# STA721 Final Project

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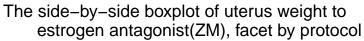
- 1. Summary
- 2. Introductions
- 3. EDA

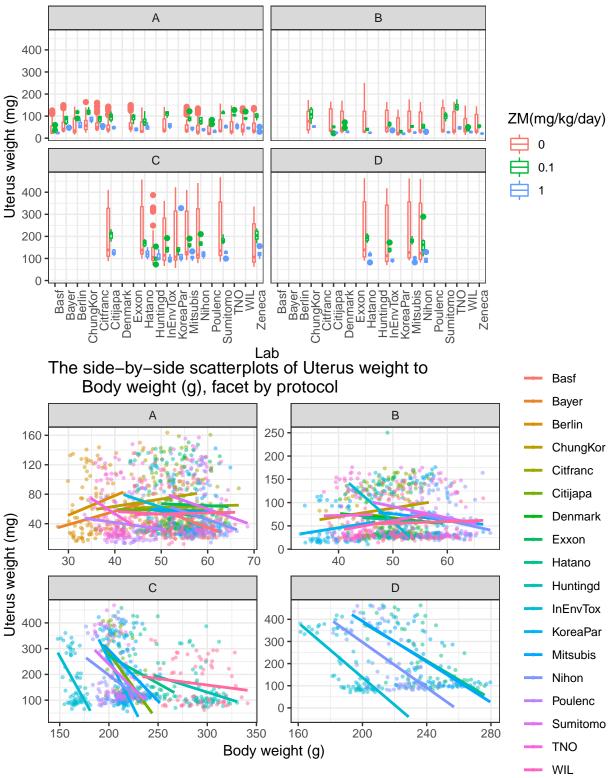
#### 4. Model I And Result

We build a linear regression model excluding the group variable, because the group index varies in labs and cannot be considered as a factor. After looking into the data, we treat all variables but uterus and weight as factor. In order to use one full model to address all question, we include the interaction term of EE:protocol, ZM:protocol, EE:lab, ZM:lab. From EDA part we can find that some experiments are not done in some EE:ZM combination. So we cannot include this interaction term. Then we use boxcox and find that the log transformation is preferred. Therefore, the final model will be:

$$\begin{split} \log(\text{uterus}) &= \beta_0 + \beta_1 \log(\text{weight}) + \beta_2 \text{EE} + \beta_3 \text{ZM} + \beta_4 \text{lab} + \beta_5 \text{protocol} \\ &+ \beta_6 \text{EE:lab} + \beta_7 \text{ZM:lab} + \beta_8 \text{EE:protocol} + \beta_9 \text{ZM:protocol} + \epsilon \\ &\epsilon \sim N(0, \sigma^2) \end{split}$$

#### 5. Conclusion



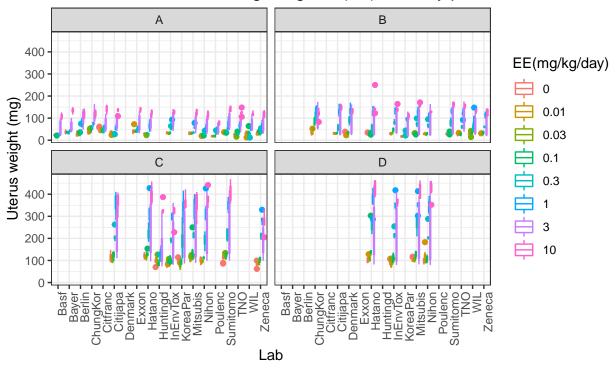


## Appendix

#### EDA

```
bioassay_lm = bioassay[,-7]
str(bioassay_lm)
## 'data.frame':
                   2677 obs. of 6 variables:
## $ uterus : num 21 22 21 26 24 25 22 26 24 22 ...
## $ weight : num 61.9 55.9 59.1 54.8 57.5 57.6 60.3 59 59.1 61.4 ...
## $ protocol: Factor w/ 4 levels "A", "B", "C", "D": 1 1 1 1 1 1 1 1 1 1 ...
             : Factor w/ 8 levels "0","0.01","0.03",...: 1 1 1 1 1 1 1 1 1 1 1 ...
## $ ZM
              : Factor w/ 3 levels "0", "0.1", "1": 1 1 1 1 1 1 1 1 1 ...
## $ lab
              : Factor w/ 19 levels "Basf", "Bayer", ...: 1 1 1 1 1 1 1 1 1 1 1 ...
table(bioassay_lm$EE, bioassay_lm$ZM)
##
##
           0 0.1
##
                   0
          484
              0
    0.01 234
##
                   0
##
    0.03 239
                   0
##
     0.1 246
    0.3 246 0
##
                   0
##
         246
##
         246 245 246
     3
     10 245
ggplot(data=bioassay,mapping = aes(y = uterus,x = lab,color=EE))+
  geom_boxplot()+theme_bw()+facet_wrap(~ protocol) +
  theme(axis.text.x = element_text(angle = 90, hjust = 1)) +
  labs(x = "Lab", y="Uterus weight (mg)", title="The side-by-side boxplot of uterus weight for differen
       different dose of estrogen agonist(EE), facet by protocol", caption="", colour="EE(mg/kg/day)")
```

# The side-by-side boxplot of uterus weight for different labs and different dose of estrogen agonist(EE), facet by protocol

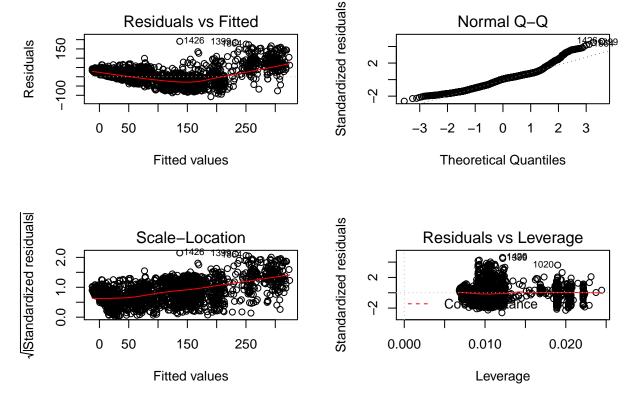


#### Model Part I

```
lm1 = lm(uterus~., data = bioassay_lm)
#summary(lm1)
step(lm1, k=log(2677))
## Start: AIC=20175.57
## uterus ~ weight + protocol + EE + ZM + lab
##
              Df Sum of Sq
                                 RSS
                                       AIC
                             4568714 20176
## <none>
                            4873553 20206
## - lab
              18
                    304839
## - weight
               1
                    117187
                            4685901 20236
                            5424374 20612
## - protocol 3
                    855660
## - ZM
               2
                   2030817
                             6599531 21144
## - EE
                   7683826 12252540 22761
##
## lm(formula = uterus ~ weight + protocol + EE + ZM + lab, data = bioassay_lm)
##
## Coefficients:
   (Intercept)
                                protocolB
                                             protocolC
                                                           protocolD
##
                     weight
                   -0.45365
                                             207.53588
                                                           221.22623
##
      15.82251
                                  7.84315
                     EE0.03
                                                 EE0.3
                                                                 EE1
##
        EE0.01
                                    EE0.1
##
      -0.60177
                    0.26008
                                  8.01257
                                              47.94479
                                                           106.35605
##
           EE3
                       EE10
                                    ZMO.1
                                                   ZM1
                                                            labBayer
```

```
136.45891
                   150.55730
                                 -80.51563
                                              -127.18576
                                                               2.60266
##
                                                            labDenmark
##
     labBerlin labChungKor
                               labCitfranc
                                             labCitijapa
      14.84134
                    32.46041
                                  26.21060
                                                21.52689
                                                              18.95727
##
##
      labExxon
                   labHatano
                               labHuntingd
                                             {\tt labInEnvTox}
                                                           labKoreaPar
      23.72114
                    26.83352
##
                                   0.09856
                                                 0.58445
                                                              -2.51500
## labMitsubis
                    labNihon
                                labPoulenc
                                            labSumitomo
                                                                labTNO
##
      24.63683
                    13.18893
                                  -4.14169
                                                28.52520
                                                              16.56429
                   labZeneca
##
        labWIL
##
      10.05022
                    17.93047
library(MASS)
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
box =boxcox(lm1)
      -7000
                                                   0006-
log-Likelihood
     -11000
             -2
                                                 0
                               -1
                                                                    1
                                                                                      2
                                                 λ
lm2 = lm(formula = log(uterus) ~ log(weight) + protocol + EE + ZM + lab, data = bioassay_lm)
lm3 = lm(formula = log(uterus) ~ log(weight) + protocol + EE*lab +ZM*lab, data = bioassay_lm)
#summary(lm3)
par(mfrow=c(2,2))
```

plot(lm1)



Frequentist Random Effect Model:

```
library(lme4)

## Loading required package: Matrix

randomeffect = lmer(log(uterus) ~ log(weight) + protocol + EE + ZM + (1+EE+ZM|lab), data = bioassay_lm)

## Warning in commonArgs(par, fn, control, environment()): maxfun < 10 *

## length(par)^2 is not recommended.

## Warning in optwrap(optimizer, devfun, getStart(start, rho$lower, rho$pp), :

## convergence code 1 from bobyqa: bobyqa -- maximum number of function

## evaluations exceeded

## singular fit

#summary(randomeffect)

lm.full = lm(uterus-EE*lab+EE*protocol+ZM*lab+ZM*protocol+protocol+weight, data = bioassay)

#summary(lm.full)

#anova(lm.full)</pre>
```

### Model Part II

#### Model Part III