# NC STATE UNIVERSITY

# ST841 STATISTICAL PRACTICE I

# Consulting TAA

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#### 1 Introduction

### 1.1 Background

For this project, we cooperate with Dr. Al Chen in the Department of Accounting to conduct research related to Tax Analytics and Automation Diffusion in Large Companies. In order to stay relevant and competitive, businesses must take advantage of the latest technologies. Many new technologies and tools can automate mundane business administration tasks. Automating administrative tasks leads to greater efficiency and fewer errors and it frees up employees to focus on tasks that add more value to the company. All of these principles hold true for a company's tax and accounting department as well.

The advent of robotic process automation (RPA), the automation of business processes using artificial intelligence and software, has had a particularly significant impact on the accounting profession. [8] The extent to which companies and accounting departments have adopted and integrated automated tax tools into their workplace varies. The aim of our client's study is to determine what factors seem to have the most significant impact on the initiation, adoption, and routinization of tax analytics and automation (TAA) tools in larger companies.

Initiation, adoption, and routinization are explained in [2]. Initiation refers to an initial evaluation of the suitability of a technology by the company, adoption refers to the the point at which a company recognizes a technology as valuable for its interests and begins to integrate that technology into its business practices, and routinization refers to the full-scale deployment of that technology.

#### 1.2 Introduction

In determining what factors most impact the initiation, adoption, and routinization of a technology by a company, our client employed the technology-organization-environment (TOE) framework that was first proposed in [12] and later used by Zhu, et al. [14] to study the diffusion of e-business technology in companies.

The TOE framework indicates that technology diffusion is impacted by the technological sophistication and preparedness of a company, the organizational and managerial attributes of a company, and the regulatory and competitive context or environment of a company.

Our client is interested in testing five hypotheses regarding TAA tools using the TOE framework:

- 1. Technology readiness is positively related to TAA initiation/adoption/routinization.
- 2. Technology integration is positively related to TAA initiation/adoption/routinization.
- 3. Managerial obstacles are negatively related to TAA initiation/adoption/routinization.
- 4. Competition intensity is positively related to TAA initiation/adoption/routinization.
- 5. A supportive regulatory environment is positively related to TAA initiation/adoption/routinization.

#### 1.3 Data

To answer these questions, our client sent surveys to a chief tax officer at each of the Fortune 1000 companies asking about the intiation, adoption and routinization of TAA within that company's tax department and the level of technological readiness, technological integration, managerial obstacles, competition intensity, and regulatory support for TAA for the company.

Several of the variables like initiation, routinization, managerial obstacles, technology integration, competition intensity, and regulatory environment were measured using a number of 5-point Likert scale survey items. For instance to measure initiation, respondents were asked to use a Likert scale on 7 survey items to rate the significance that each of 7 potential TAA benefits had in their initial decision to pursue TAA tools.

Other variables like technological readiness where measured by asking a series of questions relating to the kinds of technology used at the company and the number of tax employees at the company who specialize in the use of TAA tools.

Of the 1000 companies that received surveys, 70 responded. The client has already performed an analysis answering the hypotheses for the routinization phase of the

technology diffusion process. He wants us to perform analysis that explores the intitation, adoption, and routinization phases simultaneously.

#### 1.4 Survey Details and Preliminary Data Transformation

The data were collected using a survey with 28 questions. The first question which measures the initiation phase, asks what factors managers considered when conducting an initial evaluation of TAA tools. The question consists of 7 Likert scale items. These 7 Likert items are transformed into a composite score using the methodology in 2.2. The second question asks the respondent to select which of four applications of TAA tools their company has adopted. This question is meant to measure the level of TAA adoption in the company. The responses will be combined into a single composite score using a weighting scheme for the different items based on discussions with the client. The third question is a 4-item Likert question meant to measure the degree to which companies have routinized TAA tools. It is transformed in a similar way to the data from question 1.

The next 7 questions are used to measure the technology readiness of the company. There is a question asking about the database technologies used by the company, the responses from this question are transformed into a binary variable which is 1 if the company is using an advanced database technology and a 0 if they are using no databases or simple database technology like Excel or Access. The next question asks if the company has a manager for TAA tools. This is coded as a binary variable that is 1 if the company does have such a manager and 0 otherwise. The next question asks about the total number of IT individuals in the company. It is coded as a categorical variable taking on 0 for none, 1 for less than 20, and 2 for between 20 and 200, and 3 for more than 200. There is also a question asking how many IT professionals are dedicated to the tax department and the use of TAA tools. This question is coded as 0 for none, 1 for between 1 and 10, 2 for between 10 and 20, and 3 for more than 20. The next question asks for the total number of tax professionals in the company; this raw count is included as a variable in the dataset. Following this, there is a question about how many tax professionals specialize in TAA tools. This response is also included in the dataset as a raw count. The final technology readiness question asks the respondent to select from a list of 9 TAA tools which ones are employed by their company. This data will be condensed into a single score by consulting with the client to establish weights for the different technologies. The composite score will be a sum of the weights associated with the technologies claimed by each company.

The next question measures technology readiness using a two item Likert scale question. The data from this question is transformed into a composite score using the methodology described 2.2.

The next set of questions seeks to measure the overall size of the company. The first question asks for the total number of company employees. This data is incorporated as a categorical variable with 1 for less than 100, 2 for 100-300, 3 for 300-500, 4 for 500-1500, 5 for 1500-5000, and 6 for more than 5000. The next question asks about the geographic extent of the company. It is incorporated as a binary variable which is 0 if the company has only sites in its home country and 1 if the company has sites in multiple countries. The next question asks about the number of foreign subsidiaries of the company and is incorporated into the data as a categorical variable with one level corresponding to 0 subsidiaries, one level to 1-20 subsidiaries, and one level to more than 20 subsidiaries. The last two questions ask for the percentage of foreign sales and the percentage of foreign purchases. Both variables are incorporated as categorical variables with levels corresponding to 0 - 5%, 5.1 - 15%, 15.1 - 25%, 25.1 - 35%, 35.1 - 45%, and more than 45%.

The next three questions seek to measure the managerial obstacles to TAA, the level of competition faced by the company, and the regulatory/governmental attitude to TAA use in the company's home country. All three of these questions are multi-item Likert scale questions and are transformed and represented using the composite score method detailed in 2.2.

The last few questions are general demographic questions about the respondent and are not expected to be of interest for the data analysis.

# 2 Methodology

# 2.1 Creating Composite Scores from Multiple Likert Items

One challenge presented by the TAA dataset is the fact that several response variables of interest like TAA evaluation and routinization and several explanatory variables of interest like technology integration and managerial obstacles are measured using multiple Likert scale items.

When several survey items are used to measure a single underlying variable, it is of-

ten desirable to have some way of combining the information from the several survey items into a single composite score representing the variable of interest. A common approach for deriving such composite scores is to obtain the principal components of the several survey items and use these principal components, especially the first principal component as the composite score [5][9].

Our difficulty is that we are dealing with Likert items for which principal components analysis is not really well-defined. One solution to this problem that we employed for this data analysis is nonlinear principal components analysis with optimal scaling as described in [7] and [3]. This approach proceeds by finding an optimal transformation of the Likert data into a continuous representation and then performing standard PCA on this transformed representation.

Similar to standard principal components analysis, the nonlinear principal components analysis problem can be represented as a loss minimization problem. We minimize the loss function using a technique called alternating least squares.

Let  $\mathbf{X}_{n\times p}$  be a matrix of n observations of p Likert scale items. We assume that  $x_{ij}$ , the i-th observation of the j-th item is 1 for the lowest rank item on the Likert scale, 2 if it is the second lowest rank item on the Likert scale, and so on. This represents the raw Likert scale data we would like to condense into a composite score. Let  $\mathbf{Q}_{n\times p}$  represent the transformed version of  $\mathbf{X}$  under optimal scaling. Let  $\mathbf{H}_{n\times q}$  be the matrix of component scores where  $q \leq p$ . In our application, since we want a single composite score, we have q = 1. Finally, let  $\mathbf{A}_{q\times p}$  be the matrix of component loadings.  $\mathbf{H}\mathbf{A}$  can be interpreted as a rank q approximation to  $\mathbf{X}$ . We wish to find the optimal approximation, so we minimize the loss function:

$$L(\mathbf{Q}, \mathbf{H}, \mathbf{A}) = n^{-1} \sum_{j=1}^{p} (\mathbf{q}_j - \mathbf{H} \mathbf{a}_j)^T (\mathbf{q}_j - \mathbf{H} \mathbf{a}_j)$$
(1)

where  $\mathbf{q}_j$  and  $\mathbf{a}_j$  are the *j*-th columns of  $\mathbf{Q}$  and  $\mathbf{A}$  respectively. Alternating least squares works by iteratively minimizing the loss function with respect to one of  $\mathbf{Q}$ ,  $\mathbf{H}$ , or  $\mathbf{A}$  while holding the others constant until some convergence criterion is met. Thus, the optimal scaling problem (finding  $\mathbf{Q}$ ) is solved simultaneously with the principal components problem.

All that remains is to speak briefly about the form of **Q**. In general for each of j=1,...,p, we have

$$q_{ij} = \sum_{k=1}^{b} \alpha_k \phi_k(x_{ij}) \tag{2}$$

where  $q_{ij}$  is the *i*-th entry of  $\mathbf{q}_j$  and  $\phi_k(\cdot)$  is a basis function representation of  $x_{ij}$ . After some preliminary experimentation, a second degree B-spline was determined to do the best job of capturing the structure in the Likert items. If  $x_{ij}$  is a missing value,  $\phi_k(\cdot)$  is set to 1/b. This is one of three methods for handling missing values suggested in [3]. It is called the averaging method. After experimentation, it was found that the other two methods produced imputations for the missing values that were too extreme relative to the non-missing values. The optimization of the loss function with respect to  $\mathbf{Q}$  involves finding for each j=1,...p, the set of  $\alpha_1,...,\alpha_k$  that minimizes the loss function.

#### 2.2 Missing Value Imputation

As introduced before, there are 28 survey questions in total. However, based on subject knowledge of the client and other related reference, only 23 questions by now have enough evidence or interpretability to be extracted into the cleaned dataset for further analysis. As the following figure 1 shows, the 23 questions that involves 56 variables should map into three response variables and eleven predictor variables.

Thus, we conduct an exploratory data analysis on this cleaned datset with 68 observations and 56 original variables in total. To have some brief overview, we check the proportion of missing values that all the variables have in advance, and have observed that there are fifteen variables that have a proportion of missing values larger than fifty percent; ten variables have the 10% - 50% proportion of missing values; and only the five categorical variables corresponding to Q5 have no missing value. Since the sample size is only 68, which is too small to throw any records with missing values, and the proportion of missing values in the datasets is large in a number of variables as figure 2 show, we need find some better way to make full use of the data and conduct appropriate missing value imputation for those variables.

As for the missing value imputation, we adopt the method named AMELIA. [6] Here the method assumes the first assumption that the complete data  $\mathcal{D}_{n\times k} = (\mathcal{D}^{obs}, \mathcal{D}^{mis})$  follows the multivariate normal distribution, which is

$$\mathcal{D} \sim N_k(\mu, \Sigma) \tag{3}$$

and a second assumption that missing data are missing at random (MAR), which means the probability of missingness could be fully explained by observed data,

|              |                                      | I .   |   |  |  |
|--------------|--------------------------------------|-------|---|--|--|
|              | TAA Model Variables                  | Q#    | Interpretation  |  |  |
| Respo        | Initiation                           | Q5    | Likert scale 1-6  |  |  |
| nse          | Adoption                             | Q6    | Categorical 1=emerging, 2=intermediate, 3= advance  |  |  |
| Var.         | Routinization                        | Q10   | Likert scale 1-6  |  |  |
|              | Technology Readiness                 | Q35   | Char. Open-ended responses, ERP brands.   |  |  |
|              |                                      | Q40.2 | Char. Open-ended responses, titles  |  |  |
|              |                                      | Q36.3 | Numerical data, continuous, low numbrers  |  |  |
|              |                                      | Q37.4 | Numerical data, continuous, low numbrers  |  |  |
|              |                                      | Q38.5 | Numerical data, continuous, low numbrers  |  |  |
|              |                                      | Q39.6 | Numerical data, continuous, low numbrers  |  |  |
|              |                                      | Q22   | 10 types of technologies + other (open-ended response)  |  |  |
|              | Technology Integration               | Q23   | Likert scale 1-6  |  |  |
|              | Firm size                            | Q26   | Numerical data, continuous  |  |  |
|              | Oldslaves                            | Q24   | Ordinal variable: Global scope, Likert scale 1-4<br>Binary variable: 1-3=Domestic vs. 4=International |  |  |
| Depen        |                                      | Q27   | # of foreign subsidiaries<br>Categorical 1=0, 2=1-20, 3=over 20                                       |  |  |
| dent<br>Var. | Global scope                         | Q29   | Tradiing globalization % total sales from overseas % numerical data, continuous                       |  |  |
|              |                                      | Q29   | Tradiing globalization % total procurement spending from overseas % numerical data, continuous        |  |  |
|              | Managerial obstacles                 | Q30   | Likert scale 1-6  |  |  |
|              | Competition intensity                | Q31   | Likert scale 1-6  |  |  |
|              | Regulatory environment               | Q32   | Likert scale 1-6  |  |  |
|              | Survey respondent's job title        | Q42   | Open-ended response   |  |  |
|              | Years in the current position        | Q45.2 | Numerical data, continuous  |  |  |
|              | Head of the tax department report to | Q43.3 | Open-ended response   |  |  |
|              | Title of the head of the tax dept    | Q44.4 | Open-ended response   |  |  |

Figure 1: The mapping of useful survey questions to the variables for analysis

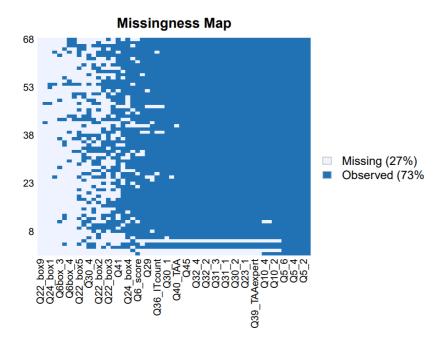


Figure 2: The visualization of missingness in the data. The y-axis is the id of the observation, and the x-axis is the variables with decreasing proportion of missing values from the left to the right

defined as

$$p(M \mid \mathcal{D}) = p(M \mid \mathcal{D}^{obs}) \tag{4}$$

where M is the missing matrix with  $M_{ij} = I(\mathcal{D}_{ij} \in \mathcal{D}^{mis})$ .

Hence, the normal assumption as well as the MAR assumption should be checked after the data are fully prepared and before the conduction of imputation.

Remembering the normality assumption Eq. 3 and the missing at random assumption Eq. 4, we can obain the following likelihood for the observed data  $\mathcal{D}^{\text{obs}}$ :

$$p\left(\mathcal{D}^{\text{obs}}, M \mid \theta\right) = p\left(M \mid \mathcal{D}^{\text{obs}}\right) p\left(\mathcal{D}^{\text{obs}} \mid \theta\right)$$
 (5)

where  $\theta = (\mu, \Sigma)$  is the parameter of interest. Thus the likelihood of  $\theta$  based on observed data can be expressed as:

$$L(\theta \mid \mathcal{D}^{\text{obs}}) \propto p(\mathcal{D}^{\text{obs}} \mid \theta) = \int p(\mathcal{D} \mid \theta) d\mathcal{D}^{\text{mis}}$$
(6)

and with a uniform prior of  $\theta$ , the posterior could be

$$p\left(\theta \mid \mathcal{D}^{\text{obs}}\right) \propto \int p(\mathcal{D} \mid \theta) d\mathcal{D}^{\text{mis}}$$
 (7)

Since the  $\mathcal{D}^{\text{mis}}$  is missing, Expectation-Maximization (EM) algorithm combined with a bootstrap approach is applied here to obtain the estimated modes of the posterior with its variance estimation. By assuming a start point of  $\theta_0$ , we define the Q function as

$$Q(\theta \mid \theta^{v}) = E_{\theta^{v}}(ln(p(\mathcal{D} \mid \theta)) \mid \mathcal{D}^{\text{obs}})$$
(8)

where  $p(\mathcal{D} \mid \theta)$  is the complete data likelihood. The updates of  $\theta^{v+1}$  given  $\theta^v$  as

$$\theta^{v+1} = \arg\max_{\theta} Q(\theta \mid \theta^v) \tag{9}$$

Thus, we have the estimations of  $\theta$ , and can make imputation of the missing data based on the observed data as well as the estimated parameters for the complete data likelihood.

Besides, m simultaneous imputations can be combined together to produce a more stable average imputation:

$$\bar{T} = \frac{1}{m} \sum_{j=1}^{m} T_j \tag{10}$$

where j represents the  $j^{th}$  datasets, and the  $\bar{T}$  has the following standard error:

$$SE(T) = \sqrt{\frac{1}{m} \sum_{j=1}^{m} SE(T_j)^2 + S_T^2 (1 + 1/m)}$$
 (11)

where,  $S_T^2 = \sum_{j=1}^m \left(T_j - \bar{T}\right)^2 / (m-1)$  is the sample variance across the m estimations, and  $SE\left(T_j\right)^2$  is the estimated variance of  $T_j$  based on the  $j^{th}$  dataset.

Besides, it's also common that to treat the missing value of a categorical variable as a new variable; for the questions related to Likert scales where there's always a level that indicating the customer don't know the answer, we can directly change the missing value into that case; some times a mean imputation would also be

appropriate if sufficient subject knowledge are grounded. Thus, the missing value imputation of this project can be quite customized to the specific variable with more subject knowledge. However, the cleaner data should be get in the first step.

#### 2.3 Structural Equation Modelling

Traditional multivariate regression is appropriate when we only have one dependent variable, but it can't handle the case where we have multiple dependent variables. Structural equation modeling (SEM) is a popular methodology in social sciences for representing, estimating, and testing a network of relationships between variables (measured variables and latent constructs) [10]. However, covariance-based methods like SEM requires a large sample size. Given that we have a small data set, it is best that we adopt a less data-intensive method to do the regression analysis.

### 2.4 Multi-response (Multivariate) Linear Regression

Another common technique for handling multiple responses is multi-response (multivariate) linear regression. Suppose we have m responses with p features and n observations, multi-response linear regression can be written in matrix form

$$Y = XB + E \tag{12}$$

where  $Y \in \mathbb{R}^{n \times m}$  are the dependent variables,  $X \in \mathbb{R}^{n \times p}$  are the independent variables,  $B \in \mathbb{R}^{p \times m}$  are the coefficients and  $E \in \mathbb{R}^{n \times m}$  are the errors. To account for the possible correlation of different columns of Y, we assume that each row  $E_i$  of E has a covariance matrix  $\Sigma \in \mathbb{R}^{m \times m}$ . If put in vectorized form,

$$\operatorname{vec}(Y)|X \sim \mathcal{N}([B' \otimes I_n] \operatorname{vec}(X), \Sigma \otimes I_n)$$
 (13)

It can be shown that the maximum likelihood estimate of B is invariant to  $\Sigma$ , which can be computed using ordinary least square

$$\hat{B} = (X'X)^{-1}X'Y \tag{14}$$

Then an unbiased estimate of error covariance matrix  $\Sigma$  is given by

$$\hat{\Sigma} = \frac{Y'(I_n - X(X'X)^{-1}X')Y}{n - p}$$
 (15)

while the MLE for  $\Sigma$  is given by

$$\tilde{\Sigma} = \frac{Y'(I_n - X(X'X)^{-1}X')Y}{n} \tag{16}$$

The least square estimate  $\hat{B}$  has the following distribution

$$\operatorname{vec}(\hat{B}) \sim \mathcal{N}(\operatorname{vec}(B), \Sigma \otimes (X'X)^{-1})$$
 (17)

Thus if we want to test  $B_{jk} = 0$  against  $B_{jk} \neq 0$ , it can be seen that

$$\frac{\hat{B}_{jk}}{\hat{\Sigma}_{kk}(X'X)_{jj}^{-1}} \sim t_{n-p} \tag{18}$$

which will provide a p value for each regression coefficient  $B_{jk}$ . It is worth pointing out that mathematically, statistical inference for a single entry  $B_{jk}$  in the coefficient matrix B is the same for single-response linear regression and multi-response linear regression. However, compared with separate single-response linear regression models, multi-response linear regression takes possible correlation of response columns into consideration, which will enable inference for blocks of B. For example, we might be interested in testing whether several independent variables have a joint significant impact on all the response variables, i.e. we want to test whether a reduced model with q < p covariates is sufficient. The hypotheses can be formulated as

$$H_0: B_2 = 0 \text{ versus } H_1: B_2 \neq 0$$
 (19)

where  $B_2 \in \mathbb{R}^{(p-q)\times m}$  is a part of the partitioned  $B = \begin{pmatrix} B_1 \\ B_2 \end{pmatrix}$ . Then the likelihood ratio statistic becomes

$$\Lambda = \frac{\sup_{B_1, \Sigma} L(B_1, \Sigma)}{\sup_{B, \Sigma} L(B, \Sigma)} = \left(\frac{|\tilde{\Sigma}|}{|\tilde{\Sigma}_1|}\right)^{n/2}$$
(20)

where  $\tilde{\Sigma}_1$  and  $\tilde{\Sigma}$  are respectively constrained and unconstrained MLEs for  $\Sigma$ . For large enough n, the modified likelihood ratio test statistic has an approximate chisquare distribution

$$-\nu\log(\Lambda) \sim \chi_{m(p-q)}^2 \tag{21}$$

where  $\nu = n - p - \frac{1}{2}(m - p + q + 2)$ . If we use E to denote  $n\tilde{\Sigma}$  and H to denote  $n(\tilde{\Sigma}_1 - \tilde{\Sigma})$ , statistics from the Multivariate Analysis of Variance (MANOVA) literature [13] which rely on F-distribution approximations can be adopted for testing (19). Let  $\lambda_1 \geq \lambda_2 \geq \cdots \geq \lambda_p$  denote the eigenvalues of matrix  $HE^{-1}$ ,

- Wilk's lambda =  $\sum_{i=1}^{p} \frac{1}{1+\lambda_i} = \frac{|E|}{|E+H|}$
- Pillai's trace =  $\sum_{i=1}^{p} \frac{\lambda_i}{1+\lambda_i} = \operatorname{tr}(H(H+E)^{-1})$
- Hotelling-Lawley's trace =  $\sum_{i=1}^{p} \lambda_i = \operatorname{tr}(HE^{-1})$

#### • Roy's largest root = $\max(\lambda_i)$

After the above test statistics are calculated, they are transformed into an F-statistic which will have an approximate or exact F-distribution under the null hypothesis. In some cases, the four tests are identical, which means they will lead to the same F-statistics and probabilities. When they do differ, Pillai's trace is often used because of its power and robustness [1]. We will take advantage of implementations of these tests in anova function of stats package in R [11] for our statistical computation.

#### 2.5 Regression Trees

Due to the outliers, missing values, and lack of normality in the data, we believed it was worthwhile to also employ regression methodology that was robust to these problems.

Regression trees [4] are a modelling framework that make fewer assumptions than linear regression models, automatically handle missing values without using imputation or ignoring data, are robust to outliers, and do not require the data to be normally distributed.

A regression tree is constructed by assigning each observation to a bin based on the values of the independent variables associated with that observation. The tree model predicts the response of a particular observation to be the mean of the responses in that observations bin.

The bins, or leaf nodes, are found by recursively splitting the set of observations on values of the independent variables so that at each split the prediction error in the resulting bins is minimized.

We illustrate a regression tree in figure 3. The tree begins by splitting on the independent variable A. Observations with A > 2 go to the left, observations with  $A \le 2$  go to the right. On the left the next optimal split is performed on variable B. The boxes at the bottom of the tree represent the leaf nodes. P is the number of observations in that box and mean is the mean of the responses for those observations which is used as the prediction value.

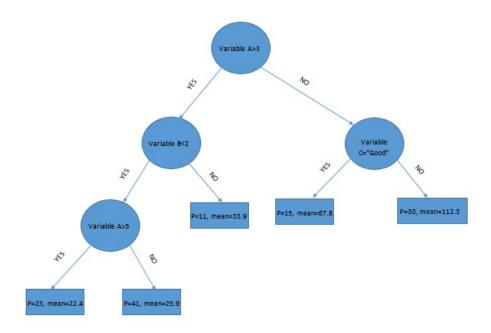


Figure 3: Regression Tree Illustrated

The splitting variables and the values for those variables that are used to define the split are chosen to optimize

$$\sum_{i \in B} \sum_{j=1}^{p_i} (y_{ij} - \bar{y}_i)^2$$

where B is the set of boxes,  $p_i$  is the number of observations in box i and  $\bar{y}_i$  is the mean of the responses for the observations in box i.

### 3 Results

#### 3.1 Transformation of Likert Scale Data

After using non-linear PCA to construct scores for the Likert data, it is useful to look at the loadings for each of the first principal component scores being used as a one-dimensional approximation. The loadings quantify the strength and direction of the relationship between each of the original Likert scale items and the first principal component. These loadings are depicted for each of the 6 Likert scale sets in Figure 4.

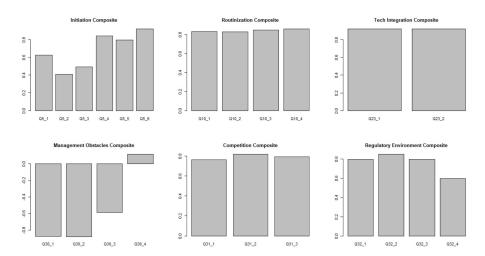


Figure 4: First Principal Component Loadings

We can use the loadings plot in Figure 4 to help us interpret the meaning of the scores that we use to represent each of the 6 variables underlying the Likert scale items. For instance, from the first plot, we can see that the score representing the consideration a firm initially gives to considering different TAA technologies is most influenced by a company's responses to the fourth, fifth, and sixth Likert items. The first, second, and third questions relate to using TAA to reduce costs, expand inhouse tax services, and improve the coordination of the tax department with other departments. The last three items relate to improving the reporting, analysis, and productivity of the tax department. We can see that the last three items relate more to the primary output of the tax department and the first three relate to how the operations of the tax department within the company. This provides insight into what the unified score is really measuring. It may be a measure of the role accounting department output played in a company's initial considerations for adopting TAA.

Another interesting variable is the management obstacles variable. For this variable, the firms rarely answered the fourth Likert question. Thus, this question was mostly missing values. This explains its almost negligible impact on the first principal component score. It is also interesting to note that the other questions have a negative relationship with the first principal component. Thus, for the managerial obstacles variable, we would interpret a lower score as indicating more significant managerial obstacles.

### 3.2 Multi-response (Multivariate) Linear Regression Results

Recall that out response variables are TAA technology initiation, adoption and routinization, our independent variables are technology readiness, technology integration, firm size, global scope, management obstacles, competition intensity and regulatory environment. The explanatory variables are standardized to make the coefficients comparable and exclude intercepts from our model. The following table summarizes the coefficient estimates and their corresponding significance level.

|                        | Initiation | Adoption | Routinization |
|------------------------|------------|----------|---------------|
| Technology Readiness   | -0.11      | 0.50***  | 0.12          |
| Technology Integration | -0.06      | -0.05    | 0.33**        |
| Firm Size              | 0.06       | 0.26*    | -0.03         |
| Global Scope           | 0.37**     | -0.18    | 0.07          |
| Management obstacles   | -0.11      | 0.19     | 0.15          |
| Competition Intensity  | 0.07       | -0.01    | 0.14          |
| Regulatory Environment | 0.06       | 0.05     | 0.15          |

Table 1: Coefficients and their significe levels. \*\*\* means p < 0.001, \*\* means p < 0.01 and \* means p < 0.05.

Notice that significant coefficients are rare. Now, let's utilize previously mentioned F-tests from MANOVA theory to decide whether a specific explanatory variable has a significant impact on all of the response variables. In other words, we can provide a single p value for each independent variable. The following table summarizes test statistics, the transformed F-statistics and their corresponding p values. Notice that in our case, the four tests, namely Wilk's lambda, Pillai's trace, Hotelling-Lawley's trace and Roy's largest root are equivalent and they produce the same F-statistics and p values, so we only report one F-statistic and p value for each independent variable. Also, Hotelling-Lawley's trace and Roy's largest root turn out to have identical test statistics, so we report them in one column.

|                        | Wilk | Pillai | Hotelling/Roy | F-statistic | p-value   |
|------------------------|------|--------|---------------|-------------|-----------|
| Technology Readiness   | 0.73 | 0.28   | 0.38          | 7.47        | 0.0003*** |
| Technology Integration | 0.86 | 0.14   | 0.16          | 3.10        | 0.03*     |
| Firm Size              | 0.90 | 0.10   | 0.11          | 2.07        | 0.11      |
| Global Scope           | 0.86 | 0.14   | 0.17          | 3.29        | 0.03*     |
| Management Obstacles   | 0.91 | 0.09   | 0.10          | 1.96        | 0.13      |
| Competition Intensity  | 0.98 | 0.02   | 0.03          | 0.50        | 0.68      |
| Regulatory Environment | 0.97 | 0.03   | 0.03          | 0.54        | 0.65      |

Table 2: MAONVA test statistics and their p values. \*\*\* means p < 0.001, \*\* means p < 0.01 and \* means p < 0.05.

From the table we can see that technology readiness, integration and global scope are statistically significant. Firm size is significant for adoption but not significant overall. We can also see that management obstacles, competition intensity and regulatory environment don't seem to have significant impact on the response variables.

### 3.3 Regression Trees

We fit a separate regression tree for each of the three response variables. The resulting trees are plotted in the below figures.

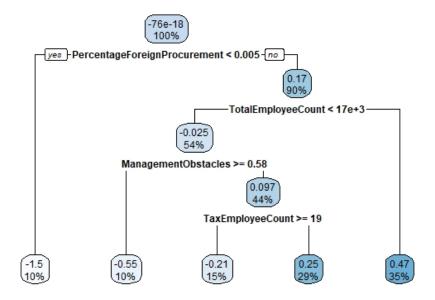


Figure 5: Initiation Tree

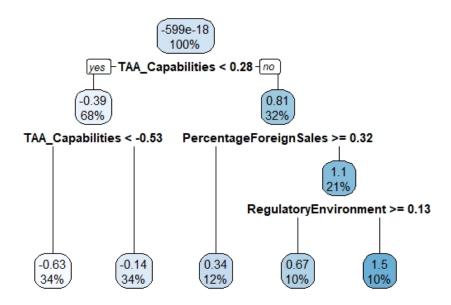


Figure 6: Adoption Tree

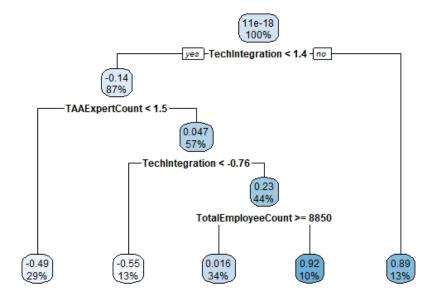


Figure 7: Routinization Tree

The first splitting variable is often interpreted as the most important or influential

variable in the model. The results agree with the linear regression results in that for initiation the global extent of the firm as measured in global scope or foreign procurements seems to be most associated with higher initial consideration of TAA, for adoption, technological readiness or capability seems to be most closely associated with adopting more advanced TAA tools, and for routinization, technological integration seems to be most closely associated with better TAA routinization.

#### 4 Discussion

In this project, we provide multi-aspect statistical supports to help the client gain better understanding of the survey data related to the diffusion of tax automation techniques. We handle the tranfermation of the Likrt scale using non-linear PCA, impute the missing values through AMELIA using em algorithm, and provide final result analysis using both multivariate linear regression and decision tree;s analysis to provide better understand and good interpretation. However, another potential question or work to be done is how to transform the R script to more replicable and tools to the client that would facilate the future. We will wrap up the materials into a better format for the client.

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