

$$I_C(t) + I_J(t) = I(z = 0, t) \quad (1)$$

$$I_C = \frac{d(CV)}{dt} = C \frac{d^2\Phi}{dt^2} = C\varphi_0 \frac{d^2\delta(t)}{dt^2} \quad (2)$$

$$\delta = \Phi/\varphi_0 \quad (3)$$

$$\varphi_0 = \hbar/2e \quad (4)$$

$$I_J = I_0 \sin(\delta(t)) \quad (5)$$

$$I(z = 0, t) = I_{in}(t) - I_{out}(t) \quad (6)$$

$$V(z = 0, t) = V_{out}(t) + V_{in}(t) = (I_{in}(t) + I_{out}(t))Z_c \quad (7)$$

$$I(z = 0, t) = 2I_{in}(t) - V(z = 0, t)/Z_c \quad (8)$$

$$C\varphi_0 \frac{d^2\delta(t)}{dt^2} + \frac{\varphi_0}{Z_c} \frac{d\delta(t)}{dt} + I_0 \sin(\delta(t)) = 2I_{in}(t) \quad (9)$$

$$\frac{d^2\delta(t)}{dt^2} + 2\gamma \frac{d\delta(t)}{dt} + \omega_0^2(\delta(t) - \frac{\delta^3(t)}{6}) = \frac{2I_p}{C\varphi_0} \cos(\omega_p t) \quad (10)$$