

# 【LeetCode】代码模板，刷题必会

原创

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本文的目的是收集一些典型的题目，记住其写法，理解其思想，即可做到一通百通。欢迎大家提出宝贵意见！

## 二分查找

最明显的题目就是34. Find First and Last Position of Element in Sorted Array

花花酱的二分查找专题视频：[https://www.youtube.com/watch?v=v57INF2mb\\_s](https://www.youtube.com/watch?v=v57INF2mb_s)

模板：

区间定义： $[l, r)$  左闭右开

其中f(m)函数代表找到了满足条件的情况，有这个条件的判断就返回对应的位置，如果没有这个条件的判断就是lower\_bound和higher\_bound.

```

1  def binary_search(l, r):
2      while l < r:
3          m = l + (r - l) // 2
4          if f(m): # 判断找有没有, optional
5              return m
6          if g(m):
7              r = m # new range [l, m)
8          else:
9              l = m + 1 # new range [m+1, r)
10     return l # or not found

```

**lower bound:** find index of i, such that  $A[i] \geq x$

```

1  def lower_bound(self, nums, target):
2      # find in range [left, right)
3      left, right = 0, len(nums)
4      while left < right:
5          mid = left + (right - left) // 2
6          if nums[mid] < target:
7              left = mid + 1
8          else:
9              right = mid
10     return left

```

**upper bound:** find index of i, such that  $A[i] > x$

```

1  def higher_bound(self, nums, target):
2      # find in range [left, right)
3      left, right = 0, len(nums)
4      while left < right:
5          mid = left + (right - left) // 2
6          if nums[mid] <= target:
7              left = mid + 1
8          else:
9              right = mid
10     return left

```

比如，题目69. Sqrt(x)。

```

1  class Solution(object):
2      def mySqrt(self, x):
3          """
4          :type x: int
5          :rtype: int
6          """
7          left, right = 0, x + 1
8          # [left, right)
9          while left < right:
10             mid = left + (right - left) // 2
11             if mid ** 2 == x:
12                 return mid
13             if mid ** 2 < x:
14                 left = mid + 1
15             else:
16                 right = mid
17     return left - 1

```

## 排序的写法

C++的排序方法，使用sort并且重写comparator，如果需要使用外部变量，需要在中括号中放入&。

题目451. Sort Characters By Frequency。

```

1  class Solution {
2  public:
3      string frequencySort(string s) {
4          unordered_map<char, int> m;
5          for (char c : s) ++m[c];
6          sort(s.begin(), s.end(), [&](char& a, char& b){
7              return m[a] > m[b] || (m[a] == m[b] && a < b);
8          });
9          return s;
10     }
11 };

```

## BFS的写法

下面的这个写法是在一个邻接矩阵中找出离某一个点距离是k的点。

来自文章：【LeetCode】863. All Nodes Distance K in Binary Tree 解题报告 (Python)

```

1  # BFS
2  bfs = [target.val]
3  visited = set([target.val])
4  for k in range(K):
5      bfs = [y for x in bfs for y in conn[x] if y not in visited]
6      visited |= set(bfs)
7  return bfs

```

## 127. Word Ladder

在BFS中保存已走过的步，并把已经走的合法路径删除掉。

```

1  class Solution(object):
2      def ladderLength(self, beginWord, endWord, wordList):
3          """
4              :type beginWord: str
5              :type endWord: str
6              :type wordList: List[str]
7              :rtype: int
8          """
9          wordset = set(wordList)
10         bfs = collections.deque()
11         bfs.append((beginWord, 1))
12         while bfs:
13             word, length = bfs.popleft()
14             if word == endWord:
15                 return length
16             for i in range(len(word)):
17                 for c in "abcdefghijklmnopqrstuvwxyz":
18                     newWord = word[:i] + c + word[i + 1:]
19                     if newWord in wordset and newWord != word:
20                         wordset.remove(newWord)
21                         bfs.append((newWord, length + 1))
22         return 0

```

## 778. Swim in Rising Water

使用优先级队列来优先走比较矮的路，最后保存最高的那个格子的高度。

```

1 class Solution(object):
2     def swimInWater(self, grid):
3         """
4         :type grid: List[List[int]]
5         :rtype: int
6         """
7         n = len(grid)
8         visited, pq = set((0, 0)), [(grid[0][0], 0, 0)]
9         res = 0
10        while pq:
11            T, i, j = heapq.heappop(pq)
12            res = max(res, T)
13            directions = [(0, 1), (0, -1), (-1, 0), (1, 0)]
14            if i == j == n - 1:
15                break
16            for dir in directions:
17                x, y = i + dir[0], j + dir[1]
18                if x < 0 or x >= n or y < 0 or y >= n or (x, y) in visited:
19                    continue
20                heapq.heappush(pq, (grid[x][y], x, y))
21                visited.add((x, y))
22        return res

```

#### 847. Shortest Path Visiting All Nodes

需要找出某顶点到其他顶点的最短路径。出发顶点不是确定的，每个顶点有可能访问多次。使用N位bit代表访问过的顶点的状态。如果到达了最终状态，那么现在步数就是所求。这个题把所有的节点都放入了起始队列中，相当于每次都是所有的顶点向前走一步。

```

1 class Solution(object):
2     def shortestPathLength(self, graph):
3         """
4         :type graph: List[List[int]]
5         :rtype: int
6         """
7         N = len(graph)
8         que = collections.deque()
9         step = 0
10        goal = (1 << N) - 1
11        visited = [[0 for j in range(1 << N)] for i in range(N)]
12        for i in range(N):
13            que.append((i, 1 << i))
14        while que:
15            s = len(que)
16            for i in range(s):
17                node, state = que.popleft()
18                if state == goal:
19                    return step
20                if visited[node][state]:
21                    continue
22                visited[node][state] = 1
23                for nextNode in graph[node]:
24                    que.append((nextNode, state | (1 << nextNode)))
25            step += 1
26        return step

```

#### 429. N-ary Tree Level Order Traversal多叉树的层次遍历，这个BFS写法我觉得很经典。适合记忆。

```

1 """
2 # Definition for a Node.
3 class Node(object):
4     def __init__(self, val, children):
5         self.val = val
6         self.children = children

```

```

6  """
7  class Solution(object):
8      def levelOrder(self, root):
9          """
10         :type root: Node
11         :rtype: List[List[int]]
12         """
13         res = []
14         que = collections.deque()
15         que.append(root)
16         while que:
17             level = []
18             size = len(que)
19             for _ in range(size):
20                 node = que.popleft()
21                 if not node:
22                     continue
23                 level.append(node.val)
24                 for child in node.children:
25                     que.append(child)
26             if level:
27                 res.append(level)
28         return res

```

## DFS的写法

329. Longest Increasing Path in a Matrix

417. Pacific Atlantic Water Flow

778. Swim in Rising Water

二分查找+DFS

```

1  class Solution(object):
2      def swimInWater(self, grid):
3          """
4          :type grid: List[List[int]]
5          :rtype: int
6          """
7          n = len(grid)
8          left, right = 0, n * n - 1
9          while left <= right:
10             mid = left + (right - left) / 2
11             if self.dfs([[False] * n for _ in range(n)], grid, mid, n, 0, 0):
12                 right = mid - 1
13             else:
14                 left = mid + 1
15         return left
16
17     def dfs(self, visited, grid, mid, n, i, j):
18         visited[i][j] = True
19         if i == n - 1 and j == n - 1:
20             return True
21         directions = [(0, 1), (0, -1), (-1, 0), (1, 0)]
22         for dir in directions:
23             x, y = i + dir[0], j + dir[1]
24             if x < 0 or x >= n or y < 0 or y >= n or visited[x][y] or max(mid, grid[i][j]) != max(mid, grid[x][y]):
25                 continue
26             if self.dfs(visited, grid, mid, n, x, y):
27                 return True
28         return False

```

## 回溯法

下面这个题使用了回溯法，但是写的不够简单干练，遇到更好的解法的时候，要把这个题进行更新。

这个回溯思想，先去添加一个新的状态，看在这个状态的基础上，能不能找结果，如果找不到结果的话，那么就回退，即把这个结果和访问的记录给去掉。这个题使用了return True的方法让我们知道已经找出了结果，所以不用再递归了。

### 753. Cracking the Safe

```

1  class Solution(object):
2      def crackSafe(self, n, k):
3          """
4              :type n: int
5              :type k: int
6              :rtype: str
7          """
8          res = ["0"] * n
9          size = k ** n
10         visited = set()
11         visited.add("".join(res))
12         if self.dfs(res, visited, size, n, k):
13             return "".join(res)
14         return ""
15
16     def dfs(self, res, visited, size, n, k):
17         if len(visited) == size:
18             return True
19         node = "".join(res[len(res) - n + 1:])
20         for i in range(k):
21             node = node + str(i)
22             if node not in visited:
23                 res.append(str(i))
24                 visited.add(node)
25                 if self.dfs(res, visited, size, n, k):
26                     return True
27                 res.pop()
28                 visited.remove(node)
29                 node = node[:-1]
```

### 312. Burst Balloons

```

1  class Solution(object):
2      def maxCoins(self, nums):
3          """
4              :type nums: List[int]
5              :rtype: int
6          """
7          n = len(nums)
8          nums.insert(0, 1)
9          nums.append(1)
10         c = [[0] * (n + 2) for _ in range(n + 2)]
11         return self.dfs(nums, c, 1, n)
12
13     def dfs(self, nums, c, i, j):
14         if i > j: return 0
15         if c[i][j] > 0: return c[i][j]
16         if i == j: return nums[i - 1] * nums[i] * nums[i + 1]
17         res = 0
18         for k in range(i, j + 1):
19             res = max(res, self.dfs(nums, c, i, k - 1) + nums[i - 1] * nums[k] * nums[j + 1] + self.dfs(nums, c, k + 1, j))
20         c[i][j] = res
21         return c[i][j]
```

```

1  class Solution {
2  public:
3      int countArrangement(int N) {
4          int res = 0;
5          vector<int> visited(N + 1, 0);
6          helper(N, visited, 1, res);
7          return res;
8      }
9  private:
10     void helper(int N, vector<int>& visited, int pos, int& res) {
11         if (pos > N) {
12             res++;
13             return;
14         }
15         for (int i = 1; i <= N; i++) {
16             if (visited[i] == 0 && (i % pos == 0 || pos % i == 0)) {
17                 visited[i] = 1;
18                 helper(N, visited, pos + 1, res);
19                 visited[i] = 0;
20             }
21         }
22     }
23 };

```

如果需要保存路径的回溯法：

```

1  class Solution {
2  public:
3      vector<vector<int>> permute(vector<int>& nums) {
4          const int N = nums.size();
5          vector<vector<int>> res;
6          vector<int> path;
7          vector<int> visited(N, 0);
8          dfs(nums, 0, visited, res, path);
9          return res;
10     }
11 private:
12     void dfs(vector<int>& nums, int pos, vector<int>& visited, vector<vector<int>>& res, vector<int>& path) {
13         const int N = nums.size();
14         if (pos == N) {
15             res.push_back(path);
16             return;
17         }
18         for (int i = 0; i < N; i++) {
19             if (!visited[i]) {
20                 visited[i] = 1;
21                 path.push_back(nums[i]);
22                 dfs(nums, pos + 1, visited, res, path);
23                 path.pop_back();
24                 visited[i] = 0;
25             }
26         }
27     }
28 };

```

## 树

### 递归

617. Merge Two Binary Trees把两个树重叠，重叠部分求和，不重叠部分是两个树不空的节点。

```

1  class Solution:
2      def mergeTrees(self, t1, t2):
3          if not t2:
4              return t1
5          if not t1:
6              return t2
7          newT = TreeNode(t1.val + t2.val)
8          newT.left = self.mergeTrees(t1.left, t2.left)
9          newT.right = self.mergeTrees(t1.right, t2.right)
10         return newT

```

## 迭代

### 226. Invert Binary Tree

```

1  # Definition for a binary tree node.
2  # class TreeNode(object):
3  #     def __init__(self, x):
4  #         self.val = x
5  #         self.left = None
6  #         self.right = None
7
8  class Solution(object):
9      def invertTree(self, root):
10         """
11         :type root: TreeNode
12         :rtype: TreeNode
13         """
14         stack = []
15         stack.append(root)
16         while stack:
17             node = stack.pop()
18             if not node:
19                 continue
20             node.left, node.right = node.right, node.left
21             stack.append(node.left)
22             stack.append(node.right)
23         return root

```

## 前序遍历

### 144. Binary Tree Preorder Traversal

迭代写法:

```

1  # Definition for a binary tree node.
2  # class TreeNode(object):
3  #     def __init__(self, x):
4  #         self.val = x
5  #         self.left = None
6  #         self.right = None
7
8  class Solution(object):
9      def preorderTraversal(self, root):
10         """
11         :type root: TreeNode
12         :rtype: List[int]
13         """
14         if not root: return []
15         res = []
16         stack = []
17         stack.append(root)
18         while stack:

```



```

18         node = stack.pop()
19         if not node:
20             continue
21         res.append(node.val)
22         stack.append(node.right)
23         stack.append(node.left)
24     return res
25
26

```

## 中序遍历

### 94. Binary Tree Inorder Traversal

迭代写法:

```

1  # Definition for a binary tree node.
2  # class TreeNode(object):
3  #     def __init__(self, x):
4  #         self.val = x
5  #         self.left = None
6  #         self.right = None
7
8  class Solution(object):
9      def inorderTraversal(self, root):
10         """
11         :type root: TreeNode
12         :rtype: List[int]
13         """
14         stack = []
15         answer = []
16         while True:
17             while root:
18                 stack.append(root)
19                 root = root.left
20             if not stack:
21                 return answer
22             root = stack.pop()
23             answer.append(root.val)
24             root = root.right

```

## 后序遍历

### 145. Binary Tree Postorder Traversal

迭代写法如下:

```

1  /**
2   * Definition for a binary tree node.
3   * struct TreeNode {
4   *     int val;
5   *     TreeNode *left;
6   *     TreeNode *right;
7   *     TreeNode(int x) : val(x), left(NULL), right(NULL) {}
8   * };
9   */
10 class Solution {
11 public:
12     vector<int> postorderTraversal(TreeNode* root) {
13         vector<int> res;
14         if (!root) return res;
15         stack<TreeNode*> st;
16         st.push(root);
17         while (!st.empty()) {
18             TreeNode* node = st.top(); st.pop();
19             if (!node) continue;

```

```

18         res.push_back(node->val);
19         st.push(node->left);
20         st.push(node->right);
21     }
22     reverse(res.begin(), res.end());
23     return res;
24 }
25 };
26

```

## 构建完全二叉树

完全二叉树是每一层都满的，因此找出要插入节点的父亲节点是很简单的。如果用数组`tree`保存着所有节点的层次遍历，那么新节点的父亲节点就是`tree[(N - 1)/2]`，`N`是未插入该节点前的树的元素个数。

构建树的时候使用层次遍历，也就是BFS把所有的节点放入到`tree`里。插入的时候直接计算出新节点的父亲节点。获取`root`就是数组中的第0个节点。

### 919. Complete Binary Tree Inserter

```

1  # Definition for a binary tree node.
2  # class TreeNode(object):
3  #     def __init__(self, x):
4  #         self.val = x
5  #         self.left = None
6  #         self.right = None
7
8  class CBTInserter(object):
9
10     def __init__(self, root):
11         """
12         :type root: TreeNode
13         """
14         self.tree = list()
15         queue = collections.deque()
16         queue.append(root)
17         while queue:
18             node = queue.popleft()
19             self.tree.append(node)
20             if node.left:
21                 queue.append(node.left)
22             if node.right:
23                 queue.append(node.right)
24
25     def insert(self, v):
26         """
27         :type v: int
28         :rtype: int
29         """
30         _len = len(self.tree)
31         father = self.tree[( _len - 1) / 2]
32         node = TreeNode(v)
33         if not father.left:
34             father.left = node
35         else:
36             father.right = node
37         self.tree.append(node)
38         return father.val
39
40     def get_root(self):
41         """
42         :rtype: TreeNode
43         """
44         return self.tree[0]
45

```

```

46
47 # Your CBTInserter object will be instantiated and called as such:
48 # obj = CBTInserter(root)
49 # param_1 = obj.insert(v)
50 # param_2 = obj.get_root()
51

```

## 并查集

不包含rank的话，代码很简短，应该背会。

### 721. Accounts Merge

<https://leetcode.com/articles/accounts-merge/>

```

1 class DSU:
2     def __init__(self):
3         self.par = range(10001)
4
5     def find(self, x):
6         if x != self.par[x]:
7             self.par[x] = self.find(self.par[x])
8         return self.par[x]
9
10    def union(self, x, y):
11        self.par[self.find(x)] = self.find(y)
12
13    def same(self, x, y):
14        return self.find(x) == self.find(y)

```

C++版本如下：

```

1 vector<int> map_; //i的parent, 默认是i
2 int f(int a) {
3     if (map_[a] == a)
4         return a;
5     return f(map_[a]);
6 }
7 void u(int a, int b) {
8     int pa = f(a);
9     int pb = f(b);
10    if (pa == pb)
11        return;
12    map_[pa] = pb;
13 }

```

包含rank的，这里的rank表示树的高度：

### 684. Redundant Connection

```

1 class DSU(object):
2     def __init__(self):
3         self.par = range(1001)
4         self.rnk = [0] * 1001
5
6     def find(self, x):
7         if self.par[x] != x:
8             self.par[x] = self.find(self.par[x])
9         return self.par[x]
10
11    def union(self, x, y):
12        xr, yr = self.find(x), self.find(y)
13        if xr == yr:

```

```

14         return False
15     elif self.rnk[xr] < self.rnk[yr]:
16         self.par[xr] = yr
17     elif self.rnk[xr] > self.rnk[yr]:
18         self.par[yr] = xr
19     else:
20         self.par[yr] = xr
21         self.rnk[xr] += 1
22     return True

```

另外一种rank方法是，保存树中节点的个数。

547. Friend Circles, 代码如下：

```

1  class Solution(object):
2      def findCircleNum(self, M):
3          """
4          :type M: List[List[int]]
5          :rtype: int
6          """
7          dsu = DSU()
8          N = len(M)
9          for i in range(N):
10             for j in range(i, N):
11                 if M[i][j]:
12                     dsu.u(i, j)
13             res = 0
14             for i in range(N):
15                 if dsu.f(i) == i:
16                     res += 1
17             return res
18
19 class DSU(object):
20     def __init__(self):
21         self.d = range(201)
22         self.r = [0] * 201
23
24     def f(self, a):
25         return a if a == self.d[a] else self.f(self.d[a])
26
27     def u(self, a, b):
28         pa = self.f(a)
29         pb = self.f(b)
30         if (pa == pb):
31             return
32         if self.r[pa] < self.r[pb]:
33             self.d[pa] = pb
34             self.r[pb] += self.r[pa]
35         else:
36             self.d[pb] = pa
37             self.r[pa] += self.r[pb]

```

## 前缀树

前缀树的题目可以使用字典解决，代码还是需要背一下的，C++版本的前缀树如下：

208. Implement Trie (Prefix Tree)这个题是纯考Trie的。参考代码如下：

```

1  class TrieNode {
2  public:
3      vector<TrieNode*> child;
4      bool isWord;
5

```

```

6     TrieNode() : isword(false), child(26, nullptr) {
7     }
8     ~TrieNode() {
9         for (auto& c : child)
10             delete c;
11     }
12 };
13
14 class Trie {
15 public:
16     /** Initialize your data structure here. */
17     Trie() {
18         root = new TrieNode();
19     }
20
21     /** Inserts a word into the trie. */
22     void insert(string word) {
23         TrieNode* p = root;
24         for (char a : word) {
25             int i = a - 'a';
26             if (!p->child[i])
27                 p->child[i] = new TrieNode();
28             p = p->child[i];
29         }
30         p->isWord = true;
31     }
32
33     /** Returns if the word is in the trie. */
34     bool search(string word) {
35         TrieNode* p = root;
36         for (char a : word) {
37             int i = a - 'a';
38             if (!p->child[i])
39                 return false;
40             p = p->child[i];
41         }
42         return p->isWord;
43     }
44
45     /** Returns if there is any word in the trie that starts with the given prefix. */
46     bool startsWith(string prefix) {
47         TrieNode* p = root;
48         for (char a : prefix) {
49             int i = a - 'a';
50             if (!p->child[i])
51                 return false;
52             p = p->child[i];
53         }
54         return true;
55     }
56 private:
57     TrieNode* root;
58 };
59
60 /**
61  * Your Trie object will be instantiated and called as such:
62  * Trie obj = new Trie();
63  * obj.insert(word);
64  * bool param_2 = obj.search(word);
65  * bool param_3 = obj.startsWith(prefix);
66  */

```

## 677. Map Sum Pairs

```

1  class MapSum {
2  public:
3      /** Initialize your data structure here. */
4      MapSum() {}
5
6      void insert(string key, int val) {
7          int inc = val - vals_[key];
8          Trie* p = &root;
9          for (const char c : key) {
10             if (!p->children[c])
11                 p->children[c] = new Trie();
12             p->children[c]->sum += inc;
13             p = p->children[c];
14         }
15         vals_[key] = val;
16     }
17
18     int sum(string prefix) {
19         Trie* p = &root;
20         for (const char c : prefix) {
21             if (!p->children[c])
22                 return 0;
23             p = p->children[c];
24         }
25         return p->sum;
26     }
27 private:
28     struct Trie {
29         Trie():children(128, nullptr), sum(0){}
30         ~Trie(){
31             for (auto child : children)
32                 if (child) delete child;
33             children.clear();
34         }
35         vector<Trie*> children;
36         int sum;
37     };
38
39     Trie root;
40     unordered_map<string, int> vals_;
41 };

```

## 图遍历

743. Network Delay Time这个题很详细。

## Dijkstra算法

时间复杂度是 $O(N^2 + E)$ ，空间复杂度是 $O(N+E)$ 。

```

1  class Solution:
2      def networkDelayTime(self, times, N, K):
3          """
4              :type times: List[List[int]]
5              :type N: int
6              :type K: int
7              :rtype: int
8              """
9          K -= 1
10         nodes = collections.defaultdict(list)
11         for u, v, w in times:
12             nodes[u - 1].append((v - 1, w))
13         dist = [float('inf')] * N

```

```

14         dist[K] = 0
15         done = set()
16         for _ in range(N):
17             smallest = min((d, i) for (i, d) in enumerate(dist) if i not in done)[1]
18             for v, w in nodes[smallest]:
19                 if v not in done and dist[smallest] + w < dist[v]:
20                     dist[v] = dist[smallest] + w
21             done.add(smallest)
22         return -1 if float('inf') in dist else max(dist)

```

## Floyd-Warshall算法

时间复杂度 $O(n^3)$ ，空间复杂度 $O(n^2)$ 。

```

1  class Solution:
2      def networkDelayTime(self, times, N, K):
3          """
4          :type times: List[List[int]]
5          :type N: int
6          :type K: int
7          :rtype: int
8          """
9          d = [[float('inf')] * N for _ in range(N)]
10         for time in times:
11             u, v, w = time[0] - 1, time[1] - 1, time[2]
12             d[u][v] = w
13         for i in range(N):
14             d[i][i] = 0
15         for k in range(N):
16             for i in range(N):
17                 for j in range(N):
18                     d[i][j] = min(d[i][j], d[i][k] + d[k][j])
19         return -1 if float('inf') in d[K - 1] else max(d[K - 1])

```

## Bellman-Ford算法

时间复杂度 $O(ne)$ ，空间复杂度 $O(n)$

```

1  class Solution:
2      def networkDelayTime(self, times, N, K):
3          """
4          :type times: List[List[int]]
5          :type N: int
6          :type K: int
7          :rtype: int
8          """
9          dist = [float('inf')] * N
10         dist[K - 1] = 0
11         for i in range(N):
12             for time in times:
13                 u = time[0] - 1
14                 v = time[1] - 1
15                 w = time[2]
16                 dist[v] = min(dist[v], dist[u] + w)
17         return -1 if float('inf') in dist else max(dist)

```

## 最小生成树

1135. Connecting Cities With Minimum Cost

## Kruskal算法

```

1  class Solution {
2  public:
3      static bool cmp(vector<int> & a,vector<int> & b){
4          return a[2] < b[2];
5      }
6
7      int find(vector<int> & f,int x){
8          while(x != f[x]){
9              x = f[x];
10         }
11         return x;
12     }
13
14     bool uni(vector<int> & f,int x,int y){
15         int x1 = find(f,x);
16         int y1 = find(f,y);
17         f[x1] = y1;
18
19         return true;
20     }
21
22     int minimumCost(int N, vector<vector<int>>& conections) {
23         int ans = 0;
24         int count = 0;
25         vector<int> father(N+1,0);
26
27         sort(conections.begin(),conections.end(),cmp);
28         for(int i = 0;i <= N; ++i){
29             father[i] = i;
30         }
31
32         for(auto conect : conections){
33             if(find(father,conect[0]) != find(father,conect[1])){
34                 count++;
35                 ans += conect[2];
36                 uni(father,conect[0],conect[1]);
37                 if(count == N-1){
38                     return ans;
39                 }
40             }
41         }
42
43         return -1;
44     }
45 };

```

## Prim算法

```

1  struct cmp {
2      bool operator () (const vector<int> &a, const vector<int> &b) {
3          return a[2] > b[2];
4      }
5  };
6
7  class Solution {
8  public:
9      int minimumCost(int N, vector<vector<int>>& conections) {
10         int ans = 0;
11         int selected = 0;
12         vector<vector<pair<int,int>>> edgs(N+1,vector<pair<int,int>>());
13         priority_queue<vector<int>,vector<vector<int>>,cmp> pq;
14         vector<bool> visit(N+1,false);
15     }

```



```

16
17     /*initial*/
18     for(auto re : conections){
19         eds[re[0]].push_back(make_pair(re[1],re[2]));
20         eds[re[1]].push_back(make_pair(re[0],re[2]));
21     }
22
23     if(eds[1].size() == 0){
24         return -1;
25     }
26
27     /*kruskal*/
28     selected = 1;
29     visit[1] = true;
30     for(int i = 0;i < eds[1].size(); ++i){
31         pq.push(vector<int>({1,eds[1][i].first,eds[1][i].second}));
32     }
33
34     while(!pq.empty()){
35         vector<int> curr = pq.top();
36         pq.pop();
37
38         if(!visit[curr[1]]){
39             visit[curr[1]] = true;
40             ans += curr[2];
41             for(auto e : eds[curr[1]]){
42                 pq.push(vector<int>({curr[1],e.first,e.second}));
43             }
44             selected++;
45             if(selected == N){
46                 return ans;
47             }
48         }
49     }
50
51     return -1;
52 }
};

```

## 拓扑排序

BFS方式:

```

1  class Solution(object):
2      def canFinish(self, N, prerequisites):
3          """
4              :type N,: int
5              :type prerequisites: List[List[int]]
6              :rtype: bool
7              """
8          graph = collections.defaultdict(list)
9          indegrees = collections.defaultdict(int)
10         for u, v in prerequisites:
11             graph[v].append(u)
12             indegrees[u] += 1
13         for i in range(N):
14             zeroDegree = False
15             for j in range(N):
16                 if indegrees[j] == 0:
17                     zeroDegree = True
18                     break
19             if not zeroDegree: return False
20             indegrees[j] = -1
21             for node in graph[j]:

```

```

21         indegrees[node] -= 1
22     return True
23

```

DFS方式:

```

1  class Solution(object):
2      def canFinish(self, N, prerequisites):
3          """
4              :type N: int
5              :type prerequisites: List[List[int]]
6              :rtype: bool
7              """
8          graph = collections.defaultdict(list)
9          for u, v in prerequisites:
10             graph[u].append(v)
11             # 0 = Unknown, 1 = visiting, 2 = visited
12             visited = [0] * N
13             for i in range(N):
14                 if not self.dfs(graph, visited, i):
15                     return False
16             return True
17
18         # Can we add node i to visited successfully?
19         def dfs(self, graph, visited, i):
20             if visited[i] == 1: return False
21             if visited[i] == 2: return True
22             visited[i] = 1
23             for j in graph[i]:
24                 if not self.dfs(graph, visited, j):
25                     return False
26             visited[i] = 2
27             return True

```

如果需要保存拓扑排序的路径:

BFS方式:

```

1  class Solution(object):
2      def findOrder(self, numCourses, prerequisites):
3          """
4              :type numCourses: int
5              :type prerequisites: List[List[int]]
6              :rtype: List[int]
7              """
8          graph = collections.defaultdict(list)
9          indegrees = collections.defaultdict(int)
10         for u, v in prerequisites:
11             graph[v].append(u)
12             indegrees[u] += 1
13         path = []
14         for i in range(numCourses):
15             zeroDegree = False
16             for j in range(numCourses):
17                 if indegrees[j] == 0:
18                     zeroDegree = True
19                     break
20             if not zeroDegree:
21                 return []
22             indegrees[j] -= 1
23             path.append(j)
24             for node in graph[j]:
25                 indegrees[node] -= 1
26         return path

```

DFS方式:

```

1 class Solution(object):
2     def findOrder(self, numCourses, prerequisites):
3         """
4         :type numCourses: int
5         :type prerequisites: List[List[int]]
6         :rtype: List[int]
7         """
8         graph = collections.defaultdict(list)
9         for u, v in prerequisites:
10             graph[u].append(v)
11         # 0 = Unknown, 1 = visiting, 2 = visited
12         visited = [0] * numCourses
13         path = []
14         for i in range(numCourses):
15             if not self.dfs(graph, visited, i, path):
16                 return []
17         return path
18
19     def dfs(self, graph, visited, i, path):
20         if visited[i] == 1: return False
21         if visited[i] == 2: return True
22         visited[i] = 1
23         for j in graph[i]:
24             if not self.dfs(graph, visited, j, path):
25                 return False
26         visited[i] = 2
27         path.append(i)
28         return True

```

207. Course Schedule

210. Course Schedule II

310. Minimum Height Trees

## 查找子字符串，双指针模板

这是一个模板，里面的map如果是双指针范围内的字符串字频的话，增加和减少的方式如下。

```

1 int findSubstring(string s){
2     vector<int> map(128,0);
3     int counter; // check whether the substring is valid
4     int begin=0, end=0; //two pointers, one point to tail and one head
5     int d; //the length of substring
6
7     for() { /* initialize the hash map here */ }
8
9     while(end<s.size()){
10
11         if(map[s[end++]]++ ?){ /* modify counter here */ }
12
13         while(/* counter condition */){
14
15             /* update d here if finding minimum*/
16
17             //increase begin to make it invalid/valid again
18
19             if(map[s[begin++]]-- ?){ /*modify counter here*/ }
20         }
21
22         /* update d here if finding maximum*/
23     }

```

```

24         }
25         return d;
    }

```

## 76. Minimum Window Substring

这个题的map是t的字频，所以使用map更方式和上是相反的。

```

1  class Solution(object):
2      def minWindow(self, s, t):
3          """
4              :type s: str
5              :type t: str
6              :rtype: str
7          """
8          res = ""
9          left, cnt, minLen = 0, 0, float('inf')
10         count = collections.Counter(t)
11         for i, c in enumerate(s):
12             count[c] -= 1
13             if count[c] >= 0:
14                 cnt += 1
15             while cnt == len(t):
16                 if minLen > i - left + 1:
17                     minLen = i - left + 1
18                     res = s[left : i + 1]
19                 count[s[left]] += 1
20                 if count[s[left]] > 0:
21                     cnt -= 1
22                 left += 1
23         return res

```

## 动态规划

### 状态搜索

688. Knight Probability in Chessboard

62. Unique Paths

63. Unique Paths II

913. Cat and Mouse

576. Out of Boundary Paths

```

1  class Solution(object):
2      def findPaths(self, m, n, N, i, j):
3          """
4              :type m: int
5              :type n: int
6              :type N: int
7              :type i: int
8              :type j: int
9              :rtype: int
10         """
11         dp = [[0] * n for _ in range(m)]
12         for s in range(1, N + 1):
13             curStatus = [[0] * n for _ in range(m)]
14             for x in range(m):
15                 for y in range(n):
16                     v1 = 1 if x == 0 else dp[x - 1][y]
17                     v2 = 1 if x == m - 1 else dp[x + 1][y]
18                     v3 = 1 if y == 0 else dp[x][y - 1]
19                     v4 = 1 if y == n - 1 else dp[x][y + 1]

```

```
19         curStatus[x][y] = (v1 + v2 + v3 + v4) % (10**9 + 7)
20         dp = curStatus
21         return dp[i][j]
22
```

## 贪心

贪心算法（又称贪婪算法）是指，在对问题求解时，总是做出在当前看来最好的选择。也就是说，不从整体最优上加以考虑，他所作出的是在某种意义上的局部最优解。贪心算法和动态规划算法都是由局部最优导出全局最优，这里不得不比较下二者的区别

贪心算法：

- 1.贪心算法中，作出的每步贪心决策都无法改变，因为贪心策略是由上一步的最优解推导下一步的最优解，而上一部之前的最优解则不作保留。
- 2.由（1）中的介绍，可以知道贪心法正确的条件是：每一步的最优解一定包含上一步的最优解

动态规划算法：

- 1.全局最优解中一定包含某个局部最优解，但不一定包含前一个局部最优解，因此需要记录之前的所有最优解
- 2.动态规划的关键是状态转移方程，即如何由以求出的局部最优解来推导全局最优解
- 3.边界条件：即最简单的，可以直接得出的局部最优解

贪心是个思想，没有统一的模板。