Import image and convert to gray scale, double. Record size of image.

```
clc;clear;
load('Contrast2.mat');
load('Contrast1.mat');
[m,n]=size(Contrast2);
origin=Contrast1;
translated=Contrast2;
```

Calculate myNCC

```
R_beforeregis=myNCC(origin(4:end,3:end),translated(4:end,3:end));
diff1=origin-translated;
```

In order to translate the contrast2 back. We should translate -1.8 in x and -2.1 in y.

```
dx=-1.8;
dy=-2.1;
```

Now translate in x and y direction and calculate pixel value using intepolation.(backward transformation)

```
% Create a grid of coordinates
[X, Y] = meshgrid(1:n, 1:m);
% Compute the translated coordinates
X_{regis} = X + dx;
Y_{regis} = Y + dy;
% Initialize the output image with NaNs
regis image = NaN(m, n);
% Find the integer coordinates surrounding the translated coordinates
x1 = floor(X_regis);
x2 = ceil(X regis);
y1 = floor(Y_regis);
y2 = ceil(Y_regis);
% Identify valid interpolation points (within image bounds)
validMask = x1 >= 1 & x2 <= n & y1 >= 1 & y2 <= m;
% Interpolation weights
wx = X_regis - x1;
wy = Y_regis - y1;
% Retrieve pixel values at the four surrounding points for valid points
Q11 = NaN(m, n); Q21 = NaN(m, n);
Q12 = NaN(m, n); Q22 = NaN(m, n);
Q11(validMask) = double(translated(sub2ind([m, n], y1(validMask), x1(validMask))));
```

```
Q21(validMask) = double(translated(sub2ind([m, n], y1(validMask), x2(validMask))));
Q12(validMask) = double(translated(sub2ind([m, n], y2(validMask), x1(validMask))));
Q22(validMask) = double(translated(sub2ind([m, n], y2(validMask), x2(validMask))));

% Perform bilinear interpolation for valid points
regis_image(validMask) = (1 - wx(validMask)) .* (1 - wy(validMask)) .*
Q11(validMask) + ...
    wx(validMask) .* (1 - wy(validMask)) .* Q21(validMask) + ...
    (1 - wx(validMask)) .* wy(validMask) .* Q12(validMask) + ...
    wx(validMask) .* wy(validMask) .* Q22(validMask);
regis_image(isnan(regis_image)) = 0;
```

Calculate myNCC and subtract image with Contrast1

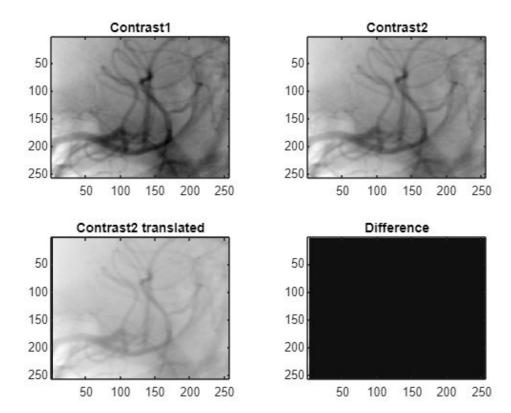
```
Difference=origin-regis_image;
% regis_image=uint8(regis_image);
% origin=uint8(origin);
% translated=uint8(translated);
R_afterregistration=myNCC(origin(4:end,3:end),regis_image(4:end,3:end));
```

Print the result value and show the difference image with scale bar

```
fprintf('The result before registration is %d and after registration is
%d.\n',R_beforeregis,R_afterregistration);
```

The result before registration is 9.778922e-01 and after registration is 9.998184e-01.

```
tiledlayout(2,2)
nexttile
imagesc(origin)
colormap('gray')
title('Contrast1')
nexttile
imagesc(translated)
title('Contrast2')
colormap('gray')
nexttile
imagesc(regis_image)
title('Contrast2 translated')
colormap('gray')
nexttile
imagesc(Difference)
title('Difference')
colormap('gray')
```



Q3

NEW

```
% %initialize first guess for translation, [tx, ty]
% t_i= [0,0];
% frames = struct('cdata', {}, 'colormap', {});
% %initialize array
% param=struct();
% param.scaling=1;
% %calling the cost function SSE
% costF= @(t) registrationcost(t, origin, translated);
% %costF= @(t) SSE(origin, translated, t(1),t(2), param );
% % cost_test= SSE(origin, translated, -1.8, -2.1);
% % display(cost_test)
%
% %run fminsearch on optimal translation parameters
% % and custom options to show iterations
% options = optimset( 'TolFun',1e-3, 'TolX',1e-3);
% %
        'OutputFcn', @(x, optimValues, state) ...
% %
        updateFrames(x, optimValues, state, frames)
%
                      %'OutputFcn',@regOutFun);
% [t_optimal, fval]= fminsearch(costF, t_i, options);
%
```

```
% fprintf(['The optimal translation parameters t x is %.4f, t y is %4f, ' ...
%
      'and minimal cost function is %d\n'], ...
%
      t optimal(1), t optimal(2), fval);
%
% %subtracted image without registration
% diffImg_noReg= abs(origin-translated);
%
% figure;
% subplot(2,2,1), imshow(origin,[]), title('Contrast 1');
% subplot(2,2,2), imshow(translated,[]), title('Contrast 2');
% subplot(2,2,3), imshow(uint8(diffImg_noReg)), title('Subtracted Image without
Registration');
%
% figure;
% axis off;
% movie(frames);
function cost = registrationcost(params, fixedImage, movingImage)
    persistent frames;
    if isempty(frames)
        frames = struct('cdata', {}, 'colormap', {});
    end
    % Extract translation parameters
    tx = params(1);
    ty = params(2);
    % Translate the moving image
    translatedImage = imtranslate(movingImage, [tx, ty]);
    % Compute the difference image
    differenceImage = abs(fixedImage - translatedImage);
    % Compute the sum of squared errors
    cost = sum(differenceImage(4:end,3:end).^2,"all");
    % Capture the difference image as a frame
    figure(100);
    imshow(uint8(differenceImage));
    drawnow;
    frame = getframe(gcf);
    % Store the frame
    frames(end+1) = frame;
    % Assign the updated frames to the base workspace
    assignin('base', 'frames', frames);
end
%%
```

Q4

```
t_i= [0,0];
%initialize array
param=struct();
param.scaling=1;
tolFun = [1e-1, 1e-3, 1e-5]; % Different TolFun values
tolX = [1e-1, 1e-3, 1e-5]; % Different TolX values
scaling= [1,10,100] % scaling factor
scaling = 1 \times 3
    1
        10
             100
costF= @(t) SSE(origin, translated, t(1),t(2),param );
%initialize arrays to store result
results_fun=[];
results_x=[];
results_scaling=[];
%chaing tolerance for function value
for f=1:length(tolFun)
    options=optimset('TolFun', tolFun(f), 'Display', 'off');
    [t_op, fvalue,exitflag, output]=fminsearch(costF, t_i, options)
    r1.TolFun= tolFun(f);
    r1.Cost= fvalue;
    r1.Iteration= output.iterations;
    if exitflag==1;
         r1.Outcomes='Sucess';
    else
         r1.Outcomes='Failure';
    results_fun= [results_fun, r1];
end
t_op = 1 \times 2
   1.8398
            2.0642
fvalue = 7.1007e + 04
exitflag = 1
output = struct with fields:
   iterations: 83
    funcCount: 160
    algorithm: 'Nelder-Mead simplex direct search'
      message: 'Optimization terminated: → the current x satisfies the termination criteria using OPTIONS.TolX of 1
t op = 1 \times 2
   1.8398
            2.0642
fvalue = 7.1007e + 04
exitflag = 1
output = struct with fields:
   iterations: 86
    funcCount: 166
```

```
        TolFun
        Cost
        Iteration
        Outcomes

        0.1
        71007
        83
        {'Sucess'}

        0.001
        71007
        86
        {'Sucess'}

        1e-05
        71007
        94
        {'Sucess'}
```

```
%changing tolerance for x value
for x= 1:length(tolX)
    options= optimset('TolX', tolX(x),'Display','off');
    [t_op, fvalue,exitflag, output]=fminsearch(costF, t_i, options)
    r2.TolX= tolX(x);
    r2.Cost=fvalue;
    r2.Iteration= output.iterations;
    if exitflag==1;
        r2.Outcomes='Sucess';
    else
        r2.Outcomes='Failure';
    end
    results_x=[results_x, r2];
end
```

```
t_op = 1 \times 2
    1.8399
              2.0642
fvalue = 7.1007e + 04
exitflag = 1
output = struct with fields:
    iterations: 89
     funcCount: 172
     algorithm: 'Nelder-Mead simplex direct search'
       message: 'Optimization terminated: → the current x satisfies the termination criteria using OPTIONS.TolX of 1
t_op = 1 \times 2
    1.8399
              2.0642
fvalue = 7.1007e + 04
exitflag = 1
output = struct with fields:
    iterations: 89
     funcCount: 172
     algorithm: 'Nelder-Mead simplex direct search'
       message: 'Optimization terminated: → the current x satisfies the termination criteria using OPTIONS.TolX of 1
t_op = 1 \times 2
    1.8399
              2.0642
fvalue = 7.1007e+04
exitflag = 1
```

```
TolX
         Cost
                  Iteration
                                 Outcomes
 0.1
         71007
                     89
                                {'Sucess'}
                                {'Sucess'}
0.001
         71007
                     89
1e-05
         71007
                     90
                                {'Sucess'}
```

funcCount: 172

```
%changing scaling factor
for s=1:length(scaling)
    param.scaling= scaling(s);
    options=optimset('Display','off');
    [t_op, fvalue,exitflag, output]=fminsearch(costF, t_i, options)
    r3.Scale= scaling(s);
    r3.Cost=fvalue;
    r3.Iteration= output.iterations;
    if exitflag==1;
        r3.Outcomes='Sucess';
    else
        r3.Outcomes='Failure';
    end
    results_scaling=[results_scaling, r3];
end
```

```
t_op = 1 \times 2
    1.8399
              2.0642
fvalue = 7.1007e + 04
exitflag = 1
output = struct with fields:
    iterations: 89
     funcCount: 172
     algorithm: 'Nelder-Mead simplex direct search'
       message: 'Optimization terminated: → the current x satisfies the termination criteria using OPTIONS.TolX of 1
t_op = 1 \times 2
    1.8399
fvalue = 7.1007e + 04
exitflag = 1
output = struct with fields:
    iterations: 89
     funcCount: 172
     algorithm: 'Nelder-Mead simplex direct search'
       message: 'Optimization terminated: → the current x satisfies the termination criteria using OPTIONS.TolX of 1
t op = 1\times2
    1.8399
              2.0642
fvalue = 7.1007e+04
exitflag = 1
output = struct with fields:
    iterations: 89
```

algorithm: 'Nelder-Mead simplex direct search'

message: 'Optimization terminated:

the current x satisfies the termination criteria using OPTIONS.TolX of 1

table3= struct2table(results_scaling);
disp(table3);

Scale	Cost	Iteration	Outcomes
			
1	71007	89	{'Sucess'}
10	71007	89	{'Sucess'}
100	71007	89	{'Sucess'}