

2 3 5 7 11 13 17 19 23 29 31 37

---

1 ~ n

0(n)

<del>2</del>	3	<del>4</del>	5	<del>6</del>	7	<del>8</del>	<del>9</del>	<del>10</del>
11	<del>12</del>	13	<del>14</del>	<del>15</del>	<del>16</del>	17	<del>18</del>	19
<del>21</del>	<del>22</del>	23	<del>24</del>	<del>25</del>	<del>26</del>	<del>27</del>	<del>28</del>	29
31	<del>32</del>	<del>33</del>	<del>34</del>	<del>35</del>	<del>36</del>	37	<del>38</del>	<del>39</del>

bool deleted [ ];

$j \leq \frac{n}{i}$

```

for (int i=2; i<=n; i++)
    if (deleted[i] != true)
        for (int j=2; j<=n/i; j++)
            deleted[i*j] = true;

```

$i \times j \leq n$

deleted[i] == 0

```

prime[]
for (int i=2; i<=n; i++)
    if (deleted[i] == 0)
        prime[cnt++] = i;

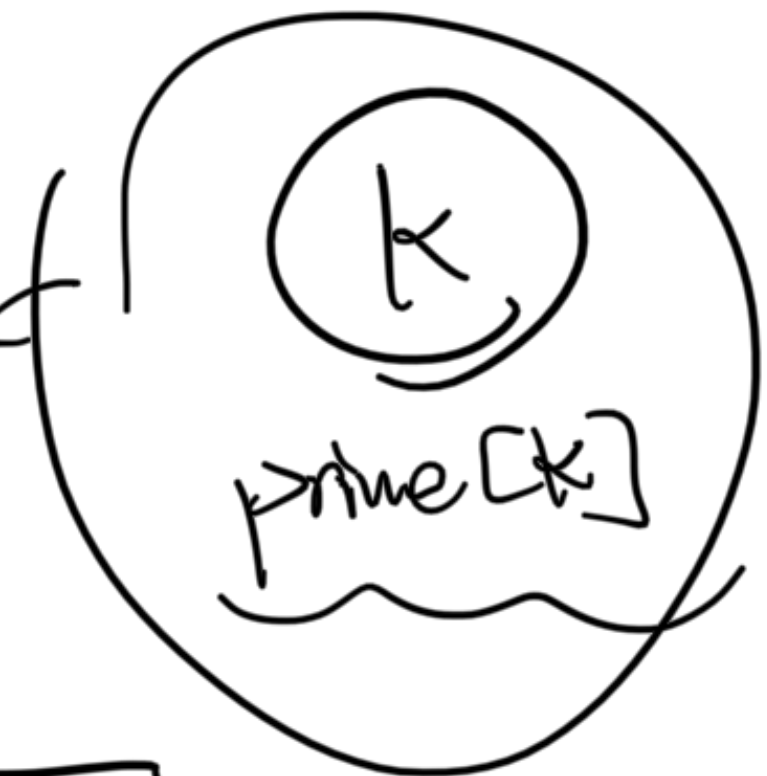
```

→ cnt++  
→ prime[cnt] = i

	↓	↓				
	0	1	2	3	4	5
prime	2	3	5	7	11	13
	→ 2	3	5	7		
	cnt					

cnt

prime[cnt] = 11



prime [cnt] = 3  $\searrow$  cnt++

2 3 5 7 11 13 17 19 23 29 31 37

6

	$2 \times 2$	$3 \times 2$	$5 \times 2$	$7 \times 2$	$11 \times 2$	$13 \times 2$	$17 \times 2$	$19 \times 2$
	$2 \times 3$	$3 \times 3$	$5 \times 3$	$7 \times 3$	$11 \times 3$	$13 \times 3$		
	$2 \times 4$	$3 \times 4$		$7 \times 4$				
	$2 \times 5$			$7 \times 5$				
	.	.	.					
	.	.	.					
	.	.	.					
	.	.	.					
	.	.	.					
	$2 \times 20$	$3 \times 13$						

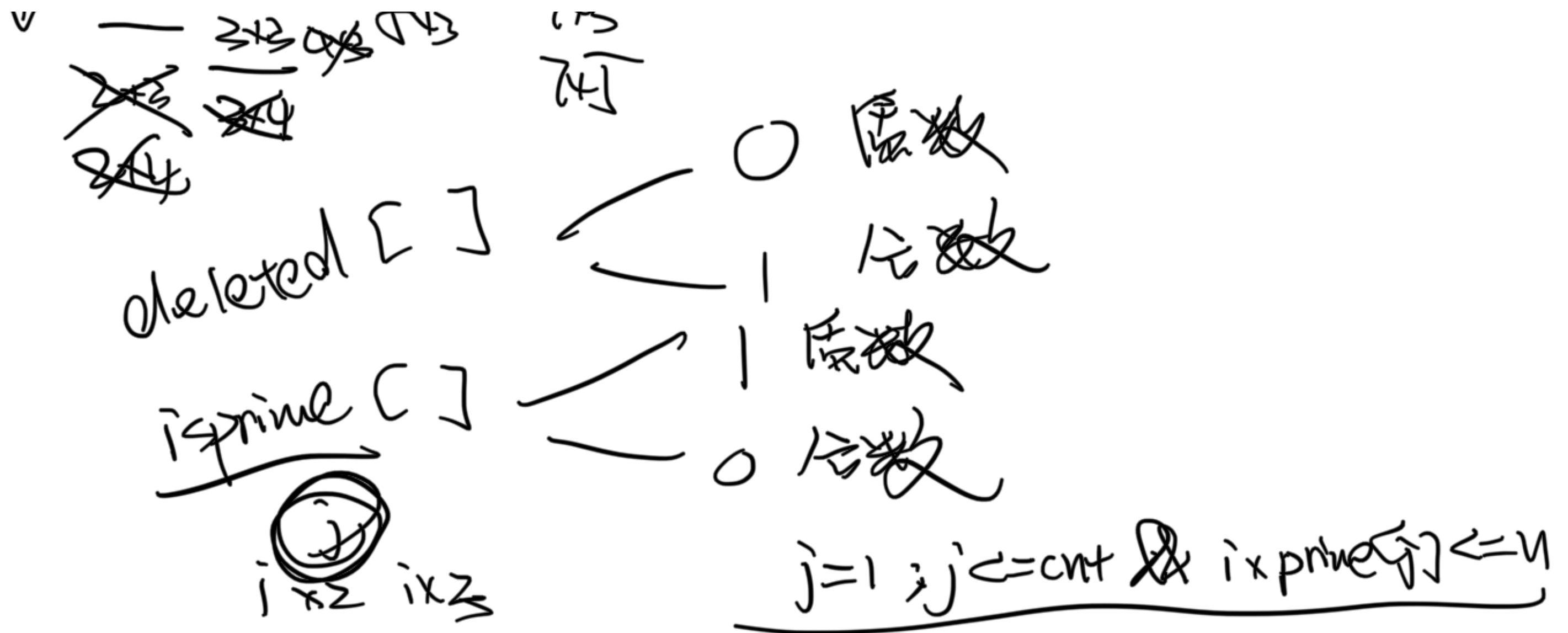
$\textcircled{2} \times \frac{1}{2}$   
 $\textcircled{3} \times \frac{6}{1}$

②  $\frac{6}{2}$

③  $\frac{6}{3}$

$\underline{2} \ 3 \ 4 \ 5 \ 6 \ 7$   
 $\downarrow$





```

14 for (int i = 2; i <= n; i++) {
15     if (isPrime[i]) { // 没筛掉
16         Prime[++cnt] = i; // i成为下一个素数
17     }
18
19     for (int j = 1; j <= cnt && i * Prime[j] <= n /* 不超上限 */; j++) {
20         // 从Prime[1], 即最小质数2开始, 逐个枚举已知的质数, 并期望Prime[j]是(i*Prime[j])的最小质因数
21         // 当然, i肯定比Prime[j]大, 因为Prime[j]是在i之前得出的
22         isPrime[i * Prime[j]] = 0;
23
24         if (i % Prime[j] == 0) { // i中也含有Prime[j]这个因子
25             break; // 重要步骤。见原理
26         }
27     }

```

$$n = 15$$
$$\underline{2} \quad \underline{3} \quad \underline{1} \quad \underline{7} \quad || \quad \underline{13}$$

↑  
cnt

$$6 + 6 = 12$$

242

→  $\frac{2}{4}$     $\frac{3}{6}$     $\frac{4}{8}$     $\frac{3}{9}$     $\frac{5}{10}$     $\frac{6}{12}$     $\frac{7}{14}$     $\frac{1}{15}$

$$4 = 2 \times 2$$
$$6 = 2 \times 3$$
$$8 = 2 \times 4$$

$$8 = \underline{2+2+2}$$

$$; \leq 7411 = 77$$

$9 = 3 \times 3$   
 $10 = 2 \times 5$   
 $12 = 2 \times 6$

$$12 = 2 + 2 + 3$$

$14 = 2 + 7$   
 $15 = 2 + 5$

$$\frac{1 \times 2}{1 \times 2}$$

$p_1 \times p_2 \times \dots \times p_n$

77

$1 \times 7$

$77 \times 1$   
 $77 \times 7$   
 $77 \times 11$   
 $77 \% 7 = 0$

$77 \times 2 =$

7

2

3

4



$77 \times 2 = 2 + 74 + 11$   
 $77 \times 3$   
 $77 \times 4$   
 $77 \times 7$