

#### 软件理论基础与实践

#### TYPECHECKING: A Typechecker for STLC

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### 类型检查



- 之前只定义了归纳定义的has\_type关系
- 能否定义为函数自动检查类型正确性?

## 辅助函数: 判断类型等价



```
Fixpoint eqb_ty (T1 T2:ty) : bool :=
   match T1,T2 with
   | <{ Bool }> , <{ Bool }> =>
        true
   | <{ T11->T12 }>, <{ T21->T22 }> =>
        andb (eqb_ty T11 T21) (eqb_ty T12 T22)
   | _,_ =>
        false
end.
```

#### 类型检查函数



```
Fixpoint type check (Gamma : context) (t : tm) : option ty :=
  match t with
  | tm var x =>
      Gamma x
  | <{\{ x:T2, t1 \}} > = >
      match type_check (x |-> T2; Gamma) t1 with
       Some T1 \Rightarrow Some < \{T2->T1\}>
        => None
      end
  | <{t1 t2}> =>
      match type check Gamma t1, type check Gamma t2 with
      | Some <{T11->T12}>, Some T2 =>
          if eqb ty T11 T2 then Some T12 else None
      | __,_ => None
      end
```

#### 类型检查函数



```
| <{true}> =>
   Some <{Bool}>
| <{false}> =>
    Some <{Bool}>
<{if guard then t else f}> =>
    match type_check Gamma guard with
    | Some <{Bool}> =>
        match type_check Gamma t, type_check Gamma f with
        | Some T1, Some T2 =>
            if eqb_ty T1 T2 then Some T1 else None
        _,_ => None
        end
        => None
    end
end.
```

#### 类型检查函数的性质



```
Theorem type_checking_sound : forall Gamma t T,
  type_check Gamma t = Some T -> has_type Gamma t T.
```

```
Theorem type_checking_complete : forall Gamma t T,
  has_type Gamma t T -> type_check Gamma t = Some T.
```

证明思路:在t或者has\_type上做归纳,对应调用 另外一边函数或者constructor即可

# 作业



• 无