# DS-Autumn 2023 — Homework 3Solutions

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#### 摘要

二叉树实现及应用面向过程面向对象定义
二叉树遍历(九种方法递归非递归\*2\*3
preorder inorder postorder
复杂度时间空间
最坏情况最好情况最废空间最省空间
二叉树的主要性质
语法制导编辑器
修改数据结构(不借助外力 stack queue
三叉链表利用空指针(增加标识
哈夫曼树定义性质应用
二叉树分类
BST

# 1. 二叉树实现

- (a) 功能实现
- (b) 应用

# 1.1 面向过程

#### **Solutions**:

1. 结构体 ArrayDeque.java

ASL 平均查找长度

```
/** Array based list.

* @author zilong

*/
```

### 1.2 面向对象

#### **Solutions**:

1. interface BinaryTree.java

```
#include <iostream>
       #include "../hw2/SeqStack.cpp"
2
       //#define NULL nullptr
       #define cin std::cin
       #define cout std::cout
       #define endl std::endl
       template <class T>
9
       class BinaryTreeNode{
       private:
           T data;
12
            BinaryTreeNode<T>* left;
            BinaryTreeNode<T>* right;
14
15
16
       public:
17
            BinaryTreeNode();
18
            BinaryTreeNode(const T& elem);
            BinaryTreeNode(const T& elem, BinaryTreeNode<T>* 1,
20
               BinaryTreeNode<T>* r);
            ~BinaryTreeNode(){};
21
           T value() const;
            BinaryTreeNode<T>* leftchild() const;
23
            BinaryTreeNode<T>* rightchild() const;
24
25
                  setLeftchild(BinaryTreeNode <T>*);
            void
                  setRightchild(BinaryTreeNode <T>*);
26
                  setValue(const T& val);
            void
            bool
                  isLeaf() const;
       };
29
30
32
       template < class T>
33
       BinaryTreeNode <T>::BinaryTreeNode(){
            data = T();
35
            left = nullptr;
36
            right = nullptr;
       }
38
39
       template < class T>
```

```
BinaryTreeNode <T>::BinaryTreeNode(const T& elem){
41
            data = elem;
42
            left = nullptr;
43
            right = nullptr;
44
       }
45
46
        template < class T>
47
        BinaryTreeNode <T>::BinaryTreeNode(const T& elem, BinaryTreeNode <T>* 1,
           BinaryTreeNode<T>* r){
            data = elem;
49
            left = 1;
50
            right = r;
51
       }
52
53
54
        template < class T>
55
       T BinaryTreeNode <T>::value() const{
56
            return this->data;
57
       }
58
59
        template < class T>
60
        BinaryTreeNode<T>* BinaryTreeNode<T>::leftchild() const{
61
            return this->left;
62
       }
64
        template < class T>
65
        BinaryTreeNode <T>* BinaryTreeNode <T>::rightchild() const{
            return this->right;
67
       }
68
70
        template < class T>
        void BinaryTreeNode<T>::setLeftchild(BinaryTreeNode<T>* Lchild){
71
            this->left = Lchild;
       }
73
74
        template < class T>
75
       void BinaryTreeNode <T>::setRightchild(BinaryTreeNode <T>* Rchild){
76
            this->right = Rchild;
77
       }
79
        template < class T>
80
        void BinaryTreeNode <T>::setValue(const T& Value){
            this->data = Value;
83
84
       template < class T>
85
```

```
bool BinaryTreeNode <T>::isLeaf() const{
86
            return false;
87
        }
88
90
        enum Tag{L, R, M};
91
        template <class T>
92
        class StackNode{
93
        public:
94
            BinaryTreeNode<T>* pointer;
95
            Tag tag;
            StackNode() {pointer = nullptr; tag = L;}
97
            StackNode(BinaryTreeNode < T > * ptr, Tag tg) {pointer = ptr; tag = tg;}
98
        };
103
        template <class T>
        class BinaryTree{
105
        protected:
            BinaryTreeNode<T>* root;
        public:
108
            BinaryTree() {root = nullptr;}
            BinaryTree(BinaryTreeNode<T>* r) {root = r;}
            ~BinaryTree() { DeleteBinaryTree(root); };
111
            bool isEmpty() { return root==nullptr; };
            void visit(const BinaryTree <T>& curr){cout << curr.root->value() << "u
113
            BinaryTreeNode < T > *& Root() {return root;};
            void CreateTree(const T& data, BinaryTreeNode<T>* lefttree,
115
                BinaryTreeNode<T>* righttree);
            void CreateTree(BinaryTreeNode <T> *&r);
            void DeleteBinaryTree(BinaryTreeNode<T>* root);
117
118
            void PreOrder(BinaryTreeNode < T > * root);
            void InOrder(BinaryTreeNode <T>* root);
120
            void PostOrder(BinaryTreeNode <T>* root);
121
            void PreOrderLikeRecusion(BinaryTreeNode <T>* root);
122
            void InOrderLikeRecusion(BinaryTreeNode<T>* root);
123
            void PostOrderLikeRecusion(BinaryTreeNode <T>* root);
124
            void PreOrderWithoutRecusion(BinaryTreeNode<T>* root);
125
            void InOrderWithoutRecusion(BinaryTreeNode<T>* root);
126
            void PostOrderWithoutRecusion(BinaryTreeNode<T>* root);
            void LevelOrder(BinaryTreeNode <T>* root);
128
        };
129
```

```
130
131
        template < class T>
132
        void BinaryTree<T>::CreateTree(const T& data, BinaryTreeNode<T>*
133
            leftTree, BinaryTreeNode<T>* rightTree) {
            root = new BinaryTreeNode<T>(data, leftTree, rightTree);
134
            BinaryTree(root);
135
        }
136
137
138
139
140
        template < class T>
141
        void BinaryTree<T>::DeleteBinaryTree(BinaryTreeNode<T>* Root){
142
            if (Root != NULL) {
143
                 DeleteBinaryTree(Root->leftchild());
144
                 DeleteBinaryTree(Root->rightchild());
145
                 Root -> ~ BinaryTreeNode();
146
            }
147
        }
148
```

# 2.二叉树遍历

(a) 二叉树遍历(九种方法递归非递归 \* 2 \* 3 preorder inorder postorder 复杂度时间空间 最坏情况最好情况最废空间最省空间

#### preorder

#### recursive

#### **Solutions**:

```
template < class T>
void BinaryTree < T>::PreOrder (BinaryTreeNode < T>* root) {
    if (root == NULL) return;
    visit(root);
    PreOrder (root->leftchild());
    PreOrder (root->rightchild());
}
```

#### nonrecursive

1. recursivelike

#### **Solutions**:

```
template < class T>
   void BinaryTree <T>::PreOrderLikeRecusion(BinaryTreeNode <T> * root){
       SeqStack < BinaryTreeNode < T > * > tStack (10);
       BinaryTreeNode<T>* pointer = root;
       while(!tStack.IsEmpty() || pointer){
5
           if (pointer){
                visit(pointer);
                tStack.Push(pointer);
                pointer = pointer->leftchild();
           } else{
                pointer = tStack.Pop();
11
                //tStack.Pop();
12
                pointer = pointer->rightchild(); }
13
       }
14
15
```

2. other way

```
template < class T>
   void BinaryTree<T>::PreOrderWithoutRecusion(BinaryTreeNode <T> * root){
       SeqStack < BinaryTreeNode < T > * > tStack (10);
       BinaryTreeNode<T>* pointer = root;
       if (!pointer) {return;};
       tStack.Push(pointer);
       while(!tStack.IsEmpty()){    //use the feature of stack
           pointer = tStack.Pop();
           visit(pointer);
           if(pointer->rightchild()){
               tStack.Push(pointer->rightchild());// first in then out
           if (pointer->leftchild()){
13
               tStack.Push(pointer->leftchild());
14
16
       //does queue do the same work?
17
```

#### inorder

#### recursive

#### Solutions:

```
template < class T>
void BinaryTree < T>::InOrder (BinaryTreeNode < T>* root) {
    if (root == NULL) return;
    InOrder (root -> leftchild());
    visit (root);
    InOrder (root -> rightchild());
}
```

#### nonrecursive

1. recursivelike

```
template < class T>
void BinaryTree < T>::InOrderLikeRecusion(BinaryTreeNode < T> * root){

SeqStack < BinaryTreeNode < T> *> tStack(10);

BinaryTreeNode < T> * pointer = root;

while (!tStack.IsEmpty() || pointer){

if (pointer) {

tStack.Push(pointer);
```

```
pointer = pointer->leftchild();

pointer = tStack.Pop();

pointer = tStack.Pop();

visit(pointer);

//tStack.Push(pointer);

//tStack.Pop();

pointer = pointer->rightchild(); }

}
```

2. other way

#### **Solutions**:

```
template < class T>
   void BinaryTree <T>::InOrderWithoutRecusion(BinaryTreeNode <T> * root){
       SeqStack<StackNode<T>*> tStack(10);
       //BinaryTreeNode<T>* pointer = root;
       StackNode <T>* Tagptr = new StackNode <T>();
       Tagptr->pointer = root;
       if (!Tagptr->pointer) {return;};
       tStack.Push(Tagptr);
       while(!tStack.IsEmpty()){
            Tagptr = tStack.Pop();
11
            if (Tagptr->tag == L) {
                if (Tagptr->pointer->rightchild()){
13
                    StackNode < T > * tem = new
14
                        StackNode <T > (Tagptr -> pointer -> rightchild(), L);
                    tStack.Push(tem);
15
                }
16
                StackNode < T > * tem = new StackNode < T > (Tagptr -> pointer, R);
                tStack.Push(tem);
18
                if (Tagptr->pointer->leftchild()){
19
                    StackNode < T > * tem = new
                        StackNode <T>(Tagptr->pointer->leftchild(), L);
                    tStack.Push(tem);
21
                }
            } else visit(Tagptr->pointer);
23
       }
24
```

postorder

recursive

```
template < class T>
void BinaryTree < T>::PostOrder (BinaryTreeNode < T>* root) {
   if (root == NULL) return;
   PostOrder (root -> leftchild());
   PostOrder (root -> rightchild());
   visit (root);
}
```

#### nonrecursive

1. recursivelike

#### **Solutions**:

```
template < class T>
   void BinaryTree <T>::PostOrderLikeRecusion(BinaryTreeNode <T> * root){
       SeqStack<StackNode<T>* > tStack(10);
       StackNode < T > * Tagptr = new StackNode < T > (root, L);
       while (!tStack.IsEmpty() || Tagptr->pointer != nullptr ){
           while (Tagptr->pointer != nullptr) {
                StackNode <T>* tem = new StackNode <T>(Tagptr->pointer, L);
                tStack.Push(tem);
                Tagptr->pointer = Tagptr->pointer->leftchild();
10
           if (!tStack.IsEmpty()) {
12
                Tagptr = tStack.Pop();
13
                if (Tagptr->tag == L ) {
14
                    StackNode <T>* tem = new StackNode <T>(Tagptr->pointer, R);
15
                    tStack.Push(tem);
16
                    Tagptr->pointer = Tagptr->pointer->rightchild();
18
                    visit(Tagptr->pointer);
19
                    Tagptr->pointer = nullptr;
                }
21
           }
22
       }
24
```

2. other way

```
template < class T>
void BinaryTree < T>::PostOrderWithoutRecusion(BinaryTreeNode < T> * root){
    SeqStack < StackNode < T> * tStack(10);
    //BinaryTreeNode < T> * pointer = root;
```

```
StackNode <T>* Tagptr = new StackNode <T>();
5
       Tagptr->pointer = root;
       if (!Tagptr->pointer) {return;};
       tStack.Push(Tagptr);
       while(!tStack.IsEmpty()){
            Tagptr = tStack.Pop();
11
            if (Tagptr->tag == L) {
12
                StackNode < T > * tem = new StackNode < T > (Tagptr -> pointer, R);
13
                tStack.Push(tem);
14
                if (Tagptr->pointer->rightchild()){
15
                     StackNode <T>* tem = new
16
                        StackNode <T>(Tagptr->pointer->rightchild(), L);
                    tStack.Push(tem);
                }
18
                if (Tagptr->pointer->leftchild()){
19
                    StackNode <T>* tem = new StackNode <T>
                        (Tagptr->pointer->leftchild(), L);
                    tStack.Push(tem);
21
                }
22
            } else if (Tagptr->tag == R) {
23
                StackNode <T>* tem = new StackNode <T>(Tagptr->pointer, M);
24
                tStack.Push(tem);
            } else {
26
                visit(Tagptr->pointer);
27
           }
28
       }
30
```

#### 复杂度分析

- 1. 复杂度时间空间
- 2. 最坏情况最好情况

#### 层次遍历

- 1. 复杂度时间空间
- 2. 借助外力 stack queue 逻辑

# 3.二叉树的定义、主要性质、定理

- (a) 递归定义及基本术语
- (b) 分类顺序存储链式存储
- (c) 性质\*5

### definition

#### **Solutions**:

1. a recursive definition

## category

#### **Solutions**:

- 1. sequential structure
- 2. list structure

## properties quality character

- 1. i &  $2^{i-1}$  floor
- 2. k &  $2^k 1$  all the tree
- 3.  $n_0 = n_2 + 1$
- 4. height =  $[\log_2 n] + 1$
- 5. structure of root, Lchild, Rchild

# 4.证明

### YOUR ANSWER GOES HERE

# something to prove

### ${\bf Solutions:}$

- 1. 给定tree 遍历序列唯一给定位置唯一存在(顺序唯一
- 2. 中序遍历猜想 + 先序猜想
- 3. 遍历时的性质\*5
- 4. n node 2\*n pointer N-1 in use

# 5.修改数据结构

#### YOUR ANSWER GOES HERE

- (a) 利用空指针(增加标识
- (b) 三叉链表

## 1.1 利用空指针

#### **Solutions**:

1. 结构体 ArrayDeque.java

```
/** Array based list.
* @author zilong
*/
```

## 1.2 三叉链表

#### **Solutions**:

1. interface List.java

```
public interface List<Item>
```

## 6.Huffman tree

- (a) 递归定义及基本术语
- (b) 分类顺序存储链式存储
- (c) 应用\*4

## definition

#### **Solutions**:

1. a recursive definition

## category

#### **Solutions**:

- 1. sequential structure
- 2. list structure

## properties quality character

- 1. i &  $2^{i-1}$  floor
- 2. k &  $2^k 1$  all the tree
- 3.  $n_0 = n_2 + 1$
- 4. height =  $[\log_2 n] + 1$
- 5. structure of root, Lchild, Rchild

# 7.Binary searching/sorting Tree

# 8.BinaryTree categories

# 9.BinaryTree in java