

誠,樸,精,勤



## Matlab HW7: Exercise from Chap 4

曾柏軒 (Po-Hsuan Tseng) phtseng@ntut.edu.tw

November 15, 2016



# TAIPEI

#### **Matlab HW5**

1 Exercise 4.4: AR(1) PSD - lowpass or highpass

**2** Exercise 4.5: Filter frequency response

3 Exercise 4.12: Verification of the PSD

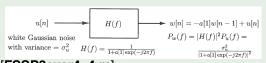


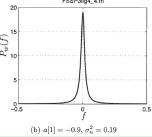
## AR(1) PSD - lowpass or highpass

#### Example 1 (Exercise 4.4: AR(1) PSD - lowpass or highpass)

Choose for the AR parameters a[1] = 0.9 and  $\sigma_u^2 = 0.19$ .

- 1 Using ARpsd.m obtain values of the AR(1) PSD and the corresponding frequencies and plot the results.
- 2 Compare the PSD against the one a[1] = -0.9 and  $\sigma_u^2 = 0.19$  as shown in the left figure below. What can you say about the effect of the sign of a[1] upon the PSD?









## Filter frequency response

## Example 2 (Exercise 4.5: Filter frequency response)

Plot the magnitude of the filter frequency response given by (4.5) for  $-1/2 \le f \le 1/2$  using a[1] = -0.9.

$$u[n] \longrightarrow H(f) \longrightarrow w[n] = -a[1]w[n-1] + u[n]$$
 white Gaussian noise 
$$P_w(f) = |H(f)|^2 P_u(f) = \frac{1}{1+a[1]\exp(-j2\pi f)}$$
 
$$\frac{\sigma_u^2}{|1+a[1]\exp(-j2\pi f)|^2}$$

#### [FSSP3exer4\_5.m]



#### Verification of the PSD

#### Example 3 (Exercise 4.12: Verification of the PSD)

Using **ARpsd.m**, plot the PSD for AR process where  $\sigma_u^2=1$  and a[1]=-0.9, a[1]=-0.8, and a[1]=-0.7. Compare your results to Fig. 1. Note at which times the AR(1) filter parameters takes on these values from the expression a[1,n]=-0.9+0.2(n/N).

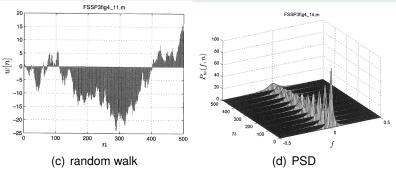


Figure 1: (a) Realization of random walk (Wiener process); (b)  $P_{W}(f,n)$  for  $n=0,50,100,\ldots,500$ : Time-varying power spectral density for the AR(1) dynamical noise process. The AR(1) filter has a time-varying and constant excitation noise variance.

