

Assignment 2

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19 de diciembre de 2015

```
library(TSA)
```

```
## Warning: package 'TSA' was built under R version 3.2.2

## Loading required package: leaps

## Warning: package 'leaps' was built under R version 3.2.2

## Loading required package: locfit

## Warning: package 'locfit' was built under R version 3.2.2

## locfit 1.5-9.1    2013-03-22
## Loading required package: mgcv
## Loading required package: nlme
## This is mgcv 1.8-6. For overview type 'help("mgcv-package")'.
## Loading required package: tseries

## Warning: package 'tseries' was built under R version 3.2.2

##
## Attaching package: 'TSA'
##
## The following objects are masked from 'package:stats':
##
##     acf, arima
##
## The following object is masked from 'package:utils':
##
##     tar
```

```
library(forecast)
```

```
## Warning: package 'forecast' was built under R version 3.2.2

## Loading required package: zoo

## Warning: package 'zoo' was built under R version 3.2.2

##
## Attaching package: 'zoo'
##
## The following objects are masked from 'package:base':
##
##     as.Date, as.Date.numeric
##
## Loading required package: timeDate
```

```
## Warning: package 'timeDate' was built under R version 3.2.2
```

```
##
## Attaching package: 'timeDate'
##
## The following objects are masked from 'package:TSA':
##
##      kurtosis, skewness
##
## This is forecast 6.1
##
## Attaching package: 'forecast'
##
## The following objects are masked from 'package:TSA':
##
##      fitted.Arima, plot.Arima
##
## The following object is masked from 'package:nlme':
##
##      getResponse
```

```
library(astsa)
```

```
## Warning: package 'astsa' was built under R version 3.2.2
```

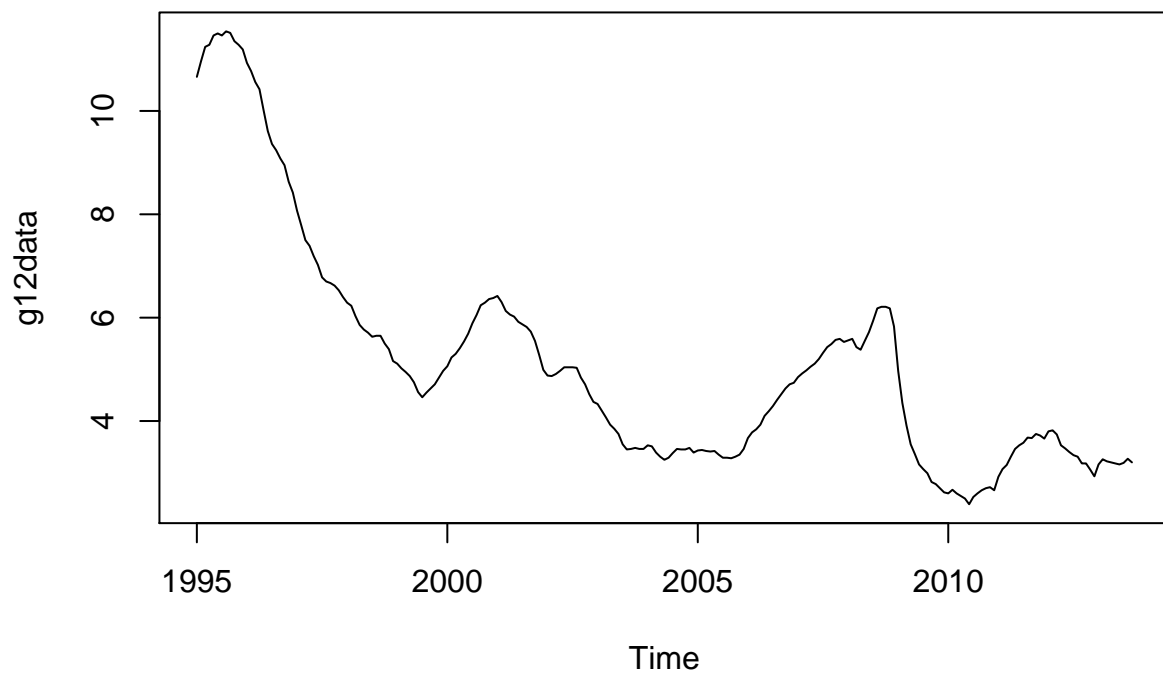
```
##
## Attaching package: 'astsa'
##
## The following object is masked from 'package:forecast':
##
##      gas
```

```
dataAsigment2 <- read.csv("~/MIS DOCUMENTOS/DATA SCIENCE MASTER (EIT DIGITAL)/Intelligent Data Analysis
```

```
g12data=ts(dataAsigment2$Tipo,start=c(1995,1), end=c(2013,9),frequency=12)
str(g12data)
```

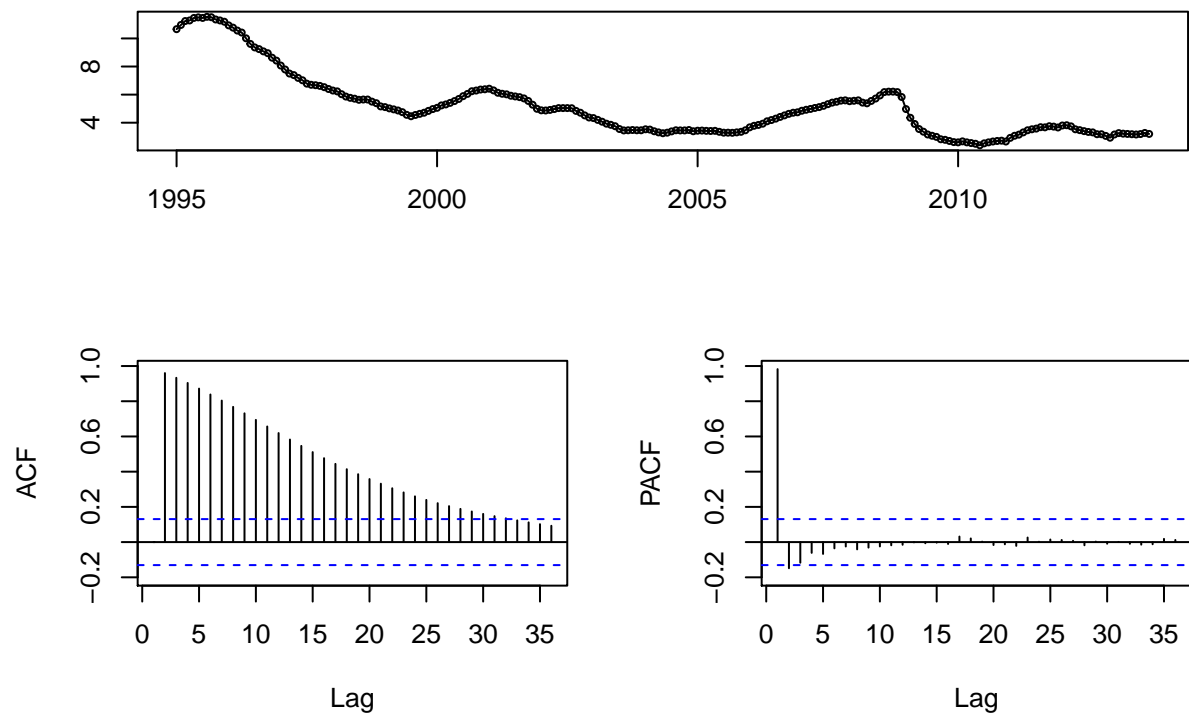
```
## Time-Series [1:225] from 1995 to 2014: 10.7 11 11.2 11.3 11.5 ...
```

```
plot(g12data)
```

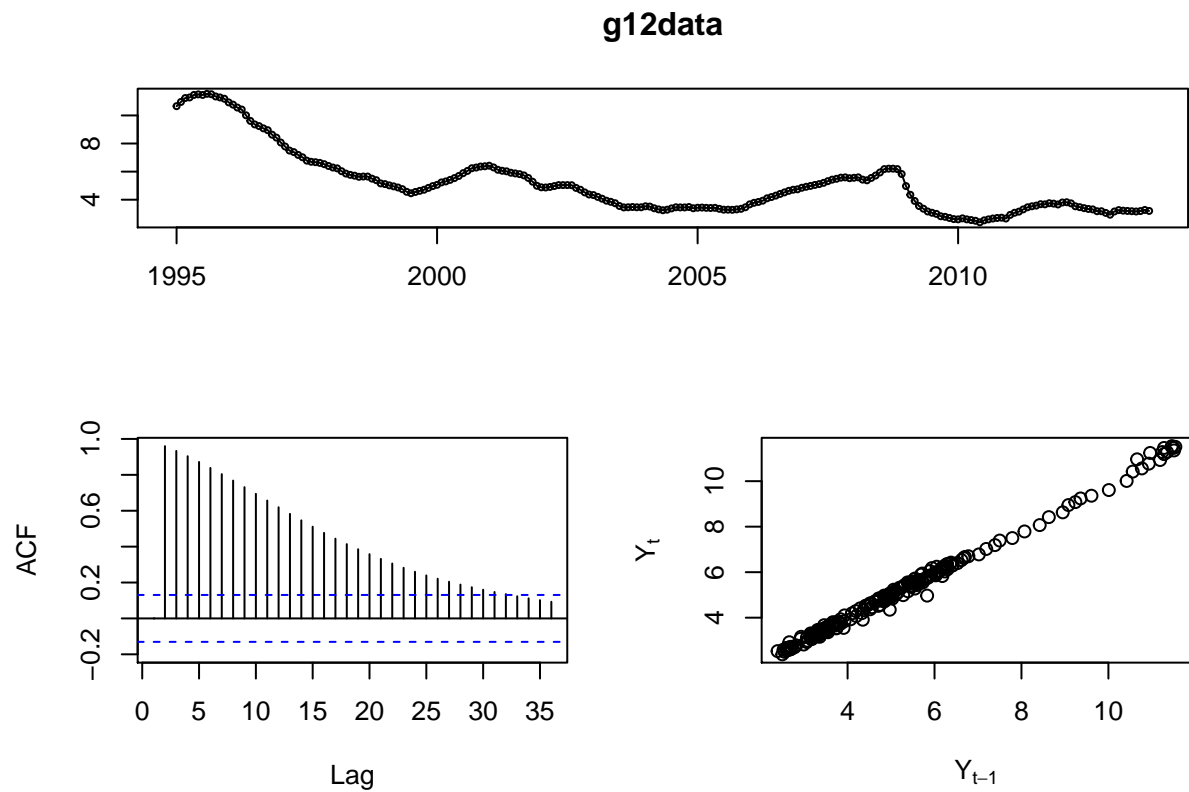


```
tsdisplay(g12data, plot.type="partial")
```

g12data



```
tsdisplay(g12data, plot.type="scatter") #The one Arminda likes most
```

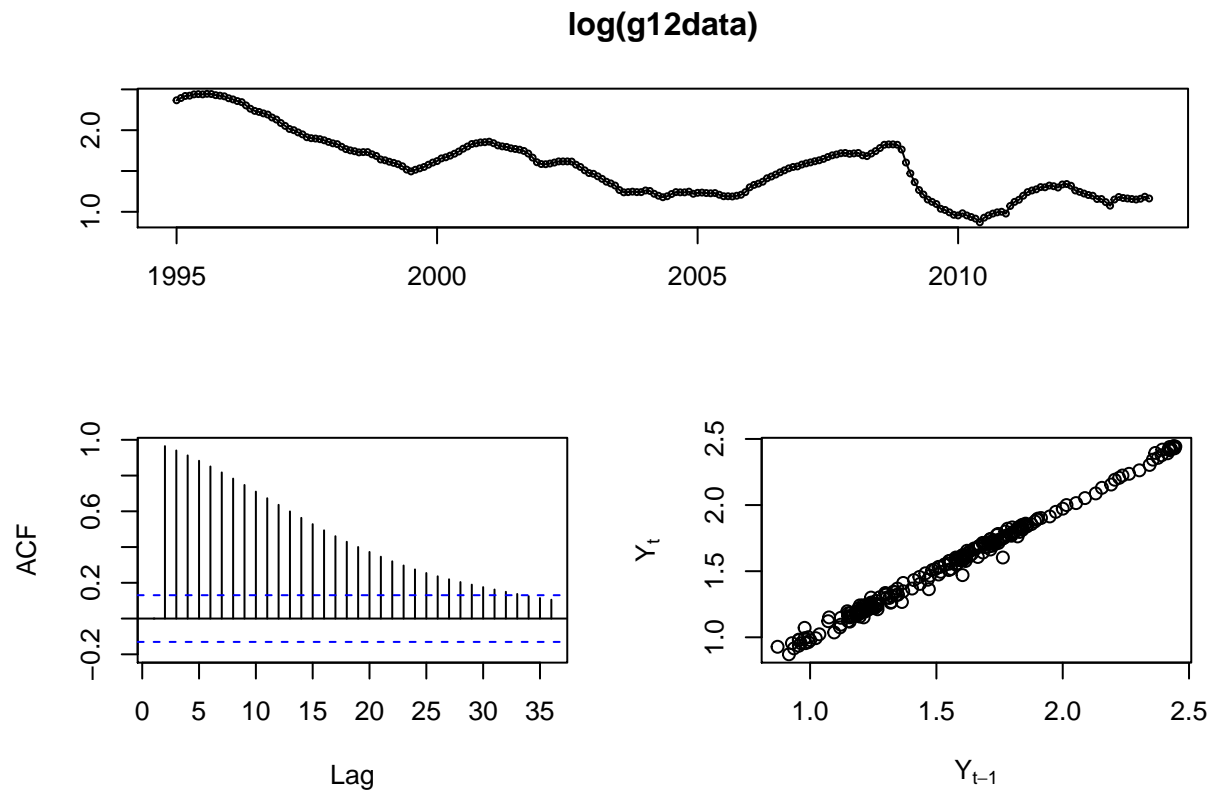


Let's apply BoxCox transformations to check if it is possible to apply a logarithmic transformation to our time series.

```
BoxCox.lambda(g12data, lower=0, upper=2)
```

```
## [1] 0.6487093
```

```
tsdisplay(log(g12data), plot.type="scatter")
```



As it is not close to zero we can't apply this transformation. There is a slight improvement because we can see in the third plot that the values are more spread across the plot.

We can observe that we have a linear trend (decreasing values over time) and a seasonal component as after some years decreasing the time series goes up again (and that happens several times).

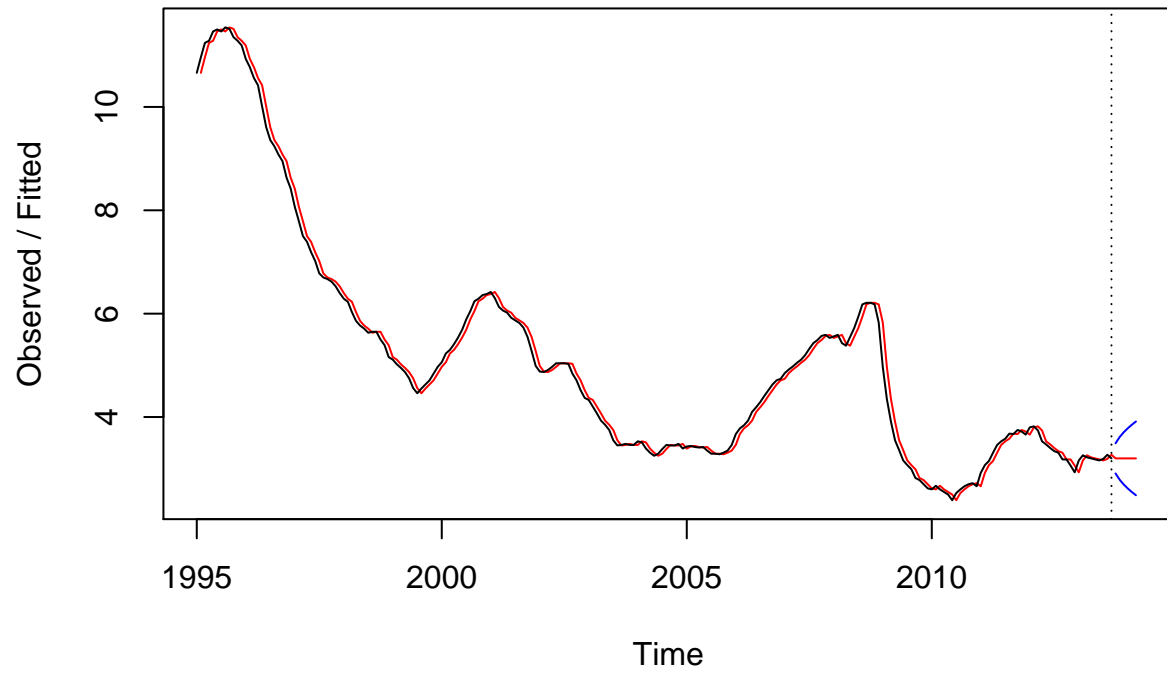
```
## Holt-Winters smoothing with series with linear trend and seasonal variation

smoothing1=HoltWinters(g12data,gamma=FALSE,beta=FALSE)
smoothing2=HoltWinters(g12data,gamma=FALSE)
smoothing3=HoltWinters(g12data)
smoothing4=HoltWinters(g12data,seasonal = "mult")

forecast1=predict(smoothing1, n.ahead=6, prediction.interval=TRUE, level=0.95)
forecast2=predict(smoothing2, n.ahead=6, prediction.interval=TRUE, level=0.95)
forecast3=predict(smoothing3, n.ahead=6, prediction.interval=TRUE, level=0.95)
forecast4=predict(smoothing4, n.ahead=6, prediction.interval=TRUE, level=0.95)

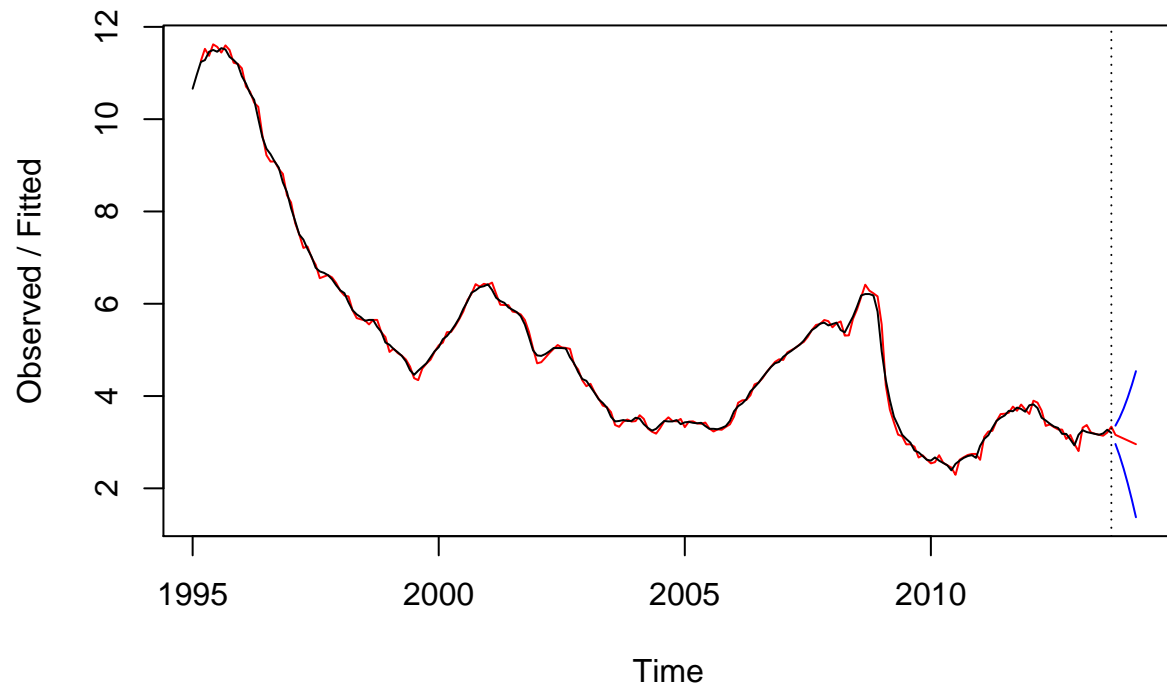
plot(smoothing1, forecast1)
```

Holt-Winters filtering



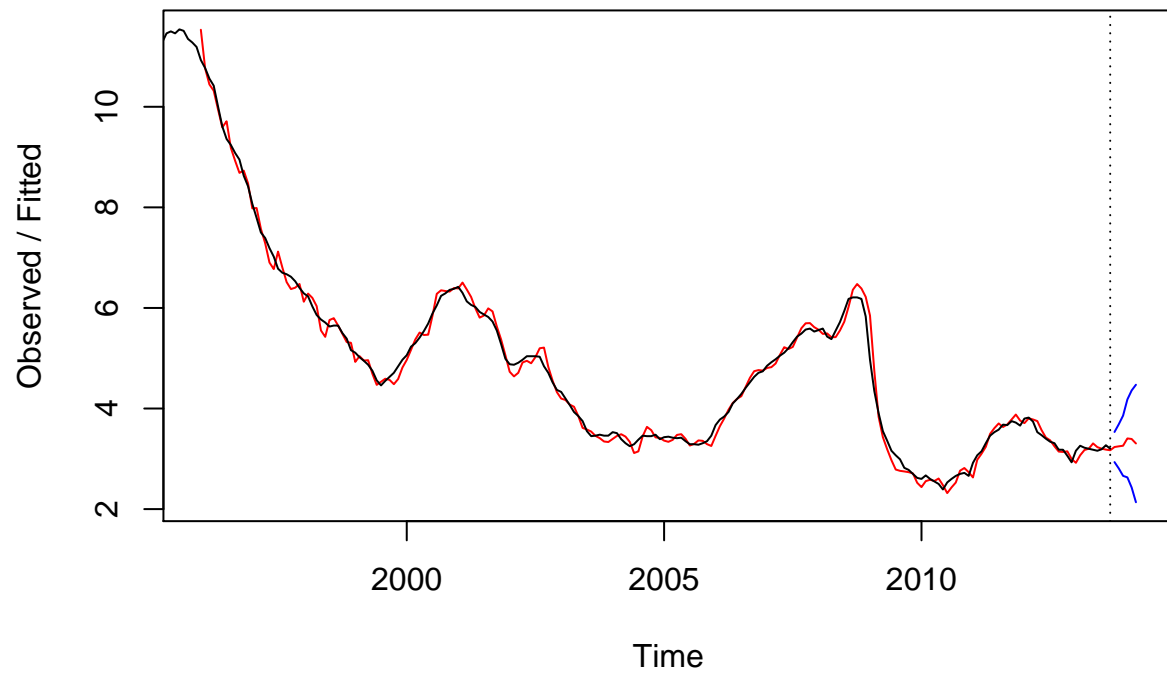
```
plot(smoothing2, forecast2)
```

Holt-Winters filtering



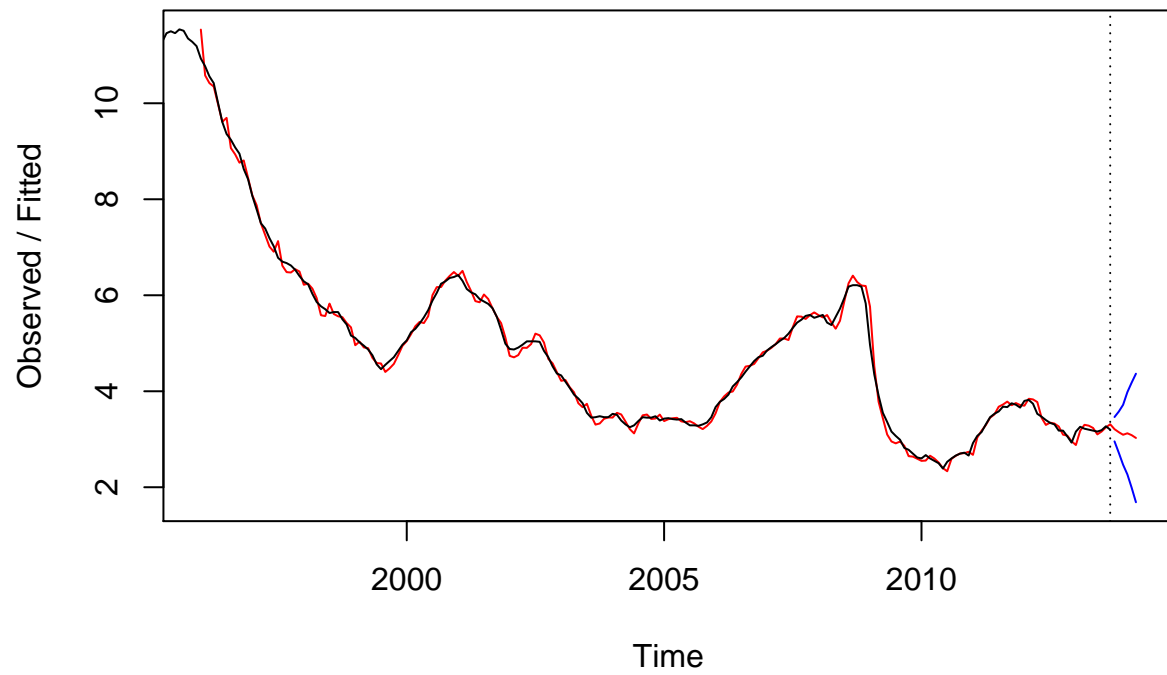
```
plot(smoothing3, forecast3)
```


Holt-Winters filtering



```
plot(smoothing4, forecast4)
```

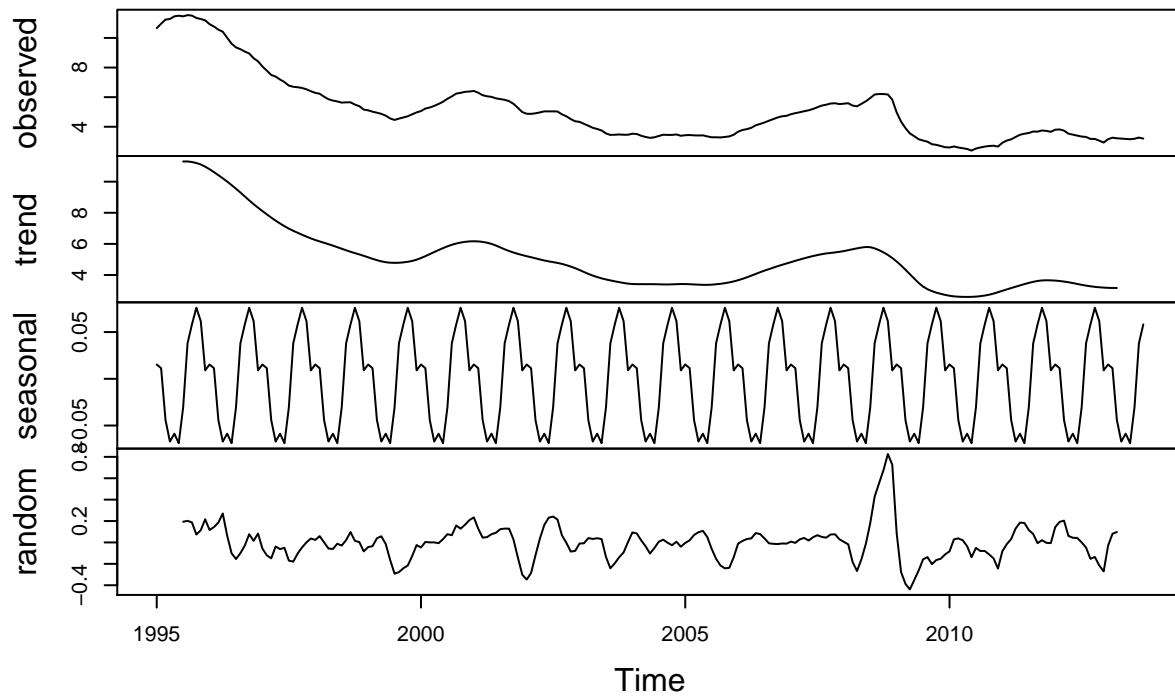
Holt-Winters filtering



Let's try to decompose this time series.

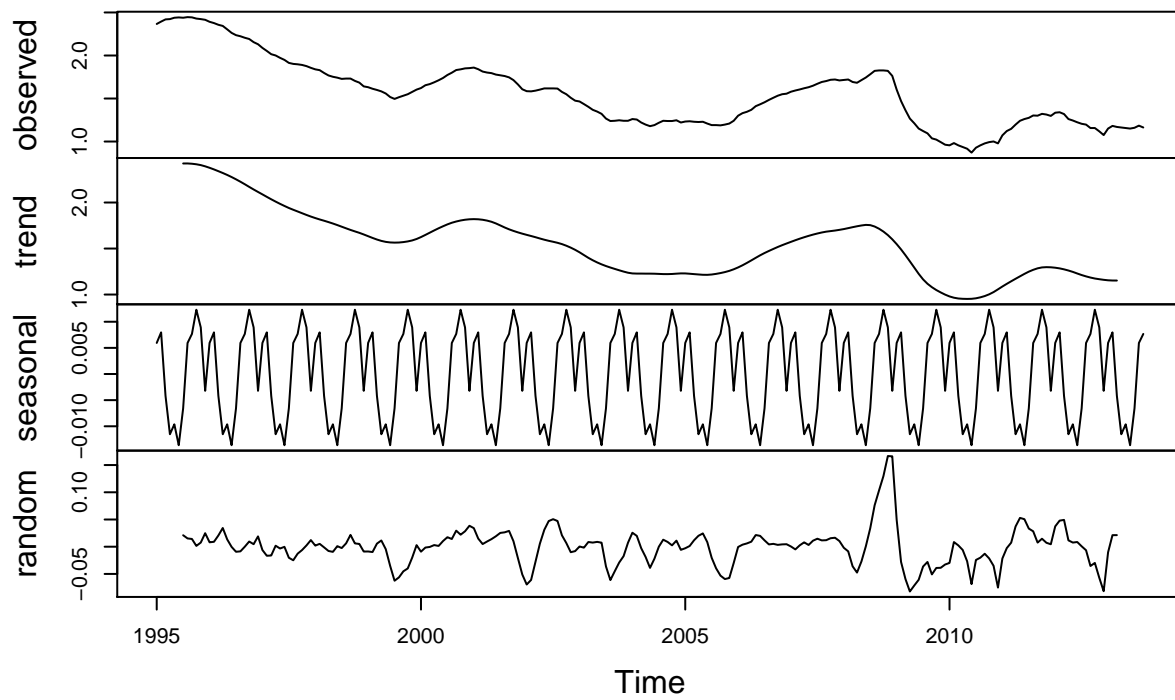
```
decomp=decompose(g12data)
plot(decomp)
```

Decomposition of additive time series



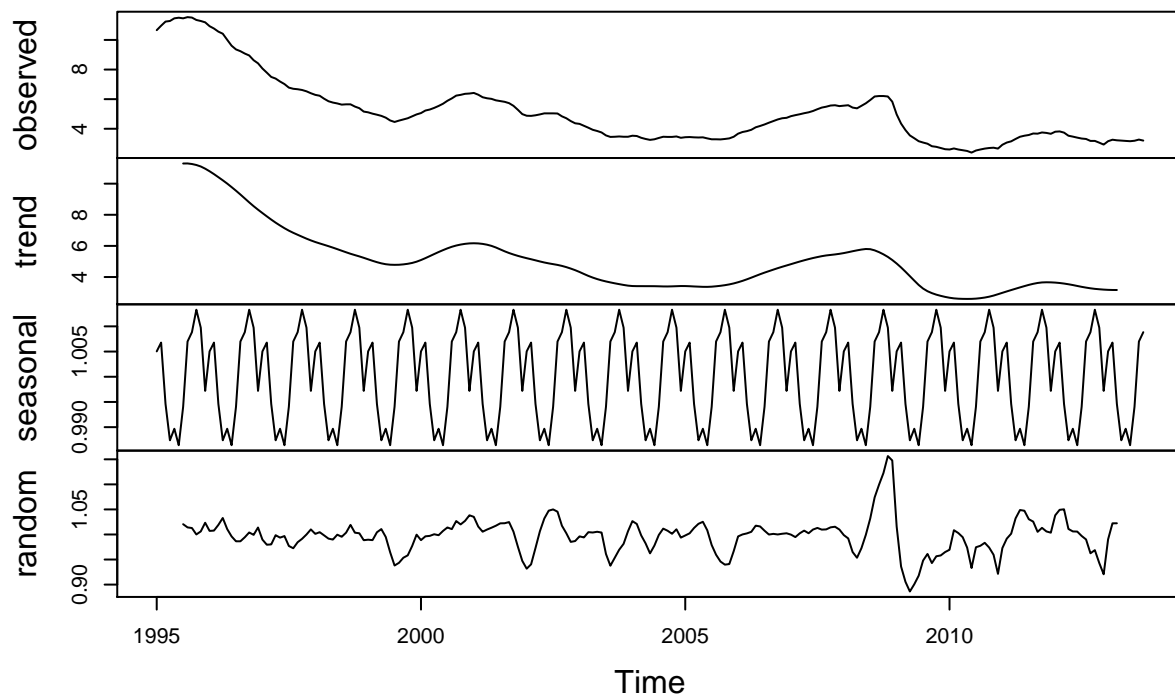
```
decompLog=decompose(log(g12data))  
plot(decompLog)
```

Decomposition of additive time series

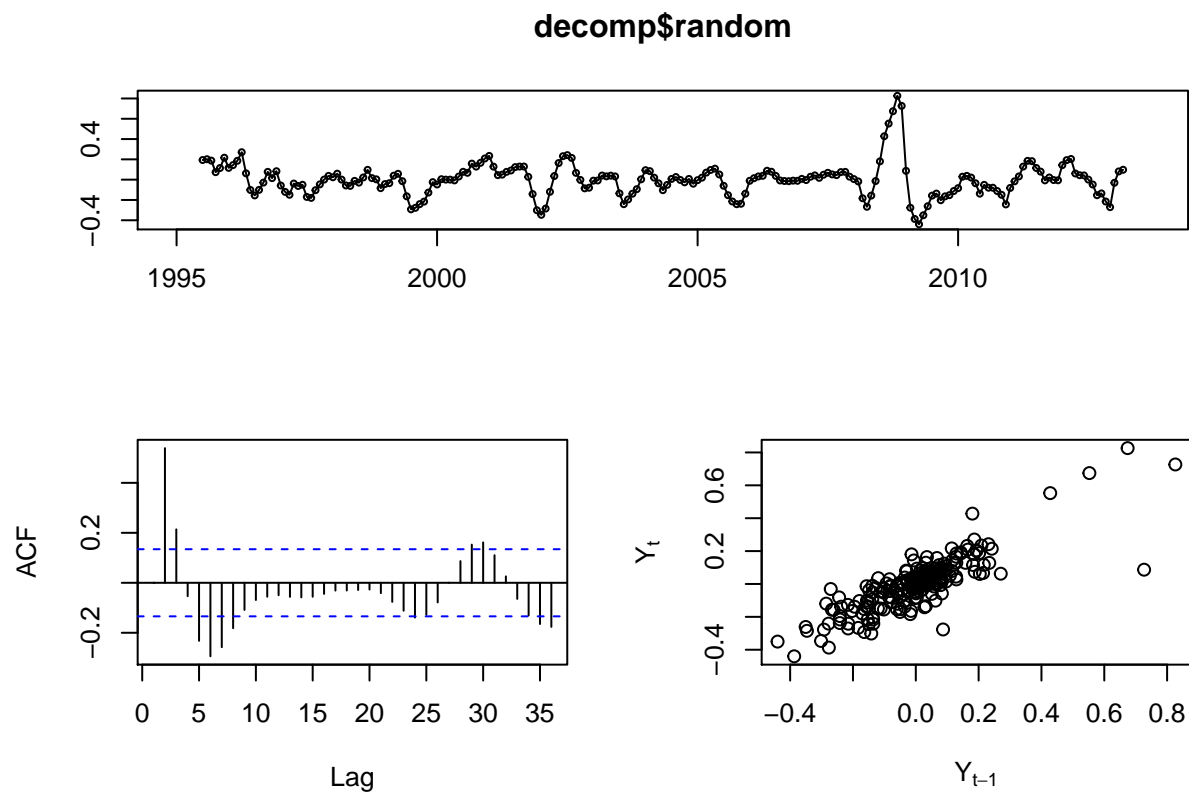


```
### Decomposition of time series, multiplicative decomposition
decompMult=decompose(g12data,type="multiplicative")
plot(decompMult)
```

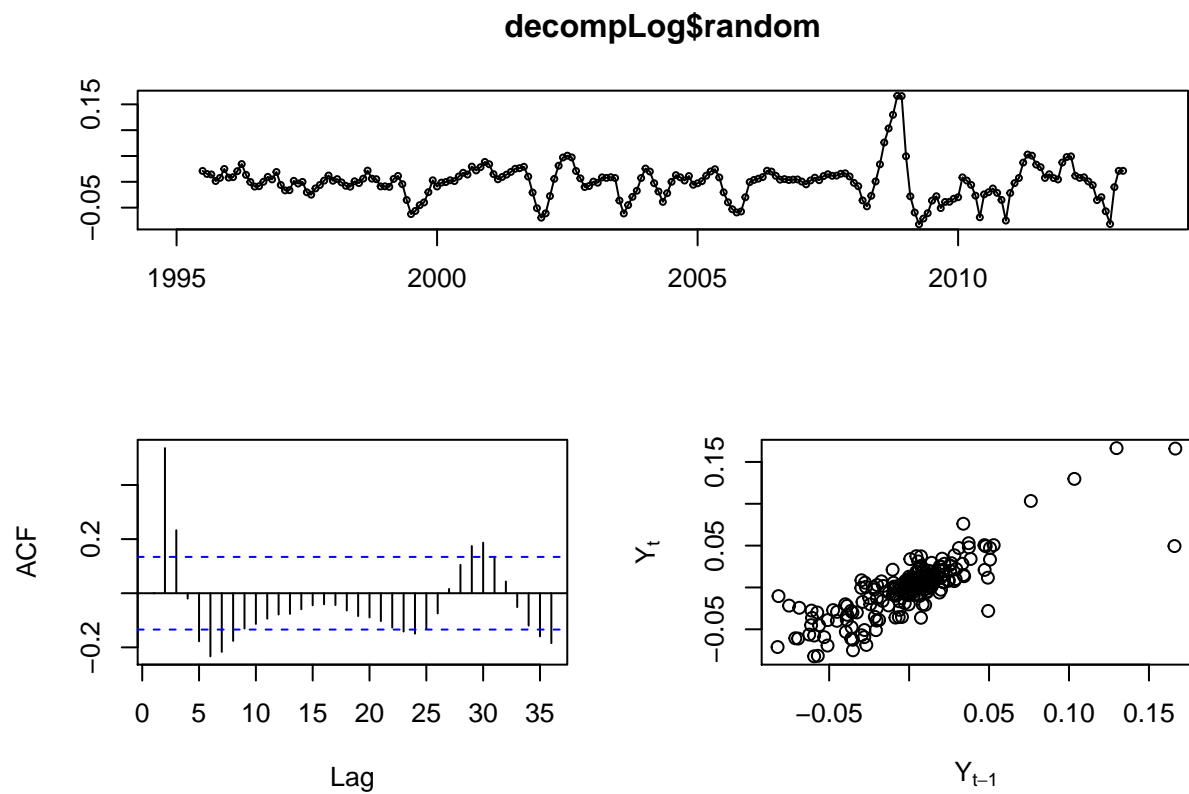
Decomposition of multiplicative time series



```
tsdisplay(decomp$random,plot.type="scatter")
```

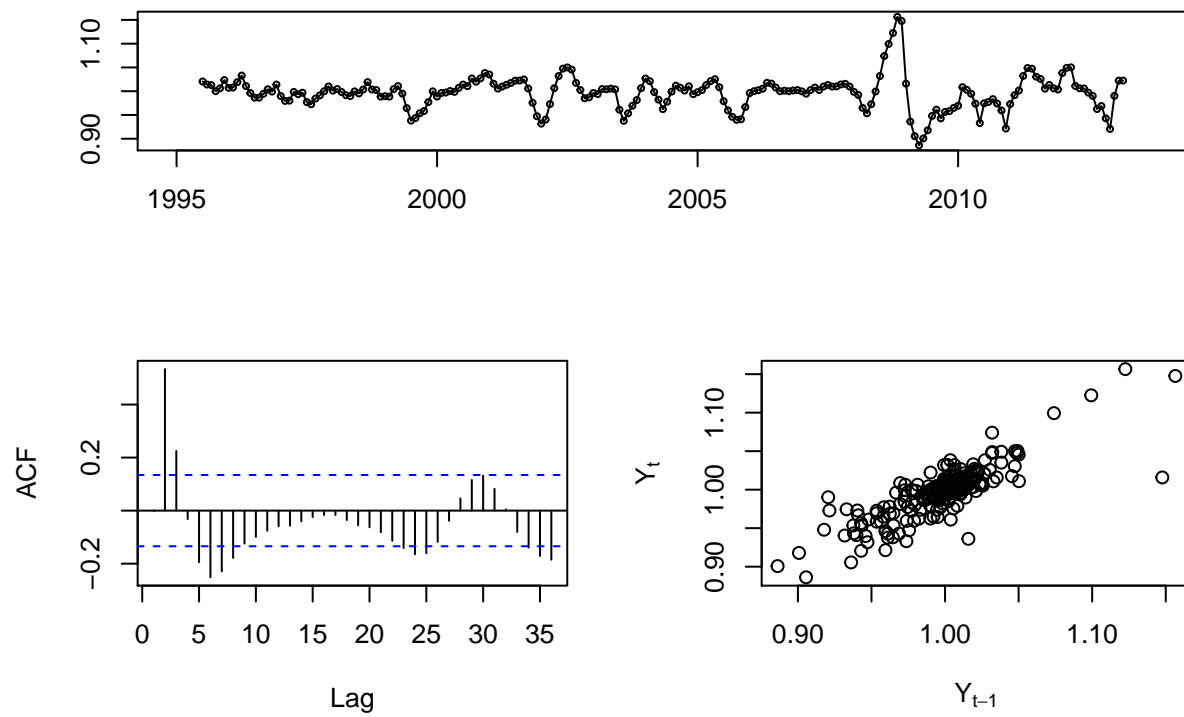


```
tsdisplay(decompLog$random,plot.type="scatter")
```

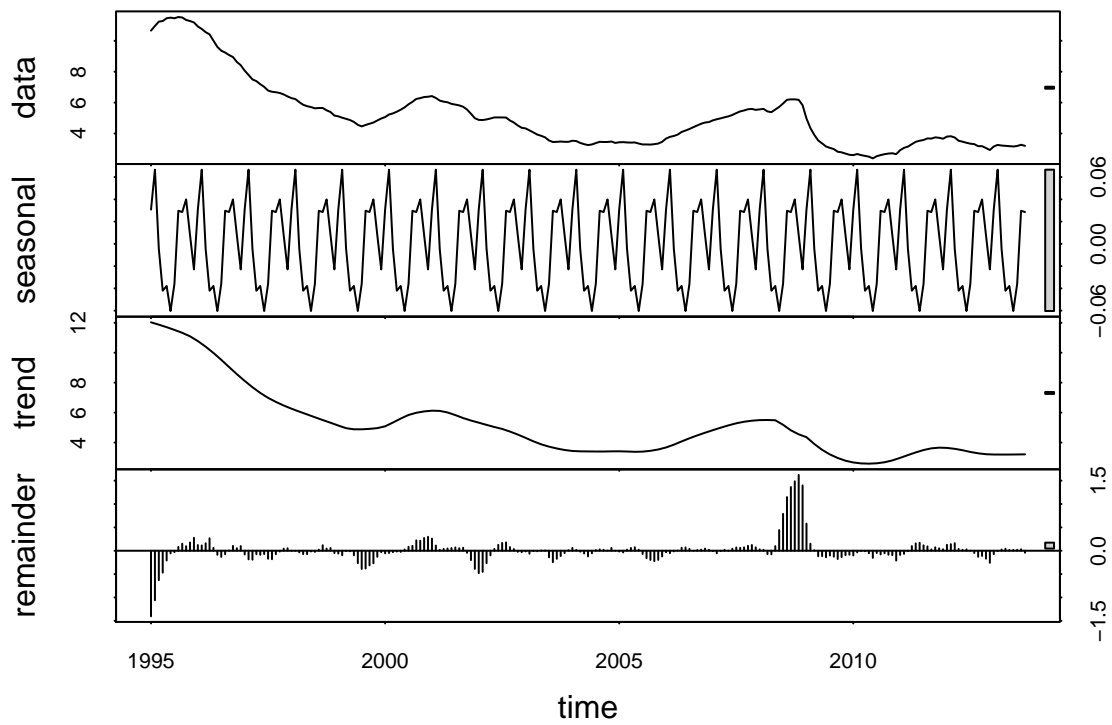


```
tsdisplay(decompMult$random,plot.type="scatter")
```

decompMult\$random



```
stl=stl(g12data, s.window="periodic", robust=TRUE)
plot(stl)
```

```

par(mfrow=c(3,1))
fcst1=forecast(stl, method="naive")
plot(fcst1)
fcst2=forecast(stl, method="arima")
plot(fcst2)
fcst3=forecast(stl, method="rwdrift")
plot(fcst3)

```

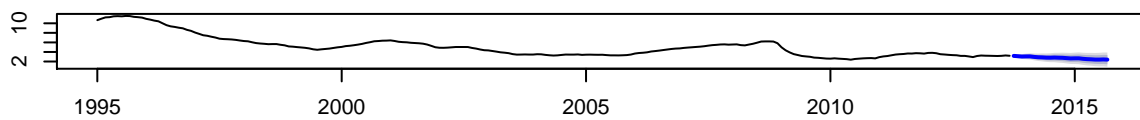
Forecasts from STL + Random walk



Forecasts from STL + ARIMA(2,1,1) with drift



Forecasts from STL + Random walk with drift

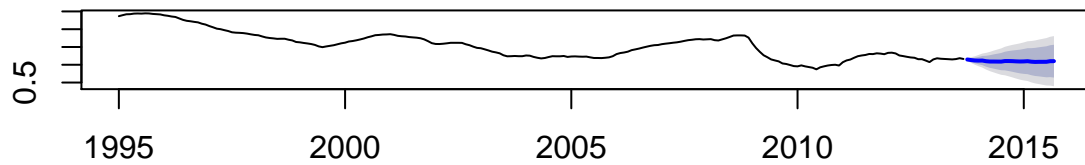


```
fcst3$mean
```

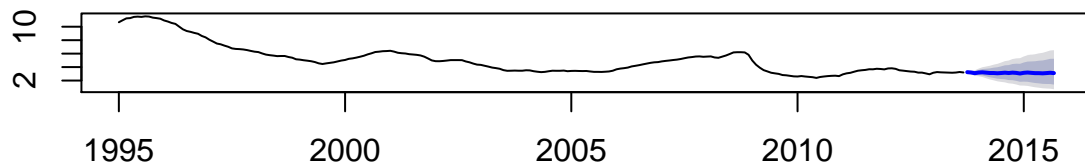
```
##           Jan      Feb      Mar      Apr      May      Jun      Jul
## 2013
## 2014 3.069032 3.071608 2.967108 2.896285 2.867203 2.811453 2.802564
## 2015 2.669507 2.672084 2.567583 2.496760 2.467678 2.411929 2.403039
##           Aug      Sep      Oct      Nov      Dec
## 2013                3.178048 3.112710 3.048582
## 2014 2.834928 2.800475 2.778523 2.713185 2.649057
## 2015 2.435404 2.400951
```

```
par(mfrow=c(2,1))
## in the logarithmic scale (log(a.ts))
lstl=stl(log(g12data), s.window="periodic", robust=TRUE)
fcst4=forecast(lstl, method="arima")
plot(fcst4)
## in the original scale
fcst5=stlf(g12data,method="arima",lambda=BoxCox.lambda(g12data))
plot(fcst5)
```

Forecasts from STL + ARIMA(2,1,0)

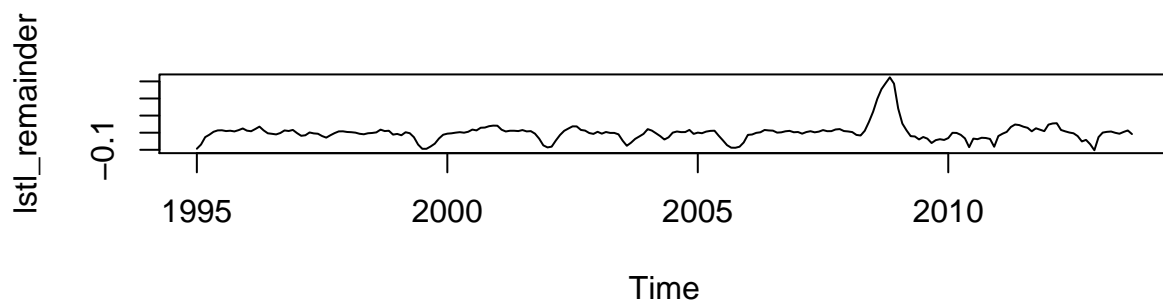
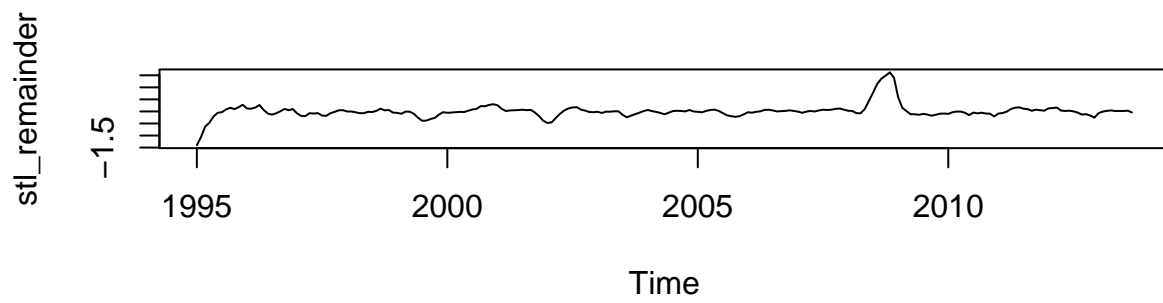


Forecasts from STL + ARIMA(1,1,0)

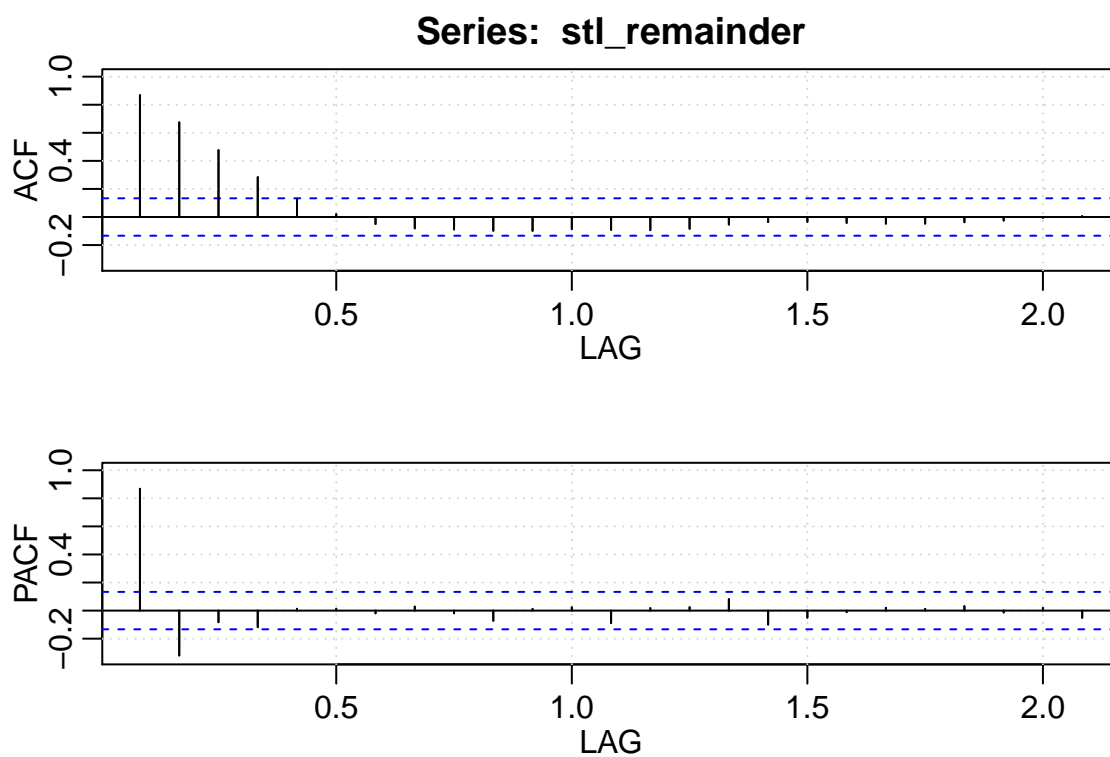


No parece que haya una mejora apreciable al realizar la transformación logarítmica.

```
par(mfrow=c(2,1))
stl_remainder=stl$time.series[,3]
lstl_remainder=lstl$time.series[,3]
plot(stl_remainder)
plot(lstl_remainder)
```

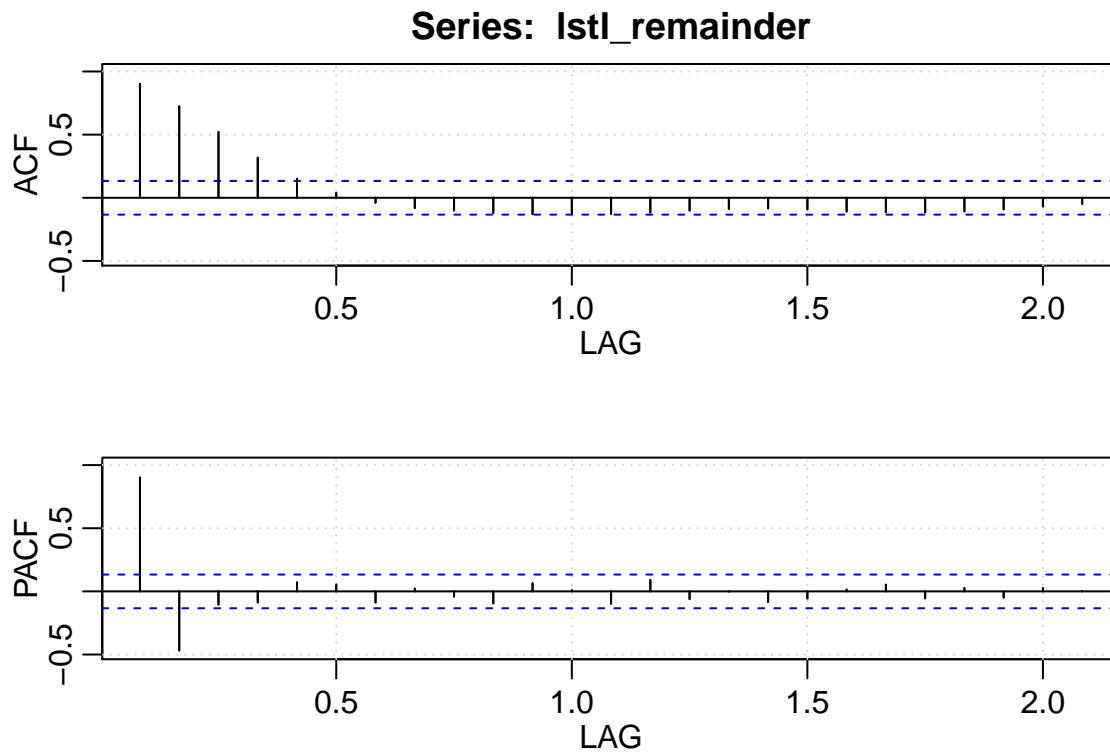


```
acf2(stl_remainder)
```



##		ACF	PACF
##	[1,]	0.87	0.87
##	[2,]	0.67	-0.32
##	[3,]	0.48	-0.08
##	[4,]	0.28	-0.12
##	[5,]	0.13	0.01
##	[6,]	0.02	0.01
##	[7,]	-0.05	-0.02
##	[8,]	-0.08	0.03
##	[9,]	-0.09	-0.02
##	[10,]	-0.10	-0.07
##	[11,]	-0.10	0.01
##	[12,]	-0.09	0.02
##	[13,]	-0.09	-0.09
##	[14,]	-0.09	0.02
##	[15,]	-0.08	0.02
##	[16,]	-0.05	0.08
##	[17,]	-0.04	-0.10
##	[18,]	-0.04	-0.05
##	[19,]	-0.04	-0.01
##	[20,]	-0.05	0.02
##	[21,]	-0.05	0.01
##	[22,]	-0.04	0.03
##	[23,]	-0.03	-0.01
##	[24,]	-0.01	0.02
##	[25,]	0.01	-0.05

```
acf2(lstl_remainder)
```

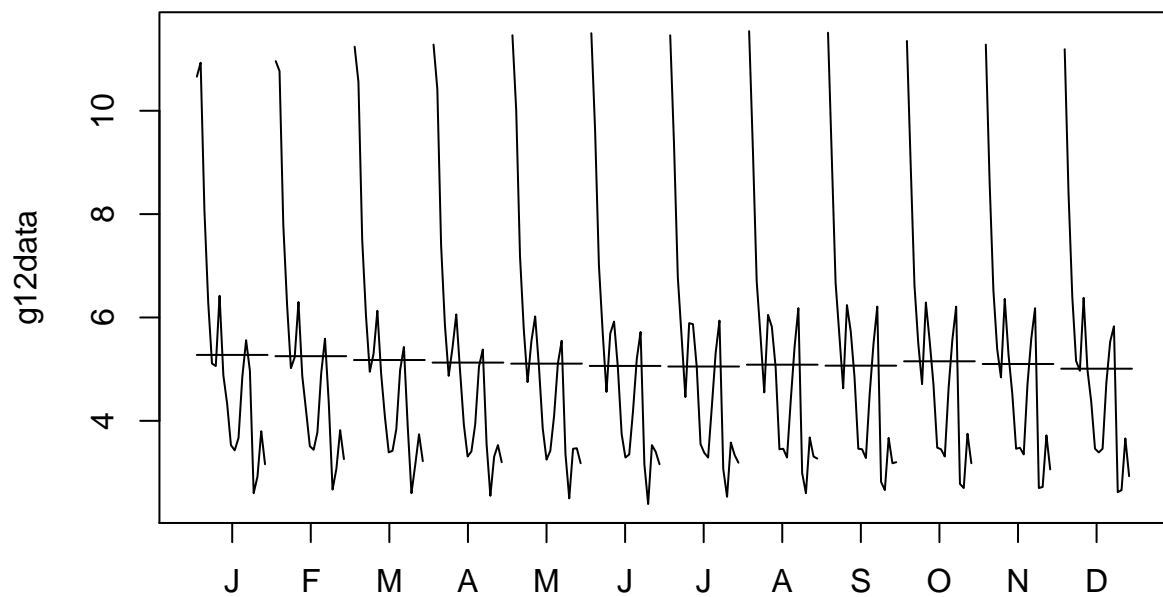


##		ACF	PACF
##	[1,]	0.90	0.90
##	[2,]	0.72	-0.47
##	[3,]	0.52	-0.11
##	[4,]	0.32	-0.09
##	[5,]	0.15	0.07
##	[6,]	0.04	0.05
##	[7,]	-0.04	-0.09
##	[8,]	-0.08	0.02
##	[9,]	-0.10	-0.04
##	[10,]	-0.12	-0.10
##	[11,]	-0.13	0.06
##	[12,]	-0.13	0.01
##	[13,]	-0.13	-0.10
##	[14,]	-0.12	0.09
##	[15,]	-0.10	-0.06
##	[16,]	-0.09	0.00
##	[17,]	-0.08	-0.08
##	[18,]	-0.09	-0.06
##	[19,]	-0.11	0.01
##	[20,]	-0.11	0.05
##	[21,]	-0.12	-0.06
##	[22,]	-0.11	0.03

```
## [23,] -0.09 -0.05  
## [24,] -0.07  0.03  
## [25,] -0.05  0.00
```

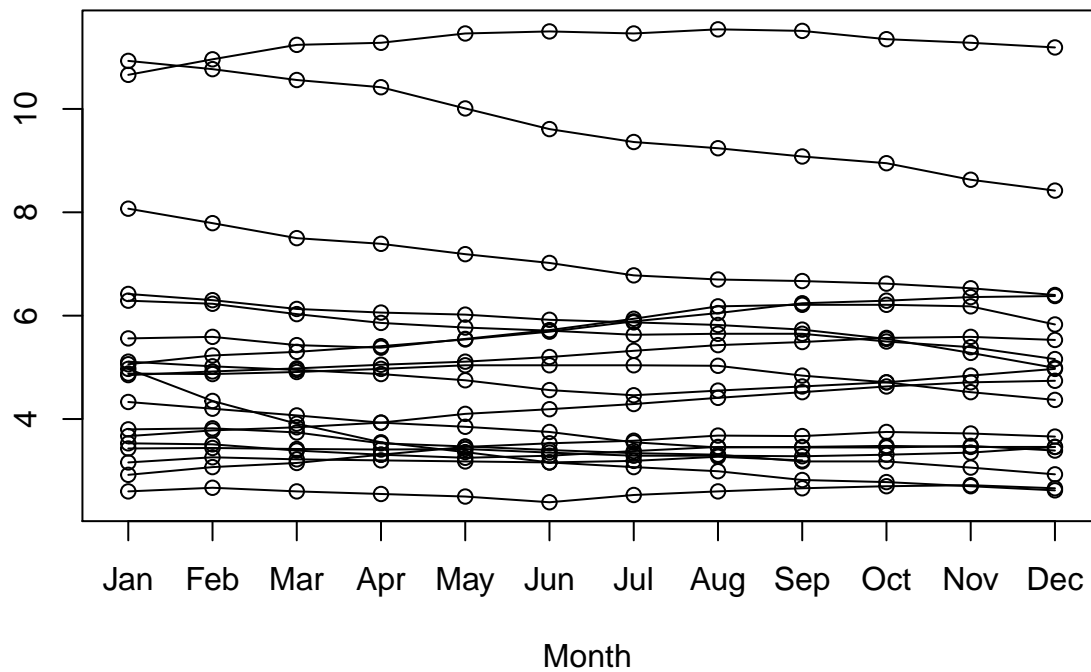
There's not a clear seasonality pattern in the season plot. But in each season trough the years (monthplot) some patterns can be found

```
par(mfrow=c(1,1))  
monthplot(g12data)
```



```
seasonplot(g12data)
```

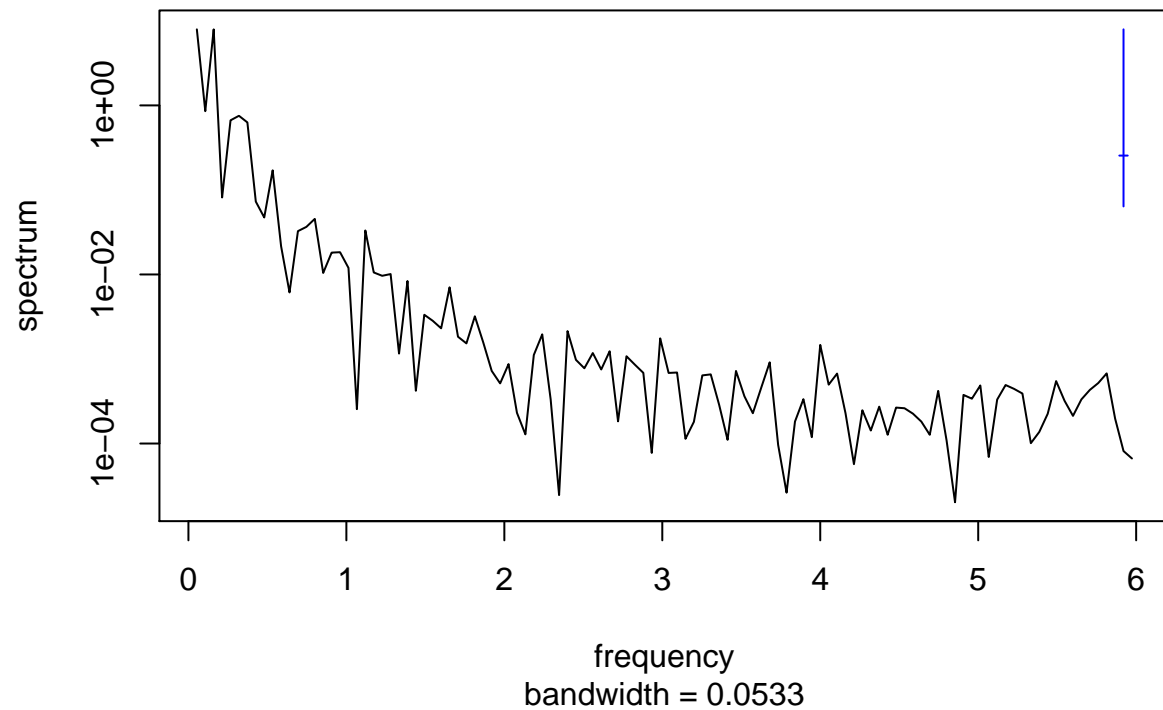
Seasonal plot: g12data



It may help us in determining the period of the series, if any. No idea!!!

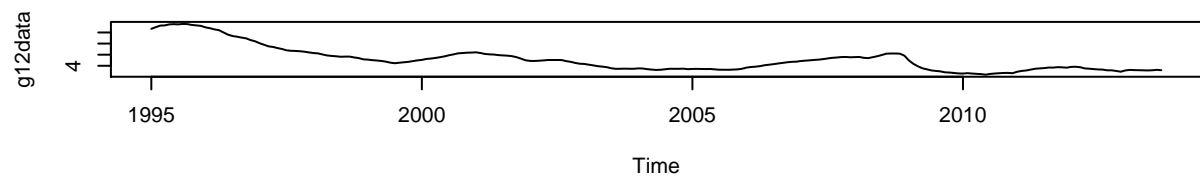
```
mvspec(g12data)
```


Series: g12data
Raw Periodogram

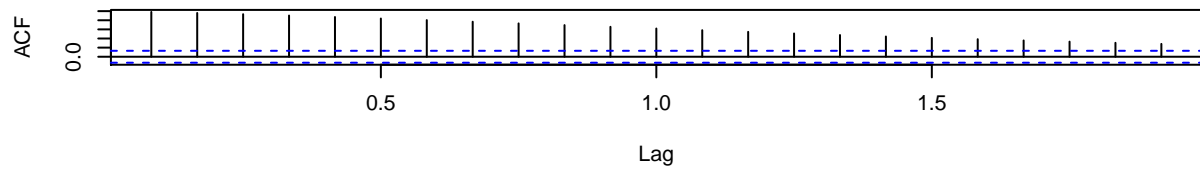


Exploring the autocorrelation structure of time series

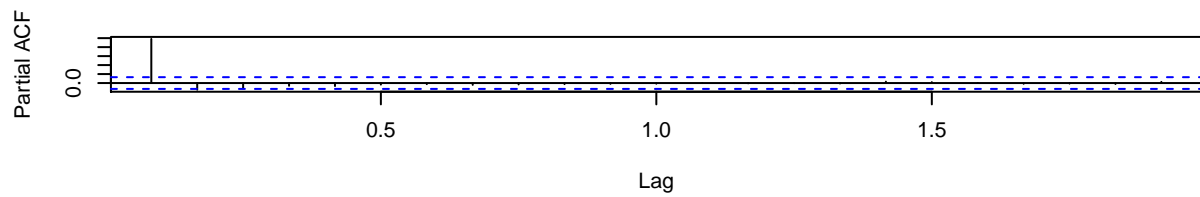
```
par(mfrow=c(3,1))  
plot(g12data)  
acf(g12data)  
pacf(g12data)
```



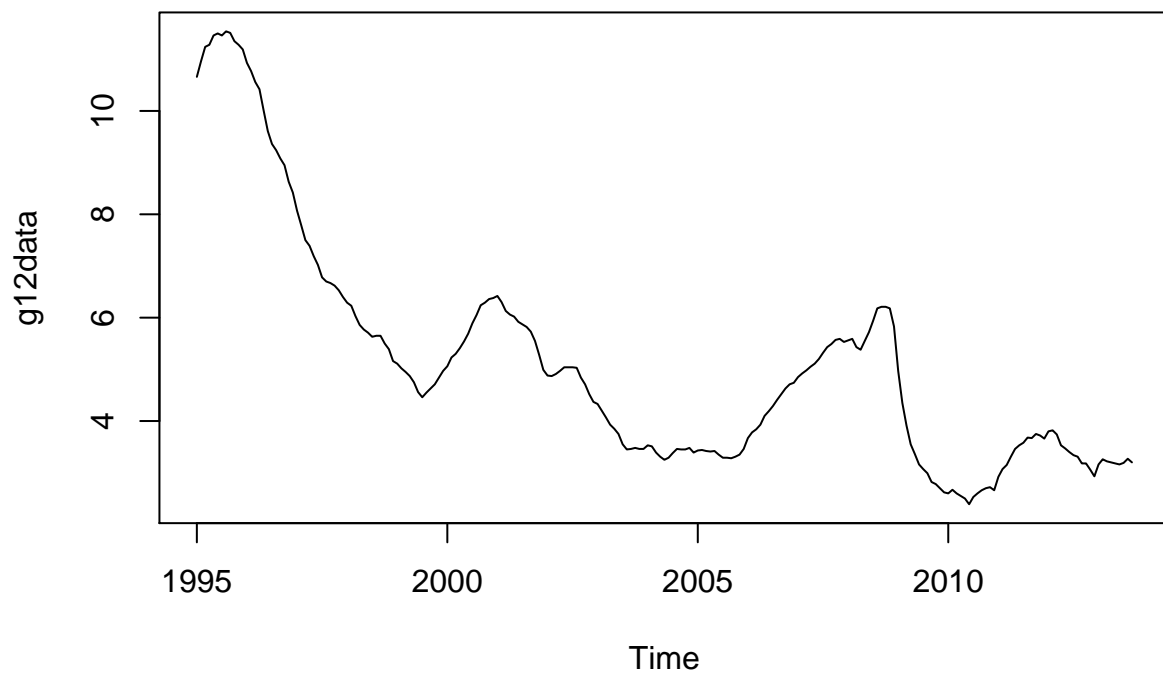
Series g12data



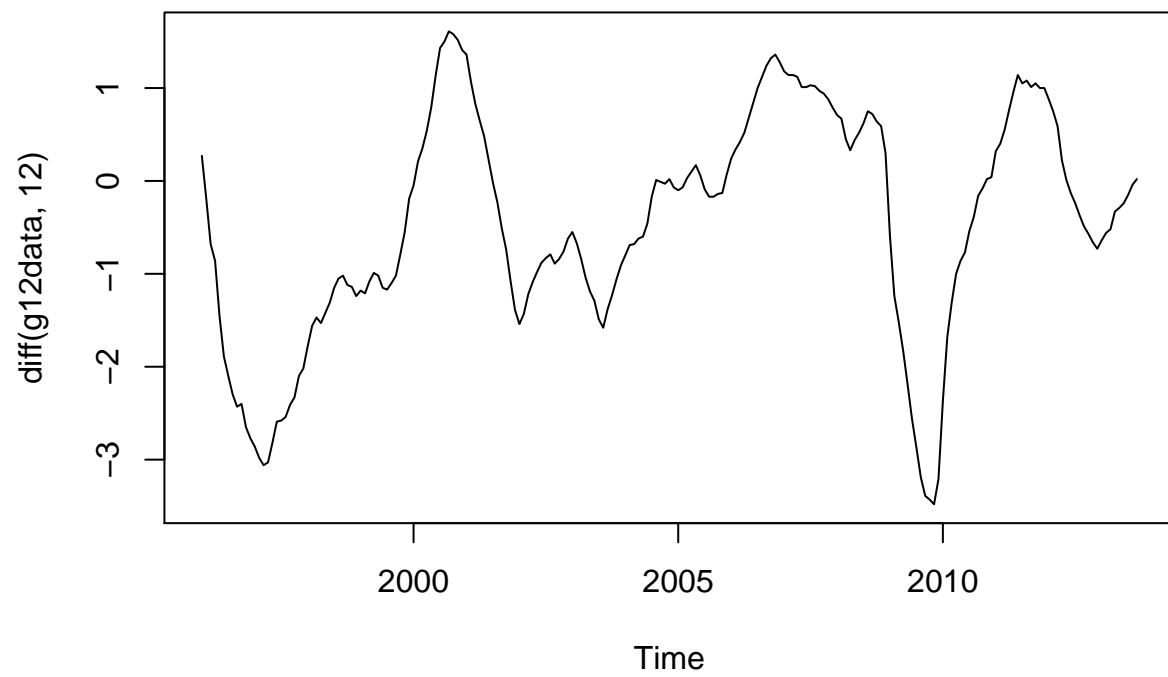
Series g12data



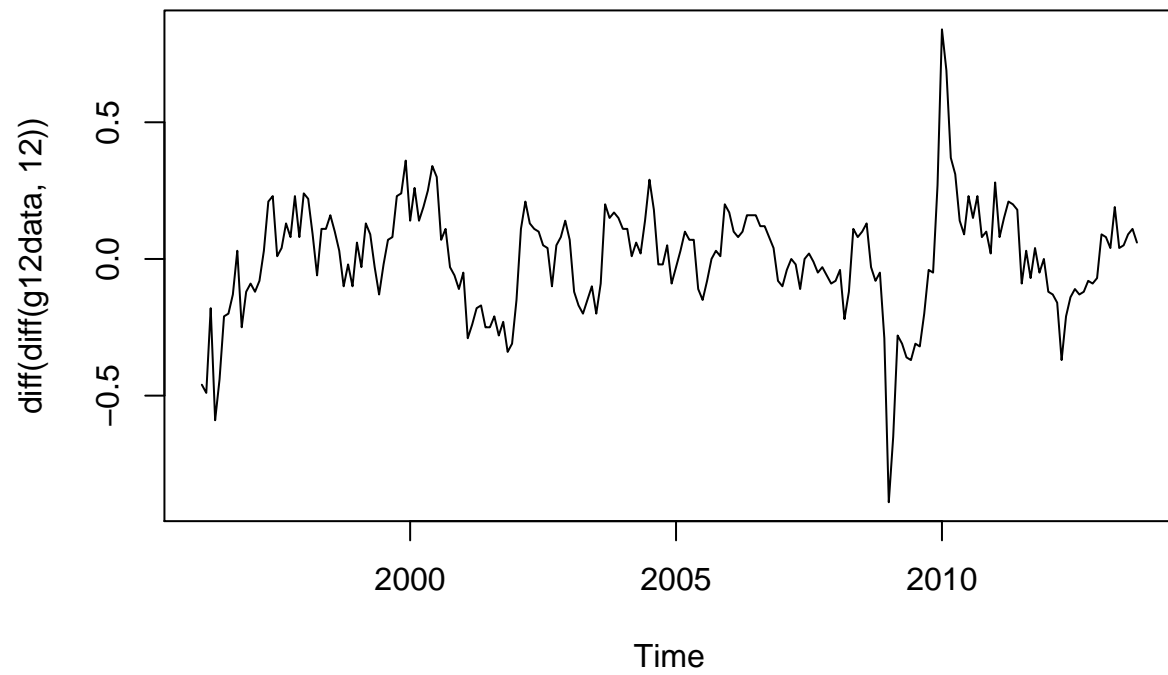
```
plot(g12data)
```



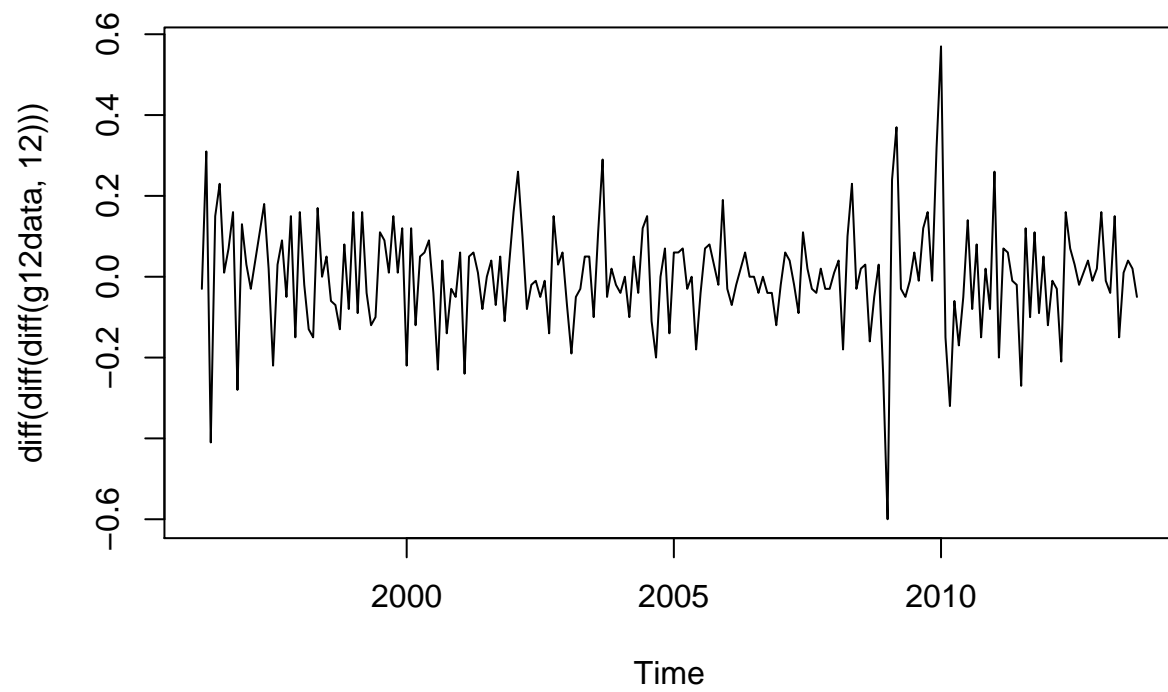
```
plot(diff(g12data,12))
```



```
plot(diff(diff(g12data,12))) #it looks more random
```

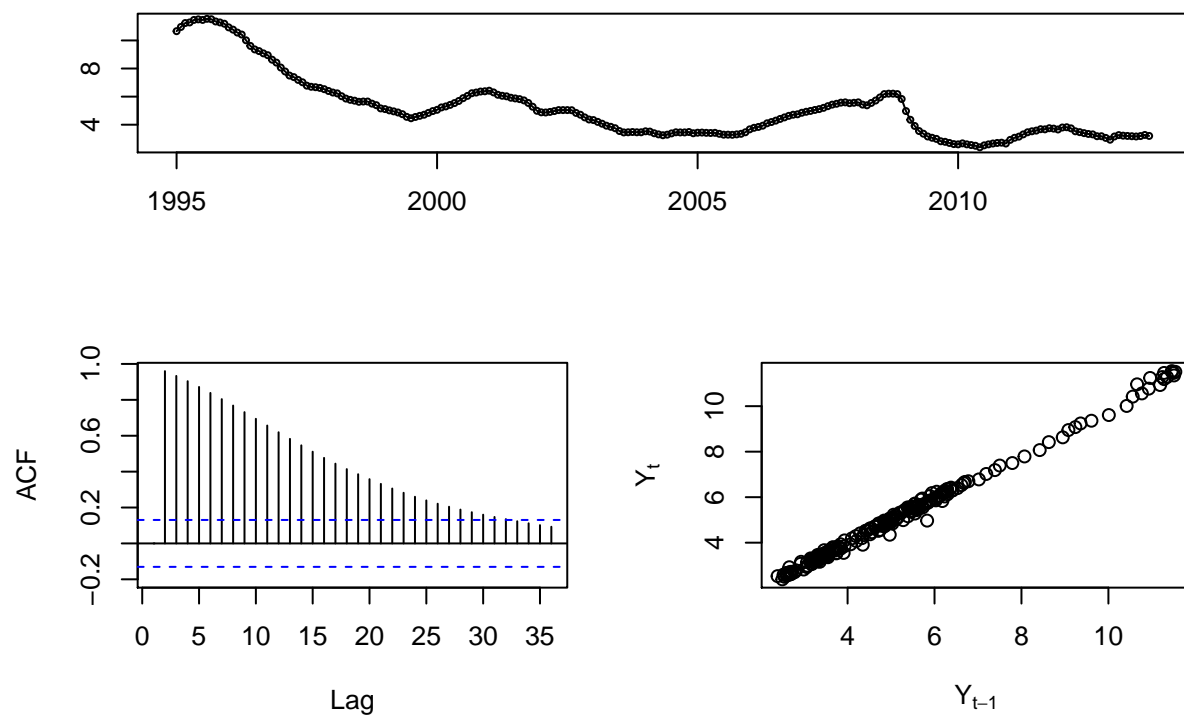


```
plot(diff(diff(diff(g12data,12)))) #it looks more random (seems the best one)
```

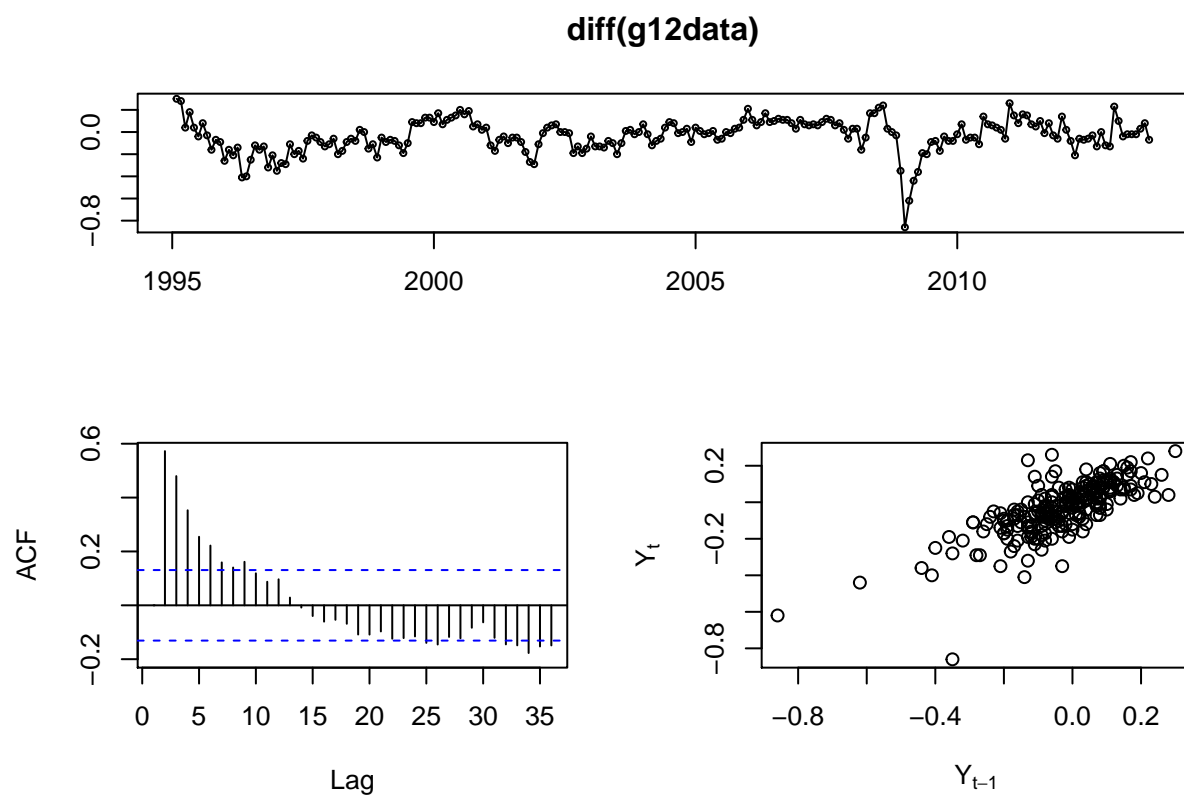


```
# exploring ggb  
tsdisplay(g12data, plot.type="scatter")
```

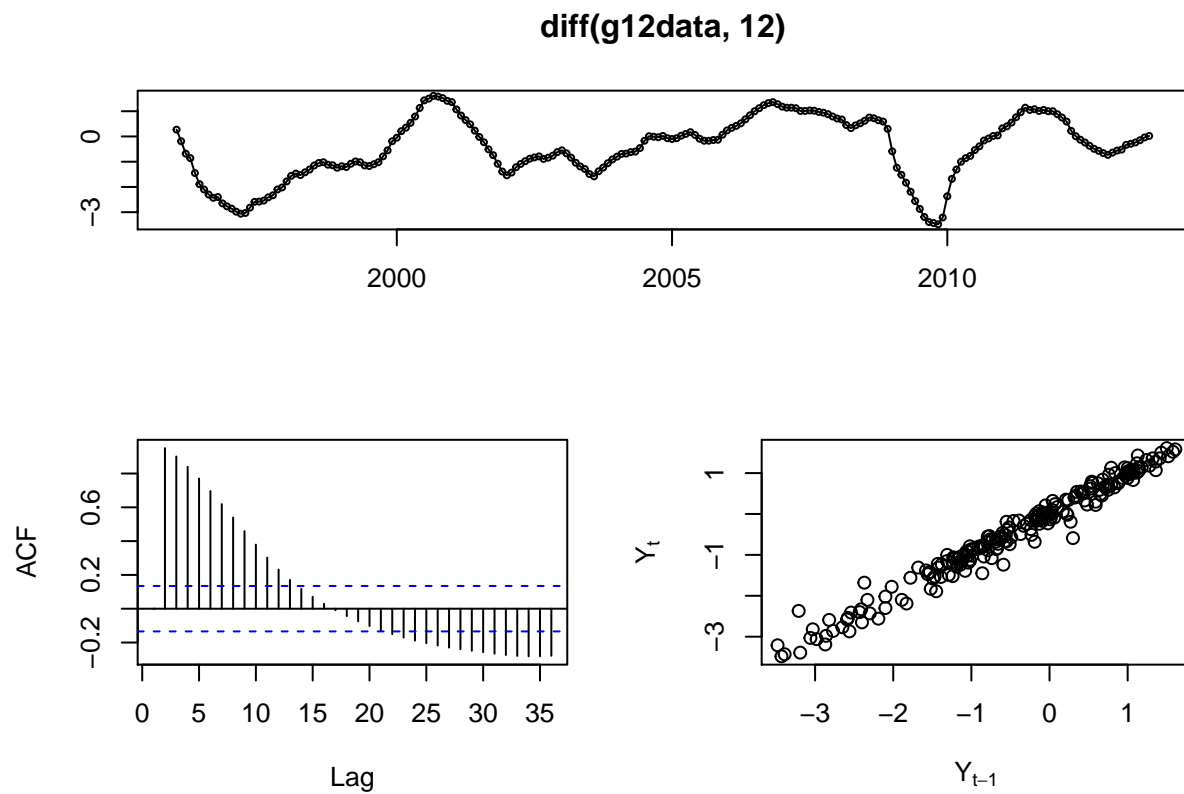
g12data



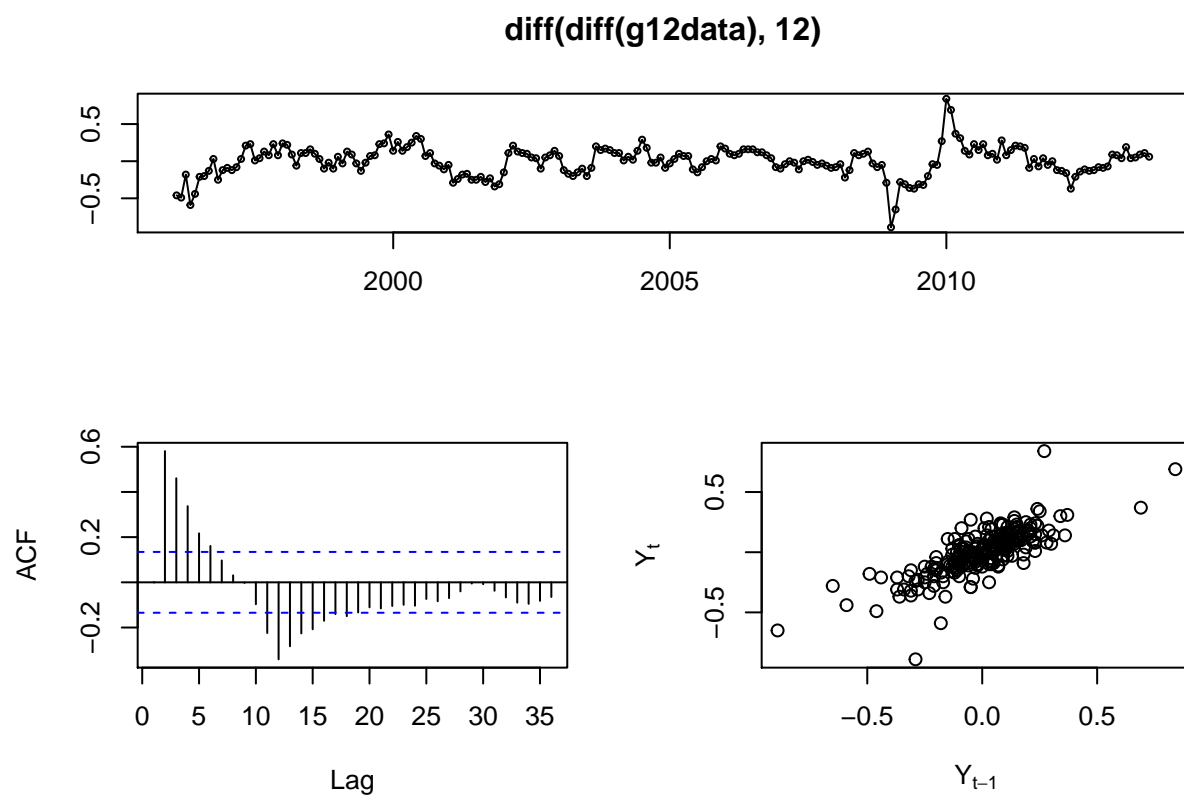
```
tsdisplay(diff(g12data), plot.type="scatter")
```



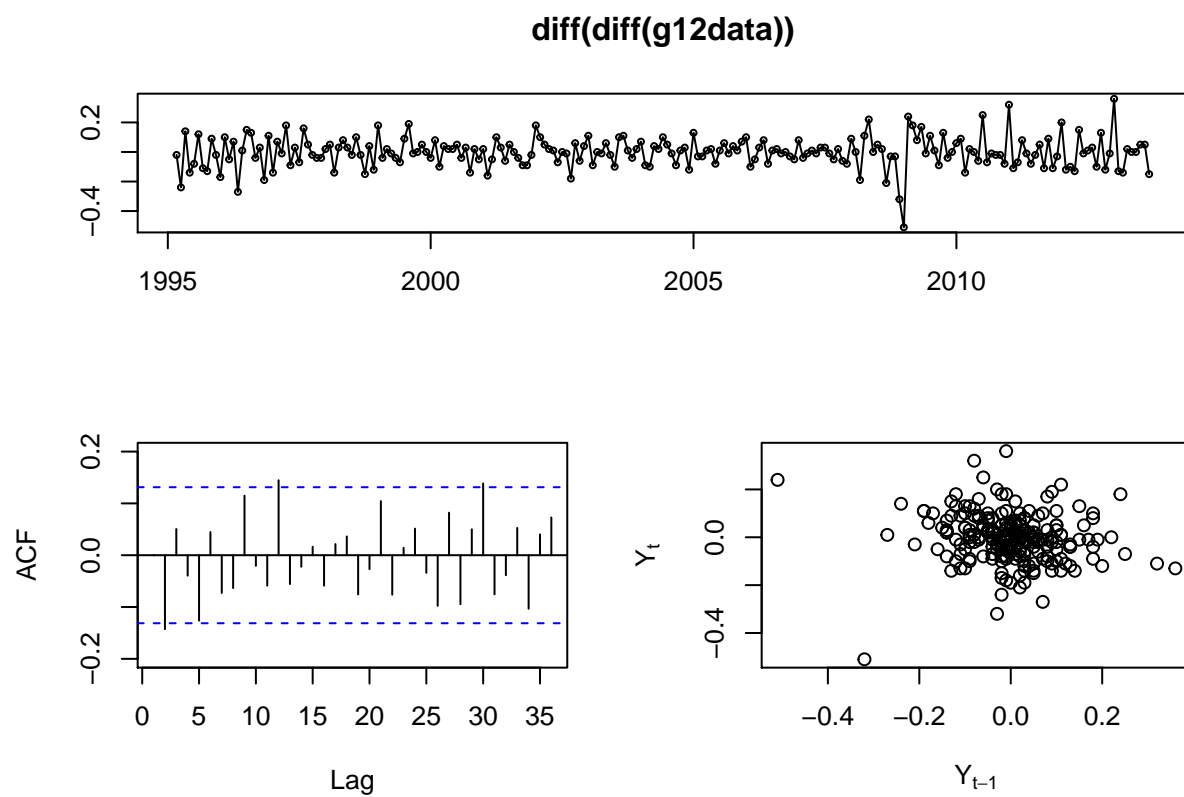
```
tsdisplay(diff(g12data,12), plot.type="scatter")
```

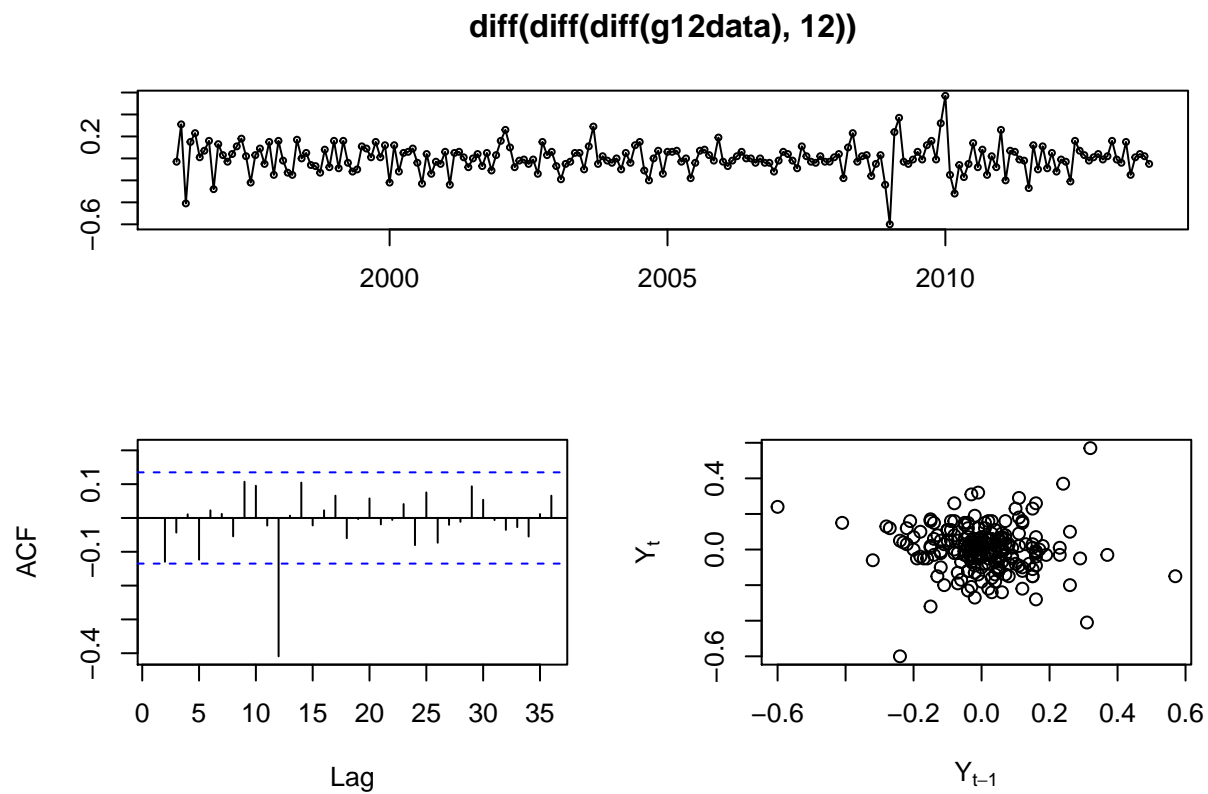
```
tsdisplay(diff(diff(g12data),12), plot.type="scatter")
```



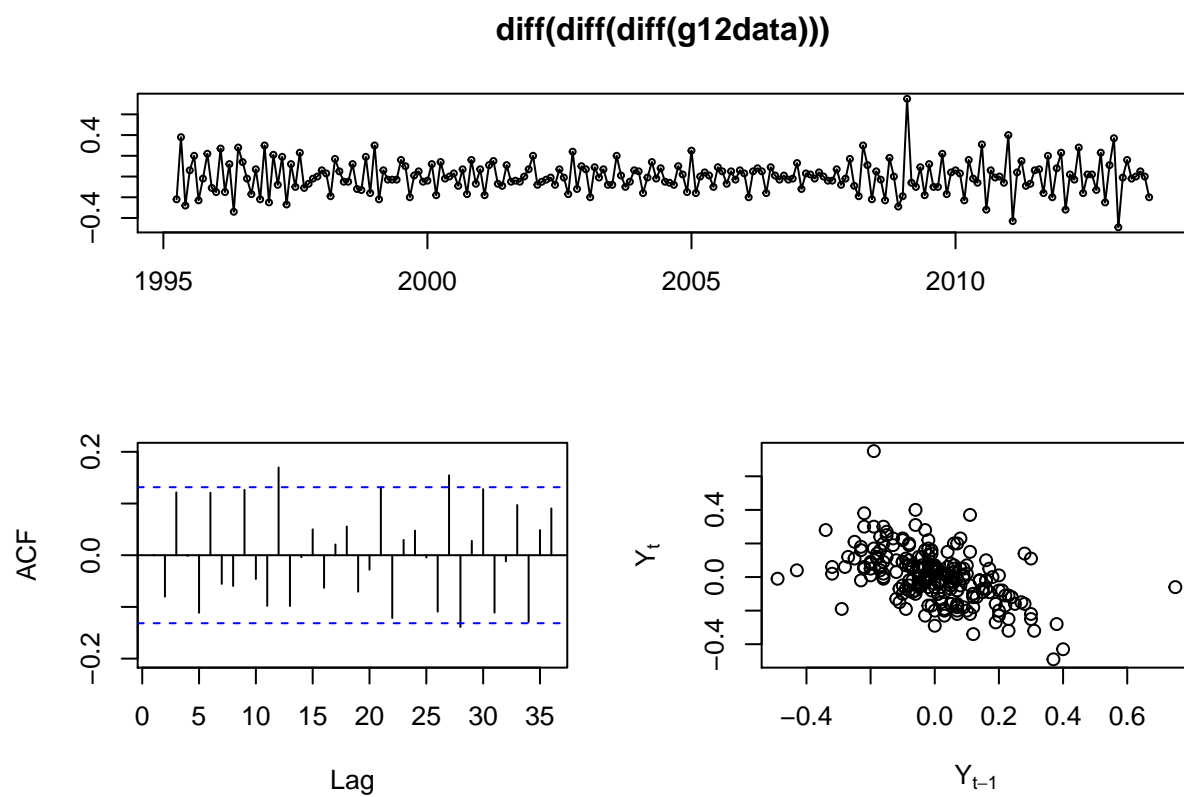
```
tsdisplay(diff(diff(g12data)), plot.type="scatter")
```



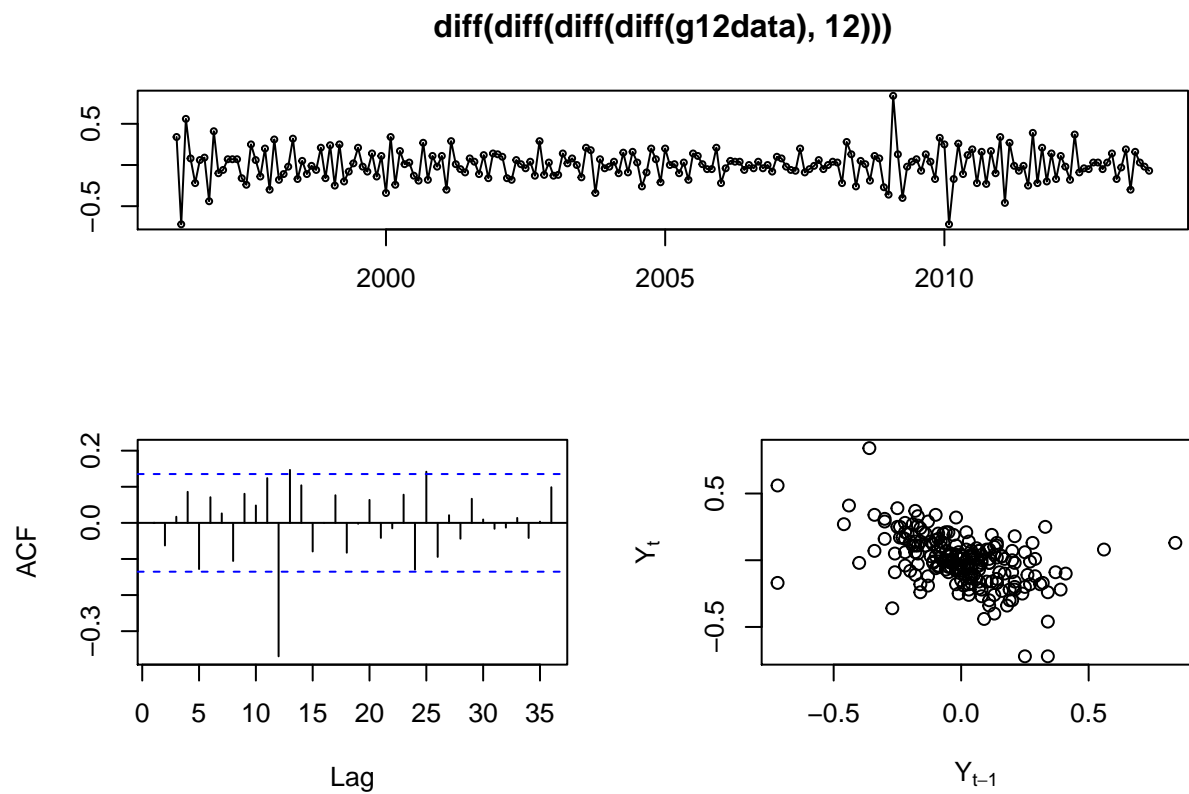
```
tsdisplay(diff(diff(diff(g12data),12)), plot.type="scatter")
```



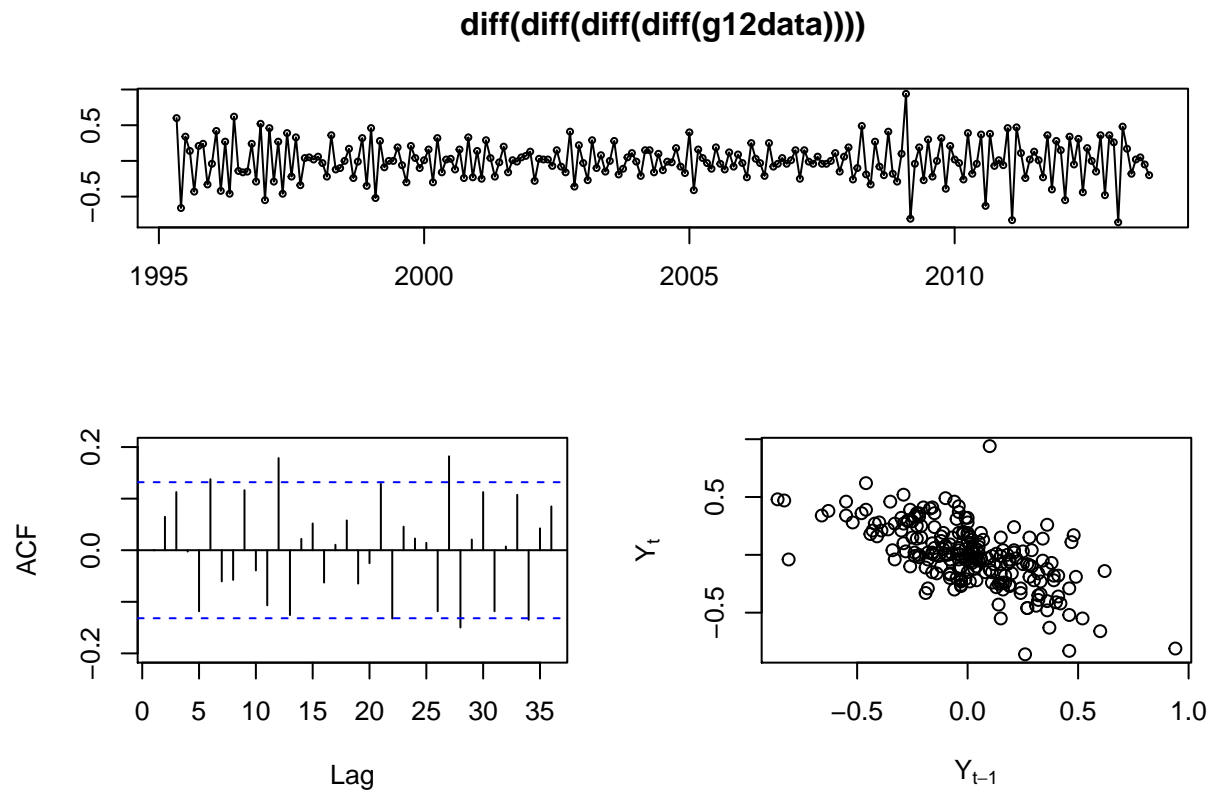
```
tsdisplay(diff(diff(diff(g12data))), plot.type="scatter")
```



```
tsdisplay(diff(diff(diff(diff(g12data),12))), plot.type="scatter") #not improved
```



```
tsdisplay(diff(diff(diff(diff(g12data)))), plot.type="scatter") #not improved (bad)
```



Check if it's stationary to see when we can stop differentiating Can only be applied to seasonality adjusted data (in our case we didn't find a seasonality pattern so it's ok)

```
adf.test(diff(g12data,12))
```

```
##
## Augmented Dickey-Fuller Test
##
## data: diff(g12data, 12)
## Dickey-Fuller = -3.534, Lag order = 5, p-value = 0.04067
## alternative hypothesis: stationary
```

```
adf.test(diff(g12data))
```

```
## Warning in adf.test(diff(g12data)): p-value smaller than printed p-value
```

```
##
## Augmented Dickey-Fuller Test
##
## data: diff(g12data)
## Dickey-Fuller = -4.3715, Lag order = 6, p-value = 0.01
## alternative hypothesis: stationary
```

```
adf.test(diff(diff(g12data,12)))
```

```
## Warning in adf.test(diff(diff(g12data, 12))): p-value smaller than printed  
## p-value
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: diff(diff(g12data, 12))  
## Dickey-Fuller = -4.2591, Lag order = 5, p-value = 0.01  
## alternative hypothesis: stationary
```

```
adf.test(diff(diff(g12data)))
```

```
## Warning in adf.test(diff(diff(g12data))): p-value smaller than printed p-  
## value
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: diff(diff(g12data))  
## Dickey-Fuller = -7.6347, Lag order = 6, p-value = 0.01  
## alternative hypothesis: stationary
```

```
#Check when to stop using standard deviation  
sd(g12data)
```

```
## [1] 2.239662
```

```
sd(diff(g12data)) #BETTER
```

```
## [1] 0.1486072
```

```
sd(diff(g12data,12))
```

```
## [1] 1.205867
```

```
sd(diff(diff(g12data,12)))
```

```
## [1] 0.199808
```

```
sd(diff(diff(g12data))) #Smallest!!! Not seasonality applied
```

```
## [1] 0.1030107
```



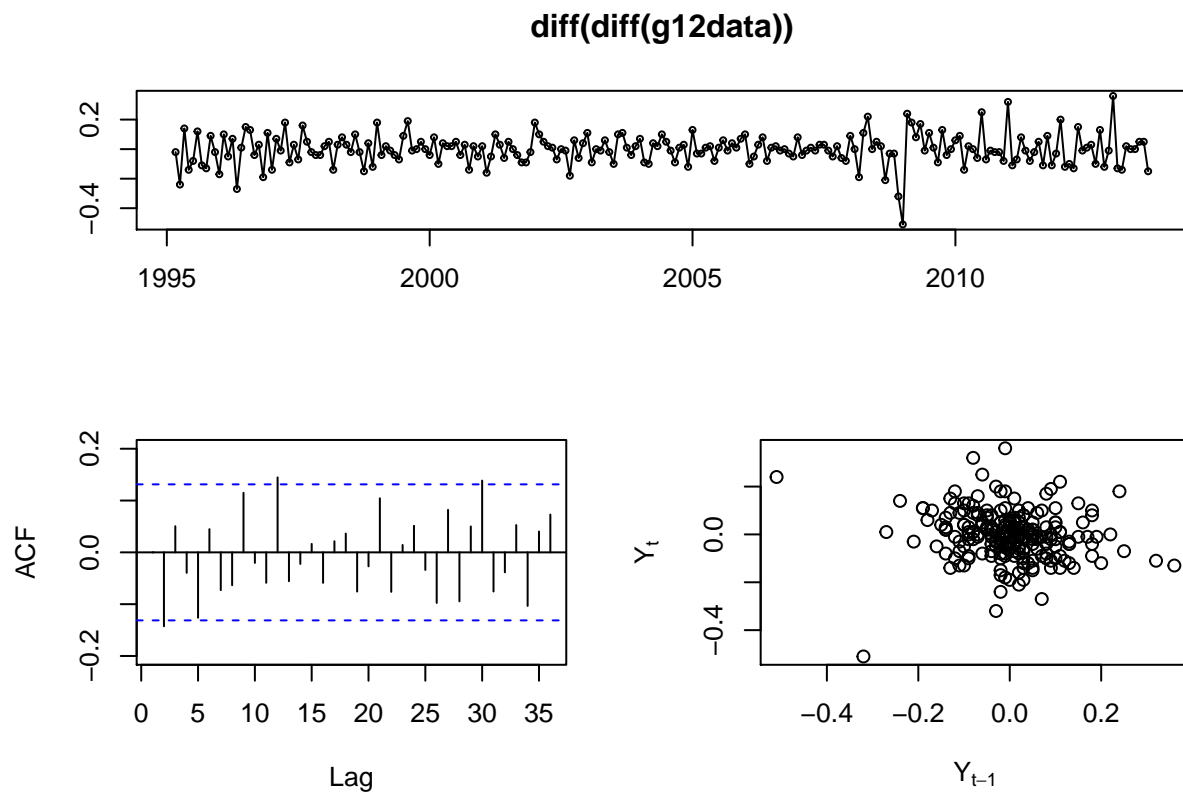
```
sd(diff(diff(diff(g12data,12))))
```

```
## [1] 0.1311037
```

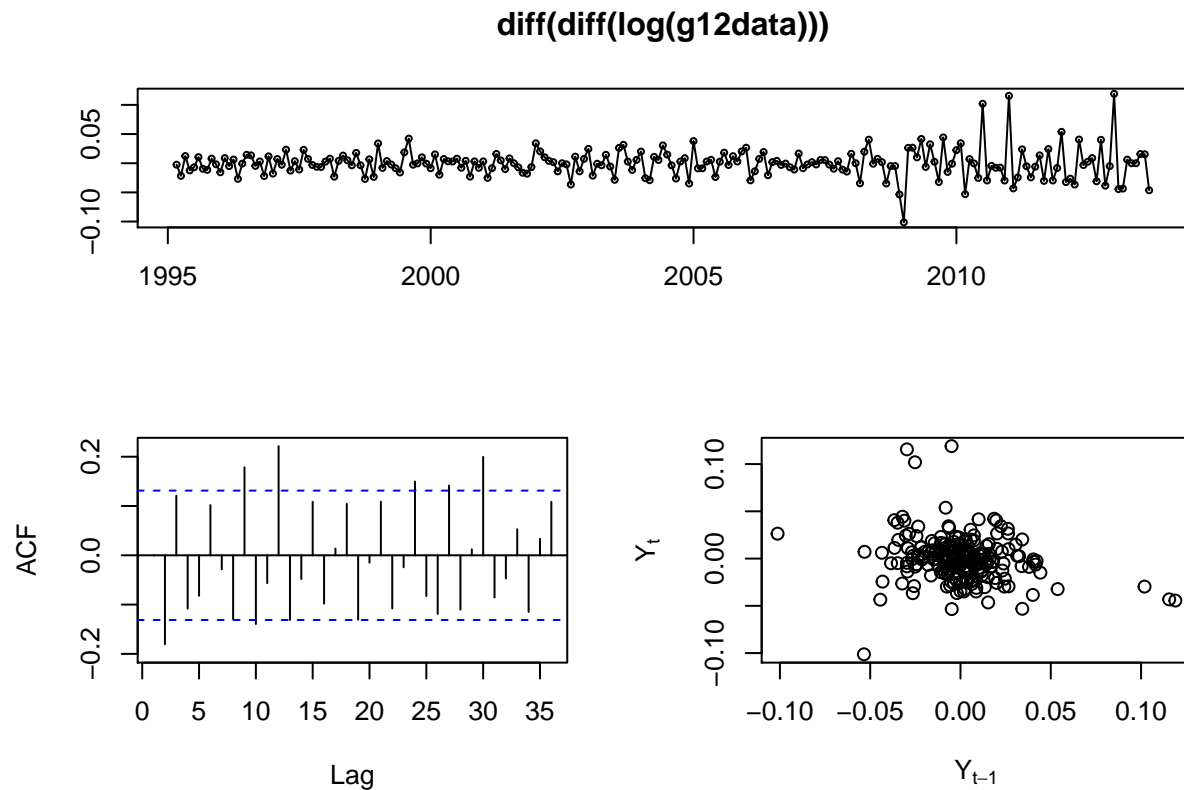
```
sd(diff(diff(diff(g12data))))
```

```
## [1] 0.1562024
```

```
tsdisplay(diff(diff(g12data)), plot.type="scatter")
```



```
tsdisplay(diff(diff(log(g12data))), plot.type="scatter") #Improves slightly (but model is more complicated)
```



ARIMA(p,d,q)(P,D,Q) p->past observations q->past errors d->diferentiation order

D-> seasonal differentiation order (D=0)

```
#We start from 2 normal diffs and none in the seasonal part because
#any diff with period was done before to improve the sd
g12arima.1=Arima(g12data,order=c(0,2,0),include.mean=1,seasonal=list(order=c(0,0,0)))
```

```
#The best one is Arima3
g12arima.2=Arima(g12data,order=c(1,2,0),include.mean=1,seasonal=list(order=c(0,0,0)))
g12arima.3=Arima(g12data,order=c(1,2,1),include.mean=1,seasonal=list(order=c(0,0,0)))
g12arima.4=Arima(g12data,order=c(0,2,1),include.mean=1,seasonal=list(order=c(0,0,0)))

g12arima.4=Arima(g12data,order=c(1,0,1),include.mean=1,seasonal=list(order=c(0,1,0)))
```

```
#The best one now is Arima7
g12arima.5=Arima(g12data,order=c(1,2,1),include.mean=1,seasonal=list(order=c(1,0,1)))
g12arima.6=Arima(g12data,order=c(2,1,1),include.mean=1,seasonal=list(order=c(1,0,1)))
g12arima.7=Arima(g12data,order=c(2,1,0),include.mean=1,seasonal=list(order=c(1,0,1)))
```

```
#my-automatic (d=1 D=0): 1 0 1 0 (sarima)
sarima(g12data,1,1,0,1,0,0,12)
```

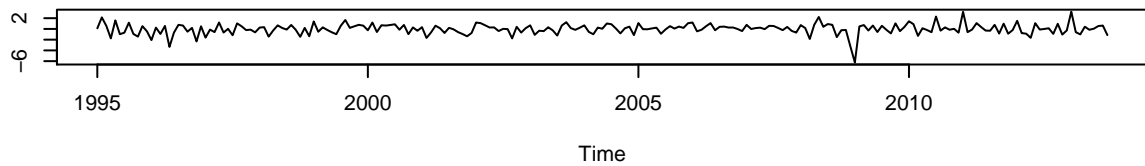
```
## initial value -1.917453
## iter 2 value -2.365786
## iter 3 value -2.366825
```

```

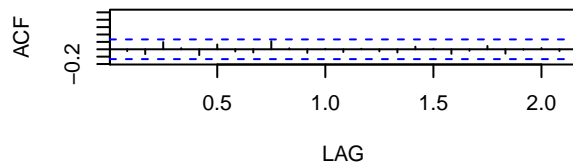
## iter 4 value -2.366826
## iter 5 value -2.366828
## iter 6 value -2.366828
## iter 7 value -2.366831
## iter 8 value -2.366832
## iter 9 value -2.366833
## iter 10 value -2.366833
## iter 10 value -2.366833
## iter 10 value -2.366833
## final value -2.366833
## converged
## initial value -2.344369
## iter 2 value -2.344408
## iter 3 value -2.344421
## iter 4 value -2.344436
## iter 5 value -2.344453
## iter 6 value -2.344469
## iter 7 value -2.344481
## iter 8 value -2.344485
## iter 9 value -2.344485
## iter 10 value -2.344485
## iter 10 value -2.344485
## iter 10 value -2.344485
## final value -2.344485
## converged

```

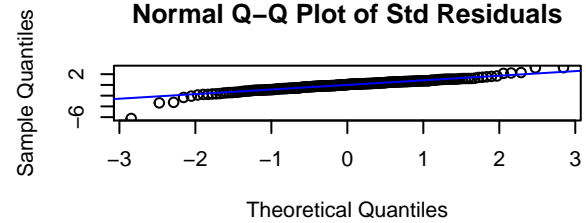
Standardized Residuals



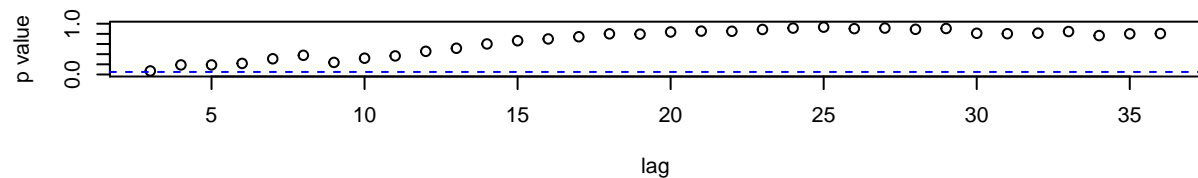
ACF of Residuals



Normal Q-Q Plot of Std Residuals



p values for Ljung-Box statistic



```

## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##      Q), period = S), xreg = constant, optim.control = list(trace = trc, REPORT = 1,
##      reltol = tol))
##
## Coefficients:
##          ar1      sar1  constant
##      0.7679  0.1523   -0.0269
## s.e.  0.0434  0.0704    0.0318
##
## sigma^2 estimated as 0.009148:  log likelihood = 207.32,  aic = -406.64
##
## $AIC
## [1] -3.667596
##
## $AICc
## [1] -3.657899
##
## $BIC
## [1] -4.622048

```

```

#my-automatic (d=2 D=0): 1 1 1 1 (sarima) -> more complex and less aic
sarima(g12data,1,2,1,1,0,1,12)

```

```

## initial  value -2.288639
## iter    2 value -2.302680
## iter    3 value -2.310837
## iter    4 value -2.311133
## iter    5 value -2.318350
## iter    6 value -2.322359
## iter    7 value -2.324525
## iter    8 value -2.328000
## iter    9 value -2.330996
## iter   10 value -2.336800
## iter   11 value -2.339097
## iter   12 value -2.346044
## iter   13 value -2.351003
## iter   14 value -2.354731
## iter   15 value -2.355292
## iter   16 value -2.355456
## iter   17 value -2.356229
## iter   18 value -2.356539
## iter   19 value -2.357263
## iter   20 value -2.357301
## iter   21 value -2.357314
## iter   22 value -2.357359
## iter   23 value -2.357401
## iter   24 value -2.357441
## iter   25 value -2.357454
## iter   26 value -2.357455
## iter   27 value -2.357456
## iter   27 value -2.357456

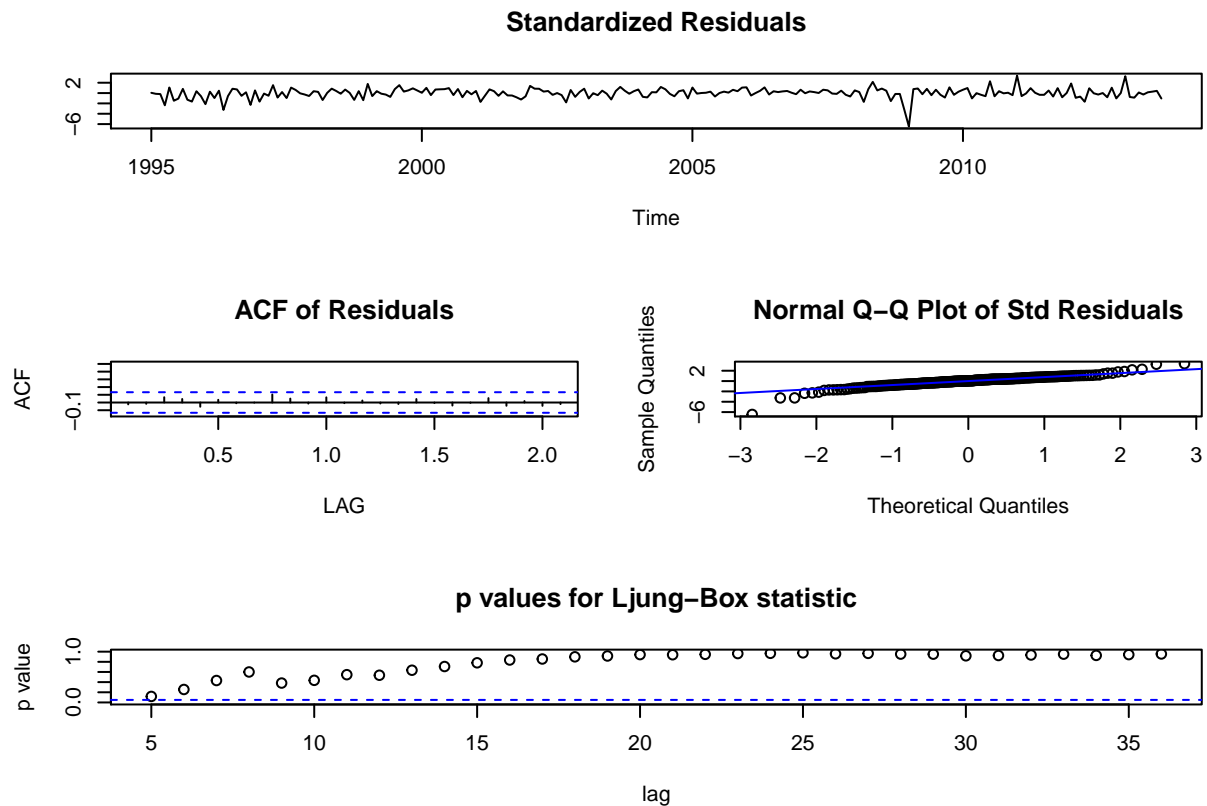
```

```
## iter 27 value -2.357456
## final value -2.357456
## converged
## initial value -2.329487
## iter 2 value -2.334453
## iter 3 value -2.335600
## iter 4 value -2.336010
## iter 5 value -2.336288
## iter 6 value -2.336374
## iter 7 value -2.336381
## iter 8 value -2.336411
## iter 9 value -2.336492
## iter 10 value -2.336606
## iter 11 value -2.336653
## iter 12 value -2.336697
## iter 13 value -2.336725
## iter 14 value -2.336730
## iter 15 value -2.336758
## iter 16 value -2.336784
## iter 17 value -2.336859
## iter 18 value -2.337004
## iter 19 value -2.337293
## iter 20 value -2.337326
## iter 21 value -2.337534
## iter 22 value -2.337589
## iter 23 value -2.337597
## iter 24 value -2.337598
## iter 25 value -2.337629
## iter 26 value -2.337666
## iter 27 value -2.337727
## iter 28 value -2.337835
## iter 29 value -2.337884
## iter 30 value -2.337910
## iter 31 value -2.338006
## iter 32 value -2.338013
## iter 33 value -2.338019
## iter 34 value -2.338039
## iter 35 value -2.338081
## iter 36 value -2.338359
## iter 37 value -2.338374
## iter 38 value -2.338718
## iter 39 value -2.338757
## iter 40 value -2.338781
## iter 41 value -2.338923
## iter 42 value -2.339119
## iter 43 value -2.339412
## iter 44 value -2.339925
## iter 45 value -2.340382
## iter 46 value -2.342693
## iter 47 value -2.342921
## iter 48 value -2.343036
## iter 49 value -2.343080
## iter 50 value -2.343165
## iter 51 value -2.343363
```

```

## iter 52 value -2.343736
## iter 53 value -2.343876
## iter 54 value -2.343978
## iter 55 value -2.343980
## iter 56 value -2.344027
## iter 57 value -2.344041
## iter 58 value -2.344052
## iter 59 value -2.344054
## iter 60 value -2.344054
## iter 61 value -2.344062
## iter 62 value -2.344066
## iter 63 value -2.344069
## iter 64 value -2.344069
## iter 64 value -2.344069
## iter 64 value -2.344069
## final value -2.344069
## converged

```



```

## $fit
##
## Call:
## stats::arima(x = xdata, order = c(p, d, q), seasonal = list(order = c(P, D,
##     Q), period = S), include.mean = !no.constant, optim.control = list(trace = trc,
##     REPORT = 1, reltol = tol))
##

```

```
## Coefficients:
##          ar1      ma1      sar1      sma1
##      0.7897 -1.00  0.9537 -0.8819
## s.e.  0.0436  0.01  0.0610  0.1001
##
## sigma^2 estimated as 0.009001:  log likelihood = 206.3,  aic = -402.61
##
## $AIC
## [1] -3.674919
##
## $AICc
## [1] -3.664812
##
## $BIC
## [1] -4.614188
```

```
#The one obtained with my-automatic is better (less aic and less complex)
g12arima.8=Arima(g12data,order=c(1,1,0),include.mean=1,seasonal=list(order=c(1,0,0)))
auto.arima(g12data)
```

```
## Series: g12data
## ARIMA(2,1,1)(2,0,0)[12]
##
## Coefficients:
```

```
## Warning in sqrt(diag(x$var.coef)): Se han producido NaNs
```

```
##          ar1      ar2      ma1      sar1      sar2
##      -0.0471  0.6336  0.8311  0.1583  0.0089
## s.e.      NaN      NaN      NaN  0.0709  0.0762
##
## sigma^2 estimated as 0.009169:  log likelihood=207.03
## AIC=-402.06  AICc=-401.68  BIC=-381.59
```

```
AIC(g12arima.1)
```

```
## [1] -379.8211
```

```
AIC(g12arima.2)
```

```
## [1] -382.8607
```

```
AIC(g12arima.3)
```

```
## [1] -398.6795
```

```
AIC(g12arima.4)
```

```
## [1] -201.8503
```

```
AIC(g12arima.5)
```

```
## [1] -402.608
```

```
AIC(g12arima.6)
```

```
## [1] -404.0317
```

```
AIC(g12arima.7) #This is the best one (it is the lowest one)
```

```
## [1] -406.672
```

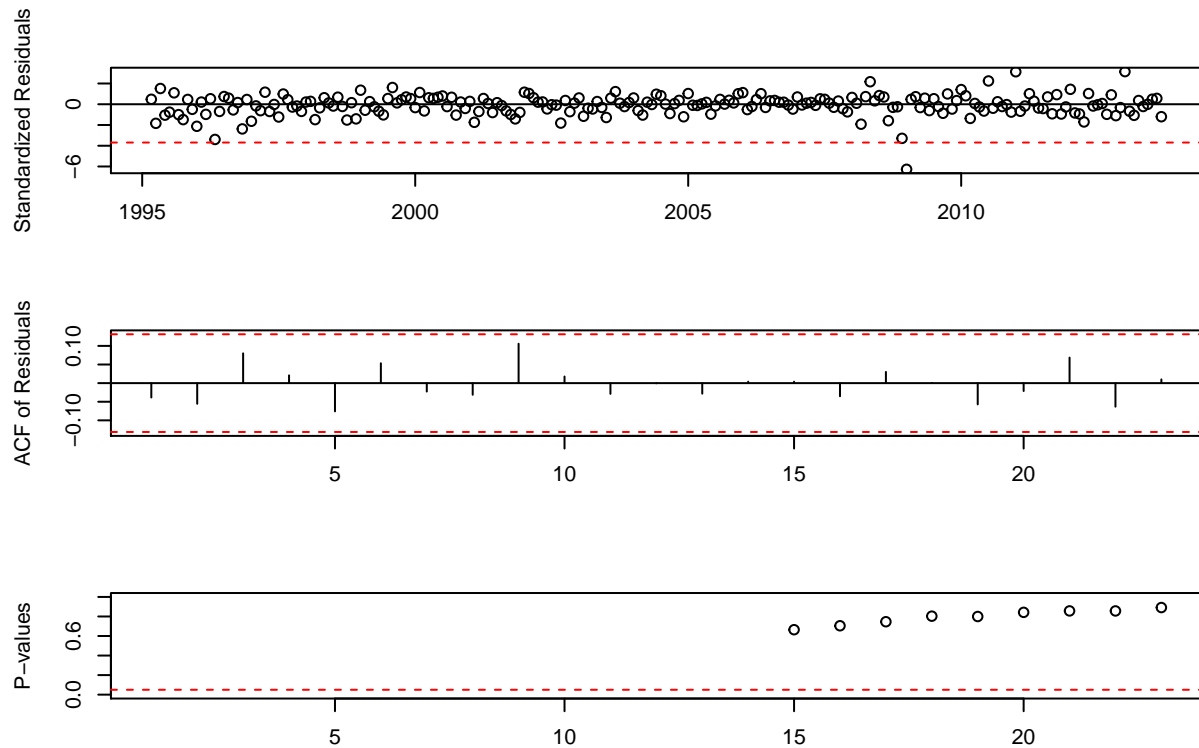
```
AIC(g12arima.8) #This is the best one (it is the lowest one being simpler)
```

```
## [1] -407.9574
```

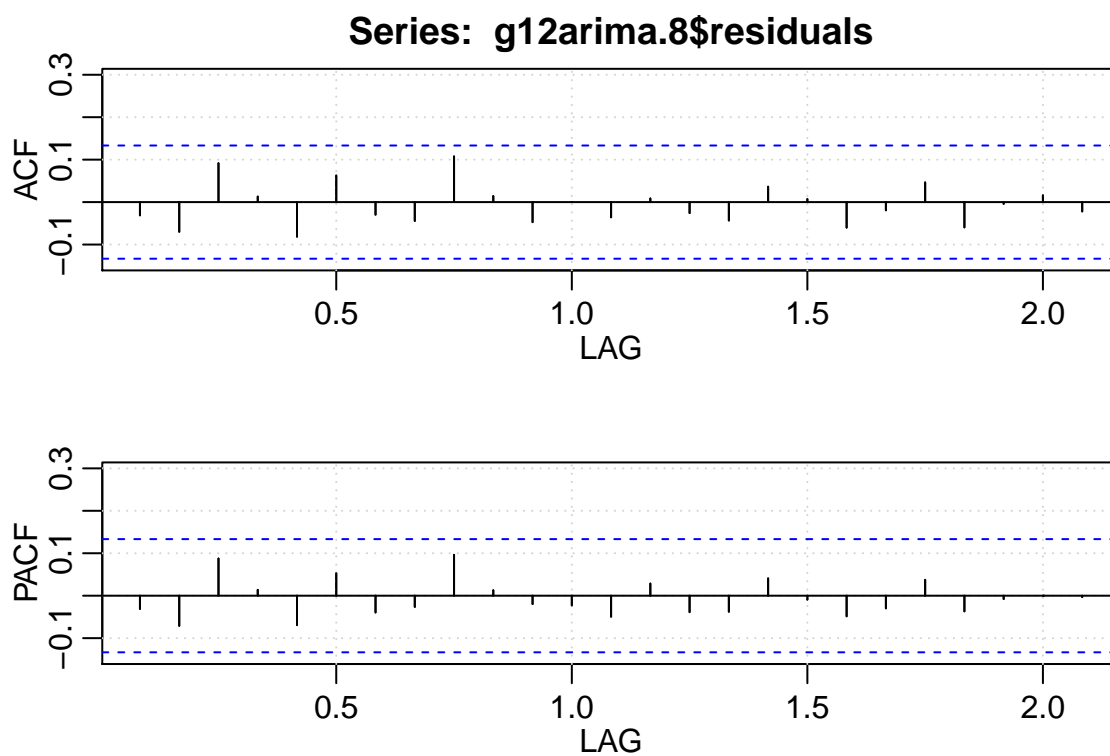
We'll keep the last one

Maybe compare them with bad ones?? WTF?

```
tsdiag(g12arima.8)
```




```
acf2(g12arima.8$residuals)
```



##		ACF	PACF
##	[1,]	-0.03	-0.03
##	[2,]	-0.07	-0.07
##	[3,]	0.09	0.09
##	[4,]	0.01	0.01
##	[5,]	-0.08	-0.07
##	[6,]	0.06	0.05
##	[7,]	-0.03	-0.04
##	[8,]	-0.04	-0.03
##	[9,]	0.11	0.10
##	[10,]	0.01	0.01
##	[11,]	-0.05	-0.02
##	[12,]	0.00	-0.02
##	[13,]	-0.04	-0.05
##	[14,]	0.01	0.03
##	[15,]	-0.03	-0.04
##	[16,]	-0.04	-0.04
##	[17,]	0.04	0.04
##	[18,]	0.01	-0.01
##	[19,]	-0.06	-0.05
##	[20,]	-0.02	-0.03
##	[21,]	0.05	0.04
##	[22,]	-0.06	-0.04

```
## [23,] 0.00 -0.01
## [24,] 0.02 0.00
## [25,] -0.02 0.00
```

```
#correlations between model coefficients
cov2cor(g12arima.8$var.coef) #Not greater than 0.8 so it is good
```

```
##          ar1          sar1
## ar1  1.00000000 0.01790429
## sar1 0.01790429 1.00000000
```

```
#testing independence of the residuals (apparently they are not independent???)
#CHECK THE P-VALUES (are them white noise or not???)
LB.test(g12arima.8) #it seems ok because in the bubble example the values are the same
```

```
##
## Box-Ljung test
##
## data: residuals from g12arima.8
## X-squared = 9.8561, df = 10, p-value = 0.4532
```

```
#or
LB.test(g12arima.8, lag=20)
```

```
##
## Box-Ljung test
##
## data: residuals from g12arima.8
## X-squared = 12.098, df = 18, p-value = 0.8421
```

```
#normality of the residuals
jarque.bera.test(residuals(g12arima.8)) #less than 0.05, they are not normal (seems bad)
```

```
##
## Jarque Bera Test
##
## data: residuals(g12arima.8)
## X-squared = 505.13, df = 2, p-value < 2.2e-16
```

```
#Checks the independence in a time series (greater than 0.05 seems alright)
Box.test(residuals(g12arima.8),lag=12)
```

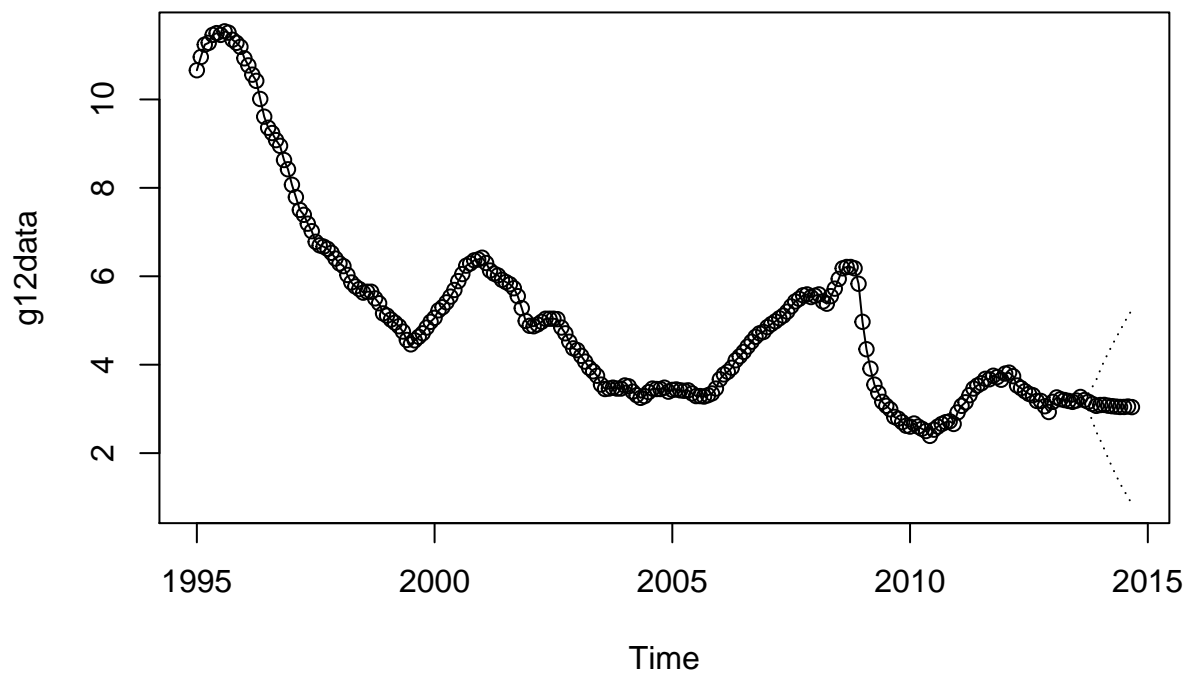
```
##
## Box-Pierce test
##
## data: residuals(g12arima.8)
## X-squared = 9.4269, df = 12, p-value = 0.6661
```

#So the residuals seem normal but not independent

```
## Forecasting with the model lynx.3  
predict(g12arima.8,n.ahead=20)
```

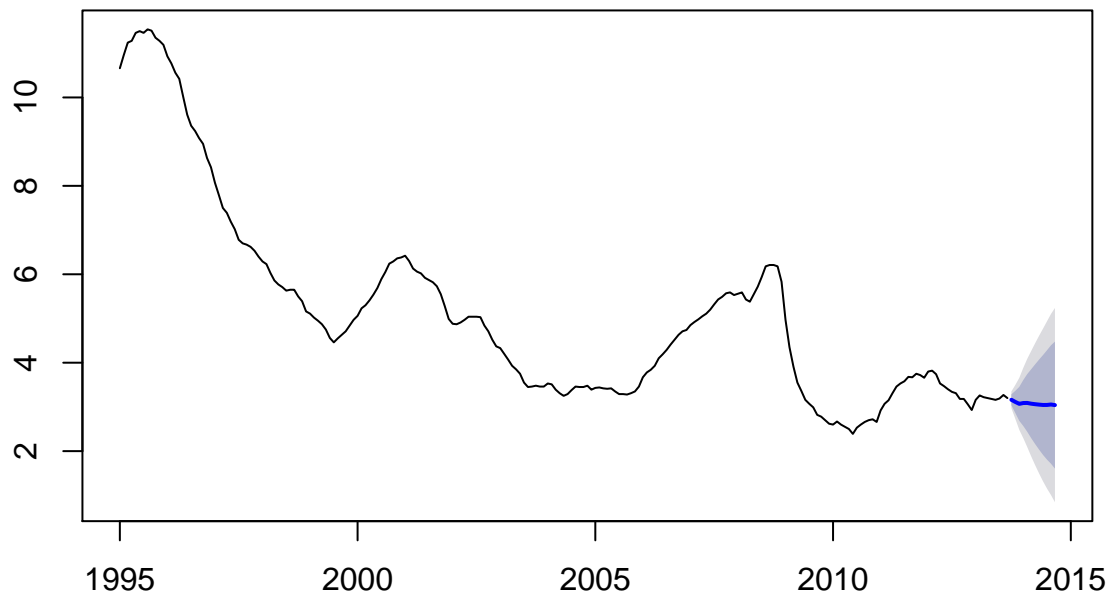
```
## $pred  
##      Jan      Feb      Mar      Apr      May      Jun      Jul  
## 2013  
## 2014 3.088048 3.090078 3.073036 3.061571 3.051973 3.043821 3.044712  
## 2015 3.018141 3.017814 3.014611 3.012406 3.010583  
##      Aug      Sep      Oct      Nov      Dec  
## 2013              3.161711 3.113026 3.069434  
## 2014 3.054393 3.040984 3.033120 3.024014 3.016029  
## 2015  
##  
## $se  
##      Jan      Feb      Mar      Apr      May      Jun  
## 2013  
## 2014 0.40484209 0.50788243 0.60756348 0.70327324 0.79479915 0.88215913  
## 2015 1.43162373 1.50639006 1.57925959 1.65014272 1.71902671  
##      Jul      Aug      Sep      Oct      Nov      Dec  
## 2013              0.09577884 0.19513118 0.29974721  
## 2014 0.96550099 1.04504139 1.12102862 1.19901895 1.27741513 1.35516915  
## 2015
```

```
TSA::plot.Arima(g12arima.8) #TSA package
```



```
plot(forecast(g12arima.8,h=12))
```

Forecasts from ARIMA(1,1,0)(1,0,0)[12]



```
forecast(g12arima.8,h=12) #same predictions plotted with the TSA package
```

	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## Oct 2013	3.161711	3.038966	3.284457	2.9739881	3.349434
## Nov 2013	3.113026	2.862956	3.363097	2.7305762	3.495476
## Dec 2013	3.069434	2.685292	3.453575	2.4819401	3.656928
## Jan 2014	3.088048	2.569222	3.606874	2.2945724	3.881524
## Feb 2014	3.090078	2.439200	3.740955	2.0946466	4.085509
## Mar 2014	3.073036	2.294412	3.851660	1.8822334	4.263839
## Apr 2014	3.061571	2.160290	3.962852	1.6831809	4.439961
## May 2014	3.051973	2.033397	4.070549	1.4941952	4.609751
## Jun 2014	3.043821	1.913289	4.174354	1.3148212	4.772821
## Jul 2014	3.044712	1.807373	4.282052	1.1523650	4.937059
## Aug 2014	3.054393	1.715119	4.393668	1.0061497	5.102637
## Sep 2014	3.040984	1.604328	4.477640	0.8438082	5.238160

We could try logs to see if the bad distribution of the residuals is fixed.

```
g12arima.9=Arima(log(g12data),order=c(1,1,0),include.mean=1,seasonal=list(order=c(1,0,0)))
AIC(g12arima.9) #aic lower than before (by a lot)
```

```
## [1] -1074.566
```

```
cov2cor(g12arima.9$var.coef) #Not greater than 0.8 so it is good
```

```
##          ar1      sar1
## ar1  1.000000 0.128937
## sar1 0.128937 1.000000
```

```
#testing independence of the residuals (apparently they are not independent???)
```

```
#CHECK THE P-VALUES (are them white noise or not???)
```

```
LB.test(g12arima.9) #it seems ok because in the first example the values are the same (it is lower now
```

```
##
## Box-Ljung test
##
## data: residuals from g12arima.9
## X-squared = 16.193, df = 10, p-value = 0.09425
```

```
#or
```

```
LB.test(g12arima.9, lag=20)
```

```
##
## Box-Ljung test
##
## data: residuals from g12arima.9
## X-squared = 23.981, df = 18, p-value = 0.1557
```

```
#normality of the residuals
```

```
jarque.bera.test(residuals(g12arima.9)) #less than 0.05, they are not normal (seems bad)
```

```
##
## Jarque Bera Test
##
## data: residuals(g12arima.9)
## X-squared = 612.57, df = 2, p-value < 2.2e-16
```

```
#Checks the independence in a time series (greater than 0.05 seems alright)
```

```
Box.test(residuals(g12arima.9),lag=12) #She uses it instead of jarque.bera when the other doesn't work
```

```
##
## Box-Pierce test
##
## data: residuals(g12arima.9)
## X-squared = 15.569, df = 12, p-value = 0.2118
```

We don't take logs as it doesn't improve anything