

Homework Assignments

MATH231

Spring 2022

1	Homework 0	2
2	Homework 1	4

Homework 0

Due: Friday, Jan 21 (no need to turn in)

1. Calculating Limits

- $\lim_{x \rightarrow 2} \frac{x^2 + x - 6}{x - 2}$
- $\lim_{h \rightarrow 0} \frac{(x + h)^2 - x^2}{h}$
- $\lim_{x \rightarrow 0} \left(\frac{1}{x} - \frac{1}{x^2 + x} \right)$

2. The Chain Rule

- $\frac{d}{dx} \ln(x + \sin x)$
- $\frac{d}{dx} \cos(x^2 e^x)$

3. Implicit Differentiation: Solve for $\frac{dy}{dx}$ for the following implicit function.

- $x^2 + y^2 = r^2$, where r is a constant
- $\frac{x + y}{x - y} = x$

4. Linear Approximations and Differentials: Find the Taylor polynomials of degree two approximating the given function centered at the given point.

- $f(x) = \sin(2x)$ at $a = \frac{\pi}{2}$
- $f(x) = e^x$ at $a = 1$

5. Mean Value Theorem: Determine if the Mean Value Theorem can be applied to the following function on the the given closed interval.

- $f(x) = 3 + \sqrt{x}, x \in [0, 4]$
- $f(x) = \frac{x}{1 + x}, x \in [1, 3]$

6. L'Hospital's Rule

- $\lim_{x \rightarrow 2} \frac{x^3 - 7x^2 + 10x}{x^2 + x - 6}$

- $\lim_{x \rightarrow \infty} (e^x + x)^{\frac{1}{x}}$

- $\lim_{x \rightarrow \infty} x \ln \left(1 + \frac{3}{x} \right)$

7. The Fundamental Theorem of Calculus: Find the derivative of the following

- $\int_1^x \frac{1}{t^3 + 1} dt$

- $\int_1^{\sqrt{x}} \sin t dt$

- $\int_x^{2x} t^3 dt$

8. Substitution Rule

- $\int_{\frac{1}{2}}^0 \frac{x}{\sqrt{1 - 4x^2}} dx$

- $\int_{\frac{1}{4}}^{\frac{1}{2}} \frac{\cos(\pi x)}{\sin^2(\pi x)} dx$

- $\int_0^1 x e^{4x^2+3} dx$

Homework 1

Due: Friday, Feb 4, by the end of class

1. Integration by parts (Note that the following integrals are indefinite. You need to add constants to your final answer.)

- $\int \frac{\ln x}{x^2} dx$

- $\int (\ln x)^2 dx$

- $\int \arccos x dx$

- $\int e^{\sqrt{x}} dx$

2. Trigonometric integration: Evaluate the following integral of the form $\int \sin^n x \cos^m x dx$.

- $\int \sin^2 x \cos x dx$

- $\int \sin^2 x \cos^3 x dx$

- $\int \cos^4 x dx$

3. Trigonometric substitution

- $\int \frac{x^2}{\sqrt{9-x^2}} dx$

- $\int \frac{1}{\sqrt{25+x^2}} dx$

- $\int \frac{x^3}{\sqrt{x^2-9}} dx$

- $\int \frac{1}{\sqrt{x^2+2x}} dx$

- $\int (x-2)^3 \sqrt{5+4x-x^2} dx$