

Q1:

(1)

```
import numpy as np
import scipy.special as sp
import matplotlib.pyplot as pl
```

```
comb= sp.comb
```

```
n=10
```

```
x= np.arange(0,n+1)
```

```
c= comb(n,x)
```

```
def binom(x,n,p):
```

```
    prob= comb(n,x) * p**x * (1-p)**(n-x)
```

```
    return prob
```

```
b= binom(x, n=10, p=1/10)
```

```
x, b
```

```
(array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10]),
 array([0.34867844, 0.38742049, 0.19371024, 0.05739563, 0.0111602
6,
        0.00148803, 0.00013778, 0.00000875, 0.00000036, 0.00000001,
        0.          ]))
```

(2)

```
n=10
```

```
p=1/10
```

```
E[X]=n*p
```

```
E[X]=0.1
```

(3)

$$Std[x] = \sqrt{n * p * (1 - p)} = \sqrt{10 * 0.1 * 0.9} = 0.9487$$

(4)

$$\sum_{x=10}^{10} (x; 10 * \frac{100-x}{100})$$

Q3:

(1)

$$P(X \geq 10) = 1 - (P(0) + P(1) + \dots + P(9)) = 1 - b(0; 100, 0.05) - b(1; 100, 0.05) - \dots - b(9; 100, 0.05)$$

(2)

$$P(x \geq 10 | p = 5\%) = P(x \geq 10)$$

"p=5%" → "x ≥ 10" 機率很小，但 x ≥ 10 確實發生

$$p \rightarrow q \quad \sim q \rightarrow \sim p \quad p \rightarrow \sim q \quad q \rightarrow \sim p$$

Q4:

$$b(x; n, p) \rightarrow (C_x^n) * p^x * q^{n-x}$$

$$p(x; \mu) \rightarrow \frac{\mu^x}{x!} * e^{-\mu}$$

$$n \rightarrow \infty$$

$$p \rightarrow 0$$

$$np = \mu$$