Team Reference Document

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1 Template

1.1 .clang-format

```
1 BasedOnStyle: Google
2 IndentWidth: 4
3 ColumnLimit: 160
```

1.2 debug.cpp

```
#include <bits/stdc++.h>

using namespace std;

template <class T, size_t size = tuple_size<T>::value>
string to_debug(T, string s = "") requires(not ranges::range<T>);

template <class T>
concept check = requires(T x, ostream &os) {
    os << x;
};

template <check T>
```

```
14 string to_debug(T x) {
      return static_cast<ostringstream>(ostringstream() << x).str();</pre>
16 }
17
18 string to_debug(ranges::range auto x, string s = "") requires(not is_same_v<
        decltype(x), string>) {
     for (auto xi : x) {
        s += ", " + to_debug(xi);
21
     return "[__" + s.substr(s.empty() ? 0 : 2) + "__]";
23 }
24
25 template <class T, size_t size>
   string to_debug(T x, string s) requires(not ranges::range<T>) {
      [&] < size_t... I > (index_sequence < I... >) {
       ((s += ", " + to_debug(get < I > (x))), ...);
     }(make index sequence<size>());
      return "{" + s.substr(s.empty() ? 0 : 2) + "}";
31 }
32
   #define debug(...) [](auto... $){ ((cout << to_debug($) << "_{\sqcup}"), ...); cout
        << endl; }("[", #__VA_ARGS__, "]:", __VA_ARGS__)
```

1.3 gen.py

```
from random import *
  n = 10000

s = 'qwertyuiopasdfghjklzxcvbnm'

for i in range(n):
  print(choice(s), end = '')

print()

print()

print(randint(0, 1), randint(1, n))
```

1.4 head.cpp

```
#pragma GCC optimize("Ofast", "inline", "unroll-loops")
#include <bits/stdc++.h>
using namespace std;
#define rep(i, a, n) for (int i = a; i <= n; i++)
#define per(i, a, n) for (int i = a; i >= n; i--)
#define pb push_back
#define eb emplace_back
#define all(x) (x).begin(), (x).end()
```

```
#define fi first
11 #define se second
12 #define SZ(x) ((int)(x).size())
   using VI = vector<int>;
14 using PII = pair<int, int>;
15 using 11 = long long;
16 using ull = unsigned long long;
17 using db = double;
18 using ldb = long double;
   mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
21
   #ifdef DEBUG
   #include "debug.cpp"
   #else
   #define debug(...) 42
   #endif
27
28 void solve() {}
   int main() {
       cin.tie(nullptr)->sync_with_stdio(false);
30
       cout << fixed << setprecision(16);</pre>
31
32
       int tt = 1;
33
       cin >> tt:
34
       while (tt--) {
            solve();
       }
37 }
```

1.5 head-apiadu.cpp

#define bit(x) (111 << (x))

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 #define rep(i,a,n) for (int i=a;i<n;i++)
4 #define per(i,a,n) for (int i=n-1;i>=a;i--)
5 #define pb push_back
6 #define eb emplace_back
7 #define mp make_pair
8 #define all(x) (x).begin(),(x).end()
9 #define fi first
10 #define se second
11 #define SZ(x) ((int)(x).size())
```

```
12 typedef vector<int> VI;
13 typedef basic_string<int> BI;
14 typedef long long ll;
15 typedef pair<int,int> PII;
16 typedef double db;
17 mt19937 mrand(random_device{}());
18 const ll mod=10000000007;
19 int rnd(int x) { return mrand() % x;}
20 ll powmod(ll a,ll b) {ll res=1;a%=mod; assert(b>=0); for(;b;b>>=1){if(b&1) res=res*a%mod;a=a*a%mod;}return res;}
21 ll gcd(ll a,ll b) { return b?gcd(b,a%b):a;}
22 // head
```

1.6 Makefile

```
1 %: %.cpp
2 g++-13 $< -o $@ -std=gnu++20 -g -02 -Wall -Wextra -DDEBUG -
D_GLIBCXX_DEBUG -D_GLIBCXX_DEBUG_PEDANTIC
```

1.7 pai.py

```
1 import os
2 \text{ tt = 0}
3 while True:
        os.system('python_gen.py_>_A.in')
        os.system('./a,<,A.in,>,a.out')
        os.system('./b_{\parallel} < A.in_{\parallel} > b.out')
        # diff for linux or macos, fc for windows
        if os.system('diffua.outub.out'):
             print("WA")
10
             exit(0)
11
        else:
12
             tt += 1
13
             print("AC:", tt)
```

1.8 settings.json

```
1 {
2     "editor.formatOnSave": true,
3     "files.autoSave": "afterDelay",
4     "files.autoSaveDelay": 350,
5     "C_Cpp.default.cppStandard": "gnu++20"
6 }
```

2 Data

2.1 01trie.cpp

```
1 struct node {
       int son[2]:
       int end;
       int sz;
   } seg[maxn << 2];</pre>
    int root, tot;
7 int n, m;
   void insert(ll x) {
10
       int cnt = root;
11
       for (int i = 62; i >= 0; i--) {
            int w = (x >> i) & 1;
12
            if (seg[cnt].son[w] == 0) seg[cnt].son[w] = ++tot;
13
            cnt = seg[cnt].son[w];
14
            seg[cnt].sz++;
15
16
       }
17
        seg[cnt].end++;
18 }
19
   ll query(ll x, ll k) {
       ll res = 0:
21
22
       int cnt = root;
       for (int i = 62; i >= 0; i--) {
23
24
            int w = (x >> i) & 1;
            if (seg[seg[cnt].son[w]].sz >= k) cnt = seg[cnt].son[w];
25
26
            else {
                k -= seg[seg[cnt].son[w]].sz;
27
                cnt = seg[cnt].son[abs(w - 1)];
28
29
                res += bit(i);
           }
30
       }
31
       return res;
33 }
```

2.2 2dtree(bqi343).cpp

```
1 const int SZ = 1.1e5;
2 template <class T>
3 struct node {
```

```
T val = 0;
        node<T>* c[2];
6
        node() { c[0] = c[1] = NULL; }
7
        void upd(int ind, T v, int L = 0, int R = SZ - 1) { // add v
8
            if (L == ind && R == ind) {
9
                 val += v:
10
                 return;
11
            }
12
            int M = (L + R) / 2;
            if (ind <= M) {
13
14
                 if (!c[0]) c[0] = new node();
15
                 c[0]->upd(ind, v, L, M);
            } else {
16
17
                 if (!c[1]) c[1] = new node();
18
                 c[1] \rightarrow upd(ind, v, M + 1, R);
            }
19
20
            val = 0;
21
            rep(i, 0, 1) if (c[i]) val += c[i] -> val;
22
23
        T query(int lo, int hi, int L = 0, int R = SZ - 1) { // query sum of
             segment
24
            if (hi < L || R < lo) return 0:
25
            if (lo <= L && R <= hi) return val;
26
            int M = (L + R) / 2;
            T res = 0;
27
28
            if (c[0]) res += c[0]->query(lo, hi, L, M);
29
            if (c[1]) res += c[1]->query(lo, hi, M + 1, R);
30
            return res;
31
        }
32
        void UPD(int ind, node* c0, node* c1, int L = 0, int R = SZ - 1) { //
             for 2D seatree
33
            if (L != R) {
34
                 int M = (L + R) / 2;
                 if (ind <= M) {
36
                     if (!c[0]) c[0] = new node();
37
                     c[0] \rightarrow UPD(ind, c0 ? c0 \rightarrow c[0] : NULL, c1 ? c1 \rightarrow c[0] : NULL, L
                          , M);
                 } else {
39
                     if (!c[1]) c[1] = new node();
40
                     c[1] \rightarrow UPD(ind, c0 ? c0 \rightarrow c[1] : NULL, c1 ? c1 \rightarrow c[1] : NULL, M
                           + 1, R);
41
                 }
42
            }
```

```
val = (c0 ? c0 -> val : 0) + (c1 ? c1 -> val : 0):
       }
44
45 }:
46
47
    * Description: BIT of SeqTrees. x\in (0,SZ), y\in [0,SZ).
    * Memory: O(N\log^2 N)
    * Source: USACO Mowing the Field
    * Verification:
    * USACO Mowing the Field
    * http://www.usaco.org/index.php?page=viewproblem2&cpid=722 (13/15, 15/15
         and 1857ms with BumpAllocator)
    */
54
55
   #include "../1D_{\sqcup}Range_{\sqcup}Queries_{\sqcup}(9.2)/SparseSeg_{\sqcup}(9.2).h"
57
    template <class T>
    struct BITseg {
        node<T> seg[SZ];
60
        BITseg() { fill(seg, seg + SZ, node<T>()); }
61
62
        void upd(int x, int y, int v) { // add v
            for (; x < SZ; x += x & -x) seg[x].upd(y, v);
63
       }
64
65
       T query(int x, int yl, int yr) {
66
            T res = 0:
            for (; x; x \rightarrow x \& x) res += seg[x].query(yl, yr);
69
       }
70
       T query(int xl, int xr, int yl, int yr) { // query sum of rectangle
71
            return query(xr, yl, yr) - query(xl - 1, yl, yr);
72
       }
73 }:
74
75
    * Description: SeqTree of SeqTrees. x,y \in [0,SZ).
76
    * Memory: O(N\log^2 N)
    * Source: USACO Mowing the Field
   * Verification:
    * http://www.usaco.org/index.php?page=viewproblem2&cpid=722 (9/15 w/
         BumpAllocator)
    * http://www.usaco.org/index.php?page=viewproblem2&cpid=601 (4238 ms, 2907
         ms w/ BumpAllocator)
82
```

```
83
    #include "../1D,Range,Queries,(9.2)/SparseSeg,(9.2).h"
    template <class T>
     struct Node {
         node<T> seg;
         Node* c[2];
         Node() \{ c[0] = c[1] = NULL: \}
 91
         void upd(int x, int y, T v, int L = 0, int R = SZ - 1) { // add v
 92
             if (L == x && R == x) {
 93
                 seg.upd(y, v);
 94
                 return;
             }
 95
 96
             int M = (L + R) / 2;
 97
             if (x <= M) {
                 if (!c[0]) c[0] = new Node();
 99
                 c[0] \rightarrow upd(x, v, v, L, M);
             } else {
100
                 if (!c[1]) c[1] = new Node();
101
102
                 c[1] - \sup (x, y, v, M + 1, R);
103
104
             seg.upd(y, v); // only for addition
105
             // sea.UPD(u.c[0]?&c[0]->sea:NULL.c[1]?&c[1]->sea:NULL):
106
         }
107
         T query(int x1, int x2, int y1, int y2, int L = 0, int R = SZ - 1) { //
               query sum of rectangle
108
             if (x1 <= L && R <= x2) return seg.query(y1, y2);
             if (x2 < L \mid | R < x1) return 0:
110
             int M = (L + R) / 2;
111
             T res = 0:
112
             if (c[0]) res += c[0]->query(x1, x2, y1, y2, L, M);
113
             if (c[1]) res += c[1]->query(x1, x2, y1, y2, M + 1, R);
114
             return res:
115
         }
116 };
```

2.3 cdq.cpp

```
int ans[maxn], lev[maxn];
array<int, 5> v[maxn], tmp[maxn];

struct BIT {

...
```

```
6 } c:
   void solve(int 1. int r) {
9
        if (1 >= r) return;
        int mid = (1 + r) / 2:
10
        solve(1, mid), solve(mid + 1, r);
11
        int i = 1, j = mid + 1;
12
        int piv = 1;
13
        while (i <= mid || j <= r) {
14
            if (i <= mid && (j > r || mp(v[i][1], v[i][2]) <= mp(v[j][1], v[j
15
                ][2]))) {
                c.modify(v[i][2], v[i][3]);
16
                tmp[piv++] = v[i++];
17
18
            } else {
                v[j][4] += c.query(v[j][2]);
19
                tmp[piv++] = v[j++];
20
            }
21
        }
22
        rep(i, 1, mid) c.modify(v[i][2], -v[i][3]);
23
        rep(i, 1, r) v[i] = tmp[i];
24
25 }
   void solve() {
27
        cin >> n >> k;
28
29
        c.resize(k):
        rep(i, 1, n) {
30
            int s, c, m;
            cin >> s >> c >> m;
32
33
            v[i] = {s, c, m, 1, 0};
        }
34
        v[0][0] = -1;
35
36
        sort(v + 1, v + n + 1);
        int cnt = 0;
37
38
        rep(i, 1, n) {
39
            if (v[i][0] == v[cnt][0] \&\& v[i][1] == v[cnt][1] \&\& v[i][2] == v[cnt]
                ][2]) v[cnt][3]++;
            else v[++cnt] = v[i];
40
        }
41
        solve(1, cnt);
42
        rep(i, 1, cnt) {
43
            ans[v[i][4] + v[i][3] - 1] += v[i][3];
44
45
        }
        rep(i, 0, n - 1) cout << ans[i] << '\n';
```

47 }

2.4 compact.cpp

```
1 namespace compact {
2 const int LOGN=18;
3 int 1[N],r[N],tot,p[N][20],n;
4 map<int,int> cv;
5 int lca(int u,int v) {
       if (dep[u]>dep[v]) swap(u,v);
7
       per(i,LOGN-1,0) if (dep[p[v][i]]>=dep[u]) v=p[v][i];
       if (u==v) return u;
       per(i,LOGN-1,0) if (p[v][i]!=p[u][i]) u=p[u][i],v=p[v][i];
10
       return p[u][0];
11 }
12 void dfs(int u,int f) {
       l[u]=++tot; dep[u]=dep[f]+1; p[u][0]=f;
       vec[dep[u]].pb(u);
14
15
       for (auto v:vE[u]) {
16
           if (v==f) continue;
17
           dfs(v.u):
18
       }
       r[u]=tot:
19
20 }
21 void build(int n) {
       n=_n; tot=0;
       dfs(1,0);
24
       rep(j,1,LOGN-1) rep(i,1,n) p[i][j]=p[p[i][j-1]][j-1];
25 }
26
27 bool cmp(int u,int v) { return l[u]<l[v]; }
   vector<PII> compact(VI v) {
29
       int m=SZ(v):
30
       vector<PII> E;
31
       sort(all(v),cmp);
32
       rep(i,0,m-2) {
           int w=lca(v[i],v[i+1]);
34
           v.pb(w);
35
       }
       v.pb(0);
37
       v.pb(1);
38
       sort(all(v),cmp);
39
       v.erase(unique(all(v)), v.end());
```

```
cv.clear();
40
        per(i,SZ(v)-1,1) {
41
            int u=v[i]:
43
            while (1) {
                auto it=cv.lower_bound(1[u]);
44
                if (it==cv.end()||it->fi>r[u]) break;
45
                E.pb(mp(u,v[it->se]));
                cv.erase(it);
47
            }
            cv[l[u]]=i;
49
50
        }
51
        return E;
53 };
```

2.5 dominator.cpp

```
void solve(int u. int S) {
      int best = -1, cnt = S + 1;
      auto find best = [&](auto &find best, int u, int par) -> void {
        sz[u] = 1, sdom[u] = 0;
       for (auto v : e[u]) {
         if (v == par || del[v]) continue;
         find best(find best, v, u);
         sz[u] += sz[v];
         sdom[u] = max(sdom[u], sz[v]);
10
11
       sdom[u] = max(sdom[u], S - sz[u]);
       if (sdom[u] < cnt) {</pre>
12
          cnt = sdom[u]. best = u:
13
14
       }
     };
15
     find_best(find_best, u, 0);
16
17
      int id1 = tot++, dep1 = 0;
      int id2, dep2;
18
19
      auto dfs = [&](auto &dfs, int u, int par, int dep) -> void {
20
       dep1 = max(dep1, dep);
21
       dep2 = max(dep2, dep);
       Q[u].pb({id1, 1, dep});
22
23
       Q[u].pb({id2, -1, dep});
       for (auto v : e[u]) {
24
25
         if (v == par || del[v]) continue;
26
          dfs(dfs, v, u, dep + 1);
```

```
27
       }
     };
     Q[best].pb({id1, 1, 0});
     for (auto v : e[best]) {
31
       if (del[v]) continue:
       id2 = tot++, dep2 = 0;
32
       dfs(dfs, v, best, 1);
       fenw[id2] = BIT<11>(dep2 + 1);
35
     fenw[id1] = BIT<11>(dep1 + 1);
     del[best] = 1;
     for (auto v : e[best]) {
       if (!del[v]) solve(v, sz[v]);
40
    }
41 }
```

2.6 dsu.cpp

```
1 class dsu {
    public:
     vector<int> fa;
     vector<ll> dist;
5
     int n:
6
     dsu(int n) : n( n) {
       fa.resize(n):
       dist.assign(n, 0);
10
       iota(fa.begin(), fa.end(), 0);
11
12
     int find(int x) {
14
       if (fa[x] == x) return x;
       int par = fa[x];
15
       fa[x] = find(fa[x]);
16
17
       dist[x] += dist[par]:
       return fa[x];
18
19
     }
20
21
      void unite(int x, int y, ll v) {
22
       int px = find(x);
23
       int py = find(y);
24
       fa[py] = px;
25
        dist[py] = dist[x] - dist[y] - v;
```

```
26 }
27 };
```

2.7 dsu-on-tree.cpp

```
1 void dfs(int x, int fa) {
       hs[x] = -1, w[x] = 1:
       l[x] = ++tot;
       id[tot] = x:
       for (auto y : g[x]) if (y != fa) {
                dfs(y, x);
               w[x] += w[y];
                if (hs[x] == -1 \mid | w[y] > w[hs[x]])
                   hs[x] = y;
           }
11
       r[x] = tot;
13
   void dsu(int x, int fa, int keep) {
       for (auto y : g[x]) {
15
16
           if (y != hs[x] && y != fa) {
                dsu(y, x, 0);
18
           }
19
       if (hs[x] != -1) dsu(hs[x], x, 1);
21
22
       for (auto y : g[x]) {
           if (y != hs[x] && y != fa) {
23
               for (int i = l[v]; i <= r[v]; i++) {
               }
27
           }
28
       // add current node
30
31
       ans[x] = cnt;
32
       if (!keep) {
34
           // clear
```

2.8 fenwick.cpp

```
1 template <typename T>
2 struct BIT {
     vector<T> fenw;
     int n, pw;
     BIT(int n = 0) : n(n) {
     fenw.assign(n + 1, 0);
       pw = bit_floor(unsigned(n));
10
11
   void Modify(int x, T v) {
    if (x \le 0) return; // assert (0 \le x \& x \le n);
    while (x \le n) \{ // x < n \}
       fenw[x] += v;
         x += (x \& -x); // x /= x + 1;
16
       }
17
    }
    T Query(int x) {
    // assert(0 <= x && x <= n);
21
    T v{};
    while (x > 0) {
         v += fenw[x]; // fenw[x - 1];
         x = (x \& -x); // x \& = x - 1;
25
26
       return v;
27
28
     // Returns the length of the longest prefix with sum <= c
     int MaxPrefix(T c) {
31
     T v{};
      int at = 0:
       for (int i = 20; i >= 0; i--) {
         if (at + bit(i) <= n && v + fenw[at + bit(i)] <= c) {</pre>
           v += fenw[at + bit(i)];
           at += bit(i);
         }
       }
       /**
        * for (int len = pw; len > 0; len >>= 1) {
41
         * if (at + len <= n) {
42
              auto nv = v:
```

```
43  * nv += fenw[at + len - 1];

44  * if (!(c < nv)) {

45  * v = nv;

46  * at += len;

47  * }

48  * }

49  * }

50  * assert(0 <= at && at <= n);

51  */

52  return at;

53 }

54 };
```

2.9 fenwick2d.cpp

```
1 template <typename T>
   class fenwick2d {
    public:
     vector<vector<T>> fenw;
     int n, m;
     fenwick2d(int n, int m) : n(n), m(m) {
       fenw.resize(n);
       for (int i = 0; i < n; i++) {
         fenw[i].resize(m);
       }
11
12
     }
13
     inline void modify(int i, int j, T v) {
14
       int x = i:
15
16
       while (x < n) {
17
        int y = j;
         while (y < m) {
18
19
           fenw[x][y] += v;
           y = (y + 1);
20
21
         x = (x + 1);
23
24
     }
25
26
     inline T get(int i, int j) {
27
       T v{};
28
       int x = i:
```

```
29
        while (x \ge 0) {
         int y = j;
31
         while (y \ge 0) {
32
           v += fenw[x][v];
           y = (y & (y + 1)) - 1;
34
          x = (x & (x + 1)) - 1;
37
       return v;
39 };
40
41 struct node {
     int a = ...; // don't forget to set default value
43
44
     inline void operator+=(node &other) { ... }
45 };
```

2.10 hash-table.cpp

```
1 struct Hash table {
        static const int V = 1000003;
       int fst[V], nxt[V];
       int ctm, ptm[V], T;
       int val[V];
       ll key[V];
       void init() \{T = 0, ctm++;\}
       void insert(ll k, int v) {
9
           int s = k \% V;
10
            if (ptm[s] != ctm) ptm[s] = ctm, fst[s] = -1;
            for (int i = fst[s]; i != -1; i = nxt[i]) if (key[i] == k) {
11
12
                    return;
13
            nxt[T] = fst[s], fst[s] = T, key[T] = k, val[T] = v;
14
15
           T++:
16
       }
17
       int query(ll k) {
18
            int s = k \% V:
19
            if (ptm[s] != ctm) return -1;
            for (int i = fst[s]: i != -1: i = nxt[i]) {
21
                if (key[i] == k) return val[i];
22
           }
23
            return -1:
```

```
24 }
25 };
```

2.11 HLD.cpp

```
struct HLD {
        int n;
        std::vector<int> siz, top, dep, parent, in, out, seq;
        std::vector<std::vector<int>> adj;
        int cur;
        HLD() {}
        HLD(int n) {
            init(n);
10
       }
11
        void init(int n) {
12
            this -> n = n;
            siz.resize(n);
13
14
            top.resize(n);
            dep.resize(n);
15
            parent.resize(n);
16
17
            in.resize(n);
            out.resize(n):
18
19
            seq.resize(n);
            cur = 0;
20
21
            adj.assign(n, {});
22
       }
23
        void addEdge(int u, int v) {
            adj[u].push_back(v);
24
            adj[v].push_back(u);
25
       }
26
        void work(int root = 0) {
27
            top[root] = root;
28
            dep[root] = 0;
29
            parent[root] = -1;
            dfs1(root);
31
            dfs2(root);
32
       }
33
        void dfs1(int u) {
34
            if (parent[u] != -1) {
35
                adj[u].erase(std::find(adj[u].begin(), adj[u].end(), parent[u]))
36
37
            }
```

```
38
39
            siz[u] = 1;
            for (auto &v : adj[u]) {
40
41
                 parent[v] = u;
42
                 dep[v] = dep[u] + 1;
                dfs1(v);
43
44
                 siz[u] += siz[v];
                 if (siz[v] > siz[adj[u][0]]) {
                     std::swap(v, adj[u][0]);
46
47
                }
48
            }
49
        }
        void dfs2(int u) {
50
51
            in[u] = cur++;
52
            seq[in[u]] = u;
53
            for (auto v : adj[u]) {
54
                 top[v] = v == adi[u][0] ? top[u] : v;
                 dfs2(v):
56
            }
            out[u] = cur;
57
58
        }
        int lca(int u. int v) {
            while (top[u] != top[v]) {
61
                 if (dep[top[u]] > dep[top[v]]) {
62
                     u = parent[top[u]];
63
                } else {
                     v = parent[top[v]];
66
67
            return dep[u] < dep[v] ? u : v;</pre>
68
        }
69
70
        int dist(int u, int v) {
71
            return dep[u] + dep[v] - 2 * dep[lca(u, v)];
72
        }
73
74
        int jump(int u, int k) {
75
            if (dep[u] < k) {</pre>
76
                 return -1;
77
            }
78
79
            int d = dep[u] - k;
80
```

```
while (dep[top[u]] > d) {
 81
                 u = parent[top[u]];
 83
             }
 84
             return seq[in[u] - dep[u] + d];
 85
         }
 86
 87
         bool isAncester(int u. int v) {
 88
             return in[u] <= in[v] && in[v] < out[u];
 89
         }
 90
 91
 92
         int rootedParent(int u, int v) {
             std::swap(u, v);
 93
 94
             if (u == v) {
 95
                 return u;
             if (!isAncester(u, v)) {
                 return parent[u];
 98
 99
             }
             auto it = std::upper_bound(adj[u].begin(), adj[u].end(), v, [&](int
100
                 x, int y) {
                 return in[x] < in[y];</pre>
101
102
             }) - 1:
103
             return *it;
104
         }
105
         int rootedSize(int u, int v) {
106
             if (u == v) {
107
108
                 return n;
109
             if (!isAncester(v, u)) {
110
111
                 return siz[v];
             }
112
113
             return n - siz[rootedParent(u, v)];
         }
114
115
         int rootedLca(int a, int b, int c) {
116
             return lca(a, b) ^ lca(b, c) ^ lca(c, a);
117
118
         }
119 };
```

2.12 kdtree.cpp

```
1 namespace kd {
2 const int K = 2, N = 2.1e5;
3 template <typename T>
4 using P = array<T, K>;
    template <typename T>
    struct node {
      P<T> pt, mx, mn;
      ll val, sum;
      node *1, *r, *p;
      int id;
11
      node(const P < T > \&_pt = P < T > (), ll _val = 0, int _id = 0)
           : pt(_pt), val(_val), sum(_val), id(_id) {
13
         mx = mn = pt;
14
         p = 1 = r = nullptr;
15
16 }:
17 node<11> *ptr[N];
    template <typename T>
    void pull(node<T> *u) {
      if (not u) return;
21
      u \rightarrow sum = u \rightarrow val:
      rep(i, 0, K - 1) u \rightarrow mx[i] = u \rightarrow mn[i] = u \rightarrow pt[i];
23
     if (u->1) {
24
      u->sum += u->1->sum;
        u - > 1 - > p = u;
26
27
      if (u->r) {
        u->sum += u->r->sum:
29
        u \rightarrow r \rightarrow p = u;
30
     }
31
      rep(i, 0, K - 1) {
        if (u->1) {
32
           u \to mx[i] = max(u \to mx[i], u \to 1 \to mx[i]);
           u \rightarrow mn[i] = min(u \rightarrow mn[i], u \rightarrow 1 \rightarrow mn[i]);
34
35
        }
        if (u->r) {
           u \to mx[i] = max(u \to mx[i], u \to r \to mx[i]);
           u - mn[i] = min(u - mn[i], u - r - mn[i]);
        }
40
     }
41 }
42
43 template <typename T>
```

```
node<T> *build(vector<node<T>> &a. int l. int r. int d = 0) {
      if (d == K) d = 0;
      if (1 >= r) {
46
47
        return nullptr;
     } else {
48
        int md = (1 + r) >> 1:
49
        nth element(a.begin() + 1, a.begin() + md, a.begin() + r,
50
                    [&](node<T> &x. node<T> &v) { return x.pt[d] < v.pt[d]: });</pre>
51
52
        node<T> *p = new node<T>(a[md]);
        ptr[p->id] = p;
53
        p->1 = build(a, 1, md, d + 1);
54
        p->r = build(a, md + 1, r, d + 1);
55
56
        pull(p):
57
        return p;
58
59 }
60
61
   template <typename T>
    node<T> *search(node<T> *u, P<T> p, int d = 0) {
     if (d == K) d = 0:
63
      if (not u) return nullptr;
     if (u->pt == p) return u:
65
     if (p[d] < u->pt[d]) {
66
67
       return search(u->1, p, d + 1);
     } else if (p[d] > u->pt[d]) {
68
        return search(u->r, p, d + 1);
69
     } else {
70
71
        auto tmp = search(u->1, p, d + 1);
72
       if (tmp) return tmp;
        return search(u->r, p, d + 1);
73
74
75 }
76
   template <typename T>
    void modify(node<T> *u, ll v) {
79
     if (not u) return;
     u \rightarrow val = v:
     for (auto cur = u; cur; cur = cur->p) {
81
82
        pull(cur);
    }
83
84 }
85
86 template <typename T>
```

```
bool inside(node<T> *nd, P<T> p, ll c) {
      int cc = 0;
      if (nd->mx[0] * p[0] + nd->mx[1] * p[1] >= c) cc++;
      if (nd-mn[0] * p[0] + nd-mn[1] * p[1] >= c) cc++;
      if (nd->mx[0] * p[0] + nd->mn[1] * p[1] >= c) cc++;
 91
 92
      if (nd->mn[0] * p[0] + nd->mx[1] * p[1] >= c) cc++;
 93
      return cc == 0;
 94 }
 95
     template <typename T>
     bool outside(node<T> *nd, P<T> p, 11 c) {
      int cc = 0;
      if (nd->mx[0] * p[0] + nd->mx[1] * p[1] >= c) cc++:
      if (nd->mn[0] * p[0] + nd->mn[1] * p[1] >= c) cc++;
100
101
      if (nd->mx[0] * p[0] + nd->mn[1] * p[1] >= c) cc++:
102
      if (nd-mn[0] * p[0] + nd-mx[1] * p[1] >= c) cc++;
103
      return cc == 4;
104 }
105
    template <typename T>
    11 query(node<T> *u, P<T> p, 11 c) {
      if (inside(u, p, c)) return u->sum:
      if (outside(u, p, c)) return 0;
110
      11 s = 0:
111
      if (u-pt[0] * p[0] + u-pt[1] * p[1] < c) {
112
        s += u -> val:
113
     }
114
      if (u->1) s += query(u->1, p, c);
115
      if (u->r) s += query(u->r, p, c);
116
      return s:
117 }
118
    template <typename T>
    T eval min(node<T> *nd,
121
               P<T> p) { // 通过估价函数进行启发式搜索,根据当前结果对搜索剪枝
122
      if (not nd) return numeric limits<T>::max() / 4;
123
      11 s = 0:
124
      rep(i, 0, K - 1) {
125
        if (p[i] <= nd->mn[i]) s += nd->mn[i] - p[i];
126
        if (p[i] >= nd -> mx[i]) s += p[i] - nd -> mx[i];
127
      }
128
      return s;
129 }
```

```
130
     template <typename T>
131
132
     11 mindist(node<T> *u. P<T> p) {
       11 s = numeric limits<T>::max() / 4;
133
       if (u->pt != p) {
134
         s = min(s, abs(u->pt[0] - p[0]) + abs(u->pt[1] - p[1]));
135
136
       ll best1 = eval_min(u->1, p), best2 = eval_min(u->r, p);
137
138
       if (best1 < best2) {
         if (u->1) s = min(s, mindist(u->1, p));
139
         if (u->r) and best2 < s) s = min(s, mindist(u->r, p));
140
141
         return s;
142
       } else {
143
         if (u\rightarrow r) s = min(s, mindist(u\rightarrow r, p));
         if (u\rightarrow 1 \text{ and best} 1 < s) s = min(s, mindist(u\rightarrow 1, p));
144
145
         return s;
146
147 }
148
     template <typename T>
149
150
     T eval max(node<T> *nd,
                P<T> p) { // 通过估价函数进行启发式搜索,根据当前结果对搜索剪枝
151
       if (not nd) return 0:
152
       11 s = 0;
153
       rep(i, 0, K - 1) s += max(abs(nd->mx[i] - p[i]), abs(nd->mn[i] - p[i]));
154
       return s;
155
156 }
157
     template <typename T>
158
     11 maxdist(node<T> *u, P<T> p) {
159
       11 s = 0;
160
       if (u->pt != p) {
161
         s = max(s, abs(u->pt[0] - p[0]) + abs(u->pt[1] - p[1]));
162
       }
163
       ll best1 = eval_max(u->1, p), best2 = eval_max(u->r, p);
164
       if (best1 > best2) {
165
         if (u->1) s = max(s, maxdist(u->1, p));
166
         if (u->r) and best2 > s) s = max(s, maxdist(u->r, p));
167
         return s:
168
       } else {
169
         if (u->r) s = max(s, maxdist(u->r, p));
170
         if (u\rightarrow 1 \text{ and best} 1 > s) s = max(s, maxdist(u\rightarrow 1, p));
171
172
         return s;
```

```
173
174 }
175 } // namespace kd
```

2.13 LCT.cpp

```
1 namespace linkCutTree {
   struct node {
       node *child[2], *parent, *max;
       int id;
5
       ll sum, val, sz, weight, rev;
       node(ll val, ll weight, int id) : child {nullptr, nullptr}, parent(
            nullptr), max(this), sum(val), val(val), sz(weight), weight(weight),
             id(id), rev(false) {}
7 };
9 bool isRoot(node *p) { return p->parent == nullptr || (p->parent->child[0]
        != p && p->parent->child[1] != p); }
   int side(node *p) { return p->parent->child[1] == p; }
12
   11 sum(node *p) { return p == nullptr ? 0 : p->sum; }
14
   11 sz(node *p) { return p == nullptr ? 0 : p->sz; }
16
   node *max(node *p) { return p == nullptr ? nullptr : p->max; }
18
19
   node *max(node *p, node *q) {
20
       if (p == nullptr)
21
           return a:
22
       if (q == nullptr)
23
           return p;
24
       return p->weight > q->weight ? p : q;
25 }
26
   void reverse(node *p) {
28
       if (p == nullptr)
29
           return:
30
        swap(p->child[0], p->child[1]);
31
       p->rev ^= 1:
32 }
33
34 void push(node *p) {
```

```
35
        if (p\rightarrow rev == 0)
36
             return;
37
        p \rightarrow rev = 0;
38
        reverse(p->child[0]);
        reverse(p->child[1]);
39
40 }
41
   void pull(node *p) {
43
        p\rightarrow sum = sum(p\rightarrow child[0]) + sum(p\rightarrow child[1]) + p\rightarrow val;
        p\rightarrow max = max(max(max(p\rightarrow child[0]), max(p\rightarrow child[1])), p);
44
45
        p->sz = p->weight + sz(p->child[0]) + sz(p->child[1]);
46 }
47
    void connect(node *p, node *q, int side) {
        q->child[side] = p;
49
50
        if (p != nullptr)
51
             p->parent = q;
52 }
53
    void rotate(node *p) {
54
55
        auto q = p->parent;
        int dir = side(p) ^ 1;
56
        connect(p->child[dir], q, dir ^ 1);
57
58
        if (!isRoot(q))
59
             connect(p, q->parent, side(q));
60
61
             p->parent = q->parent;
62
        connect(q, p, dir);
63
        pull(q);
64 }
65
66
    void splay(node *p) {
67
        vector<node *> stk;
68
        for (auto i = p; !isRoot(i); i = i->parent)
69
             stk.push_back(i->parent);
70
        while (!stk.empty()) {
71
             push(stk.back());
72
             stk.pop_back();
73
        }
        push(p);
74
75
        while (!isRoot(p)) {
76
             auto q = p->parent;
77
             if (!isRoot(q))
```

```
78
                 rotate(side(p) == side(q) ? q : p);
 79
             rotate(p);
         }
 80
 81
         pull(p);
 82 }
 83
     node *access(node *p) {
         node *j = nullptr;
 86
         for (node *i = p; i != nullptr; j = i, i = i -> parent) {
 87
             splay(i);
             i->val -= sum(j);
 88
 89
             i->val += sum(i->child[1]);
 90
             i \rightarrow child[1] = j;
 91
             pull(i);
 92
         }
 93
         splay(p);
 94
         return j;
 95 }
    void makeRoot(node *p) {
         access(p);
 99
         reverse(p);
100 }
101
102 void link(node *p, node *q) {
103
         makeRoot(p);
104
         access(q);
105
         p->parent = q;
106
         q->val += sum(p);
107 }
108
     void cut(node *p, node *q) {
110
         makeRoot(p);
111
         access(q);
112
         p->parent = q->child[0] = nullptr;
113 }
114
115 node *pathMax(node *p, node *q) {
116
         makeRoot(p);
117
         access(q);
118
         return max(q);
119 }
120
```

```
121 ll pathSize(node *p, node *q) {
         makeRoot(p);
122
123
         access(q);
124
         return sz(q);
125 }
126
    11 rootedSum(node *p) {
127
         makeRoot(p):
128
129
         return sum(p);
130 }
131
     11 getSubtree(node *rt, node *v) {
132
         makeRoot(rt):
133
134
         access(v);
         return v->val:
135
136 }
137
138
    bool connected(node *p, node *q) {
139
         access(p);
         access(q);
140
141
         return p->parent != nullptr;
142 }
143
    void fix(node *p, ll v) {
144
145
         access(p);
         push(p);
146
         // modify ...
147
148
         p \rightarrow val += v;
149
         pull(p);
150 }
151
    node *lca(node *z,node *x,node *y) {
152
         makeRoot(z):
153
154
         access(x);
         return access(y);
155
156 }
157 } // namespace linkCutTree
158 using namespace linkCutTree;
```

2.14 lichao-tree.cpp

```
1 struct Line {
2    i64 k, b;
```

```
i64 operator()(i64 x) const { return k * x + b; }
4 };
5 template <i64 L. i64 R>
   struct Segments {
      struct Node {
        optional < Line > s;
        Node *1, *r;
     }:
11
      Node *root;
      Segments() : root(nullptr) {}
13
      void add(i64 l, i64 r, i64 k, i64 b) {
14
        auto rec = [&](auto &rec, Node *&p, i64 tl, i64 tr, Line s) -> void {
15
          if (p == nullptr) p = new Node();
16
          i64 tm = midpoint(tl, tr);
17
          if (t1 >= 1 and tr <= r) {
18
            if (not p->s) return p->s = s, void();
19
            auto t = p->s.value();
20
            if (t(t1) >= s(t1)) {
21
              if (t(tr) >= s(tr)) return;
              if (t(tm) \ge s(tm)) return rec(rec, p->r, tm + 1, tr, s);
22
23
              return p \rightarrow s = s, rec(rec, p \rightarrow l, tl, tm, t);
24
25
            if (t(tr) \le s(tr)) return p->s = s, void();
            if (t(tm) \le s(tm)) return p->s = s, rec(rec, p->r, tm + 1, tr, t);
27
            return rec(rec, p->1, t1, tm, s);
28
          if (1 <= tm) rec(rec, p->1, t1, tm, s);
          if (r > tm) rec(rec, p->r, tm + 1, tr, s);
31
        };
32
        rec(rec, root, L, R, {k, b});
33
34
      optional < i64 > get(i64 x) {
35
        optional < i64> res = {};
36
        auto rec = [&](auto &rec, Node *p, i64 tl, i64 tr) -> void {
37
          if (p == nullptr) return;
          i64 tm = midpoint(tl, tr);
39
          if (p\rightarrow s) {
            i64 y = p -> s.value()(x);
            if (not res or res.value() < y) res = y;</pre>
41
42
          }
43
          if (x <= tm)
44
            rec(rec, p->1, t1, tm);
45
          else
```

2.15 Mo.cpp

```
1 int main() {
        std::ios::sync_with_stdio(false);
        cin.tie(0); cout.tie(0);
4
       for (int i = 1; i <= m; i++) {
            int x. v:
            cin >> x >> y;
           q.pb({x, y, i});
            rej[i] = (y - x + 1LL) * (y - x) / 2LL;
9
10
       sort(q.begin(), q.end(), [&](array<int, 3> a, array<int, 3> b)->bool{
11
12
            if (getb(a[0]) == getb(b[0]))
13
                if (getb(a[0]) & 1)
                    return a[1] < b[1];
14
15
                else
                    return a[1] > b[1]:
16
            else return getb(a[0]) < getb(b[0]);</pre>
17
18
       });
19
20
       int L = 1, R = 0;
21
       for (int i = 0: i < m: i++) {
22
            while (R < q[i][1]) R++, add(R);
23
            while (L > q[i][0]) L--, add(L);
            while (L < q[i][0]) del(L), L++;
24
25
            while (R > q[i][1]) del(R), R--;
26
            ans[a[i][2]] = tmp:
       }
27
28 }
```

2.16 moTree.cpp

```
1 void add(int ind, int end) { ... } // add a [ ind ] (end = 0 or 1)
2 void del(int ind, int end) { ... } // remove a [ ind ]
3 int calc() { ... } // compute current answer
```

```
4 vi mo(vector<pii> Q) {
    int L = 0, R = 0, blk = 350; // N/sqrt (Q)
     vi s(sz(Q)), res = s:
7 #define K(x) pii(x.first/blk, x.second ^ -(x.first/blk & 1))
     iota(all(s), 0):
     sort(all(s), [\&](int s, int t) { return K(Q[s]) < K(Q[t]); });
     for (int qi : s) {
11
       pii q = Q[qi];
12
       while (L > q.first) add(--L, 0);
       while (R < q.second) add(R++, 1);
14
       while (L < q.first) del(L++, 0);
       while (R > q.second) del(--R, 1);
      res[qi] = calc();
17
    }
18
     return res:
19 }
   vi moTree(vector<array<int, 2>> Q, vector<vi>& ed, int root = 0) {
     int N = sz(ed), pos[2] = {}, blk = 350; // N/sqrt(Q)
     vi s(sz(Q)), res = s, I(N), L(N), R(N), in(N), par(N);
     add(0, 0), in[0] = 1:
23
24
     auto dfs = [&](int x, int p, int dep, auto & f) -> void {
25
       par[x] = p:
26
      L[x] = N:
27
      if (dep) I[x] = N++;
     for (int y : ed[x]) if (y != p) f(y, x, !dep, f);
       if (!dep) I[x] = N++;
       R[x] = N:
31
    };
     dfs(root, -1, 0, dfs);
33 #define K(x) pii(I[x[0]] / blk, I[x[1]] ^ -(I[x[0]] / blk & 1))
     iota(all(s), 0);
     sort(all(s), [\&](int s, int t) { return K(Q[s]) < K(Q[t]); });
     for (int qi : s) rep(end, 0, 2) {
       int &a = pos[end], b = Q[qi][end], i = 0;
38 #define step(c) { if (in[c]) { del(a, end); in[a] = 0; } \
   else { add(c, end); in[c] = 1; } a = c; }
       while (!(L[b] \le L[a] \&\& R[a] \le R[b]))
        I[i++] = b, b = par[b];
41
       while (a != b) step(par[a]);
       while (i--) step(I[i]);
44
       if (end) res[qi] = calc();
45
    }
46
     return res;
```

```
47 }
```

2.17 MSTMo.cpp

```
#include <bits/stdc++.h>
2 using namespace std;
3 #define rep(i,a,n) for (int i=a;i<n;i++)</pre>
   #define per(i,a,n) for (int i=n-1; i>=a; i--)
5 #define pb push_back
   #define mp make_pair
7 #define all(x) (x).begin(),(x).end()
   #define fi first
9 #define se second
   #define SZ(x) ((int)(x).size())
11 typedef vector <int> VI;
12 typedef long long 11;
    typedef pair<int,int> PII;
   typedef double db;
   mt19937 mrand(random_device{}());
16 const ll mod=1000000007;
17 int rnd(int x) { return mrand() % x;}
18 ll powmod(ll a,ll b) {ll res=1; a%=mod; assert(b>=0); for(;b;b>>=1){if(b&1)
        res=res*a%mod:a=a*a%mod:}return res:}
19 11 gcd(11 a,11 b) { return b?gcd(b,a%b):a;}
    // head
21
22
    const int N=1010000:
   int a[N];
   namespace Mo {
     int Q,1[N],r[N],f[N],10,r0,ans[N],n;
27
     VI ne[N];
     struct point {
28
29
       int x, y, o;
       point(int a, int b, int c): x(a), y(b), o(c) {}
31
     };
32
     inline bool operator<(const point &a, const point &b) {</pre>
       if (a.x != b.x) return a.x > b.x:
33
34
       else return a.y < b.y;</pre>
     }
35
36
     vector<point> p;
37
     struct edge {
       int s. t. d:
```

```
39
        edge(const point &a, const point &b): s(a.o), t(b.o),
          d(abs(a.x - b.x) + abs(a.y - b.y)) \{ \}
40
41
42
      inline bool operator < (const edge &a, const edge &b) {return a.d < b.d;}
43
      vector<edge> e;
44
      int g[N],z[N];
45
      int cc, cnt[101000];
      void addedge() {
46
47
       sort(all(p));
48
          memset(g,0,sizeof(g));
49
          z[0]=N;
       rep(i,0,SZ(p)) z[i+1]=p[i].x-p[i].y;
51
       rep(i,0,SZ(p)) {
52
              int k = 0, t = p[i].x + p[i].y;
53
              for (int j = t; j; j -= j & -j)
                  if (z[g[j]] < z[k]) k = g[j];
              if (k) e.pb(edge(p[i], p[k - 1]));
              k = z[i + 1]:
56
57
              for (int j = t; j < N; j += j & -j)
                  if (k < z[g[j]]) g[j] = i + 1;
         }
59
60
     }
61
      void updata(int i, bool j,bool k=0) {
       // j=1 insert j=0 delete
62
63
       // k=0 left k=1 right
       if (j==1) {
64
          cnt[a[i]]++;
          if (cnt[a[i]]%2==0) cc++;
67
       } else {
          if (cnt[a[i]]%2==0) cc--:
          cnt[a[i]]--;
70
       }
71
      void init(int 1,int r) {
73
       for (int i=1;i<=r;i++) {
74
          cnt[a[i]]++;
          if (cnt[a[i]]%2==0) cc++;
76
       }
77
78
     inline int query() {
79
       return cc;
80
      int find(int x) { if (f[x] != x) f[x] = find(f[x]); return f[x];}
```

```
int l1 = l[i], r1 = r[i];
 83
         per(j,11,10) updata(j,1,0);
 84
 85
         rep(j,r0+1,r1+1) updata(j,1,1);
         rep(j,10,11) updata(j,0,0);
 86
         per(j,r1+1,r0+1) updata(j,0,1);
 87
         ans[i]=query();10=11;r0=r1;
         rep(j,0,SZ(ne[i])) if (ne[i][j]!=p) dfs(ne[i][j],i);
 89
      }
 90
       void solve() {
 91
 92
         p.clear();e.clear();
         rep(i,1,Q+1) ans[i]=0;
 93
         rep(i,1,Q+1) p.pb(point(l[i],r[i],i));
 94
 95
         addedge();
         rep(i,0,SZ(p)) p[i].y =n-p[i].y+1;
 96
 97
         addedge();
 98
         rep(i,0,SZ(p)) {
          int j =n-p[i].x+1;
          p[i].x = p[i].y; p[i].y = j;
100
        }
101
102
         addedge();
         rep(i,0,SZ(p)) p[i].x=n-p[i].x+1;
103
         addedge();
104
         sort(all(e));
105
106
         rep(i,1,Q+1) ne[i].clear(),f[i]=i;
         rep(i,0,SZ(e)) {
107
          int j=e[i].s,k=e[i].t;
108
          if (find(j)!=find(k)) f[f[j]]=f[k],ne[j].pb(k),ne[k].pb(j);
109
110
        }
111
        10=1[1]:r0=r[1]:
         init(10,r0);
112
113
         dfs(1.0):
114
      }
115 }
116
117 int main() {
       scanf("%d",&Mo::n);
118
      for (int i=1;i<=Mo::n;i++) scanf("%d",a+i);
119
       scanf("%d",&Mo::Q);
120
121
      rep(i,1,Mo::Q+1) scanf("%d%d",&Mo::1[i],&Mo::r[i]);
      Mo::solve();
122
      rep(i,1,Mo::Q+1) printf("%d\n",Mo::ans[i]);
123
124 }
```

void dfs(int i,int p) {

82

2.18 psegt.cpp

```
1 struct node {
      node *1, *r;
      ll val, sz, add;
4 };
5
    void pull(node *u) {
       u -> sz = 0, u -> val = 0;
      if (u->1) u->sz += u->1->sz, u->val += u->1->val;
       if (u\rightarrow r) u\rightarrow sz += u\rightarrow r\rightarrow sz, u\rightarrow val += u\rightarrow r\rightarrow val;
10 }
11
12 void push(node *u) {
      if (u->add) {
14
         if (u->1) {
           node *p = new node();
16
           *p = *u ->1;
17
           u \rightarrow 1 = p;
           p->add += u->add;
19
            p->val += p->sz * u->add;
20
        }
21
         if (u->r) {
22
           node *p = new node();
23
           *p = *u->r;
            u \rightarrow r = p;
            p->add += u->add;
26
           p \rightarrow val += p \rightarrow sz * u \rightarrow add;
27
         }
28
         u->add = 0;
29
30 }
31
32 node *build(int 1, int r) {
      node *p = new node();
     p->add = 0;
     if (1 == r) {
         p->1 = p->r = nullptr;
         p \rightarrow val = a[1];
37
         p->sz = 1;
     } else {
         int mid = (1 + r) >> 1;
41
         p->1 = build(1, mid);
42
         p \rightarrow r = build(mid + 1, r);
```

```
pull(p);
45
      return p;
46 }
47
    11 query(node *v, int 1, int r, int ql, int qr) {
      if (ql == 1 && qr == r) {
        return v->val:
50
     } else {
51
        push(v);
52
53
        int mid = (1 + r) >> 1;
        if (qr <= mid)
54
         return query(v->1, 1, mid, q1, qr);
55
        else if (ql > mid)
56
57
          return query(v->r, mid + 1, r, ql, qr);
58
59
          return query(v->1, 1, mid, ql, mid) +
                  query(v->r, mid + 1, r, mid + 1, qr);
60
61
62 }
    node *modify(node *v, int 1, int r, int q1, int qr, 11 x) {
      if (al == 1 && ar == r) {
65
66
        node *p = new node();
67
        *p = *v;
        p->add += x;
        p \rightarrow val += p \rightarrow sz * x;
        return p;
70
71
     } else {
72
        push(v):
        int mid = (1 + r) >> 1;
73
74
        node *p = new node();
75
        *p = *v;
76
        if (qr <= mid)</pre>
77
         p->1 = modify(v->1, 1, mid, ql, qr, x);
78
        else if (ql > mid)
          p->r = modify(v->r, mid + 1, r, ql, qr, x);
79
80
        else
          p->1 = modify(v->1, 1, mid, ql, mid, x),
81
82
          p->r = modify(v->r, mid + 1, r, mid + 1, qr, x);
        pull(p);
83
        return p;
84
     }
```

2.19 rollbackMo.cpp

86 }

```
1 int n, q, k, block;
2 int cnt[maxn], ans[maxn], a[maxn], vis[maxn];
3 vector<array<int, 4>> que;
5 int getb(int x) {
        return (x - 1) / block + 1;
7 }
9 int main() {
        std::ios::sync_with_stdio(false);
11
        cin.tie(0); cout.tie(0);
12
13
       cin >> n;
       block = sqrt(n);
14
15
16
       rep(i, 1, n) cin >> a[i];
17
       cin >> a:
18
       rep(i, 1, q) {
19
           int 1, r;
20
            cin >> 1 >> r >> k;
21
            que.pb({1, r, i, k});
22
23
        sort(ALL(que), [&](array<int, 4> a, array<int, 4> b)->bool{
24
            if (getb(a[0]) != getb(b[0]))
25
                return getb(a[0]) < getb(b[0]);</pre>
26
27
                return a[1] < b[1]:
28
       });
29
       int len = que.size();
31
       int 1. r:
        auto add = [&](int x, int t) {
            cnt[vis[a[x]]]--;
            vis[a[x]]++:
34
35
            cnt[vis[a[x]]]++;
       }:
37
        auto del = [\&] (int x) {
38
            cnt[vis[a[x]]]--;
39
            vis[a[x]]--;
```

```
cnt[vis[a[x]]]++;
       };
41
42
43
       for (int x = 0; x < len;) {
            int v = x:
44
            while (y < len && getb(que[y][0]) == getb(que[x][0])) y++;
45
            //暴力块内
            while (x < y && que[x][1] \le getb(que[x][0])*block) {
47
                for (int j = que[x][0]; j <= que[x][1]; j++)</pre>
                    add(j, que[x][3]);
49
50
                ans[que[x][2]] = cnt[que[x][3]];
                for (int j = que[x][0]; j \le que[x][1]; j++)
51
                    del(i):
52
53
                x++;
54
            }
            //块外
55
            r = getb(que[x][0]) * block;
            while (x < y) {
57
               1 = getb(que[x][0]) * block + 1;
58
                while (r < que[x][1]) r++, add(r, que[x][3]);
59
                while (1 > que[x][0]) 1--, add(1, que[x][3]);
60
61
                ans [que[x][2]] = cnt[que[x][3]]:
                for (int j = que[x][0]; j <= getb(que[x][0])*block; j++)</pre>
63
                    del(j);
64
                x++:
65
            for (int j = getb(que[x - 1][0]) * block + 1; j <= que[x - 1][1]; j
                ++)
67
                del(j);
68
       rep(i, 1, q) cout << ans[i] << '\n';
69
70 }
```

2.20 segtree.cpp

```
1 struct info {
2    ll sum;
3    int sz;
4    friend info operator+(const info &a, const info &b) {
5       return {(a.sum + b.sum) % mod, a.sz + b.sz};
6    }
7 };
8
```

```
9 struct tag {
10
       ll add, mul;
       friend tag operator+(const tag &a, const tag &b) {
12
           tag res = {(a.add * b.mul + b.add) % mod, a.mul * b.mul % mod};
13
           return res:
14
       }
15 };
16 info operator+(const info &a, const tag &b) {
        return {(a.sum * b.mul + a.sz * b.add) % mod, a.sz};
18 }
19
20 struct node {
       info val:
       tag t;
23 } seg[maxn << 2];
24
25 void update(int id) {
        seg[id].val = seg[id * 2].val + seg[id * 2 + 1].val:
27 }
28 void settag(int id, tag t) {
       seg[id].val = seg[id].val + t;
       seg[id].t = seg[id].t + t:
31 }
32 void pushdown(int id) {
       if (seg[id].t.mul == 1 and seg[id].t.add == 0) return:
34
       settag(id * 2, seg[id].t);
       settag(id * 2 + 1, seg[id].t);
       seg[id].t.mul = 1;
37
       seg[id].t.add = 0;
38 }
39 void build(int 1, int r, int id) {
       seg[id].t = {0, 1};
41
       if (1 == r) {
           seg[id].val = {a[1], 1};
       } else {
43
44
           int mid = (1 + r) >> 1;
           build(1, mid, id * 2);
           build(mid + 1, r, id * 2 + 1);
           update(id):
47
48
       }
49 }
50 void change(int 1, int r, int id, int q1, int qr, tag t) {
51
       if (1 == q1 && r == qr) {
```

```
52
            settag(id, t);
       } else {
53
54
            int mid = (1 + r) >> 1:
55
           pushdown(id);
56
           if (qr <= mid) {
                change(1, mid, id * 2, ql, qr, t);
57
58
           } else if (ql > mid) {
                change(mid + 1, r, id * 2 + 1, ql, qr, t);
59
60
           } else {
                change(1, mid, id * 2, q1, mid, t);
61
62
                change(mid + 1, r, id * 2 + 1, mid + 1, qr, t);
           }
63
64
           update(id):
65
       }
66 }
67 info query(int 1, int r, int id, int q1, int qr) {
       if (1 == ql && r == qr) {
69
           return seg[id].val;
70
       } else {
           int mid = (1 + r) >> 1:
71
72
           pushdown(id);
73
           if (ar <= mid)
74
                return query(1, mid, id * 2, ql, qr);
75
            else if (ql > mid)
76
                return query(mid + 1, r, id * 2 + 1, ql, qr);
77
            else
                return query(1, mid, id * 2, q1, mid) +
                       query(mid + 1, r, id * 2 + 1, mid + 1, qr);
79
80
       }
81 }
   11 search(int 1, int r, int id, int q1, int qr, int d) {
        if (al == 1 && ar == r) {
           int mid = (1 + r) / 2;
84
85
           // if (l != r) pushdown(id); ...
           if (seg[id].val < d)</pre>
87
                return -1;
            else {
                if (1 == r)
                    return 1:
91
                else if (seg[id * 2].val >= d)
92
                    return search(1, mid, id * 2, ql, mid, d);
93
                else
94
                    return search(mid + 1, r, id * 2 + 1, mid + 1, qr, d);
```

```
95
             }
         } else {
 97
             int mid = (1 + r) >> 1:
 98
             // pushdown(id); ...
             if (ar <= mid)
 99
100
                 return search(1, mid, id * 2, ql, qr, d);
101
             else if (ql > mid)
102
                 return search(mid + 1, r, id * 2 + 1, al, ar, d):
103
104
                 int tmp = search(1, mid, id * 2, ql, mid, d);
105
                 if (tmp != -1)
106
                     return tmp;
107
108
                     return search(mid + 1, r, id * 2 + 1, mid + 1, qr, d);
109
             }
110
         }
111 }
```

2.21 segtreefast.cpp

```
1 /**
2 * Author: Lucian Bicsi
   * Description: Very fast and quick segment tree.
    * Only useful for easy invariants. O-indexed.
    * Range queries are half-open.
    */
   #pragma once
   struct SegmTree {
10
     vector<int> T: int n:
      SegmTree(int n) : T(2 * n, (int)2e9), n(n) {}
12
13
     void Update(int pos, int val) {
       for (T[pos += n] = val; pos > 1; pos /= 2)
14
15
         T[pos / 2] = min(T[pos], T[pos ^ 1]):
16
     }
17
18
     int Querv(int b. int e) {
19
       int res = (int)2e9;
       for (b += n, e += n; b < e; b /= 2, e /= 2) {
21
         if (b \% 2) res = min(res. T[b++]):
22
         if (e \% 2) res = min(res, T[--e]);
23
       }
```

```
24 return res;
25 }
26 };
```

2.22 SparseTable.cpp

```
1 template <typename T, class F = function <T(const T&, const T&)>>
2 class SparseTable {
   public:
     int n;
     vector<vector<T>> mat:
     F func;
      SparseTable(const vector < T > & a, const F & f) : func(f) {
       n = static cast<int>(a.size()):
       int max_log = 32 - __builtin_clz(n);
11
       mat.resize(max log);
       mat[0] = a:
12
       for (int j = 1; j < max log; <math>j++) {
13
         mat[i].resize(n - (1 << i) + 1):
14
15
         for (int i = 0; i \le n - (1 \le j); i++) {
16
           mat[j][i] = func(mat[j-1][i], mat[j-1][i+(1 << (j-1))]);
         }
17
18
       }
19
20
21
     T get(int from, int to) const {
22
        assert(0 <= from && from <= to && to <= n - 1);
23
       int lg = 32 - __builtin_clz(to - from + 1) - 1;
       return func(mat[lg][from], mat[lg][to - (1 << lg) + 1]);
24
25
     }
26 };
```

2.23 SparseTable2D.cpp

```
1  // lg[1] = 0;
2  // rep(i, 2, N - 1) {
3    // lg[i] = lg[i / 2] + 1;
4    // }
5    // int k = log2(r - l + 1); very slow!!!
6    // int k = __lg(r - l + 1);
7    // int k = lg[r - l + 1];
8    // int k = 32 - __builtin_clz(r - l + 1) - 1;
```

```
vector<vector<int>> sparse[12];
10
11 int query(int x, int y, int d) {
     int k = lg(d);
    int s = d - bit(k):
13
     return min({sparse[k][x][y], sparse[k][x + s][y], sparse[k][x][y + s],
14
         sparse[k][x + s][y + s]);
15 }
16
17 void build() {
     rep(i, 1, n) rep(j, 1, m) sparse[0][i][j] = mat[i][j];
    rep(k, 1, 11) rep(i, 1, n) rep(j, 1, m) {
     int d = bit(k - 1):
20
21
     if (i + d > n || j + d > m) continue;
       sparse[k][i][j] = min({sparse[k - 1][i][j], sparse[k - 1][i + d][j],}
           sparse[k - 1][i][j + d], sparse[k - 1][i + d][j + d]});
23
24 }
```

2.24 treap.cpp

```
1 /**
         author: tourist
         created: 07.10.2022 20:32:03
5 #include <bits/stdc++.h>
   using namespace std;
  #ifdef LOCAL
10 #include "algo/debug.h"
11 #else
12 #define debug(...) 42
   #endif
14
15 mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
17 class node {
18 public:
    int id:
    node* 1;
21
     node* r;
22
     node* p;
```

```
bool rev;
     int sz;
     // declare extra variables:
25
26
     long long P;
     long long add;
27
     long long x;
28
29
     node(int _id, long long _x) {
30
31
       id = id;
       l = r = p = nullptr;
32
33
       rev = false;
34
       sz = 1;
       // init extra variables:
35
36
       P = rng();
       add = 0;
37
       x = _x;
39
     }
40
41
     // push everything else:
     void push_stuff() {
42
       if (add != 0) {
43
44
         if (1 != nullptr) {
           1->unsafe_apply(add);
45
46
         }
47
         if (r != nullptr) {
           r->unsafe_apply(add);
48
         }
50
          add = 0;
51
     }
52
53
     void unsafe_reverse() {
54
55
       push_stuff();
       rev ^= 1;
56
57
       swap(1, r);
       pull();
59
     }
60
61
     // apply changes:
62
     void unsafe_apply(long long delta) {
       add += delta;
63
       x += delta;
65
     }
```

```
66
       void push() {
        if (rev) {
 68
 69
          if (1 != nullptr) {
            1->unsafe_reverse();
 70
 71
          }
 72
          if (r != nullptr) {
 73
            r->unsafe_reverse();
          }
 74
 75
          rev = 0:
 76
        }
 77
        push_stuff();
 78
 79
       void pull() {
         sz = 1;
        if (l != nullptr) {
          1->p = this;
 84
           sz += 1->sz;
        }
 85
        if (r != nullptr) {
          r->p = this:
           sz += r->sz:
        }
 90
      }
 91 };
 92
 93 void debug_node(node* v, string pref = "") {
 94 #ifdef LOCAL
     if (v != nullptr) {
        debug_node(v->r, pref + "\");
 97
        cerr << pref << "-" << "<sub>||</sub>" << v->id << '\n';
        debug_node(v->1, pref + "\");
     } else {
        cerr << pref << "-" << "nullptr" << '\n';
100
101
     }
102 #endif
103 }
104
105 namespace treap {
106
    pair < node *, int > find (node * v, const function < int (node *) > &go_to) {
     // go_to returns: 0 -- found; -1 -- go left; 1 -- go right
```

```
// find returns the last vertex on the descent and its go to
109
       if (v == nullptr) {
110
         return {nullptr, 0};
111
112
       }
       int dir:
113
       while (true) {
114
         v->push();
115
         dir = go_to(v);
116
117
         if (dir == 0) {
           break:
118
119
         node* u = (dir == -1 ? v -> 1 : v -> r);
120
         if (u == nullptr) {
121
122
           break;
         }
123
124
125
126
       return {v, dir};
127 }
128
     node* get_leftmost(node* v) {
       return find(v, [&](node*) { return -1; }).first;
130
131 }
132
     node* get_rightmost(node* v) {
133
       return find(v, [&](node*) { return 1; }).first;
134
135 }
136
     node* get_kth(node* v, int k) { // O-indexed
137
       pair<node*, int> p = find(v, [&](node * u) {
138
         if (u->1 != nullptr) {
139
140
           if (u->1->sz > k) {
             return -1;
141
142
           }
           k \rightarrow u \rightarrow 1 \rightarrow sz;
143
         }
144
         if (k == 0) {
145
           return 0;
146
147
         }
         k--;
148
         return 1;
149
150
       });
       return (p.second == 0 ? p.first : nullptr);
151
```

```
152 }
153
154 int get_pos(node* v) { // 0-indexed
155
       int k = (v->1 != nullptr ? v->1->sz : 0);
156
       while (v->p != nullptr) {
157
        if (v == v -> p -> r) {
158
           k++;
           if (v->p->l != nullptr) {
160
             k += v->p->l->sz;
161
           }
162
        }
163
         v = v -> p;
164
165
       return k;
166 }
167
    node* get root(node* v) {
      while (v->p != nullptr) {
170
        v = v -> p;
171
      }
172
       return v;
173 }
174
     pair<node*, node*> split(node* v, const function<bool(node*)> &is_right) {
176
      if (v == nullptr) {
177
         return {nullptr, nullptr};
      }
178
179
      v->push();
180
      if (is_right(v)) {
181
         pair < node *, node *> p = split(v->1, is_right);
182
        if (p.first != nullptr) {
183
           p.first->p = nullptr;
184
        }
185
        v->1 = p.second;
186
        v->pull();
187
         return {p.first, v};
188
      } else {
189
         pair<node*, node*> p = split(v->r, is_right);
190
        v->r = p.first;
191
        if (p.second != nullptr) {
192
           p.second->p = nullptr;
193
        }
194
         v->pull();
```

```
return {v, p.second};
195
       }
196
197 }
198
     pair<node*, node*> split_cnt(node* v, int k) {
199
       if (v == nullptr) {
200
         return {nullptr, nullptr};
201
       }
202
203
       v->push();
       int left_and_me = (v->1 != nullptr ? v->1->sz : 0) + 1;
204
       if (k < left and me) {</pre>
205
         pair < node*, node*> p = split cnt(v->1, k);
206
         if (p.first != nullptr) {
207
208
           p.first->p = nullptr;
         }
209
210
         v->1 = p.second;
211
         v->pull();
         return {p.first, v};
212
       } else {
213
         pair<node*, node*> p = split_cnt(v->r, k - left_and_me);
214
         v \rightarrow r = p.first;
215
         if (p.second != nullptr) {
216
           p.second->p = nullptr;
217
218
         }
219
         v->pull();
220
         return {v, p.second};
       }
221
222 }
223
     node* merge(node* v. node* u) {
224
       if (v == nullptr) {
225
226
         return u:
       }
227
       if (u == nullptr) {
228
         return v;
229
230
       }
       if (v->P > u->P) {
231
            if (rng() \% (v\rightarrow sz + u\rightarrow sz) < (unsigned int) v\rightarrow sz) {
232
233
         v->push();
         v \rightarrow r = merge(v \rightarrow r, u);
234
         v->pull();
235
         return v:
       } else {
```

```
238
        u->push();
239
        u -> 1 = merge(v, u -> 1);
240
        u->pull();
241
        return u;
242
      }
243 }
244
     int count left(node* v. const function<bool(node*)> &is right) {
       if (v == nullptr) {
247
        return 0:
248
      }
249
      v->push();
250
      if (is right(v)) {
251
        return count left(v->1, is right);
252
      }
253
       return (v->1 != nullptr ? v->1->sz : 0) + 1 + count left(v->r, is right);
254 }
255
     int count_less(node* v, long long val) {
257
      int res = 0:
258
       while (v != nullptr) {
259
        v->push():
260
        if (v->x >= val) {
261
          v = v -> 1:
262
        } else {
263
           res += (v->1 != nullptr ? v->1->sz : 0) + 1;
           v = v -> r:
265
        }
      }
266
267
       return res:
268 }
269
     node* add(node* r, node* v, const function<bool(node*)> &go left) {
271
       pair<node*, node*> p = split(r, go_left);
272
       return merge(p.first, merge(v, p.second));
273 }
274
     node* remove(node* v) { // returns the new root
276
      v->push();
277
      node* x = v->1;
278
      node* v = v->r;
279
      node* p = v->p;
      v->1 = v->r = v->p = nullptr;
```

```
v->push();
281
       v->pull(); // now v might be reusable...
282
       node* z = merge(x, y);
283
       if (p == nullptr) {
284
         if (z != nullptr) {
285
           z->p = nullptr;
286
         }
287
288
         return z;
289
      }
       if (p->1 == v) {
290
         p->1 = z;
291
292
       if (p->r == v) {
293
294
         p->r = z;
       }
295
296
       while (true) {
297
         p->push();
298
         p->pull();
299
         if (p->p == nullptr) {
           break;
300
301
         }
302
         p = p \rightarrow p;
303
304
       return p;
305 }
306
     node* next(node* v) {
307
       if (v->r == nullptr) {
308
309
         while (v->p != nullptr && v->p->r == v) {
           v = v -> p;
310
         }
311
312
         return v->p;
      }
313
       v->push();
314
       v = v -> r;
315
       while (v->1 != nullptr) {
316
         v->push();
317
         v = v -> 1;
318
319
      }
       return v;
320
321 }
322
323 node* prev(node* v) {
```

```
324
       if (v->1 == nullptr) {
325
         while (v->p != nullptr && v->p->l == v) {
326
           v = v -> p;
327
        }
328
        return v->p;
329
      }
330
      v->push();
331
      v = v -> 1:
332
      while (v->r != nullptr) {
333
        v->push();
334
        v = v -> r;
335
      }
336
       return v;
337 }
338
339
     int get_size(node* v) {
       return (v != nullptr ? v->sz : 0);
341 }
342
343 template<typename... T>
344 void Apply(node* v, T... args) {
      v->unsafe_apply(args...);
346 }
347
348 void reverse(node* v) {
349
      v->unsafe reverse();
350 }
351
352 // extra of mine
353 long long lower(node* u, long long x) {
354
      if (u == nullptr)
355
        return numeric_limits<long long>::min();
356
       else if (x \le u -> x)
357
        return lower(u->1, x);
358
       else
359
         return max(u->x, lower(u->r, x));
360 }
361
362 long long upper(node* u, long long x) {
363
      if (u == nullptr)
364
        return numeric_limits<long long>::max();
365
       else if (u->x <= x)
366
        return upper(u->r, x);
```

```
367
       else
         return min(u->x, upper(u->1, x));
368
369 }
370
    } // namespace treap
372
373
     using namespace treap;
374
375
    int n;
376
     int main() {
377
       ios::sync_with_stdio(false);
378
       cin.tie(0):
379
380
       node* root = nullptr;
       cin >> n:
381
       for (int i = 1; i <= n; i++) {
382
         int op;
383
384
         long long x;
385
         cin >> op >> x;
         switch (op) {
386
387
           case 1: {
             root = add(root. new node(x, x), [&](node * u) {
388
               return x < u->x:
389
390
             });
391
             break:
           }
392
           case 2: {
393
             auto [pt, w] = find(root, [&](node * u) {
394
395
               if (x < u \rightarrow x) return -1;
               else if (x == u->x) return 0:
396
397
               else return 1;
398
             }):
             assert(w == 0);
399
400
             root = remove(pt);
             break;
401
402
           }
           case 3: {
403
             cout << count less(root, x) + 1 << '\n';</pre>
404
405
             break;
           }
406
           case 4: {
407
             cout << get_kth(root, x - 1)->x << '\n';</pre>
408
             break;
409
```

```
410
            }
411
            case 5: {
              cout << lower(root, x) << '\n';</pre>
413
              break;
414
           }
415
            case 6: {
416
              cout << upper(root, x) << '\n';</pre>
           }
418
419
         }
420
      }
421 }
```

2.25 UnionFindRollback.cpp

```
1 vector<int> fa(n):
2 iota(all(fa), 0);
3 vector<int> sz(n, 1);
   vector<pair<int, int>> ops;
   auto Get = [&](int i) {
7
       while (i != fa[i]) {
           i = fa[i];
       }
       return i;
11 };
12 auto Unite = [&](int i, int j) {
13
       i = Get(i), j = Get(j);
14
       if (i == j) {
15
           return:
16
       }
17
       if (sz[i] > sz[j]) {
18
           swap(i, j);
19
       }
       ops.emplace_back(i, fa[i]);
21
       fa[i] = j;
       ops.emplace_back(~j, sz[j]);
       sz[j] += sz[i];
23
24 };
25 auto RollBack = [\&] (int T) {
26
       while (SZ(ops) > T) {
27
           auto [i, j] = ops.back();
28
           ops.pop_back();
```

```
if (i >= 0) {
29
                fa[i] = j;
31
            } else {
32
                sz[~i] = j;
            }
33
34
37 11 ans = 0;
    auto Dfs = [&](auto &&Dfs, int 1, int r) -> void {
        if (1 == r) {
39
            for (auto [x, y] : g[1]) {
40
                x = Get(x);
41
                y = Get(y);
                ans += 111 * sz[x] * sz[y];
43
            }
44
        } else {
45
            int mid = midpoint(l, r);
47
                int save = SZ(ops);
48
                for (int i = mid + 1; i <= r; i++) {
                    for (auto [x, y] : g[i]) {
50
51
                        Unite(x, y);
52
                    }
                }
53
                Dfs(Dfs, 1, mid);
54
                RollBack(save);
55
            }
57
                int save = SZ(ops);
58
                for (int i = 1; i <= mid; i++) {
60
                    for (auto [x, y] : g[i]) {
                        Unite(x, y);
61
                    }
                }
                Dfs(Dfs, mid + 1, r);
                RollBack(save);
65
            }
67
69 Dfs(Dfs, 0, n - 1);
```

2.26 树哈希.cpp

```
1 basic_string<int> e[maxn];
2 ull hashv[maxn];
   ull seed1, seed2, seed3, seed4;
   ull f(ull x) { return x * x * x * seed1 + x * seed2; }
   ull h(ull x) { return f(x) ^ ((x \& seed3) >> 31) ^ ((x \& seed4) << 31); }
   void dfs1(int u, int fa) {
       hashv[u] = 1;
       for (auto v : e[u]) if (v != fa) {
11
               dfs1(v, u);
12
               hashv[u] += h(hashv[v]);
13
           }
14 }
15
16 void dfs2(int u, int fa, ull fv) {
17 // for each root
       hashv[u] += fv;
       for (auto v : e[u]) if (v != fa) {
                dfs2(v, u, h(hashv[u] - h(hashv[v])));
21
           }
22 }
23
24 void solve() {
       seed1 = rng(), seed2 = rng();
       seed3 = rng(), seed4 = rng();
       cin >> n:
       rep(i, 2, n) {
           int u, v;
30
           cin >> u >> v;
31
           e[u].pb(v);
32
           e[v].pb(u);
33
       }
       dfs1(1, 0);
       sort(hashv + 1, hashv + n + 1);
       n = unique(hashv + 1, hashv + n + 1) - hashv - 1;
       cout << n << '\n':
38 }
```

2.27 树链剖分 segtree.cpp

```
1 int n, m, a[N];
```

```
2 vector<int> e[N]:
3 int 1[N], r[N], idx[N];
4 int sz[N], hs[N], tot, top[N], dep[N], fa[N];
6 struct info {
       int maxv, sum;
10 info operator + (const info &1, const info &r) {
       return (info){max(1.maxv, r.maxv), 1.sum + r.sum};
11
12 }
13
14 struct node {
       info val;
16 } seg[N * 4];
18 // [l, r]
   void update(int id) {
       seg[id].val = seg[id * 2].val + seg[id * 2 + 1].val;
21
22 }
24 void build(int id, int 1, int r) {
       if (1 == r) {
25
           // 1号点, DFS序中第1个点
26
           seg[id].val = {a[idx[1]], a[idx[1]]};
       } else {
           int mid = (1 + r) / 2;
30
           build(id * 2, 1, mid);
           build(id * 2 + 1, mid + 1, r);
31
32
           update(id);
       }
34 }
35
   void change(int id, int 1, int r, int pos, int val) {
37
       if (1 == r) {
           seg[id].val = {val, val};
       } else {
39
           int mid = (1 + r) / 2;
           if (pos <= mid) change(id * 2, 1, mid, pos, val);</pre>
41
           else change(id * 2 + 1, mid + 1, r, pos, val);
           update(id);
44
       }
```

```
45 }
46
47 info query(int id, int 1, int r, int ql, int qr) {
       if (l == ql && r == qr) return seg[id].val;
49
       int mid = (1 + r) / 2:
       if (qr <= mid) return query(id * 2, 1, mid, ql, qr);</pre>
       else if (ql > mid) return query(id * 2 + 1, mid + 1, r, ql,qr);
53
           return query(id * 2, 1, mid, ql, mid) +
54
               query(id * 2 + 1, mid + 1, r, mid + 1, qr);
       }
56 }
57
58 // 第一端 DFS, 子树大小, 重儿子, 父亲, 深度
59 void dfs1(int u.int f) {
       sz[u] = 1;
       hs[u] = -1;
    fa[u] = f:
    dep[u] = dep[f] + 1;
    for (auto v : e[u]) {
           if (v == f) continue;
           dfs1(v. u):
           sz[u] += sz[v]:
           if (hs[u] == -1 || sz[v] > sz[hs[u]])
               hs[u] = v:
       }
71 }
73 // 第二遍 DFS, 每个点 DFS 序, 重链上的链头的元素。
74 void dfs2(int u. int t) {
       top[u] = t;
      l[u] = ++tot;
      idx[tot] = u;
       if (hs[u] != -1) {
79
           dfs2(hs[u], t);
       }
       for (auto v : e[u]) {
           if (v != fa[u] && v != hs[u]) {
               dfs2(v, v);
84
           }
       }
       r[u] = tot;
87 }
```

```
int LCA(int u, int v) {
         while (top[u] != top[v]) {
 90
 91
             if (dep[top[u]] < dep[top[v]]) v = fa[top[v]];</pre>
             else u = fa[top[u]];
 92
         }
 93
         if (dep[u] < dep[v]) return u;</pre>
 94
         else return v:
 95
 96 }
 97
     info query(int u,int v) {
         info ans{(int)-1e9, 0};
 99
         while (top[u] != top[v]) {
100
101
             if (dep[top[u]] < dep[top[v]]) {</pre>
                  ans = ans + query(1, 1, n, l[top[v]], l[v]);
102
                 v = fa[top[v]];
103
             } else {
104
105
                  ans = ans + query(1, 1, n, l[top[u]], l[u]);
106
                 u = fa[top[u]];
             }
107
108
         if (dep[u] \le dep[v]) ans = ans + query(1, 1, n, l[u], l[v]);
109
         else ans = ans + query(1, 1, n, 1[v], 1[u]);
110
111
         return ans;
112 }
```

2.28 笛卡尔树.cpp

```
int a[maxn], l[maxn], r[maxn], root;
2 int ans[maxn], tot:
   void build() {
       stack<int> stk:
       for (int i = 1; i <= n; i++) {
           int last = 0:
            while (!stk.empty() && a[stk.top()] > a[i]) {
                last = stk.top();
10
                stk.pop();
11
           }
           if (stk.empty())
12
13
                root = i;
14
            else
                r[stk.top()] = i;
15
```

2.29 线段树合并.cpp

```
1 struct node {
     int sz, sum;
     node *1, *r;
     node() : sz(0), sum(0), l(nullptr), r(nullptr) {}
5 } pool[N * 20], *cur = pool;
   node *newnode() {
     return cur++:
9 }
10
11 void upd(node *rt) {
     if (not rt) return;
     rt->sum = rt->sz > 0:
14
     if (rt->1) rt->sum += rt->1->sum;
15
     if (rt->r) rt->sum += rt->r->sum:
16 }
17
18 node *modify(node *rt, int 1, int r, int pos, int d) {
19
     if (not rt) rt = newnode();
    if (1 == r) {
20
21
     rt->sz += d;
22
       upd(rt):
       return rt;
24
    } else {
       int md = (1 + r) >> 1;
26
       if (pos <= md)
27
         rt->1 = modify(rt->1, 1, md, pos, d);
29
         rt->r = modify(rt->r, md + 1, r, pos, d);
30
       upd(rt);
```

```
}
33 }
34
    node *merge(node *u, node *v, int 1, int r) {
      if (not u) return v;
37
      if (not v) return u;
      if (1 == r) {
38
39
        u->sz += v->sz;
40
        upd(u);
        return u;
41
      } else {
        int md = (1 + r) >> 1:
43
44
        u -> 1 = merge(u -> 1, v -> 1, 1, md);
        u \rightarrow r = merge(u \rightarrow r, v \rightarrow r, md + 1, r);
45
        upd(u);
        return u;
47
49 }
50
    11 query(node *rt, int 1, int r) {
      if (not rt) return 0:
53
      return rt->sum:
54 }
55
    pair<node *, node *> split(node *rt, int l, int r, int ql, int qr) {
      if (not rt) return {nullptr, nullptr};
57
      if (ql == 1 && qr == r) {
58
59
        return {nullptr, rt};
     } else {
60
61
        int md = (1 + r) >> 1;
62
        if (qr <= md) {
          auto [p1, p2] = split(rt->1, 1, md, q1, qr);
63
64
          rt->1 = p1;
          upd(rt);
65
          if (not p2) return {rt, nullptr};
          node *u = newnode();
67
          u ->1 = p2;
          upd(u);
          return {rt, u};
70
        } else if (ql > md) {
71
72
          auto [p1, p2] = split(rt->r, md + 1, r, ql, qr);
73
          rt->r = p1;
```

31

return rt;

```
74
          upd(rt);
          if (not p2) return {rt, nullptr};
          node *u = newnode();
76
77
          u - r = p2;
          upd(u);
78
          return {rt, u};
79
        } else {
81
          auto [p1, p2] = split(rt->1, 1, md, q1, md);
          auto [p3, p4] = split(rt->r, md + 1, r, md + 1, qr);
          rt -> 1 = p1, rt -> r = p3;
          upd(rt);
          if (not p2 and not p4) return {rt, nullptr};
          node *u = newnode():
          u \rightarrow 1 = p2, u \rightarrow r = p4;
          upd(u);
          return {rt, u};
        }
     }
92 }
```

3 DP

3.1 Convex hull optimization.cpp

```
1 array<11, 3> a[maxn];
2 int q[maxn];
3 ll ans[maxn]:
5 11 X(int p) {
       return 211 * a[p][0];
7 }
8 11 Y(int p) {
       return a[p][0] * a[p][0] + a[p][1];
10 }
11 ldb slope(int x, int y) {
12
       return (1db)(Y(y) - Y(x)) / (X(y) - X(x));
13 }
14 void solve() {
       cin >> n:
       int head = 1, rear = 0;
17
       rep(i, 1, n) {
18
           cin >> a[i][0] >> a[i][1];
```

```
a[i][2] = i:
19
       }
20
21
       sort(a + 1, a + n + 1);
22
       rep(i, 1, n) {
23
            while (head < rear && slope(q[rear], i) <= slope(q[rear], q[rear -
24
                1])) rear--;
           a[++rear] = i:
25
26
       }
       rep(i, 1, n) {
27
28
           11 k = -a[i][0];
            while (head < rear && slope(q[head], q[head + 1]) <= k) head++;
29
            ans[a[i][2]] = (a[i][0] + a[q[head]][0]) * (a[i][0] + a[q[head]][0])
30
                 + a[i][1] + a[q[head]][1];
31
       }
32
        rep(i, 1, n) cout << ans[i] << '\n';
33 }
```

3.2 DivideAndConquerDP.cpp

3.3 有依赖决策单调.cpp

```
1 pair<int, int> stk[N];
2 auto calc = [&](int i, int j) { ... } // dp[j] -> dp[i]
3 int h = 0, t = 0;
4 stk[t++] = {1, 0}; // {left, opt}
5
6 for (int i = 1; i <= n; i++) {</pre>
```

```
if (h < t && stk[h].first < i) stk[h].first++:</pre>
       if (h + 1 < t \&\& stk[h].first >= stk[h + 1].first) ++h;
        dp[i] = calc(i, stk[h].second);
10
        while (h < t \&\& calc(stk[t - 1].first, stk[t - 1].second) >= calc(stk[t
            - 1].first. i))
11
            --t:
12
       if (h < t) {
13
            int l = stk[t - 1].first, r = n + 1;
14
            while (1 + 1 < r) {
15
                int md = (1 + r) >> 1:
16
                if (calc(md, stk[t - 1].second) < calc(md, i)) l = md; else r =
17
            if (r \le n) stk[t++] = {r, i};
       } else stk[t++] = {i, i}:
20 }
```

4 Geometry

4.1 1 (1).cpp

```
1 typedef double db:
2 const db EPS = 1e-9;
   inline int sign(db a) { return a < -EPS ? -1 : a > EPS; }
   inline int cmp(db a, db b) { return sign(a - b); }
  struct P {
       db x, y;
       P() {}
11
       P(db _x, db _y) : x(_x), y(_y) {}
       P operator+(P p) { return \{x + p.x, y + p.y\}; \}
        P operator-(P p) { return \{x - p.x, y - p.y\}; \}
        P operator*(db d) { return {x * d, y * d}; }
14
15
        P operator/(db d) { return \{x / d, y / d\}; }
16
17
       bool operator<(P p) const {</pre>
18
            int c = cmp(x, p.x):
            if (c) return c == -1;
20
            return cmp(y, p.y) == -1;
21
       }
```

```
22
23
       bool operator == (P o) const {
24
           return cmp(x, o.x) == 0 && cmp(v, o.v) == 0:
25
       }
26
27
       db dot(P p) { return x * p.x + y * p.y; }
28
       db det(P p) { return x * p.y - y * p.x; }
29
30
       db distTo(P p) { return (*this - p).abs(); }
       db alpha() { return atan2(v, x): }
31
32
       void read() { cin >> x >> y; }
        void write() {cout << "(" << x << "," << y << ")" << endl;}</pre>
33
       db abs() { return sgrt(abs2()):}
34
35
       db abs2() { return x * x + y * y; }
       P rot90() { return P(-v. x):}
36
37
       P unit() { return *this / abs(): }
       int quad() const { return sign(y) == 1 \mid | (sign(y) == 0 \&\& sign(x) >= 0)
39
       Prot(db an) { return \{x * \cos(an) - y * \sin(an), x * \sin(an) + y * \cos(an) \}
            an)}: }
40 }:
41
42 #define cross(p1,p2,p3) ((p2,x-p1,x)*(p3,y-p1,y)-(p3,x-p1,x)*(p2,y-p1,y))
43 #define crossOp(p1,p2,p3) sign(cross(p1,p2,p3))
44
45 // 直线 p1p2, q1q2 是否恰有一个交点
46 bool chkLL(P p1, P p2, P q1, P q2) {
       db a1 = cross(q1, q2, p1), a2 = -cross(q1, q2, p2);
47
       return sign(a1 + a2) != 0;
49 }
50
51 // 求直线 p1p2, q1q2 的交点
52 P isLL(P p1, P p2, P q1, P q2) {
       db a1 = cross(q1, q2, p1), a2 = -cross(q1, q2, p2);
54
       return (p1 * a2 + p2 * a1) / (a1 + a2);
55 }
57 // 判断区间 [l1, r1], [l2, r2] 是否相交
58 bool intersect(db 11, db r1, db 12, db r2) {
59
       if (11 > r1) swap(11, r1); if (12 > r2) swap(12, r2);
       return !( cmp(r1, 12) == -1 \mid | cmp(r2, 11) == -1 );
61 }
62
```

```
63 // 线段 p1p2, q1q2 相交
64 bool isSS(P p1, P p2, P q1, P q2) {
        return intersect(p1.x, p2.x, q1.x, q2.x) && intersect(p1.y, p2.y, q1.y,
               crossOp(p1, p2, q1) * crossOp(p1, p2, q2) \le 0 && crossOp(q1, q2, q2)
66
                    p1)
67
               * crossOp(q1, q2, p2) <= 0;
68 }
70 // 线段 p1p2, q1q2 严格相交
71 bool isSS strict(P p1, P p2, P q1, P q2) {
        return crossOp(p1, p2, q1) * crossOp(p1, p2, q2) < 0 && crossOp(q1, q2,
73
               * crossOp(q1, q2, p2) < 0;
74 }
76 // m 在 a 和 b 之间
77 bool isMiddle(db a. db m. db b) {
        /*if (a > b) swap(a, b);
        return cmp(a, m) \le 0 && cmp(m, b) \le 0:*/
79
        return sign(a - m) == 0 \mid \mid sign(b - m) == 0 \mid \mid (a < m != b < m);
81 }
82
83 bool isMiddle(Pa. Pm. Pb) {
        return isMiddle(a.x. m.x. b.x) && isMiddle(a.v. m.v. b.v):
85 }
87 // 点 p 在线段 p1p2 上
88 bool onSeg(P p1, P p2, P q) {
        return crossOp(p1, p2, q) == 0 && isMiddle(p1, q, p2);
90 }
91 // q1q2 和 p1p2 的交点 在 p1p2 上?
93 // 点 p 严格在 p1p2 上
94 bool onSeg_strict(P p1, P p2, P q) {
        return crossOp(p1, p2, q) == 0 && sign((q - p1).dot(p1 - p2)) * sign((q
            - p2).dot(p1 - p2)) < 0;
96 }
98 // 求 q 到 直线 p1p2 的投影 (垂足) : p1 != p2
99 P proj(P p1, P p2, P q) {
100
        P dir = p2 - p1:
        return p1 + dir * (dir.dot(q - p1) / dir.abs2());
```

```
102 }
103
104 // 求 q 以 直线p1p2 为轴的反射
105 P reflect(P p1, P p2, P q) {
106
        return proj(p1, p2, q) * 2 - q;
107 }
108
109 // 求 q 到 线段p1p2 的最小距离
    db nearest(P p1, P p2, P q) {
110
        if (p1 == p2) return p1.distTo(q);
111
        P h = proj(p1, p2, q);
112
113
        if (isMiddle(p1, h, p2))
114
            return q.distTo(h);
115
        return min(p1.distTo(q), p2.distTo(q));
116 }
117
118 // 求 线段p1p2 与 线段q1q2 的距离
119
    db disSS(P p1, P p2, P q1, P q2) {
120
        if (isSS(p1, p2, q1, q2)) return 0;
        return min(min(nearest(p1, p2, q1), nearest(p1, p2, q2)), min(nearest(q1
121
            , q2, p1), nearest(q1, q2, p2)));
122 }
123
124 // 极角排序
125 sort(p, p + n, [&](P a, P b) {
        int qa = a.quad(), qb = b.quad();
126
127
        if (qa != qb) return qa < qb;
128
        else return sign(a.det(b)) > 0;
129 });
    4.2 1 (2).cpp
    db area(vector <P > ps){
```

```
1  db area(vector<P> ps){
2    db ret = 0; rep(i,0,ps.size()) ret += ps[i].det(ps[(i+1)%ps.size()]);
3    return ret/2;
4  }
5    int contain(vector<P> ps, P p){ //2:inside,1:on_seg,0:outside
    int n = ps.size(), ret = 0;
8    rep(i,0,n){
9         P u=ps[i],v=ps[(i+1)%n];
10         if(onSeg(u,v,p)) return 1;
11         if(cmp(u.v,v.v)<=0) swap(u,v);</pre>
```

```
12
            if (cmp(p.y,u.y) > 0 \mid | cmp(p.y,v.y) \le 0) continue;
13
            ret ^= crossOp(p,u,v) > 0;
14
        }
15
        return ret*2;
16 }
17
    vector<P> convexHull(vector<P> ps) {
19
        int n = ps.size(); if(n <= 1) return ps;</pre>
20
        sort(ps.begin(), ps.end());
21
        vectorP> qs(n * 2); int k = 0;
22
        for (int i = 0; i < n; qs[k++] = ps[i++])
23
            while (k > 1 \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) \le 0) --k;
24
        for (int i = n - 2, t = k; i \ge 0; qs[k++] = ps[i--])
25
            while (k > t \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) \le 0) --k;
26
        qs.resize(k - 1);
27
        return qs;
28 }
29
    vector<P> convexHullNonStrict(vector<P> ps) {
31
        //caution: need to unique the Ps first
32
        int n = ps.size(); if(n <= 1) return ps;</pre>
33
        sort(ps.begin(), ps.end());
34
        vectorP> qs(n * 2); int k = 0;
35
        for (int i = 0; i < n; qs[k++] = ps[i++])
36
            while (k > 1 \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) < 0) --k;
37
        for (int i = n - 2, t = k; i \ge 0; qs[k++] = ps[i--])
38
            while (k > t \&\& crossOp(qs[k-2], qs[k-1], ps[i]) < 0) --k;
39
        qs.resize(k - 1);
40
        return qs;
41 }
42
   db convexDiameter(vector < P > ps) {
44
        int n = ps.size(); if (n \le 1) return 0;
45
        int is = 0, js = 0; rep(k,1,n) is = ps[k] < ps[is]?k:is, js = ps[js] < ps[is]
            k]?k:js;
46
        int i = is, j = js;
47
        db ret = ps[i].distTo(ps[j]);
48
        do{
49
            if((ps[(i+1)\%n]-ps[i]).det(ps[(j+1)\%n]-ps[j]) >= 0)
50
                 (++j)%=n;
51
            else
52
                (++i)%=n:
53
            ret = max(ret,ps[i].distTo(ps[j]));
```

```
54
        }while(i!=is || j!=js);
55
        return ret;
56 }
57
    vector<P> convexCut(const vector<P>&ps, P q1, P q2) {
        vector<P> qs;
59
        int n = ps.size();
60
        rep(i.0.n){
61
62
            P p1 = ps[i], p2 = ps[(i+1)%n];
            int d1 = crossOp(q1,q2,p1), d2 = crossOp(q1,q2,p2);
63
64
            if (d1 >= 0) qs.push back(p1);
            if (d1 * d2 < 0) qs.push back(isLL(p1,p2,q1,q2));
65
        }
66
67
        return qs;
68 }
69
    void reorderPolygon(vector<P> &ps) {
71
        size t pos = 0:
72
        for(size_t i = 1; i < ps.size(); i++){</pre>
            if(ps[i].y < ps[pos].y \mid | (ps[i].y == ps[pos].y && ps[i].x < ps[pos]
73
                1.x))
74
                pos = i;
75
        }
76
        rotate(ps.begin(), ps.begin() + pos, ps.end());
77 }
78
    vector<P> minkowski(vector<P> p, vector<P> q){
        if(p.empty()) return q;
80
81
        // the first vertex must be the lowest
82
        reorderPolygon(p);
83
        reorderPolygon(q);
84
        // must ensure cyclic indexing
        p.push back(p[0]);
85
86
        p.push_back(p[1]);
87
        q.push_back(q[0]);
88
        q.push_back(q[1]);
        // main part
89
90
        vector<P> result;
91
        size_t i = 0, j = 0;
92
        while(i < p.size() - 2 || j < q.size() - 2){</pre>
93
            result.push_back(p[i] + q[j]);
94
            auto cross = (p[i + 1] - p[i]).det(q[j + 1] - q[j]);
95
            if(cross \geq = 0 \&\& i < SZ(p) - 2)
```

```
96
                  ++i:
 97
             if (cross \leq 0 \&\& j \leq SZ(q) - 2)
                  ++i:
 98
 99
         }
100
         return result:
101 }
102
     bool convexContain(const vector<P> &l. P p. bool strict = true) {
         int a = 1, b = l.size() - 1, r = !strict;
104
105
         if (1.size() < 3) return r && onSeg(1[0], 1.back(), p);
106
         if (crossOp(1[0], 1[a], 1[b]) > 0) swap(a, b);
107
         if (cross0p(1[0], 1[a], p) >= r || cross0p(1[0], 1[b], p) <= -r)
108
             return false:
109
         while (abs(a - b) > 1) {
110
             int c = (a + b) / 2:
1111
             (crossOp(1[0], 1[c], p) > 0 ? b : a) = c;
112
113
         return sign(cross(l[a], l[b], p)) < r;</pre>
1114 }
```

4.3 1 (3).cpp

```
1 int type(P o1,db r1,P o2,db r2){
       db d = o1.distTo(o2);
       if(cmp(d,r1+r2) == 1) return 4;
       if(cmp(d,r1+r2) == 0) return 3;
       if(cmp(d,abs(r1-r2)) == 1) return 2;
6
       if(cmp(d,abs(r1-r2)) == 0) return 1;
7
       return 0;
8 }
   vector<P> isCL(P o,db r,P p1,P p2){
11
       if (cmp(abs((o-p1).det(p2-p1)/p1.distTo(p2)),r)>0) return {};
12
       db x = (p1-o).dot(p2-p1), y = (p2-p1).abs2(), d = x * x - y * ((p1-o).
           abs2() - r*r):
       d = max(d,(db)0.0); P m = p1 - (p2-p1)*(x/y), dr = (p2-p1)*(sqrt(d)/y);
       return {m-dr,m+dr}; //along dir: p1->p2
14
15 }
16
17 vector <P isCC(P o1, db r1, P o2, db r2) { //need to check whether two
        circles are the same
18
       db d = o1.distTo(o2);
19
       if (cmp(d, r1 + r2) == 1) return {}:
```

```
20
        if (cmp(d,abs(r1-r2))==-1) return {};
21
        d = min(d, r1 + r2);
        db y = (r1 * r1 + d * d - r2 * r2) / (2 * d), x = sqrt(r1 * r1 - y * y);
22
23
        P dr = (o2 - o1).unit();
        P q1 = o1 + dr * y, q2 = dr.rot90() * x;
24
        return {q1-q2,q1+q2}; //along circle 1
25
26 }
27
    // extanCC, intanCC : -r2, tanCP : r2 = 0
    vector<pair<P, P>> tanCC(P o1, db r1, P o2, db r2) {
        P d = o2 - o1;
30
        db dr = r1 - r2, d2 = d.abs2(), h2 = d2 - dr * dr;
31
        if (sign(d2) == 0|| sign(h2) < 0) return {};</pre>
32
33
        h2 = max((db)0.0, h2);
       vector<pair<P, P>> ret;
34
35
        for (db sign : {-1, 1}) {
            P v = (d * dr + d.rot90() * sqrt(h2) * sign) / d2;
36
37
            ret.push_back(\{01 + v * r1, 02 + v * r2\});
38
       }
        if (sign(h2) == 0) ret.pop_back();
39
40
        return ret;
41 }
42
    db rad(P p1,P p2){
        return atan21(p1.det(p2),p1.dot(p2));
44
45 }
46
   db areaCT(db r, P p1, P p2){
48
        vector\langle P \rangle is = isCL(P(0,0),r,p1,p2);
        if(is.empty()) return r*r*rad(p1,p2)/2;
49
50
        bool b1 = cmp(p1.abs2(),r*r) == 1, b2 = cmp(p2.abs2(),r*r) == 1;
51
        if(b1 && b2){
            P md=(is[0]+is[1])/2:
52
53
            if(sign((p1-md).dot(p2-md)) <= 0)
                return r*r*(rad(p1,is[0]) + rad(is[1],p2))/2 + is[0].det(is[1])
54
            else return r*r*rad(p1,p2)/2;
55
       }
56
57
        if(b1) return (r*r*rad(p1,is[0]) + is[0].det(p2))/2;
        if(b2) return (p1.det(is[1]) + r*r*rad(is[1],p2))/2;
58
        return p1.det(p2)/2;
59
60 }
61
```

```
62 PinCenter(PA. PB. PC) {
63
        double a = (B - C).abs(), b = (C - A).abs(), c = (A - B).abs();
        return (A * a + B * b + C * c) / (a + b + c):
64
65 }
66
67 P circumCenter(P a. P b. P c) {
        P bb = b - a, cc = c - a;
        double db = bb.abs2(), dc = cc.abs2(), d = 2 * bb.det(cc);
70
        return a - P(bb.v * dc - cc.v * db, cc.x * db - bb.x * dc) / d;
71 }
72
73 P othroCenter(P a, P b, P c) {
       P ba = b - a, ca = c - a, bc = b - c:
75
       double Y = ba.v * ca.v * bc.v,
76
       A = ca.x * ba.y - ba.x * ca.y,
        x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
       y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
        return {x0, y0};
80 }
81
   pair < P, db > min_circle(vector < P > ps) {
        random_shuffle(ps.begin(), ps.end());
84
       int n = ps.size();
       P \circ = ps[0]; db r = 0;
       rep(i,1,n) if (o.distTo(ps[i]) > r + EPS){
87
            o = ps[i], r = 0;
            rep(j,0,i) if (o.distTo(ps[j]) > r + EPS){
                o = (ps[i] + ps[j]) / 2; r = o.distTo(ps[i]);
90
                rep(k,0,j) if (o.distTo(ps[k]) > r + EPS){
91
                     o = circumCenter(ps[i],ps[j],ps[k]);
92
                     r = o.distTo(ps[i]);
               }
94
           }
95
       }
96
        return {o,r};
97 }
```

4.4 all.cpp

```
1 typedef double db;
2 const db EPS = 1e-9;
3
4 inline int sign(db a) { return a < -EPS ? -1 : a > EPS; }
```

```
5
6 inline int cmp(db a, db b){ return sign(a-b); }
   struct P {
        db x, y;
        P() {}
10
        P(db x, db y) : x(x), y(y) {}
11
12
        P operator+(P p) { return \{x + p.x, y + p.y\}; \}
       P operator-(P p) { return {x - p.x, y - p.y}; }
13
        P operator*(db d) { return \{x * d, v * d\}: }
14
15
        P operator/(db d) { return \{x / d, y / d\}; }
16
17
        bool operator<(P p) const {</pre>
18
            int c = cmp(x, p.x);
19
            if (c) return c == -1:
            return cmp(v, p.v) == -1;
20
       }
21
22
23
        bool operator == (P o) const{
            return cmp(x,o.x) == 0 && cmp(y,o.y) == 0;
24
       }
25
26
27
        db dot(P p) { return x * p.x + v * p.v: }
        db det(P p) { return x * p.y - y * p.x; }
28
29
        db distTo(P p) { return (*this-p).abs(); }
30
        db alpha() { return atan2(y, x); }
31
        void read() { cin>>x>>y; }
32
33
        void write() {cout<<"("<<x<<","<<y<")"<<endl;}</pre>
        db abs() { return sgrt(abs2());}
34
        db abs2() { return x * x + y * y; }
35
36
        P rot90() { return P(-y,x);}
        P unit() { return *this/abs(): }
37
        int quad() const { return sign(y) == 1 \mid | (sign(y) == 0 \&\& sign(x) >= 0)
38
39
        P rot(db an) { return \{x*\cos(an)-y*\sin(an),x*\sin(an) + y*\cos(an)\}; }
40 }:
41
42 struct L{ //ps[0] -> ps[1]
       P ps[2];
43
        P& operator[](int i) { return ps[i]; }
44
45
       P dir() { return ps[1] - ps[0]; }
        bool include(P p) { return sign((ps[1] - ps[0]).det(p - ps[0])) > 0; }
```

```
47
       L push(){ // push eps outward
48
            const double eps = 1e-6;
49
            P delta = (ps[1] - ps[0]).rot90().unit() * eps;
50
            return {{ps[0] - delta, ps[1] - delta}};
51
       }
52 };
   #define cross(p1,p2,p3) ((p2.x-p1.x)*(p3.y-p1.y)-(p3.x-p1.x)*(p2.y-p1.y))
    #define crossOp(p1,p2,p3) sign(cross(p1,p2,p3))
56
   bool chkLL(P p1, P p2, P q1, P q2) {
        db a1 = cross(q1, q2, p1), a2 = -cross(q1, q2, p2);
       return sign(a1+a2) != 0:
60 }
61
62 P isLL(P p1, P p2, P q1, P q2) {
        db a1 = cross(q1, q2, p1), a2 = -cross(q1, q2, p2);
        return (p1 * a2 + p2 * a1) / (a1 + a2):
65 }
  P isLL(L 11,L 12) { return isLL(11[0],11[1],12[0],12[1]); }
69 bool intersect(db 11.db r1.db 12.db r2){
70
       if(l1>r1) swap(l1,r1); if(l2>r2) swap(l2,r2);
71
        return !( cmp(r1.12) == -1 \mid | cmp(r2.11) == -1 );
72 }
73
74 bool isSS(P p1, P p2, P q1, P q2){
        return intersect(p1.x,p2.x,q1.x,q2.x) && intersect(p1.y,p2.y,q1.y,q2.y)
76
        crossOp(p1,p2,q1) * crossOp(p1,p2,q2) \le 0 \&\& crossOp(q1,q2,p1)
77
                * crossOp(q1,q2,p2) <= 0;
78 }
79
   bool isSS_strict(P p1, P p2, P q1, P q2){
81
        return crossOp(p1,p2,q1) * crossOp(p1,p2,q2) < 0 && crossOp(q1,q2,p1)
82
                * crossOp(q1,q2,p2) < 0;
83 }
85 bool isMiddle(db a, db m, db b) {
        return sign(a - m) == 0 \mid \mid sign(b - m) == 0 \mid \mid (a < m != b < m);
87 }
88
```

```
bool isMiddle(P a. P m. P b) {
         return isMiddle(a.x, m.x, b.x) && isMiddle(a.v, m.v, b.v);
 90
 91 }
 92
    bool onSeg(P p1, P p2, P q){
 94
         return crossOp(p1,p2,q) == 0 && isMiddle(p1, q, p2);
 95 }
    bool onSeg strict(P p1, P p2, P q){
 97
 98
         return crossOp(p1,p2,q) == 0 && sign((q-p1).dot(p1-p2)) * sign((q-p2).
             dot(p1-p2)) < 0;
99 }
100
101 P proj(P p1, P p2, P q) {
        P dir = p2 - p1;
102
         return p1 + dir * (dir.dot(q - p1) / dir.abs2());
103
104 }
105
106 P reflect(P p1, P p2, P q){
         return proj(p1,p2,q) * 2 - q;
107
108 }
109
110 db nearest(P p1,P p2,P q){
111
        P h = proj(p1,p2,q);
112
        if(isMiddle(p1,h,p2))
113
             return q.distTo(h);
         return min(p1.distTo(q),p2.distTo(q));
114
115 }
116
117 db disSS(P p1, P p2, P q1, P q2){
118
         if(isSS(p1,p2,q1,q2)) return 0;
119
         return min(min(nearest(p1,p2,q1),nearest(p1,p2,q2)), min(nearest(q1,q2,
             p1), nearest(q1,q2,p2)));
120 }
121
122 db rad(P p1,P p2){
         return atan21(p1.det(p2),p1.dot(p2));
123
124 }
125
126 db incircle(P p1, P p2, P p3){
         db A = p1.distTo(p2);
127
         db B = p2.distTo(p3);
128
129
         db C = p3.distTo(p1);
```

```
130
         return sqrtl(A*B*C/(A+B+C));
131 }
132
133 //polygon
134
135
     db area(vector <P> ps){
136
         db ret = 0; rep(i,0,ps.size()) ret += ps[i].det(ps[(i+1)\%ps.size()]);
137
         return ret/2:
138 }
139
     int contain(vector < P > ps, P p) { //2: inside, 1: on seq, 0: outside
141
         int n = ps.size(), ret = 0;
142
         rep(i.0.n){
143
             P = u = ps[i], v = ps[(i+1)%n];
144
             if(onSeg(u,v,p)) return 1;
145
             if (cmp(u.y,v.y) \le 0) swap(u,v);
146
             if (cmp(p.y,u.y) > 0 \mid | cmp(p.y,v.y) \le 0) continue;
147
             ret ^= crossOp(p.u.v) > 0:
148
         }
149
         return ret*2:
150 }
151
    vector<P> convexHull(vector<P> ps) {
153
         int n = ps.size(); if(n <= 1) return ps;</pre>
154
         sort(ps.begin(), ps.end());
155
         vector\langle P \rangle qs(n * 2); int k = 0;
156
         for (int i = 0; i < n; qs[k++] = ps[i++])
157
             while (k > 1 \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) \le 0) --k;
158
         for (int i = n - 2, t = k; i \ge 0; qs[k++] = ps[i--])
159
             while (k > t \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) \le 0) --k;
160
         qs.resize(k - 1);
161
         return qs;
162 }
163
164
     vector<P> convexHullNonStrict(vector<P> ps) {
165
         //caution: need to unique the Ps first
166
         int n = ps.size(); if(n <= 1) return ps;</pre>
167
         sort(ps.begin(), ps.end());
168
         vectorP> qs(n * 2); int k = 0;
169
         for (int i = 0; i < n; qs[k++] = ps[i++])
170
             while (k > 1 \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) < 0) --k;
171
         for (int i = n - 2, t = k; i \ge 0; qs[k++] = ps[i--])
172
             while (k > t \&\& crossOp(qs[k - 2], qs[k - 1], ps[i]) < 0) --k;
```

```
173
                         qs.resize(k - 1);
174
                          return qs;
175 }
176
177 db convexDiameter(vector < P > ps) {
                         int n = ps.size(); if(n <= 1) return 0;</pre>
178
                          int is = 0, js = 0; rep(k,1,n) is = ps[k] < ps[is] ?k:is, js = ps[js] < ps[is] > ps[i
179
                                     kl?k:is:
180
                         int i = is, j = js;
                         db ret = ps[i].distTo(ps[j]);
181
182
                         do{
                                    if((ps[(i+1)\%n]-ps[i]).det(ps[(i+1)\%n]-ps[i]) >= 0)
183
                                                 (++i)%=n:
184
185
                                     else
                                                 (++i)%=n:
186
187
                                     ret = max(ret,ps[i].distTo(ps[j]));
                         }while(i!=is || j!=js);
188
189
                         return ret:
190 }
191
192
               vector<P> convexCut(const vector<P>&ps, P q1, P q2) {
                          vector<P> as:
193
                         int n = ps.size();
194
195
                         rep(i,0,n){
                                    P p1 = ps[i], p2 = ps[(i+1)%n];
196
197
                                     int d1 = crossOp(q1,q2,p1), d2 = crossOp(q1,q2,p2);
                                    if(d1 >= 0) qs.pb(p1);
198
                                    if(d1 * d2 < 0) qs.pb(isLL(p1,p2,q1,q2));
199
200
                         }
201
                         return as:
202 }
203
204 //min dist
205
               db min_dist(vector < P > & ps, int 1, int r) {
206
207
                         if(r-1<=5){
                                     db ret = 1e100:
208
                                     rep(i,l,r) rep(j,l,i) ret = min(ret,ps[i].distTo(ps[j]));
209
210
                                     return ret:
211
                         }
                         int m = (l+r) >> 1;
212
                         db ret = min(min_dist(ps,1,m),min_dist(ps,m,r));
213
214
                          vector < P > qs; rep(i,l,r) if(abs(ps[i].x-ps[m].x) <= ret) qs.pb(ps[i]);
```

```
215
         sort(qs.begin(), qs.end(),[](P a,P b) -> bool {return a.y<b.y; });</pre>
216
         rep(i,1,qs.size()) for(int j=i-1;j>=0&&qs[j].y>=qs[i].y-ret;--j)
217
             ret = min(ret,qs[i].distTo(qs[j]));
218
         return ret;
219 }
220
221
     int type(P o1,db r1,P o2,db r2){
222
         db d = o1.distTo(o2):
223
        if(cmp(d,r1+r2) == 1) return 4;
224
        if(cmp(d,r1+r2) == 0) return 3;
225
        if(cmp(d,abs(r1-r2)) == 1) return 2;
226
         if(cmp(d,abs(r1-r2)) == 0) return 1;
227
         return 0:
228 }
229
230
    vector<P> isCL(P o,db r,P p1,P p2){
         db x = (p1-o).dot(p2-p1), y = (p2-p1).abs2(), d = x * x - y * ((p1-o).
231
             abs2() - r*r):
232
        if(sign(d) < 0) return {};</pre>
233
         d = max(d,0.0); P = p1 - (p2-p1)*(x/y), dr = (p2-p1)*(sqrt(d)/y);
234
         return \{m-dr, m+dr\}; //along dir: p1->p2
235 }
236
237 vector <P isCC(P o1, db r1, P o2, db r2) { //need to check whether two
         circles are the same
238
         db d = o1.distTo(o2);
         if (cmp(d, r1 + r2) == 1) return {};
240
         d = min(d, r1 + r2);
241
         db y = (r1 * r1 + d * d - r2 * r2) / (2 * d), x = sqrt(r1 * r1 - y * y);
        P dr = (o2 - o1).unit():
243
        P q1 = o1 + dr * v, q2 = dr.rot90() * x;
244
         return {q1-q2,q1+q2}; //along circle 1
245 }
246
247 vector<P> tanCP(P o, db r, P p) {
248
         db x = (p - o).abs2(), d = x - r * r;
249
         if (sign(d) <= 0) return {}; // on circle => no tangent
250
        P q1 = o + (p - o) * (r * r / x);
251
        P q2 = (p - o).rot90() * (r * sqrt(d) / x);
252
         return {q1-q2,q1+q2}; //counter clock-wise
253 }
254
255
```

```
vector<L> extanCC(P o1, db r1, P o2, db r2) {
257
         vector<L> ret;
         if (cmp(r1, r2) == 0) {
258
259
             P dr = (o2 - o1).unit().rot90() * r1;
             ret.pb({{o1 + dr. o2 + dr}}), ret.pb({{o1 - dr. o2 - dr}});
260
        } else {
261
             P p = (o2 * r1 - o1 * r2) / (r1 - r2);
262
             vector < P > ps = tanCP(o1, r1, p), qs = tanCP(o2, r2, p):
263
             rep(i,0,min(ps.size(),qs.size())) ret.pb({{ps[i], qs[i]}}); //c1
264
                 counter-clock wise
        }
265
         return ret;
266
267 }
268
     vector<L> intanCC(P o1, db r1, P o2, db r2) {
269
270
         vector<L> ret;
271
         P p = (o1 * r2 + o2 * r1) / (r1 + r2);
         vector\langle P \rangle ps = tanCP(o1,r1,p), qs = tanCP(o2,r2,p);
         rep(i,0,min(ps.size(),qs.size())) ret.pb({{ps[i], qs[i]}}); //c1 counter
273
             -clock wise
274
         return ret;
275 }
276
    db areaCT(db r, P p1, P p2){
277
278
         vector < P > is = isCL(P(0.0).r.p1.p2):
         if(is.empty()) return r*r*rad(p1,p2)/2;
279
         bool b1 = cmp(p1.abs2(),r*r) == 1, b2 = cmp(p2.abs2(),r*r) == 1;
280
         if(b1 && b2){
281
282
             if(sign((p1-is[0]).dot(p2-is[0])) <= 0 &&
                 sign((p1-is[0]).dot(p2-is[0])) \le 0)
283
             return r*r*(rad(p1,is[0]) + rad(is[1],p2))/2 + is[0].det(is[1])/2;
284
285
             else return r*r*rad(p1,p2)/2;
        }
286
         if(b1) return (r*r*rad(p1,is[0]) + is[0].det(p2))/2;
287
288
         if(b2) return (p1.det(is[1]) + r*r*rad(is[1],p2))/2;
289
         return p1.det(p2)/2;
290 }
291
292
     bool parallel(L 10, L 11) { return sign( 10.dir().det( 11.dir() ) ) == 0; }
293
    bool sameDir(L 10, L 11) { return parallel(10, 11) && sign(10.dir().dot(11.
         dir()) ) == 1: }
295
```

```
296 bool cmp (Pa. Pb) {
297
         if (a.quad() != b.quad()) {
298
             return a.quad() < b.quad();</pre>
299
        } else {
300
             return sign(a.det(b)) > 0:
301
        }
302 }
303
304
    bool operator < (L 10, L 11) {
305
         if (sameDir(10, 11)) {
306
             return 11.include(10[0]);
307
        } else {
308
             return cmp( 10.dir(), 11.dir() ):
309
        }
310 }
311
312 bool check(L u, L v, L w) {
313
         return w.include(isLL(u.v)):
314 }
315
316
     vector<P> halfPlaneIS(vector<L> &1) {
317
         sort(l.begin(), l.end());
318
         deaue<L> a:
319
         for (int i = 0; i < (int)1.size(); ++i) {
320
             if (i && sameDir(l[i], l[i - 1])) continue:
321
             while (q.size() > 1 && !check(q[q.size() - 2], q[q.size() - 1], 1[i]
                 ])) q.pop_back();
322
             while (q.size() > 1 && !check(q[1], q[0], l[i])) q.pop_front();
323
             q.push_back(l[i]);
324
325
         while (q.size() > 2 && !check(q[q.size() - 2], q[q.size() - 1], q[0])) q
             .pop_back();
         while (q.size() > 2 \&\& !check(q[1], q[0], q[q.size() - 1])) q.pop_front
326
             ();
327
         vector<P> ret:
328
         for (int i = 0; i < (int)q.size(); ++i) ret.push back(isLL(q[i], q[(i +
             1) % q.size()]));
329
         return ret;
330 }
331
332 PinCenter(PA, PB, PC) {
333
         double a = (B - C).abs(), b = (C - A).abs(), c = (A - B).abs();
334
         return (A * a + B * b + C * c) / (a + b + c);
```

```
335 }
336
337 P circumCenter(P a. P b. P c) {
338
        P bb = b - a, cc = c - a;
        double db = bb.abs2(), dc = cc.abs2(), d = 2 * bb.det(cc);
339
        return a - P(bb.y * dc - cc.y * db, cc.x * db - bb.x * dc) / d;
340
341 }
342
343 P othroCenter(P a, P b, P c) {
        P ba = b - a, ca = c - a, bc = b - c;
344
        double Y = ba.y * ca.y * bc.y,
345
346
        A = ca.x * ba.y - ba.x * ca.y
        x0 = (Y + ca.x * ba.y * b.x - ba.x * ca.y * c.x) / A,
347
348
        y0 = -ba.x * (x0 - c.x) / ba.y + ca.y;
        return {x0, y0};
349
350 }
```

4.5 圆面积并.cpp

```
db intergal(db x,db y,db r,db L,db R){
        return r*r*(R-L) + x*r*(sinl(R) - sinl(L)) + y*r*(-cosl(R) + cosl(L));
3 }
4
   db calc area circle(P c,db r,db L,db R){
        return intergal(c.x,c.y,r,L,R) / 2;
7 }
   db norm(db x){
10
       while(x < 0) x += 2 * PI;
       while(x > 2 * PI) x -= 2 * PI:
11
       return x:
13 }
14
15 P cs[N]; db rs[N];
17
   void work(){
18
       vector<int> cand = {};
19
       rep(i,0,m){
20
           bool ok = 1;
           rep(j,0,m) if(i!=j){
21
                if(rs[j] > rs[i] + EPS && rs[i] + cs[i].distTo(cs[j]) \le rs[j] +
22
                     EPS){
                    ok = 0: break:
23
```

```
24
                }
25
                if(cs[i] == cs[j] \&\& cmp(rs[i],rs[j]) == 0 \&\& j < i){
                     ok = 0: break:
26
27
                }
            }
28
29
            if(ok) cand.pb(i);
30
        }
31
32
        rep(i,0,cand.size()) cs[i] = cs[cand[i]], rs[i] = rs[cand[i]];
        m = cand.size():
33
34
35
        db area = 0;
36
37
        //work
38
        rep(i,0,m){
39
            vector<pair<db,int>> ev = {{0,0},{2*PI,0}};
40
41
            int cur = 0:
42
43
            rep(j,0,m) if(j!=i){
                auto ret = isCC(cs[i],rs[i],cs[j],rs[j]);
44
45
                if(!ret.emptv()){
                    db 1 = (ret[0] - cs[i]).alpha();
46
                    db r = (ret[1] - cs[i]).alpha();
47
48
                    l = norm(1): r = norm(r):
                    ev.pb({1,1}); ev.pb({r,-1});
49
                    if(1 > r) ++cur:
51
                }
52
            }
53
54
            sort(ev.begin(), ev.end());
            rep(j,0,ev.size() - 1){
56
                cur += ev[j].se;
57
                if(cur == 0){
                     area += calc_area_circle(cs[i],rs[i],ev[j].fi,ev[j+1].fi);
61
        }
62 }
```

5 Graph

5.1 bellmanford.cpp

```
1 vector<PII> e[N];
   template <typename T>
   void add(int u, int v, T w) {
        e[u].eb(v, w);
6 }
   template <typename T>
    vector<T> bellmanford(vector<pair<int, T>> *g, int start) {
10
        // assert(0 <= start && start < q.n);
11
        // maybe use inf = numeric limits<T>::max() / 4
        const T inf = numeric limits<T>::max() / 4;
12
13
        vector<T> dist(n, inf);
14
        dist[start] = 0;
        int cnt = 0;
15
16
        while (true) {
17
            bool upd = 0;
            cnt++:
18
            for (int i = 0; i < n; i++) {
19
                for (auto [to, cost] : e[i]) {
20
                    if (dist[to] > dist[i] + cost) {
21
                        upd = 1;
                        dist[to] = dist[i] + cost;
23
24
                    }
                }
25
26
            if (!upd || cnt == n) {
27
28
                break:
29
            }
       }
30
31
        return dist:
        // returns inf if there's no path
33 }
```

5.2 BlockCutTree.cpp

```
1 struct BlockCutTree {
2   int n;
3   std::vector<std::vector<int>> adj;
```

```
std::vector<int> dfn, low, stk;
5
        int cnt, cur;
6
        std::vector<std::pair<int, int>> edges;
7
8
        BlockCutTree() {}
        BlockCutTree(int n) {
9
10
            init(n);
11
        }
12
13
        void init(int n) {
14
            this -> n = n;
15
            adj.assign(n, {});
            dfn.assign(n, -1);
16
17
            low.resize(n);
18
            stk.clear();
            cnt = cur = 0;
19
20
            edges.clear();
21
22
23
        void addEdge(int u, int v) {
24
            adj[u].push_back(v);
25
            adj[v].push_back(u);
26
        }
27
28
        void dfs(int x) {
29
            stk.push_back(x);
30
            dfn[x] = low[x] = cur++;
31
32
            for (auto y : adj[x]) {
33
                if (dfn[y] == -1) {
34
                    dfs(v);
35
                    low[x] = std::min(low[x], low[y]);
                    if (low[y] == dfn[x]) {
36
37
                        int v;
38
                        do {
39
                             v = stk.back();
40
                             stk.pop_back();
41
                             edges.emplace_back(n + cnt, v);
42
                        } while (v != y);
43
                         edges.emplace_back(x, n + cnt);
44
                         cnt++;
                    }
45
46
                } else {
```

```
low[x] = std::min(low[x], dfn[y]);
47
                }
48
49
            }
50
       }
51
52
        std::pair<int, std::vector<std::pair<int, int>>> work() {
            for (int i = 0; i < n; i++) {
53
                if (dfn[i] == -1) {
54
55
                    stk.clear();
                    dfs(i):
56
57
                }
            }
58
            return {cnt, edges};
59
60
       }
61 };
```

5.3 boruvka.cpp

```
* while component > 1:
           for each component:
               find select[i]
           for each component:
                if select[i] != i:
                    merge(i, select[i])
                    component --
   11 \text{ ans} = 0, \text{ cnt} = n;
    while (cnt > 1) {
13
        fill(select + 1, select + n + 1, -1);
14
        vector<int> cand;
15
        for (int i = 1; i <= n; i++) {
16
            cand.push_back(col[i]);
        }
17
18
        ranges::sort(cand);
19
        cand.erase(unique(all(cand)), cand.end());
20
        for (auto id : cand) {
21
22
            for (auto x : S[id]) remove(x):
            for (auto x : S[id]) {
23
24
                 auto [opt, w] = get(x);
25
                if (select[id] == -1 || w < mn[id]) {
```

```
26
                    select[id] = opt, mn[id] = w;
27
                }
28
            }
29
            for (auto x : S[id]) insert(x);
       }
30
31
32
        for (int i = 1; i <= n; i++) if (col[i] == i) {
            int j = col[select[i]];
34
            if (i == j) continue;
35
            ans += mn[i]:
36
            merge(i, j);
37
            cnt--;
       }
39 }
```

5.4 dijfast.cpp

```
1 vector < PII > e[N]:
   template <typename T>
   void add(int u, int v, T w) {
5
        e[u].eb(v, w);
6 }
   template <typename T>
   vector<T> dijkstra(vector<pair<int, T>> *g, int start) {
        // assert(0 <= start && start < q.n);
11
        // maybe use inf = numeric limits <T>::max() / 4
12
        vector<T> dist(n, numeric_limits<T>::max());
13
        priority_queue<pair<T, int>, vector<pair<T, int>>, greater<pair<T, int</pre>
            >>> s:
14
        dist[start] = 0;
        s.emplace(dist[start], start);
15
        while (!s.empty()) {
16
17
            T expected = s.top().first;
            int i = s.top().second;
18
19
            s.pop();
            if (dist[i] != expected) {
20
21
                continue;
22
            }
23
            for (auto [to, cost] : g[i]) {
24
                if (dist[i] + cost < dist[to]) {</pre>
25
                    dist[to] = dist[i] + cost:
```

5.5 dijkstra.cpp

```
vector<PII> e[N];
3 template <typename T>
   void add(int u, int v, T w) {
       e[u].eb(v, w);
   template <typename T>
   vector<T> dijkstra(vector<pair<int, T>> *g, int start) {
       // assert(0 <= start && start < q.n);
       // maybe use inf = numeric limits<T>::max() / 4
11
12
       const T inf = numeric limits<T>::max();
13
       vector<T> dist(n, inf);
14
       vector<int> was(n, 0);
       dist[start] = 0;
15
        while (true) {
16
17
            int cur = -1;
            for (int i = 0; i < n; i++) {
18
19
                if (was[i] || dist[i] == inf) continue;
                if (cur == -1 || dist[i] < dist[cur]) {</pre>
21
                    cur = i:
22
               }
            }
23
24
            if (cur == -1 || dist[cur] == inf) {
                break:
25
            }
26
27
            was[cur] = 1;
            for (auto [to, cost] : g[cur]) {
28
                dist[to] = min(dist[to], dist[cur] + cost);
29
30
            }
31
       }
32
       return dist;
33
        // returns inf if there's no path
```

5.6 dinic.cpp

34 }

```
1 template < typename T >
2 struct FlowGraph {
3
        static const int V = 1015;
        static const int E = 100015;
       int s, t, vtot;
        int head[V], etot;
       int dis[V], cur[V];
        struct edge {
9
            int v, nxt;
10
            T f:
11
       } e[E * 2];
12
        void addedge(int u, int v, T f) {
13
            e[etot] = {v, head[u], f};
            head[u] = etot++;
14
15
            e[etot] = {u, head[v], 0};
            head[v] = etot++;
16
17
       }
       bool bfs() {
18
19
            for (int i = 1; i <= vtot; i++) {
20
                dis[i] = 0;
21
                cur[i] = head[i];
22
            }
23
            queue < int > q;
24
            q.push(s); dis[s] = 1;
25
            while (!q.empty()) {
26
                int u = q.front(); q.pop();
27
                for (int i = head[u]; i != -1; i = e[i].nxt) {
28
                    if (e[i].f && !dis[e[i].v]) {
                        int v = e[i].v:
29
30
                        dis[v] = dis[u] + 1;
31
                        if (v == t) return true:
32
                        q.push(v);
33
                    }
                }
34
35
            }
36
            return false:
37
       }
38
       T dfs(int u, T m) {
39
            if (u == t) return m:
```

```
40
            T flow = 0:
            for (int i = cur[u]; i != -1; cur[u] = i = e[i].nxt) {
41
                if (e[i].f && dis[e[i].v] == dis[u] + 1) {
43
                    T f = dfs(e[i].v, min(m, e[i].f));
                    e[i].f -= f:
44
                    e[i ^1].f += f;
45
                    m -= f;
                    flow += f:
47
                    if (!m) break;
               }
50
            if (!flow) dis[u] = -1;
51
            return flow:
52
53
       }
54
       T dinic() {
55
            T flow = 0;
            while (bfs()) flow += dfs(s, numeric limits<T>::max());
57
            return flow:
58
       }
        void init(int _s, int _t, int _vtot) {
59
60
            s = _s;
61
            t = _t;
            vtot = _vtot;
63
            etot = 0;
64
            for (int i = 1: i <= vtot: i++) head[i] = -1:
       }
65
66 };
```

5.7 dinic-tourist.cpp

```
1 template <typename T>
2 class flow_graph {
3   public:
4   static constexpr T eps = (T)1e-9;
5
6   struct edge {
7    int from;
8   int to;
9   T c;
10   T f;
11   };
12
13   vector<vector<int>> g;
```

```
14
     vector<edge> edges;
     int n;
16
     int st:
17
     int fin;
18
     T flow:
19
20
     flow graph(int n, int st, int fin): n(n), st(st), fin(fin) {
21
       assert(0 <= st && st < n && 0 <= fin && fin < n && st != fin):
22
       g.resize(n);
23
       flow = 0:
24
     }
25
26
     void clear flow() {
27
       for (const edge &e : edges) {
28
         e.f = 0:
29
       }
30
       flow = 0;
31
32
     int add(int from, int to, T forward_cap, T backward_cap) {
33
34
       assert(0 <= from && from < n && 0 <= to && to < n);
35
       int id = (int)edges.size();
       g[from].push_back(id);
37
       edges.push_back({from, to, forward_cap, 0});
       g[to].push_back(id + 1);
       edges.push_back({to, from, backward_cap, 0});
       return id:
41
     }
42 };
43
44 template <typename T>
   class dinic {
    public:
47
     flow_graph<T> &g;
48
49
     vector<int> ptr;
     vector<int> d;
51
     vector<int> q;
52
53
     dinic(flow_graph<T> &_g) : g(_g) {
54
       ptr.resize(g.n);
       d.resize(g.n);
       q.resize(g.n);
```

```
}
57
58
      bool expath() {
59
60
       fill(d.begin(), d.end(), -1);
       q[0] = g.fin;
61
       d[g.fin] = 0;
62
        int beg = 0, end = 1;
        while (beg < end) {
64
         int i = q[beg++];
65
         for (int id : g.g[i]) {
66
67
            const auto &e = g.edges[id];
            const auto &back = g.edges[id ^ 1];
            if (back.c - back.f > g.eps && d[e.to] == -1) {
69
70
              d[e.to] = d[i] + 1;
71
              if (e.to == g.st) {
72
                return true;
73
74
              q[end++] = e.to;
75
         }
76
77
       }
       return false:
78
     }
79
80
81
     T dfs(int v. T w) {
       if (v == g.fin) {
82
         return w;
84
       }
85
       int &j = ptr[v];
       while (j \ge 0) {
         int id = g.g[v][j];
87
          const auto &e = g.edges[id];
         if (e.c - e.f > g.eps && d[e.to] == d[v] - 1) {
89
           T t = dfs(e.to, min(e.c - e.f, w));
90
91
            if (t > g.eps) {
92
              g.edges[id].f += t;
              g.edges[id ^ 1].f -= t;
94
              return t;
95
            }
         }
96
         j--;
97
       return 0;
```

```
100
101
102
      T max_flow() {
103
         while (expath()) {
104
           for (int i = 0; i < g.n; i++) {
105
             ptr[i] = (int)g.g[i].size() - 1;
106
           }
107
           T big_add = 0;
           while (true) {
108
             T add = dfs(g.st, numeric_limits<T>::max());
109
110
             if (add <= g.eps) {</pre>
111
               break;
112
             }
113
             big add += add;
114
           }
115
           if (big_add <= g.eps) {</pre>
116
             break;
117
           }
118
           g.flow += big_add;
119
         }
120
         return g.flow;
121
122
123
       vector<bool> min_cut() {
124
         max_flow();
125
         vector<bool> ret(g.n);
         for (int i = 0; i < g.n; i++) {
127
           ret[i] = (d[i] != -1);
128
         }
129
         return ret:
130
131 }:
```

5.8 eulerian-digraph.cpp

```
optional < vector < int >> eulerian_path(int n, const vector < PII > & E) {
    vector < int > res;
    if (E.empty()) return res;
    vector < VI > adj(n + 1);
    vector < int > in(n + 1);
    for (int i = 0; i < ssize(E); i++) {
        auto [u, v] = E[i];
        adj[u].push_back(i);
    }
}</pre>
```

```
in[v] += 1:
     }
10
11
12
      int s = -1, hi = 0, lo = 0;
      for (int i = 1: i <= n: i++) {
13
        if (SZ(adj[i]) == in[i]) continue;
14
        if (abs(SZ(adj[i]) - in[i]) > 1) return {};
15
        if (SZ(adj[i]) > in[i]) {
16
17
         hi++, s = i;
       } else {
18
         lo++;
       }
20
     }
21
22
      if (!(hi == 0 && lo == 0) && !(hi == 1 && lo == 1)) {
        return {}:
23
24
      for (int i = 1; s == -1 && i <= n; i++)
25
        if (!adj[i].empty()) s = i;
26
27
      auto Dfs = [&](auto &Dfs. int u) -> void {
28
        while (!adj[u].empty()) {
29
30
          auto id = adj[u].back();
31
          adj[u].pop_back();
         int v = E[id].second;
32
         Dfs(Dfs, v);
33
34
          res.push_back(v);
       }
     };
37
     Dfs(Dfs, s);
     if (SZ(res) != SZ(E)) return {}:
38
      ranges::reverse(res);
39
      return res;
41 }
```

5.9 eulerian-undigraph.cpp

```
optional < vector < int > eulerian_path(int n, const vector < PII > &E) {
   vector < int > res;
   if (E.empty()) return res;

   vector < VI > adj(n + 1);

   for (int i = 0; i < ssize(E); i++) {
      auto [u, v] = E[i];
      adj[u].push_back(i);
   }
}</pre>
```

```
adj[v].push_back(i);
9
10
11
     int s = -1, odd = 0;
12
     for (int i = 1; i <= n; i++) {
13
       if (ssize(adj[i]) % 2 == 0) continue;
       if (++odd > 2) return {};
       s = i:
16
    }
17
     for (int i = 1; s == -1 && i <= n; i++)
18
       if (!adj[i].empty()) s = i;
19
20
      vector<int> vis(ssize(E)):
21
      auto Dfs = [&](auto &Dfs, int u) -> void {
22
        while (!adj[u].empty()) {
23
          auto id = adj[u].back();
24
          adj[u].pop back();
          if (vis[id]) continue;
         vis[id] = 1;
         int v = u ^ E[id].fi ^ E[id].se;
27
         Dfs(Dfs, v);
          res.push_back(v);
30
       }
31
     };
     Dfs(Dfs. s):
     if (SZ(res) != SZ(E)) return {};
     ranges::reverse(res);
     return res;
36 }
```

5.10 hungarian.cpp

```
vector<int> g[maxn];
int idx;
int a[N][N], use[N][N], p[maxn], vis[maxn];

bool find(int x) {
   vis[x] = 1;
   for (auto y : g[x]) {
       if (!p[y] || (!vis[p[y]] && find(p[y]))) {
           p[y] = x;
           return true;
}
```

```
12
        }
13
        return false;
14 }
15
16 int match() {
        int res = 0:
17
18
        fill(p + 1, p + idx + 1, 0);
        for (int i = 1; i <= idx; i++) {
19
20
            fill(vis + 1, vis + idx + 1, 0);
            if (find(i)) res++:
21
22
        }
23
        return res;
24 }
```

5.11 KM.cpp

```
1 #include <bits/stdc++.h>
2 using namespace std;
  using ll = long long;
5 // L <= R. 左边完全匹配
6 // 最小权完备匹配
8 // 带权匹配: 使得该二分图的权值和最大(或最小)的匹配。
9 // 最大匹配: 使得该二分图边数最多的匹配。
10 // 宗备匹配: 使得点数较小的点集中每个点都被匹配的匹配。
11 // 完美匹配: 所有点都被匹配的匹配。
12 // 定理1: 最大匹配数 = 最小点覆盖数 (Konig 定理)
13 // 定理2: 最大匹配数 = 最大独立数
14 // 定理3: 最小路径覆盖数 = 顶点数 - 最大匹配数
15
16 // 二分图的最小点覆盖
17 // 定义: 在二分图中, 求最少的点集, 使得每一条边至少都有端点在这个点集中。
18 // 二分图的最小点覆盖 = 二分图的最大匹配
20 // 二分图的最少边覆盖
21 // 定义: 在二分图中, 求最少的边, 使得他们覆盖所有的点, 并且每一个点只被一条
     边覆盖。
22 // 二分图的最少边覆盖 = 点数 - 二分图的最大匹配
24 // 二分图的最大独立集
25 // 定义: 在二分图中, 选最多的点, 使得任意两个点之间没有直接边连接。
26 // 二分图的最大独立集 = 点数 - 二分图的最大匹配
```

```
27
   template < class T>
   pair<T, vector<int>> hungarian(const vector<vector<T>> &a) {
        if (a.empty()) return {0, {}};
31
       int n = a.size() + 1, m = a[0].size() + 1;
32
       vector<T> u(n), v(m); // 顶标
       vector<int> p(m), ans(n - 1);
        for (int i = 1: i < n: i++) {
35
            p[0] = i;
36
            int j0 = 0;
37
            vector<T> dist(m, numeric_limits<T>::max());
38
            vector<int> pre(m, -1);
39
            vector<bool> done(m + 1);
40
            do { // dijkstra
41
                done[j0] = true;
42
                int i0 = p[j0], j1;
43
                T delta = numeric limits<T>::max();
                for (int j = 1; j < m; j++) if (!done[j]) {
45
                    auto cur = a[i0 - 1][j - 1] - u[i0] - v[j];
                    if (cur < dist[j]) dist[j] = cur, pre[j] = j0;</pre>
46
47
                    if (dist[j] < delta) delta = dist[j], j1 = j;</pre>
                }
48
                for (int j = 0; j < m; j++) {
50
                    if (done[j]) u[p[j]] += delta, v[j] -= delta;
51
                    else dist[j] -= delta;
52
                }
                j0 = j1;
54
            } while (p[j0]);
55
            while (j0) { // update alternating path
56
                int j1 = pre[j0];
57
                p[j0] = p[j1], j0 = j1;
            }
       }
59
60
       for (int j = 1; j < m; j++) {
61
            if (p[j]) ans [p[j] - 1] = j - 1;
62
       }
        return {-v[0], ans}; // min cost
64 }
66 int L, R, m;
67 int main() {
        scanf("%d%d%d", &L, &R, &m);
69
       R = max(L, R);
```

```
auto a = vector<vector<11>>(L, vector<11>(R, 0));
70
71
        for (int i = 0; i < m; i++) {
72
             int u, v, w;
73
             scanf("%d%d%d", &u, &v, &w);
74
             --u: --v:
            a[u][v] = -w;
75
        }
76
        auto [val, ans] = hungarian(a);
77
78
        printf("%lld\n", -val);
        for (int i = 0: i < L: i++) {
79
80
            if (a[i][ans[i]] >= 0) ans[i] = -1;
             printf("\frac{1}{2}d\frac{1}{2}c", ans[i] + 1, "\frac{1}{2}\n"[i == L - 1]);
81
        }
82
83 }
```

5.12 kosaraju.cpp

```
vector<int> e[maxn], erev[maxn];
   vector<int> c, out;
   vector<vector<int>> scc;
4 int vis[maxn]:
5 void dfs(int u) {
        vis[u] = 1:
        for (auto v : e[u]) if (!vis[v]) dfs(v);
        out.pb(u);
   void dfs rev(int u) {
11
        vis[u] = 1:
12
        for (auto v : erev[u]) if (!vis[v]) dfs_rev(v);
        c.pb(u):
13
14 }
15 void solve() {
        cin >> n >> m:
16
17
        rep(i, 1, m) {
18
            int u, v;
19
            cin >> u >> v;
20
            e[u].pb(v);
21
            erev[v].pb(u);
22
       }
        rep(i, 1, n) if (!vis[i]) dfs(i);
23
        fill(vis + 1, vis + n + 1, 0);
24
25
        reverse(all(out));
26
        for (auto v : out) if (!vis[v]) {
```

5.13 kruskal 重构树.cpp

```
1 /**
   * 构建后是一颗二叉树, 如果按最小生成树建立的话是大根堆。
   *性质:原图中两个点间所有路径上的边最大权值的最小值=最小生成树上两点简单路
       径的边最大权值
   * = kruskal 重构树上两点LCA的权值。
   * 重构树中代表原树中的点的节点全是叶子节点, 其余节点都代表了一条边的边权。
   * 利用这个性质可以找到点P的简单路径上边权最大值小于lim深度最小的节点。
   * 要求最小权值最大值,可以建最大生成树的重构树从而达到一样的效果。
  vector<tuple<11, 11, 11>> E;
11 rep(i, 1, m) {
12
     int u, v, w;
     cin >> u >> v >> w;
14
     E.emplace_back(w, u, v);
15 }
16 ranges::sort(E):
17 for (auto [w, u, v] : E) {
     u = find(u), v = find(v);
     if (u == v) continue:
20
     int p = ++idx;
21
     lim[p] = w;
     fa[u] = p, fa[v] = p;
     e[p].push_back(u);
     e[u].push_back(p);
     e[p].push_back(v);
26
      e[v].push_back(p);
27 }
```

5.14 MCMF.cpp

```
1 template < typename T >
2 struct MinCostGraph {
3     static const int V = 20100;
4     static const int E = 201000;
```

```
int s, t, vtot;
        int head[V], etot;
       T dis[V], flow, cost;
8
        int pre[V];
        bool vis[V];
10
11
        struct edge {
12
            int v, nxt;
13
           T f, c;
       } e[E * 2]:
14
        void addedge(int u,int v, T f, T c, T f2 = 0){
15
            e[etot] = {v, head[u], f, c}; head[u] = etot++;
16
            e[etot] = {u, head[v], f2, -c}; head[v] = etot++;
17
18
       }
19
20
        bool spfa() {
21
            T inf = numeric limits<T>::max() / 2;
            for (int i = 1; i <= vtot; i++) {
22
23
                dis[i] = inf;
                vis[i] = false:
24
25
                pre[i] = -1;
            }
26
            dis[s] = 0;
27
            vis[s] = true;
28
29
            queue < int > q;
30
            q.push(s);
            while (!q.empty()) {
31
32
                int u = q.front();
33
                for (int i = head[u]; ~i; i = e[i].nxt) {
                    int v = e[i].v:
34
                    if (e[i].f && dis[v] > dis[u] + e[i].c) {
35
36
                        dis[v] = dis[u] + e[i].c;
                        pre[v] = i;
37
38
                        if (!vis[v]) {
39
                            vis[v] = 1;
40
                            q.push(v);
                        }
41
                    }
42
                }
43
44
                q.pop();
                vis[u] = false;
45
46
47
            return dis[t] != inf;
```

```
48
       }
49
50
        void augment() {
51
            int u = t;
52
            T f = numeric_limits<T>::max();
            while (~pre[u]) {
53
                f = min(f, e[pre[u]].f);
54
                u = e[pre[u] ^ 1].v;
55
56
            }
57
            flow += f:
            cost += f * dis[t];
59
            u = t;
            while (~pre[u]) {
60
                e[pre[u]].f -= f;
61
62
                e[pre[u] ^ 1].f += f;
                u = e[pre[u] ^ 1].v;
            }
       }
65
66
       pair<T, T> solve() {
67
            flow = 0;
            cost = 0:
70
            while (spfa()) augment();
71
            return {flow, cost};
72
       }
73
        void init(int s_, int t_, int vtot_) {
            s = s_{-};
75
            t = t_;
76
            vtot = vtot_;
77
            etot = 0:
            for (int i = 1; i <= vtot; i++) head[i] = -1;
       }
80 };
```

5.15 MCMFfast.cpp

```
1 template <typename flow_t = int, typename cost_t = long long>
2 struct MCMF_SSPA {
3    int N;
4    vector<vector<int>> adj;
5    struct edge_t {
6       int dest;
7    flow_t cap;
```

```
8
           cost_t cost;
       };
9
10
       vector<edge_t> edges;
11
12
       vector < char > seen:
13
       vector<cost_t> pi;
14
       vector<int> prv;
15
       16
17
18
       void addEdge(int from, int to, flow_t cap, cost_t cost) {
           assert(cap >= 0);
19
           int e = int(edges.size());
20
21
           edges.emplace back(edge t{to, cap, cost});
22
           edges.emplace_back(edge_t{from, 0, -cost});
23
           adj[from].push_back(e);
24
           adj[to].push back(e+1);
       }
25
26
27
       const cost t INF COST = numeric limits<cost t>::max() / 4:
28
       const flow t INF FLOW = numeric limits<flow t>::max() / 4;
       vector<cost t> dist:
29
30
       __gnu_pbds::priority_queue<pair<cost_t, int>> q;
31
       vector<typename decltype(q)::point_iterator> its;
32
       void path(int s) {
           dist.assign(N, INF_COST);
33
           dist[s] = 0;
34
35
36
           its.assign(N, q.end());
           its[s] = q.push({0, s});
37
38
39
           while (!q.empty()) {
40
               int i = q.top().second; q.pop();
41
               cost t d = dist[i];
42
               for (int e : adj[i]) {
43
                   if (edges[e].cap) {
                       int j = edges[e].dest;
44
                       cost_t nd = d + edges[e].cost;
45
46
                       if (nd < dist[j]) {</pre>
                           dist[j] = nd;
47
                           prv[i] = e;
48
49
                           if (its[j] == q.end()) {
50
                               its[j] = q.push({-(dist[j] - pi[j]), j});
```

```
51
                            } else {
52
                                 q.modify(its[j], {-(dist[j] - pi[j]), j});
53
54
                        }
                    }
55
                }
56
            }
57
58
59
            swap(pi, dist);
60
       }
61
62
        vector<pair<flow t, cost t>> maxflow(int s, int t) {
63
            assert(s != t):
64
            flow t totFlow = 0; cost t totCost = 0;
65
            vector<pair<flow_t, cost_t>> res;
66
            while (path(s), pi[t] < INF_COST) {</pre>
67
                flow t curFlow = numeric limits<flow t>::max();
68
                for (int cur = t; cur != s; ) {
69
                    int e = prv[cur];
                    int nxt = edges[e^1].dest;
70
71
                    curFlow = min(curFlow, edges[e].cap);
72
                    cur = nxt:
                }
73
74
                totFlow += curFlow;
75
                totCost += pi[t] * curFlow;
76
                for (int cur = t; cur != s; ) {
77
                    int e = prv[cur];
78
                    int nxt = edges[e^1].dest;
79
                    edges[e].cap -= curFlow;
80
                    edges[e^1].cap += curFlow;
81
                    cur = nxt;
82
                }
83
84
                res.emplace_back(totFlow, totCost);
85
            }
            return res;
       }
88 };
```

5.16 MCMFfull.cpp

```
1 template <typename T, typename C>
2 class MCMF {
```

```
public:
      static constexpr T eps = (T) 1e-9;
6
      struct edge {
       int from:
       int to;
       T c;
       T f:
11
       C cost;
12
     }:
13
14
      int n;
15
      vector<vector<int>> g;
16
     vector<edge> edges;
17
     vector<C> d:
18
      vector<C> pot;
      __gnu_pbds::priority_queue<pair<C, int>> q;
19
20
      vector<typename decltype(q)::point_iterator> its;
21
      vector<int> pe;
      const C INF C = numeric limits<C>::max() / 2:
22
23
24
      explicit MCMF(int n_{-}): n(n_{-}), g(n), d(n), pot(n, 0), its(n), pe(n) {}
25
      int add(int from, int to, T forward_cap, T backward_cap, C edge_cost) {
26
        assert(0 \le from && from < n && 0 \le to && to < n):
27
28
        assert(forward cap >= 0 && backward cap >= 0);
29
        int id = static_cast<int>(edges.size());
        g[from].push back(id);
30
31
        edges.push_back({from, to, forward_cap, 0, edge_cost});
32
        g[to].push_back(id + 1);
        edges.push_back({to, from, backward_cap, 0, -edge_cost});
33
34
        return id:
     }
35
36
37
      void expath(int st) {
38
        fill(d.begin(), d.end(), INF_C);
39
        q.clear();
        fill(its.begin(), its.end(), q.end());
40
        its[st] = q.push({pot[st], st});
41
42
        d[st] = 0;
        while (!q.empty()) {
43
44
         int i = q.top().second;
45
          q.pop();
```

```
46
          its[i] = q.end();
47
          for (int id : g[i]) {
            const edge &e = edges[id];
48
49
            int j = e.to;
            if (e.c - e.f > eps && d[i] + e.cost < d[j]) {
50
              d[j] = d[i] + e.cost;
51
              pe[i] = id;
              if (its[j] == q.end()) {
               its[j] = q.push({pot[j] - d[j], j});
54
55
              } else {
                q.modify(its[j], {pot[j] - d[j], j});
57
           }
58
         }
59
60
       }
61
        swap(d, pot);
62
63
64
     pair<T, C> calc(int st, int fin) { // max_flow_min_cost
       T flow = 0:
65
66
       C cost = 0;
67
       bool ok = true:
68
        for (auto& e : edges) {
69
          if (e.c - e.f > eps && e.cost + pot[e.from] - pot[e.to] < 0) {
70
            ok = false:
71
            break;
         }
72
73
       }
74
       if (ok) {
75
          expath(st);
       } else {
76
77
          vector<int> deg(n, 0);
78
          for (int i = 0; i < n; i++) {
79
           for (int eid : g[i]) {
80
              auto& e = edges[eid];
81
              if (e.c - e.f > eps) {
82
                deg[e.to] += 1;
              }
84
           }
85
          }
          vector<int> que;
          for (int i = 0; i < n; i++) {
87
88
            if (deg[i] == 0) {
```

```
que.push_back(i);
 90
             }
           }
 91
 92
           for (int b = 0; b < (int) que.size(); b++) {</pre>
             for (int eid : g[que[b]]) {
 93
                auto& e = edges[eid];
 94
               if (e.c - e.f > eps) {
 95
                  deg[e.to] -= 1;
 96
                  if (deg[e.to] == 0) {
 97
                    que.push_back(e.to);
 98
 99
                 }
               }
100
101
             }
102
           }
           fill(pot.begin(), pot.end(), INF_C);
103
           pot[st] = 0;
104
           if (static cast<int>(que.size()) == n) {
105
             for (int v : que) {
106
107
                if (pot[v] < INF_C) {</pre>
                  for (int eid : g[v]) {
108
109
                    auto& e = edges[eid];
                    if (e.c - e.f > eps) {
110
                      if (pot[v] + e.cost < pot[e.to]) {</pre>
111
112
                        pot[e.to] = pot[v] + e.cost;
113
                        pe[e.to] = eid;
                     }
114
                    }
115
116
                 }
117
                }
             }
118
           } else {
119
120
             que.assign(1, st);
             vector < bool > in_queue(n, false);
121
122
             in_queue[st] = true;
             for (int b = 0; b < (int) que.size(); b++) {</pre>
123
124
                int i = que[b];
               in_queue[i] = false;
125
               for (int id : g[i]) {
126
127
                  const edge &e = edges[id];
128
                  if (e.c - e.f > eps && pot[i] + e.cost < pot[e.to]) {</pre>
                    pot[e.to] = pot[i] + e.cost;
129
                    pe[e.to] = id;
130
131
                    if (!in_queue[e.to]) {
```

```
132
                      que.push_back(e.to);
133
                      in_queue[e.to] = true;
134
                   }
135
                 }
136
               }
137
             }
138
           }
139
         }
140
         // debug(pot[fin]);
141
         while (pot[fin] < INF_C) { // < 0
142
           T push = numeric_limits<T>::max();
143
           int v = fin;
144
           while (v != st) {
145
             const edge &e = edges[pe[v]];
146
             push = min(push, e.c - e.f);
147
             v = e.from;
148
           }
149
           v = fin:
150
           while (v != st) {
151
             edge &e = edges[pe[v]];
152
             e.f += push;
153
             edge &back = edges[pe[v] ^ 1];
154
             back.f -= push;
155
             v = e.from;
156
           }
157
           flow += push;
158
           cost += push * pot[fin];
159
           expath(st);
160
         }
161
         return {flow, cost};
162
163 };
```

5.17 prim.cpp

```
vector<PII> e[N];

template <typename T>
void add(int u, int v, T w) {
    e[u].eb(v, w);
}

template <typename T>
```

```
9 T prim(vector<pair<int, T>> *g, int start) {
        const T inf = numeric limits<T>::max() / 4;
10
        T res = 0:
11
12
        vector<T> dist(n, inf);
        dist[start] = 0:
13
        priority_queue<pair<T, int>, vector<pair<T, int>>, greater<pair<T, int</pre>
14
            >>> s;
        s.emplace(dist[start], start);
15
        vector<int> was(n, 0);
16
        while (!s.empty()) {
17
18
            T expected = s.top().first;
            int i = s.top().second;
19
20
            s.pop();
21
            if (dist[i] != expected || was[i]) {
22
                continue:
            }
23
24
            was[i] = 1;
25
            res += expected:
26
            for (auto [to, cost] : g[i]) {
                if (cost < dist[to]) {</pre>
27
                    dist[to] = cost;
28
                    s.emplace(dist[to], to):
29
                }
31
            }
32
        }
33
        return res;
34 }
```

5.18 PushRelabel.cpp

```
1 /**
2 * Author: Simon Lindholm
3 * Date: 2015-02-24
4 * License: CCO
5 * Source: Wikipedia, tinyKACTL
6 * Description: Push-relabel using the highest label selection rule and the gap heuristic. Quite fast in practice.
7 * To obtain the actual flow, look at positive values only.
8 * Time: $O(V^2\sqrt E)$
9 * Status: Tested on Kattis and SPOJ, and stress-tested
10 */
11 #pragma once
```

```
13 struct PushRelabel {
     typedef vector<int> vi;
15
     struct Edge {
16
     int dest, back;
17
      11 f. c:
18
     };
19
     vector<vector<Edge>> g;
20
     vector<ll> ec:
21
     vector<Edge*> cur;
22
      vector<vi> hs: vi H:
23
      PushRelabel(int n): g(n), ec(n), cur(n), hs(2*n), H(n) {}
24
25
     void addEdge(int s. int t. 11 cap. 11 rcap=0) {
26
       if (s == t) return;
27
       g[s].push_back({t, SZ(g[t]), 0, cap});
       g[t].push_back({s, SZ(g[s])-1, 0, rcap});
29
30
31
     void addFlow(Edge& e, ll f) {
       Edge &back = g[e.dest][e.back];
32
33
       if (!ec[e.dest] && f) hs[H[e.dest]].push back(e.dest);
       e.f += f: e.c -= f: ec[e.dest] += f:
       back.f -= f: back.c += f: ec[back.dest] -= f:
36
    }
37
     ll calc(int s. int t) {
       int v = SZ(g); H[s] = v; ec[t] = 1;
       vi co(2*v); co[0] = v-1;
       rep(i,0,v-1) cur[i] = g[i].data();
41
       for (Edge& e : g[s]) addFlow(e, e.c);
42
43
       for (int hi = 0;;) {
44
          while (hs[hi].empty()) if (!hi--) return -ec[s];
          int u = hs[hi].back(); hs[hi].pop back();
45
46
          while (ec[u] > 0) // discharge u
47
           if (cur[u] == g[u].data() + SZ(g[u])) {
48
             H[u] = 1e9:
49
              for (Edge& e : g[u]) if (e.c && H[u] > H[e.dest]+1)
50
               H[u] = H[e.dest] + 1, cur[u] = &e;
              if (++co[H[u]], !--co[hi] && hi < v)
51
52
                rep(i,0,v-1) if (hi < H[i] && H[i] < v)
53
                  --co[H[i]], H[i] = v + 1;
54
              hi = H[u]:
55
           } else if (cur[u]->c && H[u] == H[cur[u]->dest]+1)
```

```
addFlow(*cur[u], min(ec[u], cur[u]->c));
else ++cur[u];

}

bool leftOfMinCut(int a) { return H[a] >= SZ(g); }

}
```

5.19 tarjan 割点.cpp

```
1 vector<int> g[maxn], ans;
   stack<int> stk:
3 int dfn[maxn], cut[maxn], low[maxn], idx;
5 void dfs(int x, int f) {
        low[x] = dfn[x] = ++idx;
        stk.push(x);
       int ch = 0;
       for (auto y : g[x]) {
10
            if (!dfn[v]) {
11
                ch++:
12
                dfs(y, x);
13
                low[x] = min(low[x], low[y]);
                if (low[y] >= dfn[x]) cut[x] = 1;
14
15
            } else {
                if (y != f) low[x] = min(low[x], dfn[y]);
            }
17
18
       if (x == 1 \&\& ch <= 1) cut[x] = 0:
19
        if (cut[x]) ans.pb(x);
21 }
```

5.20 tarjan 割边.cpp

```
1  vector<PII> g[maxn];
2  stack<int> stk;
3  int dfn[maxn], ins[maxn], low[maxn];
4  int idx, tot;
5  VI ans;
6  void dfs(int x, int f) {
7    low[x] = dfn[x] = ++idx;
8    stk.push(x);
9    ins[x] = 1;
10    for (auto [y, id] : g[x]) {
```

```
11
            if (!dfn[y]) {
                dfs(v, id);
13
                low[x] = min(low[x], low[y]);
14
                if (ins[y] && id != f) low[x] = min(low[x], dfn[y]);
15
            }
16
       }
17
18
       if (low[x] >= dfn[x]) {
19
            ++tot;
20
            while (true) {
21
                int cur = stk.top();
22
                stk.pop();
                ins[cur] = 0;
23
24
                if (cur == x) break;
25
            }
            if (f != 0) ans.pb(f);
27
28 }
```

5.21 tarjan 强连通分量.cpp

```
1 vector<int> g[maxn];
2 stack<int> stk;
3 int dfn[maxn], ins[maxn], low[maxn], belong[maxn];
   int idx, tot;
5
   void dfs(int x) {
       low[x] = dfn[x] = ++idx;
       ins[x] = 1;
       stk.push(x);
       for (auto y : g[x]) {
11
           if (!dfn[v]) {
12
                dfs(y);
13
               low[x] = min(low[x], low[y]);
14
           } else {
15
                if (ins[y]) low[x] = min(low[x], dfn[y]);
16
           }
       }
17
       if (low[x] >= dfn[x]) {
19
           ++tot:
20
            while (true) {
21
                int cur = stk.top(); stk.pop();
22
                ins[cur] = 0:
```

```
belong[cur] = tot;
                if (cur == x) break;
25
26
       }
27 }
   5.22 tarjan 点双.cpp
1 vector<int> g[maxn];
2 stack<int> stk;
   int dfn[maxn], low[maxn], idx, tot, cut[maxn];
   vector<int> bcc[maxn];
   void dfs(int x, int f) {
        low[x] = dfn[x] = ++idx;
        stk.push(x);
       int ch = 0;
        for (auto y : g[x]) {
10
11
            if (!dfn[v]) {
                ch++:
12
13
                dfs(y, x);
                low[x] = min(low[x], low[y]);
14
                if (low[y] >= dfn[x]) {
15
16
                    cut[x] = 1;
17
                    ++tot:
18
                    bcc[tot].pb(x);
19
                    while (true) {
20
                        int cur = stk.top();
21
                        stk.pop();
                        bcc[tot].pb(cur);
22
23
                        if (cur == y) break;
24
                    }
                }
25
            } else {
26
                if (y != f) low[x] = min(low[x], dfn[v]);
27
28
29
        if (x == 1 && ch <= 1) cut[x] = 0:
31 }
```

5.23 tarjan 边双.cpp

```
1 vector < PII > g[maxn];
```

```
2 stack<int> stk;
3 int dfn[maxn], low[maxn], idx, tot, belong[maxn];
   vector<int> bcc[maxn]:
5
   void dfs(int x, int f) {
       low[x] = dfn[x] = ++idx;
        stk.push(x);
        for (auto [y, id] : g[x]) {
10
            if (!dfn[y]) {
11
                dfs(y, id);
12
                low[x] = min(low[x], low[y]);
13
14
                if (id != f) low[x] = min(low[x], dfn[y]);
15
           }
16
       }
17
        if (low[x] >= dfn[x]) {
18
            ++tot;
            while (true) {
20
                int cur = stk.top();
21
                stk.pop();
22
                belong[cur] = tot;
                bcc[tot].pb(cur):
                if (cur == x) break:
           }
26
       }
27 }
```

5.24 twosat.cpp

```
1 class twosat {
2 public:
        digraph<int> g;
4
        int n:
6
       twosat(int _n) : g(digraph<int>(2 * _n)), n(_n) {
7
       }
8
9
       // (v[x] == value x)
10
        inline void add(int x, int value_x) {
11
            assert(0 <= x && x < n):
12
            assert(0 <= value_x && value_x <= 1);</pre>
13
            g.add(2 * x + (value_x ^ 1), 2 * x + value_x);
14
       }
```

```
15
        // (v[x] == value x // v[y] == value y)
16
        inline void add(int x, int value_x, int y, int value_y) {
17
18
            assert(0 <= x && x < n && 0 <= y && y < n);
            assert(0 <= value_x && value_x <= 1 && 0 <= value_y && value_y <= 1)
19
            g.add(2 * x + (value_x ^ 1), 2 * y + value_y);
20
            g.add(2 * y + (value_y ^ 1), 2 * x + value_x);
21
22
       }
23
24
        inline vector<int> solve() {
25
            int cnt;
            vector<int> c = find_scc(g, cnt);
26
27
            vector<int> res(n);
            for (int i = 0; i < n; i++) {
28
29
                if (c[2 * i] == c[2 * i + 1]) {
                    return vector<int>();
31
                res[i] = (c[2 * i] < c[2 * i + 1]);
33
34
            return res;
36 };
```

5.25 差分约束系统.cpp

```
1 /**
      Description:
      求解方程组 x_u - x_v \le w_i, 求出的x_i为满足条件的最大值
       转化为x u \ll x v + w i
      问题等价于求最短路 (bellmanford或Floyd)
      即加一条有向边add(u, v, w), dist[v] = min(dist[v], dist[u] + w)
      求最小值(满足条件情况下尽量小)等价于求(-x i)最大(或者转化为求最长路)
       求非负解只需要添加超级节点S, S向各个点连边(S + O \le xi), 再设dist[S]
           = 0
   void solve() {
11
      cin >> n >> m:
12
      vector<int> dist(n, 0);
      vector<vector<PII>>> g(n);
13
14
      rep(i, 0, m - 1) {
15
         int u, v, w;
16
         cin >> u >> v >> w:
```

```
17
            u--. v--:
18
            g[u].eb(v, -w);
19
20
       bool ok = 1;
21
       rep(i, 1, n) {
22
            bool upd = 0;
23
            rep(u, 0, n - 1) {
24
                for (auto [v, w] : g[u]) {
25
                    if (dist[v] < dist[u] + w) {</pre>
26
                        dist[v] = dist[u] + w;
27
                        upd = 1;
28
                    }
                }
29
30
            }
31
            if (!upd) break;
            // 仍然有约束未满足
            if (i == n && upd) ok = 0;
34
       }
       if (!ok) {
            return cout << -1 << '\n', void();
37
       }
       rep(i, 0, n - 1) {
            cout << dist[i] << "..\n"[i == n - 1]:
40
       }
41 }
```

6 Math

6.1 binom.cpp

```
1  vector<Mint> fact(1, 1);
2  vector<Mint> inv_fact(1, 1);
3
4  Mint C(int n, int k) {
5    if (k < 0 || k > n) {
6       return 0;
7    }
8    while ((int)fact.size() < n + 1) {
9       fact.push_back(fact.back() * (int)fact.size());
10       inv_fact.push_back(1 / fact.back());
11    }
12    return fact[n] * inv_fact[k] * inv_fact[n - k];</pre>
```

```
13 }
14
15 const int mod = 1000000007:
16 const int T = 1000000;
17 ll fact[] = {};
18 ll powmod(ll a, ll b) {
       ll ret = 1;
20
        for (; b; b >>= 1) {
21
            if (b & 1) ret = ret * a % mod;
22
            a = a * a \% mod:
23
       }
24
        return ret;
25 }
26 ll fac(int n) {
       ll v = fact[n / T]:
27
        for (int i = n / T * T + 1; i <= n; i++)
29
            v = v * i \% mod;
30
        return v:
31 }
32 ll binom(int n. int m) {
33
        if (m < 0 \mid | m > n) return 0;
        return fac(n) * powmod(fac(m) * fac(n - m) % mod, mod - 2) % mod;
34
35 }
```

6.2 bsgs.cpp

```
int bsgs(int a, int b, int m) { // a^x=b \pmod{m}
       int res = m + 1:
       int t = sqrt(m) + 2;
       11 d = powmod(a, t, m);
       ll cnt = 1:
       //map<int,int> p;
       hs.init():
       for (int i = 1; i <= t; i++) {
            cnt = cnt * d % m:
10
           //if (!p.count(cnt)) p[cnt] = i;
11
           if (hs.query(cnt) == -1) hs.insert(cnt, i);
12
       }
13
       cnt = b;
       for (int i = 1: i <= t: i++) {
14
15
            cnt = cnt * a % m;
16
           //if (p.count(cnt)) res = min(res, p[cnt] * t - i);
           int tmp = hs.query(cnt);
17
```

6.3 cantor.cpp

```
1 ll fac[maxn], A[maxn], w[maxn];
  2 void init(int n) {
                              fac[0] = 1:
                             rep(i, 1, n) fac[i] = fac[i - 1] * i % mod;
  5 }
  6 ll cantor(int w[], int n) {
                             ll ans = 1:
                              for (int i = 1; i \le n; i++) { // can optimize by BIT
                                             for (int j = i + 1; j \le n; j++) {
                                                             if (w[i] > w[j]) A[i]++;
10
11
                                            }
12
                             }
13
                             for (int i = 1: i < n: i++) {
14
                                             ans += A[i] * fac[n - i];
15
                            }
16
                              return ans;
17 }
18
19
              void decanter(ll x, int n) { // x - rank n - r
20
21
                             vector<int> rest(n, 0);
22
                             iota(rest.begin(), rest.end(), 1); // rest->1,2,3,4...
23
                              for (int i = 1; i <= n; i++) {
24
                                             A[i] = x / fac[n - i];
25
                                            x %= fac[n - i];
26
                            }
27
                             for (int i = 1: i <= n: i++) {
                                             w[i] = rest[A[i]];
                                             rest.erase(lower_bound(rest.begin(), rest.end(), w[i]));
29
                             }
31 }
```

6.4 EXCRT modequ exgcd.cpp

```
1 ll exgcd(ll a, ll b, ll &x, ll &y) {
```

```
if (b == 0) {
           x = 1, y = 0;
           return a:
5
       }
       ll d = exgcd(b, a \% b, y, x);
       y = (a / b) * x;
       return d;
10
12 11 modequ(11 a, 11 b, 11 m) {
       11 x, y;
       11 d = exgcd(a, m, x, y);
15
      if (b % d != 0) return -1;
16
       m /= d: a /= d: b /= d:
17
       x = x * b \% m;
       if (x < 0) x += m;
18
       return x:
20 }
21
   void merge(ll &a, ll &b, ll c, ll d) {
23
       if (a == -1 || b == -1) return:
24
       11 x, y;
25
       11 g = exgcd(b, d, x, y);
26
       if ((c - a) % g != 0) {
           a = -1, b = -1;
27
           return:
       }
29
30
       d /= g;
31
       11 t = ((c - a) / g) \% d * x \% d;
       if (t < 0) t += d;
32
33
       a = b * t + a:
34
       b = b * d:
35 }
```

6.5 factor.cpp

```
1  namespace Factor {
2    const int N=1010000;
3    ll C,fac[10010],n,mut,a[1001000];
4    int T,cnt,i,l,prime[N],p[N],psize,_cnt;
5    ll _e[100],_pr[100];
6    vector<ll> d;
```

```
inline ll mul(ll a,ll b,ll p) {
            if (p<=1000000000) return a*b%p;
            else if (p \le 100000000000011) return (((a*(b>>20)%p) \le 20)+(a*(b))
                 &((1<<20)-1))))%p;
            else {
10
11
                11 d=(11)floor(a*(long double)b/p+0.5);
12
                11 \text{ ret}=(a*b-d*p)\%p;
13
                if (ret<0) ret+=p;</pre>
                return ret;
14
15
            }
16
       }
17
        void prime_table(){
            int i,j,tot,t1;
19
            for (i=1;i<=psize;i++) p[i]=i;
20
            for (i=2,tot=0;i<=psize;i++){
21
                if (p[i]==i) prime[++tot]=i;
22
                for (j=1;j<=tot && (t1=prime[j]*i)<=psize;j++){</pre>
                    p[t1]=prime[j];
24
                    if (i%prime[j]==0) break;
25
                }
26
            }
27
       }
        void init(int ps) {
29
            psize=ps;
30
            prime_table();
31
        11 powl(ll a,ll n,ll p) {
            ll ans=1;
34
            for (;n;n>>=1) {
35
                if (n&1) ans=mul(ans,a,p);
                a=mul(a,a,p);
            }
37
38
            return ans;
39
        }
        bool witness(ll a,ll n) {
40
41
            int t=0;
42
            11 u=n-1:
43
            for (;~u&1;u>>=1) t++;
            11 x=powl(a,u,n),_x=0;
44
45
            for (;t;t--) {
46
                x=mul(x,x,n);
47
                if (_x==1 && x!=1 && x!=n-1) return 1;
48
                x = _x;
```

```
49
            }
                                                                                            92
                                                                                            93
                                                                                                         }
50
            return x!=1;
        }
                                                                                            94
                                                                                                    }
51
52
        bool miller(ll n) {
                                                                                            95
                                                                                                    void factor(ll n) {
            if (n<2) return 0:
                                                                                                         for (int i=0:i<cnt:i++) {</pre>
53
                                                                                            96
                                                                                                             if (n%fac[i]==0) n/=fac[i],fac[cnt++]=fac[i];}
54
            if (n<=psize) return p[n]==n;</pre>
                                                                                            97
55
            if (~n&1) return 0;
                                                                                            98
                                                                                                         if (n<=psize) {
            for (int j=0; j \le 7; j++) if (witness(rng()%(n-1)+1,n)) return 0;
                                                                                            99
                                                                                                             for (;n!=1;n/=p[n]) fac[cnt++]=p[n];
56
57
            return 1;
                                                                                           100
                                                                                                             return;
                                                                                           101
                                                                                                         }
        }
58
59
        11 gcd(ll a,ll b) {
                                                                                           102
                                                                                                         if (miller(n)) fac[cnt++]=n;
60
            ll ret=1;
                                                                                           103
                                                                                                         else {
                                                                                                             11 x=rho(n):
            while (a!=0) {
                                                                                           104
61
62
                if ((~a&1) && (~b&1)) ret <<=1,a>>=1,b>>=1;
                                                                                           105
                                                                                                             factor(x); factor(n/x);
                else if (~a&1) a>>=1; else if (~b&1) b>>=1;
                                                                                           106
                                                                                                         }
63
                                                                                           107
                                                                                                    }
64
                else {
                                                                                           108
                     if (a<b) swap(a,b);
                                                                                                     void dfs(ll x,int dep) {
                                                                                           109
                                                                                                         if (dep==_cnt) d.pb(x);
                    a-=b:
                                                                                           110
                                                                                                         else {
67
                }
            }
                                                                                           111
                                                                                                             dfs(x,dep+1);
68
                                                                                           112
69
            return ret*b;
                                                                                                             for (int i=1;i<=_e[dep];i++) dfs(x*=_pr[dep],dep+1);</pre>
70
        }
                                                                                           113
                                                                                                         }
        11 rho(11 n) {
                                                                                           114
                                                                                                    }
71
                                                                                           115
            while (1) {
                                                                                                     void norm() {
72
73
                11 X=rng()%n,Y,Z,T=1,*1Y=a,*1X=1Y;
                                                                                           116
                                                                                                         sort(fac,fac+cnt);
                                                                                           117
74
                int tmp=20;
                                                                                                         cnt=0;
                C=rng()%10+3;
75
                                                                                           118
                                                                                                         rep(i,0,cnt-1) if (i==0||fac[i]!=fac[i-1]) _pr[_cnt]=fac[i],_e[_cnt
                X=mul(X,X,n)+C;*(1Y++)=X;1X++;
                                                                                                             ++]=1:
76
77
                Y=mul(X,X,n)+C;*(1Y++)=Y;
                                                                                           119
                                                                                                             else _e[_cnt-1]++;
78
                for(:X!=Y:) {
                                                                                           120
                                                                                                    }
                                                                                           121
                    11 t=X-Y+n;
                                                                                                     vector<ll> getd() {
79
                                                                                           122
80
                    Z=mul(T,t,n);
                                                                                                         d.clear();
                    if(Z==0) return gcd(T,n);
                                                                                           123
                                                                                                         dfs(1,0);
81
                                                                                           124
82
                    tmp--;
                                                                                                         return d;
                                                                                                    }
83
                     if (tmp==0) {
                                                                                           125
                                                                                           126
84
                         tmp=20;
                                                                                                     vector<ll> factor(ll n) {
                                                                                           127
                         Z=gcd(Z,n);
                                                                                                         cnt=0:
                         if (Z!=1 && Z!=n) return Z;
                                                                                           128
                                                                                                         factor(n);
86
                                                                                           129
87
                    }
                                                                                                         norm();
88
                    T=Z:
                                                                                           130
                                                                                                         return getd();
                    Y = *(1Y + +) = mul(Y, Y, n) + C;
                                                                                           131
                                                                                                    }
89
                                                                                           132
                                                                                                     vector<PLL> factorG(ll n) {
90
                    Y = *(1Y + +) = mul(Y, Y, n) + C;
                                                                                           133
91
                    X = *(1X + +);
                                                                                                         cnt=0;
```

```
134
             _factor(n);
             norm();
135
             vector < PLL > d:
136
137
             rep(i,0, cnt-1) d.pb(mp( pr[i], e[i]));
             return d:
138
        }
139
140
         bool is primitive(ll a,ll p) {
             assert(miller(p));
141
142
             vector<PLL> D=factorG(p-1);
             rep(i,0,SZ(D)-1) if (powl(a,(p-1)/D[i].fi,p)==1) return 0;
143
             return 1;
144
        }
145
        11 phi(11 n) {
146
147
             auto d=factorG(n);
             for (auto p:d) n=n/p.fi*(p.fi-1);
148
149
             return n;
150
        }
151 }
```

6.6 fft.cpp

```
namespace fft {
      typedef double dbl;
      struct num {
       dbl x, y;
       num() { x = y = 0; }
       num(dbl x, dbl y) : x(x), y(y) { }
     };
      inline num operator+(num a, num b) { return num(a.x + b.x, a.y + b.y); }
10
      inline num operator-(num a, num b) { return num(a.x - b.x, a.y - b.y); }
11
      inline num operator*(num a, num b) { return num(a.x * b.x - a.y * b.y, a.x
12
           * b.y + a.y * b.x); }
      inline num conj(num a) { return num(a.x, -a.y); }
13
14
15
      int base = 1;
16
      vector<num> roots = \{\{0, 0\}, \{1, 0\}\};
17
      vector < int > rev = \{0, 1\};
18
19
      const dbl PI = acosl(-1.0);
20
21
      void ensure base(int nbase) {
```

```
22
        if (nbase <= base) {
23
          return;
24
        }
25
        rev.resize(1 << nbase);</pre>
26
        for (int i = 0; i < (1 << nbase); i++) {
27
          rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
28
29
        roots.resize(1 << nbase):
30
        while (base < nbase) {
31
          dbl \ angle = 2 * PI / (1 << (base + 1));
32 //
            num z(cos(angle), sin(angle));
33
          for (int i = 1 << (base - 1); i < (1 << base); i++) {
34
            roots[i << 1] = roots[i]:</pre>
35 //
              roots[(i << 1) + 1] = roots[i] * z;
            dbl angle_i = angle * (2 * i + 1 - (1 << base));
            roots[(i << 1) + 1] = num(cos(angle_i), sin(angle_i));</pre>
         }
39
          base++:
40
     }
41
42
43
      void fft(vector<num> &a. int n = -1) {
44
        if (n == -1) {
45
          n = a.size();
46
47
        assert((n & (n - 1)) == 0);
        int zeros = __builtin_ctz(n);
        ensure base(zeros);
        int shift = base - zeros;
51
        for (int i = 0: i < n: i++) {
52
          if (i < (rev[i] >> shift)) {
53
            swap(a[i], a[rev[i] >> shift]);
54
          }
55
56 /*
          for (int k = 1; k < n; k <<= 1) {
57
          for (int \ i = 0; \ i < n; \ i += 2 * k) {
            for (int j = 0; j < k; j++) {
              num z = a[i + j + k] * roots[j + k];
              a[i + j + k] = a[i + j] - z;
61
              a[i + j] = a[i + j] + z;
            7
          7
63
64
        }*/
```

```
65
         for (int len = 1: len < n: len <<= 1) {
          for (int i = 0; i < n; i += 2 * len) {
 66
             for (int j = i, k = i + len; j < i + len; j++, k++) {
 67
 68
               num z = a[k] * roots[k - i];
               a[k] = a[i] - z:
 69
               a[i] = a[i] + z;
 70
            }
 71
          }
 73
        }
      }
 74
 75
 76
       vector<num> fa, fb;
 77
 78
       vector<long long> multiply(vector<int> &a, vector<int> &b) {
 79
        int need = a.size() + b.size() - 1:
 80
         int nbase = 0;
         while ((1 << nbase) < need) nbase++;
         ensure base(nbase):
 83
         int sz = 1 << nbase;</pre>
         if (sz > (int) fa.size()) {
 84
 85
          fa.resize(sz);
 86
        for (int i = 0: i < sz: i++) {
 87
          int x = (i < (int) a.size() ? a[i] : 0);</pre>
 88
 89
          int v = (i < (int) b.size() ? b[i] : 0):
 90
          fa[i] = num(x, y);
        }
        fft(fa, sz);
 92
 93
         num r(0, -0.25 / sz);
 94
         for (int i = 0: i <= (sz >> 1): i++) {
 95
          int j = (sz - i) & (sz - 1);
          num z = (fa[j] * fa[j] - conj(fa[i] * fa[i])) * r;
97
          if (i != j) {
 98
             fa[j] = (fa[i] * fa[i] - conj(fa[j] * fa[j])) * r;
          }
99
100
          fa[i] = z;
        }
101
102
         fft(fa, sz);
103
         vector<long long> res(need);
        for (int i = 0; i < need; i++) {
104
          res[i] = fa[i].x + 0.5;
105
        }
106
107
         return res;
```

```
108
      }
109
110
       vector<int> multiply_mod(vector<int> &a, vector<int> &b, int m, int eq =
111
         int need = a.size() + b.size() - 1:
112
         int nbase = 0:
113
         while ((1 << nbase) < need) nbase++;</pre>
114
         ensure base(nbase):
115
         int sz = 1 << nbase;</pre>
         if (sz > (int) fa.size()) {
1117
           fa.resize(sz);
118
119
         for (int i = 0: i < (int) a.size(): i++) {
120
           int x = (a[i] \% m + m) \% m;
121
          fa[i] = num(x & ((1 << 15) - 1), x >> 15):
122
123
         fill(fa.begin() + a.size(), fa.begin() + sz, num {0, 0});
124
         fft(fa. sz):
125
         if (eq) {
126
           copy(fa.begin(), fa.begin() + sz, fb.begin());
127
        } else {
128
           if (sz > (int) fb.size()) {
129
             fb.resize(sz):
130
          }
131
           for (int i = 0: i < (int) b.size(): i++) {
132
             int x = (b[i] \% m + m) \% m;
             fb[i] = num(x & ((1 << 15) - 1), x >> 15);
133
134
135
           fill(fb.begin() + b.size(), fb.begin() + sz, num {0, 0});
136
           fft(fb. sz):
137
        }
138
         dbl ratio = 0.25 / sz:
139
         num r2(0, -1):
140
         num r3(ratio, 0);
141
         num r4(0, -ratio);
142
         num r5(0, 1);
143
         for (int i = 0; i \le (sz >> 1); i++) {
144
           int j = (sz - i) & (sz - 1);
145
           num a1 = (fa[i] + conj(fa[j]));
146
           num a2 = (fa[i] - conj(fa[j])) * r2;
147
           num b1 = (fb[i] + conj(fb[j])) * r3;
148
           num b2 = (fb[i] - conj(fb[j])) * r4;
149
           if (i != j) {
```

```
150
             num c1 = (fa[j] + conj(fa[i]));
             num c2 = (fa[i] - conj(fa[i])) * r2;
151
             num d1 = (fb[j] + conj(fb[i])) * r3;
152
153
             num d2 = (fb[i] - conj(fb[i])) * r4;
             fa[i] = c1 * d1 + c2 * d2 * r5:
154
             fb[i] = c1 * d2 + c2 * d1;
155
156
157
           fa[i] = a1 * b1 + a2 * b2 * r5:
158
          fb[j] = a1 * b2 + a2 * b1;
        }
159
         fft(fa, sz);
160
         fft(fb, sz);
161
         vector<int> res(need):
162
163
         for (int i = 0; i < need; i++) {
          long long aa = fa[i].x + 0.5:
164
          long long bb = fb[i].x + 0.5;
165
          long long cc = fa[i].y + 0.5;
166
167
          res[i] = (aa + ((bb \% m) << 15) + ((cc \% m) << 30)) \% m:
168
        }
169
        return res:
170
      }
171
       vector<int> square mod(vector<int> &a. int m) {
172
173
         return multiply_mod(a, a, m, 1);
174
      }
       // fft::multiply uses dbl, outputs vector<long long> of rounded values
175
       // fft::multiply mod might work for res.size() up to 2^21
177
      // typedef long double dbl;
                                                       up to 2^25 (but takes a lot
            of memory)
178 }:
```

6.7 fftfast.cpp

```
// FFT_MAXN = 2^k
// fft_init() to precalc FFT_MAXN-th roots

typedef long double db;
const int FFT_MAXN = 262144;
const int N = 3.1e5;
const db pi = acosl(-1.);
struct cp {
    db a, b;
    cp operator+(const cp &y) const { return (cp){a + y.a, b + y.b}; }
```

```
11
       cp operator-(const cp &y) const { return (cp){a - y.a, b - y.b}; }
12
       cp operator*(const cp &y) const { return (cp){a * y.a - b * y.b, a * y.b
             + b * v.a}: 
13
       cp operator!() const { return (cp){a, -b}; };
14 } nw[FFT MAXN + 1]:
15 int bitrev[FFT_MAXN];
16 void dft(cp *a, int n, int flag = 1) {
17
       int d = 0:
       while ((1 << d) * n != FFT_MAXN) d++;
18
       rep(i, 0, n - 1) if (i < (bitrev[i] >> d)) swap(a[i], a[bitrev[i] >> d])
20
       for (int 1 = 2; 1 <= n; 1 <<= 1) {
21
           int del = FFT MAXN / 1 * flag:
22
           for (int i = 0; i < n; i += 1) {
23
                cp *le = a + i, *ri = a + i + (l >> 1), *w = flag == 1 ? nw : nw
                     + FFT MAXN;
                rep(k, 0, 1 / 2 - 1) {
24
                    cp ne = *ri * *w:
26
                    *ri = *le - ne, *le = *le + ne;
27
                   le++, ri++, w += del:
28
               }
29
           }
30
       }
31
       if (flag != 1) rep(i, 0, n - 1) a[i].a /= n, a[i].b /= n;
32 }
33 void fft init() {
       int L = 0:
       while ((1 << L) != FFT_MAXN) L++;
36
       bitrev[0] = 0;
37
       rep(i, 1, FFT MAXN - 1) bitrev[i] = bitrev[i >> 1] >> 1 | ((i & 1) << (L
             - 1)):
       nw[0] = nw[FFT_MAXN] = (cp){1, 0};
       rep(i, 0, FFT MAXN)
39
       nw[i] = (cp){cosl(2 * pi / FFT_MAXN * i), sinl(2 * pi / FFT_MAXN * i)};
             // very slow
41 }
42
   void convo(db *a, int n, db *b, int m, db *c) {
44
       static cp f[FFT_MAXN >> 1], g[FFT_MAXN >> 1], t[FFT_MAXN >> 1];
45
       int N = 2:
46
       while (N \le n + m) N \le 1;
47
       rep(i, 0, N - 1) if (i & 1) {
48
           f[i >> 1].b = (i <= n) ? a[i] : 0.0;
```

```
}
50
51
        else {
52
            f[i >> 1].a = (i <= n) ? a[i] : 0.0;
            g[i >> 1].a = (i <= m) ? b[i] : 0.0:
53
        }
54
        dft(f, N >> 1);
        dft(g, N >> 1);
        int del = FFT MAXN / (N >> 1);
57
        cp qua = (cp)\{0, 0.25\}, one = (cp)\{1, 0\}, four = (cp)\{4, 0\}, *w = nw;
58
59
        rep(i, 0, N / 2 - 1) {
60
            int j = i ? (N >> 1) - i : 0;
            t[i] = (four * !(f[i] * g[i]) - (!f[i] - f[i]) * (!g[i] - g[i]) * (
61
                one + *w)) * qua;
            w += del:
62
        dft(t, N >> 1, -1);
        rep(i, 0, n + m) c[i] = (i & 1) ? t[i >> 1].a : t[i >> 1].b:
67
    void mul(int *a, int *b, int n) { // n \le N. 0 \le a \lceil i \rceil. b \lceil i \rceil \le mo
        static cp f[N], g[N], t[N], r[N];
70
71
        int nn = 2;
72
        while (nn \le n + n) nn \le 1:
73
        rep(i, 0, nn - 1) {
            f[i] = (i \le n) ? (cp){(db)(a[i] >> 15), (db)(a[i] & 32767)} : (cp)
                {0, 0};
75
            g[i] = (i \le n) ? (cp){(db)(b[i] >> 15), (db)(b[i] & 32767)} : (cp)
                 {0. 0}:
76
        }
77
        swap(n, nn);
        dft(f, n, 1);
78
79
        dft(g, n, 1);
        rep(i, 0, n - 1) {
80
            int j = i ? n - i : 0;
            t[i] = ((f[i] + !f[i]) * (!g[i] - g[i]) + (!f[i] - f[i]) * (g[i] + !
82
                 g[j])) * (cp){0, 0.25};
            r[i] = (!f[i] - f[i]) * (!g[i] - g[i]) * (cp){-0.25, 0} + (cp){0,}
                0.25} * (f[i] + !f[j]) * (g[i] + !g[j]);
        }
        dft(t, n, -1);
        dft(r, n, -1);
```

g[i >> 1].b = (i <= m) ? b[i] : 0.0:

```
87 rep(i, 0, n - 1)

88 a[i] = ((ll(t[i].a + 0.5) % mo << 15) + ll(r[i].a + 0.5) + (ll(r[i].b + 0.5) % mo << 30)) % mo;

89 }
```

6.8 fftnew.cpp

```
1 namespace fft {
2
   typedef double dbl;
5 struct num {
   dbl x, y;
   num() { x = y = 0; }
     num(dbl x , dbl y ) : x(x ), y(y ) {}
9 };
10
11 inline num operator+(num a, num b) { return num(a.x + b.x, a.y + b.y); }
12 inline num operator-(num a, num b) { return num(a.x - b.x, a.y - b.y); }
13 inline num operator*(num a, num b) { return num(a.x * b.x - a.y * b.y, a.x *
         b.y + a.y * b.x); }
14 inline num conj(num a) { return num(a.x, -a.y); }
15
16 int base = 1:
17 vector<num> roots = {{0, 0}, {1, 0}};
18 vector<int> rev = {0, 1}:
19
20
   const dbl PI = static_cast<dbl>(acosl(-1.0));
21
22 void ensure_base(int nbase) {
     if (nbase <= base) {
24
       return;
25
26
    rev.resize(1 << nbase);
     for (int i = 0: i < (1 << nbase): i++) {
28
       rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
29
30
     roots.resize(1 << nbase):
     while (base < nbase) {</pre>
31
32
       dbl \ angle = 2 * PI / (1 << (base + 1)):
33 //
           num z(cos(angle), sin(angle));
34
       for (int i = 1 << (base - 1); i < (1 << base); i++) {
35
         roots[i << 1] = roots[i]:</pre>
```

```
36 //
              roots \lceil (i \ll 1) + 1 \rceil = roots \lceil i \rceil * z:
37
          dbl angle i = angle * (2 * i + 1 - (1 << base));
          roots[(i << 1) + 1] = num(cos(angle_i), sin(angle_i));</pre>
38
39
       }
40
       base++:
     }
41
42 }
    void fft(vector<num>& a, int n = -1) {
     if (n == -1) {
45
        n = (int) a.size();
     assert((n & (n - 1)) == 0):
48
      int zeros = builtin ctz(n);
49
     ensure base(zeros):
50
51
      int shift = base - zeros;
     for (int i = 0; i < n; i++) {
52
53
       if (i < (rev[i] >> shift)) {
54
          swap(a[i], a[rev[i] >> shift]);
       }
55
56
     }
57
     for (int k = 1: k < n: k <<= 1) {
       for (int i = 0: i < n: i += 2 * k) {
58
59
         for (int j = 0; j < k; j++) {
60
            num z = a[i + j + k] * roots[j + k];
            a[i + j + k] = a[i + j] - z;
            a[i + j] = a[i + j] + z;
         }
       }
66 }
67
   vector < num > fa, fb;
69
   vector<int64_t> square(const vector<int>& a) {
71
     if (a.empty()) {
       return {}:
73
74
     int need = (int) a.size() + (int) a.size() - 1;
     int nbase = 1:
75
     while ((1 << nbase) < need) nbase++;</pre>
76
77
     ensure base(nbase):
    int sz = 1 \ll nbase;
```

```
if ((sz >> 1) > (int) fa.size()) {
        fa.resize(sz >> 1);
 81
 82
      for (int i = 0; i < (sz >> 1); i++) {
        int x = (2 * i < (int) a.size() ? a[2 * i] : 0):
        int v = (2 * i + 1 < (int) a.size() ? a[2 * i + 1] : 0);</pre>
 84
 85
        fa[i] = num(x, y);
 86
 87
      fft(fa, sz >> 1);
      num r(1.0 / (sz >> 1), 0.0):
      for (int i = 0; i \le (sz >> 2); i++) {
        int j = ((sz >> 1) - i) & ((sz >> 1) - 1);
        num fe = (fa[i] + coni(fa[i])) * num(0.5, 0):
        num fo = (fa[i] - conj(fa[j])) * num(0, -0.5);
        num aux = fe * fe + fo * fo * roots[(sz >> 1) + i] * roots[(sz >> 1) + i]
            ];
 94
        num tmp = fe * fo;
        fa[i] = r * (coni(aux) + num(0, 2) * coni(tmp)):
        fa[j] = r * (aux + num(0, 2) * tmp);
     }
 97
      fft(fa, sz >> 1);
      vector<int64 t> res(need):
      for (int i = 0: i < need: i++) {
101
        res[i] = llround(i % 2 == 0 ? fa[i >> 1].x : fa[i >> 1].y);
102
      }
103
      return res;
104 }
105
106 vector<int64_t> multiply(const vector<int>& a, const vector<int>& b) {
      if (a.empty() || b.empty()) {
108
      return {};
109
     }
110
      if (a == b) {
111
      return square(a);
112
113
      int need = (int) a.size() + (int) b.size() - 1;
114
      int nbase = 1:
      while ((1 << nbase) < need) nbase++;</pre>
116
      ensure_base(nbase);
117
      int sz = 1 \ll nbase:
118
      if (sz > (int) fa.size()) {
119
      fa.resize(sz):
120
     }
```

```
121
      for (int i = 0: i < sz: i++) {
        int x = (i < (int) a.size() ? a[i] : 0);</pre>
122
        int v = (i < (int) b.size() ? b[i] : 0):
123
124
        fa[i] = num(x, y);
      }
125
      fft(fa. sz):
126
       num r(0, -0.25 / (sz >> 1));
127
       for (int i = 0: i \le (sz >> 1): i++) {
128
129
        int j = (sz - i) & (sz - 1);
        num z = (fa[j] * fa[j] - conj(fa[i] * fa[i])) * r;
130
        fa[j] = (fa[i] * fa[i] - conj(fa[j] * fa[j])) * r;
131
        fa[i] = z;
132
133
      }
134
      for (int i = 0; i < (sz >> 1); i++) {
        num A0 = (fa[i] + fa[i + (sz >> 1)]) * num(0.5, 0):
135
136
         num A1 = (fa[i] - fa[i + (sz >> 1)]) * num(0.5, 0) * roots[(sz >> 1) + i]
        fa[i] = A0 + A1 * num(0, 1);
137
138
      }
      fft(fa. sz >> 1):
139
140
       vector<int64 t> res(need);
      for (int i = 0: i < need: i++) {
141
        res[i] = llround(i % 2 == 0 ? fa[i >> 1].x : fa[i >> 1].v):
142
143
      }
      return res;
144
145 }
146
147 vector<int> multiply mod(const vector<int>& a, const vector<int>& b, int m)
        {
      if (a.emptv() || b.emptv()) {
148
        return {};
149
150
      }
       int eq = (a.size() == b.size() && a == b):
151
152
       int need = (int) a.size() + (int) b.size() - 1;
       int nbase = 0:
153
       while ((1 << nbase) < need) nbase++;
154
       ensure base(nbase):
155
       int sz = 1 << nbase;</pre>
156
157
       if (sz > (int) fa.size()) {
        fa.resize(sz);
158
      }
159
      for (int i = 0: i < (int) a.size(): i++) {
160
        int x = (a[i] \% m + m) \% m;
161
```

```
162
        fa[i] = num(x & ((1 << 15) - 1), x >> 15);
163
164
      fill(fa.begin() + a.size(), fa.begin() + sz, num {0, 0}):
165
      fft(fa, sz);
      if (sz > (int) fb.size()) {
166
167
        fb.resize(sz):
168
      }
169
      if (ea) {
170
         copy(fa.begin(), fa.begin() + sz, fb.begin());
171
      } else {
172
        for (int i = 0; i < (int) b.size(); i++) {
173
          int x = (b[i] \% m + m) \% m;
174
          fb[i] = num(x & ((1 << 15) - 1), x >> 15):
175
        }
176
        fill(fb.begin() + b.size(), fb.begin() + sz, num {0, 0}):
177
        fft(fb, sz);
178
179
       dbl ratio = 0.25 / sz:
180
       num r2(0, -1);
181
      num r3(ratio, 0):
182
       num r4(0, -ratio);
183
       num r5(0, 1):
       for (int i = 0: i <= (sz >> 1): i++) {
185
        int j = (sz - i) & (sz - 1);
186
        num a1 = (fa[i] + conj(fa[j]));
187
        num a2 = (fa[i] - conj(fa[j])) * r2;
188
         num b1 = (fb[i] + conj(fb[j])) * r3;
189
        num b2 = (fb[i] - conj(fb[j])) * r4;
190
        if (i != j) {
191
           num c1 = (fa[j] + conj(fa[i]));
192
           num c2 = (fa[i] - coni(fa[i])) * r2;
193
           num d1 = (fb[j] + conj(fb[i])) * r3;
194
           num d2 = (fb[i] - conj(fb[i])) * r4;
           fa[i] = c1 * d1 + c2 * d2 * r5;
196
           fb[i] = c1 * d2 + c2 * d1;
197
        }
198
        fa[j] = a1 * b1 + a2 * b2 * r5;
199
        fb[j] = a1 * b2 + a2 * b1;
200
201
      fft(fa, sz);
202
      fft(fb, sz);
203
       vector<int> res(need);
204
       for (int i = 0; i < need; i++) {
```

```
205
        int64_t aa = llround(fa[i].x);
        int64 t bb = llround(fb[i].x);
206
        int64_t cc = llround(fa[i].y);
207
208
        res[i] = static cast<int>((aa + ((bb % m) << 15) + ((cc % m) << 30)) % m
            ):
      }
209
210
      return res;
211 }
212
213 } // namespace fft
```

6.9 FST.cpp

```
void fst(VI &a,bool inv) {
        for (int n=SZ(a),step=1;step<n;step*=2) {</pre>
            for (int i=0; i< n; i+=2*step) rep(j,i,i+step-1) {
                int &u=a[j],&v=a[j+step];
                tie(u.v)=
                inv?PII(v-u,u):PII(v,u+v); // AND
                inv?PII(v.u-v):PII(u+v.u): // OR
                PII(u+v,u-v); // XOR
           }
       }
10
        if (inv) for (auto &x : a) x/=SZ(a); // XOR only
11
12 }
13 VI conv(VI a, VI b) {
        fst(a,0),fst(b,0);
14
       rep(i,0,SZ(a)-1) a[i]=a[i]*b[i];
15
        fst(a,1); return a;
16
17 }
```

6.10 FWT.cpp

```
11
        for (int i = 0; i < bit(n); i++) {
12
            f[i] %= mod;
13
            g[i] %= mod;
14
            h[i] = f[i] * g[i] % mod;
15
       }
        for (int i = 0; i < n; i++) {
16
17
            for (int j = 0; j < bit(n); j++) {
18
                if ((j & bit(i)) == 0)
19
                    h[j] = h[j + bit(i)];
            }
20
21
       }
22
        for (int i = 0; i < bit(n); i++) {
23
            h[i] %= mod:
24
            if (h[i] < 0) h[i] += mod;
25
       }
26
27
        11 \text{ ans} = 0;
        rep(i, 0, bit(n) - 1) ans ^= h[i];
        cout << ans << '\n';
30 }
```

6.11 gauss(合数).cpp

```
1 void gauss(int n) {
       int ans = 1;
3
       //rep(i,1,n) rep(j,1,n) p[i][j]%=mod;
       for (int i = 1; i <= n; i++) {
            for (int j = i + 1; j \le n; j++) {
                int x = i, y = j;
7
                while (p[x][i]) {
                    int t = p[y][i] / p[x][i];
                    for (int k = i; k \le n; k++)
10
                        p[y][k] = (p[y][k] - p[x][k] * t) % mod;
11
                    swap(x, y);
12
                if (x == i) {
13
14
                    for (int k = i; k \le n; k++) swap(p[i][k], p[j][k]);
15
                    ans = -ans;
16
17
           }
18
       }
19 }
```

6.12 gauss.cpp

```
1 11 f[N][N];
2 11 v[N], a[N];
3 void gauss() {
        for (int i = 1; i <= n; i++) {
            for (int j = i; j \le n; j++) {
                if (f[j][i] > f[i][i]) {
                    swap(v[i], v[j]);
                    for (int k = 1; k \le n; k++)
                        swap(f[j][k], f[i][k]);
10
               }
11
            }
12
            for (int j = i + 1; j \le n; j++) {
13
                if (f[j][i]) {
14
                    int delta = f[j][i] * fpow(f[i][i], mod - 2) % mod;
15
                    for (int k = i; k <= n; k++) {
                        f[i][k] -= f[i][k] * delta % mod;
16
                        if (f[j][k] < 0)
17
                            f[j][k] += mod;
18
19
                    v[j] -= v[i] * delta % mod;
20
21
                    if (v[i] < mod)</pre>
                        v[i] += mod;
               }
23
24
            }
25
        }
26
        for (int j = n; j > 0; j--) {
27
            for (int k = j + 1; k \le n; k++) {
28
                v[j] -= f[j][k] * a[k] % mod;
                if (v[i] < 0)
                    v[j] += mod;
30
31
32
            a[j] = v[j] * fpow(f[j][j], mod - 2) % mod;
33
34 }
```

6.13 linearbasis.cpp

```
1 struct linear_base {
2     ll w[64];
3     ll zero = 0;
4     ll tot = -1;
5     void clear() {
```

```
rep(i, 0, 63) w[i] = 0;
            zero = 0;
8
            tot = -1:
9
       }
10
       void insert(ll x) {
11
            for (int i = 62; i >= 0; i--) {
12
               if (x & bit(i))
13
                    if (!w[i]) {w[i] = x; return;}
14
                    else x ^= w[i];
15
           }
16
            zero++;
17
       }
       void build() {
18
19
            rep(i, 0, 63) rep(j, 0, i - 1) {
20
                if (w[i]&bit(j)) w[i] ^= w[j];
21
22
            for (int i = 0; i <= 62; i++) {
                if (w[i] != 0) w[++tot] = w[i]:
24
           }
       }
25
26
       11 qmax() {
27
           ll res = 0:
28
            for (int i = 62; i >= 0; i--) {
29
                res = max(res, res ^ w[i]);
30
           }
31
            return res;
       bool check(ll x) {
34
            for (int i = 62; i >= 0; i--) {
35
                if (x & bit(i))
                   if (!w[i]) return false;
37
                    else x ^= w[i];
           }
39
            return true;
40
       }
41
       11 query(11 k) {
42
           ll res = 0;
           // if (zero) k=1;
44
           // if (k \ge bit(tot)) return -1;
45
            for (int i = tot; i >= 0; i--) {
                if (k & bit(i)) {
47
                   res = max(res, res ^ w[i]);
48
               } else {
```

6.14 lucas.cpp

```
1 11 fac[maxn], fnv[maxn];
3 11 binom(11 a, 11 b) {
       if (b > a || b < 0) return 0;
       return fac[a] * fnv[a - b] % p * fnv[b] % p;
8 ll lucas(ll a, ll b, ll p) {
       ll ans = 1:
       while (a > 0 | | b > 0) {
           ans = (ans * binom(a % p, b % p)) % p;
11
12
           a /= p, b /= p;
13
       }
14
       return ans;
15 }
16
17 int main() {
18
       cin >> p >> T;
19
       fac[0] = 1:
       rep(i, 1, p - 1) fac[i] = fac[i - 1] * i % p;
20
       fnv[p-1] = powmod(fac[p-1], p-2, p);
21
       per(i, p - 2, 0) fnv[i] = fnv[i + 1] * (i + 1) % p;
23
       assert(fnv[0] == 1);
24 }
```

6.15 mathdiv.cpp

```
1 ll floor_div(ll x, ll y) {
2    assert(y != 0);
3    if (y < 0) {
4         y = -y;
5         x = -x;
6    }
7    if (x >= 0) return x / y;
```

```
8    return (x + 1) / y - 1;

9  }

10  ll ceil_div(ll x, ll y) {

11    assert(y != 0);

12    if (y < 0) {

13        y = -y;

14        x = -x;

15   }

16    if (x <= 0) return x / y;

17    return (x - 1) / y + 1;

18 }
```

6.16 matrix.cpp

```
1 template <typename T>
2 vector<vector<T>> operator*(const vector<vector<T>>& a, const vector<vector</pre>
       T>>& b) {
     if (a.empty() || b.empty()) {
4
       return {{}};
     vector<vector<T>> c(a.size(), vector<T>(b[0].size()));
     for (int i = 0; i < static cast<int>(c.size()); i++) {
       for (int j = 0; j < static_cast < int > (c[0].size()); <math>j++) {
         c[i][i] = 0;
         for (int k = 0; k < static cast<int>(b.size()); k++) {
            c[i][j] += a[i][k] * b[k][j];
12
         }
13
       }
14
     return c:
16 }
17
18 template <typename T>
19 vector<vector<T>>& operator*=(vector<vector<T>>& a, const vector<vector<T>>&
         b) {
     return a = a * b;
21 }
22
23 template <typename T, typename U>
24 vector<vector<T>> power(const vector<vector<T>>& a, const U& b) {
     assert(b >= 0);
26
     vector<U> binary;
27
     U bb = b:
```

```
while (bb > 0) {
       binary.push back(bb & 1);
        bb >>= 1:
31
      vector<vector<T>> res(a.size(), vector<T>(a.size()));
32
     for (int i = 0; i < static_cast<int>(a.size()); i++) {
33
        res[i][i] = 1;
     for (int j = (int)binary.size() - 1; j >= 0; j--) {
36
       res *= res:
37
        if (binary[i] == 1) {
38
         res *= a;
41
     }
     return res:
43 }
```

6.17 matrixfast.cpp

```
1 Description: Basic operations on square matrices.
2 Usage: Matrix<int, 3> A;
3 \quad A.d = \{\{\{1, 2, 3\}\}, \{\{4, 5, 6\}\}, \{\{7, 8, 9\}\}\}\};
4 vector<int> vec = {1, 2, 3}:
5 \text{ vec} = (A^N) * \text{vec};
   template < class T, int N> struct Matrix {
        typedef Matrix M;
        array<array<T, N>, N> d{};
10
        M operator*(const M& m) const {
            M a:
11
            rep(i, 0, N) rep(j, 0, N)
13
            rep(k, 0, N) \ a.d[i][j] += d[i][k] * m.d[k][j];
            return a:
14
15
        vector<T> operator*(const vector<T>& vec) const {
16
17
            vector<T> ret(N);
18
            rep(i, 0, N) rep(j, 0, N) ret[i] += d[i][j] * vec[j];
19
            return ret:
20
        }
21
        M operator^(ll p) const {
            assert(p >= 0);
23
            M a, b(*this);
24
            rep(i, 0, N) a.d[i][i] = 1;
```

6.18 MillerRabbin pollard modmul.cpp

```
1 /*ModMulLL.h
2 Description: Calculate a b mod c (or a
3 b mod c) for 0 a, b c 7.2 • 10^18
4 Time: O (1) for modmul, O (log b) for modpow*/
5 /*ull modmul(ull a, ull b, ull M) {
       ll \ ret = a * b - M * ull(1.L / M * a * b);
       return ret + M * (ret < 0) - M * (ret >= (ll)M):
8 }
9 ull modpow(ull b, ull e, ull mod) {
       ull \ ans = 1:
11
       for (; e; b = modmul(b, b, mod), e \neq 2)
           if (e \& 1) ans = modmul(ans. b. mod):
13
       return ans;
14 7*/
15 ll modmul(ll a. ll b. ll m) {
       a \% = m, b \% = m;
       11 d = ((1db)a * b / m);
       d = a * b - d * m;
       if (d >= m) d -= m:
       if (d < 0) d += m:
21
       return d;
22 }
23 ll modpow(ll a, ll b, ll p) {
       ll ans = 1:
       while (b) {
26
           if (b & 1) ans = modmul(ans, a, p);
27
           a = modmul(a, a, p); b >>= 1;
       } return ans;
29 }
30 /*MillerRabin.h
31 Description: Deterministic Miller-Rabin primality test. Guaranteed to
32 work for numbers up to 7 · 1018; for larger numbers, use Python and extend A
```

```
randomly.
33 Time: 7 times the complexity of a^b mod c.*/
   bool isPrime(ll n) {
35
        if (n < 2 | | n % 6 % 4 != 1) return (n | 1) == 3;
        11 A[] = \{2, 325, 9375, 28178, 450775, 9780504, 1795265022\},
36
                  s = \_builtin\_ctzll(n - 1), d = n >> s;
37
        for (11 a : A) { // ^ count trailing zeroes
38
            11 p = modpow(a % n, d, n), i = s;
39
            while (p != 1 && p != n - 1 && a % n && i--)
41
                p = modmul(p, p, n);
            if (p != n - 1 && i != s) return 0;
42
       }
43
44
        return 1:
45 }
46 /*Factor.h
   Description: Pollard-rho randomized factorization algorithm. Returns
    prime factors of a number, in arbitrary order (e.g. 2299 -> {11, 19, 11}).
    Time: O(n^{1/4}), less for numbers with small factors.*/
   ll pollard(ll n) {
        auto f = [n](11 x) \{ return modmul(x, x, n) + 1; \};
51
        11 x = 0, y = 0, t = 30, prd = 2, i = 1, q;
        while (t++ \% 40 || _-gcd(prd, n) == 1) {
53
            if (x == y) x = ++i, y = f(x);
54
55
            if ((q = modmul(prd, max(x, y) - min(x, y), n))) prd = q;
56
            x = f(x), y = f(f(y));
        return __gcd(prd, n);
59 }
   vector<ll> factor(ll n) {
        if (n == 1) return {};
61
        if (isPrime(n)) return {n};
63
       11 x = pollard(n);
        auto 1 = factor(x), r = factor(n / x);
64
65
       l.insert(l.end(), all(r));
        return 1;
66
67 }
```

6.19 ntt(polynomial).cpp

```
1 #include<bits/stdc++.h>
2 using namespace std;
3
4 const int mod = 998244353;
```

```
6 inline void add(int &x, int y) {
     x += y;
     if (x \ge mod) {
       x -= mod:
10
11 }
12
13 inline void sub(int &x, int y) {
    x -= y;
14
     if (x < 0) {
       x += mod;
17
18 }
19
    inline int mul(int x, int y) {
21
      return (long long) x * y % mod;
22 }
23
24 inline int power(int x, int y) {
     int res = 1;
     for (; y; y >>= 1, x = mul(x, x)) {
27
       if (v & 1) {
         res = mul(res, x);
29
       }
31
     return res;
32 }
34 inline int inv(int a) {
     a %= mod;
     if (a < 0) {
37
       a += mod;
     int b = mod, u = 0, v = 1;
     while (a) {
       int t = b / a;
       b -= t * a;
       swap(a, b);
       u = t * v;
       swap(u, v);
47
     if (u < 0) {
```

```
u += mod:
      return u:
51 }
52
    namespace ntt {
    int base = 1, root = -1, max base = -1;
    vector<int> rev = {0, 1}, roots = {0, 1};
56
   void init() {
57
58
      int temp = mod - 1;
      max base = 0;
      while (temp % 2 == 0) {
60
61
        temp >>= 1;
62
        ++max_base;
     }
63
      root = 2;
64
65
      while (true) {
        if (power(root, 1 << max_base) == 1 && power(root, 1 << (max_base - 1))</pre>
            != 1) {
67
          break;
       }
68
        ++root;
70
71 }
72
    void ensure_base(int nbase) {
      if (max base == -1) {
74
75
        init();
76
      if (nbase <= base) {</pre>
77
78
        return:
79
80
      assert(nbase <= max base);</pre>
      rev.resize(1 << nbase);</pre>
81
82
      for (int i = 0; i < 1 << nbase; ++i) {
        rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (nbase - 1));
83
84
85
      roots.resize(1 << nbase);</pre>
      while (base < nbase) {</pre>
86
        int z = power(root, 1 << (max base - 1 - base));</pre>
87
        for (int i = 1 << (base - 1): i < 1 << base: ++i) {
88
          roots[i << 1] = roots[i];
```

```
roots[i \ll 1 \mid 1] = mul(roots[i], z):
 91
        }
         ++base;
 93
 94 }
 95
     void dft(vector<int> &a) {
       int n = a.size(), zeros = __builtin_ctz(n);
 98
      ensure base(zeros);
       int shift = base - zeros:
100
      for (int i = 0; i < n; ++i) {
101
        if (i < rev[i] >> shift) {
102
           swap(a[i], a[rev[i] >> shift]);
103
        }
104
      }
105
      for (int i = 1; i < n; i <<= 1) {
106
        for (int j = 0; j < n; j += i << 1) {
107
          for (int k = 0: k < i: ++k) {
108
             int x = a[j + k], y = mul(a[j + k + i], roots[i + k]);
109
            a[i + k] = (x + y) \% mod;
110
            a[j + k + i] = (x + mod - y) \% mod;
111
          }
112
        }
113
      }
114 }
115
     vector<int> multiply(vector<int> a, vector<int> b) {
       int need = a.size() + b.size() - 1, nbase = 0;
118
       while (1 << nbase < need) {
119
        ++nbase:
120
121
      ensure_base(nbase);
122
      int sz = 1 \ll nbase:
123
      a.resize(sz);
124
      b.resize(sz);
125
       bool equal = a == b;
126
       dft(a);
127
      if (equal) {
128
        b = a:
129
      } else {
130
        dft(b);
131
      int inv sz = inv(sz);
```

```
133
       for (int i = 0: i < sz: ++i) {
         a[i] = mul(mul(a[i], b[i]), inv sz);
134
      }
135
136
       reverse(a.begin() + 1, a.end());
       dft(a):
137
       a.resize(need);
138
139
       return a;
140 }
141
     vector<int> inverse new(const vector<int> &a) {
143
       assert(!a.empty());
       int n = (int) a.size();
144
       vector<int> b = {inv(a[0])}:
145
       while ((int) b.size() < n) {</pre>
146
         vector<int> x(a.begin(), a.begin() + min(a.size(), b.size() << 1));</pre>
147
         x.resize(b.size() << 1);</pre>
148
         b.resize(b.size() << 1);</pre>
149
150
         vector<int> c = b:
151
         // NTT<T>::fft(c);
         // NTT<T>::fft(x):
152
153
         dft(c);
         dft(x):
154
         // Modular < T > inv = 1 / static cast < Modular < T >>>((int) x.size()):
155
         int inv sz = inv((int)x.size()):
156
         for (int i = 0: i < (int) x.size(): i++) {</pre>
157
           // x[i] *= c[i] * inv;
158
           x[i] = mul(x[i], mul(c[i], inv_sz));
159
160
161
         reverse(x.begin() + 1, x.end());
         // NTT < T > :: fft(x):
162
163
         dft(x):
164
         rotate(x.begin(), x.begin() + (x.size() >> 1), x.end());
         fill(x.begin() + (x.size() >> 1), x.end(), 0);
165
166
         // NTT < T > :: fft(x);
         dft(x):
167
168
         for (int i = 0; i < (int) x.size(); i++) {</pre>
           // x \lceil i \rceil *= c \lceil i \rceil * inv:
169
           x[i] = mul(x[i], mul(c[i], inv sz));
170
171
172
         reverse(x.begin() + 1, x.end());
         // NTT < T > :: fft(x);
173
174
         dft(x):
175
         for (int i = 0; i < ((int) x.size() >> 1); i++) {
```

```
176
          // b [i + ((int) x.size() >> 1)] = -x[i]:
177
          int t = 0; sub(t, x[i]);
          b[i + ((int) x.size() >> 1)] = t:
179
        }
180
     }
181
      b.resize(n):
182
      return b;
183 }
184
     vector<int> inverse(vector<int> a) {
      int n = a.size(), m = (n + 1) >> 1;
187
      if (n == 1) {
      return vector<int>(1. inv(a[0])):
189
      } else {
190
        vector<int> b = inverse(vector<int>(a.begin(), a.begin() + m));
191
        int need = n << 1, nbase = 0;
192
        while (1 << nbase < need) {
193
          ++nbase:
194
        }
195
         ensure base(nbase):
196
         int sz = 1 << nbase;</pre>
197
        a.resize(sz):
198
        b.resize(sz):
199
        dft(a);
200
        dft(b):
201
        int inv sz = inv(sz);
202
        for (int i = 0; i < sz; ++i) {
203
          a[i] = mul(mul(mod + 2 - mul(a[i], b[i]), b[i]), inv sz);
204
        reverse(a.begin() + 1, a.end());
205
206
        dft(a):
207
        a.resize(n):
208
        return a:
209
     }
210 }
211 }
212
213 using ntt::multiply;
214 using ntt::inverse;
215
216 vector<int>& operator += (vector<int> &a, const vector<int> &b) {
217
      if (a.size() < b.size()) {
218
        a.resize(b.size());
```

```
219
      }
       for (int i = 0; i < b.size(); ++i) {
220
         add(a[i], b[i]):
221
222
      }
223
      return a:
224 }
225
     vector<int> operator + (const vector<int> &a. const vector<int> &b) {
226
227
       vector<int> c = a;
      return c += b:
228
229 }
230
     vector<int>& operator -= (vector<int> &a. const vector<int> &b) {
231
232
       if (a.size() < b.size()) {
         a.resize(b.size()):
233
234
      for (int i = 0; i < b.size(); ++i) {
235
         sub(a[i], b[i]):
236
237
      }
238
      return a:
239 }
240
     vector<int> operator - (const vector<int> &a. const vector<int> &b) {
241
242
       vector<int> c = a:
243
      return c -= b:
244 }
245
     vector<int>& operator *= (vector<int> &a, const vector<int> &b) {
246
247
       if (min(a.size(), b.size()) < 128) {</pre>
         vector<int> c = a:
248
         a.assign(a.size() + b.size() - 1, 0);
249
         for (int i = 0: i < c.size(): ++i) {
250
          for (int j = 0; j < b.size(); ++j) {
251
             add(a[i + j], mul(c[i], b[j]));
252
          }
253
        }
      } else {
255
         a = multiply(a, b);
256
      }
257
       return a;
258
259 }
260
261 vector<int> operator * (const vector<int> &a, const vector<int> &b) {
```

```
262
      vector<int> c = a:
263
      return c *= b;
264 }
265
     vector<int>& operator /= (vector<int> &a. const vector<int> &b) {
267
      int n = a.size(), m = b.size();
268
      if (n < m) {
269
        a.clear():
270
      } else {
271
        vector<int> c = b:
272
        reverse(a.begin(), a.end());
273
        reverse(c.begin(), c.end());
274
        c.resize(n - m + 1):
275
        a *= inverse(c):
276
        a.erase(a.begin() + n - m + 1, a.end());
277
        reverse(a.begin(), a.end());
278
279
      return a:
280 }
281
     vector<int> operator / (const vector<int> &a, const vector<int> &b) {
      vector<int> c = a:
284
      return c /= b:
285 }
286
     vector<int>& operator %= (vector<int> &a, const vector<int> &b) {
      int n = a.size(), m = b.size();
289
      if (n >= m) {
        vector<int> c = (a / b) * b;
290
291
        a.resize(m - 1):
292
        for (int i = 0; i < m - 1; ++i) {
293
           sub(a[i], c[i]):
294
        }
295
      }
296
      return a;
297 }
298
    vector<int> operator % (const vector<int> &a, const vector<int> &b) {
      vector<int> c = a:
301
      return c %= b;
302 }
303
304 vector<int> derivative(const vector<int> &a) {
```

```
305
      int n = a.size():
      vector<int> b(n - 1);
306
      for (int i = 1: i < n: ++i) {
307
308
        b[i - 1] = mul(a[i], i);
      }
309
310
      return b;
311 }
312
     vector<int> primitive(const vector<int> &a) {
313
      int n = a.size():
314
       vector<int> b(n + 1), invs(n + 1);
315
      for (int i = 1; i <= n; ++i) {
316
        invs[i] = i == 1 ? 1 : mul(mod - mod / i, invs[mod % i]);
317
        b[i] = mul(a[i - 1], invs[i]);
318
      }
319
      return b;
320
321 }
322
     vector<int> logarithm(const vector<int> &a) {
      vector<int> b = primitive(derivative(a) * inverse(a)):
324
325
      b.resize(a.size());
      return b:
326
327 }
328
     vector<int> exponent(const vector<int> &a) {
329
       vector<int> b(1, 1);
330
       while (b.size() < a.size()) {</pre>
331
         vector<int> c(a.begin(), a.begin() + min(a.size(), b.size() << 1));</pre>
332
333
         add(c[0], 1);
         vector<int> old b = b:
334
         b.resize(b.size() << 1);</pre>
335
336
         c -= logarithm(b);
        c *= old b;
337
338
         for (int i = b.size() >> 1; i < b.size(); ++i) {
          b[i] = c[i];
339
340
        }
341
      b.resize(a.size());
342
343
       return b:
344 }
345
     vector<int> power(vector<int> a, int m) {
      int n = a.size(), p = -1;
347
```

```
348
       vector<int> b(n):
349
      for (int i = 0; i < n; ++i) {
        if (a[i]) {
351
          p = i;
352
           break:
353
        }
354
      }
355
      if (p == -1) {
356
        b[0] = !m;
357
        return b:
358
359
      if ((long long) m * p >= n) {
        return b:
360
361
      }
362
      int mu = power(a[p], m), di = inv(a[p]);
363
       vector<int> c(n - m * p);
      for (int i = 0; i < n - m * p; ++i) {
364
        c[i] = mul(a[i + p], di);
366
367
      c = logarithm(c):
      for (int i = 0; i < n - m * p; ++i) {
368
369
        c[i] = mul(c[i], m):
370
      }
371
      c = exponent(c);
372
     for (int i = 0; i < n - m * p; ++i) {
373
        b[i + m * p] = mul(c[i], mu);
374
     }
375
      return b;
376 }
377
     vector<int> sgrt(const vector<int> &a) {
379
       vector<int> b(1, 1);
380
       while (b.size() < a.size()) {
381
        vector<int> c(a.begin(), a.begin() + min(a.size(), b.size() << 1));</pre>
382
        vector<int> old_b = b;
383
        b.resize(b.size() << 1);</pre>
384
         c *= inverse(b):
         for (int i = b.size() >> 1; i < b.size(); ++i) {
           b[i] = mul(c[i], (mod + 1) >> 1);
387
        }
388
      }
389
      b.resize(a.size());
390
       return b;
```

```
391 }
392
     vector<int> multiply all(int l. int r. vector<vector<int>> &all) {
394
      if (1 > r) {
        return vector<int>():
395
      } else if (1 == r) {
396
         return all[1];
      } else {
398
        int y = (1 + r) >> 1;
399
        return multiply_all(1, y, all) * multiply_all(y + 1, r, all);
400
401
402 }
403
     vector<int> evaluate(const vector<int> &f, const vector<int> &x) {
       int n = x.size():
405
      if (!n) {
406
         return vector<int>();
407
408
      vector<vector<int>> up(n * 2);
409
      for (int i = 0: i < n: ++i) {
410
         up[i + n] = vector < int > \{(mod - x[i]) \% mod, 1\};
411
412
      for (int i = n - 1: i: --i) {
413
         up[i] = up[i << 1] * up[i << 1 | 1];
414
      }
415
       vector<vector<int>> down(n * 2);
416
       down[1] = f % up[1];
417
       for (int i = 2; i < n * 2; ++i) {
418
419
        down[i] = down[i >> 1] % up[i];
      }
420
       vector<int> v(n);
421
422
      for (int i = 0: i < n: ++i) {
        v[i] = down[i + n][0];
423
424
      }
425
      return y;
426 }
427
     vector<int> interpolate(const vector<int> &x, const vector<int> &y) {
428
429
       int n = x.size():
      vector<vector<int>> up(n * 2);
430
      for (int i = 0; i < n; ++i) {
431
         up[i + n] = vector < int > {(mod - x[i]) % mod. 1}:
432
      }
433
```

```
434
      for (int i = n - 1: i: --i) {
435
        up[i] = up[i << 1] * up[i << 1 | 1];
436
437
       vector<int> a = evaluate(derivative(up[1]), x);
      for (int i = 0: i < n: ++i) {
438
439
        a[i] = mul(y[i], inv(a[i]));
440
441
       vector<vector<int>> down(n * 2):
442
      for (int i = 0; i < n; ++i) {
443
        down[i + n] = vector<int>(1, a[i]);
444
445
      for (int i = n - 1; i; --i) {
        down[i] = down[i << 1] * up[i << 1 | 1] + down[i << 1 | 1] * up[i << 1]:
446
447
448
      return down[1]:
449 }
450
451 int main() {
453 }
```

6.20 simplex.cpp

```
1 /**
   * Author: Stanford
   * Source: Stanford Notebook
   * License: MIT
  * Description: Solves a general linear maximization problem: maximize $c^T
         x$ subject to $Ax \le b$, $x \qe 0$.
6 * Returns -inf if there is no solution, inf if there are arbitrarily good
         solutions, or the maximum value of $c^T x$ otherwise.
7 * The input vector is set to an optimal $x$ (or in the unbounded case, an
         arbitrary solution fulfilling the constraints).
8 * Numerical stability is not quaranteed. For better performance, define
         variables such that $x = 0$ is viable.
    * Usage:
    * vvd A = {{1,-1}, {-1,1}, {-1,-2}};
   * vd b = \{1, 1, -4\}, c = \{-1, -1\}, x:
12 * T val = LPSolver(A, b, c).solve(x);
   * Time: O(NM * \#rivots). where a rivot may be e.a. an edge relaxation. O
         (2^n) in the general case.
14
    * Status: seems to work?
15
```

```
16
    typedef long double T; // long double, Rational, double + mod <P>...
    typedef vector <T> vd:
    typedef vector < vd > vvd;
20
    const T eps = 1e-8, inf = 1/.0;
    #define MP make pair
    #define ltj(X) if(s == -1 || MP(X[j],N[j]) < MP(X[s],N[s])) s=j
24
   struct LPSolver {
25
26
       int m, n;
27
       vector<int> N, B;
       vvd D:
28
29
30
       LPSolver(const vvd& A. const vd& b. const vd& c) :
31
            m(b.size()), n(c.size()), N(n+1), B(m), D(m+2, vd(n+2)) {
                for(int i = 0; i < m; i++){
32
                    for(int j = 0; j < n; j++){
34
                        D[i][j] = A[i][j];
                    }
35
36
37
                for(int i = 0: i < m: i++){
                    B[i] = n+i: D[i][n] = -1: D[i][n+1] = b[i]:
39
40
                for(int j = 0; j < n; j++){
41
                    N[j] = j; D[m][j] = -c[j];
42
               }
                N[n] = -1; D[m+1][n] = 1;
44
           }
45
46
       void pivot(int r, int s) {
47
           T *a = D[r].data(), inv = 1 / a[s];
           for(int i = 0; i < m+2; i++){
48
49
                if (i != r && abs(D[i][s]) > eps) {
                   T *b = D[i].data(), inv2 = b[s] * inv;
50
51
                    for(int j = 0; j < n+2; j++){
52
                        b[j] -= a[j] * inv2;
53
54
                    b[s] = a[s] * inv2;
55
               }
56
           }
57
           for(int j = 0; j < n+2; j++){
58
                if (j != s) D[r][j] *= inv;
```

```
59
             }
 60
             for(int i = 0; i < m+2; i++){
                 if (i != r) D[i][s] *= -inv;
 61
 62
             }
 63
             D[r][s] = inv;
64
             swap(B[r], N[s]);
 65
        }
 66
67
         bool simplex(int phase) {
 68
             int x = m + phase - 1;
 69
             for (;;) {
 70
                 int s = -1;
 71
                 for(int j = 0; j < n+1; j++){
 72
                     if (N[i] != -phase) lti(D[x]);
 73
                 }
 74
                 if (D[x][s] >= -eps) return true;
                 int r = -1;
 76
                 for(int i = 0; i < m; i++){
 77
                     if (D[i][s] <= eps) continue;</pre>
                     if (r == -1 \mid | MP(D[i][n+1] / D[i][s], B[i])
 78
                              < MP(D[r][n+1] / D[r][s], B[r])) r = i;
 79
                 if (r == -1) return false:
                 pivot(r, s);
 83
             }
 84
        }
         T solve(vd &x) {
87
             int r = 0;
             for(int i = 1: i < m: i++){
                 if (D[i][n+1] < D[r][n+1]) r = i;
             }
             if (D[r][n+1] < -eps) {
91
 92
                 pivot(r, n);
93
                 if (!simplex(2) || D[m+1][n+1] < -eps) return -inf;</pre>
 94
                 for(int i = 0; i < m; i++) if (B[i] == -1) {
 95
                     int s = 0:
 96
                     for(int j = 1; j < n+1; j++){
97
                         ltj(D[i]);
98
                     }
                     pivot(i, s);
100
                 }
101
             }
```

```
102 bool ok = simplex(1); x = vd(n);

103 for(int i = 0; i < m; i++){

104 if (B[i] < n) x[B[i]] = D[i][n+1];

105 }

106 return ok ? D[m][n+1] : inf;

107 }

108 };
```

6.21 区间互质.cpp

```
1 int p[N / 5], num;
2 void prime(int n) {
        num = 0;
        for (int i = 2; i * i <= n; i++) {
            if ((n % i) == 0) {
                p[++num] = i;
                while ((n \% i) == 0) n /= i;
            }
       }
9
10
        if (n > 1) p[++num] = n;
11 }
12 11 solve(11 r, int k) {
        prime(k);
13
        11 \text{ res} = 0;
14
15
        for (int i = 1; i < (1 << num); i++) {
           int k = 0;
16
17
           ll div = 1;
            for (int j = 1; j <= num; j++) {
18
                if (i & (1 << (j - 1))) {
19
20
                   k++:
21
                    div *= p[i];
               }
22
23
            }
            if (k % 2)
24
25
                res += r / div;
            else
26
27
                res -= r / div;
28
        }
29
        return r - res;
30 }
31 11 que(11 L, 11 R, 11 k) {
        return solve(R, k) - solve(L - 1, k);
33 }
```

6.22 幂转下降幂 (求幂和).cpp

```
1 ll comb[N][N];
2 11 s[maxn], inv[maxn], p;
3 // 1^k+2^k+...+n^k
4 void solve() {
       cin >> k >> n >> p;
       rep(i, 0, k + 1) {
           comb[i][0] = comb[i][i] = 1;
           rep(j, 1, i - 1) {
                comb[i][j] = (comb[i - 1][j - 1] + comb[i - 1][j]) % p;
10
           }
11
       }
12
       inv[1] = 1;
13
       rep(i, 2, k + 1) inv[i] = (p - p / i) * inv[p % i] % p;
14
       assert(inv[k] * k % p == 1);
15
16
       11 pw = 1;
17
       //(k+1)*S[k]=(n+1)^{(k+1)}-[0-k-1](k+1,j)*S[j]-1
18
       rep(i, 0, k) {
19
           pw = pw * (n + 1) % p;
20
           s[i] = (pw - 1 + p) \% p;
21
           rep(i, 0, i - 1) {
22
                s[i] = (s[i] - comb[i + 1][j] * s[j] % p + p) % p;
24
           s[i] = s[i] * inv[i + 1] % p;
25
       }
26
       cout << s[k] << '\n';
27 }
```

6.23 扩展欧拉定理.cpp

```
1 // mod \{min(b, b \% phi + phi)\}
2 ll calc(ll p) {
       if (p == 1) return 0;
       int phi = p, q = p;
       for (int i = 2; i * i <= p; i++) {
6
           if (q % i == 0) {
7
               phi = phi / i * (i - 1);
               while (q \% i == 0) q /= i;
9
           }
10
       }
11
       if (q != 1) phi = phi / q * (q - 1);
12
       return powmod(2, calc(phi) + phi, p);
```

```
13 }
```

6.24 拉格朗日插值.cpp

```
1 // k阶多项式(需要k+1个点)
2 // 求在点n上的值
3 // O(k)
4 ll lagrange(ll n, int k) {
       vector<11> x(k + 5), y(k + 5);
       rep(i, 1, k + 1) {
          x[i] = i:
           // y[i] = (y[i-1] + powmod(i,k-1,mod)) \% mod;
       }
9
10
       if (n <= k + 1) return y[n];
11
       vector<ll> fac(k + 5);
13
       fac[0] = 1;
       ll coe = 1;
14
       rep(i, 1, k + 4) fac[i] = fac[i - 1] * i % mod;
15
       rep(i, 1, k + 1) coe = coe * (n - i + mod) % mod;
       ll ans = 0:
17
       rep(i, 1, k + 1) {
18
           ll sgn = (((k + 1 - i) \% 2) ? -1 : 1);
19
20
           11 f1 = powmod(fac[i - 1] * fac[k + 1 - i] % mod, mod - 2, mod);
           11 f2 = powmod(n - i, mod - 2, mod);
           ans += sgn * coe * f1 % mod * f2 % mod * y[i] % mod;
23
           ans = (ans + mod) \% mod;
24
       }
25
       return ans;
26 }
```

6.25 整除分块.cpp

```
void solve() {
    u64 ans = 0;
    cin >> n;

for (ll l = 1; l <= n; l++) {
    ll d = n / l, r = n / d;
    ans += (l + r) * (r - l + 1) / 2 * d;
    l = r;
}
</pre>
```

6.26 枚举子集.cpp

```
1 void solve() {
2     f[0] = 1;
3     for (int i = 1; i < (1ll << n); i++) {
4         int t = i;
5         ll res = 0;
6         while (true) {
7             if (t == 0) break;
8             t = (t - 1)&i;
9             res = (res + f[t]) % mod;
10         }
11         f[i] = res * i;
12     }
13 }</pre>
```

6.27 枚举超集.cpp

```
void solve() {
   for (int i = 1; i < (111 << n); i++) {
      int t = i;
      while (true) {
            t = (t + 1) | i;
            if (t == bit(n) - 1) break;
      }
   }
}</pre>
```

6.28 狄利克雷卷积.cpp

```
const int N = 1010000;
int p[N], pr[N / 5], n, tot;
unsigned int A, B, C, mu[N], f[N], g[N];

inline unsigned int rng61() {
    A ^= A << 16;
    A ^= A >> 5;
    A ^= A << 1;
    unsigned int t = A;
    A = B;
    B = C;
    C ^= t ^ A;
    return C;</pre>
```

```
15
16 int main() {
17
        scanf("%d%u%u%u", &n, &A, &B, &C);
        for (int i = 1; i <= n; i++)
18
19
            f[i] = rng61();
20
21
        p[1] = 1; mu[1] = 1;
22
        for (int i = 2; i <= n; i++) {
            if (!p[i]) p[i] = i, mu[i] = (uint)-1, pr[++tot] = i;
23
24
            for (int j = 1; j \le tot && pr[j] * i \le n; j++) {
25
                p[i * pr[j]] = pr[j];
                if (p[i] == pr[j]) {
26
27
                    mu[i * pr[j]] = 0;
28
                    break:
                } else {
                    mu[i * pr[j]] = (uint)-mu[i];
31
32
            }
       }
33
34
        for (int d1 = 1; d1 \le n; d1++)
            for (int d2 = 1; d1 * d2 <= n; d2++)
35
36
                g[d1 * d2] += f[d1] * mu[d2];
37
        uint ans = 0;
38
        for (int i = 1; i <= n; i++) ans ^= g[i];
39
        printf("%u\n", ans);
40 }
```

6.29 线性筛常见积性函数.cpp

14 }

```
1 const int N = 20010000;
2 int p[N], pr[N / 5], n, pe[N], tot;
3 uint f[N], a, b, ans;
4
5 void compute(int n, function<void(int)> calcpe) {
6 ans = 0;
7 f[1] = 1;
8 for (int i = 2; i <= n; i++) {
9 if (i == pe[i])
10 calcpe(i);
11 else
12 f[i] = f[pe[i]] * f[i / pe[i]];
13 }</pre>
```

```
14
       for (uint i = 1; i <= n; i++) {
15
           ans \hat{} = (a * i * f[i] + b);
16
17
       printf("%u\n", ans);
18 }
19
   int main() {
       scanf("%d%u%u", &n, &a, &b);
       p[1] = 1;
       for (int i = 2; i <= n; i++) {
23
24
           if (!p[i]) p[i] = i, pe[i] = i, pr[++tot] = i;
25
           for (int j = 1; j <= tot && pr[j] * i <= n; j++) {
26
                p[i * pr[j]] = pr[j];
27
               if (p[i] == pr[j]) {
                    pe[i * pr[j]] = pe[i] * pr[j];
28
29
                    break;
               } else {
31
                    pe[i * pr[j]] = pr[j];
           }
33
34
       // 因子个数,因子和,欧拉函数,莫比乌斯函数
35
        compute(n, [&](int x) {
37
           f[x] = f[x / p[x]] + 1;
38
       }):
39
       compute(n, [&](int x) {
41
           f[x] = f[x / p[x]] + x;
42
       });
43
44
        compute(n, [&](int x) {
45
           f[x] = x / p[x] * (p[x] - 1);
46
       });
47
48
        compute(n, [&](int x) {
49
           f[x] = x == p[x] ? -1 : 0;
       });
51 }
```

6.30 莫比乌斯反演 gcd 常见结论.cpp

```
1 // u * 1 = e, phi * 1 = id, phi = id * u
2 const int N = 10100000, M = 10000000;
```

```
3 int p[N], pr[N / 5], n, tot;
4 int mu[N], smu[N];
6 int main() {
       p[1] = 1; mu[1] = 1;
       for (int i = 2; i <= M; i++) {
            if (!p[i]) p[i] = i, mu[i] = -1, pr[++tot] = i;
            for (int j = 1; j <= tot && pr[j] * i <= M; j++) {
10
11
                p[i * pr[j]] = pr[j];
                if (p[i] == pr[j]) {
12
13
                    mu[i * pr[j]] = 0;
                    break;
14
15
               } else {
16
                    mu[i * pr[i]] = -mu[i];
               }
17
            }
18
19
20
       for (int i = 1; i <= M; i++)
21
            smu[i] = smu[i - 1] + mu[i];
22
       int T:
23
       scanf("%d", &T);
       for (int tc = 0; tc < T; tc++) {
24
25
            int n. m:
26
            scanf("%d%d", &n, &m);
27
            if (n > m) swap(n, m);
28
            11 \text{ ans} = 0;
            for (int 1 = 1; 1 <= n; 1++) {
29
                int n1 = n / 1, m1 = m / 1;
30
31
                int r = min(n / n1, m / m1);
                // l ... r
32
33
                ans += 111 * (smu[r] - smu[1 - 1]) * n1 * m1;
34
               1 = r;
            }
35
36
            printf("%lld\n", ans);
37
       }
38 }
```

7 String

7.1 ACAM.cpp

```
1 const int AC_SIGMA = 26, AC_V = 26, AC_N = 810000;
```

```
2 struct AC_automaton {
         struct node {
             node *go[AC_V], *fail, *f;
   // declare extra variables:
        } pool[AC_N], *cur, *root, *q[AC_N];
        node* newnode() {
             node *p = cur++;
    // init extra variables:
             return p;
11
        }
12 // CALL init() and CHECK all const variables:
        void init() { cur = pool; root = newnode(); }
14
        node* append(node *p, int w) {
15
             if (!p->go[w]) p->go[w] = newnode(), p->go[w]->f = p;
16
             return p->go[w];
17
        }
18
        void build() {
19
             int t = 0:
20
            q[t++] = root;
21
            root->fail = root;
22
             rep(i, 0, AC_SIGMA - 1) if (root->go[i]) {
                 a[t++] = root->go[i];
24
                 root->go[i]->fail = root;
25
            } else {
26
                 root->go[i] = root;
27
             rep(i, 1, t - 1) {
                 node *u = q[i];
30
                 rep(j, 0, AC_SIGMA - 1) if (u->go[j]) {
31
                      u \rightarrow go[j] \rightarrow fail = u \rightarrow fail \rightarrow go[j];
32
                     q[t++] = u->go[j];
33
                 } else {
34
                     u \rightarrow go[j] = u \rightarrow fail \rightarrow go[j];
36
            }
        }
   typedef AC_automaton::node ACnode;
40
41 const int M = 2, N = 2.1e5;
42 struct node {
43
        node *son[M], *go[M], *fail;
44
        int cnt, vis, ins;
```

```
45 } pool[N], *cur = pool, *q[N], *root;
47 node *newnode() { return cur++; }
    int t, n;
49
    void build() {
51
         t = 0;
         q[t++] = root;
52
53
         for (int i = 0; i < t; i++) {
              node *u = q[i];
54
55
              for (int j = 0; j < M; j++) {
                   if (u->son[i]) {
56
                       u \rightarrow go[j] = u \rightarrow son[j];
57
58
                       if (u != root)
                            u \rightarrow go[j] \rightarrow fail = u \rightarrow fail \rightarrow go[j];
59
60
                        else
                            u->go[j]->fail = root;
61
62
                       q[t++] = u->son[j];
63
                  } else {
                       if (u != root)
64
                            u \rightarrow go[j] = u \rightarrow fail \rightarrow go[j];
66
                            u \rightarrow go[j] = root;
67
68
                  }
69
              }
70
71 }
72
73
    void insert(string &s) {
74
         node *cur = root:
75
         for (auto c : s) {
76
              int w = c - '0':
77
              if (!cur->son[w]) {
78
                   cur->son[w] = newnode();
              }
79
80
              cur = cur->son[w];
         }
81
82
         cur -> cnt = 1;
83 }
```

7.2 hash61.cpp

```
1 struct hash61 {
```

```
static const uint64_t md = (1LL << 61) - 1;
     static uint64 t step;
4
     static vector < uint 64_t > pw;
5
     uint64_t addmod(uint64_t a, uint64_t b) const {
       a += b:
       if (a >= md) a -= md;
       return a:
10
11
12
      uint64_t submod(uint64_t a, uint64_t b) const {
13
       a += md - b;
14
       if (a >= md) a -= md:
15
       return a;
16
     }
17
18
      uint64 t mulmod(uint64 t a, uint64 t b) const {
19
        uint64_t 11 = (uint32_t) a, h1 = a >> 32, 12 = (uint32_t) b, h2 = b >>
            32;
20
       uint64 t l = 11 * 12. m = 11 * h2 + 12 * h1. h = h1 * h2:
        uint64 t ret = (1 \& md) + (1 >> 61) + (h << 3) + (m >> 29) + (m << 35 >>
21
             3) + 1:
       ret = (ret & md) + (ret >> 61):
22
       ret = (ret & md) + (ret >> 61);
24
       return ret - 1:
25
26
27
      void ensure_pw(int sz) {
28
       int cur = (int) pw.size();
29
       if (cur < sz) {
          pw.resize(sz);
31
          for (int i = cur; i < sz; i++) {
            pw[i] = mulmod(pw[i - 1], step);
32
33
         }
34
       }
35
36
37
      vector<uint64_t> pref;
38
     int n;
39
40
     template < typename T>
41
     hash61(const T& s) {
42
       n = (int) s.size();
```

```
ensure_pw(n + 1);
43
       pref.resize(n + 1);
44
       pref[0] = 1;
45
       for (int i = 0; i < n; i++) {
46
         pref[i + 1] = addmod(mulmod(pref[i], step), s[i]);
       }
48
     }
49
50
     inline uint64 t operator()(const int from, const int to) const {
51
       assert(0 <= from && from <= to && to <= n - 1):
52
53
       return submod(pref[to + 1], mulmod(pref[from], pw[to - from + 1]));
     }
55 }:
56
57 uint64_t hash61::step = (md >> 2) + rng() % (md >> 1);
   vector<uint64_t> hash61::pw = vector<uint64_t>(1, 1);
```

7.3 kmp.cpp

```
1 template <typename T>
   vector<int> kmp_table(int n, const T &s) {
      vector<int> p(n, 0);
     int k = 0:
     for (int i = 1; i < n; i++) {
       while (k > 0 \&\& !(s[i] == s[k])) {
         k = p[k - 1];
       if (s[i] == s[k]) {
         k++;
11
       }
       p[i] = k:
13
14
      return p;
15 }
   template <typename T>
   vector<int> kmp_table(const T &s) {
      return kmp_table((int) s.size(), s);
20 }
21
   template <typename T>
23 vector<int> kmp_search(int n, const T &s, int m, const T &w, const vector<
        int> &p) {
```

```
24
     assert(n >= 1 && (int) p.size() == n);
     vector<int> res;
     int k = 0:
27
     for (int i = 0; i < m; i++) {
28
       while (k > 0 && (k == n || !(w[i] == s[k]))) {
29
         k = p[k - 1];
       }
       if (w[i] == s[k]) {
         k++;
33
       }
       if (k == n) {
         res.push back(i - n + 1);
36
37
     }
     return res:
     // returns 0-indexed positions of occurrences of s in w
40 }
41
42 template <typename T>
43 vector<int> kmp_search(const T &s, const T &w, const vector<int> &p) {
      return kmp_search((int) s.size(), s, (int) w.size(), w, p);
45 }
```

7.4 manacherfast.cpp

```
1 template <typename T>
2 vector<int> manacher(int n, const T &s) {
     if (n == 0) {
       return vector<int>();
     vector<int> res(2 * n - 1, 0):
     int 1 = -1, r = -1;
     for (int z = 0: z < 2 * n - 1: z++) {
       int i = (z + 1) >> 1;
       int i = z \gg 1:
       int p = (i \ge r ? 0 : min(r - i, res[2 * (1 + r) - z]));
11
       while (j + p + 1 < n \&\& i - p - 1 >= 0) {
13
         if (!(s[j + p + 1] == s[i - p - 1])) {
14
           break;
         }
16
          p++;
17
18
       if (j + p > r) {
```

```
1 = i - p;
         r = j + p;
        res[z] = p;
     }
24
     return res:
     // res[2 * i] = odd radius in position i
      // res[2*i+1] = even radius between positions i and i+1
     // s = "abaa" \rightarrow res = \{0, 0, 1, 0, 0, 1, 0\}
     // in other words, for every z from 0 to 2 * n - 2:
     // calculate i = (z + 1) \gg 1 and j = z \gg 1
     // now there is a palindrome from i - res[z] to j + res[z]
     // (watch out for i > j and res[z] = 0)
31
32 }
33
   template <typename T>
   vector<int> manacher(const T &s) {
      return manacher((int) s.size(), s):
37 }
```

7.5 MinRotation.cpp

```
Description: Finds the lexicographically smallest rotation of a string.
Usage: rotate(v.begin(), v.begin() + minRotation(v), v.end());
Time: O (N)

int minRotation(string s) {
   int a = 0, N = sz(s); s += s;
   rep(b, 0, N) rep(k, 0, N) {
        if (a + k == b || s[a + k] < s[b + k]) {b += max(0, k - 1); break;}
        if (s[a + k] > s[b + k]) { a = b; break; }

return a;
}
```

7.6 PAM.cpp

```
1 struct PAM {
2    struct T {
3         array<int, 10> tr;
4         int fail, len, tag;
5         T() : fail(0), len(0), tag(0) {
6         tr.fill(0);
```

```
};
        vector<T> t:
10
       vector<int> stk;
11
        int newnode(int len) {
12
            t.emplace_back();
13
           t.back().len = len;
14
            return (int)t.size() - 1;
15
       }
16
       PAM() : t(2) {
17
            t[0].fail = 1, t[0].len = 0;
18
            t[1].fail = 0, t[1].len = -1;
19
            stk.push_back(-1);
20
       }
21
       int getfail(int v) {
22
            while (stk.end()[-2 - t[v].len] != stk.back()) {
23
                v = t[v].fail;
24
25
            return v;
       }
26
27
        int insert(int lst, int c, int td) {
            stk.emplace_back(c);
29
            int x = getfail(lst);
           if (!t[x].tr[c]) {
30
31
                int u = newnode(t[x].len + 2);
32
                t[u].fail = t[getfail(t[x].fail)].tr[c];
                t[x].tr[c] = u;
34
35
            t[t[x].tr[c]].tag += td;
36
            return t[x].tr[c]:
37
38
       int build(int n) {
39
            int ans = 0:
            for (int i = (int)t.size() - 1; i > 1; i--) {
40
41
                t[t[i].fail].tag += t[i].tag;
42
                if (t[i].len > n) {
                    continue:
44
                ans = (ans + 111 * t[i].tag * t[i].tag % M * t[i].len) % M;
46
            return ans;
49 };
```

7.7 rollingHash.cpp

```
typedef pair<int,int> hashv;
    const ll mod1=1000000007;
   const 11 mod2=1000000009;
   // prefixSum trick for high dimensions
   hashv operator + (hashv a, hashv b) {
       int c1=a.fi+b.fi,c2=a.se+b.se;
       if (c1>=mod1) c1-=mod1;
       if (c2>=mod2) c2-=mod2:
10
11
       return mp(c1,c2);
12 }
13
14 hashv operator - (hashv a, hashv b) {
        int c1=a.fi-b.fi.c2=a.se-b.se:
15
       if (c1<0) c1+=mod1;
16
       if (c2<0) c2+=mod2;
17
       return mp(c1,c2);
18
19 }
20
   hashv operator * (hashv a, hashv b) {
22
        return mp(111*a.fi*b.fi%mod1,111*a.se*b.se%mod2);
23 }
```

7.8 SA.cpp

```
#include <bits/stdc++.h>
   using namespace std;
4 const int N = 101000:
5 \quad char s[N];
6 int sa[N], rk[N], ht[N], n:
   // O-based sa 表示第i大的为哪个, rk 表示第i个后缀第几大
8 // ht表示 lcp(sa[i], sa[i-1])
   void buildSA(char *s, int *sa, int *rk, int *ht, int n, int m = 128) {
10
       static int x[N], y[N], c[N];
       s[n] = 0:
11
       for (int i = 0; i < m; i++) c[i] = 0;
12
       for (int i = 0: i < n: i++) c[x[i] = s[i]]++:
13
14
       for (int i = 1; i < m; i++) c[i] += c[i-1];
15
       for (int i = n - 1; i \ge 0; i--) sa[--c[x[i]]] = i;
       for (int k = 1: k < n: k <<= 1) {
16
```

```
17
            int p=0;
18
            for (int i = n - 1; i \ge n - k; i--) y[p++] = i;
            for (int i = 0; i < n; i++) if (sa[i] >= k) y[p++] = sa[i] - k;
19
20
            for (int i = 0; i < m; i++) c[i] = 0;
            for (int i = 0: i < n: i++) c[x[v[i]]]++:
21
22
            for (int i = 1; i < m; i++) c[i] += c[i - 1];
23
            for (int i = n - 1; i \ge 0; i--) sa[--c[x[y[i]]]] = y[i];
24
            swap(x, v):
25
           p = 1; x[sa[0]] = 0; y[n] = -1;
            for (int i = 1: i < n: i++) {
26
27
                if (y[sa[i-1]] == y[sa[i]] && y[sa[i-1] + k] == y[sa[i] + k]
                    x[sa[i]] = p - 1;
28
29
                else
                    x[sa[i]] = p++;
31
32
            if (p == n) break;
34
       }
       for (int i = 0: i < n: i++) rk[sa[i]] = i:
       int k = 0:
37
       for (int i = 0: i < n: i++) {
           k = max(k - 1, 0):
39
            if (rk[i] == 0) continue;
40
            int j = sa[rk[i] - 1];
41
            while (s[i + k] == s[j + k]) k++;
            ht[rk[i]] = k:
       }
44 }
46 int LCP(int u, int v) {
       if (u == v) return n - u;
       if (rk[u] > rk[v]) swap(u, v);
49
       // RMQ(ht, rk[u] + 1, rk[v])
50 }
51
52 int main() {
       scanf("%s", s);
54
       n = strlen(s);
55
       buildSA(s, sa, rk, ht, n);
       for (int i = 0; i < n; i++) printf("%d<sub>i</sub>,", sa[i] + 1); puts("");
       for (int i = 1; i < n; i++) printf("%d", ht[i]); puts("");
58 }
```

7.9 SAfast.cpp

```
template <typename T>
    vector<int> suffix_array(int n, const T &s, int char_bound) {
      vector<int> a(n);
     if (n == 0) {
       return a:
     if (char bound !=-1) {
       vector<int> aux(char_bound, 0);
       for (int i = 0; i < n; i++) {
10
          aux[s[i]]++:
       }
11
12
       int sum = 0;
13
       for (int i = 0; i < char_bound; i++) {</pre>
          int add = aux[i];
14
15
         aux[i] = sum:
16
         sum += add;
       }
17
18
       for (int i = 0; i < n; i++) {
         a[aux[s[i]]++] = i;
19
       }
20
     } else {
21
22
       iota(a.begin(), a.end(), 0);
23
        sort(a.begin(), a.end(), [&s](int i, int j) { return s[i] < s[j]; });
     }
24
     vector<int> sorted_by_second(n);
25
26
     vector<int> ptr group(n);
     vector<int> new_group(n);
27
28
     vector<int> group(n);
     group[a[0]] = 0:
29
     for (int i = 1; i < n; i++) {
30
       group[a[i]] = group[a[i - 1]] + (!(s[a[i]] == s[a[i - 1]]));
31
32
33
     int cnt = group[a[n - 1]] + 1;
      int step = 1:
34
      while (cnt < n) {
35
36
       int at = 0;
       for (int i = n - step: i < n: i++) {
37
38
         sorted_by_second[at++] = i;
       }
39
40
       for (int i = 0; i < n; i++) {
41
         if (a[i] - step >= 0) {
42
            sorted_by_second[at++] = a[i] - step;
```

```
43
         }
44
       }
45
       for (int i = n - 1; i \ge 0; i--) {
46
          ptr_group[group[a[i]]] = i;
47
       }
48
       for (int i = 0; i < n; i++) {
         int x = sorted by second[i];
          a[ptr_group[group[x]]++] = x;
50
       }
51
52
       new_group[a[0]] = 0;
       for (int i = 1; i < n; i++) {
54
         if (group[a[i]] != group[a[i - 1]]) {
           new_group[a[i]] = new_group[a[i - 1]] + 1;
55
56
         } else {
57
           int pre = (a[i - 1] + step >= n ? -1 : group[a[i - 1] + step]);
           int cur = (a[i] + step >= n ? -1 : group[a[i] + step]);
           new group[a[i]] = new group[a[i - 1]] + (pre != cur);
         }
60
61
       }
       swap(group, new_group);
       cnt = group[a[n - 1]] + 1;
       step <<= 1:
64
65
     }
     return a;
67 }
68
   template <typename T>
   vector<int> suffix_array(const T &s, int char_bound) {
71
      return suffix_array((int) s.size(), s, char_bound);
72 }
73
   template <typename T>
    vector<int> build_lcp(int n, const T &s, const vector<int> &sa) {
76
     assert((int) sa.size() == n);
     vector<int> pos(n);
77
78
     for (int i = 0; i < n; i++) {
79
       pos[sa[i]] = i;
80
     vector<int> lcp(max(n - 1, 0));
81
     int k = 0:
     for (int i = 0; i < n; i++) {
       k = max(k - 1, 0);
       if (pos[i] == n - 1) {
```

```
k = 0:
       } else {
        int j = sa[pos[i] + 1];
        k++:
        }
91
        lcp[pos[i]] = k;
94
     }
95
     return lcp;
96 }
97
   template <typename T>
    vector<int> build lcp(const T &s, const vector<int> &sa) {
     return build_lcp((int) s.size(), s, sa);
100
101 }
```

7.10 SAM.cpp

```
struct SAM {
        static constexpr int ALPHABET_SIZE = 26;
        struct Node {
            int len:
            int link;
            std::array<int, ALPHABET SIZE> next;
            Node() : len{}, link{}, next{} {}
       };
       std::vector<Node> t:
10
       SAM() {
            init():
11
12
       }
13
       void init() {
            t.assign(2, Node());
14
15
            t[0].next.fill(1);
            t[0].len = -1:
16
17
       }
18
       int newNode() {
19
            t.emplace_back();
20
            return t.size() - 1;
21
       }
22
       int extend(int p, int c) {
23
            if (t[p].next[c]) {
24
                int q = t[p].next[c];
```

```
25
                if (t[q].len == t[p].len + 1) {
26
                    return q;
                }
27
28
                int r = newNode();
                t[r].len = t[p].len + 1;
29
30
                t[r].link = t[q].link;
31
                t[r].next = t[q].next;
                t[q].link = r;
                while (t[p].next[c] == q) {
33
                    t[p].next[c] = r;
34
35
                    p = t[p].link;
36
37
                return r:
            }
            int cur = newNode():
39
            t[cur].len = t[p].len + 1;
            while (!t[p].next[c]) {
41
                t[p].next[c] = cur;
                p = t[p].link;
44
45
            t[cur].link = extend(p, c);
            return cur:
47
       }
48 };
```

7.11 SA-IS.cpp

```
* Time Complexity: Suffix Array: O(N + Character_Set_Size) time and space
         //
    128 --- ASCII
                        LCP: O(N) time and space
    * Usage:
            1. Suffix Array (returns s.size() elements, NOT considering
     0-length/empty suffix)
                   auto sa = suffix_array(s); // s is the input string with
         ASCII
    characters
                   auto sa_wide_char = suffix_array(s, LIM); // LIM = max(s[i])
         + 2.
11
    s is the string with arbitary big characters.
12
             2. LCP:
13
                  auto lcp = LCP(s, suffix array(s)); // returns s.size()
```

```
elements.
           where lcp[i]=LCP(sa[i], sa[i+1])
        * Status: Tested (DMOJ: ccc03s4. SPOJ: SARRAY (100pts). Yosupo's: Suffix
          & Number of Substrings, CodeForces EDU
          */
17
         // Based on: Rickypon, https://judge.yosupo.jp/submission/10105
          void induced sort(const std::vector<int>& vec, int val_range,
20
                                                  std::vector<int>& SA, const std::vector<bool>& sl,
21
                                                  const std::vector<int>& lms idx) {
22
                  std::vector<int> l(val range, 0), r(val range, 0);
23
                  for (int c : vec) {
                          if (c + 1 < val_range) ++1[c + 1];
24
25
                           ++r[c]:
26
                 }
27
                  std::partial sum(l.begin(), l.end(), l.begin());
28
                  std::partial sum(r.begin(), r.end(), r.begin());
29
                  std::fill(SA.begin(), SA.end(), -1):
                  for (int i = (int)lms idx.size() - 1; i >= 0; --i)
30
                           SA[--r[vec[lms idx[i]]]] = lms idx[i]:
31
32
                  for (int i : SA)
33
                           if (i \ge 1 \&\& sl[i - 1]) SA[l[vec[i - 1]]++] = i - 1:
34
                  std::fill(r.begin(), r.end(), 0):
35
                  for (int c : vec) ++r[c];
36
                  std::partial sum(r.begin(), r.end(), r.begin());
                  for (int k = (int)SA.size() - 1, i = SA[k]; k \ge 1; k \ge 1;
37
38
                           if (i >= 1 && !sl[i - 1]) {
                                    SA[--r[vec[i - 1]]] = i - 1;
39
                           }
41 }
42
         std::vector<int> SA IS(const std::vector<int>& vec. int val range) {
44
                  const int n = vec.size():
45
                  std::vector<int> SA(n). lms idx:
46
                  std::vector<bool> sl(n):
47
                  sl[n - 1] = false:
                  for (int i = n - 2: i \ge 0: --i) {
48
                           sl[i] = (vec[i] > vec[i + 1] || (vec[i] == vec[i + 1] && sl[i + 1]))
49
50
                           if (sl[i] && !sl[i + 1]) lms_idx.push_back(i + 1);
                 }
51
52
                  std::reverse(lms_idx.begin(), lms_idx.end());
53
                  induced sort(vec, val range, SA, sl, lms idx);
```

```
54
        std::vector<int> new_lms_idx(lms_idx.size()), lms_vec(lms_idx.size());
55
        for (int i = 0, k = 0; i < n; ++i)
56
            if (!sl[SA[i]] \&\& SA[i] >= 1 \&\& sl[SA[i] - 1]) {
57
                new lms idx[k++] = SA[i];
            }
58
        int cur = 0:
59
        SA[n - 1] = cur;
61
        for (size t k = 1: k < new lms idx.size(): ++k) {</pre>
62
            int i = new lms idx[k - 1], j = new lms idx[k];
63
            if (vec[i] != vec[i]) {
64
                SA[i] = ++cur;
65
                continue;
            }
66
67
            bool flag = false;
68
            for (int a = i + 1, b = i + 1:: ++a, ++b) {
                if (vec[a] != vec[b]) {
70
                    flag = true;
                    break:
72
73
                if ((!sl[a] && sl[a - 1]) || (!sl[b] && sl[b - 1])) {
                     flag = !((!sl[a] \&\& sl[a - 1]) \&\& (!sl[b] \&\& sl[b - 1]));
74
75
                    break:
                }
76
77
78
            SA[i] = (flag ? ++cur : cur):
79
80
        for (size_t i = 0; i < lms_idx.size(); ++i) lms_vec[i] = SA[lms_idx[i]];</pre>
81
        if (cur + 1 < (int)lms idx.size()) {</pre>
82
            auto lms_SA = SA_IS(lms_vec, cur + 1);
83
            for (size t i = 0: i < lms idx.size(): ++i) {</pre>
84
                new lms idx[i] = lms idx[lms SA[i]];
85
            }
       }
86
        induced sort(vec, val range, SA, sl, new lms idx);
        return SA:
89 }
90
    std::vector<int> suffix array(const std::string& s, const char first = 'a',
92
                              const char last = |z|) {
93
        std::vector<int> vec(s.size() + 1):
94
        std::copy(std::begin(s), std::end(s), std::begin(vec));
95
        for (auto& x : vec) x = (int)first - 1:
        vec.back() = 0;
```

```
auto ret = SA_IS(vec, (int)last - (int)first + 2);
 97
         ret.erase(ret.begin());
 98
 99
         return ret:
100 }
101 // Author: https://codeforces.com/bloq/entry/12796?#comment-175287
     // Uses kasai's algorithm linear in time and space
     std::vector<int> LCP(const std::string& s, const std::vector<int>& sa) {
103
         int n = s.size(), k = 0;
104
105
         std::vector<int> lcp(n), rank(n);
         for (int i = 0: i < n: i++) rank[sa[i]] = i:</pre>
106
         for (int i = 0; i < n; i++, k ? k-- : 0) {
107
             if (rank[i] == n - 1) {
108
                 k = 0:
109
110
                 continue;
             }
111
             int j = sa[rank[i] + 1];
112
             while (i + k < n \&\& j + k < n \&\& s[i + k] == s[j + k]) k++;
113
114
             lcp[rank[i]] = k:
115
        }
        lcp[n-1] = 0;
116
117
         return lcp;
118 }
119
     template <typename T, class F = function<T(const T&, const T&)>>
120
     class SparseTable {
121
      public:
122
123
      int n;
124
       vector<vector<T>> mat;
125
      F func;
126
       SparseTable(const vector < T > & a, const F & f) : func(f) {
127
128
         n = static_cast<int>(a.size());
         int max log = 32 - builtin clz(n);
129
130
         mat.resize(max_log);
         mat[0] = a;
131
132
         for (int j = 1; j < max_log; j++) {
           mat[j].resize(n - (1 << j) + 1);
133
           for (int i = 0; i \le n - (1 \le j); i++) {
134
135
             mat[j][i] = func(mat[j-1][i], mat[j-1][i+(1 << (j-1))]);
          }
136
        }
137
      }
138
```

139

```
140 T get(int from, int to) const {
141    assert(0 <= from && from <= to && to <= n - 1);
142    int lg = 32 - __builtin_clz(to - from + 1) - 1;
143    return func(mat[lg][from], mat[lg][to - (1 << lg) + 1]);
144   }
145 };
```

7.12 Z.cpp

```
1 template <typename T>
2 vector<int> z function(int n, const T &s) {
     vector<int> z(n, n);
     int 1 = 0, r = 0;
    for (int i = 1; i < n; i++) {
       z[i] = (i > r ? 0 : min(r - i + 1, z[i - 1]));
       while (i + z[i] < n \&\& s[z[i]] == s[i + z[i]]) {
8
         z[i]++;
9
       }
10
       if (i + z[i] - 1 > r) {
11
        1 = i:
         r = i + z[i] - 1;
12
       }
13
14
     return z;
16 }
17
18 template <typename T>
19 vector<int> z function(const T &s) {
     return z function((int) s.size(), s);
21 }
```

8 Basic

8.1 AST.py

```
class Solution:
def calculate(self, s: str) -> int:
sign = ['+', '-', '*', '/', '(', ')']
v = []
num = ''
for c in s:
if c in sign:
```

```
8
                    if num:
                         v.append(num)
                         num = ''
10
11
                    if c == '-' and (not v or v[-1] == '('):
12
                        v.append('0')
13
                    v.append(c)
14
                elif c.isnumeric():
                     num += c
15
16
            if num:
                v.append(num)
17
18
            stk0 = []
19
            stk1 = []
20
21
            for e in v:
22
                if e.isnumeric():
23
                    stk0.append(e)
                elif e in ['+', '-']:
24
                     while stk1 and stk1[-1] in ['*', '/', '+', '-']:
25
                         stk0.append(stk1.pop())
27
                    stk1.append(e)
                elif e in ['*', '/', '(']:
28
                    stk1.append(e)
29
30
                else:
31
                     while stk1 and stk1[-1] != '(':
32
                         stk0.append(stk1.pop())
33
                     stk1.pop()
            while stk1:
34
35
                stk0.append(stk1.pop())
36
37
            res = []
38
            for e in stk0:
39
                if e.isnumeric():
                    res.append(int(e))
40
41
                else:
42
                    v = res.pop()
43
                    u = res.pop()
                    if e == '+':
                        res.append(u + v)
                    if e == '-':
                        res.append(u - v)
47
                    if e == '*':
48
49
                         res.append(u * v)
50
                    if e == '/':
```

```
51
                        res.append(u // v)
52
            return res[0]
```

8.2 bitset.cpp

```
1 template <int len = 1>
2 void solve(int n) {
        if (n > len) {
4
            solve<std::min(len*2, MAXLEN)>(n);
5
            return;
       }
6
        // solution using bitset < len>
8 }
9
    struct Bitset {
        vector<ull> b:
12
        int n;
       Bitset(int x = 0) {
13
14
            n = x;
15
            b.resize((n + 63) / 64, 0);
16
       }
17
18
       int get(int x) {
19
            return (b[x >> 6] >> (x & 63)) & 1;
20
       }
21
22
       void set(int x, int y) {
23
            b[x >> 6] = 1ULL << (x & 63);
24
            if (!y) b[x >> 6] = 1ULL << (x & 63);
25
       }
26
27
        Bitset &operator&=(const Bitset &another) {
28
            rep(i, 0, min(SZ(b), SZ(another.b)) - 1) {
29
                b[i] &= another.b[i];
30
           }
31
            return (*this);
32
       }
33
34
        Bitset operator&(const Bitset &another)const {
35
            return (Bitset(*this) &= another):
36
       }
37
38
        Bitset &operator | = (const Bitset &another) {
```

```
39
            rep(i, 0, min(SZ(b), SZ(another.b)) - 1) {
                b[i] |= another.b[i];
40
41
42
            return (*this);
       }
43
44
       Bitset operator | (const Bitset & another) const {
45
            return (Bitset(*this) |= another);
46
47
       }
48
49
       Bitset &operator^=(const Bitset &another) {
            rep(i, 0, min(SZ(b), SZ(another.b)) - 1) {
50
                b[i] ^= another.b[i]:
51
52
            }
53
            return (*this);
       }
54
55
56
       Bitset operator^(const Bitset &another)const {
            return (Bitset(*this) ^= another);
57
       }
58
59
60
       Bitset &operator>>=(int x) {
            if (x & 63) {
61
                rep(i, 0, SZ(b) - 2) {
62
63
                    b[i] >>= (x \& 63):
                    b[i] = (b[i + 1] << (64 - (x & 63)));
                b.back() >>= (x & 63);
67
69
            x >>= 6;
70
            rep(i, 0, SZ(b) - 1) {
                if (i + x < SZ(b)) b[i] = b[i + x];
71
72
                else b[i] = 0;
73
74
            return (*this);
75
       }
76
77
       Bitset operator>>(int x)const {
78
            return (Bitset(*this) >>= x);
       }
79
80
81
       Bitset &operator<<=(int x) {</pre>
```

```
if (x & 63) {
                 for (int i = SZ(b) - 1; i >= 1; i--) {
                     b[i] <<= (x & 63):
 84
                     b[i] = b[i - 1] >> (64 - (x & 63));
                }
                 b[0] <<= x & 63;
             }
             x >>= 6;
             for (int i = SZ(b) - 1; i \ge 0; i--) {
91
                 if (i - x >= 0) b[i] = b[i - x];
 93
                 else b[i] = 0;
             }
94
             return (*this);
96
        }
97
         Bitset operator<<(int x)const {</pre>
             return (Bitset(*this) <<= x):</pre>
100
        }
101 }:
```

8.3 fastIO.cpp

```
1 static struct FastInput {
     static constexpr int BUF SIZE = 1 << 20;
    char buf[BUF_SIZE];
     size t chars read = 0;
     size_t buf_pos = 0;
     FILE *in = stdin;
     char cur = 0:
8
     inline char get char() {
       if (buf_pos >= chars_read) {
10
         chars_read = fread(buf, 1, BUF_SIZE, in);
11
12
         buf pos = 0:
         buf[0] = (chars_read == 0 ? -1 : buf[0]);
13
14
       return cur = buf[buf_pos++];
15
16
17
18
      template <typename T>
19
      inline void tie(T) {}
20
```

```
21
     inline explicit operator bool() {
       return cur != -1;
     }
23
24
     inline static bool is_blank(char c) {
25
       return c <= '';
26
     }
27
28
     inline bool skip blanks() {
29
       while (is_blank(cur) && cur != -1) {
30
31
         get_char();
32
       return cur != -1:
33
34
     }
35
36
     inline FastInput& operator>>(char& c) {
37
        skip blanks();
       c = cur:
39
       get_char();
       return *this:
40
     }
41
42
43
     inline FastInput& operator>>(string& s) {
       if (skip_blanks()) {
44
45
         s.clear();
         do {
           s += cur:
         } while (!is_blank(get_char()));
48
49
       }
       return *this:
50
     }
51
52
     template <typename T>
53
54
      inline FastInput& read_integer(T& n) {
55
       // unsafe, doesn't check that characters are actually digits
56
       n = 0:
       if (skip_blanks()) {
         int sign = +1;
58
         if (cur == '-') {
59
60
           sign = -1;
           get char();
61
62
         }
          do {
```

```
64
             n += n + (n << 3) + cur - '0':
           } while (!is blank(get char()));
           n *= sign:
 66
 67
        }
         return *this;
 69
      }
 70
 71
       template <typename T>
 72
       inline typename enable if < is integral < T > :: value, FastInput & > :: type
           operator>>(T& n) {
 73
         return read_integer(n);
 74
      }
 75
 76
       #if !defined( WIN32) || defined( WIN64)
 77
       inline FastInput& operator>>(__int128& n) {
 78
         return read_integer(n);
 79
      }
       #endif
 81
       template <typename T>
       inline typename enable_if < is_floating_point < T > :: value, FastInput & > :: type
           operator>>(T& n) {
 84
         // not sure if really fast, for compatibility only
         n = 0:
        if (skip_blanks()) {
           string s;
           (*this) >> s;
           sscanf(s.c_str(), "%lf", &n);
 90
 91
         return *this:
    } fast_input;
 94
     #define cin fast_input
 96
 97
    static struct FastOutput {
       static constexpr int BUF_SIZE = 1 << 20;</pre>
      char buf[BUF SIZE];
100
       size_t buf_pos = 0;
101
       static constexpr int TMP_SIZE = 1 << 20;</pre>
102
       char tmp[TMP_SIZE];
       FILE *out = stdout;
104
```

```
105
       inline void put_char(char c) {
         buf[buf pos++] = c;
106
         if (buf_pos == BUF_SIZE) {
107
108
           fwrite(buf, 1, buf_pos, out);
           buf_pos = 0;
109
        }
110
      }
111
112
       ~FastOutput() {
113
         fwrite(buf, 1, buf_pos, out);
114
115
      }
116
       inline FastOutput& operator << (char c) {</pre>
117
118
         put char(c);
         return *this:
119
      }
120
121
122
       inline FastOutput& operator<<(const char* s) {</pre>
         while (*s) {
123
           put_char(*s++);
124
125
         }
         return *this:
126
       }
127
128
129
       inline FastOutput& operator<<(const string& s) {</pre>
         for (int i = 0; i < (int) s.size(); i++) {
130
           put_char(s[i]);
131
         }
132
133
         return *this;
134
      }
135
136
       template <typename T>
       inline char* integer_to_string(T n) {
137
138
         // beware of TMP_SIZE
139
         char* p = tmp + TMP_SIZE - 1;
140
         if (n == 0) {
           *--p = '0';
141
         } else {
142
           bool is_negative = false;
143
144
           if (n < 0) {
           is_negative = true;
145
146
             n = -n;
147
           }
```

```
148
           while (n > 0) {
149
             *--p = (char) ('0' + n % 10);
150
             n /= 10:
151
          }
152
           if (is_negative) {
153
             *--p = '-';
154
          }
155
        }
156
         return p;
157
158
159
       template <typename T>
       inline typename enable_if<is_integral<T>::value, char*>::type stringify(T
160
161
        return integer_to_string(n);
162
      }
163
164
       #if !defined(_WIN32) || defined(_WIN64)
165
       inline char* stringify(__int128 n) {
166
        return integer_to_string(n);
167
      }
168
       #endif
169
170
       template <typename T>
171
       inline typename enable_if < is_floating_point < T >:: value, char * >:: type
           stringify(T n) {
172
         sprintf(tmp, "%.17f", n);
173
         return tmp;
174
      }
175
176
       template <typename T>
177
       inline FastOutput& operator<<(const T& n) {</pre>
178
        auto p = stringify(n);
179
        for (; *p != 0; p++) {
180
           put_char(*p);
181
        }
182
         return *this;
183
184 } fast_output;
186 #define cout fast_output
```

8.4 FastMod.cpp

```
Description: Compute a % b about 5 times faster than usual, where b is
constant but not known at compile time. Returns a value congruent to a
(mod b) in the range [0, 2b).

typedef unsigned long long ull;
struct FastMod {
   ull b, m;
FastMod(ull b) : b(b), m(-1ULL / b) {}
ull reduce(ull a) { // a % b + (0 or b)
   return a - (ull)((__uint128_t(m) * a) >> 64) * b;
}

return a - (ull) ((__uint128_t(m) * a) >> 64) * b;
}
```

8.5 intervalContainer.cpp

```
1 Description: Add and remove intervals from a set of disjoint intervals.
2 Will merge the added interval with any overlapping intervals in the set when
   adding. Intervals are [inclusive, exclusive).
   Time: O (log N)
   set<pii>::iterator addInterval(set<pii>& is, int L, int R) {
       if (L == R) return is.end():
       auto it = is.lower bound({L, R}), before = it;
       while (it != is.end() && it->first <= R) {</pre>
            R = max(R, it->second):
           before = it = is.erase(it);
11
       }
12
       if (it != is.begin() && (--it)->second >= L) {
13
           L = min(L, it->first):
14
           R = max(R, it->second):
15
16
           is.erase(it);
17
       }
        return is.insert(before, {L, R});
18
19 }
   void removeInterval(set<pii>& is, int L, int R) {
21
        if (L == R) return;
       auto it = addInterval(is, L, R):
22
       auto r2 = it->second;
23
24
       if (it->first == L) is.erase(it):
       else (int&)it->second = L:
       if (R != r2) is.emplace(R, r2);
27 }
```

8.6 lineContainer.cpp

```
1 /**
    * Author: Simon Lindholm
   * Date: 2017-04-20
    * License: CCO
    * Source: own work
    * Description: Container where you can add lines of the form kx+m, and
         query maximum values at points x.
    * Useful for dynamic programming (``convex hull trick'').
    * Time: O(\log N)
    * Status: stress-tested
10
11 #pragma once
12
   struct Line {
        mutable ll k, m, p;
15
        bool operator<(const Line& o) const { return k < o.k; }</pre>
       bool operator<(ll x) const { return p < x; }</pre>
16
17 };
18
    struct LineContainer : multiset<Line. less<>> {
20
       // (for doubles, use inf = 1/.0, div(a,b) = a/b)
21
        static const ll inf = LLONG MAX:
22
       ll div(ll a, ll b) { // floored division
23
            return a / b - ((a ^ b) < 0 && a % b); }
24
       bool isect(iterator x. iterator v) {
25
            if (y == end()) return x \rightarrow p = inf, 0;
26
            if (x->k == y->k) x->p = x->m > y->m ? inf : -inf:
27
            else x -> p = div(y -> m - x -> m, x -> k - y -> k);
28
            return x->p >= v->p:
29
       }
30
       void add(ll k, ll m) {
            auto z = insert(\{k, m, 0\}), y = z++, x = y;
31
32
            while (isect(y, z)) z = erase(z);
            if (x != begin() \&\& isect(--x, v)) isect(x, v = erase(v)):
            while ((y = x) != begin() && (--x)->p >= y->p)
34
35
                isect(x, erase(y));
       }
       11 query(11 x) {
37
            assert(!emptv()):
39
            auto 1 = *lower bound(x);
40
            return 1.k * x + 1.m;
41
       }
```

```
42 };
```

8.7 mint.cpp

```
template<int MOD, int RT> struct mint {
        static const int mod = MOD:
        static constexpr mint rt() { return RT; } // primitive root for FFT
       int v; explicit operator int() const { return v; } // explicit -> don't
            silently convert to int
       mint():v(0) {}
       mint(ll _v) { v = int((-MOD < _v && _v < MOD) ? _v : _v % MOD);
           if (v < 0) v += MOD; }
       bool operator == (const mint& o) const {
            return v == o.v; }
10
       friend bool operator!=(const mint& a, const mint& b) {
            return !(a == b): }
11
12
       friend bool operator<(const mint& a, const mint& b) {</pre>
            return a.v < b.v: }
13
14
15
        mint& operator+=(const mint& o) {
            if ((v += o.v) >= MOD) v -= MOD;
16
            return *this; }
17
       mint& operator -= (const mint& o) {
18
19
            if ((v -= o.v) < 0) v += MOD;
            return *this; }
20
       mint& operator*=(const mint& o) {
21
22
           v = int((11)v*o.v%MOD); return *this; }
23
       mint& operator/=(const mint& o) { return (*this) *= inv(o): }
24
       friend mint pow(mint a, ll p) {
            mint ans = 1: assert(p >= 0):
25
26
           for (; p; p /= 2, a *= a) if (p&1) ans *= a;
27
           return ans: }
28
       friend mint inv(const mint& a) { assert(a.v != 0):
            return pow(a,MOD-2); }
29
30
31
        mint operator-() const { return mint(-v); }
32
        mint& operator++() { return *this += 1; }
33
       mint& operator -- () { return *this -= 1: }
34
       friend mint operator+(mint a, const mint& b) { return a += b; }
       friend mint operator-(mint a. const mint& b) { return a -= b: }
35
       friend mint operator*(mint a. const mint& b) { return a *= b: }
36
37
       friend mint operator/(mint a, const mint& b) { return a /= b; }
38 }:
```

```
39
    const int MOD=998244353;
    using mi = mint<MOD.5>: // 5 is primitive root for both common mods
42
43
   namespace simp {
44
        vector<mi> fac.ifac.invn:
45
        void check(int x) {
            if (fac.empty()) {
46
47
                fac={mi(1),mi(1)};
                ifac={mi(1).mi(1)}:
48
49
                invn={mi(0),mi(1)};
50
            }
            while (SZ(fac)<=x) {
51
52
                int n=SZ(fac),m=SZ(fac)*2;
53
                fac.resize(m):
54
                ifac.resize(m);
                invn.resize(m);
                for (int i=n:i<m:i++) {</pre>
                     fac[i]=fac[i-1]*mi(i);
57
                    invn[i]=mi(MOD-MOD/i)*invn[MOD%i]:
58
59
                    ifac[i]=ifac[i-1]*invn[i];
                }
61
            }
62
        }
        mi gfac(int x) {
            check(x); return fac[x];
        mi ginv(int x) {
67
            check(x); return invn[x];
68
        }
69
        mi gifac(int x) {
70
            check(x); return ifac[x];
71
       }
72
        mi binom(int n.int m) {
73
            if (m < 0 \mid | m > n) return mi(0);
74
            return gfac(n)*gifac(m)*gifac(n - m);
        }
76 }
```

8.8 pbds.cpp

```
1 #include <bits/extc++.h>
2 using namespace __gnu_cxx;
```

```
using namespace __gnu_pbds;
5 #include<ext/pb_ds/assoc_container.hpp>
   #include<ext/pb ds/tree policy.hpp>
   #include<ext/pb_ds/hash_policy.hpp>
   #include<ext/pb_ds/trie_policy.hpp>
   #include<ext/pb ds/priority queue.hpp>
   pairing heap tag: 配对堆
11
12 thin_heap_tag: 斐波那契堆
   binomial heap tag: 二项堆
   binary heap tag: 二叉堆
15
   gnu pbds::priority queue<PII, greater<PII>, pairing heap tag> q;
   __gnu_pbds::priority_queue<PII, greater<PII>, pairing_heap_tag>::
       point_iterator its[N];
19 its[v] = q.push({dis[v], v});
   q.modify(its[v], {dis[v], v});
21
22 可以将两个优先队列中的元素合并(无任何约束)
23 使用方法为a.join(b)
24 此时优先队列b内所有元素就被合并进优先队列a中, 且优先队列b被清空
26 cc hash table < string, int > mp1拉链法
27 gp hash table < string, int > mp2查探法
```

8.9 simu.cpp

```
1 db rnd(db 1, db r) {
     static uniform real distribution <db> u(0, 1):
     static default random engine e(rng());
     return 1 + (r - 1) * u(e); // u(rnq);
5 }
   db eval(pair<db, db> x) { ... }
   void simulate anneal() {
     pair < db, db > cur(rnd(0, 10000), rnd(0, 10000));
10
11
     for (double k = 10000; k > 1e-5; k *= 0.99) {
12
       // [start, end, step]
13
       pair<db, db> nxt(cur.fi + rnd(-k, k), cur.se + rnd(-k, k));
14
       db delta = eval(nxt) - eval(cur):
```

```
15
       if (exp(-delta / k) > rnd(0, 1)) {
16
          cur = nxt;
17
       }
     }
19 }
20
21 /**
    * https://codeforces.com/qym/104813/submission/234982955
    * The 9th CCPC (Harbin) 2023
    * Author: OwertuPi
25
    */
26 LD Prob() {
     static uniform real distribution <> dist(0.0, 1.0):
     return dist(rng);
29 }
   LD Sigma(LD x) { return 1 / (1 + \exp(-x)); }
31
32 LD overall max score = 0:
33 for (int main_loop = 0; main_loop < 5; main_loop++) {
     vector<LD> e(n, (LD)1 / n):
     for (int tr = 0; tr < 1000; tr++) {
       vector<LD> ne(n):
37
       for (int i = 0: i < n: i++) {
38
         ne[i] = Prob();
39
       }
       LD s = accumulate(all(ne), 0.0L);
       for (int i = 0; i < n; i++) {
42
         ne[i] /= s;
43
44
       if (eval(ne) > eval(e)) e = ne:
45
46
     LD t = (LD)0.0002:
47
     LD max score = 0;
     const LD depr = 0.999995;
49
     const int tries = 2E6;
     const int loop = 1E5;
51
     LD score_old = eval(e);
     for (int tr = 0; tr < tries; tr++) {
54 #ifdef LOCAL
       if (tr % loop == loop - 1) {
          cout << fixed << setprecision(10) << "current_score_=" << max_score
57
               << ",,,t,,=,," << t << '\n';
```

```
}
   #endif
       int x = rng() % n, y = rng() % n;
60
61
       if (e[x] < t | | x == y) {
62
         t *= depr;
63
         continue;
64
65
       e[x] -= t;
       e[v] += t;
       LD score_new = eval(e);
67
       if (score_new > score_old) { // ok
       } else { // revert
70
71
         e[x] += t;
72
         e[y] -= t;
73
74
        score old = score new;
75
       max_score = max(max_score, score_new);
76
       t *= depr;
77
     overall_max_score = max(overall_max_score, max_score);
   #ifdef LOCAL
     cout << "Loopu#" << main_loop << ":" << max_score << '\n';
81 #endif
82 }
```

8.10 sort.cpp

```
void merge_sort(int q[], int l, int r) {
        if (1 >= r) return:
        int mid = 1 + r >> 1:
        merge sort(q, 1, mid);
        merge_sort(q, mid + 1, r);
        int k = 0, i = 1, j = mid + 1;
        while (i <= mid && j <= r)
            if (q[i] <= q[j])</pre>
10
                tmp[k++] = q[i++];
11
            else
12
                tmp[k++] = q[j++];
13
14
        while (i <= mid)
15
            tmp[k++] = q[i++];
```

```
16
        while (j <= r)
17
            tmp[k++] = q[j++];
18
19
        for (i = 1, j = 0; i \le r; i++, j++) q[i] = tmp[j];
20 }
21
   void quick sort(int q[], int l, int r) {
        if (1 \ge r) return:
24
       int i = 1 - 1, j = r + 1, x = q[1 + r >> 1];
25
       while (i < j) {
26
           do i ++; while (q[i] < x);
27
            do j --; while (q[j] > x);
           if (i < j) swap(q[i], q[j]);</pre>
29
       }
        quick_sort(q, 1, j), quick_sort(q, j + 1, r);
31 }
32
33 template < class T>
    void radixsort(T *a, ll n) {
       int base = 0:
       rep(i, 1, n) sa[i] = i;
37
       rep(k, 1, 5) {
           rep(i, 0, 255) c[i] = 0;
39
           rep(i, 1, n) c[(a[i] >> base) & 255]++;
40
           rep(i, 1, 255) c[i] += c[i - 1];
41
            per(i, n, 1) {
42
                rk[sa[i]] = c[(a[sa[i]] >> base) & 255]--;
44
           rep(i, 1, n) sa[rk[i]] = i;
45
            base += 7:
       }
46
47 }
```

8.11 高精度.cpp

```
1 vector<int> add(vector<int> &A, vector<int> &B) {
2     if (A.size() < B.size()) return add(B, A);
3     vector<int> C;
4     int t = 0;
5     for (int i = 0; i < A.size(); i ++ ) {
6         t += A[i];
7         if (i < B.size()) t += B[i];
8         C.push_back(t % 10);</pre>
```

```
t /= 10;
10
       }
11
        if (t) C.push_back(t);
12
        return C;
13 }
14
15 vector<int> sub(vector<int> &A, vector<int> &B) {
16
        vector<int> C:
        for (int i = 0, t = 0; i < A.size(); i ++ ) {
17
18
            t = A[i] - t;
           if (i < B.size()) t -= B[i];</pre>
19
20
            C.push_back((t + 10) % 10);
           if (t < 0) t = 1;
21
            else t = 0;
22
23
       }
        while (C.size() > 1 && C.back() == 0) C.pop_back();
24
25
        return C;
26 }
27
28 vector<int> mul(vector<int> &A, int b) {
        vector<int> C;
29
30
        int t = 0:
```

```
31
       for (int i = 0; i < A.size() || t; i ++ ) {
           if (i < A.size()) t += A[i] * b;
32
           C.push_back(t % 10);
34
           t /= 10;
35
       }
       while (C.size() > 1 && C.back() == 0) C.pop_back();
37
       return C;
38 }
39
40 vector<int> div(vector<int> &A, int b, int &r) {
41
       vector<int> C;
42
    r = 0;
      for (int i = A.size() - 1; i >= 0; i -- ) {
44
           r = r * 10 + A[i];
45
          C.push_back(r / b);
46
           r %= b;
47
       reverse(C.begin(), C.end());
       while (C.size() > 1 && C.back() == 0) C.pop_back();
50
       return C;
51 }
```