Team Reference Document

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1 Template

1.1 .clang-format

```
BasedOnStyle: Google
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```

1.2 debug.cpp

```
#include <bits/stdc++.h>

using namespace std;

template <class T, size_t size = tuple_size<T>::value>
string to_debug(T, string s = "") requires(not ranges::range<T>);

template <class T>
concept check = requires(T x, ostream &os) {
    os << x;
};

template <check T>
```

```
14 string to_debug(T x) {
        return static_cast<ostringstream>(ostringstream() << x).str();</pre>
16 }
17
18 string to_debug(ranges::range auto x, string s = "") requires(not is_same_v<
        decltype(x), string>) {
19
            for (auto xi : x) {
20
                    s += ", " + to_debug(xi);
21
            return "[_" + s.substr(s.empty() ? 0 : 2) + "__]";
23 }
24
   template <class T, size_t size>
    string to_debug(T x, string s) requires(not ranges::range<T>) {
27
            [&] < size_t... I > (index_sequence < I... >) {
                    ((s += ", " + to_debug(get < I > (x))), ...);
            }(make index sequence<size>());
            return "{" + s.substr(s.empty() ? 0 : 2) + "}";
31 }
   #define debug(...) [](auto... $){ ((cout << to_debug($) << "□"), ...); cout
        << endl; }("[", #__VA_ARGS__, "]:", __VA_ARGS__)
```

1.3 gen.py

```
from random import *
n=10000
s='qwertyuiopasdfghjklzxcvbnm'
for i in range(n):
print(choice(s),end='')
print()
print()
print(randint(0,1),randint(1,n))
```

1.4 head.cpp

```
#pragma GCC optimize(2,"Ofast","inline","unroll-loops")
#include <bits/stdc++.h>
using namespace std;
#define rep(i,a,n) for (int i=a;i<=n;i++)
#define per(i,a,n) for (int i=a;i>=n;i--)
#define pb push_back
#define eb emplace_back
#define mp make_pair
```

```
#define all(x) (x).begin(),(x).end()
   #define bit(x) (111 << (x))
11 #define fi first
12 #define se second
   #define SZ(x) ((int)(x).size())
14 typedef vector <int > VI;
   typedef long long 11;
   typedef pair<int, int> PII;
17 typedef double db;
   mt19937_64 rng(random_device {}());
   typedef long double ldb;
   typedef unsigned long long ull;
21 ll powmod(ll a,ll b,const ll p) { ll res=1; while (b) { if (b&1) res=res*a%p
        ; b>>=1; a=a*a%p; } return res; }
22 // head
   #ifdef DEBUG
   #include "debug.cpp"
   #else
27 #define debug(...) 42
   #endif
   const int mod = 1e9 + 7:
    const 11 inf = 111 << 55;</pre>
   const double pi = acosl(-1);
    const double eps = 1e-12;
    const int maxn = 2e5 + 105;
    const int N = 2000005;
36
   void solve() {}
   int main() {
39
       ios::sync_with_stdio(false);
       cin.tie(nullptr);
40
       int tt = 1;
41
       // cin >> tt;
42
43
        while (tt--) {
            solve();
44
45
46 }
```

1.5 head-apiadu.cpp

```
1 #include <bits/stdc++.h>
```

```
2 using namespace std;
3 #define rep(i,a,n) for (int i=a;i<n;i++)</pre>
4 #define per(i,a,n) for (int i=n-1;i>=a;i--)
5 #define pb push_back
   #define eb emplace_back
7 #define mp make_pair
   #define all(x) (x).begin(),(x).end()
  #define fi first
  #define se second
11 #define SZ(x) ((int)(x).size())
12 typedef vector <int> VI;
   typedef basic_string<int> BI;
14 typedef long long 11;
15 typedef pair<int,int> PII;
16 typedef double db;
17 mt19937 mrand(random device{}());
18 const 11 mod=1000000007;
19 int rnd(int x) { return mrand() % x;}
20 ll powmod(ll a,ll b) {ll res=1;a%=mod; assert(b>=0); for(;b;b>>=1){if(b&1)
       res=res*a%mod:a=a*a%mod:}return res:}
21 11 gcd(11 a,11 b) { return b?gcd(b,a%b):a;}
22 // head
```

1.6 Makefile

```
1 %: %.cpp
2 g++-13 $< -o $@ -std=gnu++20 -g -02 -Wall -Wextra -DDEBUG -
D_GLIBCXX_DEBUG -D_GLIBCXX_DEBUG_PEDANTIC
```

1.7 pai.py

```
1 import os
2 tt=0
3 while True:
         os.system('python_gen.py_>_A.in')
         os.system('./a,,<,,A.in,,>,,a.out')
         os.system('./b_{\sqcup} <_{\sqcup} A.in_{\sqcup} >_{\sqcup} b.out')
         if os.system('diffua.outub.out'):
              print("WA")
9
              exit(0)
10
         else:
11
              tt+=1
12
              print("AC:",tt)
```

1.8 settings.json

```
1 {
2     "editor.formatOnSave": true,
3     "files.autoSave": "afterDelay",
4     "files.autoSaveDelay": 350,
5     "C_Cpp.default.cppStandard": "gnu++20"
6 }
```

1 #pragma GCC optimize(2, "Ofast", "inline", "unroll-loops")

1.9 template.cpp

```
#include <bits/stdc++.h>
3 using namespace std;
4 #define rep(i, a, n) for (int i = a; i \leq n; i++)
5 #define per(i, a, n) for (int i = a; i \ge n; i--)
6 #define pb push_back
7 #define eb emplace_back
8 #define all(x) (x).begin(), (x).end()
   #define bit(x) (111 << (x))
10 #define fi first
11 #define se second
12 #define SZ(x) ((int)(x).size())
13 using VI = vector<int>;
14 using PII = pair<int, int>;
15 using 11 = long long;
16 using ull = unsigned long long;
17 using db = double;
   using ldb = long double;
   mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
  // head
21
   #ifdef DEBUG
   #include "debug.cpp"
   #else
   #define debug(...) 42
   #endif
28 void solve() {}
   int main() {
       cin.tie(nullptr)->sync_with_stdio(false);
30
       cout << fixed << setprecision(16);</pre>
31
32
       int tt = 1;
33
       cin >> tt;
```

```
34 while (tt--) {
35 solve();
36 }
37 }
```

2 Data

2.1 Oltrie.cpp

```
1 struct node {
       int son[2];
       int end;
        int sz;
5 } seg[maxn << 2];</pre>
6 int root, tot;
   int n, m;
   void insert(11 x) {
        int cnt = root:
11
       for (int i = 62; i >= 0; i--) {
            int w = (x >> i) & 1;
12
13
            if (seg[cnt].son[w] == 0) seg[cnt].son[w] = ++tot;
14
            cnt = seg[cnt].son[w];
            seg[cnt].sz++;
16
17
        seg[cnt].end++;
18 }
19
20 ll query(ll x, ll k) {
21
       ll res = 0;
22
       int cnt = root;
23
       for (int i = 62; i >= 0; i--) {
24
            int w = (x >> i) & 1;
            if (seg[seg[cnt].son[w]].sz >= k) cnt = seg[cnt].son[w];
26
            else {
27
                k -= seg[seg[cnt].son[w]].sz;
                cnt = seg[cnt].son[abs(w - 1)];
                res += bit(i);
30
           }
31
       }
32
        return res;
33 }
```

2.2 2dtree(bqi343).cpp

```
const int SZ = 1.1e5;
    template <class T>
   struct node {
            T val = 0;
            node<T>* c[2]:
            node() { c[0] = c[1] = NULL; }
            void upd(int ind, T v, int L = 0, int R = SZ - 1) { // add v
                    if (L == ind && R == ind) {
                             val += v;
10
                            return:
                    }
11
12
                    int M = (L + R) / 2:
13
                    if (ind <= M) {
                            if (!c[0]) c[0] = new node();
14
                            c[0]->upd(ind, v, L, M);
15
16
                    } else {
                            if (!c[1]) c[1] = new node();
17
18
                            c[1] - vpd(ind, v, M + 1, R);
                    }
19
                    val = 0:
20
                    rep(i, 0, 1) if (c[i]) val += c[i] -> val;
21
22
23
            T query(int lo, int hi, int L = 0, int R = SZ - 1) { // query sum
                    if (hi < L || R < lo) return 0;
24
25
                    if (lo <= L && R <= hi) return val;
                    int M = (L + R) / 2:
26
27
                    T res = 0;
                    if (c[0]) res += c[0]->query(lo, hi, L, M);
28
29
                    if (c[1]) res += c[1]->query(lo, hi, M + 1, R);
30
                    return res;
31
            }
            void UPD(int ind, node* c0, node* c1, int L = 0, int R = SZ - 1) {
32
                // for 2D segtree
33
                    if (L != R) {
34
                            int M = (L + R) / 2;
35
                            if (ind <= M) {
36
                                     if (!c[0]) c[0] = new node();
37
                                     c[0] \rightarrow UPD(ind, c0 ? c0 \rightarrow c[0] : NULL, c1 ? c1
                                         ->c[0] : NULL, L, M);
38
                            } else {
39
                                     if (!c[1]) c[1] = new node():
```

```
40
                                    c[1]->UPD(ind, c0 ? c0->c[1] : NULL, c1 ? c1
                                        ->c[1] : NULL, M + 1, R);
41
                            }
42
                   }
43
                    val = (c0 ? c0 -> val : 0) + (c1 ? c1 -> val : 0):
44
           }
45 };
46
47 /**
    * Description: BIT of SeqTrees. x\in (0,SZ), y\in [0,SZ).
    * Memory: O(N\log^2 N)
    * Source: USACO Mowing the Field
    * Verification:
51
52
    * USACO Mowing the Field
    * http://www.usaco.org/index.php?page=viewproblem2&cpid=722 (13/15, 15/15
         and 1857ms with BumpAllocator)
54
    */
55
   #include "../1DuRangeuQueriesu(9.2)/SparseSegu(9.2).h"
57
   template <class T>
    struct BITseg {
60
           node<T> seg[SZ];
61
           BITseg() { fill(seg, seg + SZ, node<T>()); }
62
           void upd(int x, int y, int v) { // add v
63
                    for (; x < SZ; x += x & -x) seg[x].upd(y, v);
64
           }
           T query(int x, int yl, int yr) {
66
                   T res = 0;
67
                   for (; x; x \rightarrow x & -x) res += seg[x].query(yl, yr);
                    return res;
69
           }
70
           T query(int xl, int xr, int yl, int yr) { // query sum of rectangle
71
                    return query(xr, yl, yr) - query(xl - 1, yl, yr);
72
           }
73 };
74
75
76
    * Description: SeqTree of SeqTrees. x,y \in [0,SZ).
    * Memory: O(N\log^2 N)
77
    * Source: USACO Mowing the Field
    * Verification:
    * http://www.usaco.org/index.php?page=viewproblem2&cpid=722 (9/15 w/
```

```
BumpAllocator)
      * http://www.usaco.org/index.php?page=viewproblem2&cpid=601 (4238 ms, 2907
           ms w/ BumpAllocator)
 82
      */
 83
     #include "../1DuRangeuQueriesu(9.2)/SparseSegu(9.2).h"
 85
     template <class T>
     struct Node {
 88
             node <T> seg;
             Node* c[2];
 89
 90
             Node() \{ c[0] = c[1] = NULL; \}
             void upd(int x, int y, T v, int L = 0, int R = SZ - 1) { // add v
 91
 92
                      if (L == x && R == x) {
 93
                               seg.upd(y, v);
 94
                              return;
                      }
 95
                      int M = (L + R) / 2;
 97
                      if (x \le M) {
                              if (!c[0]) c[0] = new Node();
 98
 99
                              c[0] \rightarrow upd(x, y, v, L, M);
                      } else {
100
                              if (!c[1]) c[1] = new Node():
101
102
                              c[1] \rightarrow upd(x, y, v, M + 1, R);
103
                      }
                      seg.upd(y, v); // only for addition
104
                      // seq.UPD(y,c[0]?&c[0] \rightarrow seq:NULL,c[1]?&c[1] \rightarrow seq:NULL);
105
106
             }
107
             T query(int x1, int x2, int y1, int y2, int L = 0, int R = SZ - 1) {
                    // query sum of rectangle
                      if (x1 <= L && R <= x2) return seg.query(y1, y2);
108
109
                      if (x2 < L || R < x1) return 0;
                      int M = (L + R) / 2;
110
111
                      T res = 0;
                      if (c[0]) res += c[0]->query(x1, x2, y1, y2, L, M);
112
                      if (c[1]) res += c[1]->query(x1, x2, y1, y2, M + 1, R);
113
                      return res:
114
115
             }
116 };
```

2.3 cdq.cpp

```
1 int ans[maxn], lev[maxn];
```

```
2 array<int, 5> v[maxn], tmp[maxn];
3
4
    struct BIT {
5
            . . .
6 } c:
7
   void solve(int 1, int r) {
        if (1 \ge r) return:
10
       int mid = (1 + r) / 2;
11
       solve(1, mid), solve(mid + 1, r);
12
       int i = 1, j = mid + 1;
13
       int piv = 1;
14
        while (i <= mid || j <= r) {
15
            if (i <= mid && (j > r || mp(v[i][1], v[i][2]) <= mp(v[j][1], v[j
                1[2]))) {
16
                c.modify(v[i][2], v[i][3]);
17
                tmp[piv++] = v[i++];
18
           } else {
19
                v[j][4] += c.query(v[j][2]);
                tmp[piv++] = v[j++];
20
21
           }
22
       }
23
        rep(i, 1, mid) c.modify(v[i][2], -v[i][3]);
24
       rep(i, 1, r) v[i] = tmp[i];
25 }
26
   void solve() {
28
        cin >> n >> k;
29
       c.resize(k);
30
       rep(i, 1, n) {
31
            int s, c, m;
32
            cin >> s >> c >> m;
33
            v[i] = {s, c, m, 1, 0};
34
       }
35
       v[0][0] = -1;
36
        sort(v + 1, v + n + 1);
37
        int cnt = 0:
38
       rep(i, 1, n) {
39
            if (v[i][0] == v[cnt][0] && v[i][1] == v[cnt][1] && v[i][2] == v[cnt]
                ][2]) v[cnt][3]++;
            else v[++cnt] = v[i];
40
41
       }
42
        solve(1, cnt);
```

2.4 compact.cpp

```
namespace compact {
   const int LOGN=18;
3 int 1[N],r[N],tot,p[N][20],n;
   map<int,int> cv;
5 int lca(int u,int v) {
        if (dep[u]>dep[v]) swap(u,v);
        per(i,LOGN-1,0) if (dep[p[v][i]]>=dep[u]) v=p[v][i];
        if (u==v) return u:
        per(i,LOGN-1,0) if (p[v][i]!=p[u][i]) u=p[u][i],v=p[v][i];
10
        return p[u][0];
11 }
12 void dfs(int u,int f) {
        l[u]=++tot; dep[u]=dep[f]+1; p[u][0]=f;
13
        vec[dep[u]].pb(u);
14
       for (auto v:vE[u]) {
15
16
            if (v==f) continue;
            dfs(v,u);
17
       }
18
19
        r[u]=tot;
20 }
   void build(int n) {
        n= n: tot=0:
22
23
        dfs(1,0);
24
        rep(j,1,LOGN-1) rep(i,1,n) p[i][j]=p[p[i][j-1]][j-1];
25 }
26
   bool cmp(int u,int v) { return l[u]<l[v]; }</pre>
   vector<PII> compact(VI v) {
28
        int m=SZ(v);
29
        vector<PII> E:
30
        sort(all(v),cmp);
31
32
        rep(i.0.m-2) {
            int w=lca(v[i],v[i+1]);
33
34
            v.pb(w);
35
       }
```

```
v.pb(0);
37
       v.pb(1);
        sort(all(v),cmp);
39
       v.erase(unique(all(v)), v.end());
40
       cv.clear():
41
        per(i,SZ(v)-1,1) {
42
            int u=v[i];
43
            while (1) {
44
                auto it=cv.lower bound(1[u]);
45
                if (it==cv.end()||it->fi>r[u]) break;
46
                E.pb(mp(u,v[it->se]));
47
                cv.erase(it);
           }
48
49
            cv[1[u]]=i;
       }
50
51
        return E;
52 }
53 }:
```

2.5 dominator.cpp

```
1 void solve(int u, int S) {
            int best = -1, cnt = S + 1;
3
            auto find best = [&](auto &find best, int u, int par) -> void {
                    sz[u] = 1, sdom[u] = 0;
                    for (auto v : e[u]) {
                            if (v == par || del[v]) continue;
                            find_best(find_best, v, u);
                            sz[u] += sz[v];
                            sdom[u] = max(sdom[u], sz[v]):
                    }
10
                    sdom[u] = max(sdom[u], S - sz[u]);
11
12
                    if (sdom[u] < cnt) {</pre>
13
                            cnt = sdom[u], best = u;
14
                    }
15
            };
16
            find_best(find_best, u, 0);
            int id1 = tot++, dep1 = 0;
17
18
            int id2, dep2;
19
            auto dfs = [&](auto &dfs. int u. int par. int dep) -> void {
20
                    dep1 = max(dep1, dep);
21
                    dep2 = max(dep2, dep);
22
                    Q[u].pb({id1, 1, dep});
```

```
23
                    Q[u].pb({id2, -1, dep});
24
                    for (auto v : e[u]) {
                            if (v == par || del[v]) continue;
25
26
                            dfs(dfs, v, u, dep + 1);
                   }
27
28
            };
29
            Q[best].pb({id1, 1, 0});
            for (auto v : e[best]) {
30
31
                    if (del[v]) continue;
                   id2 = tot++, dep2 = 0;
32
33
                    dfs(dfs, v, best, 1);
                    fenw[id2] = BIT<11>(dep2 + 1);
34
            }
35
36
            fenw[id1] = BIT<11>(dep1 + 1);
37
            del[best] = 1;
38
            for (auto v : e[best]) {
                    if (!del[v]) solve(v, sz[v]);
39
41 }
```

2.6 dsu.cpp

```
1 class dsu {
2 public:
           vector<int> fa;
           vector<ll> dist:
           int n;
           dsu(int _n) : n(_n) {
                   fa.resize(n):
                   dist.assign(n, 0);
                   iota(fa.begin(), fa.end(), 0);
10
           }
11
12
13
           int find(int x) {
                    if (fa[x] == x) return x;
14
15
                   int par = fa[x];
                   fa[x] = find(fa[x]);
16
                   dist[x] += dist[par];
17
18
                   return fa[x]:
19
           }
20
21
           void unite(int x, int y, ll v) {
```

2.7 dsu-on-tree.cpp

```
1 void dfs(int x, int fa) {
       hs[x] = -1, w[x] = 1;
      l[x] = ++tot;
4
       id[tot] = x;
       for (auto y : g[x]) if (y != fa) {
                dfs(v, x);
                w[x] += w[y];
                if (hs[x] == -1 || w[y] > w[hs[x]])
                   hs[x] = y;
           }
11
       r[x] = tot;
12 }
13
14 void dsu(int x, int fa, int keep) {
15
        for (auto y : g[x]) {
16
            if (y != hs[x] && y != fa) {
                dsu(y, x, 0);
18
           }
19
       }
       if (hs[x] != -1) dsu(hs[x], x, 1);
20
21
22
       for (auto y : g[x]) {
23
            if (y != hs[x] && y != fa) {
24
                for (int i = l[y]; i \le r[y]; i++) {
25
26
27
           }
28
        // add current node
29
30
31
       ans[x] = cnt:
32
33
        if (!keep) {
34
           // clear
```

```
35 }
36 }
```

2.8 fenwick.cpp

```
1 template <typename T>
   struct BIT {
     vector<T> fenw:
     int n, pw;
     BIT(int n_ = 0) : n(n_ ) {
       fenw.assign(n + 1, 0);
       pw = bit_floor(unsigned(n));
    }
10
     void Modify(int x, T v) {
11
12
       if (x \le 0) return; // assert(0 \le x \&\& x \le n);
       while (x \le n) {
                            // x < n
13
         fenw[x] += v;
         x += (x \& -x); // x /= x + 1;
       }
16
17
     }
18
19
     T Query(int x) {
       // assert(0 <= x && x <= n);
       T v{}:
       while (x > 0) {
         v += fenw[x]; // fenw[x - 1];
         x = (x \& -x); // x \& = x - 1;
24
       }
25
       return v:
27
     }
28
29
     // Returns the length of the longest prefix with sum <= c
     int MaxPrefix(T c) {
       T v{};
31
       int at = 0;
       for (int i = 20; i >= 0; i--) {
33
         if (at + bit(i) <= n && v + fenw[at + bit(i)] <= c) {</pre>
34
           v += fenw[at + bit(i)]:
           at += bit(i):
37
         }
       }
```

2.9 fenwick2d.cpp

```
1 template <typename T>
2 class fenwick2d {
3 public:
           vector<vector<T>> fenw;
           int n, m;
           fenwick2d(int _n, int _m) : n(_n), m(_m) {
                   fenw.resize(n);
                   for (int i = 0: i < n: i++) {
                            fenw[i].resize(m);
10
11
                   }
           }
12
13
           inline void modify(int i, int j, T v) {
14
                   int x = i;
15
16
                    while (x < n) {
17
                           int y = j;
                            while (y < m) {
19
                                    fenw[x][y] += v;
                                   y = (y + 1);
21
                           x = (x + 1);
23
                   }
24
           }
```

```
25
            inline T get(int i, int j) {
26
                    T v{}:
27
28
                    int x = i;
29
                    while (x \ge 0) {
30
                            int y = j;
                            while (y >= 0) {
31
                                    v += fenw[x][y];
33
                                    y = (y & (y + 1)) - 1;
34
                            }
35
                            x = (x & (x + 1)) - 1;
                    }
36
37
                    return v:
38
            }
39 }:
40
    struct node {
            int a = ...; // don't forget to set default value
43
            inline void operator+=(node &other) {
44
45
46
            }
47 }:
```

2.10 hash-table.cpp

```
struct Hash table {
        static const int V = 1000003:
        int fst[V], nxt[V];
        int ctm, ptm[V], T;
        int val[V];
       11 kev[V];
        void init() \{T = 0, ctm++:\}
        void insert(ll k, int v) {
            int s = k \% V:
            if (ptm[s] != ctm) ptm[s] = ctm, fst[s] = -1;
10
            for (int i = fst[s]; i != -1; i = nxt[i]) if (key[i] == k) {
11
12
                    return:
               }
13
14
            nxt[T] = fst[s], fst[s] = T, kev[T] = k, val[T] = v:
15
            T++;
16
       }
17
        int query(ll k) {
```

2.11 HLD.cpp

```
1 struct HLD {
        int n:
        std::vector<int> siz, top, dep, parent, in, out, seq;
        std::vector<std::vector<int>> adj;
       int cur:
6
7
       HLD() {}
        HLD(int n) {
9
            init(n);
10
       }
11
        void init(int n) {
12
            this->n = n:
13
            siz.resize(n);
            top.resize(n);
14
15
            dep.resize(n);
16
            parent.resize(n);
17
            in.resize(n):
18
            out.resize(n);
19
            sea.resize(n):
20
            cur = 0:
21
            adj.assign(n, {});
22
       }
23
        void addEdge(int u, int v) {
24
            adj[u].push_back(v);
25
            adj[v].push_back(u);
26
        void work(int root = 0) {
27
28
            top[root] = root;
29
            dep[root] = 0:
30
            parent[root] = -1;
31
            dfs1(root);
32
            dfs2(root);
```

```
33
       }
                                                                                           75
34
        void dfs1(int u) {
                                                                                           76
            if (parent[u] != -1) {
                                                                                           77
35
                                                                                                       }
36
                adj[u].erase(std::find(adj[u].begin(), adj[u].end(), parent[u]))
                                                                                           78
                                                                                           79
            }
                                                                                           80
37
                                                                                           81
            siz[u] = 1:
                                                                                           82
            for (auto &v : adj[u]) {
                                                                                           83
                                                                                                       }
                parent[v] = u;
                                                                                           84
41
42
                dep[v] = dep[u] + 1;
                                                                                           85
                dfs1(v);
                                                                                           86
                                                                                                   }
43
                siz[u] += siz[v];
                                                                                           87
44
                if (siz[v] > siz[adj[u][0]]) {
45
                    std::swap(v, adj[u][0]);
                                                                                           89
46
               }
                                                                                           90
                                                                                                   }
47
            }
                                                                                           91
       }
                                                                                           92
50
        void dfs2(int u) {
            in[u] = cur++:
51
                                                                                           94
            seq[in[u]] = u;
                                                                                           95
52
53
            for (auto v : adj[u]) {
                                                                                                       }
54
                top[v] = v == adj[u][0] ? top[u] : v;
55
                dfs2(v);
56
            }
                                                                                           99
            out[u] = cur;
                                                                                          100
57
        int lca(int u, int v) {
59
                                                                                          101
60
            while (top[u] != top[v]) {
                                                                                          102
61
                if (dep[top[u]] > dep[top[v]]) {
                                                                                          103
                    u = parent[top[u]];
                                                                                          104
                                                                                                   }
62
                                                                                          105
                } else {
                    v = parent[top[v]];
                                                                                          106
64
               }
                                                                                          107
65
66
            }
                                                                                          108
67
            return dep[u] < dep[v] ? u : v;</pre>
                                                                                          109
                                                                                          110
       }
68
                                                                                          111
69
                                                                                          112
70
        int dist(int u, int v) {
71
            return dep[u] + dep[v] - 2 * dep[lca(u, v)];
                                                                                          113
72
       }
                                                                                          114
                                                                                                   }
                                                                                          115
73
74
        int jump(int u, int k) {
                                                                                          116
```

```
if (dep[u] < k) {
        return -1;
    int d = dep[u] - k;
    while (dep[top[u]] > d) {
        u = parent[top[u]];
    return seq[in[u] - dep[u] + d];
bool isAncester(int u, int v) {
    return in[u] <= in[v] && in[v] < out[u];
int rootedParent(int u. int v) {
    std::swap(u, v);
    if (u == v) {
        return u;
    if (!isAncester(u, v)) {
        return parent[u];
    auto it = std::upper_bound(adj[u].begin(), adj[u].end(), v, [&](int
        x, int y) {
        return in[x] < in[y];</pre>
    }) - 1;
    return *it:
int rootedSize(int u, int v) {
    if (u == v) {
        return n;
    if (!isAncester(v, u)) {
        return siz[v];
    return n - siz[rootedParent(u, v)];
int rootedLca(int a, int b, int c) {
```

```
117 return lca(a, b) ^ lca(b, c) ^ lca(c, a);
118 }
119 };
```

2.12 kdtree.cpp

```
namespace kd {
2
               const int K = 2, N = 2.1e5;
               template <typename T>
               using P = array<T, K>;
               template <typename T>
               struct node {
                          P<T> pt, mx, mn;
                          ll val, sum;
                          node *1, *r, *p;
                          int id:
10
11
                          node(const P<T> &_pt = P<T>(), 11 _val = 0, int _id = 0) :
                               pt(_pt), val(_val), sum(_val), id(_id) {
12
                                     mx = mn = pt;
13
                                     p = 1 = r = nullptr;
                          }
14
               };
15
               node<11> *ptr[N];
16
17
               template <typename T>
               void pull(node<T> *u) {
18
                          if (not u) return:
19
20
                          u \rightarrow sum = u \rightarrow val;
                          rep(i, 0, K - 1) u \rightarrow mx[i] = u \rightarrow mn[i] = u \rightarrow pt[i];
21
22
                          if (u->1) {
23
                                     u \rightarrow sum += u \rightarrow 1 \rightarrow sum:
24
                                     u -> 1 -> p = u;
25
                          }
                          if (u->r) {
26
27
                                     u \rightarrow sum += u \rightarrow r \rightarrow sum;
28
                                     u \rightarrow r \rightarrow p = u;
29
                          }
30
                          rep(i, 0, K - 1) {
31
                                     if (u->1) {
                                               u - mx[i] = max(u - mx[i], u - l - mx[i]);
32
33
                                               u \rightarrow mn[i] = min(u \rightarrow mn[i], u \rightarrow 1 \rightarrow mn[i]):
34
                                     }
35
                                     if (u->r) {
36
                                               u \rightarrow mx[i] = max(u \rightarrow mx[i], u \rightarrow r \rightarrow mx[i]):
```

```
37
                                      u-mn[i] = min(u-mn[i], u-r-mn[i]);
38
                             }
                    }
39
40
            }
41
42
            template <typename T>
43
            node<T> *build(vector<node<T>> &a, int 1, int r, int d = 0) {
44
                     if (d == K) d = 0:
45
                    if (1 >= r) {
46
                             return nullptr;
47
                    } else {
48
                             int md = (1 + r) >> 1;
                             nth_element(a.begin() + 1, a.begin() + md, a.begin()
49
                                  + r, [&](node<T> &x, node<T> &y) { return x.pt[
                                  d] < y.pt[d]; });</pre>
50
                             node<T> *p = new node<T>(a[md]);
51
                             ptr[p->id] = p;
52
                             p \rightarrow 1 = build(a, 1, md, d + 1);
53
                             p->r = build(a, md + 1, r, d + 1);
54
                             pull(p);
55
                             return p;
56
                    }
            }
57
58
59
            template <typename T>
60
            node<T> *search(node<T> *u, P<T> p, int d = 0) {
61
                     if (d == K) d = 0:
62
                    if (not u) return nullptr;
63
                    if (u->pt == p) return u;
64
                     if (p[d] < u->pt[d]) {
                             return search(u->1, p, d + 1);
65
                    } else if (p[d] > u->pt[d]) {
                             return search(u->r, p, d + 1);
67
68
                    } else {
69
                             auto tmp = search(u \rightarrow 1, p, d + 1);
70
                             if (tmp) return tmp;
71
                             return search(u->r, p, d + 1);
72
                    }
73
            }
74
75
            template <typename T>
76
            void modify(node<T> *u, ll v) {
77
                     if (not u) return;
```

```
78
                     u \rightarrow val = v:
                                                                                         120
                                                                                                               11 s = 0:
                                                                                         121
                                                                                                               rep(i, 0, K - 1) {
 79
                     for (auto cur = u; cur; cur = cur->p) {
                                                                                          122
                                                                                                                       if (p[i] <= nd->mn[i]) s += nd->mn[i] - p[i];
                             pull(cur):
 81
                     }
                                                                                          123
                                                                                                                       if (p[i] >= nd -> mx[i]) s += p[i] - nd -> mx[i];
             }
                                                                                         124
                                                                                                              }
 82
                                                                                         125
 83
                                                                                                               return s;
                                                                                         126
                                                                                                      }
 84
             template <typename T>
             bool inside(node<T> *nd. P<T> p. 11 c) {
                                                                                          127
 85
 86
                     int cc = 0:
                                                                                         128
                                                                                                      template <typename T>
                                                                                          129
                     if (nd->mx[0] * p[0] + nd->mx[1] * p[1] >= c) cc++;
                                                                                                      11 mindist(node<T> *u. P<T> p) {
 87
 88
                     if (nd-mn[0] * p[0] + nd-mn[1] * p[1] >= c) cc++;
                                                                                          130
                                                                                                               ll s = numeric limits<T>::max() / 4;
                     if (nd->mx[0] * p[0] + nd->mn[1] * p[1] >= c) cc++;
                                                                                          131
                                                                                                               if (u->pt != p) {
 89
                     if (nd-mn[0] * p[0] + nd-mx[1] * p[1] >= c) cc++:
                                                                                          132
                                                                                                                       s = min(s, abs(u->pt[0] - p[0]) + abs(u->pt[1] - p
 90
                     return cc == 0:
 91
                                                                                                                            [1]));
 92
             }
                                                                                         133
                                                                                                               }
 93
                                                                                         134
                                                                                                               11 best1 = eval min(u->1, p), best2 = eval min(u->r, p);
                                                                                          135
 94
             template <typename T>
                                                                                                               if (best1 < best2) {</pre>
             bool outside(node<T> *nd, P<T> p, 11 c) {
                                                                                          136
                                                                                                                       if (u\rightarrow 1) s = min(s, mindist(u\rightarrow 1, p)):
                                                                                                                       if (u->r \text{ and best2} < s) s = min(s, mindist(u->r, p))
 96
                     int cc = 0:
                                                                                          137
                     if (nd-mx[0] * p[0] + nd-mx[1] * p[1] >= c) cc++;
 97
                     if (nd-mn[0] * p[0] + nd-mn[1] * p[1] >= c) cc++;
 98
                                                                                          138
                                                                                                                       return s;
                     if (nd - mx[0] * p[0] + nd - mn[1] * p[1] >= c) cc++:
                                                                                          139
                                                                                                               } else {
 99
                                                                                         140
                     if (nd-mn[0] * p[0] + nd-mx[1] * p[1] >= c) cc++:
                                                                                                                       if (u\rightarrow r) s = min(s, mindist(u\rightarrow r, p)):
100
                     return cc == 4:
                                                                                         141
                                                                                                                       if (u->1) and best1 < s) s = min(s, mindist(u->1, p))
101
102
             }
                                                                                         142
103
                                                                                                                       return s;
             template <typename T>
                                                                                         143
                                                                                                              }
104
                                                                                         144
                                                                                                      }
105
             ll query(nodeT> *u, PT> p, ll c) {
106
                     if (inside(u, p, c)) return u->sum;
                                                                                         145
                     if (outside(u, p, c)) return 0;
                                                                                         146
                                                                                                      template <tvpename T>
107
                                                                                         147
                                                                                                      T eval max(node<T> *nd, P<T> p) { // 通过估价函数进行启发式搜索,根
108
                     11 s = 0:
                                                                                                           据当前结果对搜索剪枝
109
                     if (u-pt[0] * p[0] + u-pt[1] * p[1] < c) {
                                                                                                               if (not nd) return 0:
                             s += u -> val:
                                                                                         148
110
111
                     }
                                                                                         149
112
                     if (u->1) s += query(u->1, p, c);
                                                                                          150
                                                                                                               rep(i, 0, K - 1) s += max(abs(nd->mx[i] - p[i]), abs(nd->mn[i])
113
                     if (u->r) s += query(u->r, p, c);
                                                                                                                   i] - p[i]));
                     return s:
                                                                                          151
                                                                                                               return s:
114
                                                                                         152
                                                                                                      }
115
             }
116
                                                                                         153
117
             template <typename T>
                                                                                         154
                                                                                                      template <typename T>
             T eval min(node<T> *nd, P<T> p) { // 通过估价函数进行启发式搜索,根
                                                                                          155
                                                                                                      11 maxdist(node<T> *u, P<T> p) {
118
                 据当前结果对搜索剪枝
                                                                                         156
                                                                                                              11 s = 0:
                                                                                         157
119
                     if (not nd) return numeric limits<T>::max() / 4;
                                                                                                               if (u->pt != p) {
```

```
158
                              s = max(s, abs(u->pt[0] - p[0]) + abs(u->pt[1] - p
                                   [1]));
                     }
159
160
                     ll best1 = eval max(u->1, p), best2 = eval max(u->r, p);
                     if (best1 > best2) {
161
                              if (u->1) s = max(s, maxdist(u->1, p));
162
                              if (u->r \text{ and best2} > s) s = max(s, maxdist(u->r, p))
163
164
                              return s;
                     } else {
165
                              if (u->r) s = max(s, maxdist(u->r, p));
166
                              if (u->1 \text{ and best1} > s) s = max(s, maxdist(u->1, p))
167
168
                              return s;
                     }
169
170
171 } // namespace kd
```

2.13 LCT.cpp

```
namespace linkCutTree {
   struct node {
       node *child[2], *parent, *max;
       int sum, val, sz, weight, id, rev;
       node(int val, int weight, int id): child {nullptr, nullptr}, parent(
            nullptr), max(this), sum(val), val(val), sz(weight), weight(weight),
            id(id), rev(false) {}
7 };
9 bool isRoot(node *p) {return p->parent == nullptr || p->parent->child[0] !=
       p && p->parent->child[1] != p;}
10
   int side(node *p) {return p->parent->child[1] == p;}
12
13
   int sum(node *p) {return p == nullptr ? 0 : p->sum;}
14
15
    int sz(node *p) {return p == nullptr ? 0 : p->sz;}
16
   node *max(node *p) {return p == nullptr ? nullptr : p->max;}
18
19
   node *max(node *p, node *q) {
       if (p == nullptr)
20
```

```
21
             return q;
22
         if (q == nullptr)
23
             return p;
24
         return p->weight > q->weight ? p : q;
25 }
26
    void reverse(node *p) {
28
         if (p == nullptr)
29
             return;
30
         swap(p->child[0], p->child[1]);
31
         p->rev ^= 1;
32 }
33
34
    void push(node *p) {
35
         if (p\rightarrow rev == 0)
             return;
37
         p \rightarrow rev = 0;
         reverse(p->child[0]);
         reverse(p->child[1]);
40 }
41
42 void pull(node *p) {
         p\rightarrow sum = sum(p\rightarrow child[0]) + sum(p\rightarrow child[1]) + p\rightarrow val;
         p\rightarrow max = max(max(p\rightarrow child[0]), max(p\rightarrow child[1])), p);
44
45
         p\rightarrow sz = p\rightarrow weight + sz(p\rightarrow child[0]) + sz(p\rightarrow child[1]);
46 }
47
    void connect(node *p, node *q, int side) {
49
         q->child[side] = p;
50
         if (p != nullptr)
51
             p->parent = q;
52 }
53
    void rotate(node *p) {
55
         auto q = p->parent;
         int dir = side(p) ^ 1;
         connect(p->child[dir], q, dir ^ 1);
         if (!isRoot(q))
59
              connect(p, q->parent, side(q));
60
         else
61
             p->parent = q->parent;
62
         connect(q, p, dir);
63
         pull(q);
```

```
64 }
 65
    void splay(node *p) {
 66
 67
         vector<node *> stk;
         for (auto i = p; !isRoot(i); i = i->parent)
 68
 69
             stk.push_back(i->parent);
         while (!stk.empty()) {
 70
             push(stk.back());
 71
 72
             stk.pop_back();
         }
 73
 74
         push(p);
         while (!isRoot(p)) {
 75
             auto q = p->parent;
 76
             if (!isRoot(q))
 77
 78
                 rotate(side(p) == side(q) ? q : p);
             rotate(p);
 79
         }
 80
 81
         pull(p);
 82 }
 83
     node *access(node *p) {
         node *j = nullptr;
 85
         for (node *i = p; i != nullptr; j = i, i = i->parent) {
 86
 87
             splay(i);
 88
             i->val -= sum(j);
             i->val += sum(i->child[1]);
             i \rightarrow child[1] = j;
 90
             pull(i);
 91
 92
         }
 93
         splay(p);
 94
         return j;
 95 }
 96
    void makeRoot(node *p) {
 97
 98
         access(p);
 99
         reverse(p);
100 }
101
    void link(node *p, node *q) {
102
103
         makeRoot(p);
         access(q);
104
         p->parent = q;
105
106
         q->val += sum(p);
```

```
107 }
108
    void cut(node *p, node *q) {
110
         makeRoot(p);
111
        access(q);
112
        p->parent = q->child[0] = nullptr;
113 }
114
115
    node *pathMax(node *p, node *q) {
116
         makeRoot(p);
117
         access(q);
118
         return max(q);
119 }
120
121
    int pathSum(node *p, node *q) {
122
         makeRoot(p);
123
         access(q);
124
         return sz(q);
125 }
126
127
    int size(node *p) {
128
         makeRoot(p):
129
         return sum(p);
130 }
131
132
    bool connected(node *p, node *q) {
133
         access(p);
134
         access(q);
135
        return p->parent != nullptr;
136 }
137
    void fix(node *p, ll v) {
139
         access(p);
140
        // modify ...
141
         pull(p);
142 }
143
    node *lca(node *z,node *x,node *y) {
145
         makeRoot(z);
146
         access(x);
147
         return access(y);
148 }
149
```

```
150 } // namespace linkCutTree
151
152 using namespace linkCutTree;
```

2.14 lichao-tree.cpp

```
struct Line {
      i64 k, b;
      i64 operator()(i64 x) const { return k * x + b; }
5 template <i64 L, i64 R>
   struct Segments {
      struct Node {
        optional < Line > s;
        Node *1, *r;
     }:
11
     Node *root;
      Segments() : root(nullptr) {}
12
      void add(i64 1, i64 r, i64 k, i64 b) {
13
        auto rec = [%](auto &rec, Node *%p, i64 tl, i64 tr, Line s) -> void {
14
15
          if (p == nullptr) p = new Node();
          i64 tm = midpoint(tl, tr);
16
          if (tl >= 1 \text{ and } tr <= r) {
17
18
            if (not p->s) return p->s = s, void();
            auto t = p->s.value();
19
            if (t(t1) >= s(t1)) {
20
21
              if (t(tr) >= s(tr)) return;
22
              if (t(tm) \ge s(tm)) return rec(rec, p->r, tm + 1, tr, s);
23
              return p \rightarrow s = s, rec(rec, p \rightarrow 1, tl, tm, t);
24
25
            if (t(tr) \le s(tr)) return p->s = s, void();
26
            if (t(tm) \le s(tm)) return p->s = s, rec(rec, p->r, tm + 1, tr, t);
27
            return rec(rec, p->1, t1, tm, s);
28
         }
          if (1 <= tm) rec(rec, p->1, t1, tm, s);
30
          if (r > tm) rec(rec, p->r, tm + 1, tr, s);
31
        };
32
        rec(rec, root, L, R, {k, b});
33
      optional <i64> get(i64 x) {
34
35
        optional < i64> res = {};
36
        auto rec = [&](auto &rec, Node *p, i64 tl, i64 tr) -> void {
37
          if (p == nullptr) return;
```

```
i64 tm = midpoint(tl, tr);
          if (p\rightarrow s) {
40
            i64 y = p->s.value()(x);
41
            if (not res or res.value() < y) res = y;</pre>
42
          }
43
          if (x <= tm)
            rec(rec, p->1, t1, tm);
46
            rec(rec, p->r, tm + 1, tr);
47
        }:
        rec(rec, root, L, R);
        return res;
51 };
```

2.15 Mo.cpp

```
1 int main() {
        std::ios::sync with stdio(false);
3
        cin.tie(0); cout.tie(0);
5
       for (int i = 1; i <= m; i++) {
            int x, y;
            cin >> x >> y;
            q.pb({x, y, i});
            rej[i] = (y - x + 1LL) * (y - x) / 2LL;
10
11
        sort(q.begin(), q.end(), [&](array<int, 3> a, array<int, 3> b)->bool{
12
            if (getb(a[0]) == getb(b[0]))
13
                if (getb(a[0]) & 1)
14
                    return a[1] < b[1];
15
                else
16
                    return a[1] > b[1];
17
            else return getb(a[0]) < getb(b[0]);</pre>
18
       }):
19
20
       int L = 1, R = 0;
21
       for (int i = 0; i < m; i++) {
22
            while (R < q[i][1]) R++, add(R);
23
            while (L > q[i][0]) L--, add(L);
24
            while (L < q[i][0]) del(L), L++;
25
            while (R > q[i][1]) del(R), R--;
26
            ans[q[i][2]] = tmp;
```

```
27 }
28 }
```

2.16 moTree.cpp

```
1 void add(int ind, int end) { ... } // add a [ ind ] (end = 0 or 1)
   void del(int ind, int end) { ... } // remove a [ ind ]
   int calc() { ... } // compute current answer
   vi mo(vector<pii> Q) {
      int L = 0, R = 0, blk = 350; // N/sqrt(Q)
     vi s(sz(0)). res = s:
7 #define K(x) pii(x.first/blk, x.second ^ -(x.first/blk & 1))
     iota(all(s), 0);
     sort(all(s), [\&](int s, int t) { return K(Q[s]) < K(Q[t]); });
     for (int qi : s) {
       pii q = Q[qi];
11
12
       while (L > q.first) add(--L, 0);
       while (R < q.second) add(R++, 1);
13
       while (L < q.first) del(L++, 0);</pre>
14
       while (R > q.second) del(--R, 1);
15
16
       res[qi] = calc();
17
     }
18
     return res:
19 }
   vi moTree(vector<array<int, 2>> Q, vector<vi>& ed, int root = 0) {
      int N = sz(ed), pos[2] = \{\}, blk = 350; // N/sqrt (Q)
21
     vi s(sz(Q)), res = s, I(N), L(N), R(N), in(N), par(N);
     add(0, 0), in[0] = 1:
23
24
      auto dfs = [&](int x, int p, int dep, auto & f) -> void {
       par[x] = p:
25
26
       L[x] = N:
27
       if (dep) I[x] = N++;
       for (int y : ed[x]) if (y != p) f(y, x, !dep, f);
28
       if (!dep) I[x] = N++;
       R[x] = N:
31
     };
     dfs(root, -1, 0, dfs);
    #define K(x) pii(I[x[0]] / blk, I[x[1]] ^ -(I[x[0]] / blk & 1))
34
     iota(all(s), 0);
     sort(all(s), [\&](int s, int t) \{ return K(Q[s]) < K(Q[t]); \});
36
     for (int qi : s) rep(end, 0, 2) {
37
       int &a = pos[end], b = Q[qi][end], i = 0;
   #define step(c) { if (in[c]) { del(a, end); in[a] = 0; }
```

2.17 MSTMo.cpp

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 #define rep(i,a,n) for (int i=a;i<n;i++)</pre>
4 #define per(i,a,n) for (int i=n-1;i>=a;i--)
5 #define pb push_back
6 #define mp make_pair
  #define all(x) (x).begin(),(x).end()
8 #define fi first
9 #define se second
10 #define SZ(x) ((int)(x).size())
11 typedef vector<int> VI;
12 typedef long long 11;
13 typedef pair<int,int> PII;
14 typedef double db;
15 mt19937 mrand(random device{}());
16 const ll mod=1000000007:
17 int rnd(int x) { return mrand() % x;}
18 ll powmod(11 a,11 b) {ll res=1;a%=mod; assert(b>=0); for(;b;b>>=1){if(b&1)
        res=res*a%mod:a=a*a%mod:}return res:}
19 ll gcd(ll a, ll b) { return b?gcd(b, a%b):a;}
20 // head
21
   const int N=1010000;
24 int a[N];
25 namespace Mo {
     int Q,1[N],r[N],f[N],10,r0,ans[N],n;
     VI ne[N]:
     struct point {
29
       int x, y, o;
30
       point(int a, int b, int c): x(a), y(b), o(c) {}
```

```
31
     };
32
      inline bool operator<(const point &a, const point &b) {</pre>
       if (a.x != b.x) return a.x > b.x;
33
34
       else return a.v < b.v;</pre>
     }
35
      vector<point> p;
36
      struct edge {
       int s, t, d;
38
39
       edge(const point &a, const point &b): s(a.o), t(b.o),
          d(abs(a.x - b.x) + abs(a.y - b.y)) {}
40
41
     };
      inline bool operator < (const edge &a, const edge &b) {return a.d < b.d;}
42
      vector<edge> e:
43
44
      int g[N],z[N];
      int cc.cnt[101000]:
45
46
     void addedge() {
47
       sort(all(p));
         memset(g,0,sizeof(g));
         z[0]=N;
49
       rep(i,0,SZ(p)) z[i+1]=p[i].x-p[i].y;
50
       rep(i,0,SZ(p)) {
51
52
              int k = 0, t = p[i].x + p[i].y;
              for (int j = t; j; j -= j & -j)
54
                  if (z[g[j]] < z[k]) k = g[j];
55
              if (k) e.pb(edge(p[i], p[k - 1]));
              k = z[i + 1];
56
57
              for (int j = t; j <N; j += j & -j)
                  if (k < z[g[j]]) g[j] = i + 1;
58
59
         }
60
     }
      void updata(int i, bool j,bool k=0) {
61
62
       // j=1 insert j=0 delete
63
       // k=0 left k=1 right
64
       if (j==1) {
65
         cnt[a[i]]++;
66
         if (cnt[a[i]]%2==0) cc++;
       } else {
67
         if (cnt[a[i]]%2==0) cc--;
          cnt[a[i]]--;
69
70
       }
     }
71
72
     void init(int 1,int r) {
73
       for (int i=1;i<=r;i++) {
```

```
74
           cnt[a[i]]++;
           if (cnt[a[i]]%2==0) cc++;
 76
        }
 77
      }
      inline int query() {
 78
 79
        return cc;
 80
 81
       int find(int x) { if (f[x] != x) f[x] = find(f[x]); return f[x];}
       void dfs(int i,int p) {
 83
        int 11 = 1[i], r1 = r[i]:
 84
        per(j,11,10) updata(j,1,0);
 85
        rep(j,r0+1,r1+1) updata(j,1,1);
        rep(j,10,11) updata(j,0,0);
        per(j,r1+1,r0+1) updata(j,0,1);
        ans[i]=query();10=11;r0=r1;
 89
        rep(j,0,SZ(ne[i])) if (ne[i][j]!=p) dfs(ne[i][j],i);
 90
 91
      void solve() {
        p.clear();e.clear();
        rep(i,1,Q+1) ans[i]=0;
 93
 94
        rep(i,1,Q+1) p.pb(point(l[i],r[i],i));
        addedge():
        rep(i,0,SZ(p)) p[i].y = n-p[i].y+1;
 97
         addedge();
 98
        rep(i,0,SZ(p)) {
          int j = n-p[i].x+1;
100
          p[i].x = p[i].y; p[i].y = j;
101
        }
102
         addedge();
103
        rep(i,0,SZ(p)) p[i].x=n-p[i].x+1;
104
         addedge();
105
         sort(all(e));
         rep(i,1,Q+1) ne[i].clear(),f[i]=i;
107
        rep(i,0,SZ(e)) {
108
           int j=e[i].s,k=e[i].t;
109
           if (find(j)!=find(k)) f[f[j]]=f[k],ne[j].pb(k),ne[k].pb(j);
110
        }
        10=1[1];r0=r[1];
111
        init(10,r0);
113
        dfs(1,0);
114
     }
115 }
116
```

```
117 int main() {
118     scanf("%d",&Mo::n);
119     for (int i=1;i<=Mo::n;i++) scanf("%d",a+i);
120     scanf("%d",&Mo::Q);
121     rep(i,1,Mo::Q+1) scanf("%d%d",&Mo::1[i],&Mo::r[i]);
122     Mo::solve();
123     rep(i,1,Mo::Q+1) printf("%d\n",Mo::ans[i]);
124 }</pre>
```

2.18 psegt.cpp

```
1 struct node {
             node *1, *r;
             ll val, sz, add;
4 };
    void pull(node *u) {
             u->sz = 0, u->val = 0:
             if (u->1) u->sz += u->1->sz, u->val += u->1->val;
             if (u\rightarrow r) u\rightarrow sz += u\rightarrow r\rightarrow sz, u\rightarrow val += u\rightarrow r\rightarrow val;
10 }
11
    void push(node *u) {
12
13
             if (u->add) {
                       if (u->1) {
14
                                node *p = new node();
15
16
                                *p = *u ->1;
                                u \rightarrow 1 = p;
17
18
                                p->add += u->add;
                                p->val += p->sz * u->add;
19
                       }
20
                       if (u->r) {
21
22
                                node *p = new node();
23
                                *p = *u->r;
24
                                u->r = p;
25
                                p->add += u->add;
                                p->val += p->sz * u->add;
27
                      }
28
                       u->add = 0;
29
             }
30 }
31
32 node *build(int 1, int r) {
```

```
33
            node *p = new node();
34
            p->add = 0;
35
            if (1 == r) {
36
                     p->1 = p->r = nullptr;
37
                    p->val = a[1];
38
                     p->sz = 1;
            } else {
                     int mid = (1 + r) >> 1;
41
                    p->1 = build(1, mid);
42
                     p \rightarrow r = build(mid + 1, r);
43
                     pull(p);
44
            }
45
            return p;
46 }
47
    ll query(node *v, int l, int r, int ql, int qr) {
49
            if (ql == 1 && qr == r) {
50
                     return v->val:
51
            } else {
52
                     push(v);
53
                     int mid = (1 + r) >> 1;
54
                     if (ar <= mid)
55
                             return query(v->1, 1, mid, q1, qr);
56
                     else if (ql > mid)
57
                             return query(v->r, mid + 1, r, ql, qr);
                     else
                             return query(v->1, 1, mid, q1, mid) + query(v->r,
                                  mid + 1, r, mid + 1, qr);
            }
61 }
62
    node *modify(node *v, int 1, int r, int q1, int qr, 11 x) {
64
            if (ql == 1 && qr == r) {
65
                    node *p = new node();
66
                     *p = *v;
67
                     p->add += x;
                     p\rightarrow val += p\rightarrow sz * x;
                     return p;
70
            } else {
71
                     push(v);
72
                     int mid = (1 + r) >> 1;
73
                    node *p = new node();
74
                     *p = *v;
```

```
if (qr <= mid)
75
                            p->1 = modify(v->1, 1, mid, ql, qr, x);
76
                    else if (al > mid)
77
78
                            p->r = modify(v->r, mid + 1, r, ql, qr, x);
79
                    else
                            p->1 = modify(v->1, 1, mid, ql, mid, x),
80
                                             p->r = modify(v->r, mid + 1, r, mid
81
                                                 + 1, qr, x);
82
                    pull(p);
83
                    return p;
84
            }
85 }
```

2.19 rollbackMo.cpp

```
1 int n, q, k, block;
2 int cnt[maxn], ans[maxn], a[maxn], vis[maxn];
   vector<array<int, 4>> que;
  int getb(int x) {
        return (x - 1) / block + 1:
7 }
   int main() {
        std::ios::sync with stdio(false);
10
       cin.tie(0); cout.tie(0);
11
12
13
       cin >> n:
14
       block = sqrt(n);
15
16
       rep(i, 1, n) cin >> a[i];
17
       cin >> q;
18
       rep(i, 1, q) {
19
            int 1, r;
            cin >> 1 >> r >> k:
20
            que.pb({1, r, i, k});
21
22
       sort(ALL(que), [&](array<int, 4> a, array<int, 4> b)->bool{
23
            if (getb(a[0]) != getb(b[0]))
24
                return getb(a[0]) < getb(b[0]);</pre>
25
26
            else
27
                return a[1] < b[1];
28
       });
```

```
29
30
        int len = que.size();
31
        int 1. r:
32
        auto add = [&](int x, int t) {
33
            cnt[vis[a[x]]]--:
34
            vis[a[x]]++;
35
            cnt[vis[a[x]]]++;
36
       }:
        auto del = [\&](int x) {
37
38
            cnt[vis[a[x]]]--:
39
            vis[a[x]]--;
40
            cnt[vis[a[x]]]++;
41
       }:
42
43
       for (int x = 0: x < len:) {
44
45
            while (y < len && getb(que[y][0]) == getb(que[x][0])) y++;
            //暴力块内
46
            while (x < y \&\& que[x][1] \le getb(que[x][0])*block) {
47
                for (int j = que[x][0]; j \le que[x][1]; j++)
48
49
                    add(j, que[x][3]);
                ans[que[x][2]] = cnt[que[x][3]];
51
                for (int j = que[x][0]; j \le que[x][1]; j++)
52
                    del(j);
53
                x++:
            }
54
            //块外
            r = getb(que[x][0]) * block;
57
            while (x < y) {
58
                1 = getb(que[x][0]) * block + 1;
                while (r < que[x][1]) r++, add(r, que[x][3]);
                while (1 > que[x][0]) 1--, add(1, que[x][3]);
                ans[que[x][2]] = cnt[que[x][3]];
61
                for (int j = que[x][0]; j \le getb(que[x][0])*block; j++)
62
63
                    del(j);
64
                x++;
65
            for (int j = getb(que[x - 1][0]) * block + 1; j <= que[x - 1][1]; j
66
                ++)
67
                del(j);
       }
       rep(i, 1, q) cout << ans[i] << '\n';
70 }
```

2.20 segtree.cpp

```
struct info {
           ll sum;
            int sz;
            friend info operator+(const info &a, const info &b) {
                    return {(a.sum + b.sum) % mod. a.sz + b.sz}:
           }
7 }:
    struct tag {
10
           ll add. mul:
11
            friend tag operator+(const tag &a, const tag &b) {
                    tag res = {(a.add * b.mul + b.add) % mod. a.mul * b.mul %
12
                        mod}:
                    return res;
13
15 };
   info operator+(const info &a, const tag &b) {
17
            return {(a.sum * b.mul + a.sz * b.add) % mod, a.sz};
18 }
19
   struct node {
21
           info val:
            tag t;
   } seg[maxn << 2];</pre>
24
   void update(int id) {
26
            seg[id].val = seg[id * 2].val + seg[id * 2 + 1].val;
27 }
   void settag(int id, tag t) {
            seg[id].val = seg[id].val + t;
29
            seg[id].t = seg[id].t + t;
30
31 }
   void pushdown(int id) {
33
            if (seg[id].t.mul == 1 and seg[id].t.add == 0) return:
            settag(id * 2, seg[id].t);
34
35
            settag(id * 2 + 1, seg[id].t);
            seg[id].t.mul = 1;
36
            seg[id].t.add = 0;
37
38 }
   void build(int 1, int r, int id) {
40
            seg[id].t = {0, 1};
41
           if (1 == r) {
```

```
42
                    seg[id].val = {a[1], 1};
43
           } else {
44
                    int mid = (1 + r) >> 1:
45
                    build(1, mid, id * 2);
                    build(mid + 1, r, id * 2 + 1);
46
47
                    update(id);
48
           }
49 }
    void change(int 1, int r, int id, int q1, int qr, tag t) {
51
            if (1 == q1 && r == qr) {
52
                    settag(id, t);
53
           } else {
54
                    int mid = (1 + r) >> 1:
55
                    pushdown(id);
56
                    if (qr <= mid) {
57
                            change(1, mid, id * 2, q1, qr, t);
                    } else if (ql > mid) {
                            change(mid + 1, r, id * 2 + 1, ql, qr, t);
                    } else {
61
                            change(1, mid, id * 2, al, mid, t):
62
                            change (mid + 1, r, id * 2 + 1, mid + 1, qr, t);
                    }
                    update(id):
65
           }
66 }
   info query(int 1, int r, int id, int q1, int qr) {
            if (1 == q1 && r == qr) {
                    return seg[id].val;
70
           } else {
71
                    int mid = (1 + r) >> 1:
72
                    pushdown(id);
73
                    if (qr <= mid)
74
                            return query(1, mid, id * 2, q1, qr);
75
                    else if (ql > mid)
76
                            return query(mid + 1, r, id * 2 + 1, ql, qr);
77
                    else
                            return query(1, mid, id * 2, ql, mid) +
                                        query(mid + 1, r, id * 2 + 1, mid + 1, qr)
79
                                            );
           }
81 }
82 ll search(int l, int r, int id, int ql, int qr, int d) {
83
            if (ql == 1 && qr == r) {
```

```
84
                     int mid = (1 + r) / 2:
                     // if (l != r) pushdown(id); ...
 85
                     if (seg[id].val < d)</pre>
                              return -1;
                      else {
                              if (1 == r)
                                       return 1;
                              else if (seg[id * 2].val >= d)
 91
                                       return search(1, mid, id * 2, ql, mid, d);
                              else
 94
                                       return search(mid + 1, r, id * 2 + 1, mid +
                                           1, qr, d);
                     }
 95
 96
             } else {
                     int mid = (1 + r) >> 1:
 97
 98
                     // pushdown(id); ...
                      if (qr <= mid)</pre>
100
                              return search(1, mid, id * 2, q1, qr, d);
101
                      else if (ql > mid)
                              return search(mid + 1, r, id * 2 + 1, ql, qr, d);
102
103
                      else {
                              int tmp = search(1, mid, id * 2, ql, mid, d);
104
                              if (tmp != -1)
105
106
                                       return tmp;
107
                              else
                                       return search(mid + 1, r, id * 2 + 1, mid +
108
                                           1, qr, d);
109
                     }
110
111 }
```

2.21 segtreefast.cpp

```
1  /**
2  * Author: Lucian Bicsi
3  * Description: Very fast and quick segment tree.
4  * Only useful for easy invariants. O-indexed.
5  * Range queries are half-open.
6  */
7  #pragma once
8
9  struct SegmTree {
10  vector<int> T; int n;
```

```
11
      SegmTree(int n) : T(2 * n, (int)2e9), n(n) {}
12
13
      void Update(int pos, int val) {
14
       for (T[pos += n] = val; pos > 1; pos /= 2)
         T[pos / 2] = min(T[pos], T[pos ^ 1]);
15
16
     }
17
     int Query(int b, int e) {
18
19
       int res = (int)2e9;
       for (b += n, e += n; b < e; b /= 2, e /= 2) {
20
21
         if (b \% 2) res = min(res, T[b++]);
22
         if (e % 2) res = min(res, T[--e]);
23
       }
24
       return res;
25
26 };
```

2.22 SparseTable.cpp

```
1 template <typename T, class F = function <T(const T&, const T&)>>
2 class SparseTable {
3 public:
4
            int n:
            vector<vector<T>> mat;
            F func;
            SparseTable(const vector<T>& a, const F& f) : func(f) {
9
                    n = static_cast<int>(a.size());
10
                    int max log = 32 - builtin clz(n);
11
                    mat.resize(max log):
12
                    mat[0] = a:
13
                    for (int j = 1; j < max log; <math>j++) {
14
                            mat[j].resize(n - (1 << j) + 1);
                            for (int i = 0; i \le n - (1 \le j); i++) {
15
                                    mat[j][i] = func(mat[j - 1][i], mat[j - 1][i
                                          + (1 << (i - 1))]);
17
                            }
18
                    }
           }
19
21
           T get(int from, int to) const {
22
                    assert(0 <= from && from <= to && to <= n - 1);
23
                    int lg = 32 - __builtin_clz(to - from + 1) - 1;
```

```
24 return func(mat[lg][from], mat[lg][to - (1 << lg) + 1]);
25 }
26 };
```

2.23 SparseTable2D.cpp

```
1 // lg[1] = 0;
2 // rep(i, 2, N-1) {
          lq[i] = lq[i / 2] + 1;
5 // int k = log2(r - l + 1); very slow!!!
6 // int k = _- lg(r - l + 1);
7 // int k = lq[r - l + 1];
8 // int k = 32 - builtin clz(r - l + 1) - 1;
9 vector<vector<int>> sparse[12];
11 int query(int x, int y, int d) {
12
           int k = __lg(d);
13
           int s = d - bit(k);
           return min({sparse[k][x][y], sparse[k][x + s][y], sparse[k][x][y + s
14
               ], sparse[k][x + s][y + s]);
15 }
16
17 void build() {
           rep(i, 1, n) rep(j, 1, m) sparse[0][i][j] = mat[i][j];
18
19
           rep(k, 1, 11) rep(i, 1, n) rep(j, 1, m) {
20
                   int d = bit(k - 1);
21
                   if (i + d > n \mid | j + d > m) continue;
                    sparse[k][i][j] = min({sparse[k - 1][i][j], sparse[k - 1][i]
22
                       + d][j], sparse[k - 1][i][j + d], sparse[k - 1][i + d][j
                        + d]});
           }
23
24 }
```

2.24 treap.cpp

```
1  /**
2  * author: tourist
3  * created: 07.10.2022 20:32:03
4  **/
5  #include <bits/stdc++.h>
6
7  using namespace std;
```

```
8
9 #ifdef LOCAL
10 #include "algo/debug.h"
11 #else
12 #define debug(...) 42
13 #endif
14
   mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
16
17 class node {
   public:
     int id;
     node* 1:
21
     node* r;
     node* p;
     bool rev;
     int sz;
     // declare extra variables:
26
     long long P;
27
     long long add;
28
      long long x;
29
30
     node(int _id, long long _x) {
31
      id = _id;
32
       l = r = p = nullptr;
       rev = false;
       sz = 1:
       // init extra variables:
       P = rng();
37
       add = 0:
38
        x = _x;
39
40
41
      // push everything else:
42
     void push_stuff() {
43
       if (add != 0) {
44
          if (1 != nullptr) {
45
           1->unsafe_apply(add);
46
         }
47
          if (r != nullptr) {
           r->unsafe_apply(add);
         }
49
50
          add = 0;
```

```
}
52
     }
53
54
     void unsafe reverse() {
       push_stuff();
55
       rev ^= 1;
56
57
       swap(1, r);
       pull();
58
59
     }
60
61
      // apply changes:
62
      void unsafe_apply(long long delta) {
       add += delta:
63
64
       x += delta;
     }
65
66
67
      void push() {
       if (rev) {
68
69
          if (l != nullptr) {
            1->unsafe_reverse();
70
71
72
         if (r != nullptr) {
           r->unsafe_reverse();
73
74
         }
75
         rev = 0:
76
       push_stuff();
77
78
     }
79
      void pull() {
80
81
       sz = 1;
82
       if (l != nullptr) {
         1->p = this;
83
84
         sz += 1->sz;
85
       if (r != nullptr) {
         r->p = this;
87
         sz += r->sz;
88
     }
90
91
92
93 void debug_node(node* v, string pref = "") {
```

```
94 #ifdef LOCAL
      if (v != nullptr) {
         debug_node(v->r, pref + "\");
 97
        cerr << pref << "-" << "<sub>||</sub>" << v->id << '\n';
         debug_node(v->1, pref + "\");
      } else {
100
         cerr << pref << "-" << "nullptr" << '\n';</pre>
101
102 #endif
103 }
104
    namespace treap {
107
     pair < node * , int > find (node * v , const function < int (node *) > &go to) {
108
       // go to returns: 0 -- found; -1 -- go left; 1 -- go right
109
      // find returns the last vertex on the descent and its go_to
110
      if (v == nullptr) {
111
         return {nullptr, 0};
112
113
      int dir:
114
       while (true) {
115
       v->push():
116
        dir = go_to(v);
117
        if (dir == 0) {
118
           break:
119
120
         node* u = (dir == -1 ? v -> 1 : v -> r);
121
        if (u == nullptr) {
122
           break;
123
        }
124
         v = u;
125
126
       return {v, dir};
127 }
128
129 node* get_leftmost(node* v) {
       return find(v, [&](node*) { return -1; }).first;
131 }
132
133 node* get_rightmost(node* v) {
       return find(v, [&](node*) { return 1; }).first;
135 }
136
```

```
node* get_kth(node* v, int k) { // O-indexed
       pair<node*, int> p = find(v, [&](node * u) {
138
         if (u->1 != nullptr) {
139
140
           if (u->1->sz > k) {
             return -1:
141
          }
142
143
          k = u > 1 > sz;
144
        if (k == 0) {
145
          return 0:
146
        }
147
        k--;
148
149
        return 1:
150
      });
       return (p.second == 0 ? p.first : nullptr);
151
152 }
153
     int get_pos(node* v) { // O-indexed
154
       int k = (v->1 != nullptr ? v->1->sz : 0);
155
       while (v->p != nullptr) {
156
        if (v == v -> p -> r) {
157
158
          if (v->p->l != nullptr) {
159
160
           k += v->p->l->sz;
161
          }
162
        }
         v = v -> p;
163
164
165
       return k;
166 }
167
168
    node* get_root(node* v) {
       while (v->p != nullptr) {
169
170
        v = v -> p;
      }
171
172
       return v;
173 }
174
175
     pair<node*, node*> split(node* v, const function<bool(node*)> &is_right) {
176
      if (v == nullptr) {
        return {nullptr, nullptr};
177
      }
178
     v->push();
179
```

```
180
       if (is_right(v)) {
181
         pair < node * , node * > p = split(v->1, is right);
182
         if (p.first != nullptr) {
183
           p.first->p = nullptr;
184
         }
185
         v \rightarrow 1 = p.second;
186
         v->pull();
187
         return {p.first, v};
188
      } else {
189
         pair < node *, node *> p = split(v->r, is_right);
190
         v->r = p.first;
191
         if (p.second != nullptr) {
192
           p.second->p = nullptr;
193
         }
194
         v->pull();
195
         return {v, p.second};
196
197 }
198
     pair<node*, node*> split_cnt(node* v, int k) {
       if (v == nullptr) {
201
         return {nullptr, nullptr};
202
      }
203
       v->push();
204
       int left_and_me = (v\rightarrow l != nullptr ? v\rightarrow l\rightarrow sz : 0) + 1;
205
       if (k < left and me) {</pre>
206
         pair < node * , node *> p = split_cnt(v->1, k);
207
         if (p.first != nullptr) {
208
           p.first->p = nullptr;
209
210
         v->1 = p.second;
211
         v->pull();
212
         return {p.first, v};
213
      } else {
214
         pair<node*, node*> p = split_cnt(v->r, k - left_and_me);
215
         v->r = p.first;
216
         if (p.second != nullptr) {
217
           p.second->p = nullptr;
218
         }
219
         v->pull();
220
         return {v, p.second};
221
222 }
```

```
223
     node* merge(node* v, node* u) {
       if (v == nullptr) {
225
226
          return u;
       }
227
       if (u == nullptr) {
228
229
          return v;
230
       }
231
       if (v->P > u->P) {
            if (rnq() \% (v\rightarrow sz + u\rightarrow sz) < (unsigned int) v\rightarrow sz) {
232
          v->push();
233
          v \rightarrow r = merge(v \rightarrow r, u);
234
          v->pull();
235
236
          return v;
       } else {
237
238
          u->push();
          u \rightarrow 1 = merge(v, u \rightarrow 1);
239
240
          u->pull();
          return u;
241
       }
242
243 }
244
     int count left(node* v. const function<bool(node*)> &is right) {
245
       if (v == nullptr) {
246
          return 0:
247
       }
248
       v->push();
249
       if (is_right(v)) {
250
251
          return count_left(v->1, is_right);
252
        return (v->1 != nullptr ? v->1->sz : 0) + 1 + count left(v->r, is right);
253
254 }
255
     int count_less(node* v, long long val) {
256
       int res = 0;
257
       while (v != nullptr) {
258
          v->push();
259
          if (v\rightarrow x >= val) {
260
            v = v -> 1:
261
         } else {
262
            res += (v->1 != nullptr ? v->1->sz : 0) + 1;
263
            v = v -> r:
264
         }
265
```

```
266
267
       return res;
268 }
269
270
     node* add(node* r, node* v, const function<bool(node*)> &go_left) {
271
       pair<node*, node*> p = split(r, go_left);
272
       return merge(p.first, merge(v, p.second));
273 }
274
     node* remove(node* v) { // returns the new root
276
       v->push();
277
       node* x = v->1;
278
       node* y = v -> r;
279
       node* p = v -> p;
280
       v \rightarrow l = v \rightarrow r = v \rightarrow p = nullptr;
281
       v->push();
282
       v->pull(); // now v might be reusable...
       node* z = merge(x, y);
284
       if (p == nullptr) {
285
         if (z != nullptr) {
286
           z->p = nullptr;
287
288
         return z:
289
       }
290
       if (p->1 == v) {
291
         p->1 = z;
      }
292
293
       if (p->r == v) {
294
         p->r = z;
295
296
       while (true) {
297
         p->push();
298
         p->pull();
299
         if (p->p == nullptr) {
300
           break;
301
         }
302
         p = p->p;
303
304
       return p;
305 }
306
     node* next(node* v) {
308
       if (v->r == nullptr) {
```

```
309
         while (v->p != nullptr && v->p->r == v) {
310
           v = v -> p;
311
         }
312
         return v->p;
       }
313
314
       v->push();
315
       v = v -> r;
       while (v->1 != nullptr) {
316
317
         v->push();
         v = v -> 1:
318
       }
319
320
       return v;
321 }
322
     node* prev(node* v) {
323
324
       if (v->1 == nullptr) {
         while (v\rightarrow p != nullptr \&\& v\rightarrow p\rightarrow l == v) {
325
326
           v = v -> p;
327
         }
328
         return v->p;
329
       }
330
       v->push();
331
       v = v -> 1:
332
       while (v->r != nullptr) {
333
         v->push();
         v = v -> r;
334
       }
335
336
       return v;
337 }
338
     int get_size(node* v) {
339
       return (v != nullptr ? v->sz : 0);
340
341 }
342
    template < typename . . . T>
343
     void Apply(node* v, T... args) {
344
       v->unsafe_apply(args...);
345
346 }
347
348 void reverse(node* v) {
       v->unsafe reverse();
349
350 }
351
```

```
352 // extra of mine
353 long long lower(node* u, long long x) {
      if (u == nullptr)
355
        return numeric_limits<long long>::min();
356
      else if (x \le u -> x)
357
        return lower(u->1, x);
358
359
        return max(u->x, lower(u->r, x));
360 }
361
     long long upper(node* u, long long x) {
      if (u == nullptr)
364
       return numeric_limits<long long>::max();
      else if (u->x <= x)
365
366
        return upper(u->r, x);
367
368
         return min(u->x, upper(u->1, x));
369 }
370
371 } // namespace treap
372
    using namespace treap;
374
375 int n;
376
377 int main() {
      ios::sync_with_stdio(false);
379
      cin.tie(0);
380
      node* root = nullptr;
381
       cin >> n:
382
      for (int i = 1; i <= n; i++) {
383
        int op;
384
        long long x;
385
        cin >> op >> x;
386
        switch (op) {
387
           case 1: {
388
             root = add(root, new node(x, x), [&](node * u) {
389
               return x < u->x;
390
            });
391
             break;
392
           }
393
           case 2: {
394
             auto [pt, w] = find(root, [&](node * u) {
```

```
395
                if (x < u \rightarrow x) return -1;
                else if (x == u->x) return 0;
396
                else return 1:
397
398
              });
              assert(w == 0):
399
              root = remove(pt);
400
401
              break;
402
403
            case 3: {
              cout << count less(root, x) + 1 << '\n':</pre>
404
              break;
405
           }
            case 4: {
407
408
              cout << get kth(root, x - 1)->x << '\n';
409
              break:
           }
410
            case 5: {
411
              cout << lower(root, x) << '\n':</pre>
412
413
              break;
           }
414
415
            case 6: {
              cout << upper(root, x) << '\n';</pre>
416
417
              break:
           }
418
419
420
421 }
```

2.25 树哈希.cpp

```
1 basic_string<int> e[maxn];
2 ull hashv[maxn];
3 ull seed1, seed2, seed3, seed4;
4
5 ull f(ull x) { return x * x * x * seed1 + x * seed2; }
6 ull h(ull x) { return f(x) ^ ((x & seed3) >> 31) ^ ((x & seed4) << 31); }
7
8 void dfs1(int u, int fa) {
9    hashv[u] = 1;
10    for (auto v : e[u]) if (v != fa) {
11         dfs1(v, u);
12         hashv[u] += h(hashv[v]);
13    }</pre>
```

```
14 }
15
16 void dfs2(int u. int fa. ull fv) {
17 // for each root
       hashv[u] += fv:
       for (auto v : e[u]) if (v != fa) {
               dfs2(v, u, h(hashv[u] - h(hashv[v])));
21
22 }
23
24 void solve() {
       seed1 = rng(), seed2 = rng();
       seed3 = rng(), seed4 = rng();
27
    cin >> n;
28
       rep(i, 2, n) {
           int u, v;
           cin >> u >> v;
31
           e[u].pb(v);
           e[v].pb(u);
       }
       dfs1(1, 0);
       sort(hashv + 1, hashv + n + 1):
       n = unique(hashv + 1, hashv + n + 1) - hashv - 1;
       cout << n << '\n';
38 }
```

2.26 树链剖分 segtree.cpp

```
int n, m, a[N];
vector<int> e[N];
int l[N], r[N], idx[N];
int sz[N], hs[N], tot, top[N], dep[N], fa[N];

struct info {
    int maxv, sum;
};

info operator + (const info &l, const info &r) {
    return (info){max(l.maxv, r.maxv), l.sum + r.sum};
}

struct node {
    info val;
```

```
16 } seg[N * 4];
17
18 // [l. r]
19
   void update(int id) {
            seg[id].val = seg[id * 2].val + seg[id * 2 + 1].val;
21
22 }
23
   void build(int id, int 1, int r) {
           if (1 == r) {
25
                    // 1号点, DFS序中第1个点
26
                    seg[id].val = {a[idx[1]], a[idx[1]]};
27
28
           } else {
29
                    int mid = (1 + r) / 2;
30
                   build(id * 2, 1, mid):
                    build(id * 2 + 1, mid + 1, r);
31
32
                    update(id);
34 }
35
    void change(int id, int 1, int r, int pos, int val) {
37
           if (1 == r) {
                    seg[id].val = {val, val};
38
39
           } else {
40
                    int mid = (1 + r) / 2:
                    if (pos <= mid) change(id * 2, 1, mid, pos, val);</pre>
41
                    else change(id * 2 + 1, mid + 1, r, pos, val);
                    update(id);
44
           }
45 }
46
   info query(int id, int 1, int r, int q1, int qr) {
           if (1 == ql && r == qr) return seg[id].val;
48
49
           int mid = (1 + r) / 2;
50
            if (qr <= mid) return query(id * 2, 1, mid, ql, qr);</pre>
51
            else if (ql > mid) return query(id * 2 + 1, mid + 1, r, ql,qr);
            else {
52
53
                    return query(id * 2, 1, mid, ql, mid) +
54
                            query(id * 2 + 1, mid + 1, r, mid + 1, qr);
55
           }
56 }
58 // 第一遍 DFS, 子树大小, 重儿子, 父亲, 深度
```

```
void dfs1(int u.int f) {
60
            sz[u] = 1;
61
            hs[u] = -1:
62
            fa[u] = f;
            dep[u] = dep[f] + 1;
 64
            for (auto v : e[u]) {
                     if (v == f) continue;
                    dfs1(v. u):
 67
                     sz[u] += sz[v];
                     if (hs[u] == -1 \mid | sz[v] > sz[hs[u]])
                             hs[u] = v;
 70
            }
71 }
 73 // 第二遍 DFS, 每个点 DFS 序, 重链上的链头的元素。
 74 void dfs2(int u, int t) {
            top[u] = t;
            l[u] = ++tot:
 77
            idx[tot] = u;
            if (hs[u] != -1) {
 79
                     dfs2(hs[u], t);
            for (auto v : e[u]) {
                     if (v != fa[u] && v != hs[u]) {
                             dfs2(v, v):
 84
                     }
            }
            r[u] = tot;
87 }
 89 int LCA(int u, int v) {
             while (top[u] != top[v]) {
91
                     if (dep[top[u]] < dep[top[v]]) v = fa[top[v]];</pre>
                     else u = fa[top[u]];
93
94
            if (dep[u] < dep[v]) return u;</pre>
             else return v:
 96 }
97
98 info query(int u,int v) {
99
            info ans{(int)-1e9, 0};
100
            while (top[u] != top[v]) {
101
                     if (dep[top[u]] < dep[top[v]]) {</pre>
```

```
ans = ans + query(1, 1, n, l[top[v]], l[v]);
102
                             v = fa[top[v]];
103
                     } else {
104
105
                             ans = ans + query(1, 1, n, l[top[u]], l[u]);
                             u = fa[top[u]];
106
                     }
107
108
             if (dep[u] \le dep[v]) ans = ans + query(1, 1, n, l[u], l[v]);
109
110
             else ans = ans + query(1, 1, n, 1[v], 1[u]);
111
             return ans:
112 }
```

2.27 笛卡尔树.cpp

```
int a[maxn], l[maxn], r[maxn], root;
   int ans[maxn], tot;
   void build() {
       stack<int> stk;
       for (int i = 1: i <= n: i++) {
           int last = 0:
           while (!stk.empty() && a[stk.top()] > a[i]) {
                last = stk.top();
10
                stk.pop();
           }
11
12
            if (stk.empty())
13
                root = i;
14
            else
                r[stk.top()] = i;
15
           l[i] = last:
16
17
            stk.push(i);
18
       }
19 }
20
   void dfs(int c, int L, int R) {
       ans[c] = ++tot;
       if (l[c]) dfs(l[c], L, c - 1);
23
24
       if (r[c]) dfs(r[c], c + 1, R);
25 }
```

2.28 线段树合并.cpp

```
1 struct node {
```

```
int sz, sum;
3
            node *1, *r;
            node() : sz(0), sum(0), l(nullptr), r(nullptr) {}
5 } pool[N * 20], *cur = pool;
7 node *newnode() {
            return cur++;
9 }
10
11 void upd(node *rt) {
12
            if (not rt) return;
13
            rt->sum = rt->sz > 0;
            if (rt->1) rt->sum += rt->1->sum:
            if (rt->r) rt->sum += rt->r->sum;
15
16 }
17
    node *modify(node *rt, int 1, int r, int pos, int d) {
19
            if (not rt) rt = newnode():
20
            if (1 == r) {
21
                     rt->sz += d:
22
                     upd(rt);
23
                     return rt:
24
            } else {
25
                     int md = (1 + r) >> 1;
26
                     if (pos <= md)
27
                              rt->1 = modify(rt->1, 1, md, pos, d);
                     else
29
                              rt \rightarrow r = modify(rt \rightarrow r, md + 1, r, pos, d);
30
                     upd(rt);
31
                     return rt;
32
            }
33 }
34
    node *merge(node *u, node *v, int 1, int r) {
36
            if (not u) return v;
37
            if (not v) return u;
            if (1 == r) {
39
                     u->sz += v->sz;
40
                     upd(u);
41
                     return u;
42
            } else {
43
                     int md = (1 + r) >> 1;
44
                     u \rightarrow 1 = merge(u \rightarrow 1, v \rightarrow 1, 1, md);
```

```
u \rightarrow r = merge(u \rightarrow r, v \rightarrow r, md + 1, r);
45
                     upd(u);
46
47
                     return u;
48
            }
49 }
50
51
    11 query(node *rt, int 1, int r) {
            if (not rt) return 0;
53
            return rt->sum;
54 }
55
    pair<node *, node *> split(node *rt, int 1, int r, int ql, int qr) {
            if (not rt) return {nullptr, nullptr};
57
58
            if (ql == 1 && qr == r) {
                     return {nullptr, rt};
59
60
            } else {
                     int md = (1 + r) >> 1;
61
62
                     if (ar <= md) {
                             auto [p1, p2] = split(rt->1, 1, md, q1, qr);
63
                             rt->1 = p1;
64
65
                             upd(rt);
                             if (not p2) return {rt, nullptr};
66
                             node *u = newnode();
67
68
                             u ->1 = p2;
69
                             upd(u);
                             return {rt, u};
                    } else if (ql > md) {
71
72
                             auto [p1, p2] = split(rt->r, md + 1, r, ql, qr);
73
                             rt->r = p1;
                             upd(rt);
74
75
                             if (not p2) return {rt, nullptr};
76
                             node *u = newnode();
77
                             u->r = p2;
78
                             upd(u);
                             return {rt, u};
79
                    } else {
                             auto [p1, p2] = split(rt->1, 1, md, q1, md);
81
                             auto [p3, p4] = split(rt->r, md + 1, r, md + 1, qr);
                             rt -> 1 = p1, rt -> r = p3;
84
                             upd(rt);
                             if (not p2 and not p4) return {rt, nullptr};
85
                             node *u = newnode();
87
                             u->1 = p2, u->r = p4;
```

3 DP

3.1 Convex hull optimization.cpp

```
1 array<11, 3> a[maxn];
2 int q[maxn];
3 11 ans[maxn];
5 11 X(int p) {
        return 211 * a[p][0];
7 }
8 11 Y(int p) {
        return a[p][0] * a[p][0] + a[p][1];
10 }
11 ldb slope(int x, int y) {
12
        return (1db)(Y(y) - Y(x)) / (X(y) - X(x));
13 }
14 void solve() {
       cin >> n:
16
       int head = 1, rear = 0;
17
       rep(i, 1, n) {
18
           cin >> a[i][0] >> a[i][1];
19
           a[i][2] = i:
20
       }
21
       sort(a + 1, a + n + 1);
22
23
       rep(i, 1, n) {
24
            while (head < rear && slope(q[rear], i) <= slope(q[rear], q[rear -
                1])) rear--;
25
           q[++rear] = i;
       }
26
27
       rep(i, 1, n) {
28
           11 k = -a[i][0]:
29
            while (head < rear && slope(q[head], q[head + 1]) <= k) head++;
30
           ans[a[i][2]] = (a[i][0] + a[q[head]][0]) * (a[i][0] + a[q[head]][0])
                 + a[i][1] + a[q[head]][1];
```

```
31 }
32 rep(i, 1, n) cout << ans[i] << '\n';
33 }
```

3.2 DivideAndConquerDP.cpp

```
1  11 w[N][N], sum[N][N], opt[N], dp[805][N];
2
3  11 calc(int i,int j) { return sum[j][j]-sum[j][i]-sum[i][j]+sum[i][i]; }
4
5  void rec(int d,int 1,int r,int opt1,int optr) {
6    if (1>r) return;
7    int md=(1+r)>>1;
8    rep(i,opt1,optr) if (dp[d-1][i]+calc(i,md)<dp[d][md]) {
9        dp[d][md]=dp[d-1][i]+calc(i,md);
10        opt[md]=i;
11    }
12    rec(d,1,md-1,opt1,opt[md]);
13    rec(d,md+1,r,opt[md],optr);
14 }</pre>
```

3.3 有依赖决策单调.cpp

```
pair<int, int> stk[N];
    auto calc = [\&] (int i, int j) \{\ldots\} // dp[i] \rightarrow dp[i]
3 int h = 0, t = 0:
   stk[t++] = \{1, 0\}; // \{left, opt\}
6 for (int i = 1; i \le n; i++) {
        if (h < t && stk[h].first < i) stk[h].first++:</pre>
        if (h + 1 < t && stk[h].first >= stk[h + 1].first) ++h;
        dp[i] = calc(i, stk[h].second);
        while (h < t \&\& calc(stk[t - 1].first. stk[t - 1].second) >= calc(stk[t - 1].second)
10
            - 1].first, i))
11
            --t:
12
        if (h < t) {
13
            int l = stk[t - 1].first, r = n + 1;
14
            while (1 + 1 < r) {
                 int md = (1 + r) >> 1;
15
                 if (calc(md. stk[t - 1].second) < calc(md. i)) l = md: else r =
                     md:
17
18
            if (r \le n) stk[t++] = \{r, i\}:
```

```
19 } else stk[t++] = {i, i};
20 }
```

4 Geometry

4.1 1 (1).cpp

```
1 typedef double db;
   const db EPS = 1e-9;
3
   inline int sign(db a) { return a < -EPS ? -1 : a > EPS; }
5
    inline int cmp(db a, db b) { return sign(a - b); }
   struct P {
            db x, y;
            P() {}
10
11
            P(db \ x, db \ y) : x(x), y(y) \{\}
12
            P operator+(P p) { return \{x + p.x, y + p.y\}; }
            P operator-(P p) { return \{x - p.x, y - p.y\}; \}
            P operator*(db d) { return \{x * d, y * d\}; }
14
            P operator/(db d) { return \{x / d, y / d\}; }
15
16
17
            bool operator < (P p) const {</pre>
                    int c = cmp(x, p.x);
19
                    if (c) return c == -1;
20
                    return cmp(y, p.y) == -1;
21
            }
22
23
            bool operator == (P o) const {
24
                    return cmp(x, o.x) == 0 && cmp(y, o.y) == 0;
25
            }
26
27
            db dot(P p) { return x * p.x + y * p.y; }
28
            db det(P p) { return x * p.y - y * p.x; }
29
30
            db distTo(P p) { return (*this - p).abs(); }
31
            db alpha() { return atan2(y, x); }
32
            void read() { cin >> x >> v: }
33
            void write() {cout << "(" << x << "," << y << ")" << endl;}</pre>
34
            db abs() { return sqrt(abs2());}
35
            db abs2() { return x * x + y * y; }
```

```
36
           P rot90() { return P(-y, x);}
           P unit() { return *this / abs(); }
37
           int quad() const { return sign(y) == 1 || (sign(y) == 0 && sign(x)
39
           Prot(db an) { return \{x * \cos(an) - v * \sin(an), x * \sin(an) + v * \sin(an)\}
               cos(an)}: }
40 };
42 #define cross(p1,p2,p3) ((p2.x-p1.x)*(p3.y-p1.y)-(p3.x-p1.x)*(p2.y-p1.y))
   #define crossOp(p1,p2,p3) sign(cross(p1,p2,p3))
45 // 直线 p1p2, q1q2 是否恰有一个交点
46 bool chkLL(P p1, P p2, P q1, P q2) {
47
           db a1 = cross(q1, q2, p1), a2 = -cross(q1, q2, p2);
           return sign(a1 + a2) != 0:
48
49 }
51 // 求直线 p1p2, q1q2 的交点
52 P isLL(P p1, P p2, P q1, P q2) {
           db a1 = cross(q1, q2, p1), a2 = -cross(q1, q2, p2);
54
           return (p1 * a2 + p2 * a1) / (a1 + a2);
55 }
57 // 判断区间 [l1, r1], [l2, r2] 是否相交
58 bool intersect(db 11, db r1, db 12, db r2) {
           if (11 > r1) swap(11, r1); if (12 > r2) swap(12, r2);
           return !( cmp(r1, 12) == -1 \mid | cmp(r2, 11) == -1 );
61 }
62
63 // 线段 p1p2, q1q2 相交
64 bool isSS(P p1, P p2, P q1, P q2) {
65
           return intersect(p1.x, p2.x, q1.x, q2.x) && intersect(p1.y, p2.y, q1
               .v, q2.v) &&
66
                 crossOp(p1, p2, q1) * crossOp(p1, p2, q2) <= 0 && crossOp(q1,
                      q2, p1)
                 * crossOp(q1, q2, p2) <= 0;
70 // 线段 p1p2, q1q2 严格相交
71 bool isSS_strict(P p1, P p2, P q1, P q2) {
           72
               q2, p1)
73
                 * crossOp(q1, q2, p2) < 0;
```

```
74 }
 75
 76 // m 在 a 和 b 之间
 77 bool isMiddle(db a, db m, db b) {
            /*if (a > b) swap(a, b):
 79
            return \ cmp(a, m) \le 0 \ \&\& \ cmp(m, b) \le 0;*/
            return sign(a - m) == 0 || sign(b - m) == 0 || (a < m != b < m);
 81 }
 83 bool isMiddle(Pa. Pm. Pb) {
 84
            return isMiddle(a.x, m.x, b.x) && isMiddle(a.y, m.y, b.y);
 85 }
 87 // 点 p 在线段 p1p2 上
 88 bool onSeg(P p1, P p2, P q) {
            return crossOp(p1, p2, q) == 0 && isMiddle(p1, q, p2);
 90 }
 91 // a1a2 和 p1p2 的交点 在 p1p2 上?
 93 // 点 p 严格在 p1p2 上
 94 bool onSeg_strict(P p1, P p2, P q) {
            return crossOp(p1, p2, q) == 0 \&\& sign((q - p1).dot(p1 - p2)) * sign
                ((q - p2).dot(p1 - p2)) < 0:
 96 }
 98 // 求 q 到 直线 p1p2 的投影 (垂足) : p1 != p2
 99 P proj(P p1, P p2, P q) {
100
            P dir = p2 - p1;
101
            return p1 + dir * (dir.dot(q - p1) / dir.abs2());
102 }
103
|104 // 求 q 以 直线p1p2 为轴的反射
105 P reflect(P p1, P p2, P q) {
            return proj(p1, p2, q) * 2 - q;
107 }
108
| 109 // 求 q 到 线段p1p2 的最小距离
110 db nearest(P p1, P p2, P q) {
111
            if (p1 == p2) return p1.distTo(q);
112
            P h = proj(p1, p2, q);
113
            if (isMiddle(p1, h, p2))
114
                   return q.distTo(h);
115
            return min(p1.distTo(q), p2.distTo(q));
```

```
116 }
117
118 // 求 线段p1p2 与 线段q1q2 的距离
119 db disSS(P p1, P p2, P q1, P q2) {
            if (isSS(p1, p2, q1, q2)) return 0;
120
            return min(min(nearest(p1, p2, q1), nearest(p1, p2, q2)), min(
121
                nearest(q1, q2, p1), nearest(q1, q2, p2)));
122 }
123
124 // 极角排序
125 sort(p, p + n, [&](P a, P b) {
            int qa = a.quad(), qb = b.quad();
126
127
            if (qa != qb) return qa < qb;
128
            else return sign(a.det(b)) > 0;
129 }):
```

4.2 1 (2).cpp

```
db area(vector<P> ps){
            db ret = 0; rep(i,0,ps.size()) ret += ps[i].det(ps[(i+1)\%ps.size()])
3
            return ret/2;
4 }
   int contain(vector <P> ps, P p){ //2:inside,1:on seq,0:outside
            int n = ps.size(), ret = 0;
            rep(i,0,n){
                    P u=ps[i],v=ps[(i+1)%n];
10
                    if(onSeg(u,v,p)) return 1;
11
                    if(cmp(u.v.v.v) \le 0) swap(u.v):
12
                    if (cmp(p.y,u.y) > 0 \mid | cmp(p.y,v.y) \le 0) continue;
13
                    ret ^= crossOp(p,u,v) > 0;
14
            }
15
            return ret*2;
16 }
17
18
    vector<P> convexHull(vector<P> ps) {
19
            int n = ps.size(); if(n <= 1) return ps;</pre>
20
            sort(ps.begin(), ps.end());
21
            vector < P > qs(n * 2): int k = 0:
            for (int i = 0; i < n; qs[k++] = ps[i++])
22
23
                     while (k > 1 \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) \le 0)
                         --k:
```

```
24
            for (int i = n - 2, t = k; i \ge 0; qs[k++] = ps[i--])
25
                    while (k > t \&\& crossOp(qs[k-2], qs[k-1], ps[i]) \le 0)
26
            qs.resize(k - 1);
27
            return qs;
28 }
29
    vector<P> convexHullNonStrict(vector<P> ps) {
31
            //caution: need to unique the Ps first
32
            int n = ps.size(); if(n <= 1) return ps;</pre>
33
            sort(ps.begin(), ps.end());
34
            vector < P > qs(n * 2); int k = 0;
            for (int i = 0; i < n; as[k++] = ps[i++])
35
36
                    while (k > 1 \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) < 0) --
                         k:
37
            for (int i = n - 2, t = k; i \ge 0; qs[k++] = ps[i--])
                     while (k > t \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) < 0) --
39
            qs.resize(k - 1);
40
            return qs;
41 }
42
    db convexDiameter(vector < P > ps) {
44
            int n = ps.size(); if (n \le 1) return 0;
45
            int is = 0, js = 0; rep(k,1,n) is = ps[k] < ps[is]?k:is, js = ps[js] <
                 ps[k]?k:js;
            int i = is, j = js;
            db ret = ps[i].distTo(ps[j]);
47
            do{
49
                    if((ps[(i+1)\%n]-ps[i]).det(ps[(j+1)\%n]-ps[j]) >= 0)
50
                             (++i)%=n;
51
                     else
52
                             (++i)%=n:
                    ret = max(ret,ps[i].distTo(ps[j]));
53
54
            }while(i!=is || j!=js);
            return ret:
56 }
57
    vector<P> convexCut(const vector<P>&ps, P q1, P q2) {
59
            vector <P> qs;
60
            int n = ps.size();
61
            rep(i,0,n){
62
                    P p1 = ps[i], p2 = ps[(i+1)%n];
```

```
63
                     int d1 = crossOp(q1,q2,p1), d2 = crossOp(q1,q2,p2);
                     if(d1 >= 0) qs.push back(p1);
 64
                     if(d1 * d2 < 0) qs.push_back(isLL(p1,p2,q1,q2));
 66
             }
 67
             return qs;
 68 }
 69
     void reorderPolygon(vector<P> &ps) {
 71
         size t pos = 0;
         for(size_t i = 1; i < ps.size(); i++){</pre>
 72
 73
             if(ps[i].y < ps[pos].y \mid | (ps[i].y == ps[pos].y && ps[i].x < ps[pos]
                 1.x))
                 pos = i:
 74
 75
         }
 76
         rotate(ps.begin(), ps.begin() + pos, ps.end());
 77 }
 78
     vector<P> minkowski(vector<P> p. vector<P> a){
 80
         if(p.empty()) return q;
         // the first vertex must be the lowest
 81
 82
         reorderPolygon(p);
         reorderPolygon(a):
 83
         // must ensure cyclic indexing
 84
 85
         p.push_back(p[0]);
 86
         p.push_back(p[1]);
 87
         q.push back(q[0]);
         q.push_back(q[1]);
         // main part
 90
         vector<P> result;
 91
         size t i = 0, i = 0:
 92
         while(i < p.size() - 2 \mid j < q.size() - 2){
 93
             result.push_back(p[i] + q[j]);
             auto cross = (p[i + 1] - p[i]).det(q[i + 1] - q[i]);
 94
 95
             if(cross \geq 0 \&\& i < SZ(p) - 2)
                 ++i:
 96
 97
             if(cross \le 0 \&\& j \le SZ(q) - 2)
 98
                 ++j;
100
         return result:
101 }
102
    bool convexContain(const vector<P> &1, P p, bool strict = true) {
104
         int a = 1, b = l.size() - 1, r = !strict;
```

```
105
         if (1.size() < 3) return r && onSeg(1[0], 1.back(), p);
106
         if (crossOp(1[0], 1[a], 1[b]) > 0) swap(a, b);
107
         if (cross0p(1[0], 1[a], p) >= r \mid | cross0p(1[0], 1[b], p) <= -r)
108
             return false:
109
         while (abs(a - b) > 1) {
110
             int c = (a + b) / 2:
111
             (crossOp(1[0], 1[c], p) > 0 ? b : a) = c;
112
113
         return sign(cross(l[a], l[b], p)) < r;
114 }
```

4.3 1 (3).cpp

```
1 int type(P o1,db r1,P o2,db r2){
 2
                                     db d = o1.distTo(o2);
                                     if(cmp(d,r1+r2) == 1) return 4;
                                     if(cmp(d,r1+r2) == 0) return 3;
 5
                                     if(cmp(d,abs(r1-r2)) == 1) return 2;
                                     if(cmp(d,abs(r1-r2)) == 0) return 1;
 7
                                     return 0;
 8 }
          vector<P> isCL(P o,db r,P p1,P p2){
11
                                     if (cmp(abs((o-p1).det(p2-p1)/p1.distTo(p2)),r)>0) return {};
12
                                     db x = (p1-o) \cdot dot(p2-p1), y = (p2-p1) \cdot abs2(), d = x * x - y * ((p1-o) \cdot abs2())
                                                  ).abs2() - r*r):
13
                                     d = max(d,(db)0.0); P m = p1 - (p2-p1)*(x/y), dr = (p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(sqrt(d)/p2-p1)*(
14
                                     return \{m-dr, m+dr\}; //along dir: p1->p2
15 }
16
17 vector <P is CC (P o1, db r1, P o2, db r2) { //need to check whether two
                          circles are the same
18
                                     db d = o1.distTo(o2);
19
                                     if (cmp(d, r1 + r2) == 1) return {}:
20
                                     if (cmp(d,abs(r1-r2))==-1) return {};
21
                                     d = min(d, r1 + r2);
                                     db v = (r1 * r1 + d * d - r2 * r2) / (2 * d), x = sqrt(r1 * r1 - v * d)
22
                                                     v);
                                     P dr = (o2 - o1).unit():
23
                                     P q1 = o1 + dr * v, q2 = dr.rot90() * x;
24
25
                                     return {q1-q2,q1+q2};//along circle 1
26 }
```

```
27
   // extanCC, intanCC : -r2, tanCP : r2 = 0
    vector<pair<P. P>> tanCC(P o1. db r1. P o2. db r2) {
30
            P d = o2 - o1;
31
            db dr = r1 - r2, d2 = d.abs2(), h2 = d2 - dr * dr:
32
            if (sign(d2) == 0 | | sign(h2) < 0) return \{\};
33
            h2 = max((db)0.0, h2);
           vector<pair<P, P>> ret;
34
35
            for (db sign : {-1, 1}) {
                    P v = (d * dr + d.rot90() * sqrt(h2) * sign) / d2;
36
37
                    ret.push_back(\{01 + v * r1, 02 + v * r2\});
38
           }
39
            if (sign(h2) == 0) ret.pop_back();
40
            return ret;
41 }
42
   db rad(P p1,P p2){
            return atan2l(p1.det(p2),p1.dot(p2));
45 }
46
   db areaCT(db r, P p1, P p2){
           vector\langle P \rangle is = isCL(P(0,0),r,p1,p2);
48
            if(is.empty()) return r*r*rad(p1,p2)/2;
49
50
            bool b1 = cmp(p1.abs2(),r*r) == 1, b2 = cmp(p2.abs2(),r*r) == 1;
51
           if(b1 && b2){
                    P md=(is[0]+is[1])/2;
52
                    if(sign((p1-md).dot(p2-md)) <= 0)
                            return r*r*(rad(p1,is[0]) + rad(is[1],p2))/2 + is
54
                                 [0].det(is[1])/2;
                    else return r*r*rad(p1,p2)/2;
55
56
           }
57
            if(b1) return (r*r*rad(p1,is[0]) + is[0].det(p2))/2;
            if(b2) return (p1.det(is[1]) + r*r*rad(is[1],p2))/2;
58
59
            return p1.det(p2)/2;
60 }
61
62 PinCenter(PA. PB. PC) {
            double a = (B - C).abs(), b = (C - A).abs(), c = (A - B).abs();
64
            return (A * a + B * b + C * c) / (a + b + c):
65 }
67 P circumCenter(P a. P b. P c) {
68
           P bb = b - a, cc = c - a;
```

```
69
            double db = bb.abs2(), dc = cc.abs2(), d = 2 * bb.det(cc);
            return a - P(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
70
71 }
72
73 P othroCenter(P a, P b, P c) {
74
            P ba = b - a, ca = c - a, bc = b - c;
            double Y = ba.v * ca.v * bc.v,
76
            A = ca.x * ba.y - ba.x * ca.y,
77
            x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
78
            y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
79
            return {x0, y0};
80 }
81
82 pair < P, db > min circle(vector < P > ps) {
       random_shuffle(ps.begin(), ps.end());
       int n = ps.size();
       P \circ = ps[0]; db r = 0;
       rep(i,1,n) if (o.distTo(ps[i]) > r + EPS){
87
            o = ps[i], r = 0;
           rep(j,0,i) if(o.distTo(ps[j]) > r + EPS){
                o = (ps[i] + ps[j]) / 2; r = o.distTo(ps[i]);
                rep(k,0,i) if (o.distTo(ps[k]) > r + EPS){
91
                     o = circumCenter(ps[i],ps[j],ps[k]);
                     r = o.distTo(ps[i]);
92
93
               }
94
            }
       }
       return {o,r};
97 }
```

4.4 all.cpp

```
typedef double db;
const db EPS = 1e-9;

inline int sign(db a) { return a < -EPS ? -1 : a > EPS; }

inline int cmp(db a, db b){ return sign(a-b); }

struct P {
    db x, y;
    P() {}
    P(db _x, db _y) : x(_x), y(_y) {}
}
```

```
12
        P operator+(P p) { return \{x + p.x, y + p.y\}; \}
        P operator-(P p) { return {x - p.x, y - p.y}; }
13
        P operator*(db d) { return \{x * d, v * d\}: }
14
15
        P operator/(db d) { return \{x / d, y / d\}; }
16
17
        bool operator<(P p) const {</pre>
18
            int c = cmp(x, p.x);
            if (c) return c == -1:
19
20
            return cmp(v, p.v) == -1;
21
       }
22
23
        bool operator == (P o) const{
            return cmp(x.o.x) == 0 && cmp(v.o.v) == 0:
24
25
       }
26
27
        db dot(P p) { return x * p.x + y * p.y; }
        db det(P p) { return x * p.y - y * p.x; }
28
29
        db distTo(P p) { return (*this-p).abs(); }
30
        db alpha() { return atan2(y, x); }
31
        void read() { cin>>x>>y; }
32
33
        void write() {cout<<"("<<x<<"."<<v<<")"<<endl:}</pre>
34
        db abs() { return sgrt(abs2());}
        db abs2() { return x * x + y * y; }
35
36
        P rot90() { return P(-v.x):}
        P unit() { return *this/abs(); }
37
38
        int quad() const { return sign(y) == 1 \mid | (sign(y) == 0 \&\& sign(x) >= 0)
            : }
39
        P rot(db an) { return \{x*\cos(an)-y*\sin(an),x*\sin(an) + y*\cos(an)\}; }
40 }:
41
   struct L{ //ps[0] -> ps[1]
        P ps[2]:
43
44
        P& operator[](int i) { return ps[i]; }
45
        P dir() { return ps[1] - ps[0]; }
46
        bool include(P p) { return sign((ps[1] - ps[0]).det(p - ps[0])) > 0; }
47
        L push(){ // push eps outward
            const double eps = 1e-6;
            P delta = (ps[1] - ps[0]).rot90().unit() * eps;
50
            return {{ps[0] - delta, ps[1] - delta}};
       }
51
52 }:
53
```

```
54 #define cross(p1,p2,p3) ((p2.x-p1.x)*(p3.y-p1.y)-(p3.x-p1.x)*(p2.y-p1.y))
55 #define crossOp(p1,p2,p3) sign(cross(p1,p2,p3))
57 bool chkLL(P p1, P p2, P q1, P q2) {
        db a1 = cross(q1, q2, p1), a2 = -cross(q1, q2, p2);
       return sign(a1+a2) != 0;
60 }
61
62 P isLL(P p1, P p2, P q1, P q2) {
       db a1 = cross(q1, q2, p1), a2 = -cross(q1, q2, p2);
       return (p1 * a2 + p2 * a1) / (a1 + a2);
65 }
66
67 P isLL(L 11,L 12) { return isLL(11[0],11[1],12[0],12[1]); }
69 bool intersect(db 11,db r1,db 12,db r2){
       if(11>r1) swap(11,r1); if(12>r2) swap(12,r2);
       return !( cmp(r1,12) == -1 \mid | cmp(r2,11) == -1 );
72 }
73
74 bool isSS(P p1, P p2, P q1, P q2){
       return intersect(p1.x.p2.x.q1.x.q2.x) && intersect(p1.v.p2.v.q1.v.q2.v)
76
        crossOp(p1,p2,q1) * crossOp(p1,p2,q2) \le 0 \&\& crossOp(q1,q2,p1)
77
                * crossOp(q1,q2,p2) <= 0:
78 }
   bool isSS strict(P p1, P p2, P q1, P q2){
81
       return crossOp(p1,p2,q1) * crossOp(p1,p2,q2) < 0 && crossOp(q1,q2,p1)
82
                * crossOp(q1,q2,p2) < 0;
83 }
84
85 bool isMiddle(db a. db m. db b) {
       return sign(a - m) == 0 \mid \mid sign(b - m) == 0 \mid \mid (a < m != b < m);
87 }
89 bool isMiddle(Pa. Pm. Pb) {
       return isMiddle(a.x, m.x, b.x) && isMiddle(a.y, m.y, b.y);
91 }
93 bool onSeg(P p1, P p2, P q){
       return crossOp(p1,p2,q) == 0 && isMiddle(p1, q, p2);
95 }
```

```
96
    bool onSeg strict(P p1, P p2, P q){
 98
         return crossOp(p1,p2,q) == 0 && sign((q-p1).dot(p1-p2)) * sign((q-p2).
             dot(p1-p2)) < 0;
 99 }
100
101 P proj(P p1, P p2, P q) {
         P dir = p2 - p1;
102
103
         return p1 + dir * (dir.dot(q - p1) / dir.abs2());
104 }
105
    P reflect(P p1, P p2, P q){
107
         return proj(p1,p2,q) * 2 - q;
108 }
109
    db nearest(P p1,P p2,P q){
110
111
         P h = proj(p1,p2,q);
112
         if(isMiddle(p1,h,p2))
113
             return q.distTo(h);
         return min(p1.distTo(q),p2.distTo(q));
114
115 }
116
117 db disSS(P p1, P p2, P q1, P q2){
118
         if(isSS(p1,p2,q1,q2)) return 0;
119
         return min(min(nearest(p1,p2,q1),nearest(p1,p2,q2)), min(nearest(q1,q2,
             p1), nearest(q1,q2,p2)));
120 }
121
122 db rad(P p1,P p2){
123
         return atan21(p1.det(p2).p1.dot(p2)):
124 }
125
    db incircle(P p1, P p2, P p3){
126
127
         db A = p1.distTo(p2);
         db B = p2.distTo(p3);
128
129
         db C = p3.distTo(p1);
         return sqrtl(A*B*C/(A+B+C));
130
131 }
132
133 //polygon
134
    db area(vector <P> ps){
135
         db ret = 0; rep(i,0,ps.size()) ret += ps[i].det(ps[(i+1)\%ps.size()]);
136
```

```
137
         return ret/2:
138 }
139
140
     int contain(vector < P > ps, P p) { //2: inside, 1: on seq, 0: outside
141
         int n = ps.size(), ret = 0:
142
         rep(i,0,n){
143
             P u=ps[i], v=ps[(i+1)%n];
144
             if(onSeg(u,v,p)) return 1;
145
             if (cmp(u.v,v.v) \le 0) swap(u,v);
146
             if (cmp(p.y,u.y) > 0 \mid | cmp(p.y,v.y) \le 0) continue;
147
             ret ^= crossOp(p,u,v) > 0;
148
         }
149
         return ret*2:
150 }
151
152
    vector<P> convexHull(vector<P> ps) {
153
         int n = ps.size(); if(n <= 1) return ps;</pre>
154
         sort(ps.begin(), ps.end());
155
         vectorP> qs(n * 2); int k = 0;
156
         for (int i = 0; i < n; qs[k++] = ps[i++])
157
             while (k > 1 \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) \le 0) --k;
158
         for (int i = n - 2, t = k; i \ge 0; qs[k++] = ps[i--])
159
             while (k > t \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) \le 0) --k;
160
         qs.resize(k - 1);
161
         return as:
162 }
163
     vector<P> convexHullNonStrict(vector<P> ps) {
165
         //caution: need to unique the Ps first
166
         int n = ps.size(); if(n <= 1) return ps;</pre>
167
         sort(ps.begin(), ps.end());
168
         vector < P > qs(n * 2); int k = 0;
169
         for (int i = 0; i < n; qs[k++] = ps[i++])
170
             while (k > 1 \&\& cross0p(qs[k - 2], qs[k - 1], ps[i]) < 0) --k;
171
         for (int i = n - 2, t = k; i \ge 0; qs[k++] = ps[i--])
172
             while (k > t \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) < 0) --k;
173
         qs.resize(k - 1):
174
         return qs;
175 }
176
    db convexDiameter(vector < P > ps) {
178
         int n = ps.size(); if(n <= 1) return 0;</pre>
179
         int is = 0, js = 0; rep(k,1,n) is = ps[k] < ps[is]?k:is, js = ps[js] < ps[is]
```

```
k]?k:js;
180
         int i = is, j = js;
         db ret = ps[i].distTo(ps[j]);
181
182
         do√
             if((ps[(i+1)\%n]-ps[i]).det(ps[(j+1)\%n]-ps[j]) >= 0)
183
                 (++i)%=n:
184
185
             else
                 (++i)%=n:
186
             ret = max(ret,ps[i].distTo(ps[j]));
187
         }while(i!=is || i!=is):
188
189
         return ret;
190 }
191
192
     vector<P> convexCut(const vector<P>&ps, P q1, P q2) {
193
         vector<P> as:
194
         int n = ps.size();
195
         rep(i,0,n){
196
             P p1 = ps[i], p2 = ps[(i+1)%n];
197
             int d1 = crossOp(q1,q2,p1), d2 = crossOp(q1,q2,p2);
             if(d1 >= 0) qs.pb(p1);
198
199
             if(d1 * d2 < 0) qs.pb(isLL(p1,p2,q1,q2));
         }
200
201
         return qs;
202 }
203
204
     //min dist
205
     db min dist(vector<P>&ps,int 1,int r){
206
207
         if(r-1<=5){
208
             db ret = 1e100:
             rep(i,l,r) rep(j,l,i) ret = min(ret,ps[i].distTo(ps[j]));
209
210
             return ret:
         }
211
         int m = (l+r) >> 1;
212
213
         db ret = min(min_dist(ps,1,m),min_dist(ps,m,r));
214
         vector < P > qs; rep(i,l,r) if(abs(ps[i].x-ps[m].x) <= ret) qs.pb(ps[i]);
215
         sort(qs.begin(), qs.end(),[](Pa,Pb) -> bool {return a.y<b.y; });</pre>
         rep(i,1,qs.size()) for(int j=i-1;j>=0&&qs[j].y>=qs[i].y-ret;--j)
216
217
             ret = min(ret,qs[i].distTo(qs[j]));
218
         return ret:
219 }
220
221 int type (P o1, db r1, P o2, db r2) {
```

```
222
         db d = o1.distTo(o2):
223
         if(cmp(d,r1+r2) == 1) return 4;
224
         if(cmp(d,r1+r2) == 0) return 3:
225
         if(cmp(d,abs(r1-r2)) == 1) return 2;
226
         if(cmp(d.abs(r1-r2)) == 0) return 1:
227
         return 0:
228 }
229
230
     vector<P> isCL(P o,db r,P p1,P p2){
231
         db x = (p1-o).dot(p2-p1), y = (p2-p1).abs2(), d = x * x - y * ((p1-o).
             abs2() - r*r);
232
         if(sign(d) < 0) return {};</pre>
233
         d = max(d,0.0); P = p1 - (p2-p1)*(x/y), dr = (p2-p1)*(sqrt(d)/y);
234
         return {m-dr,m+dr}; //along dir: p1->p2
235 }
236
237 vector<P> isCC(P o1, db r1, P o2, db r2) { //need to check whether two
         circles are the same
         db d = o1.distTo(o2):
238
         if (cmp(d, r1 + r2) == 1) return {}:
239
240
         d = min(d, r1 + r2);
241
         db \ v = (r1 * r1 + d * d - r2 * r2) / (2 * d), \ x = sqrt(r1 * r1 - v * v);
242
         P dr = (o2 - o1).unit():
243
         P q1 = o1 + dr * v, q2 = dr.rot90() * x;
244
         return {q1-q2,q1+q2}; //along circle 1
245 }
246
    vector<P> tanCP(P o, db r, P p) {
248
         db x = (p - o).abs2(), d = x - r * r;
249
         if (sign(d) <= 0) return {}: // on circle => no tangent
250
         P q1 = o + (p - o) * (r * r / x);
251
         P q2 = (p - o).rot90() * (r * sqrt(d) / x);
252
         return {q1-q2,q1+q2}; //counter clock-wise
253 }
254
255
     vector<L> extanCC(P o1, db r1, P o2, db r2) {
257
         vector<L> ret;
258
         if (cmp(r1, r2) == 0) {
259
             P dr = (o2 - o1).unit().rot90() * r1;
260
             ret.pb(\{\{01 + dr, 02 + dr\}\}), ret.pb(\{\{01 - dr, 02 - dr\}\});
261
         } else {
262
             P p = (o2 * r1 - o1 * r2) / (r1 - r2);
```

```
263
             vector < P > ps = tanCP(o1, r1, p), qs = tanCP(o2, r2, p);
             rep(i,0,min(ps.size(),qs.size())) ret.pb({{ps[i], qs[i]}}); //c1
264
                 counter-clock wise
265
        }
266
         return ret:
267 }
268
     vector<L> intanCC(P o1. db r1. P o2. db r2) {
269
270
         vector<L> ret;
         P p = (o1 * r2 + o2 * r1) / (r1 + r2):
271
272
         vector\langle P \rangle ps = tanCP(o1,r1,p), qs = tanCP(o2,r2,p);
         rep(i,0,min(ps.size(),qs.size())) ret.pb({{ps[i], qs[i]}}); //c1 counter
273
274
         return ret;
275 }
276
277
    db areaCT(db r, P p1, P p2){
278
         vector < P > is = isCL(P(0.0).r.p1.p2):
279
         if(is.empty()) return r*r*rad(p1,p2)/2;
         bool b1 = cmp(p1.abs2(),r*r) == 1, b2 = cmp(p2.abs2(),r*r) == 1;
280
281
         if(b1 && b2){
             if(sign((p1-is[0]).dot(p2-is[0])) \le 0 \&\&
282
                 sign((p1-is[0]).dot(p2-is[0])) <= 0)
283
             return r*r*(rad(p1,is[0]) + rad(is[1],p2))/2 + is[0].det(is[1])/2;
284
285
             else return r*r*rad(p1,p2)/2;
286
         if(b1) return (r*r*rad(p1,is[0]) + is[0].det(p2))/2;
287
         if(b2) return (p1.det(is[1]) + r*r*rad(is[1],p2))/2;
288
289
         return p1.det(p2)/2;
290 }
291
     bool parallel(L 10, L 11) { return sign( 10.dir().det( 11.dir() ) ) == 0; }
293
294
    bool sameDir(L 10, L 11) { return parallel(10, 11) && sign(10.dir().dot(11.
         dir()) ) == 1; }
295
     bool cmp (Pa, Pb) {
296
         if (a.quad() != b.quad()) {
297
298
             return a.quad() < b.quad();</pre>
299
        } else {
             return sign(a.det(b)) > 0;
300
        }
301
302 }
```

```
303
304
     bool operator < (L 10, L 11) {</pre>
305
         if (sameDir(10, 11)) {
306
             return 11.include(10[0]);
307
        } else {
308
             return cmp( 10.dir(), 11.dir() );
309
        }
310 }
311
312 bool check(L u, L v, L w) {
313
         return w.include(isLL(u,v));
314 }
315
    vector<P> halfPlaneIS(vector<L> &1) {
316
317
         sort(l.begin(), l.end()):
318
         deque<L> q;
319
         for (int i = 0; i < (int)1.size(); ++i) {
320
             if (i && sameDir(l[i], l[i - 1])) continue:
321
             while (q.size() > 1 && !check(q[q.size() - 2], q[q.size() - 1], 1[i])
                 ])) q.pop_back();
322
             while (q.size() > 1 && !check(q[1], q[0], l[i])) q.pop_front();
323
             g.push back(l[i]):
324
        }
325
         while (q.size() > 2 && !check(q[q.size() - 2], q[q.size() - 1], q[0])) q
             .pop_back();
326
         while (q.size() > 2 && !check(q[1], q[0], q[q.size() - 1])) q.pop_front
327
         vector<P> ret:
328
         for (int i = 0; i < (int)q.size(); ++i) ret.push_back(isLL(q[i], q[(i +
             1) % a.size()])):
329
        return ret;
330 }
331
332
    P inCenter(P A. P B. P C) {
333
         double a = (B - C).abs(), b = (C - A).abs(), c = (A - B).abs();
334
         return (A * a + B * b + C * c) / (a + b + c);
335 }
336
337 P circumCenter(P a, P b, P c) {
338
        P bb = b - a, cc = c - a:
339
         double db = bb.abs2(), dc = cc.abs2(), d = 2 * bb.det(cc);
340
         return a - P(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
341 }
```

```
342
    P othroCenter(P a, P b, P c) {
343
        P ba = b - a, ca = c - a, bc = b - c;
344
345
        double Y = ba.y * ca.y * bc.y,
        A = ca.x * ba.y - ba.x * ca.y
346
        x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
347
        y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
348
        return {x0, y0};
349
350 }
```

4.5 圆面积并.cpp

```
db intergal(db x,db y,db r,db L,db R){
        return r*r*(R-L) + x*r*(sinl(R) - sinl(L)) + y*r*(-cosl(R) + cosl(L));
3 }
4
   db calc area circle(P c,db r,db L,db R){
            return intergal(c.x,c.y,r,L,R) / 2;
7 }
   db norm(db x){
            while(x < 0) x += 2 * PI;
10
            while(x > 2 * PI) x -= 2 * PI;
11
12
            return x;
13 }
14
15
   P cs[N]; db rs[N];
16
    void work(){
17
            vector<int> cand = {};
18
19
            rep(i,0,m){
20
                    bool ok = 1;
21
                    rep(j,0,m) if(i!=j){
22
                             if(rs[j] > rs[i] + EPS \&\& rs[i] + cs[i].distTo(cs[j])
                                 1) <= rs[i] + EPS){</pre>
23
                                     ok = 0; break;
24
25
                             if(cs[i] == cs[j] \&\& cmp(rs[i],rs[j]) == 0 \&\& j < i)
                                 {
26
                                     ok = 0: break:
27
                             }
28
                    }
29
                    if(ok) cand.pb(i);
```

```
30
            }
31
32
            rep(i,0,cand.size()) cs[i] = cs[cand[i]], rs[i] = rs[cand[i]];
33
            m = cand.size();
34
35
            db area = 0;
36
37
            //work
38
            rep(i,0,m){
                     vector<pair<db,int>> ev = {{0,0},{2*PI,0}};
39
40
41
                    int cur = 0;
42
43
                    rep(j,0,m) if(j!=i){
44
                             auto ret = isCC(cs[i],rs[i],cs[j],rs[j]);
                             if(!ret.empty()){
45
46
                                     db l = (ret[0] - cs[i]).alpha();
47
                                     db r = (ret[1] - cs[i]).alpha();
48
                                     1 = norm(1); r = norm(r);
49
                                     ev.pb({1,1}); ev.pb({r,-1});
50
                                     if(1 > r) ++cur;
51
                            }
                    }
52
53
54
                     sort(ev.begin(), ev.end());
                     rep(j,0,ev.size() - 1){
56
                             cur += ev[j].se;
                            if(cur == 0){
57
58
                                     area += calc_area_circle(cs[i],rs[i],ev[j].
                                         fi,ev[j+1].fi);
59
                            }
                    }
61
            }
62 }
```

5 Graph

5.1 bellmanford.cpp

```
vector<PII> e[N];

template <typename T>
```

```
4 void add(int u, int v, T w) {
           e[u].eb(v, w);
6 }
8 template <typename T>
   vector<T> bellmanford(vector<pair<int, T>> *g, int start) {
            // assert(0 <= start && start < q.n);
10
11
            // maybe use inf = numeric limits<T>::max() / 4
            const T inf = numeric limits<T>::max() / 4;
12
            vector<T> dist(n, inf):
13
14
           dist[start] = 0;
15
           int cnt = 0;
            while (true) {
16
17
                    bool upd = 0;
18
                    cnt++:
19
                    for (int i = 0; i < n; i++) {
                            for (auto [to, cost] : e[i]) {
20
                                    if (dist[to] > dist[i] + cost) {
21
22
                                            upd = 1;
                                            dist[to] = dist[i] + cost:
23
24
                                    }
25
                            }
                   }
26
                    if (!upd || cnt == n) {
27
28
                            break:
                   }
29
30
            return dist;
31
32
            // returns inf if there's no path
33 }
```

5.2 BlockCutTree.cpp

```
1 struct BlockCutTree {
2    int n;
3    std::vector<std::vector<int>> adj;
4    std::vector<int>> dfn, low, stk;
5    int cnt, cur;
6    std::vector<std::pair<int, int>> edges;
7
8    BlockCutTree() {}
9    BlockCutTree(int n) {
10    init(n);
```

```
11
       }
12
13
        void init(int n) {
14
            this -> n = n;
15
            adj.assign(n, {});
16
            dfn.assign(n, -1);
17
            low.resize(n);
18
            stk.clear():
            cnt = cur = 0;
19
20
            edges.clear():
21
       }
22
23
        void addEdge(int u, int v) {
24
            adj[u].push back(v);
25
            adj[v].push_back(u);
26
       }
27
28
        void dfs(int x) {
29
            stk.push_back(x);
            dfn[x] = low[x] = cur++;
30
31
32
            for (auto y : adj[x]) {
33
                if (dfn[v] == -1) {
34
                    dfs(y);
35
                    low[x] = std::min(low[x], low[y]);
36
                    if (low[v] == dfn[x]) {
37
                        int v:
                        do {
39
                            v = stk.back();
40
                            stk.pop_back();
41
                             edges.emplace_back(n + cnt, v);
42
                        } while (v != y);
43
                         edges.emplace_back(x, n + cnt);
44
                         cnt++;
                    }
45
46
                } else {
                    low[x] = std::min(low[x], dfn[y]);
47
48
49
            }
50
       }
51
52
        std::pair<int, std::vector<std::pair<int, int>>> work() {
53
            for (int i = 0; i < n; i++) {
```

```
54
                if (dfn[i] == -1) {
55
                    stk.clear();
                    dfs(i):
56
57
                }
            }
58
59
            return {cnt, edges};
60
61 }:
   5.3 dijfast.cpp
1 vector<PII> e[N];
   template <typename T>
   void add(int u, int v, T w) {
            e[u].eb(v, w);
   template <typename T>
   vector<T> dijkstra(vector<pair<int, T>> *g, int start) {
10
            // assert(0 <= start && start < q.n);
            // maybe use inf = numeric limits <T>::max() / 4
11
12
            vector<T> dist(n, numeric_limits<T>::max());
            priority queue<pair<T, int>, vector<pair<T, int>>, greater<pair<T,</pre>
13
                int>>> s;
            dist[start] = 0:
14
            s.emplace(dist[start], start);
15
            while (!s.empty()) {
16
                    T expected = s.top().first;
17
                    int i = s.top().second;
18
19
                    s.pop();
20
                    if (dist[i] != expected) {
                             continue:
21
22
                    for (auto [to, cost] : g[i]) {
23
24
                            if (dist[i] + cost < dist[to]) {</pre>
25
                                     dist[to] = dist[i] + cost;
26
                                     s.emplace(dist[to], to);
27
                            }
                    }
28
29
            }
```

// returns numeric limits <T>::max() if there's no path

30

31

```
5.4 dijkstra.cpp
```

32 }

```
1 vector <PII > e[N];
3 template <typename T>
4 void add(int u, int v, T w) {
            e[u].eb(v, w);
6 }
   template <typename T>
    vector<T> dijkstra(vector<pair<int, T>> *g, int start) {
10
            // assert(0 <= start && start < q.n);
11
            // maybe use inf = numeric limits <T>::max() / 4
12
            const T inf = numeric_limits<T>::max();
13
            vector<T> dist(n, inf);
14
            vector<int> was(n, 0);
15
            dist[start] = 0;
            while (true) {
16
17
                    int cur = -1:
18
                    for (int i = 0; i < n; i++) {
                            if (was[i] || dist[i] == inf) continue;
19
20
                            if (cur == -1 || dist[i] < dist[cur]) {
21
                                     cur = i:
22
23
                    }
24
                    if (cur == -1 || dist[cur] == inf) {
25
                            break;
                    }
26
27
                    was[cur] = 1;
28
                    for (auto [to, cost] : g[cur]) {
29
                            dist[to] = min(dist[to], dist[cur] + cost);
30
                    }
31
            }
            return dist;
            // returns inf if there's no path
34 }
```

5.5 dinic.cpp

```
1 template < typename T>
2 struct FlowGraph {
```

```
static const int V = 1015:
        static const int E = 100015;
       int s. t. vtot:
       int head[V], etot;
       int dis[V], cur[V];
       struct edge {
           int v, nxt;
           T f:
10
11
       e[E * 2];
       void addedge(int u, int v, T f) {
12
13
           e[etot] = {v, head[u], f};
14
           head[u] = etot++;
           e[etot] = {u, head[v], 0};
15
           head[v] = etot++;
16
17
       }
       bool bfs() {
18
19
           for (int i = 1; i <= vtot; i++) {
                dis[i] = 0:
20
                cur[i] = head[i];
21
           }
22
23
            queue < int > q;
24
           q.push(s); dis[s] = 1;
           while (!q.empty()) {
25
                int u = q.front(); q.pop();
26
27
               for (int i = head[u]: i != -1: i = e[i].nxt) {
                    if (e[i].f && !dis[e[i].v]) {
28
29
                        int v = e[i].v;
                       dis[v] = dis[u] + 1;
30
31
                       if (v == t) return true;
32
                        q.push(v);
                   }
33
               }
34
           }
35
36
           return false;
37
       }
38
       T dfs(int u, T m) {
           if (u == t) return m;
           T flow = 0;
           for (int i = cur[u]; i != -1; cur[u] = i = e[i].nxt) {
41
42
                if (e[i].f && dis[e[i].v] == dis[u] + 1) {
                   T f = dfs(e[i].v, min(m, e[i].f));
43
                   e[i].f -= f;
44
45
                    e[i ^ 1].f += f;
```

```
46
                    m -= f:
47
                   flow += f;
                    if (!m) break;
48
49
               }
           }
50
           if (!flow) dis[u] = -1;
51
           return flow;
53
       }
       T dinic() {
54
55
           T flow = 0:
           while (bfs()) flow += dfs(s, numeric limits<T>::max());
57
           return flow;
       }
58
       void init(int s, int t, int vtot) {
60
           s = _s;
61
           t = _t;
           vtot = vtot;
           etot = 0:
           for (int i = 1; i <= vtot; i++) head[i] = -1;
       }
66 };
```

5.6 dinic-tourist.cpp

```
1 template <typename T>
2 class flow_graph {
3
   public:
4
        static constexpr T eps = (T) 1e-9;
5
6
       struct edge {
7
           int from:
           int to;
9
           T c:
10
           T f;
11
       }:
12
13
       vector<vector<int>> g;
14
       vector<edge> edges;
15
       int n;
       int st:
17
       int fin;
18
       T flow;
19
```

```
20
       flow_graph(int _n, int _st, int _fin) : n(_n), st(_st), fin(_fin) {
21
            assert(0 <= st && st < n && 0 <= fin && fin < n && st != fin);
22
           g.resize(n):
23
           flow = 0;
       }
24
25
26
       void clear flow() {
27
            for (const edge &e : edges) {
28
                e.f = 0;
           }
29
30
           flow = 0;
       }
31
32
33
       int add(int from, int to, T forward cap, T backward cap) {
34
            assert(0 <= from && from < n && 0 <= to && to < n):
            int id = (int) edges.size();
35
36
            g[from].push back(id);
            edges.push_back({from, to, forward_cap, 0});
37
            g[to].push_back(id + 1);
38
            edges.push_back({to, from, backward_cap, 0});
39
40
            return id;
41
       }
42 }:
43
   template <typename T>
45 class dinic {
   public:
47
       flow_graph <T> &g;
48
49
       vector<int> ptr;
50
       vector<int> d;
51
       vector<int> q;
52
53
       dinic(flow_graph<T> &_g) : g(_g) {
54
            ptr.resize(g.n);
55
           d.resize(g.n);
56
           q.resize(g.n);
       }
57
58
59
       bool expath() {
60
           fill(d.begin(), d.end(), -1);
61
           q[0] = g.fin;
62
           d[g.fin] = 0;
```

```
63
             int beg = 0, end = 1;
 64
             while (beg < end) {
                 int i = q[beg++];
 65
 66
                 for (int id : g.g[i]) {
                     const auto &e = g.edges[id];
 67
                     const auto &back = g.edges[id ^ 1];
 68
 69
                     if (back.c - back.f > g.eps && d[e.to] == -1) {
 70
                         d[e.to] = d[i] + 1:
                         if (e.to == g.st) {
 71
 72
                             return true:
 73
                         }
 74
                         q[end++] = e.to;
 75
                     }
 76
                 }
 77
             }
 78
             return false;
 79
        }
 80
 81
        T dfs(int v, T w) {
 82
             if (v == g.fin) {
 83
                 return w;
 84
             }
             int &j = ptr[v];
             while (j \ge 0) {
 86
 87
                 int id = g.g[v][j];
                 const auto &e = g.edges[id];
                 if (e.c - e.f > g.eps \&\& d[e.to] == d[v] - 1) {
                     T t = dfs(e.to, min(e.c - e.f, w));
 91
                     if (t > g.eps) {
92
                         g.edges[id].f += t;
93
                         g.edges[id ^ 1].f -= t;
94
                         return t:
 95
                    }
                 }
97
                 j--;
             }
98
             return 0;
100
        }
101
102
        T max_flow() {
103
             while (expath()) {
104
                 for (int i = 0; i < g.n; i++) {
105
                     ptr[i] = (int) g.g[i].size() - 1;
```

```
106
                  }
                  T big add = 0;
107
                  while (true) {
108
                      T add = dfs(g.st, numeric limits<T>::max());
109
                      if (add <= g.eps) {</pre>
110
111
                          break;
112
113
                      big_add += add;
114
                  if (big_add <= g.eps) {</pre>
115
                      break;
116
                  }
117
118
                  g.flow += big_add;
119
             }
             return g.flow;
120
         }
121
122
123
         vector<bool> min cut() {
124
              max_flow();
             vector<bool> ret(g.n);
125
              for (int i = 0; i < g.n; i++) {
126
                  ret[i] = (d[i] != -1):
127
128
             }
129
              return ret;
130
         }
131 };
```

5.7 eulerian-digraph.cpp

```
1 // http://oj.daimayuan.top/course/14/problem/765 单词接龙
2 vector<int> g[N];
   int in[N], out[N], f[N], vis[N];
   string s;
   vector<int> path;
   void dfs(int x) {
           while (f[x] < SZ(g[x])) {
                   int y = g[x][f[x]];
                   f[x]++;
10
                   dfs(y);
11
12
                   path.pb(x);
13
           }
14 }
```

```
15
   bool euler() {
17
            int start = -1, diff = 0, num = 0;
18
            rep(i, 0, n - 1) {
                    if (in[i] + 1 == out[i]) num++, start = i;
19
                    if (in[i] != out[i]) diff++;
20
21
22
            // 恰好都balance或者恰好一个in = out + 1, 一个in + 1 = out
            if (!(diff == 0 || (diff == 2 && num == 1))) return false;
23
24
            if (start == -1) {
25
                    rep(i, 0, n - 1) {
26
                            if (in[i]) {
27
                                    start = i:
28
                                    break;
29
                            }
                    }
30
           }
31
            dfs(start);
            path.pb(start);
            reverse(all(path));
34
            if (SZ(path) != m + 1) return false;
            return true:
37 }
    void solve() {
40
            cin >> m;
41
            n = 26:
42
           rep(i, 1, m) {
                    cin >> s;
44
                    int u = s[0] - 'a', v = s[SZ(s) - 1] - 'a':
                    g[u].pb(v);
45
                    in[v]++, out[u]++;
47
           }
            cout << (euler() ? "Yes" : "No") << '\n';</pre>
49 }
```

5.8 eulerian-undigraph.cpp

```
1 // http://oj.daimayuan.top/course/14/problem/763 欧拉路判断
2 vector<PII>g[N];
3 int d[N], f[N], vis[N], edge_idx;
4 vector<int> path;
```

```
void dfs(int x) {
            while (f[x] < SZ(g[x])) {
                    auto [v, id] = g[x][f[x]];
                    f[x]++;
                    if (vis[id]) continue;
10
                    vis[id] = 1;
11
                    dfs(v);
12
                    path.pb(x);
13
14
            }
15 }
16
    bool euler() {
17
            int start = -1, num = 0;
18
19
            rep(i, 1, n) {
                    if (d[i] & 1) num++, start = i;
20
21
            if (!(num == 0 || (num == 2 && start != -1))) return false;
22
            if (start == -1) {
23
24
                    rep(i, 1, n) {
                             if (d[i]) {
25
26
                                     start = i;
                                     break:
27
                             }
28
                    }
29
30
            }
            dfs(start);
31
            path.pb(start);
32
            reverse(all(path));
33
34
            if (SZ(path) != m + 1) return false;
            return true:
35
36 }
37
   void solve() {
39
            cin >> n >> m;
            rep(i, 1, m) {
40
                    int u, v;
41
                    cin >> u >> v;
                    edge_idx++;
43
44
                    g[u].pb({v, edge_idx});
                    g[v].pb({u, edge_idx});
45
                    d[u]++, d[v]++;
46
47
48
            cout << (euler() ? "Yes" : "No") << '\n';</pre>
```

49 }

5.9 hungarian.cpp

```
1 vector<int> g[maxn];
2 int idx:
3 int a[N][N], use[N][N], p[maxn], vis[maxn];
4
  bool find(int x) {
       vis[x] = 1;
       for (auto y : g[x]) {
           if (!p[y] || (!vis[p[y]] && find(p[y]))) {
9
               p[y] = x;
10
               return true;
           }
11
       }
12
13
       return false;
14 }
15
16 int match() {
17
       int res = 0:
       fill(p + 1, p + idx + 1, 0);
       for (int i = 1: i <= idx: i++) {
19
20
           fill(vis + 1, vis + idx + 1, 0);
21
           if (find(i)) res++:
22
       }
       return res;
24 }
```

5.10 KM.cpp

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 using 11 = long long;
4
5 // L <= R, 左边完全匹配
6 // 最小权完备匹配
7
8 // 带权匹配: 使得该二分图的权值和最大(或最小)的匹配。
9 // 最大匹配: 使得该二分图边数最多的匹配。
10 // 完备匹配: 使得点数较小的点集中每个点都被匹配的匹配。
11 // 完美匹配: 所有点都被匹配的匹配。
12 // 定理1: 最大匹配数 = 最小点覆盖数 (Konig 定理)
```

```
13 // 定理2: 最大匹配数 = 最大独立数
14 // 定理3: 最小路径覆盖数 = 顶点数 - 最大匹配数
16 // 二分图的最小点覆盖
17 // 定义: 在二分图中, 求最少的点集, 使得每一条边至少都有端点在这个点集中。
18 // 二分图的最小点覆盖 = 二分图的最大匹配
20 // 二分图的最少边覆盖
21 // 定义:在二分图中,求最少的边,使得他们覆盖所有的点,并且每一个点只被一条
      边覆盖。
22 // 二分图的最少边覆盖 = 点数 - 二分图的最大匹配
24 // 二分图的最大独立集
25 // 定义: 在二分图中, 选最多的点, 使得任意两个点之间没有直接边连接。
26 // 二分图的最大独立集 = 点数 - 二分图的最大匹配
28 template < class T>
   pair<T, vector<int>> hungarian(const vector<vector<T>> &a) {
30
          if (a.empty()) return {0, {}};
          int n = a.size() + 1, m = a[0].size() + 1:
31
          vector<T> u(n), v(m); // 顶标
32
33
          vector<int> p(m), ans(n-1):
34
          for (int i = 1: i < n: i++) {
35
                p[0] = i;
36
                int j0 = 0;
                vector<T> dist(m, numeric limits<T>::max());
                vector<int> pre(m, -1);
                vector<bool> done(m + 1);
                do { // dijkstra
                       done[i0] = true:
41
42
                       int i0 = p[j0], j1;
                       T delta = numeric_limits<T>::max();
                       for (int j = 1; j < m; j++) if (!done[j]) {
44
                              auto cur = a[i0 - 1][j - 1] - u[i0] - v[j];
45
                              if (cur < dist[j]) dist[j] = cur, pre[j] =</pre>
46
                              if (dist[j] < delta) delta = dist[j], j1 = j</pre>
47
                       for (int j = 0; j < m; j++) {
                              if (done[j]) u[p[j]] += delta, v[j] -= delta
51
                              else dist[j] -= delta;
```

```
52
                             }
                             i0 = i1;
54
                    } while (p[j0]);
55
                     while (j0) { // update alternating path
                             int j1 = pre[j0];
56
57
                             p[j0] = p[j1], j0 = j1;
                    }
59
60
            for (int j = 1; j < m; j++) {
61
                     if (p[j]) ans[p[j] - 1] = j - 1;
62
63
            return {-v[0], ans}; // min cost
64 }
66 int L. R. m:
67 int main() {
            scanf("%d%d%d", &L, &R, &m);
            R = max(L, R):
70
            auto a = vector<vector<ll>>(L, vector<ll>(R, 0));
            for (int i = 0: i < m: i++) {
71
72
                    int u, v, w;
73
                    scanf("%d%d%d", &u, &v, &w):
74
                    --u: --v:
75
                     a[u][v] = -w;
76
            auto [val, ans] = hungarian(a);
            printf("%lld\n", -val);
79
            for (int i = 0; i < L; i++) {
                    if (a[i][ans[i]] >= 0) ans[i] = -1;
81
                     printf("\frac{1}{2}d\frac{1}{2}c", ans[i] + 1, "\frac{1}{2}n"[i == L - 1]):
82
            }
83 }
```

5.11 kosaraju.cpp

```
vector<int> e[maxn], erev[maxn];
vector<int> c, out;
vector<vector<int>> scc;
int vis[maxn];
void dfs(int u) {
   vis[u] = 1;
   for (auto v : e[u]) if (!vis[v]) dfs(v);
   out.pb(u);
```

```
9 }
10 void dfs rev(int u) {
        vis[u] = 1:
11
12
        for (auto v : erev[u]) if (!vis[v]) dfs rev(v);
        c.pb(u);
13
14 }
15 void solve() {
        cin >> n >> m:
16
17
        rep(i, 1, m) {
18
            int u, v;
19
            cin >> u >> v;
            e[u].pb(v);
20
            erev[v].pb(u);
21
22
       }
23
        rep(i, 1, n) if (!vis[i]) dfs(i);
        fill(vis + 1, vis + n + 1, 0);
24
        reverse(all(out));
25
        for (auto v : out) if (!vis[v]) {
26
                c.clear();
27
                dfs_rev(v);
28
                scc.pb(c);
29
30
            }
31 }
```

5.12 MCMF.cpp

```
template < typename T>
2 struct MinCostGraph {
        static const int V = 20100;
        static const int E = 201000:
       int s, t, vtot;
        int head[V], etot;
       T dis[V], flow, cost;
        int pre[V];
        bool vis[V]:
10
11
        struct edge {
12
            int v. nxt:
13
            T f, c;
14
       } e[E * 2]:
        void addedge(int u,int v, T f, T c, T f2 = 0){
15
16
            e[etot] = {v, head[u], f, c}; head[u] = etot++;
17
            e[etot] = \{u, head[v], f2, -c\}; head[v] = etot++;
```

```
18
       }
19
20
        bool spfa() {
21
            T inf = numeric limits <T>::max() / 2;
22
            for (int i = 1: i <= vtot: i++) {
23
                dis[i] = inf;
24
                vis[i] = false;
25
                pre[i] = -1:
            }
26
27
            dis[s] = 0;
28
            vis[s] = true;
29
            queue < int > q;
            q.push(s);
30
31
            while (!q.empty()) {
32
                int u = q.front();
33
                for (int i = head[u]; ~i; i = e[i].nxt) {
                    int v = e[i].v;
34
                    if (e[i].f && dis[v] > dis[u] + e[i].c) {
                         dis[v] = dis[u] + e[i].c;
36
                        pre[v] = i;
37
38
                        if (!vis[v]) {
39
                             vis[v] = 1:
40
                            q.push(v);
41
                        }
42
                    }
43
                }
44
                q.pop();
45
                vis[u] = false;
46
            return dis[t] != inf:
47
48
       }
49
50
        void augment() {
51
            int u = t;
52
            T f = numeric_limits<T>::max();
53
            while (~pre[u]) {
                f = min(f, e[pre[u]].f);
54
55
                u = e[pre[u] ^ 1].v;
56
            }
57
            flow += f;
            cost += f * dis[t];
59
            u = t:
60
            while (~pre[u]) {
```

```
61
                e[pre[u]].f -= f;
                e[pre[u] ^ 1].f += f;
62
                u = e[pre[u] ^ 1].v;
64
           }
       }
65
66
67
        pair<T, T> solve() {
            flow = 0:
69
            cost = 0;
            while (spfa()) augment();
70
71
            return {flow, cost};
72
       }
73
        void init(int s_, int t_, int vtot_) {
74
            s = s;
75
            t = t :
76
            vtot = vtot ;
            etot = 0;
            for (int i = 1: i \le vtot: i++) head[i] = -1:
79
       }
80 };
```

5.13 MCMFfast.cpp

```
template <typename flow t = int, typename cost t = long long>
   struct MCMF SSPA {
       int N;
       vector<vector<int>> adj;
       struct edge_t {
           int dest;
           flow_t cap;
           cost_t cost;
9
       };
10
       vector<edge_t> edges;
11
12
       vector < char > seen:
       vector<cost_t> pi;
13
14
       vector<int> prv;
15
16
        explicit MCMF_SSPA(int N_) : N(N_), adj(N), pi(N, 0), prv(N) {}
17
18
       void addEdge(int from, int to, flow_t cap, cost_t cost) {
19
            assert(cap >= 0);
            int e = int(edges.size());
20
```

```
21
            edges.emplace_back(edge_t{to, cap, cost});
22
            edges.emplace back(edge t{from, 0, -cost});
23
            adj[from].push_back(e);
24
            adj[to].push back(e+1);
25
       }
26
27
        const cost t INF COST = numeric limits<cost t>::max() / 4;
28
        const flow_t INF_FLOW = numeric_limits<flow_t>::max() / 4;
29
        vector<cost t> dist;
30
        __gnu_pbds::priority_queue<pair<cost_t, int>> q;
31
        vector<typename decltype(q)::point_iterator> its;
32
        void path(int s) {
33
            dist.assign(N, INF_COST);
34
            dist[s] = 0;
35
36
            its.assign(N, q.end());
37
            its[s] = q.push({0, s});
38
39
            while (!q.empty()) {
                int i = q.top().second; q.pop();
40
41
                cost t d = dist[i];
42
                for (int e : adi[i]) {
43
                    if (edges[e].cap) {
44
                        int j = edges[e].dest;
45
                        cost_t nd = d + edges[e].cost;
46
                        if (nd < dist[j]) {</pre>
47
                            dist[j] = nd;
48
                            prv[j] = e;
49
                            if (its[j] == q.end()) {
50
                                 its[j] = q.push({-(dist[j] - pi[j]), j});
51
                            } else {
52
                                 q.modify(its[j], {-(dist[j] - pi[j]), j});
53
                            }
54
                        }
55
                    }
56
            }
57
58
59
            swap(pi, dist);
60
       }
61
62
        vector<pair<flow_t, cost_t>> maxflow(int s, int t) {
63
            assert(s != t);
```

```
64
            flow_t totFlow = 0; cost_t totCost = 0;
65
            vector<pair<flow t, cost t>> res;
            while (path(s), pi[t] < INF_COST) {</pre>
66
67
                flow t curFlow = numeric limits<flow t>::max();
                for (int cur = t; cur != s; ) {
68
                    int e = prv[cur];
69
                    int nxt = edges[e^1].dest;
70
                    curFlow = min(curFlow, edges[e].cap);
71
72
                    cur = nxt;
                }
73
74
                totFlow += curFlow;
                totCost += pi[t] * curFlow;
75
                for (int cur = t; cur != s; ) {
76
77
                    int e = prv[cur];
78
                    int nxt = edges[e^1].dest;
79
                    edges[e].cap -= curFlow;
80
                    edges[e^1].cap += curFlow;
81
                    cur = nxt:
                }
83
84
                res.emplace_back(totFlow, totCost);
            }
85
            return res;
87
       }
88 }:
```

5.14 MCMFfull.cpp

```
template <typename T, typename C>
2 class MCMF {
    public:
4
     static constexpr T eps = (T) 1e-9;
     struct edge {
       int from:
       int to;
       T c;
10
       T f:
11
       C cost;
     }:
12
13
14
     int n;
15
     vector<vector<int>> g;
```

```
16
      vector<edge> edges;
17
      vector<C> d;
18
      vector<C> pot;
19
      __gnu_pbds::priority_queue<pair<C, int>> q;
20
      vector<typename decltype(q)::point_iterator> its;
21
      vector<int> pe;
22
      const C INF C = numeric limits<C>::max() / 2;
23
24
      explicit MCMF(int n_): n(n_), g(n), d(n), pot(n, 0), its(n), pe(n) {}
25
26
      int add(int from, int to, T forward_cap, T backward_cap, C edge_cost) {
27
        assert(0 \le from && from < n && 0 \le to && to < n);
28
        assert(forward cap >= 0 && backward cap >= 0):
29
        int id = static cast<int>(edges.size());
30
        g[from].push back(id):
31
        edges.push_back({from, to, forward_cap, 0, edge_cost});
32
        g[to].push back(id + 1);
        edges.push_back({to, from, backward_cap, 0, -edge_cost});
34
       return id;
35
     }
36
37
      void expath(int st) {
38
        fill(d.begin(), d.end(), INF_C);
39
       q.clear();
40
       fill(its.begin(), its.end(), q.end());
41
        its[st] = q.push({pot[st], st});
42
       d[st] = 0:
43
        while (!q.empty()) {
44
         int i = q.top().second;
45
          q.pop();
          its[i] = q.end();
46
47
          for (int id : g[i]) {
            const edge &e = edges[id];
48
49
            int j = e.to;
50
            if (e.c - e.f > eps && d[i] + e.cost < d[j]) {
51
              d[j] = d[i] + e.cost;
52
              pe[j] = id;
              if (its[j] == q.end()) {
53
54
                its[j] = q.push({pot[j] - d[j], j});
55
              } else {
56
                q.modify(its[j], {pot[j] - d[j], j});
57
              }
58
            }
```

```
59
          }
         }
 60
         swap(d, pot);
 61
 62
 63
       pair<T, C> calc(int st, int fin) { // max flow min cost
 64
         T flow = 0;
 65
         C cost = 0:
 67
         bool ok = true;
 68
         for (auto& e : edges) {
 69
           if (e.c - e.f > eps && e.cost + pot[e.from] - pot[e.to] < 0) {</pre>
 70
             ok = false;
 71
             break:
          }
 72
 73
         }
         if (ok) {
 74
 75
           expath(st);
         } else {
 76
 77
           vector<int> deg(n, 0);
           for (int i = 0: i < n: i++) {
 78
             for (int eid : g[i]) {
 79
 80
               auto& e = edges[eid]:
               if (e.c - e.f > eps) {
 81
 82
                 deg[e.to] += 1;
 83
               }
             }
 84
           }
 85
 86
           vector<int> que;
 87
           for (int i = 0; i < n; i++) {
 88
             if (deg[i] == 0) {
               que.push_back(i);
 89
 90
             }
           }
 91
           for (int b = 0; b < (int) que.size(); b++) {</pre>
 92
 93
             for (int eid : g[que[b]]) {
 94
               auto& e = edges[eid];
 95
               if (e.c - e.f > eps) {
                 deg[e.to] -= 1;
 96
                 if (deg[e.to] == 0) {
 97
 98
                   que.push_back(e.to);
 99
                 }
100
               }
101
             }
```

```
102
           }
103
           fill(pot.begin(), pot.end(), INF C);
104
           pot[st] = 0:
105
           if (static cast<int>(que.size()) == n) {
106
             for (int v : que) {
107
               if (pot[v] < INF_C) {</pre>
108
                 for (int eid : g[v]) {
109
                    auto& e = edges[eid];
110
                   if (e.c - e.f > eps) {
111
                      if (pot[v] + e.cost < pot[e.to]) {</pre>
112
                        pot[e.to] = pot[v] + e.cost;
113
                        pe[e.to] = eid;
114
                     }
115
                   }
116
                 }
117
               }
118
             }
119
           } else {
120
             que.assign(1, st);
121
             vector<bool> in_queue(n, false);
122
             in_queue[st] = true;
123
             for (int b = 0; b < (int) que.size(); b++) {</pre>
124
               int i = que[b];
125
               in_queue[i] = false;
126
               for (int id : g[i]) {
127
                 const edge &e = edges[id];
128
                 if (e.c - e.f > eps && pot[i] + e.cost < pot[e.to]) {</pre>
129
                    pot[e.to] = pot[i] + e.cost;
130
                   pe[e.to] = id;
131
                   if (!in_queue[e.to]) {
132
                     que.push_back(e.to);
133
                     in_queue[e.to] = true;
134
                   }
135
                 }
136
               }
137
             }
138
           }
139
         }
140
         // debug(pot[fin]);
141
         while (pot[fin] < INF_C) { // < 0
142
           T push = numeric_limits<T>::max();
143
           int v = fin:
144
           while (v != st) {
```

```
145
             const edge &e = edges[pe[v]];
             push = min(push, e.c - e.f);
146
147
             v = e.from:
148
          }
           v = fin:
149
           while (v != st) {
150
151
             edge &e = edges[pe[v]];
152
             e.f += push;
153
             edge &back = edges[pe[v] ^ 1];
154
             back.f -= push;
155
             v = e.from;
156
157
           flow += push;
158
           cost += push * pot[fin];
           expath(st);
159
160
         return {flow, cost};
161
162
163 };
```

5.15 prim.cpp

```
vector<PII> e[N];
   template <typename T>
   void add(int u, int v, T w) {
            e[u].eb(v, w);
   template <typename T>
   T prim(vector<pair<int, T>> *g, int start) {
10
            const T inf = numeric limits<T>::max() / 4;
            T res = 0:
11
            vector<T> dist(n, inf);
12
            dist[start] = 0:
13
14
            priority_queue<pair<T, int>, vector<pair<T, int>>, greater<pair<T,</pre>
                int>>> s;
15
            s.emplace(dist[start], start);
            vector<int> was(n, 0);
16
            while (!s.empty()) {
17
18
                    T expected = s.top().first;
19
                    int i = s.top().second;
20
                    s.pop();
```

```
21
                     if (dist[i] != expected || was[i]) {
22
                              continue;
23
                     }
24
                     was[i] = 1;
25
                     res += expected;
26
                     for (auto [to, cost] : g[i]) {
27
                              if (cost < dist[to]) {</pre>
                                      dist[to] = cost;
29
                                      s.emplace(dist[to], to);
30
                             }
31
                     }
32
            }
            return res;
34 }
```

5.16 PushRelabel.cpp

```
1 /**
    * Author: Simon Lindholm
    * Date: 2015-02-24
    * License: CCO
    * Source: Wikipedia, tinyKACTL
    * Description: Push-relabel using the highest label selection rule and the
         gap heuristic. Quite fast in practice.
    * To obtain the actual flow, look at positive values only.
    * Time: $0(V^2\sqrt E)$
    * Status: Tested on Kattis and SPOJ, and stress-tested
10
    */
   #pragma once
12
    struct PushRelabel {
14
            typedef vector<int> vi;
15
            struct Edge {
16
                    int dest, back;
17
                    11 f. c:
18
           };
19
           vector<vector<Edge>> g;
20
           vector<ll> ec:
21
           vector < Edge *> cur;
22
           vector<vi> hs: vi H:
23
           PushRelabel(int n): g(n), ec(n), cur(n), hs(2*n), H(n) {}
24
25
           void addEdge(int s, int t, ll cap, ll rcap=0) {
```

```
26
                    if (s == t) return;
                    g[s].push back({t, SZ(g[t]), 0, cap});
27
                    g[t].push_back({s, SZ(g[s])-1, 0, rcap});
28
29
            }
30
31
            void addFlow(Edge& e, ll f) {
32
                    Edge &back = g[e.dest][e.back];
                    if (!ec[e.dest] && f) hs[H[e.dest]].push_back(e.dest);
34
                    e.f += f; e.c -= f; ec[e.dest] += f;
                    back.f -= f; back.c += f; ec[back.dest] -= f;
35
36
            }
            ll calc(int s, int t) {
37
                    int v = SZ(g); H[s] = v; ec[t] = 1;
38
39
                    vi co(2*v); co[0] = v-1;
                    rep(i,0,v-1) cur[i] = g[i].data();
40
                    for (Edge& e : g[s]) addFlow(e, e.c);
41
                    for (int hi = 0::) {
                            while (hs[hi].empty()) if (!hi--) return -ec[s];
                            int u = hs[hi].back(); hs[hi].pop_back();
45
46
                            while (ec[u] > 0) // discharge u
47
                                    if (cur[u] == g[u].data() + SZ(g[u])) {
                                            H[u] = 1e9:
49
                                            for (Edge& e : g[u]) if (e.c && H[u]
                                                  > H[e.dest]+1)
50
                                                     H[u] = H[e.dest]+1, cur[u] =
                                                          &е:
                                            if (++co[H[u]], !--co[hi] && hi < v)
51
52
                                                     rep(i,0,v-1) if (hi < H[i]
                                                         && H[i] < v)
                                                             --co[H[i]], H[i] = v
53
                                                                  + 1:
                                            hi = H[u]:
54
                                    } else if (cur[u]->c && H[u] == H[cur[u]->
55
                                         dest[+1)
                                             addFlow(*cur[u], min(ec[u], cur[u]->
                                                 c)):
                                     else ++cur[u];
57
58
                    }
59
            bool leftOfMinCut(int a) { return H[a] >= SZ(g); }
60
61 };
```

5.17 tarjan 割点.cpp

```
1 vector<int> g[maxn], ans;
2 stack<int> stk;
3 int dfn[maxn], cut[maxn], low[maxn], idx;
5
  void dfs(int x, int f) {
       low[x] = dfn[x] = ++idx;
       stk.push(x);
       int ch = 0:
       for (auto y : g[x]) {
10
           if (!dfn[y]) {
11
               ch++;
12
               dfs(v, x);
13
               low[x] = min(low[x], low[y]);
14
               if (low[v] >= dfn[x]) cut[x] = 1;
           } else {
15
               if (y != f) low[x] = min(low[x], dfn[y]);
           }
17
       }
18
       if (x == 1 \&\& ch <= 1) cut[x] = 0;
       if (cut[x]) ans.pb(x);
21 }
```

5.18 tarjan 割边.cpp

```
1 vector < PII > g[maxn];
2 stack<int> stk;
3 int dfn[maxn], ins[maxn], low[maxn];
4 int idx, tot;
5 VI ans:
6 void dfs(int x, int f) {
7
       low[x] = dfn[x] = ++idx;
8
       stk.push(x);
9
       ins[x] = 1;
10
       for (auto [y, id] : g[x]) {
           if (!dfn[y]) {
11
12
                dfs(y, id);
13
               low[x] = min(low[x], low[y]);
14
           } else {
                if (ins[v] \&\& id != f) low[x] = min(low[x], dfn[v]):
16
           }
17
       }
18
       if (low[x] >= dfn[x]) {
```

```
++tot;
19
            while (true) {
20
                int cur = stk.top();
21
22
                stk.pop();
                ins[cur] = 0;
23
                if (cur == x) break;
24
            if (f != 0) ans.pb(f);
26
27
28 }
```

5.19 tarjan 强连通分量.cpp

```
1 vector<int> g[maxn];
2 stack<int> stk;
   int dfn[maxn], ins[maxn], low[maxn], belong[maxn];
   int idx, tot;
   void dfs(int x) {
        low[x] = dfn[x] = ++idx;
        ins[x] = 1;
        stk.push(x);
        for (auto y : g[x]) {
10
11
            if (!dfn[y]) {
12
                dfs(y);
13
                low[x] = min(low[x], low[y]);
14
                if (ins[y]) low[x] = min(low[x], dfn[y]);
15
            }
16
       }
17
        if (low[x] >= dfn[x]) {
18
19
            ++tot;
            while (true) {
                int cur = stk.top(); stk.pop();
21
                ins[cur] = 0;
22
23
                belong[cur] = tot;
                if (cur == x) break;
24
27 }
```

5.20 tarjan 点双.cpp

```
1 vector<int> g[maxn];
2 stack<int> stk;
3 int dfn[maxn], low[maxn], idx, tot, cut[maxn];
   vector<int> bcc[maxn];
   void dfs(int x, int f) {
       low[x] = dfn[x] = ++idx;
        stk.push(x);
       int ch = 0;
        for (auto y : g[x]) {
11
            if (!dfn[y]) {
12
                ch++;
13
                dfs(y, x);
14
                low[x] = min(low[x], low[y]);
15
                if (low[v] >= dfn[x]) {
                    cut[x] = 1;
16
17
                    ++tot;
18
                    bcc[tot].pb(x);
                    while (true) {
19
                        int cur = stk.top();
21
                        stk.pop();
22
                        bcc[tot].pb(cur);
23
                        if (cur == y) break;
                   }
24
25
                }
26
           } else {
27
                if (y != f) low[x] = min(low[x], dfn[y]);
28
           }
       }
29
        if (x == 1 \&\& ch <= 1) cut[x] = 0;
31 }
```

5.21 tarjan 边双.cpp

```
vector < PII > g[maxn];
stack < int > stk;
int dfn[maxn], low[maxn], idx, tot, belong[maxn];
vector < int > bcc[maxn];

void dfs(int x, int f) {
    low[x] = dfn[x] = ++idx;
stk.push(x);
```

```
9
       for (auto [y, id] : g[x]) {
10
            if (!dfn[v]) {
11
                dfs(y, id);
12
                low[x] = min(low[x], low[y]);
            } else {
13
                if (id != f) low[x] = min(low[x], dfn[y]);
14
            }
15
       }
16
17
       if (low[x] >= dfn[x]) {
18
            ++tot:
19
            while (true) {
20
                int cur = stk.top();
21
                stk.pop();
22
                belong[cur] = tot;
                bcc[tot].pb(cur);
23
                if (cur == x) break;
24
            }
25
       }
27 }
```

5.22 twosat.cpp

```
1 class twosat {
   public:
           digraph<int> g;
           int n:
           twosat(int _n) : g(digraph<int>(2 * _n)), n(_n) {
           }
           // (v \lceil x \rceil == value x)
10
           inline void add(int x, int value x) {
                   assert(0 <= x && x < n):
11
12
                   assert(0 <= value_x && value_x <= 1);</pre>
                   g.add(2 * x + (value_x ^1), 2 * x + value_x);
14
           }
15
           // (v[x] == value x // v[y] == value y)
16
           inline void add(int x, int value_x, int y, int value_y) {
17
18
                   assert(0 <= value_x && value_x <= 1 && 0 <= value_y &&
19
                       value_y <= 1);</pre>
20
                   g.add(2 * x + (value_x ^ 1), 2 * y + value_y);
```

```
21
                    g.add(2 * y + (value_y ^ 1), 2 * x + value_x);
22
            }
23
24
            inline vector<int> solve() {
25
                    int cnt:
26
                    vector<int> c = find_scc(g, cnt);
27
                    vector<int> res(n);
28
                    for (int i = 0; i < n; i++) {
29
                            if (c[2 * i] == c[2 * i + 1]) {
30
                                     return vector<int>();
31
32
                            res[i] = (c[2 * i] < c[2 * i + 1]);
                    }
33
34
                    return res;
35
            }
36 };
```

5.23 差分约束系统.cpp

```
1 /**
2
          Description:
3
          求解方程组 x u - x v \le w i, 求出的x i为满足条件的最大值
4
          转化为x u \le x v + w i
          问题等价于求最短路 (bellmanford或Floyd)
5
          即加一条有向边add(u, v, w), dist[v] = min(dist[v], dist[u] + w)
          求最小值(满足条件情况下尽量小)等价于求(-xi)最大(或者转化为求最长
          求非负解只需要添加超级节点S, S向各个点连边(S + 0 \le xi), 再设dist
              \Gamma S7 = 0
    */
9
   void solve() {
11
          cin >> n >> m;
12
          vector<int> dist(n, 0);
13
          vector<vector<PII>>> g(n);
14
          rep(i, 0, m - 1) {
15
                 int u, v, w;
16
                 cin >> u >> v >> w;
17
                 u--. v--:
18
                 g[u].eb(v, -w);
19
          }
20
          bool ok = 1;
21
          rep(i, 1, n) {
22
                 bool upd = 0;
```

```
rep(u, 0, n - 1) {
23
24
                            for (auto [v, w] : g[u]) {
                                    if (dist[v] < dist[u] + w) {</pre>
25
26
                                             dist[v] = dist[u] + w;
                                             upd = 1;
27
                                    }
28
                            }
29
                    }
31
                    if (!upd) break;
                    // 仍然有约束未满足
32
33
                    if (i == n && upd) ok = 0;
34
            }
            if (!ok) {
35
36
                    return cout << -1 << '\n', void();
            }
37
38
            rep(i, 0, n - 1) {
39
                    cout << dist[i] << ",\n"[i == n - 1];
41 }
```

6 Math

6.1 binom.cpp

```
1 vector < Mint > fact(1, 1);
2 vector < Mint > inv fact(1, 1);
   Mint C(int n, int k) {
            if (k < 0 | | k > n) {
                    return 0:
            }
            while ((int)fact.size() < n + 1) {</pre>
                    fact.push_back(fact.back() * (int)fact.size());
                    inv_fact.push_back(1 / fact.back());
11
12
            return fact[n] * inv_fact[k] * inv_fact[n - k];
13 }
14
15 const int mod = 1000000007:
16 const int T = 1000000;
17 ll fact[] = {};
18 ll powmod(ll a, ll b) {
```

```
19
           ll ret = 1;
            for (; b; b >>= 1) {
21
                    if (b & 1) ret = ret * a % mod;
22
                    a = a * a \% mod;
23
           }
24
            return ret;
25 }
26 11 fac(int n) {
           ll v = fact[n / T];
            for (int i = n / T * T + 1; i \le n; i++)
                    v = v * i \% mod;
30
            return v;
31 }
32 11 binom(int n, int m) {
            if (m < 0 \mid | m > n) return 0:
            return fac(n) * powmod(fac(m) * fac(n - m) % mod, mod - 2) % mod;
35 }
```

6.2 bsgs.cpp

```
1 int bsgs(int a, int b, int m) { // a^x=b \pmod{m}
       int res = m + 1;
       int t = sqrt(m) + 2;
       11 d = powmod(a, t, m);
       ll cnt = 1;
6
       //map<int,int> p;
7
       hs.init();
       for (int i = 1; i <= t; i++) {
9
           cnt = cnt * d % m:
10
           //if (!p.count(cnt)) p[cnt] = i;
           if (hs.query(cnt) == -1) hs.insert(cnt, i);
11
12
       }
13
       cnt = b;
       for (int i = 1; i <= t; i++) {
14
15
           cnt = cnt * a % m;
           //if (p.count(cnt)) res = min(res, p[cnt] * t - i);
16
17
           int tmp = hs.query(cnt);
           if (tmp != -1) res = min(res, tmp * t - i);
18
19
20
       if (res >= m) res = -1;
21
       return res:
22 }
```

6.3 cantor.cpp

1 11 fac[maxn], A[maxn], w[maxn];

```
void init(int n) {
                              fac[0] = 1:
                               rep(i, 1, n) fac[i] = fac[i - 1] * i % mod;
   6 ll cantor(int w[], int n) {
                               11 \text{ ans} = 1;
                               for (int i = 1; i \le n; i++) { // can optimize by BIT
                                               for (int j = i + 1; j \le n; j++) {
 10
                                                               if (w[i] > w[j]) A[i]++;
11
                                              }
 12
                              }
 13
                              for (int i = 1; i < n; i++) {
14
                                               ans += A[i] * fac[n - i];
                              }
15
16
                               return ans;
17 }
18
               void decanter(ll x, int n) { // x - rank n - r
19
                               x--:
20
21
                               vector<int> rest(n, 0);
                               iota(rest.begin(), rest.end(), 1); // rest->1,2,3,4...
22
                               for (int i = 1: i <= n: i++) {
23
                                              A[i] = x / fac[n - i];
 24
                                              x %= fac[n - i];
 25
 26
                              for (int i = 1: i <= n: i++) {
27
 28
                                              w[i] = rest[A[i]]:
                                              rest.erase(lower_bound(rest.begin(), rest.end(), w[i]));
 29
30
31 }
```

6.4 EXCRT modequ exgcd.cpp

```
1 ll exgcd(ll a, ll b, ll &x, ll &y) {
2    if (b == 0) {
3         x = 1, y = 0;
4         return a;
5    }
6    ll d = exgcd(b, a % b, y, x);
7    y -= (a / b) * x;
8    return d;
```

```
9 }
10
11 // 求 a * x = b \pmod{m} 的解
12 11 modequ(11 a, 11 b, 11 m) {
       11 x, y;
       ll d = exgcd(a, m, x, y);
       if (b % d != 0) return -1;
       m /= d; a /= d; b /= d;
17
       x = x * b % m;
       if (x < 0) x += m:
19
       return x;
20 }
21
22 void merge(ll &a, ll &b, ll c, ll d) {
       if (a == -1 || b == -1) return;
       11 x, y;
       11 g = exgcd(b, d, x, y);
       if ((c - a) % g != 0) {
27
           a = -1, b = -1;
28
           return:
29
       }
       d /= g:
       11 t = ((c - a) / g) \% d * x \% d;
       if (t < 0) t += d;
       a = b * t + a:
       b = b * d;
35 }
```

6.5 factor.cpp

```
1 namespace Factor {
        const int N=1010000;
        11 C, fac[10010], n, mut, a[1001000];
        int T,cnt,i,l,prime[N],p[N],psize,_cnt;
        ll _e[100],_pr[100];
        vector<ll> d;
7
        inline ll mul(ll a,ll b,ll p) {
            if (p<=1000000000) return a*b%p;
            else if (p \le 100000000000011) return (((a*(b>>20)%p) \le 20)+(a*(b))
                 &((1<<20)-1))))%p;
10
            else {
11
                11 d=(11)floor(a*(long double)b/p+0.5);
12
                11 \text{ ret}=(a*b-d*p)\%p;
```

```
13
                if (ret<0) ret+=p;</pre>
14
                return ret;
            }
15
16
        }
17
        void prime_table(){
            int i,j,tot,t1;
18
            for (i=1;i<=psize;i++) p[i]=i;
19
            for (i=2,tot=0;i<=psize;i++){
20
21
                if (p[i]==i) prime[++tot]=i;
                for (j=1;j<=tot && (t1=prime[j]*i)<=psize;j++){</pre>
22
23
                    p[t1]=prime[j];
24
                     if (i%prime[j]==0) break;
                }
25
26
            }
27
        }
28
        void init(int ps) {
29
            psize=ps;
30
            prime_table();
31
        }
        11 powl(11 a,11 n,11 p) {
32
33
            ll ans=1;
34
            for (:n:n>>=1) {
                if (n&1) ans=mul(ans,a,p);
35
36
                a=mul(a,a,p);
37
            }
38
            return ans;
39
        bool witness(ll a, ll n) {
40
41
            int t=0;
42
            ll u=n-1:
            for (;~u&1;u>>=1) t++;
43
44
            11 x=powl(a,u,n),_x=0;
            for (;t;t--) {
45
46
                x=mul(x,x,n);
47
                if (_x==1 && x!=1 && x!=n-1) return 1;
48
                x = _x;
            }
49
50
            return _x!=1;
51
        }
52
        bool miller(ll n) {
53
            if (n<2) return 0;
54
            if (n<=psize) return p[n]==n;</pre>
55
            if (~n&1) return 0;
```

```
56
            for (int j=0; j \le 7; j++) if (witness(rng()%(n-1)+1,n)) return 0;
57
            return 1;
        }
58
59
        11 gcd(ll a,ll b) {
60
            ll ret=1:
61
            while (a!=0) {
62
                 if ((~a&1) && (~b&1)) ret <<=1,a>>=1,b>>=1;
                 else if (~a&1) a>>=1; else if (~b&1) b>>=1;
64
                 else {
                     if (a<b) swap(a,b);</pre>
66
                     a-=b;
67
                 }
            }
68
69
            return ret*b;
70
        }
71
        11 rho(11 n) {
72
            while (1) {
                 11 X=rng()%n,Y,Z,T=1,*1Y=a,*1X=1Y;
74
                 int tmp=20;
75
                 C=rng()%10+3;
76
                 X=mul(X,X,n)+C;*(1Y++)=X;1X++;
77
                 Y=mul(X,X,n)+C:*(1Y++)=Y:
                 for(:X!=Y:) {
79
                     11 t=X-Y+n;
80
                     Z=mul(T,t,n):
81
                     if(Z==0) return gcd(T,n);
                     tmp--;
                     if (tmp==0) {
84
                         tmp=20;
85
                         Z=gcd(Z,n);
                         if (Z!=1 && Z!=n) return Z;
                     }
87
                     T=Z;
89
                     Y = *(1Y + +) = mul(Y, Y, n) + C;
90
                     Y = *(1Y + +) = mul(Y, Y, n) + C;
91
                     X = *(1X + +);
92
                }
93
94
95
        void _factor(ll n) {
96
            for (int i=0;i<cnt;i++) {
                 if (n%fac[i]==0) n/=fac[i],fac[cnt++]=fac[i];}
97
98
            if (n<=psize) {</pre>
```

```
99
                 for (;n!=1;n/=p[n]) fac[cnt++]=p[n];
100
                 return;
             }
101
102
             if (miller(n)) fac[cnt++]=n;
             else {
103
                 11 x=rho(n);
104
                 factor(x); factor(n/x);
105
             }
106
107
         }
         void dfs(ll x.int dep) {
108
109
             if (dep== cnt) d.pb(x);
             else {
110
                 dfs(x.dep+1):
111
                 for (int i=1; i \le e[dep]; i++) dfs(x*=pr[dep], dep+1);
112
             }
113
         }
114
115
         void norm() {
             sort(fac.fac+cnt):
116
117
             cnt=0;
             rep(i,0,cnt-1) if (i==0||fac[i]!=fac[i-1]) _pr[_cnt]=fac[i], e[ cnt
118
                 ++]=1:
                 else e[cnt-1]++:
119
         }
120
         vector<ll> getd() {
121
122
             d.clear():
             dfs(1,0);
123
             return d:
124
125
         }
126
         vector<ll> factor(ll n) {
127
             cnt=0:
             factor(n);
128
129
             norm():
             return getd();
130
131
         }
132
         vector<PLL> factorG(11 n) {
133
             cnt=0:
134
             _factor(n);
             norm();
135
136
             vector < PLL > d:
137
             rep(i,0,_cnt-1) d.pb(mp(_pr[i],_e[i]));
             return d;
138
139
         }
140
         bool is_primitive(ll a,ll p) {
```

```
141
             assert(miller(p));
142
             vector<PLL> D=factorG(p-1);
143
             rep(i,0,SZ(D)-1) if (powl(a,(p-1)/D[i].fi,p)==1) return 0;
144
             return 1;
145
        }
146
        11 phi(11 n) {
147
             auto d=factorG(n);
148
             for (auto p:d) n=n/p.fi*(p.fi-1);
149
             return n;
150
        }
151 }
```

6.6 fft.cpp

```
1 namespace fft {
     typedef double dbl;
3
4
     struct num {
       dbl x, y;
       num() { x = y = 0; }
7
       num(dbl x, dbl y) : x(x), y(y) { }
8
     };
9
10
      inline num operator+(num a, num b) { return num(a.x + b.x, a.y + b.y); }
11
      inline num operator-(num a, num b) { return num(a.x - b.x, a.y - b.y); }
12
      inline num operator*(num a. num b) { return num(a.x * b.x - a.v * b.v. a.x
           * b.v + a.v * b.x); }
13
     inline num conj(num a) { return num(a.x, -a.y); }
14
15
     int base = 1:
     vector<num> roots = {{0, 0}, {1, 0}};
17
     vector < int > rev = \{0, 1\};
18
19
     const dbl PI = acosl(-1.0);
20
21
      void ensure base(int nbase) {
22
       if (nbase <= base) {
23
          return:
24
       }
25
       rev.resize(1 << nbase):
       for (int i = 0: i < (1 << nbase): i++) {
27
          rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
28
       }
```

```
29
        roots.resize(1 << nbase):
        while (base < nbase) {</pre>
30
          dbl \ angle = 2 * PI / (1 << (base + 1)):
31
32 //
            num z(cos(angle), sin(angle));
         for (int i = 1 << (base - 1): i < (1 << base): i++) {
33
            roots[i << 1] = roots[i];</pre>
34
35 //
             roots[(i << 1) + 1] = roots[i] * z;
            dbl angle i = angle * (2 * i + 1 - (1 << base)):
            roots[(i << 1) + 1] = num(cos(angle i), sin(angle i));
37
         }
38
39
         base++;
       }
40
     }
41
42
      void fft(vector<num> &a. int n = -1) {
43
       if (n == -1) {
44
45
         n = a.size();
        assert((n & (n - 1)) == 0);
47
       int zeros = __builtin_ctz(n);
48
49
        ensure base(zeros);
        int shift = base - zeros:
50
       for (int i = 0: i < n: i++) {
51
         if (i < (rev[i] >> shift)) {
52
53
            swap(a[i], a[rev[i] >> shift]):
         }
54
       }
         for (int k = 1; k < n; k <<= 1) {
57
         for (int i = 0; i < n; i += 2 * k) {
           for (int j = 0; j < k; j++) {
59
              num z = a[i + j + k] * roots[j + k];
             a[i + j + k] = a[i + j] - z;
              a[i + j] = a[i + j] + z;
61
            7-
62
63
         }
64
       7*/
        for (int len = 1; len < n; len <<= 1) {
65
         for (int i = 0; i < n; i += 2 * len) {
67
            for (int j = i, k = i + len; j < i + len; j++, k++) {
68
             num z = a[k] * roots[k - i];
             a[k] = a[i] - z;
70
             a[i] = a[i] + z;
71
            }
```

```
}
 74
      }
 75
      vector < num > fa. fb:
 76
 77
 78
       vector<long long> multiply(vector<int> &a, vector<int> &b) {
 79
         int need = a.size() + b.size() - 1:
 80
        int nbase = 0;
        while ((1 << nbase) < need) nbase++:
 81
         ensure base(nbase);
        int sz = 1 << nbase;</pre>
        if (sz > (int) fa.size()) {
          fa.resize(sz):
 86
        }
        for (int i = 0; i < sz; i++) {
          int x = (i < (int) a.size() ? a[i] : 0);
          int v = (i < (int) b.size() ? b[i] : 0):
          fa[i] = num(x, y);
        }
 91
 92
        fft(fa, sz);
        num r(0, -0.25 / sz):
         for (int i = 0: i \le (sz >> 1): i++) {
          int j = (sz - i) & (sz - 1);
          num z = (fa[j] * fa[j] - conj(fa[i] * fa[i])) * r;
          if (i != i) {
            fa[j] = (fa[i] * fa[i] - conj(fa[j] * fa[j])) * r;
          }
100
          fa[i] = z;
101
102
        fft(fa, sz);
        vector<long long> res(need);
104
        for (int i = 0; i < need; i++) {
105
          res[i] = fa[i].x + 0.5;
106
        }
107
         return res;
108
109
110
       vector<int> multiply_mod(vector<int> &a, vector<int> &b, int m, int eq =
1111
        int need = a.size() + b.size() - 1;
112
        int nbase = 0:
         while ((1 << nbase) < need) nbase++;
```

```
114
         ensure base(nbase):
         int sz = 1 << nbase;</pre>
115
         if (sz > (int) fa.size()) {
116
117
           fa.resize(sz);
         }
118
         for (int i = 0: i < (int) a.size(): i++) {
119
           int x = (a[i] \% m + m) \% m;
120
          fa[i] = num(x & ((1 << 15) - 1), x >> 15):
121
122
         }
         fill(fa.begin() + a.size(), fa.begin() + sz. num {0, 0}):
123
         fft(fa, sz);
124
         if (eq) {
125
           copy(fa.begin(), fa.begin() + sz, fb.begin());
126
127
        } else {
           if (sz > (int) fb.size()) {
128
129
             fb.resize(sz);
130
131
           for (int i = 0: i < (int) b.size(): i++) {
             int x = (b[i] \% m + m) \% m;
132
             fb[i] = num(x & ((1 << 15) - 1), x >> 15):
133
134
          fill(fb.begin() + b.size(), fb.begin() + sz, num {0, 0}):
135
          fft(fb, sz):
136
137
         }
138
         dbl ratio = 0.25 / sz:
139
         num r2(0, -1);
         num r3(ratio, 0):
140
         num r4(0, -ratio);
141
142
         num r5(0, 1);
         for (int i = 0: i <= (sz >> 1): i++) {
143
           int j = (sz - i) & (sz - 1);
144
145
           num a1 = (fa[i] + conj(fa[j]));
           num a2 = (fa[i] - conj(fa[j])) * r2;
146
147
           num b1 = (fb[i] + conj(fb[j])) * r3;
           num b2 = (fb[i] - conj(fb[j])) * r4;
148
          if (i != j) {
149
             num c1 = (fa[j] + conj(fa[i]));
150
             num c2 = (fa[j] - conj(fa[i])) * r2;
151
152
             num d1 = (fb[j] + conj(fb[i])) * r3;
             num d2 = (fb[j] - conj(fb[i])) * r4;
153
             fa[i] = c1 * d1 + c2 * d2 * r5;
154
             fb[i] = c1 * d2 + c2 * d1:
155
156
          }
```

```
157
           fa[i] = a1 * b1 + a2 * b2 * r5;
158
           fb[i] = a1 * b2 + a2 * b1;
159
        }
160
         fft(fa, sz);
161
         fft(fb, sz):
162
         vector<int> res(need):
163
         for (int i = 0; i < need; i++) {
164
           long long aa = fa[i].x + 0.5;
165
          long long bb = fb[i].x + 0.5;
166
          long long cc = fa[i].v + 0.5:
167
           res[i] = (aa + ((bb \% m) << 15) + ((cc \% m) << 30)) \% m;
168
        }
169
         return res:
170
171
172
       vector<int> square mod(vector<int> &a, int m) {
173
         return multiply mod(a, a, m, 1);
174
175
      // fft::multiply uses dbl, outputs vector<long long> of rounded values
176
      // fft::multiply mod might work for res.size() up to 2^21
      // typedef long double dbl;
                                                       up to 2^25 (but takes a lot
            of memoru)
178 }:
```

6.7 fftfast.cpp

```
1 // FFT MAXN = 2^k
2 // fft_init() to precalc FFT_MAXN-th roots
4 typedef long double db:
5 const int FFT MAXN = 262144:
6 const int N = 3.1e5:
7 const db pi = acosl(-1.);
8 struct cp {
           db a. b:
           cp operator+(const cp &y) const { return (cp){a + y.a, b + y.b}; }
           cp operator-(const cp &y) const { return (cp){a - y.a, b - y.b}; }
11
           cp operator*(const cp &y) const { return (cp){a * y.a - b * y.b, a *
12
                v.b + b * v.a; }
           cp operator!() const { return (cp){a, -b}: }:
14 } nw[FFT MAXN + 1];
15 int bitrev[FFT MAXN];
16 void dft(cp *a, int n, int flag = 1) {
```

```
17
           int d = 0:
18
            while ((1 \ll d) * n != FFT MAXN) d++;
           rep(i, 0, n - 1) if (i < (bitrev[i] >> d)) swap(a[i], a[bitrev[i] >>
19
                 d]);
           for (int 1 = 2: 1 <= n: 1 <<= 1) {
20
21
                   int del = FFT_MAXN / 1 * flag;
22
                    for (int i = 0; i < n; i += 1) {
                            cp *le = a + i, *ri = a + i + (l >> 1), *w = flag ==
23
                                 1 ? nw : nw + FFT MAXN;
24
                            rep(k, 0, 1 / 2 - 1) {
25
                                    cp ne = *ri * *w;
26
                                    *ri = *le - ne, *le = *le + ne;
27
                                    le++, ri++, w += del:
28
                           }
29
                   }
30
31
            if (flag != 1) rep(i, 0, n - 1) a[i].a /= n, a[i].b /= n;
33 void fft_init() {
34
           int L = 0:
35
            while ((1 << L) != FFT MAXN) L++;
36
           bitrev[0] = 0:
           rep(i, 1, FFT MAXN - 1) bitrev[i] = bitrev[i >> 1] >> 1 | ((i & 1)
37
                << (L - 1));
38
           nw[0] = nw[FFT MAXN] = (cp){1. 0}:
39
           rep(i, 0, FFT MAXN)
           nw[i] = (cp){cosl(2 * pi / FFT_MAXN * i), sinl(2 * pi / FFT_MAXN * i)}
                )}; // very slow
41 }
   void convo(db *a, int n, db *b, int m, db *c) {
44
            static cp f[FFT_MAXN >> 1], g[FFT_MAXN >> 1], t[FFT_MAXN >> 1];
45
           int N = 2:
46
            while (N \le n + m) N \le 1;
47
           rep(i, 0, N - 1) if (i & 1) {
                   f[i >> 1].b = (i <= n) ? a[i] : 0.0;
                    g[i >> 1].b = (i <= m) ? b[i] : 0.0:
50
           }
51
            else {
52
                   f[i >> 1].a = (i <= n) ? a[i] : 0.0;
                    g[i >> 1].a = (i <= m) ? b[i] : 0.0;
53
54
           }
55
            dft(f, N >> 1);
```

```
56
            dft(g, N >> 1);
57
            int del = FFT MAXN / (N >> 1);
58
            cp qua = (cp)\{0, 0.25\}, one = (cp)\{1, 0\}, four = (cp)\{4, 0\}, *w = nw
            rep(i, 0, N / 2 - 1) {
59
                    int j = i ? (N >> 1) - i : 0;
60
                    t[i] = (four * !(f[i] * g[i]) - (!f[i] - f[i]) * (!g[i] - g[i])
                        il) * (one + *w)) * qua:
62
                    w += del;
            }
            dft(t, N >> 1, -1);
            rep(i, 0, n + m) c[i] = (i & 1) ? t[i >> 1].a : t[i >> 1].b;
66 }
68 int mo:
69 void mul(int *a, int *b, int n) { // n \le N, 0 \le a[i], b[i] \le mo
70
            static cp f[N], g[N], t[N], r[N];
71
            int nn = 2:
72
            while (nn \le n + n) nn \le 1;
            rep(i, 0, nn - 1) {
73
                    f[i] = (i \le n) ? (cp){(db)(a[i] >> 15), (db)(a[i] & 32767)}
74
                         : (cp){0, 0}:
                    g[i] = (i \le n) ? (cp) \{(db)(b[i] >> 15), (db)(b[i] & 32767)\}
75
                         : (cp)\{0, 0\};
76
            }
            swap(n, nn);
77
            dft(f, n, 1);
78
            dft(g, n, 1);
79
80
            rep(i, 0, n - 1) {
81
                   int i = i ? n - i : 0:
82
                    t[i] = ((f[i] + !f[j]) * (!g[j] - g[i]) + (!f[j] - f[i]) * (
                        g[i] + !g[j])) * (cp){0, 0.25};
83
                    r[i] = (!f[j] - f[i]) * (!g[j] - g[i]) * (cp){-0.25, 0} + (
                        cp){0, 0.25} * (f[i] + !f[j]) * (g[i] + !g[j]);
84
            }
            dft(t, n, -1);
            dft(r, n, -1);
            rep(i, 0, n - 1)
            a[i] = ((11(t[i].a + 0.5) \% mo << 15) + 11(r[i].a + 0.5) + (11(r[i].a))
                b + 0.5) % mo << 30)) % mo:
89 }
```

6.8 fftnew.cpp

```
namespace fft {
    typedef double dbl;
   struct num {
      dbl x, y;
      num() { x = y = 0; }
     num(dbl x_{-}, dbl y_{-}) : x(x_{-}), y(y_{-}) {}
10
11 inline num operator+(num a, num b) { return num(a.x + b.x, a.y + b.y); }
    inline num operator-(num a, num b) { return num(a.x - b.x, a.y - b.y); }
13 inline num operator*(num a, num b) { return num(a.x * b.x - a.y * b.y, a.x *
         b.v + a.v * b.x); }
14 inline num conj(num a) { return num(a.x, -a.y); }
15
16 int base = 1:
    vector<num> roots = \{\{0, 0\}, \{1, 0\}\};
    vector < int > rev = \{0, 1\};
19
    const dbl PI = static cast<dbl>(acosl(-1.0));
21
    void ensure base(int nbase) {
      if (nbase <= base) {</pre>
24
        return:
25
      rev.resize(1 << nbase):
26
      for (int i = 0; i < (1 << nbase); i++) {
27
        rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
28
29
30
      roots.resize(1 << nbase);</pre>
      while (base < nbase) {
31
        dbl \ angle = 2 * PI / (1 << (base + 1));
32
            num z(cos(angle), sin(angle));
        for (int i = 1 << (base - 1); i < (1 << base); i++) {
34
35
          roots[i << 1] = roots[i];</pre>
              roots \lceil (i \ll 1) + 1 \rceil = roots \lceil i \rceil * z:
36 //
          dbl angle i = angle * (2 * i + 1 - (1 << base));
37
          roots[(i << 1) + 1] = num(cos(angle i), sin(angle i)):
38
39
       }
40
        base++;
    }
41
```

```
42 }
43
44 void fft(vector<num>& a. int n = -1) {
     if (n == -1) {
       n = (int) a.size():
47
     assert((n & (n - 1)) == 0);
     int zeros = __builtin_ctz(n);
     ensure base(zeros);
51
     int shift = base - zeros:
     for (int i = 0; i < n; i++) {
      if (i < (rev[i] >> shift)) {
54
          swap(a[i], a[rev[i] >> shift]);
55
       }
56
    }
57
     for (int k = 1; k < n; k <<= 1) {
       for (int i = 0; i < n; i += 2 * k) {
         for (int j = 0; j < k; j++) {
           num z = a[i + j + k] * roots[j + k];
           a[i + j + k] = a[i + j] - z;
           a[i + j] = a[i + j] + z;
         }
       }
66 }
67
   vector<num> fa, fb;
    vector<int64_t> square(const vector<int>& a) {
71
     if (a.empty()) {
72
       return {};
73
     }
74
     int need = (int) a.size() + (int) a.size() - 1;
     int nbase = 1;
     while ((1 << nbase) < need) nbase++;</pre>
76
      ensure base(nbase);
     int sz = 1 \ll nbase:
     if ((sz >> 1) > (int) fa.size()) {
80
       fa.resize(sz >> 1);
81
    for (int i = 0; i < (sz >> 1); i++) {
      int x = (2 * i < (int) a.size() ? a[2 * i] : 0);
       int y = (2 * i + 1 < (int) a.size() ? a[2 * i + 1] : 0);
```

```
fa[i] = num(x, y);
      }
      fft(fa. sz >> 1):
 87
 88
       num r(1.0 / (sz >> 1), 0.0);
       for (int i = 0: i \le (sz >> 2): i++) {
 89
         int j = ((sz >> 1) - i) & ((sz >> 1) - 1);
 90
 91
         num fe = (fa[i] + conj(fa[j])) * num(0.5, 0);
         num fo = (fa[i] - coni(fa[i])) * num(0, -0.5):
 92
 93
         num aux = fe * fe + fo * fo * roots[(sz >> 1) + i] * roots[(sz >> 1) + i]
             1:
 94
         num tmp = fe * fo;
         fa[i] = r * (conj(aux) + num(0, 2) * conj(tmp));
 95
         fa[i] = r * (aux + num(0, 2) * tmp):
 97
      }
      fft(fa, sz >> 1):
 98
       vector<int64 t> res(need);
       for (int i = 0; i < need; i++) {
100
101
         res[i] = llround(i % 2 == 0 ? fa[i >> 1].x : fa[i >> 1].v):
102
103
      return res:
104 }
105
     vector<int64 t> multiply(const vector<int>& a. const vector<int>& b) {
106
107
       if (a.empty() || b.empty()) {
108
         return {}:
      }
109
      if (a == b) {
110
111
         return square(a);
112
      int need = (int) a.size() + (int) b.size() - 1:
113
       int nbase = 1;
114
115
       while ((1 << nbase) < need) nbase++;</pre>
       ensure base(nbase):
116
       int sz = 1 \ll nbase:
117
      if (sz > (int) fa.size()) {
118
119
        fa.resize(sz):
120
      }
       for (int i = 0; i < sz; i++) {
121
122
         int x = (i < (int) a.size() ? a[i] : 0);</pre>
123
        int y = (i < (int) b.size() ? b[i] : 0);</pre>
        fa[i] = num(x, y);
124
      }
125
      fft(fa, sz);
```

```
127
       num r(0, -0.25 / (sz >> 1)):
128
      for (int i = 0; i <= (sz >> 1); i++) {
      int i = (sz - i) & (sz - 1):
130
        num z = (fa[j] * fa[j] - conj(fa[i] * fa[i])) * r;
        fa[j] = (fa[i] * fa[i] - conj(fa[j] * fa[j])) * r;
131
132
        fa[i] = z:
133
134
      for (int i = 0: i < (sz >> 1): i++) {
135
        num A0 = (fa[i] + fa[i + (sz >> 1)]) * num(0.5, 0);
136
        num A1 = (fa[i] - fa[i + (sz >> 1)]) * num(0.5, 0) * roots[(sz >> 1) + i
            ];
137
        fa[i] = A0 + A1 * num(0, 1);
138
139
      fft(fa, sz >> 1);
140
      vector<int64 t> res(need):
141
      for (int i = 0; i < need; i++) {
142
        res[i] = 1 \cdot (i \cdot \% 2 == 0 \cdot fa[i >> 1].x : fa[i >> 1].y);
143
144
      return res;
145 }
146
147 vector<int> multiply mod(const vector<int>& a. const vector<int>& b. int m)
148
      if (a.empty() || b.empty()) {
149
        return {}:
150
151
      int eq = (a.size() == b.size() && a == b);
      int need = (int) a.size() + (int) b.size() - 1;
153
      int nbase = 0;
154
       while ((1 << nbase) < need) nbase++:
155
       ensure base(nbase);
      int sz = 1 \ll nbase:
      if (sz > (int) fa.size()) {
158
      fa.resize(sz);
159
160
      for (int i = 0; i < (int) a.size(); i++) {
161
        int x = (a[i] \% m + m) \% m:
162
        fa[i] = num(x & ((1 << 15) - 1), x >> 15);
163
164
      fill(fa.begin() + a.size(), fa.begin() + sz, num {0, 0});
      fft(fa. sz):
      if (sz > (int) fb.size()) {
167
        fb.resize(sz);
```

```
168
      }
       if (eq) {
169
170
         copy(fa.begin(), fa.begin() + sz, fb.begin());
171
      } else {
         for (int i = 0: i < (int) b.size(): i++) {
172
          int x = (b[i] \% m + m) \% m;
173
           fb[i] = num(x & ((1 << 15) - 1), x >> 15);
174
175
176
         fill(fb.begin() + b.size(), fb.begin() + sz, num {0, 0});
         fft(fb, sz):
177
      }
178
       dbl ratio = 0.25 / sz;
179
       num r2(0, -1):
180
181
       num r3(ratio, 0);
       num r4(0, -ratio);
182
       num r5(0, 1);
183
       for (int i = 0; i \le (sz >> 1); i++) {
184
185
         int j = (sz - i) & (sz - 1);
186
         num a1 = (fa[i] + conj(fa[j]));
         num a2 = (fa[i] - conj(fa[j])) * r2;
187
188
         num b1 = (fb[i] + conj(fb[j])) * r3;
         num b2 = (fb[i] - conj(fb[j])) * r4;
189
         if (i != j) {
190
191
          num c1 = (fa[j] + conj(fa[i]));
192
          num c2 = (fa[j] - conj(fa[i])) * r2;
193
          num d1 = (fb[j] + conj(fb[i])) * r3;
           num d2 = (fb[j] - conj(fb[i])) * r4;
194
195
           fa[i] = c1 * d1 + c2 * d2 * r5;
196
          fb[i] = c1 * d2 + c2 * d1;
197
         fa[j] = a1 * b1 + a2 * b2 * r5;
198
199
         fb[j] = a1 * b2 + a2 * b1;
      }
200
201
       fft(fa, sz);
       fft(fb, sz);
202
203
       vector<int> res(need);
       for (int i = 0; i < need; i++) {
204
         int64 t aa = llround(fa[i].x);
205
206
         int64_t bb = llround(fb[i].x);
         int64_t cc = llround(fa[i].y);
207
         res[i] = static cast<int>((aa + ((bb % m) << 15) + ((cc % m) << 30)) % m
             );
      }
209
```

```
210 return res;
211 }
212
213 } // namespace fft
```

6.9 FST.cpp

```
1 void fst(VI &a,bool inv) {
        for (int n=SZ(a),step=1;step<n;step*=2) {</pre>
3
            for (int i=0; i<n; i+=2*step) rep(j,i,i+step-1) {
                int &u=a[j],&v=a[j+step];
5
                tie(u,v)=
                inv?PII(v-u,u):PII(v,u+v); // AND
                inv?PII(v,u-v):PII(u+v,u); // OR
                PII(u+v,u-v): // XOR
           }
11
       if (inv) for (auto &x : a) x/=SZ(a); // XOR only
12 }
13 VI conv(VI a, VI b) {
       fst(a,0),fst(b,0);
       rep(i,0,SZ(a)-1) a[i]=a[i]*b[i];
       fst(a.1): return a:
17 }
```

6.10 FWT.cpp

```
1 11 f[maxn], g[maxn], h[maxn];
2 int main() {
           for (int i = 0: i < n: i++) {
                    for (int j = 0; j < bit(n); j++) {
5
                            if ((j & bit(i)) == 0) {
                                    f[j] += f[j + bit(i)];
                                    g[j] += g[j + bit(i)];
                            }
                   }
10
11
           for (int i = 0: i < bit(n): i++) {
12
                   f[i] %= mod;
13
                    g[i] %= mod:
14
                   h[i] = f[i] * g[i] % mod;
15
16
           for (int i = 0: i < n: i++) {
```

```
17
                     for (int j = 0; j < bit(n); j++) {
18
                             if ((j & bit(i)) == 0)
                                      h[j] -= h[j + bit(i)];
19
20
                    }
21
            }
22
            for (int i = 0; i < bit(n); i++) {
23
                    h[i] %= mod;
                    if (h[i] < 0) h[i] += mod;
24
25
            }
26
27
            11 \text{ ans} = 0;
            rep(i, 0, bit(n) - 1) ans ^= h[i];
28
            cout << ans << '\n';
29
30 }
```

6.11 gauss(合数).cpp

```
1 void gauss(int n) {
       int ans = 1;
       //rep(i,1,n) rep(j,1,n) p[i][j]%=mod;
       for (int i = 1; i <= n; i++) {
           for (int j = i + 1; j \le n; j++) {
                int x = i, y = j;
                while (p[x][i]) {
                   int t = p[y][i] / p[x][i];
                   for (int k = i; k \le n; k++)
                        p[y][k] = (p[y][k] - p[x][k] * t) % mod;
11
                    swap(x, y);
12
               }
               if (x == i) {
13
14
                   for (int k = i; k \le n; k++) swap(p[i][k], p[j][k]);
                    ans = -ans;
15
               }
16
17
           }
18
19 }
```

6.12 gauss.cpp

```
1    11 f[N][N];
2    11 v[N], a[N];
3    void gauss() {
4       for (int i = 1; i <= n; i++) {</pre>
```

```
5
            for (int j = i; j <= n; j++) {
                if (f[j][i] > f[i][i]) {
7
                    swap(v[i], v[j]);
                    for (int k = 1; k \le n; k++)
9
                        swap(f[j][k], f[i][k]);
10
                }
            }
11
12
            for (int j = i + 1; j \le n; j++) {
13
                if (f[i][i]) {
14
                    int delta = f[j][i] * fpow(f[i][i], mod - 2) % mod;
15
                    for (int k = i; k <= n; k++) {
16
                        f[j][k] -= f[i][k] * delta % mod;
17
                        if (f[j][k] < 0)
18
                            f[i][k] += mod;
19
                    }
20
                    v[j] -= v[i] * delta % mod;
21
                    if (v[i] < mod)
22
                        v[j] += mod;
               }
            }
24
25
        }
        for (int j = n; j > 0; j--) {
27
            for (int k = j + 1; k \le n; k++) {
28
                v[j] -= f[j][k] * a[k] % mod;
29
                if (v[j] < 0)
                    v[i] += mod;
            a[j] = v[j] * fpow(f[j][j], mod - 2) % mod;
33
       }
34 }
```

6.13 linearbasis.cpp

```
1 struct linear_base {
2          11 w[64];
3          11 zero = 0;
4          11 tot = -1;
5          void clear() {
6              rep(i, 0, 63) w[i] = 0;
7              zero = 0;
8              tot = -1;
9          }
10          void insert(ll x) {
```

```
12
                if (x & bit(i))
                    if (!w[i]) {w[i] = x; return;}
13
14
                    else x ^= w[i];
            }
15
16
            zero++;
17
        void build() {
18
19
            rep(i, 0, 63) rep(j, 0, i - 1) {
                if (w[i]&bit(j)) w[i] ^= w[j];
20
21
            for (int i = 0; i <= 62; i++) {
22
                if (w[i] != 0) w[++tot] = w[i]:
23
24
            }
        }
25
26
        11 qmax() {
27
            11 \text{ res} = 0;
            for (int i = 62; i >= 0; i--) {
28
                res = max(res, res ^ w[i]);
            }
30
31
            return res;
32
        bool check(ll x) {
33
            for (int i = 62; i >= 0; i--) {
34
35
                if (x & bit(i))
                    if (!w[i]) return false;
                    else x ^= w[i];
37
38
            }
39
            return true;
        }
40
41
        11 query(11 k) {
42
            11 \text{ res} = 0;
43
            // if (zero) k=1;
44
            // if (k \ge bit(tot)) return -1;
            for (int i = tot; i >= 0; i--) {
45
                if (k & bit(i)) {
                    res = max(res, res ^ w[i]);
               } else {
                    res = min(res, res ^ w[i]);
                }
50
            }
51
52
            return res;
53
        }
```

for (int i = 62; i >= 0; i--) {

11

```
54 };
```

6.14 lucas.cpp

```
1 ll fac[maxn], fnv[maxn];
3 11 binom(11 a, 11 b) {
       if (b > a || b < 0) return 0;
       return fac[a] * fnv[a - b] % p * fnv[b] % p;
6 }
7
8 ll lucas(ll a, ll b, ll p) {
       ll ans = 1:
       while (a > 0 | | b > 0) {
11
           ans = (ans * binom(a % p, b % p)) % p;
          a /= p, b /= p;
12
13
14
       return ans;
15 }
16
17 int main() {
    cin >> p >> T;
   fac[0] = 1:
   rep(i, 1, p - 1) fac[i] = fac[i - 1] * i % p;
   fnv[p-1] = powmod(fac[p-1], p-2, p);
       per(i, p - 2, 0) fnv[i] = fnv[i + 1] * (i + 1) % p;
       assert(fnv[0] == 1);
24 }
```

6.15 mathdiv.cpp

```
1 ll floor_div(ll x, ll y) {
2     assert(y != 0);
3     if (y < 0) {
4         y = -y;
5         x = -x;
6     }
7     if (x >= 0) return x / y;
8     return (x + 1) / y - 1;
9 }
10 ll ceil_div(ll x, ll y) {
11     assert(y != 0);
12     if (y < 0) {
```

6.16 matrix.cpp

```
1 template <typename T>
2 vector<vector<T>> operator*(const vector<vector<T>>& a, const vector<vector<
        T>>& b) {
            if (a.empty() || b.empty()) {
                    return {{}};
            vector<vector<T>> c(a.size(), vector<T>(b[0].size()));
            for (int i = 0; i < static cast<int>(c.size()); i++) {
                    for (int j = 0; j < static_cast<int>(c[0].size()); j++) {
                            c[i][i] = 0;
                            for (int k = 0; k < static cast<int>(b.size()); k++)
10
                                    c[i][j] += a[i][k] * b[k][j];
11
12
13
                   }
14
           return c:
16 }
17
   template <typename T>
   vector<vector<T>>& operator *= (vector<T>>& a. const vector<vector<T>>&
         b) {
20
            return a = a * b;
21 }
22
   template <typename T, typename U>
   vector<vector<T>> power(const vector<vector<T>>& a, const U& b) {
25
            assert(b >= 0);
            vector<U> binary;
26
27
           U bb = b;
28
            while (bb > 0) {
                    binary.push_back(bb & 1);
30
                    bb >>= 1:
31
           }
```

```
32
           vector<vector<T>> res(a.size(), vector<T>(a.size()));
33
           for (int i = 0; i < static cast<int>(a.size()); i++) {
34
                    res[i][i] = 1:
35
           }
           for (int j = (int)binary.size() - 1; j >= 0; j--) {
                    res *= res:
                    if (binary[j] == 1) {
                            res *= a:
40
                   }
41
           }
42
            return res;
43 }
```

6.17 matrixfast.cpp

```
1 Description: Basic operations on square matrices.
2 Usage: Matrix<int, 3> A;
3 \text{ A.d} = \{\{\{1, 2, 3\}\}, \{\{4, 5, 6\}\}, \{\{7, 8, 9\}\}\}\};
4 vector<int> vec = {1, 2, 3};
5 \text{ vec} = (A^N) * \text{vec};
7 template < class T, int N > struct Matrix {
        typedef Matrix M;
9
        array<array<T, N>, N> d{};
        M operator*(const M& m) const {
11
            M a:
            rep(i, 0, N) rep(j, 0, N)
12
13
            rep(k, 0, N) a.d[i][j] += d[i][k] * m.d[k][j];
14
            return a;
15
        }
16
        vector<T> operator*(const vector<T>& vec) const {
17
            vector<T> ret(N);
            rep(i, 0, N) rep(j, 0, N) ret[i] += d[i][j] * vec[j];
18
19
            return ret;
20
        }
        M operator^(11 p) const {
21
22
            assert(p >= 0);
23
            M a. b(*this):
24
            rep(i, 0, N) a.d[i][i] = 1;
25
            while (p) {
26
                if (p & 1) a = a * b;
27
                b = b * b;
28
                 p >>= 1;
```

```
29 }
30 return a;
31 }
32 };
```

6.18 MillerRabbin pollard modmul.cpp

```
1 /*ModMulLL.h
2 Description: Calculate a b mod c (or a
   b mod c) for 0 a, b c 7.2 • 10^18
4 Time: O (1) for modmul, O (log b) for modpow*/
    /*ull modmul(ull a, ull b, ull M) {
        ll \ ret = a * b - M * ull(1.L / M * a * b):
        return ret + M * (ret < 0) - M * (ret >= (ll)M);
   ull modpow(ull b, ull e, ull mod) {
10
        ull \ ans = 1;
        for (; e; b = modmul(b, b, mod), e /= 2)
11
12
            if (e \& 1) ans = modmul(ans, b, mod);
13
        return ans;
14 }*/
15 ll modmul(ll a, ll b, ll m) {
       a \%= m, b \%= m;
16
       11 d = ((1db)a * b / m);
       d = a * b - d * m;
19
       if (d >= m) d -= m:
       if (d < 0) d += m;
21
       return d:
23 ll modpow(ll a, ll b, ll p) {
24
       ll ans = 1:
25
       while (b) {
           if (b & 1) ans = modmul(ans, a, p);
26
27
            a = modmul(a, a, p); b >>= 1;
       } return ans:
29 }
   /*MillerRabin.h
31 Description: Deterministic Miller-Rabin primality test. Guaranteed to
   work for numbers up to 7 . 1018; for larger numbers, use Python and extend A
         randomlu.
   Time: 7 times the complexity of a^b mod c.*/
   bool isPrime(ll n) {
       if (n < 2 | | n % 6 % 4 != 1) return (n | 1) == 3:
```

```
11 A[] = \{2, 325, 9375, 28178, 450775, 9780504, 1795265022\},
37
                  s = builtin ctzll(n - 1), d = n >> s;
       for (11 a : A) { // ^ count trailing zeroes
38
39
           ll p = modpow(a % n, d, n), i = s;
40
           while (p != 1 && p != n - 1 && a % n && i--)
41
                p = modmul(p, p, n);
42
           if (p != n - 1 && i != s) return 0;
44
       return 1;
45 }
46 /*Factor.h
   Description: Pollard-rho randomized factorization algorithm. Returns
   prime factors of a number, in arbitrary order (e.g. 2299 -> {11, 19, 11}).
    Time: O(n^{1}/4), less for numbers with small factors.*/
50 11 pollard(11 n) {
       auto f = [n](11 x) \{ return modmul(x, x, n) + 1; \};
       11 x = 0, y = 0, t = 30, prd = 2, i = 1, q;
       while (t++ \% 40 | | \_gcd(prd, n) == 1) {
54
           if (x == y) x = ++i, y = f(x);
           if ((q = modmul(prd, max(x, y) - min(x, y), n))) prd = q;
           x = f(x), y = f(f(y));
57
       return __gcd(prd, n);
59 }
60 vector<11> factor(11 n) {
       if (n == 1) return {};
       if (isPrime(n)) return {n};
       11 x = pollard(n);
       auto 1 = factor(x), r = factor(n / x);
       1.insert(1.end(), all(r));
       return 1;
67 }
```

6.19 ntt(polynomial).cpp

```
#include < bits / stdc + + . h >
using namespace std;

const int mod = 998244353;

inline void add(int &x, int y) {
    x += y;
    if (x >= mod) {
```

```
x -= mod;
11 }
12
13 inline void sub(int &x, int y) {
     x -= y;
     if (x < 0) {
        x += mod;
16
17
18 }
19
    inline int mul(int x, int y) {
      return (long long) x * y % mod;
21
22 }
23
    inline int power(int x, int y) {
      int res = 1;
26
     for (; y; y >>= 1, x = mul(x, x)) {
27
        if (y & 1) {
         res = mul(res, x);
28
29
       }
     }
30
31
      return res:
32 }
33
    inline int inv(int a) {
      a %= mod:
      if (a < 0) {
37
        a += mod;
      int b = mod, u = 0, v = 1;
39
      while (a) {
        int t = b / a:
41
        b -= t * a;
43
        swap(a, b);
        u = t * v;
        swap(u, v);
45
46
      if (u < 0) {
47
        u += mod;
      return u;
51 }
```

```
52
53 namespace ntt {
54 int base = 1, root = -1, max base = -1:
55 vector<int> rev = \{0, 1\}, roots = \{0, 1\};
57 void init() {
     int temp = mod - 1;
     max_base = 0;
     while (temp % 2 == 0) {
61
      temp >>= 1;
       ++max_base;
    }
64
     root = 2:
     while (true) {
        if (power(root, 1 << max_base) == 1 && power(root, 1 << (max_base - 1))</pre>
            != 1) {
          break;
       }
        ++root;
70
71 }
72
73 void ensure base(int nbase) {
     if (\max base == -1) {
75
       init();
76
     if (nbase <= base) {</pre>
78
       return;
79
80
      assert(nbase <= max base):
     rev.resize(1 << nbase);
      for (int i = 0; i < 1 << nbase; ++i) {
83
       rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (nbase - 1));
84
      roots.resize(1 << nbase);</pre>
      while (base < nbase) {</pre>
        int z = power(root, 1 << (max_base - 1 - base));</pre>
        for (int i = 1 << (base - 1); i < 1 << base; ++i) {
          roots[i << 1] = roots[i];
90
          roots[i << 1 | 1] = mul(roots[i], z);
91
       }
        ++base;
93
     }
```

```
94 }
 95
     void dft(vector<int> &a) {
 97
       int n = a.size(), zeros = builtin ctz(n);
       ensure base(zeros):
 98
       int shift = base - zeros;
 99
       for (int i = 0; i < n; ++i) {
100
         if (i < rev[i] >> shift) {
101
102
           swap(a[i], a[rev[i] >> shift]);
        }
103
      }
104
       for (int i = 1; i < n; i <<= 1) {
105
         for (int i = 0: i < n: i += i << 1) {
106
107
          for (int k = 0; k < i; ++k) {
             int x = a[j + k], y = mul(a[j + k + i], roots[i + k]);
108
             a[j + k] = (x + y) \% mod;
109
             a[j + k + i] = (x + mod - y) \% mod;
110
111
          }
112
         }
      }
113
114 }
115
     vector<int> multiply(vector<int> a. vector<int> b) {
116
       int need = a.size() + b.size() - 1, nbase = 0;
117
118
       while (1 << nbase < need) {
119
         ++nbase;
      }
120
121
       ensure base(nbase);
122
      int sz = 1 << nbase;</pre>
       a.resize(sz):
123
       b.resize(sz);
124
125
       bool equal = a == b;
       dft(a);
126
127
       if (equal) {
         b = a;
128
129
      } else {
         dft(b):
130
      }
131
132
       int inv_sz = inv(sz);
133
      for (int i = 0; i < sz; ++i) {
         a[i] = mul(mul(a[i], b[i]), inv sz);
134
      }
135
      reverse(a.begin() + 1, a.end());
136
```

```
137
       dft(a):
138
       a.resize(need);
       return a:
140 }
141
142
     vector<int> inverse new(const vector<int> &a) {
143
       assert(!a.empty());
144
       int n = (int) a.size();
145
       vector<int> b = {inv(a[0])};
146
       while ((int) b.size() < n) {</pre>
147
         vector<int> x(a.begin(), a.begin() + min(a.size(), b.size() << 1));</pre>
148
         x.resize(b.size() << 1);</pre>
149
         b.resize(b.size() << 1):</pre>
150
         vector<int> c = b;
151
         // NTT<T>::fft(c);
152
         // NTT < T > :: fft(x);
153
         dft(c);
154
         dft(x):
155
         // Modular < T > inv = 1 / static cast < Modular < T >> ((int) x.size());
         int inv sz = inv((int)x.size()):
156
157
         for (int i = 0; i < (int) x.size(); i++) {
           // x \lceil i \rceil *= c \lceil i \rceil * inv:
           x[i] = mul(x[i], mul(c[i], inv sz)):
160
         }
161
         reverse(x.begin() + 1, x.end());
162
         // NTT < T > :: fft(x);
163
         dft(x):
164
         rotate(x.begin(), x.begin() + (x.size() >> 1), x.end());
         fill(x.begin() + (x.size() >> 1), x.end(), 0);
166
         // NTT < T > :: fft(x):
167
         dft(x);
         for (int i = 0; i < (int) x.size(); i++) {</pre>
           // x \lceil i \rceil *= c \lceil i \rceil * inv:
170
           x[i] = mul(x[i], mul(c[i], inv sz));
171
172
         reverse(x.begin() + 1, x.end());
173
         // NTT < T > :: fft(x);
174
         dft(x);
175
         for (int i = 0; i < ((int) x.size() >> 1); i++) {
176
           // b[i + ((int) x.size() >> 1)] = -x[i];
177
           int t = 0; sub(t, x[i]);
178
           b[i + ((int) x.size() >> 1)] = t;
179
         }
```

```
180
      }
      b.resize(n);
181
      return b:
182
183 }
184
     vector<int> inverse(vector<int> a) {
185
       int n = a.size(), m = (n + 1) >> 1;
186
      if (n == 1) {
187
         return vector<int>(1, inv(a[0]));
188
      } else {
189
         vector<int> b = inverse(vector<int>(a.begin(), a.begin() + m));
190
         int need = n << 1, nbase = 0;
191
         while (1 << nbase < need) {
192
193
          ++nbase;
        }
194
         ensure base(nbase);
195
         int sz = 1 << nbase;</pre>
196
197
         a.resize(sz):
198
         b.resize(sz);
         dft(a):
199
200
         dft(b);
         int inv sz = inv(sz):
201
         for (int i = 0: i < sz: ++i) {
202
203
           a[i] = mul(mul(mod + 2 - mul(a[i], b[i]), b[i]), inv_sz);
204
        }
         reverse(a.begin() + 1, a.end());
205
         dft(a):
206
207
         a.resize(n);
         return a;
208
210 }
211 }
212
     using ntt::multiply;
213
     using ntt::inverse;
214
215
     vector<int>& operator += (vector<int> &a, const vector<int> &b) {
216
       if (a.size() < b.size()) {
217
218
         a.resize(b.size());
219
      for (int i = 0; i < b.size(); ++i) {
220
         add(a[i], b[i]);
221
222
      }
```

```
return a:
224 }
225
    vector<int> operator + (const vector<int> &a, const vector<int> &b) {
227
       vector<int> c = a:
228
      return c += b:
229 }
230
231
     vector<int>& operator -= (vector<int> &a, const vector<int> &b) {
232
      if (a.size() < b.size()) {
233
        a.resize(b.size());
234
235
      for (int i = 0: i < b.size(): ++i) {
236
        sub(a[i], b[i]);
237
      }
238
      return a;
239 }
240
     vector<int> operator - (const vector<int> &a, const vector<int> &b) {
242
      vector<int> c = a:
243
      return c -= b;
244 }
245
     vector<int>& operator *= (vector<int> &a, const vector<int> &b) {
247
      if (min(a.size(), b.size()) < 128) {
248
        vector<int> c = a;
249
        a.assign(a.size() + b.size() - 1, 0);
         for (int i = 0; i < c.size(); ++i) {
251
          for (int j = 0; j < b.size(); ++j) {
252
             add(a[i + j], mul(c[i], b[j]));
253
          }
254
        }
255
      } else {
256
        a = multiply(a, b);
257
258
      return a;
259 }
260
261
     vector<int> operator * (const vector<int> &a, const vector<int> &b) {
262
      vector<int> c = a:
263
      return c *= b;
264 }
265
```

```
vector<int>& operator /= (vector<int> &a. const vector<int> &b) {
       int n = a.size(), m = b.size();
267
      if (n < m) {
268
269
        a.clear();
      } else {
270
         vector<int> c = b:
271
         reverse(a.begin(), a.end());
272
         reverse(c.begin(), c.end());
273
274
         c.resize(n - m + 1);
         a *= inverse(c):
275
         a.erase(a.begin() + n - m + 1, a.end());
276
         reverse(a.begin(), a.end());
277
278
279
      return a;
280 }
281
     vector<int> operator / (const vector<int> &a, const vector<int> &b) {
282
283
       vector<int> c = a:
      return c /= b;
284
285 }
286
     vector<int>& operator %= (vector<int> &a. const vector<int> &b) {
287
       int n = a.size(), m = b.size();
288
       if (n >= m) {
289
290
         vector < int > c = (a / b) * b:
         a.resize(m - 1);
291
        for (int i = 0; i < m - 1; ++i) {
292
          sub(a[i], c[i]);
293
294
        }
      }
295
296
       return a;
297 }
298
299
     vector<int> operator % (const vector<int> &a, const vector<int> &b) {
      vector<int> c = a:
300
301
      return c %= b;
302 }
303
304
     vector<int> derivative(const vector<int> &a) {
305
      int n = a.size():
      vector<int> b(n - 1);
306
      for (int i = 1; i < n; ++i) {
307
        b[i - 1] = mul(a[i], i);
308
```

```
309
      }
310
      return b;
311 }
312
313 vector<int> primitive(const vector<int> &a) {
314
      int n = a.size():
315
      vector<int> b(n + 1), invs(n + 1);
316
      for (int i = 1: i <= n: ++i) {
        invs[i] = i == 1 ? 1 : mul(mod - mod / i, invs[mod % i]);
317
318
        b[i] = mul(a[i - 1], invs[i]):
319
     }
320
      return b;
321 }
322
323 vector<int> logarithm(const vector<int> &a) {
324
      vector<int> b = primitive(derivative(a) * inverse(a));
325
      b.resize(a.size());
326
      return b:
327 }
328
329
     vector<int> exponent(const vector<int> &a) {
330
       vector<int> b(1, 1):
331
       while (b.size() < a.size()) {</pre>
332
        vector<int> c(a.begin(), a.begin() + min(a.size(), b.size() << 1));</pre>
333
        add(c[0], 1):
334
        vector<int> old b = b;
        b.resize(b.size() << 1);</pre>
        c -= logarithm(b);
337
        c *= old b;
        for (int i = b.size() >> 1: i < b.size(): ++i) {
339
          b[i] = c[i];
340
        }
341
      }
342
      b.resize(a.size());
343
      return b:
344 }
345
     vector<int> power(vector<int> a, int m) {
347
      int n = a.size(), p = -1;
348
      vector<int> b(n);
349
      for (int i = 0; i < n; ++i) {
        if (a[i]) {
350
351
          p = i;
```

```
352
           break:
        }
      }
354
       if (p == -1) {
355
        b[0] = !m:
356
357
         return b;
358
      if ((long long) m * p >= n) {
359
360
        return b;
      }
361
       int mu = power(a[p], m), di = inv(a[p]);
362
       vector<int> c(n - m * p);
363
      for (int i = 0; i < n - m * p; ++i) {
364
365
        c[i] = mul(a[i + p], di);
      }
366
       c = logarithm(c);
367
      for (int i = 0; i < n - m * p; ++i) {
368
369
         c[i] = mul(c[i], m):
370
      }
      c = exponent(c);
371
372
      for (int i = 0; i < n - m * p; ++i) {
        b[i + m * p] = mul(c[i], mu):
373
374
      }
375
      return b;
376 }
377
     vector<int> sqrt(const vector<int> &a) {
378
379
       vector<int> b(1, 1);
380
       while (b.size() < a.size()) {</pre>
         vector<int> c(a.begin(), a.begin() + min(a.size(), b.size() << 1));</pre>
381
382
         vector<int> old b = b;
383
         b.resize(b.size() << 1):
        c *= inverse(b):
384
385
         for (int i = b.size() >> 1; i < b.size(); ++i) {
          b[i] = mul(c[i], (mod + 1) >> 1);
386
387
        }
388
      b.resize(a.size());
389
390
       return b:
391 }
392
     vector<int> multiply_all(int 1, int r, vector<vector<int>> &all) {
      if (1 > r) {
394
```

```
395
         return vector<int>():
396
      } else if (1 == r) {
        return all[1]:
398
      } else {
399
        int y = (1 + r) >> 1;
400
        return multiply_all(1, y, all) * multiply_all(y + 1, r, all);
401
402 }
403
     vector<int> evaluate(const vector<int> &f. const vector<int> &x) {
405
      int n = x.size();
406
      if (!n) {
407
        return vector<int>():
408
409
      vector<vector<int>> up(n * 2);
410
      for (int i = 0; i < n; ++i) {
411
         up[i + n] = vector < int > \{(mod - x[i]) \% mod, 1\};
412
413
      for (int i = n - 1; i; --i) {
414
         up[i] = up[i << 1] * up[i << 1 | 1];
415
416
      vector<vector<int>> down(n * 2):
417
       down[1] = f \% up[1]:
      for (int i = 2; i < n * 2; ++i) {
418
419
        down[i] = down[i >> 1] % up[i];
420
421
      vector<int> y(n);
422
       for (int i = 0; i < n; ++i) {
423
        y[i] = down[i + n][0];
424
425
       return y;
426 }
427
428
     vector<int> interpolate(const vector<int> &x, const vector<int> &y) {
429
      int n = x.size():
430
      vector<vector<int>> up(n * 2);
431
      for (int i = 0; i < n; ++i) {
432
         up[i + n] = vector < int > {(mod - x[i]) % mod, 1};
433
434
      for (int i = n - 1; i; --i) {
435
         up[i] = up[i << 1] * up[i << 1 | 1];
436
437
       vector<int> a = evaluate(derivative(up[1]), x);
```

```
for (int i = 0; i < n; ++i) {
438
         a[i] = mul(v[i], inv(a[i]));
439
440
      }
       vector<vector<int>> down(n * 2);
441
      for (int i = 0: i < n: ++i) {
442
         down[i + n] = vector < int > (1, a[i]);
443
      }
444
      for (int i = n - 1: i: --i) {
445
446
         down[i] = down[i << 1] * up[i << 1 | 1] + down[i << 1 | 1] * up[i << 1];
      }
447
       return down[1];
448
449 }
450
451 int main() {
452
453 }
```

6.20 simplex.cpp

* Author: Stanford

1 /**

```
* Source: Stanford Notebook
   * License: MIT
    * Description: Solves a general linear maximization problem: maximize $c^T
         x$ subject to $Ax \le b$, $x \qe 0$.
6 * Returns -inf if there is no solution, inf if there are arbitrarily good
         solutions, or the maximum value of $c^T x$ otherwise.
    * The input vector is set to an optimal $x$ (or in the unbounded case, an
         arbitrary solution fulfilling the constraints).
    * Numerical stability is not avaranteed. For better performance, define
         variables such that $x = 0$ is viable.
    * Usage:
    * vvd A = \{\{1, -1\}, \{-1, 1\}, \{-1, -2\}\}\}:
    * vd b = \{1, 1, -4\}, c = \{-1, -1\}, x;
    * T val = LPSolver(A, b, c).solve(x):
    * Time: O(NM * \#pivots), where a pivot may be e.g. an edge relaxation. O
         (2^n) in the general case.
    * Status: seems to work?
    */
15
16
   typedef long double T; // long double, Rational, double + mod <P>...
    typedef vector <T> vd;
   typedef vector < vd> vvd;
```

```
20
21 const T eps = 1e-8, inf = 1/.0;
22 #define MP make_pair
   #define ltj(X) if(s == -1 || MP(X[j],N[j]) < MP(X[s],N[s])) s=j
24
    struct LPSolver {
26
            int m, n;
27
            vector<int> N. B:
28
            vvd D;
29
30
            LPSolver(const vvd& A, const vd& b, const vd& c) :
31
                    m(b.size()), n(c.size()), N(n+1), B(m), D(m+2, vd(n+2)) {
32
                            for(int i = 0: i < m: i++){
33
                                    for(int j = 0; j < n; j++){
34
                                             D[i][j] = A[i][j];
                                    }
37
                            for(int i = 0: i < m: i++){
                                     B[i] = n+i; D[i][n] = -1; D[i][n+1] = b[i];
39
40
                            for(int j = 0; j < n; j++){
                                     N[i] = i: D[m][i] = -c[i]:
41
42
                            }
43
                            N[n] = -1; D[m+1][n] = 1;
44
                    }
45
            void pivot(int r, int s) {
46
                    T *a = D[r].data(), inv = 1 / a[s];
47
48
                    for(int i = 0; i < m+2; i++){
49
                            if (i != r && abs(D[i][s]) > eps) {
                                    T *b = D[i].data(), inv2 = b[s] * inv;
50
51
                                     for(int j = 0; j < n+2; j++){
52
                                             b[j] -= a[j] * inv2;
53
54
                                     b[s] = a[s] * inv2;
                            }
                    }
57
                    for(int j = 0; j < n+2; j++){
58
                            if (j != s) D[r][j] *= inv;
59
60
                    for(int i = 0; i < m+2; i++){
61
                            if (i != r) D[i][s] *= -inv;
62
                    }
```

```
63
                     D[r][s] = inv;
                     swap(B[r], N[s]);
 64
 65
             }
 66
             bool simplex(int phase) {
 67
                     int x = m + phase - 1;
 68
                     for (;;) {
 69
                              int s = -1:
 70
 71
                              for(int j = 0; j < n+1; j++){
 72
                                      if (N[j] != -phase) ltj(D[x]);
 73
 74
                              if (D[x][s] >= -eps) return true;
 75
                              int r = -1:
 76
                              for(int i = 0; i < m; i++){
 77
                                      if (D[i][s] <= eps) continue;</pre>
                                      if (r == -1 || MP(D[i][n+1] / D[i][s], B[i])
 78
 79
                                                       < MP(D[r][n+1] / D[r][s], B[
                                                           r])) r = i;
                              }
                              if (r == -1) return false:
 81
                              pivot(r, s);
                     }
             }
 84
 85
 86
             T solve(vd &x) {
                     int r = 0;
                     for(int i = 1; i < m; i++){
                              if (D[i][n+1] < D[r][n+1]) r = i;
 90
                     }
                     if (D[r][n+1] < -eps) {
 91
 92
                              pivot(r, n);
                              if (!simplex(2) || D[m+1][n+1] < -eps) return -inf;</pre>
                              for(int i = 0; i < m; i++) if (B[i] == -1) {
 94
 95
                                      int s = 0;
 96
                                      for(int j = 1; j < n+1; j++){
 97
                                              lti(D[i]);
                                      pivot(i, s);
100
                              }
101
                     }
                     bool ok = simplex(1); x = vd(n);
102
103
                     for(int i = 0; i < m; i++){
104
                              if (B[i] < n) \times [B[i]] = D[i][n+1];
```

```
105 }
106 return ok ? D[m][n+1] : inf;
107 }
108 };
```

6.21 区间互质.cpp

```
1 int p[N / 5], num;
2 void prime(int n) {
            num = 0:
4
           for (int i = 2; i * i <= n; i++) {
5
                   if ((n % i) == 0) {
6
                            p[++num] = i;
7
                            while ((n \% i) == 0) n /= i;
                   }
           }
10
            if (n > 1) p[++num] = n;
11 }
12 11 solve(11 r, int k) {
13
            prime(k);
14
           11 \text{ res} = 0;
15
            for (int i = 1; i < (1 << num); i++) {
16
                   int k = 0;
17
                   ll div = 1;
                    for (int j = 1; j \le num; j++) {
18
19
                            if (i & (1 << (j - 1))) {
20
                                    k++;
21
                                    div *= p[j];
                            }
23
                   }
24
                    if (k % 2)
25
                            res += r / div;
26
                    else
27
                            res -= r / div;
           }
29
            return r - res;
30 }
31 ll que(11 L, 11 R, 11 k) {
            return solve(R, k) - solve(L - 1, k);
33 }
```

6.22 幂转下降幂 (求幂和).cpp

```
1 ll comb[N][N];
2 11 s[maxn], inv[maxn], p;
3 // 1^k+2^k+...+n^k
4 void solve() {
            cin >> k >> n >> p;
            rep(i, 0, k + 1) {
                    comb[i][0] = comb[i][i] = 1;
                    rep(j, 1, i - 1) {
                            comb[i][j] = (comb[i - 1][j - 1] + comb[i - 1][j]) %
                                 p;
10
                   }
11
            }
            inv[1] = 1;
12
13
            rep(i, 2, k + 1) inv[i] = (p - p / i) * inv[p % i] % p;
            assert(inv[k] * k % p == 1);
14
15
16
            11 pw = 1;
            // (k+1)*S[k]=(n+1)^(k+1)-[0-k-1](k+1,j)*S[j]-1
17
18
            rep(i, 0, k) {
19
                    pw = pw * (n + 1) \% p;
20
                    s[i] = (pw - 1 + p) \% p;
                    rep(j, 0, i - 1) {
21
                            s[i] = (s[i] - comb[i + 1][j] * s[j] % p + p) % p;
22
23
                    s[i] = s[i] * inv[i + 1] % p;
24
25
26
            cout << s[k] << '\n';
27 }
```

6.23 扩展欧拉定理.cpp

```
1  // mod {min(b, b % phi + phi)}
2  ll calc(ll p) {
3     if (p == 1) return 0;
4     int phi = p, q = p;
5     for (int i = 2; i * i <= p; i++) {
6         if (q % i == 0) {
7             phi = phi / i * (i - 1);
8             while (q % i == 0) q /= i;
9         }
10     }
11     if (q != 1) phi = phi / q * (q - 1);</pre>
```

```
12 return powmod(2, calc(phi) + phi, p);
13 }
```

6.24 拉格朗日插值.cpp

```
1 // k阶多项式(需要k+1个点)
2 // 求在点n上的值
3 // O(k)
4 ll lagrange(ll n, int k) {
            vector < 11 > x(k + 5), y(k + 5);
6
           rep(i, 1, k + 1) {
7
                   x[i] = i;
8
                   // y[i] = (y[i-1] + powmod(i,k-1,mod)) \% mod;
9
            if (n \le k + 1) return v[n]:
10
11
12
            vector<ll> fac(k + 5);
13
           fac[0] = 1:
           ll coe = 1;
14
15
            rep(i, 1, k + 4) fac[i] = fac[i - 1] * i % mod:
16
           rep(i, 1, k + 1) coe = coe * (n - i + mod) % mod;
17
           11 \text{ ans} = 0;
18
           rep(i, 1, k + 1) {
19
                    ll sgn = (((k + 1 - i) \% 2) ? -1 : 1);
20
                    11 f1 = powmod(fac[i - 1] * fac[k + 1 - i] % mod, mod - 2.
                        mod);
21
                    11 f2 = powmod(n - i, mod - 2, mod);
                    ans += sgn * coe * f1 % mod * f2 % mod * y[i] % mod;
23
                    ans = (ans + mod) % mod;
24
           }
            return ans;
26 }
```

6.25 整除分块.cpp

```
1 void solve() {
2     u64 ans = 0;
3     cin >> n;
4     for (l1 l = 1; l <= n; l++) {
5         ll d = n / l, r = n / d;
6         ans += (l + r) * (r - l + 1) / 2 * d;
7         l = r;
8     }</pre>
```

```
9 }
```

6.26 枚举子集.cpp

```
1 void solve() {
2     f[0] = 1;
3     for (int i = 1; i < (111 << n); i++) {
4         int t = i;
5         ll res = 0;
6         while (true) {
7             if (t == 0) break;
8             t = (t - 1)&i;
9             res = (res + f[t]) % mod;
10         }
11         f[i] = res * i;
12     }
13 }</pre>
```

6.27 枚举超集.cpp

```
1 void solve() {
2    for (int i = 1; i < (111 << n); i++) {
3        int t = i;
4        while (true) {
5             t = (t + 1) | i;
6             if (t == bit(n) - 1) break;
7        }
8    }
9 }</pre>
```

6.28 狄利克雷卷积.cpp

```
12
            C ^= t ^ A:
13
            return C;
14 }
15
16 int main() {
17
            scanf("%d%u%u%u", &n, &A, &B, &C);
            for (int i = 1; i <= n; i++)
19
                    f[i] = rng61();
20
21
            p[1] = 1; mu[1] = 1;
22
            for (int i = 2; i <= n; i++) {
23
                    if (!p[i]) p[i] = i, mu[i] = (uint)-1, pr[++tot] = i;
                    for (int j = 1; j <= tot && pr[j] * i <= n; j++) {
24
25
                            p[i * pr[i]] = pr[i];
26
                            if (p[i] == pr[j]) {
27
                                    mu[i * pr[j]] = 0;
28
                                    break;
                            } else {
                                    mu[i * pr[j]] = (uint)-mu[i];
                            }
31
32
                   }
33
           }
            for (int d1 = 1: d1 \le n: d1++)
                    for (int d2 = 1; d1 * d2 <= n; d2++)
35
36
                            g[d1 * d2] += f[d1] * mu[d2]:
37
            uint ans = 0;
            for (int i = 1; i <= n; i++) ans ^= g[i];
            printf("%u\n", ans);
40 }
```

6.29 线性筛常见积性函数.cpp

```
12
                           f[i] = f[pe[i]] * f[i / pe[i]];
13
14
           for (uint i = 1: i <= n: i++) {
                   ans ^= (a * i * f[i] + b);
15
16
           }
           printf("%u\n", ans);
17
18 }
   int main() {
21
           scanf("%d%u%u", &n, &a, &b);
22
           p[1] = 1;
23
           for (int i = 2; i <= n; i++) {
                   if (!p[i]) p[i] = i, pe[i] = i, pr[++tot] = i;
24
25
                   for (int j = 1; j <= tot && pr[j] * i <= n; j++) {
26
                           p[i * pr[j]] = pr[j];
27
                           if (p[i] == pr[j]) {
28
                                   pe[i * pr[j]] = pe[i] * pr[j];
29
                           } else {
31
                                   pe[i * pr[j]] = pr[j];
32
                           }
33
                   }
34
           }
           // 因子个数, 因子和, 欧拉函数, 莫比乌斯函数
35
36
           compute(n, [&](int x) {
                   f[x] = f[x / p[x]] + 1;
           });
39
40
           compute(n, [&](int x) {
41
                   f[x] = f[x / p[x]] + x;
42
           });
43
44
           compute(n, [&](int x) {
45
                   f[x] = x / p[x] * (p[x] - 1);
46
           });
47
           compute(n, [&](int x) {
                   f[x] = x == p[x] ? -1 : 0;
50
           });
51 }
```

6.30 莫比乌斯反演 gcd 常见结论.cpp

```
1 // u * 1 = e, phi * 1 = id, phi = id * u
2 const int N = 10100000, M = 10000000:
3 int p[N], pr[N / 5], n, tot;
4 int mu[N], smu[N];
6 int main() {
           p[1] = 1; mu[1] = 1;
           for (int i = 2; i <= M; i++) {
                   if (!p[i]) p[i] = i, mu[i] = -1, pr[++tot] = i;
10
                    for (int j = 1; j \le tot && pr[j] * i \le M; j++) {
11
                            p[i * pr[j]] = pr[j];
12
                            if (p[i] == pr[j]) {
13
                                    mu[i * pr[j]] = 0;
14
                                    break:
15
                            } else {
                                    mu[i * pr[j]] = -mu[i];
16
17
                            }
                   }
18
           }
19
           for (int i = 1; i <= M; i++)
20
21
                    smu[i] = smu[i - 1] + mu[i]:
22
           int T;
23
           scanf("%d", &T);
24
           for (int tc = 0; tc < T; tc++) {
25
                    int n, m;
                   scanf("%d%d", &n, &m);
27
                   if (n > m) swap(n, m);
28
                   ll ans = 0:
                   for (int 1 = 1; 1 <= n; 1++) {
29
30
                            int n1 = n / 1, m1 = m / 1;
31
                            int r = min(n / n1, m / m1);
32
                            // l ... r
                            ans += 111 * (smu[r] - smu[1 - 1]) * n1 * m1:
33
34
                            1 = r:
35
                   }
                    printf("%lld\n", ans);
37
           }
38 }
```

7 String

7.1 ACAM.cpp

```
const int AC SIGMA = 26, AC V = 26, AC N = 810000;
    struct AC_automaton {
             struct node {
                      node *go[AC_V], *fail, *f;
    // declare extra variables:
             } pool[AC_N], *cur, *root, *q[AC_N];
             node* newnode() {
                      node *p = cur++;
    // init extra variables:
10
                      return p;
11
    // CALL init() and CHECK all const variables:
13
             void init() { cur = pool; root = newnode(); }
             node* append(node *p, int w) {
14
                      if (!p->go[w]) p->go[w] = newnode(), <math>p->go[w]->f = p;
15
16
                      return p->go[w];
17
             }
             void build() {
18
19
                     int t = 0:
20
                      q[t++] = root;
21
                      root->fail = root;
                      rep(i, 0, AC_SIGMA - 1) if (root->go[i]) {
22
23
                               q[t++] = root->go[i];
                               root->go[i]->fail = root;
24
25
                     } else {
                               root->go[i] = root;
26
27
28
                      rep(i, 1, t - 1) {
                               node *u = q[i];
29
30
                               rep(j, 0, AC_SIGMA - 1) if (u->go[j]) {
                                        u \rightarrow go[j] \rightarrow fail = u \rightarrow fail \rightarrow go[j];
31
32
                                        q[t++] = u->go[j];
                               } else {
                                        u \rightarrow go[j] = u \rightarrow fail \rightarrow go[j];
34
35
                               }
                      }
37
             }
39 typedef AC_automaton::node ACnode;
```

```
40
41 const int M = 2, N = 2.1e5;
42 struct node {
             node *son[M], *go[M], *fail;
             int cnt, vis, ins;
45 } pool[N], *cur = pool, *q[N], *root;
47 node *newnode() { return cur++; }
    int t, n;
49
    void build() {
51
             t = 0;
             q[t++] = root;
52
53
             for (int i = 0; i < t; i++) {
54
                      node *u = q[i];
                      for (int j = 0; j < M; j++) {
                               if (u->son[j]) {
57
                                         u \rightarrow go[j] = u \rightarrow son[j];
58
                                         if (u != root)
                                                  u->go[j]->fail = u->fail->go[j];
59
60
61
                                                  u \rightarrow go[j] \rightarrow fail = root;
                                         q[t++] = u->son[j];
62
63
                               } else {
64
                                         if (u != root)
                                                  u \rightarrow go[j] = u \rightarrow fail \rightarrow go[j];
                                         else
67
                                                  u->go[j] = root;
                               }
                      }
70
             }
71 }
72
    void insert(string &s) {
74
             node *cur = root;
             for (auto c : s) {
                      int w = c - '0';
77
                      if (!cur->son[w]) {
78
                               cur->son[w] = newnode();
79
                      cur = cur->son[w];
81
82
             cur->cnt = 1;
```

```
83 }
```

7.2 hash61.cpp

```
struct hash61 {
            static const uint64_t md = (1LL << 61) - 1;
            static uint64 t step;
            static vector<uint64_t> pw;
            uint64 t addmod(uint64 t a, uint64 t b) const {
                    a += b:
                    if (a >= md) a -= md;
                    return a;
10
           }
11
            uint64_t submod(uint64_t a, uint64_t b) const {
13
                    a += md - b;
                    if (a >= md) a -= md:
14
15
                    return a;
16
           }
17
            uint64 t mulmod(uint64 t a, uint64 t b) const {
18
                    uint64_t l1 = (uint32_t) a, h1 = a >> 32, l2 = (uint32_t) b,
19
                         h2 = b >> 32;
                    uint64 t 1 = 11 * 12, m = 11 * h2 + 12 * h1, h = h1 * h2;
                    uint64 t ret = (1 \& md) + (1 >> 61) + (h << 3) + (m >> 29) +
21
                         (m << 35 >> 3) + 1;
22
                    ret = (ret & md) + (ret >> 61):
                    ret = (ret & md) + (ret >> 61);
23
                    return ret - 1:
25
           }
26
27
            void ensure_pw(int sz) {
28
                    int cur = (int) pw.size();
                    if (cur < sz) {
29
30
                            pw.resize(sz);
31
                            for (int i = cur; i < sz; i++) {
                                    pw[i] = mulmod(pw[i - 1], step);
32
33
                            }
34
                    }
35
           }
36
37
            vector<uint64_t> pref;
```

```
38
            int n;
39
40
            template < typename T>
41
            hash61(const T& s) {
42
                    n = (int) s.size();
43
                    ensure_pw(n + 1);
                    pref.resize(n + 1);
                    pref[0] = 1:
46
                    for (int i = 0; i < n; i++) {
47
                            pref[i + 1] = addmod(mulmod(pref[i], step), s[i]);
                    }
49
           }
50
51
            inline uint64 t operator()(const int from, const int to) const {
52
                    assert(0 <= from && from <= to && to <= n - 1):
                    return submod(pref[to + 1], mulmod(pref[from], pw[to - from
                        + 1]));
54
           }
55 };
56
   uint64_t hash61::step = (md >> 2) + rng() % (md >> 1);
58 vector<uint64 t> hash61::pw = vector<uint64 t>(1, 1):
```

7.3 kmp.cpp

```
1 template <typename T>
  vector<int> kmp_table(int n, const T &s) {
3
           vector<int> p(n, 0);
4
           int k = 0;
           for (int i = 1: i < n: i++) {
                    while (k > 0 \&\& !(s[i] == s[k]))  {
7
                           k = p[k - 1];
                   }
                    if (s[i] == s[k]) {
10
                            k++:
11
                   }
12
                   p[i] = k;
13
14
           return p;
15 }
17 template <typename T>
  vector<int> kmp_table(const T &s) {
```

```
return kmp_table((int) s.size(), s);
20 }
21
   template <typename T>
   vector<int> kmp_search(int n, const T &s, int m, const T &w, const vector<
        int> &p) {
            assert(n >= 1 && (int) p.size() == n);
25
            vector<int> res:
           int k = 0;
           for (int i = 0: i < m: i++) {
27
28
                    while (k > 0 \&\& (k == n || !(w[i] == s[k]))) {
                            k = p[k - 1];
31
                    if (w[i] == s[k]) {
32
                            k++:
33
                   }
                    if (k == n) {
                            res.push_back(i - n + 1);
                   }
37
38
            // returns O-indexed positions of occurrences of s in w
41
   template <typename T>
   vector<int> kmp_search(const T &s, const T &w, const vector<int> &p) {
            return kmp_search((int) s.size(), s, (int) w.size(), w, p);
45 }
```

7.4 manacherfast.cpp

```
1 template <typename T>
2 vector<int> manacher(int n, const T &s) {
3         if (n == 0) {
4             return vector<int>();
5         }
6         vector<int> res(2 * n - 1, 0);
7         int l = -1, r = -1;
8         for (int z = 0; z < 2 * n - 1; z++) {
9             int i = (z + 1) >> 1;
10             int j = z >> 1;
11             int p = (i >= r ? 0 : min(r - i, res[2 * (1 + r) - z]));
12             while (j + p + 1 < n && i - p - 1 >= 0) {
```

```
13
                             if (!(s[j + p + 1] == s[i - p - 1])) {
14
                                      break;
15
                             }
16
                             p++;
                    }
17
18
                     if (j + p > r) {
19
                             1 = i - p;
                             r = j + p;
20
21
22
                    res[z] = p;
23
            }
24
            return res;
25
            // res[2 * i] = odd radius in position i
26
            // res[2 * i + 1] = even \ radius \ between \ positions \ i \ and \ i + 1
27
            // s = "abaa" \rightarrow res = \{0, 0, 1, 0, 0, 1, 0\}
            // in other words, for every z from 0 to 2 * n - 2:
            // calculate i = (z + 1) \gg 1 and j = z \gg 1
            // now there is a palindrome from i - res[z] to j + res[z]
            // (watch out for i > j and res[z] = 0)
32 }
34 template <typename T>
   vector<int> manacher(const T &s) {
            return manacher((int) s.size(), s);
37 }
```

7.5 MinRotation.cpp

```
Description: Finds the lexicographically smallest rotation of a string.
Usage: rotate(v.begin(), v.begin() + minRotation(v), v.end());
Time: O (N)

int minRotation(string s) {
   int a = 0, N = sz(s); s += s;
   rep(b, 0, N) rep(k, 0, N) {
      if (a + k == b || s[a + k] < s[b + k]) {b += max(0, k - 1); break;}
   if (s[a + k] > s[b + k]) { a = b; break; }
}
return a;
}
```

7.6 PAM.cpp

```
struct PAM {
            struct T {
                    array<int, 10> tr;
                    int fail, len, tag;
                    T(): fail(0), len(0), tag(0) {
                            tr.fill(0);
                    }
            };
            vector<T> t;
            vector<int> stk;
10
            int newnode(int len) {
11
12
                    t.emplace_back();
13
                    t.back().len = len;
                    return (int)t.size() - 1;
14
15
            PAM(): t(2) {
16
17
                    t[0].fail = 1, t[0].len = 0;
                    t[1].fail = 0, t[1].len = -1;
18
                    stk.push_back(-1);
19
20
            int getfail(int v) {
21
22
                    while (stk.end()[-2 - t[v].len] != stk.back()) {
                            v = t[v].fail;
23
24
                    }
25
                    return v;
26
27
            int insert(int lst, int c, int td) {
                    stk.emplace_back(c);
28
                    int x = getfail(lst);
29
                    if (!t[x].tr[c]) {
30
31
                            int u = newnode(t[x].len + 2);
32
                            t[u].fail = t[getfail(t[x].fail)].tr[c];
                            t[x].tr[c] = u;
33
                    }
34
                    t[t[x].tr[c]].tag += td;
                    return t[x].tr[c]:
37
            int build(int n) {
38
39
                    int ans = 0;
                    for (int i = (int)t.size() - 1; i > 1; i--) {
40
                            t[t[i].fail].tag += t[i].tag;
41
42
                            if (t[i].len > n) {
43
                                     continue:
```

7.7 rollingHash.cpp

```
1 typedef pair<int,int> hashv;
2 const ll mod1=1000000007;
   const 11 mod2=1000000009;
   // prefixSum trick for high dimensions
   hashv operator + (hashv a, hashv b) {
        int c1=a.fi+b.fi,c2=a.se+b.se;
9
       if (c1>=mod1) c1-=mod1;
10
       if (c2 \ge mod2) c2 = mod2:
11
       return mp(c1,c2);
12 }
13
   hashv operator - (hashv a, hashv b) {
15
        int c1=a.fi-b.fi.c2=a.se-b.se:
       if (c1<0) c1+=mod1;
       if (c2<0) c2+=mod2;
       return mp(c1,c2);
19 }
20
   hashv operator * (hashv a, hashv b) {
       return mp(111*a.fi*b.fi%mod1,111*a.se*b.se%mod2);
23 }
```

7.8 SA.cpp

```
1 #include <bits/stdc++.h>
2 using namespace std;
3
4 const int N = 101000;
5 char s[N];
6 int sa[N], rk[N], ht[N], n;
7 // O-based sa 表示第i大的为哪个, rk 表示第i个后缀第几大
```

```
8 // ht表示 lcp(sa[i], sa[i-1])
   void buildSA(char *s, int *sa, int *rk, int *ht, int n, int m = 128) {
            static int x[N], y[N], c[N];
10
11
            s[n] = 0;
12
            for (int i = 0: i < m: i++) c[i] = 0:
            for (int i = 0; i < n; i++) c[x[i] = s[i]]++;
13
            for (int i = 1; i < m; i++) c[i] += c[i - 1];
14
            for (int i = n - 1; i \ge 0; i--) sa[--c[x[i]]] = i;
15
16
            for (int k = 1; k < n; k <<= 1) {
                    int p=0:
17
18
                    for (int i = n - 1; i \ge n - k; i--) v[p++] = i;
                    for (int i = 0; i < n; i++) if (sa[i] >= k) v[p++] = sa[i] -
19
20
                    for (int i = 0; i < m; i++) c[i] = 0;
                    for (int i = 0: i < n: i++) c[x[v[i]]]++:
21
22
                    for (int i = 1; i < m; i++) c[i] += c[i-1];
23
                    for (int i = n - 1; i \ge 0; i--) sa[--c[x[y[i]]]] = y[i];
24
                    swap(x, y);
25
                    p = 1; x[sa[0]] = 0; y[n] = -1;
                    for (int i = 1: i < n: i++) {
26
27
                            if (y[sa[i-1]] == y[sa[i]] && y[sa[i-1] + k] ==
                                v[sa[i] + k])
                                    x[sa[i]] = p - 1:
28
29
                            else
30
                                    x[sa[i]] = p++;
31
                    }
                    if (p == n) break;
32
33
                    m = p;
34
            for (int i = 0: i < n: i++) rk[sa[i]] = i:
35
36
            int k = 0:
37
            for (int i = 0; i < n; i++) {
38
                    k = max(k - 1, 0);
39
                    if (rk[i] == 0) continue;
                    int j = sa[rk[i] - 1];
40
41
                    while (s[i + k] == s[j + k]) k++;
                    ht[rk[i]] = k;
            }
44 }
45
46 int LCP(int u, int v) {
47
            if (u == v) return n - u;
48
            if (rk[u] > rk[v]) swap(u, v);
```

7.9 SAfast.cpp

```
1 template <typename T>
2 vector<int> suffix array(int n, const T &s, int char bound) {
     vector<int> a(n):
     if (n == 0) {
5
       return a:
6
7
     if (char bound != -1) {
       vector<int> aux(char_bound, 0);
8
       for (int i = 0; i < n; i++) {
9
10
          aux[s[i]]++:
11
       }
12
        int sum = 0;
        for (int i = 0; i < char_bound; i++) {</pre>
14
         int add = aux[i];
15
         aux[i] = sum:
16
          sum += add;
17
       }
       for (int i = 0: i < n: i++) {
          a[aux[s[i]]++] = i;
19
20
       }
21
    } else {
       iota(a.begin(), a.end(), 0):
23
        sort(a.begin(), a.end(), [&s](int i, int j) { return s[i] < s[j]; });
24
25
     vector<int> sorted_by_second(n);
26
     vector<int> ptr_group(n);
     vector<int> new_group(n);
     vector<int> group(n);
29
     group[a[0]] = 0;
30
     for (int i = 1: i < n: i++) {
```

```
31
       group[a[i]] = group[a[i - 1]] + (!(s[a[i]] == s[a[i - 1]]));
     }
32
     int cnt = group[a[n - 1]] + 1;
33
34
      int step = 1;
      while (cnt < n) {
35
       int at = 0:
36
       for (int i = n - step; i < n; i++) {
37
          sorted_by_second[at++] = i;
39
       for (int i = 0: i < n: i++) {
40
41
         if (a[i] - step >= 0) {
            sorted by second[at++] = a[i] - step;
         }
43
       }
44
45
       for (int i = n - 1; i \ge 0; i--) {
46
         ptr_group[group[a[i]]] = i;
47
       for (int i = 0: i < n: i++) {
         int x = sorted_by_second[i];
49
         a[ptr_group[group[x]]++] = x;
50
51
52
       new group[a[0]] = 0:
       for (int i = 1: i < n: i++) {
53
         if (group[a[i]] != group[a[i - 1]]) {
54
55
           new_group[a[i]] = new_group[a[i - 1]] + 1;
         } else {
56
            int pre = (a[i - 1] + step >= n ? -1 : group[a[i - 1] + step]);
57
           int cur = (a[i] + step >= n ? -1 : group[a[i] + step]);
58
59
           new_group[a[i]] = new_group[a[i - 1]] + (pre != cur);
60
         }
       }
61
       swap(group, new_group);
       cnt = group[a[n - 1]] + 1;
63
64
       step <<= 1;
65
     return a;
67 }
   template <typename T>
   vector<int> suffix_array(const T &s, int char_bound) {
      return suffix array((int) s.size(), s, char bound);
72 }
73
```

```
74 template <typename T>
75 vector<int> build lcp(int n, const T &s, const vector<int> &sa) {
      assert((int) sa.size() == n):
77
      vector<int> pos(n);
      for (int i = 0; i < n; i++) {
79
        pos[sa[i]] = i;
81
      vector<int> lcp(max(n - 1, 0));
      int k = 0:
      for (int i = 0: i < n: i++) {
        k = max(k - 1, 0);
        if (pos[i] == n - 1) {
          k = 0:
        } else {
          int j = sa[pos[i] + 1];
          while (i + k < n &   i + k < n &   i + k < n &   s[i + k] == s[j + k]) {
            k++;
          }
91
          lcp[pos[i]] = k;
        }
93
      }
      return lcp:
96 }
98 template <typename T>
99 vector<int> build_lcp(const T &s, const vector<int> &sa) {
      return build_lcp((int) s.size(), s, sa);
101 }
```

7.10 SAM.cpp

```
struct SAM {
       static constexpr int ALPHABET_SIZE = 26;
3
        struct Node {
4
           int len:
           int link;
           std::array<int, ALPHABET_SIZE> next;
7
           Node() : len{}, link{}, next{} {}
       };
       std::vector<Node> t:
10
       SAM() {
11
            init();
12
       }
```

```
13
       void init() {
14
           t.assign(2, Node());
           t[0].next.fill(1):
15
16
           t[0].len = -1;
       }
17
       int newNode() {
18
           t.emplace back();
19
            return t.size() - 1:
20
21
       int extend(int p, int c) {
22
23
           if (t[p].next[c]) {
24
                int q = t[p].next[c];
                if (t[q].len == t[p].len + 1) {
25
26
                    return q;
27
               }
28
                int r = newNode();
29
                t[r].len = t[p].len + 1;
                t[r].link = t[a].link:
31
                t[r].next = t[q].next;
                t[a].link = r:
32
                while (t[p].next[c] == q) {
33
                   t[p].next[c] = r:
34
                    p = t[p].link:
36
37
                return r:
38
            int cur = newNode();
            t[cur].len = t[p].len + 1;
41
            while (!t[p].next[c]) {
                t[p].next[c] = cur;
43
                p = t[p].link;
44
            t[cur].link = extend(p, c);
45
46
            return cur;
47
       }
48 };
   7.11 SA-IS.cpp
```

```
4
                                                        LCP: O(N) time and space
                              1. Suffix Array (returns s.size() elements. NOT considering
          O-length/empty suffix)
                                             auto sa = suffix_array(s); // s is the input string with
                     ASCIT
         characters
10 *
                                             auto sa wide char = suffix array(s, LIM); // LIM = max(s[i])
                      + 2.
          s is the string with arbitary big characters.
12
                              2. LCP:
13 *
                                           auto lcp = LCP(s, suffix array(s)); // returns s.size()
14 where lcp[i]=LCP(sa[i], sa[i+1])
15 * Status: Tested (DMOJ: ccc03s1. SPOJ: SARRAY (100pts). Yosupo's: Suffix
         & Number of Substrings, CodeForces EDU
        // Based on: Rickypon, https://judge.yosupo.jp/submission/10105
         void induced_sort(const std::vector<int>& vec, int val_range,
20
                                                    std::vector<int>& SA, const std::vector<bool>& sl,
21
                                                   const std::vector<int>& lms idx) {
22
                  std::vector<int> 1(val range, 0), r(val range, 0);
23
                  for (int c : vec) {
24
                           if (c + 1 < val range) ++1[c + 1]:
25
                           ++r[c]:
                 }
26
27
                  std::partial sum(l.begin(), l.end(), l.begin());
28
                  std::partial_sum(r.begin(), r.end(), r.begin());
                  std::fill(SA.begin(), SA.end(), -1);
29
                  for (int i = (int)lms idx.size() - 1; i >= 0; --i)
30
31
                           SA[--r[vec[lms_idx[i]]]] = lms_idx[i];
32
                  for (int i : SA)
33
                           if (i \ge 1 \&\& sl[i - 1]) SA[l[vec[i - 1]]++] = i - 1;
34
                  std::fill(r.begin(), r.end(), 0);
                  for (int c : vec) ++r[c];
                  std::partial_sum(r.begin(), r.end(), r.begin());
37
                  for (int k = (int)SA.size() - 1, i = SA[k]; k \ge 1; k \ge 1;
                           if (i >= 1 && !sl[i - 1]) {
39
                                      SA[--r[vec[i - 1]]] = i - 1;
40
                           }
41 }
42
```

```
43 std::vector<int> SA IS(const std::vector<int>& vec. int val range) {
                                                                                           85
        const int n = vec.size();
                                                                                                   }
44
        std::vector<int> SA(n). lms idx:
45
46
        std::vector<bool> sl(n);
                                                                                           89 }
        sl[n - 1] = false:
47
                                                                                           90
        for (int i = n - 2; i \ge 0; --i) {
48
            sl[i] = (vec[i] > vec[i + 1] || (vec[i] == vec[i + 1] && sl[i + 1]))
49
                                                                                           92
                                                                                           93
50
            if (sl[i] && !sl[i + 1]) lms idx.push back(i + 1);
                                                                                           94
       }
51
52
        std::reverse(lms idx.begin(), lms idx.end());
                                                                                           95
        induced sort(vec, val range, SA, sl, lms idx);
                                                                                           96
53
        std::vector<int> new lms idx(lms idx.size()). lms vec(lms idx.size()):
54
55
        for (int i = 0, k = 0; i < n; ++i)
56
            if (!sl[SA[i]] && SA[i] >= 1 && sl[SA[i] - 1]) {
                                                                                          99
                                                                                          100 }
57
                new lms idx[k++] = SA[i];
            }
        int cur = 0:
        SA[n - 1] = cur:
60
        for (size t k = 1: k < new lms idx.size(): ++k) {</pre>
                                                                                         104
61
                                                                                          105
62
            int i = new lms idx[k - 1], j = new lms idx[k];
            if (vec[i] != vec[i]) {
                                                                                          106
63
                                                                                          107
                SA[i] = ++cur:
64
                                                                                          108
65
                continue;
66
            }
                                                                                         109
                                                                                         110
            bool flag = false;
            for (int a = i + 1, b = j + 1; ++a, ++b) {
                                                                                         111
                                                                                         112
                if (vec[a] != vec[b]) {
69
70
                    flag = true;
                                                                                         113
                    break:
                                                                                         114
71
                                                                                         115
72
                                                                                                  }
73
                if ((!sl[a] && sl[a - 1]) || (!sl[b] && sl[b - 1])) {
                                                                                         116
                    flag = !((!sl[a] \&\& sl[a - 1]) \&\& (!sl[b] \&\& sl[b - 1]));
                                                                                         117
74
                                                                                         118 }
75
                    break:
                                                                                         119
76
                }
77
            }
                                                                                         121
78
            SA[j] = (flag ? ++cur : cur);
                                                                                         122
79
       }
80
        for (size_t i = 0; i < lms_idx.size(); ++i) lms_vec[i] = SA[lms_idx[i]];</pre>
                                                                                         123
81
        if (cur + 1 < (int)lms_idx.size()) {</pre>
                                                                                         124
            auto lms SA = SA IS(lms vec, cur + 1);
                                                                                         125
82
            for (size t i = 0; i < lms_idx.size(); ++i) {</pre>
                                                                                         126
83
84
                new lms idx[i] = lms idx[lms SA[i]];
                                                                                         127
```

```
}
         induced sort(vec. val range. SA. sl. new lms idx):
         return SA:
     std::vector<int> suffix array(const std::string& s, const char first = 'a',
                              const char last = 'z') {
         std::vector<int> vec(s.size() + 1);
         std::copy(std::begin(s), std::end(s), std::begin(vec));
        for (auto& x : vec) x -= (int)first - 1;
        vec.back() = 0;
        auto ret = SA IS(vec. (int)last - (int)first + 2):
        ret.erase(ret.begin());
        return ret:
101 // Author: https://codeforces.com/blog/entry/12796?#comment-175287
|102\> // Uses kasai's algorithm linear in time and space
     std::vector<int> LCP(const std::string& s, const std::vector<int>& sa) {
        int n = s.size(), k = 0:
         std::vector<int> lcp(n), rank(n);
        for (int i = 0: i < n: i++) rank[sa[i]] = i:
         for (int i = 0; i < n; i++, k ? k-- : 0) {
            if (rank[i] == n - 1) {
                 k = 0:
                 continue;
            int j = sa[rank[i] + 1];
            while (i + k < n \&\& j + k < n \&\& s[i + k] == s[j + k]) k++;
            lcp[rank[i]] = k:
        lcp[n-1] = 0;
        return lcp;
120 template <typename T, class F = function<T(const T&, const T&)>>
     class SparseTable {
     public:
      int n:
      vector<vector<T>> mat:
      F func:
       SparseTable(const vector <T>& a, const F& f) : func(f) {
```

```
int max log = 32 - builtin clz(n);
129
         mat.resize(max_log);
130
131
         mat[0] = a;
         for (int j = 1; j < max_log; j++) {
132
           mat[j].resize(n - (1 << j) + 1);
133
          for (int i = 0; i \le n - (1 \le j); i++) {
134
             mat[j][i] = func(mat[j - 1][i], mat[j - 1][i + (1 << (j - 1))]);
135
136
          }
         }
137
      }
138
139
      T get(int from, int to) const {
140
141
         assert(0 <= from && from <= to && to <= n - 1);
         int lg = 32 - __builtin_clz(to - from + 1) - 1;
142
         return func(mat[lg][from], mat[lg][to - (1 << lg) + 1]);</pre>
143
144
      }
145 }:
```

n = static_cast<int>(a.size());

7.12 Z.cpp

128

```
template <typename T>
   vector<int> z function(int n, const T &s) {
      vector<int> z(n, n);
     int 1 = 0, r = 0;
      for (int i = 1; i < n; i++) {
       z[i] = (i > r ? 0 : min(r - i + 1, z[i - 1]));
       while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]]) {
         z[i]++;
       if (i + z[i] - 1 > r) {
10
        1 = i:
11
         r = i + z[i] - 1;
       }
13
14
15
      return z;
16 }
17
   template <typename T>
   vector<int> z function(const T &s) {
      return z_function((int) s.size(), s);
21 }
```

8 Basic

8.1 AST.py

```
class Solution:
2
            def calculate(self, s: str) -> int:
3
                     sign = ['+', '-', '*', '/', '(', ')']
4
                    v = []
5
                    n11m = ''
                     for c in s:
7
                             if c in sign:
8
                                      if num:
9
                                              v.append(num); num = ''
10
                                      if c == '-' and (not v or v[-1] == '('):
                                              v.append('0')
11
12
                                     v.append(c)
13
                             elif c.isnumeric():
                                      n_{11}m += c
14
15
                     if num: v.append(num)
16
17
                     stk0 = []
18
                     stk1 = []
19
                     for e in v:
20
                             if e.isnumeric():
21
                                      stk0.append(e)
22
                             elif e in ['+', '-']:
23
                                      while stk1 and stk1[-1] in ['*', '/', '+', '
24
                                              stk0.append(stk1.pop())
25
                                      stk1.append(e)
                             elif e in ['*', '/', '(']:
26
27
                                      stk1.append(e)
28
                             else:
29
                                      while stk1 and stk1[-1] != '(':
                                              stk0.append(stk1.pop())
31
                                      stk1.pop()
32
                     while stk1:
33
                             stk0.append(stk1.pop())
34
                    res = []
36
                     for e in stk0:
37
                             if e.isnumeric():
38
                                      res.append(int(e))
```

```
39
                            else:
40
                                     v = res.pop(); u = res.pop()
                                     if e == '+':
41
42
                                             res.append(u + v)
                                     if e == '-':
                                             res.append(u - v)
44
                                     if e == '*':
                                             res.append(u * v)
                                     if e == '/':
47
                                             res.append(u // v)
49
                    return res[0]
```

8.2 bitset.cpp

```
1 template <int len = 1>
2 void solve(int n) {
        if (n > len) {
            solve<std::min(len*2, MAXLEN)>(n);
            return;
       }
        // solution using bitset < len >
8 }
    struct Bitset {
11
        vector<ull> b;
12
        int n:
13
        Bitset(int x = 0) {
            n = x:
14
15
            b.resize((n + 63) / 64, 0);
       }
16
17
18
        int get(int x) {
            return (b[x >> 6] >> (x & 63)) & 1:
19
20
       }
21
22
        void set(int x, int y) {
            b[x >> 6] = 1ULL << (x & 63);
23
            if (!y) b[x >> 6] ^= 1ULL << (x & 63);
24
       }
25
26
27
        Bitset &operator&=(const Bitset &another) {
28
            rep(i, 0, min(SZ(b), SZ(another.b)) - 1) {
29
                b[i] &= another.b[i]:
```

```
30
            }
31
            return (*this);
32
       }
33
34
        Bitset operator&(const Bitset &another)const {
35
            return (Bitset(*this) &= another);
36
       }
37
38
        Bitset &operator | = (const Bitset &another) {
            rep(i, 0, min(SZ(b), SZ(another.b)) - 1) {
39
40
                b[i] |= another.b[i];
41
            }
42
            return (*this);
43
       }
44
45
        Bitset operator | (const Bitset & another) const {
46
            return (Bitset(*this) |= another);
47
       }
48
       Bitset &operator^=(const Bitset &another) {
49
50
            rep(i, 0, min(SZ(b), SZ(another.b)) - 1) {
51
                b[i] ^= another.b[i]:
52
            }
53
            return (*this);
54
       }
        Bitset operator^(const Bitset &another)const {
57
            return (Bitset(*this) ^= another);
58
       }
59
60
        Bitset &operator>>=(int x) {
61
            if (x & 63) {
62
                rep(i, 0, SZ(b) - 2) {
63
                    b[i] >>= (x \& 63);
64
                    b[i] ^= (b[i + 1] << (64 - (x & 63)));
                b.back() >>= (x & 63);
            }
67
            x >>= 6;
70
            rep(i, 0, SZ(b) - 1) {
71
                if (i + x < SZ(b)) b[i] = b[i + x];
72
                else b[i] = 0;
```

```
73
             }
 74
             return (*this);
         }
 75
 76
 77
         Bitset operator>>(int x)const {
             return (Bitset(*this) >>= x);
 78
         }
 79
 80
 81
         Bitset &operator <<=(int x) {</pre>
             if (x & 63) {
 82
 83
                 for (int i = SZ(b) - 1; i >= 1; i--) {
                     b[i] <<= (x \& 63);
                     b[i] = b[i - 1] >> (64 - (x & 63));
 85
                 }
                 b[0] <<= x & 63;
             }
 90
             x >>= 6:
             for (int i = SZ(b) - 1; i >= 0; i--) {
 91
                 if (i - x \ge 0) b[i] = b[i - x]:
 92
 93
                  else b[i] = 0;
 94
             return (*this);
 95
 96
         }
 97
 98
         Bitset operator<<(int x)const {</pre>
             return (Bitset(*this) <<= x);</pre>
         }
100
101 };
```

8.3 fastIO.cpp

```
1 static struct FastInput {
2   static constexpr int BUF_SIZE = 1 << 20;
3   char buf[BUF_SIZE];
4   size_t chars_read = 0;
5   size_t buf_pos = 0;
6   FILE *in = stdin;
7   char cur = 0;
8
9   inline char get_char() {
10    if (buf_pos >= chars_read) {
11       chars_read = fread(buf, 1, BUF_SIZE, in);
}
```

```
12
          buf_pos = 0;
13
          buf[0] = (chars read == 0 ? -1 : buf[0]);
14
15
        return cur = buf[buf_pos++];
16
17
18
      template <typename T>
19
      inline void tie(T) {}
20
21
     inline explicit operator bool() {
22
       return cur != -1;
23
     }
24
25
     inline static bool is blank(char c) {
26
       return c <= 'u';
27
28
     inline bool skip_blanks() {
        while (is_blank(cur) && cur != -1) {
31
          get_char();
32
33
       return cur != -1;
34
35
     inline FastInput& operator>>(char& c) {
       skip_blanks();
       c = cur;
       get_char();
40
       return *this;
41
     }
42
43
     inline FastInput& operator>>(string& s) {
       if (skip_blanks()) {
44
45
          s.clear();
46
          do {
47
            s += cur;
         } while (!is_blank(get_char()));
       }
49
50
       return *this;
51
52
      template <typename T>
54
      inline FastInput& read_integer(T& n) {
```

```
55
        // unsafe, doesn't check that characters are actually digits
        n = 0;
56
57
        if (skip_blanks()) {
58
          int sign = +1;
         if (cur == '-') {
59
            sign = -1;
60
            get char();
63
          do {
            n += n + (n << 3) + cur - '0':
64
65
         } while (!is_blank(get_char()));
66
         n *= sign;
67
68
        return *this;
69
     }
70
71
      template <typename T>
      inline typename enable_if<is_integral<T>::value, FastInput&>::type
          operator>>(T& n) {
       return read_integer(n);
73
     }
74
75
      #if !defined(_WIN32) || defined(_WIN64)
76
      inline FastInput& operator>>(__int128& n) {
77
78
        return read_integer(n);
79
     }
      #endif
80
81
82
      template <typename T>
83
      inline typename enable_if < is_floating_point < T >:: value, FastInput & >:: type
          operator>>(T& n) {
       // not sure if really fast, for compatibility only
84
        n = 0:
85
        if (skip_blanks()) {
87
         string s;
         (*this) >> s;
          sscanf(s.c_str(), "%lf", &n);
       }
90
91
        return *this;
92
   } fast_input;
95 #define cin fast_input
```

```
96
     static struct FastOutput {
       static constexpr int BUF_SIZE = 1 << 20;</pre>
 99
       char buf[BUF SIZE];
       size_t buf_pos = 0;
100
101
       static constexpr int TMP_SIZE = 1 << 20;</pre>
102
       char tmp[TMP SIZE];
103
       FILE *out = stdout:
104
105
       inline void put_char(char c) {
106
         buf[buf_pos++] = c;
107
         if (buf pos == BUF SIZE) {
           fwrite(buf, 1, buf_pos, out);
109
           buf pos = 0;
110
        }
111
      }
112
113
       ~FastOutput() {
114
         fwrite(buf, 1, buf_pos, out);
115
116
117
       inline FastOutput& operator<<(char c) {</pre>
118
         put char(c):
119
         return *this;
120
      }
121
122
       inline FastOutput& operator<<(const char* s) {</pre>
123
         while (*s) {
124
           put_char(*s++);
125
126
         return *this;
127
128
129
       inline FastOutput& operator<<(const string& s) {</pre>
130
         for (int i = 0; i < (int) s.size(); i++) {
131
           put_char(s[i]);
132
         }
133
         return *this;
134
135
136
       template <typename T>
137
       inline char* integer_to_string(T n) {
138
         // beware of TMP_SIZE
```

```
139
         char* p = tmp + TMP_SIZE - 1;
         if (n == 0) {
140
           *--p = '0':
141
142
         } else {
           bool is_negative = false;
143
           if (n < 0) {
144
145
             is negative = true;
146
           }
147
           while (n > 0) {
148
             *--p = (char) ('0' + n \% 10);
149
             n /= 10;
150
151
152
           if (is negative) {
             *--p = '-';
153
           }
154
         }
155
156
         return p;
157
158
159
       template <typename T>
       inline typename enable_if<is_integral<T>::value, char*>::type stringify(T
160
         return integer_to_string(n);
161
      }
162
163
       #if !defined(_WIN32) || defined(_WIN64)
164
       inline char* stringify(__int128 n) {
165
166
         return integer_to_string(n);
      }
167
       #endif
168
169
170
       template <typename T>
171
       inline typename enable_if < is_floating_point < T > :: value, char * > :: type
           stringify(T n) {
172
         sprintf(tmp, "%.17f", n);
         return tmp;
173
      }
174
175
       template <typename T>
176
       inline FastOutput& operator<<(const T& n) {</pre>
177
         auto p = stringify(n);
178
         for (; *p != 0; p++) {
179
```

8.4 FastMod.cpp

```
Description: Compute a % b about 5 times faster than usual, where b is
constant but not known at compile time. Returns a value congruent to a
(mod b) in the range [0, 2b).

typedef unsigned long long ull;
struct FastMod {
ull b, m;
FastMod(ull b) : b(b), m(-1ULL / b) {}
ull reduce(ull a) { // a % b + (0 or b)
return a - (ull)((__uint128_t(m) * a) >> 64) * b;
}

return a - (ull)((__uint128_t(m) * a) >> 64) * b;
```

8.5 intervalContainer.cpp

```
1 Description: Add and remove intervals from a set of disjoint intervals.
  Will merge the added interval with any overlapping intervals in the set when
   adding. Intervals are [inclusive, exclusive).
   Time: O (log N)
   set<pii>::iterator addInterval(set<pii>& is. int L. int R) {
       if (L == R) return is.end();
       auto it = is.lower_bound({L, R}), before = it;
        while (it != is.end() && it->first <= R) {
10
           R = max(R, it->second):
11
           before = it = is.erase(it);
12
       if (it != is.begin() && (--it)->second >= L) {
13
           L = min(L, it->first);
14
           R = max(R, it->second):
16
           is.erase(it);
17
18
       return is.insert(before, {L, R});
```

```
19  }
20  void removeInterval(set<pii>% is, int L, int R) {
21     if (L == R) return;
22     auto it = addInterval(is, L, R);
23     auto r2 = it->second;
24     if (it->first == L) is.erase(it);
25     else (int%)it->second = L;
26     if (R != r2) is.emplace(R, r2);
27  }
```

8.6 lineContainer.cpp

```
1 /**
    * Author: Simon Lindholm
    * Date: 2017-04-20
    * License: CCO
    * Source: own work
    * Description: Container where you can add lines of the form kx+m, and
         query maximum values at points x.
     * Useful for dynamic programming (``convex hull trick'').
     * Time: O(\log N)
    * Status: stress-tested
11 #pragma once
12
   struct Line {
14
        mutable ll k, m, p;
        bool operator<(const Line& o) const { return k < o.k; }</pre>
15
16
        bool operator<(ll x) const { return p < x; }</pre>
17 }:
18
    struct LineContainer : multiset<Line, less<>>> {
19
        // (for doubles, use inf = 1/.0, div(a,b) = a/b)
20
21
        static const ll inf = LLONG MAX;
22
        11 div(11 a, 11 b) { // floored division
            return a / b - ((a ^ b) < 0 && a % b); }
23
24
        bool isect(iterator x, iterator y) {
25
            if (v == end()) return x \rightarrow p = inf. 0:
26
            if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
            else x -> p = div(v -> m - x -> m, x -> k - v -> k):
27
28
            return x->p >= y->p;
29
        }
30
        void add(ll k. ll m) {
```

```
31
            auto z = insert(\{k, m, 0\}), y = z++, x = y;
32
            while (isect(v, z)) z = erase(z);
            if (x != begin() \&\& isect(--x, v)) isect(x, v = erase(v)):
34
            while ((y = x) != begin() && (--x)->p >= y->p)
35
                isect(x. erase(v)):
       }
36
37
       11 query(11 x) {
            assert(!empty());
39
            auto 1 = *lower bound(x);
40
            return 1.k * x + 1.m:
41
       }
42 };
```

8.7 mint.cpp

```
1 template<int MOD. int RT> struct mint {
        static const int mod = MOD;
3
       static constexpr mint rt() { return RT; } // primitive root for FFT
4
        int v; explicit operator int() const { return v; } // explicit -> don't
            silently convert to int
       mint():v(0) {}
5
6
        mint(11 v) \{ v = int((-MOD < v \&\& v < MOD) ? v : v \% MOD); \}
            if (v < 0) v += MOD: 
        bool operator == (const mint& o) const {
            return v == o.v; }
10
        friend bool operator!=(const mint& a, const mint& b) {
11
            return !(a == b); }
12
        friend bool operator < (const mint& a. const mint& b) {
13
            return a.v < b.v; }
14
15
        mint& operator+=(const mint& o) {
16
            if ((v += o.v) >= MOD) v -= MOD;
17
            return *this: }
18
        mint& operator -= (const mint& o) {
19
            if ((v -= o.v) < 0) v += MOD:
20
            return *this: }
21
        mint& operator*=(const mint& o) {
22
            v = int((11)v*o.v%MOD): return *this: }
23
        mint& operator/=(const mint& o) { return (*this) *= inv(o); }
24
        friend mint pow(mint a. 11 p) {
            mint ans = 1; assert(p >= 0);
26
            for (; p; p /= 2, a *= a) if (p&1) ans *= a;
27
            return ans: }
```

```
friend mint inv(const mint& a) { assert(a.v != 0);
28
29
            return pow(a,MOD-2); }
30
31
        mint operator-() const { return mint(-v); }
32
        mint& operator++() { return *this += 1; }
        mint& operator--() { return *this -= 1; }
33
        friend mint operator+(mint a, const mint& b) { return a += b; }
34
        friend mint operator-(mint a, const mint& b) { return a -= b; }
35
        friend mint operator*(mint a, const mint& b) { return a *= b; }
36
        friend mint operator/(mint a, const mint& b) { return a /= b; }
37
38 };
39
    const int MOD=998244353:
    using mi = mint < MOD, 5>; // 5 is primitive root for both common mods
41
42
    namespace simp {
43
        vector<mi> fac,ifac,invn;
44
45
        void check(int x) {
46
            if (fac.empty()) {
                fac={mi(1).mi(1)}:
47
                ifac={mi(1),mi(1)};
                invn={mi(0).mi(1)}:
            }
50
51
            while (SZ(fac)<=x) {
52
                int n=SZ(fac).m=SZ(fac)*2:
53
                fac.resize(m);
                ifac.resize(m):
54
                invn.resize(m);
55
56
                for (int i=n;i<m;i++) {</pre>
                    fac[i]=fac[i-1]*mi(i):
57
                    invn[i]=mi(MOD-MOD/i)*invn[MOD%i];
58
59
                    ifac[i]=ifac[i-1]*invn[i];
60
                }
61
            }
62
        7
63
        mi gfac(int x) {
            check(x); return fac[x];
64
        }
65
66
        mi ginv(int x) {
            check(x); return invn[x];
67
        }
68
        mi gifac(int x) {
69
70
            check(x); return ifac[x];
```

```
71 }
72 mi binom(int n,int m) {
73 if (m < 0 || m > n) return mi(0);
74 return gfac(n)*gifac(m)*gifac(n - m);
75 }
76 }
```

8.8 pbds.cpp

```
1 #include <bits/extc++.h>
2 using namespace __gnu_cxx;
3 using namespace __gnu_pbds;
   #include<ext/pb ds/assoc container.hpp>
   #include<ext/pb_ds/tree_policy.hpp>
7 #include < ext/pb_ds/hash_policy.hpp>
   #include<ext/pb_ds/trie_policy.hpp>
   #include<ext/pb_ds/priority_queue.hpp>
10
11 pairing_heap_tag: 配对堆
12 thin_heap_tag: 斐波那契堆
13 binomial heap tag: 二项堆
14 binary_heap_tag: 二叉堆
15
   __gnu_pbds::priority_queue<PII, greater<PII>, pairing_heap_tag> q;
   __gnu_pbds::priority_queue<PII, greater<PII>, pairing_heap_tag>::
       point iterator its[N];
19 its[v] = q.push({dis[v], v});
   q.modify(its[v], {dis[v], v});
21
   可以将两个优先队列中的元素合并 (无任何约束)
   使用方法为a.join(b)
24 此时优先队列b内所有元素就被合并进优先队列a中,且优先队列b被清空
25
26 cc_hash_table<string, int> mp1拉链法
27 gp_hash_table < string, int > mp2 查探法
```

8.9 simu.cpp

```
1 db rnd(db 1, db r) {
2    static uniform_real_distribution<db> u(0, 1);
3    static default_random_engine e(rng());
```

```
return 1 + (r - 1) * u(e); // u(rnq);
7 db eval(pair < db, db > x) { ... }
   void simulate_anneal() {
     pair < db, db > cur(rnd(0, 10000), rnd(0, 10000));
      for (double k = 10000: k > 1e-5: k *= 0.99) {
11
12
       // [start, end, step]
       pair<db, db> nxt(cur.fi + rnd(-k, k), cur.se + rnd(-k, k));
13
       db delta = eval(nxt) - eval(cur);
14
       if (exp(-delta / k) > rnd(0, 1)) {
16
       cur = nxt:
17
       }
18
19 }
21 /**
    * https://codeforces.com/gym/104813/submission/234982955
    * The 9th CCPC (Harbin) 2023
    * Author: QwertyPi
26 LD Prob() {
    static uniform_real_distribution<> dist(0.0, 1.0);
28
    return dist(rng):
30 LD Sigma(LD x) { return 1 / (1 + exp(-x)); }
31
32 LD overall max score = 0;
   for (int main_loop = 0; main_loop < 5; main_loop++) {</pre>
     vector < LD > e(n, (LD)1 / n);
35
     for (int tr = 0; tr < 1000; tr++) {
       vector<LD> ne(n):
36
37
       for (int i = 0; i < n; i++) {
38
        ne[i] = Prob();
39
       LD s = accumulate(all(ne), 0.0L);
       for (int i = 0; i < n; i++) {
41
         ne[i] /= s;
       if (eval(ne) > eval(e)) e = ne;
45
     LD t = (LD)0.0002;
```

```
LD max_score = 0;
     const LD depr = 0.999995;
     const int tries = 2E6:
     const int loop = 1E5;
51
     LD score_old = eval(e);
    for (int tr = 0; tr < tries; tr++) {
54 #ifdef LOCAL
       if (tr % loop == loop - 1) {
         cout << fixed << setprecision(10) << "current_score_=="" << max_score
              << ",,,t,,=,," << t << '\n';
       }
59 #endif
       int x = rng() \% n, v = rng() \% n;
61
     if (e[x] < t \mid | x == v) {
        t *= depr;
         continue;
       }
       e[x] = t;
       e[y] += t;
       LD score new = eval(e);
       if (score new > score old) { // ok
       } else { // revert
70
71
        e[x] += t:
         e[v] -= t;
    score old = score new;
       max_score = max(max_score, score_new);
76
    t *= depr:
77
     overall_max_score = max(overall_max_score, max_score);
79 #ifdef LOCAL
     cout << "Loopu#" << main_loop << ":" << max_score << '\n';
81 #endif
82 }
```

8.10 sort.cpp

```
void merge_sort(int q[], int 1, int r) {
    if (1 >= r) return;
    int mid = 1 + r >> 1;
    merge_sort(q, 1, mid);
}
```

```
merge_sort(q, mid + 1, r);
        int k = 0, i = 1, j = mid + 1;
        while (i <= mid && j <= r)
            if (q[i] <= q[j])</pre>
9
                tmp[k++] = q[i++];
10
11
                tmp[k++] = q[j++];
12
13
14
        while (i <= mid)
            tmp[k++] = q[i++];
15
        while (j <= r)
16
            tmp[k++] = q[j++];
17
18
19
       for (i = 1, j = 0; i \le r; i++, j++) q[i] = tmp[j];
20 }
21
22 void quick_sort(int q[], int 1, int r) {
        if (1 >= r) return;
23
       int i = 1 - 1, j = r + 1, x = q[1 + r >> 1];
24
        while (i < j) {
25
           do i ++; while (q[i] < x);
26
            do j --; while (q[j] > x);
27
28
           if (i < j) swap(q[i], q[j]);</pre>
29
        quick_sort(q, 1, j), quick_sort(q, j + 1, r);
30
31 }
32
33 template < class T>
34 void radixsort(T *a. 11 n) {
       int base = 0;
35
36
       rep(i, 1, n) sa[i] = i;
       rep(k, 1, 5) {
37
38
            rep(i, 0, 255) c[i] = 0;
39
            rep(i, 1, n) c[(a[i] >> base) & 255]++;
40
            rep(i, 1, 255) c[i] += c[i - 1];
            per(i, n, 1) {
41
                rk[sa[i]] = c[(a[sa[i]] >> base) & 255]--;
            rep(i, 1, n) sa[rk[i]] = i;
44
            base += 7;
45
       }
46
47 }
```

8.11 高精度.cpp

```
1 vector<int> add(vector<int> &A, vector<int> &B) {
       if (A.size() < B.size()) return add(B, A);</pre>
       vector<int> C;
       int t = 0;
       for (int i = 0; i < A.size(); i ++ ) {
6
           t += A[i];
7
         if (i < B.size()) t += B[i];</pre>
           C.push_back(t % 10);
          t /= 10;
10
       }
11
       if (t) C.push_back(t);
12
       return C:
13 }
14
15 vector<int> sub(vector<int> &A. vector<int> &B) {
16
       vector<int> C;
       for (int i = 0, t = 0; i < A.size(); i ++ ) {
17
18
           t = A[i] - t;
19
           if (i < B.size()) t -= B[i];</pre>
           C.push_back((t + 10) % 10);
21
           if (t < 0) t = 1;
           else t = 0:
22
23
       while (C.size() > 1 && C.back() == 0) C.pop back();
25
       return C:
26 }
27
28 vector<int> mul(vector<int> &A, int b) {
       vector<int> C:
      int t = 0:
31
       for (int i = 0; i < A.size() || t; i ++ ) {
32
           if (i < A.size()) t += A[i] * b;
33
           C.push_back(t % 10);
           t /= 10:
       while (C.size() > 1 && C.back() == 0) C.pop_back();
       return C:
37
38 }
40 vector<int> div(vector<int> &A, int b, int &r) {
41
       vector<int> C;
42
       r = 0:
```