

# CSCI 570 - HW 11

Due: April 20th

## Graded Problems

1. State True/False.
  - (a) Assume  $P \notin NP$ . Let  $A$  and  $B$  be decision problems. If  $A \in NPC$  and  $A \leq_p B$ , then  $B \in P$ .
  - (b) If someone proves  $P=NP$ , then it would imply that every decision problem can be solved in polynomial time.
  - (c) If  $A \leq_p B$  and  $B \in NP$ , then  $A \in NP$ .
2. Given an  $n$  bit positive integer, the problem is to decide if it is composite. Here the problem size is  $n$ . Is this decision problem in **NP**?
3. State True/False. Assume you have an algorithm that given a 3-SAT instance, decides in polynomial time if it has a satisfying assignment. Then you can build a polynomial time algorithm that finds a satisfying assignment (if it exists) to a given 3-SAT instance.
4. Show that vertex cover remains **NP**-Complete even if the instances are restricted to graphs with only even degree vertices.

## Practice Problems

5. Given an integer  $m \times n$  matrix  $A$  and an integer  $m$  - vector  $b$ , the **0-1 integer programming problem** asks whether there exists an integer  $n$  - vector  $x$  with elements in the set  $\{0; 1\}$  such that  $Ax = b$ . Prove that 0-1 integer programming is NP Complete. (*Hint*: Reduce from 3-CNF-SAT.)

6. Assume that you are given a polynomial time algorithm that decides if a directed graph contains a Hamiltonian cycle. Describe a polynomial time algorithm that given a directed graph that contains a Hamiltonian cycle, lists a sequence of vertices (in order) that forms a Hamiltonian cycle.