

$$R_1 = \underset{x}{a} + \underset{y}{2a} + \underset{z}{3a} \quad , \quad R_2 = \underset{x}{3a} + \underset{y}{2a} + \underset{z}{a}$$

$$a) R_1 \cdot R_2 = 1 \cdot 3 + 2 \cdot 2 + 3 \cdot 1 = 10$$

$$\begin{aligned} b) \text{proj}_{R_2} R_1 &= \frac{R_1 \cdot R_2}{R_2 \cdot R_2} \cdot R_2 \\ &= \frac{10}{3 \cdot 3 + 2 \cdot 2 + 1 \cdot 1} \cdot R_2 = \frac{10}{14} \cdot (3a_x + 2a_y + a_z) \\ &= \frac{30}{14} a_x + \frac{20}{14} a_y + \frac{10}{14} a_z \\ &= \frac{15}{7} a_x + \frac{10}{7} a_y + \frac{5}{7} a_z \\ &= 2.1429 a_x + 1.4286 a_y + 0.7143 a_z \end{aligned}$$

$$c) R_1 \cdot R_2 = |R_1| |R_2| \cos \theta$$

$$\cos \theta = \frac{10}{\sqrt{1^2 + 2^2 + 3^2} \cdot \sqrt{3^2 + 2^2 + 1^2}}$$

$$\cos \theta = \frac{10}{14} = \frac{5}{7}$$

$$\theta = 44.415^\circ = 0.7752 \text{ rad}$$