# **System of Equations**

A system of equations is a set of two or more equations that are solved simultaneously.

# Example 1

$$\begin{cases} x+y=3 & (1) \\ x-y=1 & (2) \end{cases}$$

The curly brace means that the equations need to be simultaneously satisfied.

$$egin{cases} x+y=3 & (1) \ x-y=1 & (2) \end{cases}$$

### Solution

To solve the system of equations, we need to find the values of x and y that satisfy both equations.

We can solve the system of equations by substitution or elimination.

### **Substitution Method**

- 1. Solve one of the equations for one of the variables.
- 2. Substitute the expression for this variable into the other equation.
- 3. Solve the resulting equation.
- 4. Substitute the value found in step 3 into one of the original equations to find the value of the other variable.

Solve one of the equations for one of the variables.

$$x + y = 3 \quad (1)$$

Solve for x:

$$x = 3 - y \quad (3)$$

Substitute the expression for this variable into the other equation.

Substitute x = 3 - y into equation (2):

$$(3-y)-y=1$$

Simplify the equation:

$$3 - 2y = 1$$

Solve the resulting equation.

$$3 - 2y = 1$$

Subtract 3 from both sides:

$$-2y = 1 - 3$$

Simplify the equation:

$$-2y = -2$$

Therefore, y = 1.

Substitute the value found in step 3 into one of the original equations to find the value of the other variable.

Substitute y = 1 into equation (1):

$$x + 1 = 3$$

Solve for *x*:

$$x = 3 - 1$$

Therefore, x = 2.

#### **Final Answer**

The solution to the system of equations is x = 2 and y = 1.

#### **Review of the Substitution Method**

- 1. Solve one of the equations for one of the variables.
- 2. Substitute the expression for this variable into the other equation.
- 3. Solve the resulting equation.
- 4. Substitute the value found in step 3 into one of the original equations to find the value of the other variable.

#### **Elimination Method**

- 1. Multiply one or both equations by a constant so that the coefficients of one of the variables are opposites.
- 2. Add the equations together to eliminate one of the variables.
- 3. Solve the resulting equation for the remaining variable.
- 4. Substitute the value found in step 3 into one of the original equations to find the value of the other variable.

# Example 2

$$\begin{cases} x + 2y = 3 & (1) \\ x - y = 1 & (2) \end{cases}$$

#### Step 1

Multiply one or both equations by a constant so that the coefficients of one of the variables are opposites.

Multiply equation (2) by 2:

$$2(x-y) = 2 \quad (3)$$

Simplify the equation:

$$2x - 2y = 2 \quad (3)$$

$$\begin{cases} x + 2y = 3 & (1) \\ 2x - 2y = 2 & (3) \end{cases}$$

Add the equations together to eliminate one of the variables.

Add equation (1) and equation (3):

$$(x+2y) + (2x-2y) = 3+2$$

Simplify the equation:

$$3x = 5$$

Solve the resulting equation for the remaining variable.

$$3x = 5$$

Therefore,  $x = \frac{5}{3}$ .

Substitute the value found in step 3 into one of the original equations to find the value of the other variable.

Substitute  $x = \frac{5}{3}$  into equation (1):

$$\frac{5}{3} + 2y = 3$$

Solve for *y*:

$$2y = 3 - \frac{5}{3}$$

Therefore,  $y = \frac{4}{3}$ .

#### **Final Answer**

The solution to the system of equations is  $x = \frac{5}{3}$  and  $y = \frac{4}{3}$ .

#### **Review of the Elimination Method**

- 1. Multiply one or both equations by a constant so that the coefficients of one of the variables are opposites.
- 2. Add the equations together to eliminate one of the variables.
- 3. Solve the resulting equation for the remaining variable.
- 4. Substitute the value found in step 3 into one of the original equations to find the value of the other variable.

# **Practice Questions**

1. Solve the following system of equations using the substitution method:

$$egin{cases} 2x+y=5 & (1) \ x-y=1 & (2) \end{cases}$$

2. Solve the following system of equations using the elimination method:

$$\begin{cases} 5x + 2y = 10 & (1) \\ 3x - 4y = 2 & (2) \end{cases}$$

# **Practice Questions**

3. Solve the following system of equations using both the substitution and elimination methods. Which method is easier?

$$\begin{cases} 2.5x + 3y = 10 & (1) \ 1.5x - 2y = 5 & (2) \end{cases}$$

4. Solve the following system of equations using both the substitution and elimination methods. Which method is easier?

$$\begin{cases} 6x + 2y = 10 & (1) \\ 3x - 4y = 2 & (2) \end{cases}$$