

$$dE_z = \frac{1}{4\pi\epsilon_0} \cdot \frac{dQ}{r} \cos\phi$$

$$= \int_0^1 \int_0^{2\pi} \frac{1}{4\pi\epsilon_0} \cdot \frac{dQ}{r} \cos\phi$$

$$= \int_0^1 \int_0^{2\pi} \frac{1}{4\pi\epsilon_0} * \frac{\rho_s d\rho d\phi}{\rho^2 + z^2} * \frac{z^2}{\sqrt{\rho^2 + z^2}}$$

$$= \frac{\rho_s z}{4\pi\epsilon_0} \int_0^1 \int_0^{2\pi} \frac{\rho d\rho d\phi}{(\rho^2 + z^2)^{3/2}}$$

$$= \frac{\rho_s z}{4\pi\epsilon_0} \left[ 2\pi \left( \frac{1}{2} * \frac{-2}{\sqrt{\rho^2 + z^2}} \right) \right]_0^1$$

$$= 3.309 \times 10^4 \text{ V/m } Q_z$$