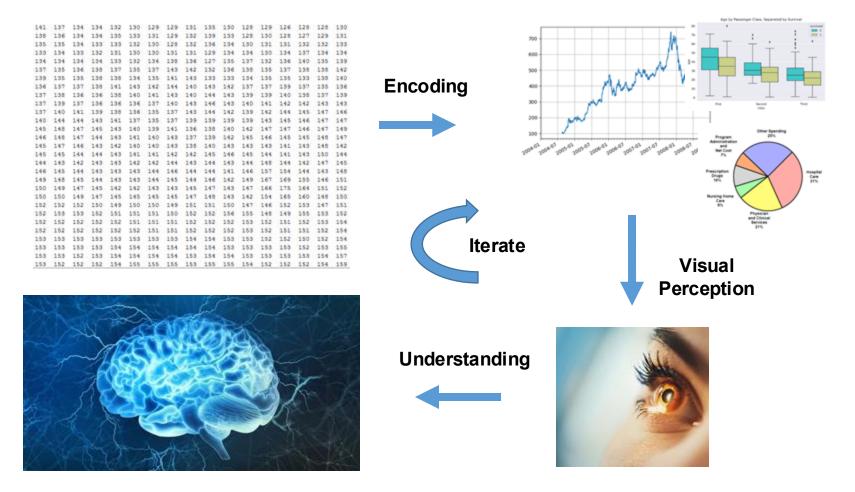
How to handle time series data with ease?

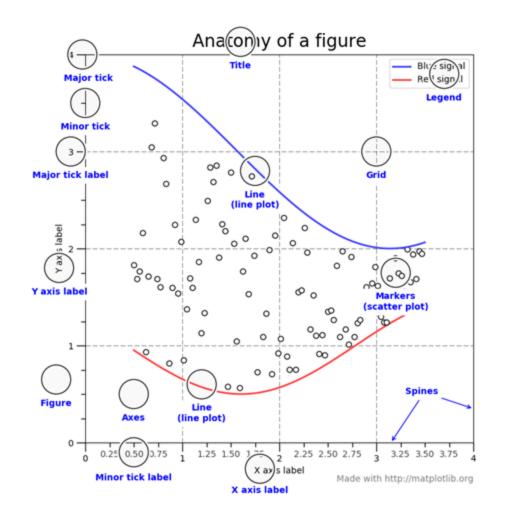
How to manipulate textual data?

Doing it by yourself helps a lot!

Data Visualization

Data Analysis, Exploration, and Visualization







components of a Matplotlib figure

Documentation + tutorials: https://matplotlib.org/

Data visualization in Python...



```
import matplotlib.pyplot as plt
import numpy as np
```

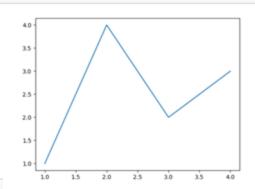
Create a simple figure

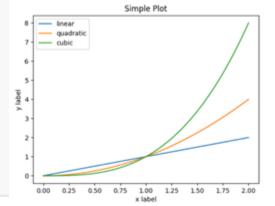
```
fig, ax = plt.subplots() # Create a figure containing a single axes.
ax.plot([1, 2, 3, 4], [1, 4, 2, 3]) # Plot some data on the axes.
```

A more complicated plot...

```
x = np.linspace(0, 2, 100)

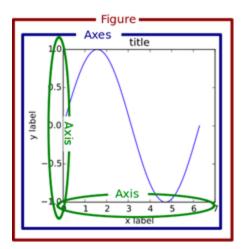
# Note that even in the 00-style, we use `.pyplot.figure` to create the figure.
fig, ax = plt.subplots() # Create a figure and an axes.
ax.plot(x, x, label='linear') # Plot some data on the axes.
ax.plot(x, x**2, label='quadratic') # Plot more data on the axes...
ax.plot(x, x**3, label='cubic') # ... and some more.
ax.set_xlabel('x label') # Add an x-label to the axes.
ax.set_ylabel('y label') # Add a y-label to the axes.
ax.set_title("Simple Plot") # Add a title to the axes.
ax.legend() # Add a legend.
```







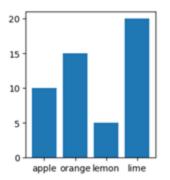
Axes: entire area of plot Axis: horizontal or vertical (2d)

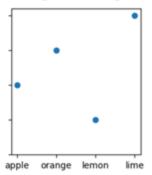


subplot() function: draw multiple plots in one figure

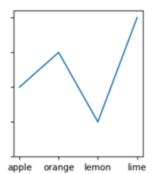
```
data = {'apple': 10, 'orange': 15, 'lemon': 5, 'lime': 20}
names = list(data.keys())
values = list(data.values())

fig, axs = plt.subplots(1, 3, figsize=(9, 3), sharey=True)
axs[0].bar(names, values)
axs[1].scatter(names, values)
axs[2].plot(names, values)
fig.suptitle('Categorical Plotting')
```



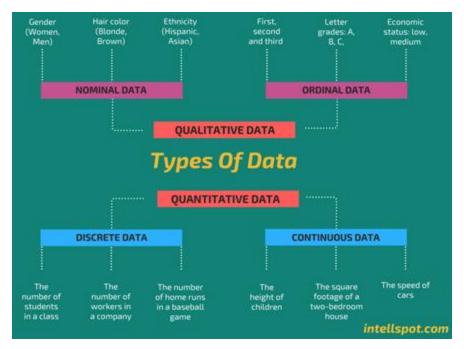


Categorical Plotting



Types of Data

Data come in many forms, each requiring different approaches & models



Qualitative or categorical: can partition values into classes

Quantitative: can perform arithmetic operations (e.g., addition, subtraction, ordering)

We often refer to different types of data as variables

Categorical Variables

Examples

- Blood Type: A, B, AB, or O
- Political Party: Democrat, Republican, etc.
- Word Identity: NP, VP, N, V, Adj, Adv, etc.
- Roll of a die: 1,2,3,4,5 or 6



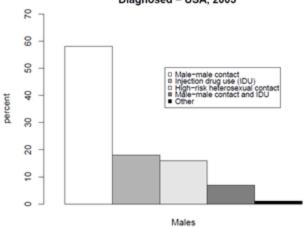
Numerical data can be categorical depending on context

<u>Conversion</u>: Quantitative data can be converted to categorical by defining ranges:

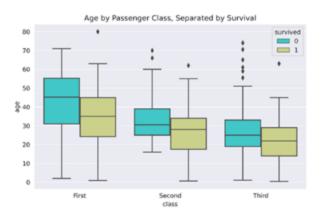
- Small [0, 10cm), Medium [10, 100cm), Large [100cm, 1m), XL [1m, -)
- Low [less than -100dB), Moderate [-100dB, -50dB), Loud [over -50dB)

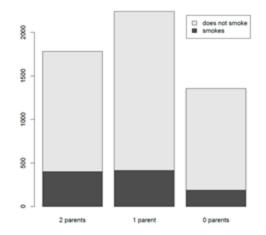
Visualizing Categorical Variables

Proportion of AIDS Cases by Sex and Transmission Category Diagnosed – USA, 2005



	student smokes	student does not smoke	total
2 parents smoke	400	1380	1780
1 parent smokes	416	1823	2239
0 parents smoke	188	1168	1356
total	1004	4371	5375





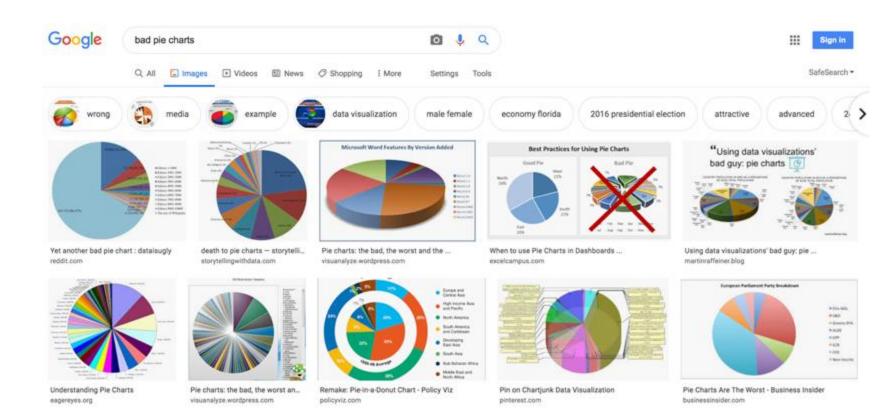
Pie Chart

Circular chart divided into sectors, illustrating relative magnitudes in frequencies or percentage.

In a pie chart, the area is proportional to the quantity it represents

Be careful with using pie charts:

- Maybe unsuitable if too many sectors are present
- 3d charts can distort the sizes of the sectors; using 2d is recommended



We perceive differences in height / length better than area...

plt.bar() error bars x = ['Nuclear', 'Hydro', 'Gas', 'Oil', 'Coal', 'Biofuel'] Energy output from various fuel sources energy = [5, 6, 15, 22, 24, 8]25 variance = [1, 2, 7, 4, 2, 3]Output (GJ) x_pos = [i for i, _ in enumerate(x)] plt.bar(x pos, energy, color='green', yerr=variance) Energy plt.xlabel("Energy Source") plt.ylabel("Energy Output (GJ)") plt.title("Energy output from various fuel sources") x-axis plt.xticks(x pos, x) ticks Nuclear Hydro Gas Oil Coal Biofuel Energy Source plt.show()

[Source: https://benalexkeen.com/bar-charts-in-matplotlib/]

Horizontal version

plt.barh()

```
x = ['Nuclear', 'Hydro', 'Gas', 'Oil', 'Coal', 'Biofuel']
                                                                                          Energy output from various fuel sources
energy = [5, 6, 15, 22, 24, 8]
                                                                                 Biofuel
variance = [1, 2, 7, 4, 2, 3]
                                                                                   Coal
x_pos = [i for i, _ in enumerate(x)]
                                                                             Energy Source
                                                                                    Oil
plt.barh(x pos, energy, color='green', xerr=variance)
                                                                                   Gas
plt.ylabel("Energy Source")
plt.xlabel("Energy Output (GJ)")
                                                                                 Hydro
plt.title("Energy output from various fuel sources")
                                                                                Nuclear
plt.yticks(x pos, x)
                                                                                                        10
                                                                                                                 15
                                                                                                                          20
                                                                                                                                    25
                                                                                                       Energy Output (GJ)
plt.show()
```

[Source: https://benalexkeen.com/bar-charts-in-matplotlib/]

Bar Chart

Multiple groups of bars...

```
import numpy as np
                                                                                           Scores by group and gender
N = 5
                                                                               35
men means = (20, 35, 30, 35, 27)
                                                                               30
women means = (25, 32, 34, 20, 25)
                                                                               25
ind = np.arange(N) //[1,2,3,4,5]
                                                                             Scores
width = 0.35
                       width of bar
plt.bar(ind, men_means, width, label='Men')
                                                                               15
plt.bar(ind + width, women_means, width,
                                                                               10
    label='Women')
                      add the offset here
                                                                                5 -
plt.ylabel('Scores')
plt.title('Scores by group and gender')
plt.xticks(ind + width / 2, ('G1', 'G2', 'G3', 'G4', 'G5'))
plt.legend(loc='best')
plt.show()
```

[Source: https://benalexkeen.com/bar-charts-in-matplotlib/]

Stacked Bar Chart

```
countries = ['USA', 'GB', 'China', 'Russia', 'Germany']
bronzes = np.array([38, 17, 26, 19, 15])
silvers = np.array([37, 23, 18, 18, 10])
golds = np.array([46, 27, 26, 19, 17])
ind = [x for x, in enumerate(countries)]
plt.bar(ind, golds, width=0.8, label='golds', color='gold', bottom=silvers+bronzes)
plt.bar(ind, silvers, width=0.8, label='silvers', color='silver', bottom=bronzes)
                                                                                          2012 Olympics Top Scorers
plt.bar(ind, bronzes, width=0.8, label='bronzes', color='#CD853F')
                                                                              120
                                                                                                                      golds
plt.xticks(ind, countries)
                                                                              100
                                                                                                                      bronzes
plt.ylabel("Medals")
                                                                               80
plt.xlabel("Countries")
                                                                            Medals
                                                                               60
plt.legend(loc="upper right")
plt.title("2012 Olympics Top Scorers")
                                                                               40
                                                                               20
plt.show()
                                                                                     USA
                                                                                             GB
                                                                                                     China
                                                                                                             Russia
                                                                                                                    Germany
```

[Source: https://benalexkeen.com/bar-charts-in-matplotlib/]

Countries

Aside: generating random data

Numpy: Python lib for scientific computing



It has general-purpose random number generator rand

```
import numpy as np

# Generate an array with 5 random numbers between 0 and 1
random_array_1d = np.random.rand(5)

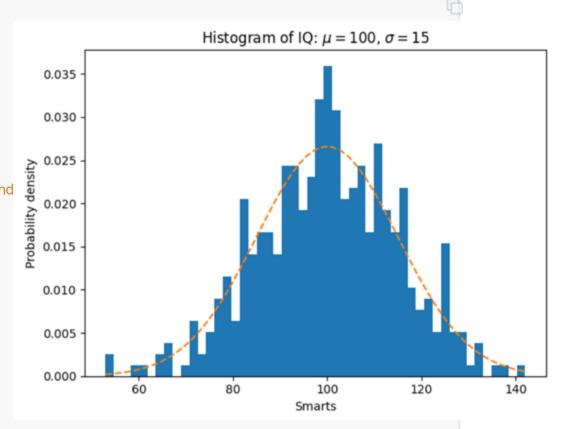
# Print the generated random array
print(random_array_1d)
```

```
[0.70620389 0.38344751 0.12382312 0.85396815 0.3684137 ] # This will vary each time
```

Histogram

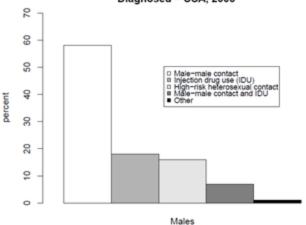
```
import numpy as np
import matplotlib.pyplot as plt
np.random.seed(19680801)
# example data
mu = 100 # mean of distribution
sigma = 15 # standard deviation of distribution
x = mu + sigma * np.random.randn(437)
num bins = 50
         Generate 437 random data; randn similar to rand
fig, ax = plt.subplots()
# the histogram of the data
n, bins, patches = ax.hist(x, num bins, density=True)
# add a 'best fit' line
y = ((1 / (np.sqrt(2 * np.pi) * sigma)) *
    np.exp(-0.5 * (1 / sigma * (bins - mu))**2))
ax.plot(bins, y, '--')
ax.set xlabel('Smarts')
ax.set ylabel('Probability density')
ax.set title(r'Histogram of IO: $\mu=100$, $\sigma=15$')
# Tweak spacing to prevent clipping of ylabel
fig.tight_layout()
```

plt.show()

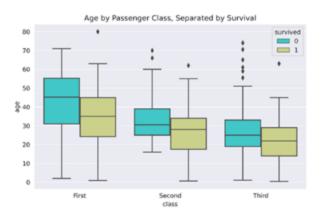


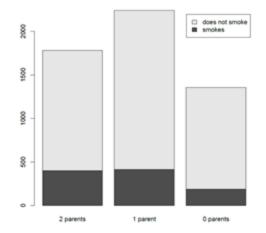
Visualizing Categorical Variables

Proportion of AIDS Cases by Sex and Transmission Category Diagnosed – USA, 2005



	student smokes	student does not smoke	total
2 parents smoke	400	1380	1780
1 parent smokes	416	1823	2239
0 parents smoke	188	1168	1356
total	1004	4371	5375





Two-Way Table

When there are two categorical variables: Also called <u>contingency table</u> or <u>cross tabulation table</u>...

Example We asked 5375 students and collected their smoking status and their parents' smoking status, and summarize it as:

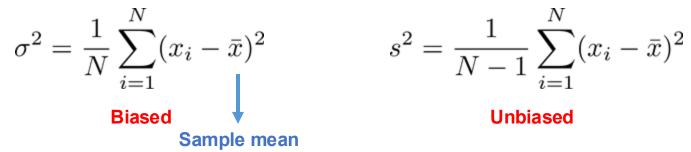
	student	student	
	smokes	does not smoke	total
2 parents smoke	400	1380	1780
1 parent smokes	416	1823	2239
0 parents smoke	188	1168	1356
total	1004	4371	5375

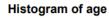
Q: is there any correlation between parents' and child's smoking statuses?

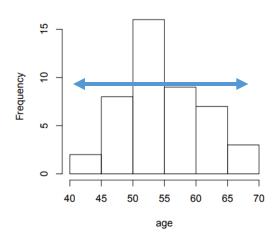
E.g. are students with 2 parents smoking more likely to smoke (compared with general students)?

Measuring Spread: sample variance

Another way to measure the spread is the sample variance,







Sample Variance

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^{N} (x_i - \bar{x})^2$$

Example calculate the sample variance of sample 4, 9, 10, 6, 6

Sample mean:
$$\bar{x} = \frac{4+9+10+6+6}{5} = 7$$

5 terms in the summation:

5 terms in the summation.
$$(4-7)^2, (9-7)^2, (10-7)^2, (6-7)^2, (6-7)^2$$
 9, 4, 9, 1, 1
$$\sigma^2 = \frac{1}{5}(9+4+9+1+1) = 4.8$$

Sample variance

When is the variance of a sample zero?

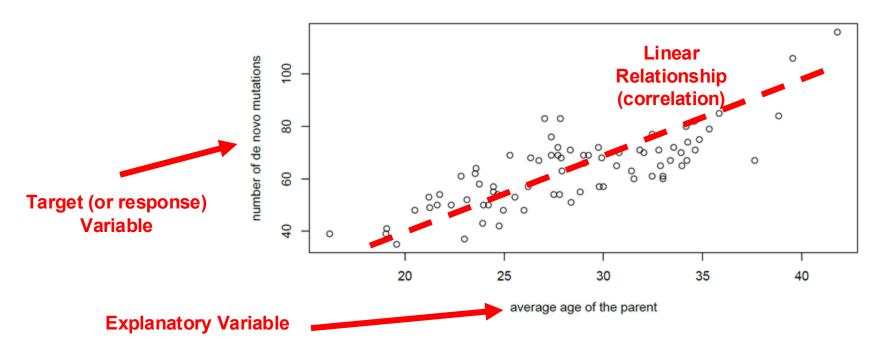
$$\sigma^2 = \frac{1}{N} \sum_{i=1}^{N} (x_i - \bar{x})^2$$

Variance of a sample is zero if all x_i's are identical, e.g.
 5, 5, .., 5

- Variance measures the degree of "fluctuations" in the data
- The square root of variance, σ , is called the *standard* deviation

Scatterplot

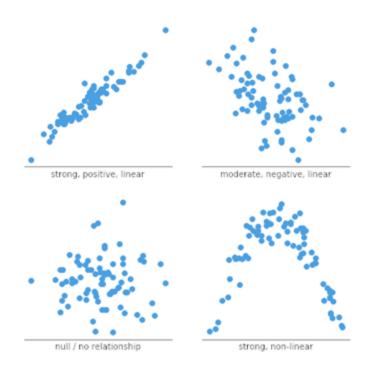
Compares relationship between two quantitative variables...



Useful for many prediction tasks: e.g. house price prediction, salary prediction, stock price prediction, etc.

Scatterplot

Compares relationship between two quantitative variables...



Relationship can also be:

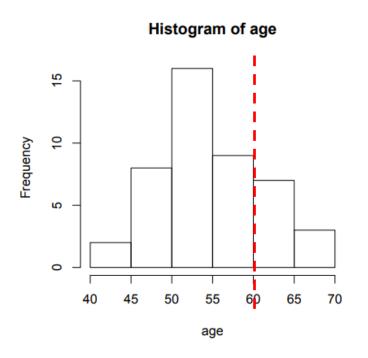
- Nonlinear (e.g. "curvy")
- Clustered or grouped

Scatterplot + Histogram

```
import numpy as np
import matplotlib.pyplot as plt
# Fixing random state for reproducibility
np.random.seed(19680801)
# some random data
x = np.random.randn(1000)
y = np.random.randn(1000)
def scatter_hist(x, y, ax, ax histx, ax histy):
   # no Labels
   ax_histx.tick_params(axis="x", labelbottom=False)
   ax_histy.tick_params(axis="y", labelleft=False)
   # the scatter plot:
   ax.scatter(x, y)
   # now determine nice limits by hand:
   binwidth = 0.25
   xymax = max(np.max(np.abs(x)), np.max(np.abs(y)))
   lim = (int(xymax/binwidth) + 1) / binwidth
                                                                                   Full Code:
                                                         https://matplotlib.org/stable/gallery/lines_bars_a
   bins = np.arange(-lim, lim + binwidth, binwidth)
   ax_histx.hist(x, bins=bins)
                                                                      nd markers/scatter hist.html
   ax_histy.hist(y, bins=bins, orientation='horizontal')
```

Percentile / Quartile

Question Is 60yrs old for a US president? Why or why not?



The number of presidents <60: 33 Total number of presidents: 44

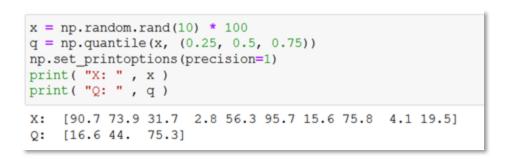
About 75% of presidents younger than 60yrs old => 60yrs old = 0.75 Quantile or 75th Percentile

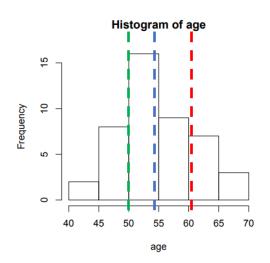
Measuring Spread

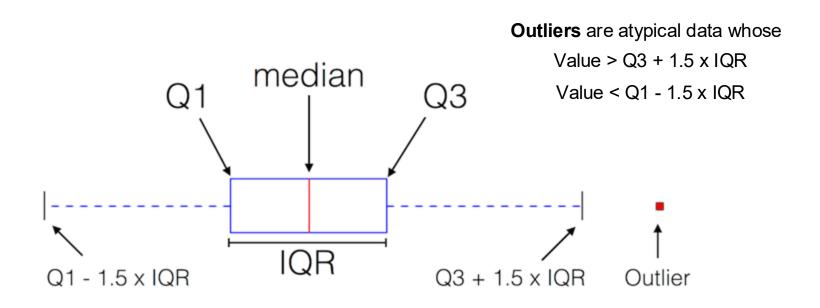
Quartile divide data into 4 equally-sized bins,

- 1st Quartile: Lowest 25% of data
- 2nd Quartile : Median (lowest 50% of data)
- 3rd Quartile: 75% of data is below 3rd quartile
- 4th Quartile: The maximum value

Compute using np.quantile():







Interquartile-Range (IQR) Measures interval containing 50% of data

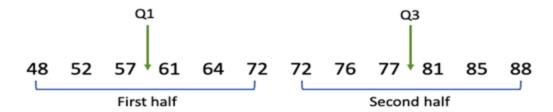
$$IQR = Q3 - Q1$$

Region of typical data

 $Q3 = \frac{77 + 81}{2} = 79$

Median





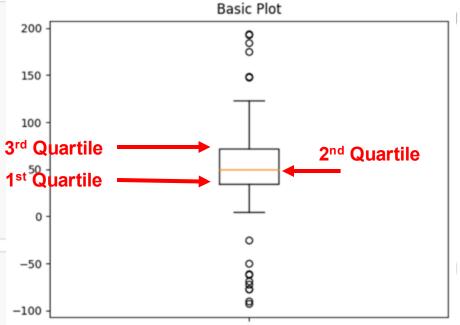
$$Q1 = \frac{57 + 61}{2} = 59$$

$$IQR = Q3 - Q1$$

 $IQR = 79 - 59 = 20$

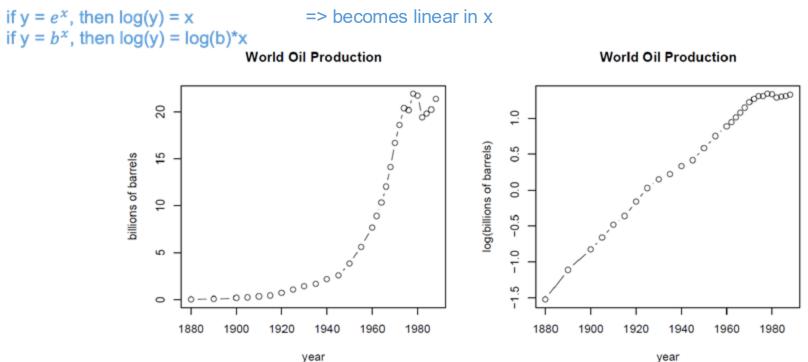
Box Plot

```
import numpy as np
import matplotlib.pyplot as plt
# Fixing random state for reproducibility
np.random.seed(19680801)
# fake up some data
spread = np.random.rand(50) * 100
center = np.ones(25) * 50
flier_high = np.random.rand(10) * 100 + 100
flier_low = np.random.rand(10) * -100
data = np.concatenate((spread, center, flier_high, flier_low))
fig1, ax1 = plt.subplots()
ax1.set_title('Basic Plot')
ax1.boxplot(data)
```



Logarithm Scale

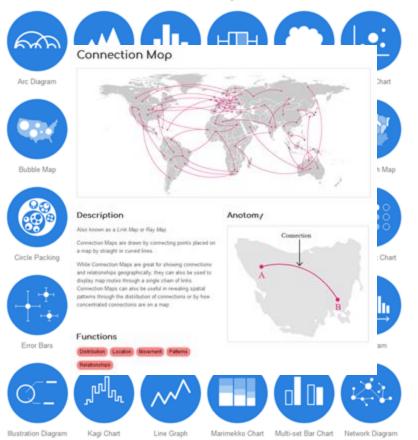
Changing limits and base of y-scale highlights different aspects...



...log-scale emphasizes relative changes in smaller quantities

More Visualization Resources

datavizcatalogue.com





matplotlib.org



scikit-learn.org