GPU-parallel Gibbs sampling of a hierarchical model of hybrid vigor in RNA-seg experiments

Will Landau

Iowa State University

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GPU-parallel Gibbs sampling of a hierarchical model of hybrid vigor in RNA-seq experiments

background

## Outline

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#### The Gibbs sampler

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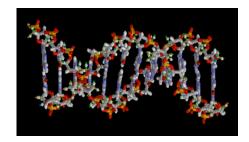
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## DNA



··· GTGCATCTGACTCCTGAGGAGAAG ··· CACGTAGACTGAGGACTCCTCTTC

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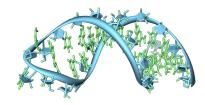
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## **RNA**



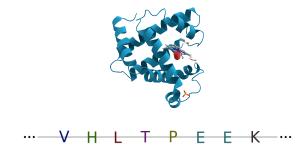
GUGCAUCUGACUCCUGAGGAGAAG · · ·

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DNA and RNA

## **Proteins**



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DNA and RNA

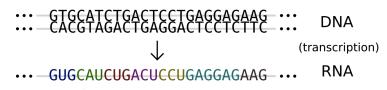
# Central dogma: how organisms make proteins

```
GTGCATCTGACTCCTGAGGAGAAG ...
                               DNA
```

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Central dogma

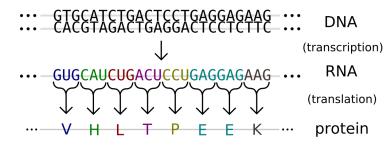
# Central dogma: how organisms make proteins



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## Central dogma of genetics



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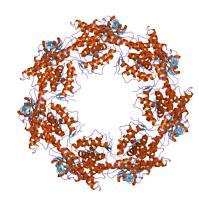
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### HSP<sub>60</sub>

- ► HSP = heat shock protein.
- ▶ Prevent heat damage to other proteins.



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# Temperature spike triggers HSP60 production.

HSP60 Gene

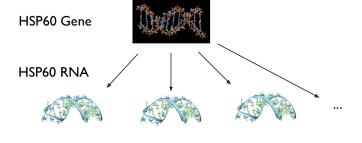


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Examples of gene regulation

## Temperature spike causes HSP60 expression.

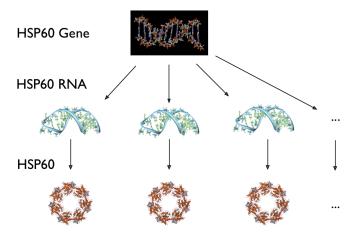


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## Temperature spike causes HSP60 expression.



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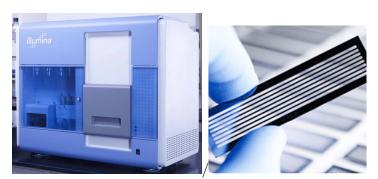
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## RNA-seq

- RNA sequencing: measure gene expression using relative abundance of RNA.
- Illumina Genome Analyzer:



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RNA-seq

# RNA-seq data: counts of amplified RNA fragments

	Treatment I		Treatn	nent 2	Treatment 3		
Gene I	100	225	0	70	279	300	106
Gene 2	0	1	I	50	501	2	7
Gene 3	3	4	2	700	900	0	0
Gene 4	893	400	760	5	5	1000	513
Gene 34897	10	13	6	819	761	902	912

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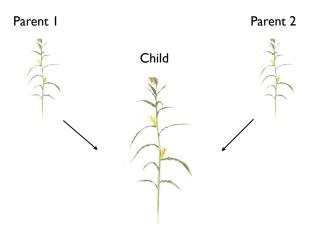
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► Goal: use RNA-seq to study hybrid vigor (heterosis).

# High-parent heterosis: child's trait surpasses both parents



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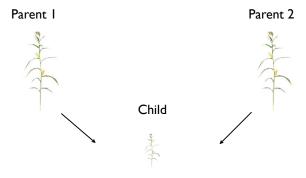
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# Low-parent heterosis: child's trait is weaker than in each parent

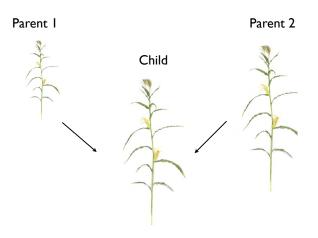


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# Mid-parent heterosis: child's trait is different than average of parents



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## High-parent heterosis in gene expression

	Parent I			Ch	ild	Parent 2	
Gene I	100	225	0	70	279	300	106
Gene 2	0	I	I	50	501	2	7
Gene 3	3	4	2	700	900	0	0
Gene 4	893	400	760	5	5	1000	513
	•••						
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$$\begin{aligned} y_{g,n} & \overset{\text{ind}}{\sim} \mathsf{Poisson}(y_{g,n} \mid \mathsf{exp}(c_n + \varepsilon_{g,n} + \mu(n,\phi_g,\alpha_g,\delta_g))) \\ c_n & \overset{\text{ind}}{\sim} \mathsf{N}(c_n \mid 0,\sigma_c^2) \\ \sigma_c & \sim \mathsf{U}(\sigma_c \mid 0,\sigma_{c0}) \\ \varepsilon_{g,n} & \overset{\text{ind}}{\sim} \mathsf{N}(\varepsilon_{g,n} \mid 0,\eta_g^2) \\ \eta_g^2 & \overset{\text{ind}}{\sim} \mathsf{Inv-Gamma}\left(\eta_g^2 \mid \mathsf{shape} = \frac{d}{2} \;, \; \mathsf{rate} = \frac{d \cdot \tau^2}{2}\right) \\ d & \sim \mathsf{U}(d \mid 0,d_0) \\ \tau^2 & \sim \mathsf{Gamma}(\tau^2 \mid \mathsf{shape} = a_\tau,\mathsf{rate} = b_\tau) \end{aligned}$$

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$$\mu(n,\phi_g,\alpha_g,\delta_g) = \begin{cases} \phi_g - \alpha_g & \text{sample } n \text{ from parent } 1 \\ \phi_g + \delta_g & \text{sample } n \text{ from child} \\ \phi_g + \alpha_g & \text{sample } n \text{ from parent } 3 \end{cases}$$

$$y_{g,n} \overset{\text{ind}}{\sim} \text{Poisson}(y_{g,n} \mid \exp(c_n + \varepsilon_{g,n} + \mu(n,\phi_g,\alpha_g,\delta_g)))$$

$$\phi_g \overset{\text{ind}}{\sim} \text{N}(\phi_g \mid \theta_\phi, \sigma_\phi^2)$$

$$\theta_\phi \sim \text{N}(\theta_\phi \mid 0, \gamma_\phi^2)$$

$$\sigma_\phi \sim \text{U}(\sigma_\phi \mid 0, \sigma_{\phi 0})$$

$$\alpha_g \overset{\text{ind}}{\sim} \pi_\alpha^{1-I(\alpha_g)}[(1 - \pi_\alpha)\text{N}(\alpha_g \mid \theta_\alpha, \sigma_\alpha^2)]^{I(\alpha_g)}$$

$$\theta_\alpha \sim \text{N}(\theta_\alpha \mid 0, \gamma_\alpha^2)$$

$$\sigma_\alpha \sim \text{U}(\sigma_\alpha \mid 0, \sigma_{\alpha 0})$$

$$\pi_\alpha \sim \text{Beta}(\pi_\alpha \mid a_\alpha, b_\alpha)$$

$$\delta_g \overset{\text{ind}}{\sim} \pi_\delta^{1-I(\delta_g)}[(1 - \pi_\delta)\text{N}(\delta_g \mid \theta_\delta, \sigma_\delta^2)]^{I(\delta_g)}$$

$$\theta_\delta \sim \text{N}(\theta_\delta \mid 0, \gamma_\delta^2)$$

$$\sigma_\delta \sim \text{U}(\sigma_\delta \mid 0, \sigma_{\delta 0})$$

$$\pi_\delta \sim \text{Beta}(\pi_\delta \mid a_\delta, b_\delta)$$

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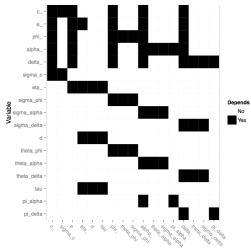
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# Partition parameters by conditional independence.



Has a full conditional that depends on...

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# Use these partitions as Gibbs steps.

$$y_{g,n} \stackrel{\text{ind}}{\sim} \mathsf{Poisson}(y_{g,n} \mid \exp(c_n + \varepsilon_{g,n} + \mu(n, \phi_g, \alpha_g, \delta_g)))$$

- From the appropriate full conditional distributions, sample the following:
- 1.  $c_1, \ldots, c_N$
- 2.  $\tau$ ,  $\pi_{\alpha}$ ,  $\pi_{\delta}$
- 3. d,  $\theta_{\phi}$ ,  $\theta_{\alpha}$ ,  $\theta_{\delta}$
- 4.  $\sigma_c$ ,  $\sigma_\phi$ ,  $\sigma_\alpha$ ,  $\sigma_\delta$ ,  $\eta_1^2$ , ...,  $\eta_c^2$
- 5.  $\varepsilon_{1,1}, \ \varepsilon_{1,2}, \ \ldots, \ \varepsilon_{1,N}, \ \varepsilon_{2,N}, \ \ldots, \ \varepsilon_{G,N}$
- $6. \phi_1, \ldots, \phi_G$
- 7.  $\alpha_1, \ldots, \alpha_G$
- 8.  $\delta_1, \ldots, \delta_C$
- and then repeat.

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## Estimated heterosis probabilities

$$\mu(\textit{n}, \phi_{\textit{g}}, \alpha_{\textit{g}}, \delta_{\textit{g}}) = \begin{cases} \phi_{\textit{g}} - \alpha_{\textit{g}} & \text{sample } \textit{n} \text{ from parent } 1 \\ \phi_{\textit{g}} + \delta_{\textit{g}} & \text{sample } \textit{n} \text{ from child} \\ \phi_{\textit{g}} + \alpha_{\textit{g}} & \text{sample } \textit{n} \text{ from parent } 3 \end{cases}$$

$$y_{g,n} \stackrel{\text{ind}}{\sim} \operatorname{Poisson}(y_{g,n} \mid \exp(c_n + \varepsilon_{g,n} + \mu(n,\phi_g,\alpha_g,\delta_g)))$$

Consider one chain with M iterations.

$$P(\text{high-parent heterosis in gene }g) pprox rac{1}{M} \sum_{i=1}^{M} I(\delta_{g}^{(i)} > |lpha_{g}^{(i)}|)$$

$$P(\text{low-parent heterosis in gene } g \ ) pprox rac{1}{M} \sum_{i=1}^{M} I(\delta_{g}^{(i)} < -|lpha_{g}^{(i)}|)$$

$$P(\text{mid-parent heterosis in gene } g) \approx \frac{1}{M} \sum_{i=1}^{M} I(\delta_g^{(i)} \neq 0)$$

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# Tons of opportunity for GPU parallelism across genes!

$$y_{g,n} \stackrel{\text{ind}}{\sim} \mathsf{Poisson}(y_{g,n} \mid \exp(c_n + \varepsilon_{g,n} + \mu(n, \phi_g, \alpha_g, \delta_g)))$$

- Sample in parallel:
  - $\blacktriangleright \phi_g$ 's
  - $ightharpoonup lpha_{
    m g}$ 's
  - $\triangleright$   $\delta_g$ 's
  - $ightharpoonup arepsilon_{{f g},{m n}}$ 's
  - $\rightarrow \eta_g$ 's

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# Example: $\phi_{\sigma}$ 's

$$y_{g,n} \stackrel{\text{ind}}{\sim} \text{Poisson}(y_{g,n} \mid \exp(c_n + \varepsilon_{g,n} + \mu(n, \phi_g, \alpha_g, \delta_g)))$$

$$\phi_g \stackrel{\text{ind}}{\sim} \text{N}(\phi_g \mid \theta_\phi, \sigma_\phi^2)$$

$$\theta_\phi \sim \text{N}(\theta_\phi \mid 0, \gamma_\phi^2)$$

$$\sigma_\phi \sim \text{U}(\sigma_\phi \mid 0, \sigma_{\phi 0})$$

• Using parallel random walk Metropolis steps, sample the  $\phi_{\sigma}$ 's from their full conditional distributions.

$$p(\phi_g \mid \cdots) \propto \exp\left(\sum_{n=1}^{N} \left[y_{g,n} \cdot \mu(n, \phi_g, \alpha_g, \delta_g)\right] - \exp(c_n + \varepsilon_{g,n} + \mu(n, \phi_g, \alpha_g, \delta_g))\right] - \frac{(\phi_g - \theta_\phi)^2}{2\sigma_\phi^2}$$

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# Tons of opportunity for GPU parallelism across genes!

$$y_{g,n} \stackrel{\text{ind}}{\sim} \text{Poisson}(y_{g,n} \mid \exp(c_n + \varepsilon_{g,n} + \mu(n, \phi_g, \alpha_g, \delta_g)))$$

- Use parallel reductions to calculate sufficient statistics for:
  - $\triangleright$   $C_n$ 's
  - τ, d
  - $\bullet$   $\theta_{\phi}$ ,  $\theta_{\alpha}$ ,  $\theta_{\delta}$
  - $\triangleright$   $\sigma_{\phi}$ ,  $\sigma_{\alpha}$ ,  $\sigma_{\delta}$ ,  $\sigma_{c}$
  - $\blacktriangleright \pi_{\alpha}, \pi_{\delta}$

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Let's take the pairwise sum of the vector,

$$(5, 2, -3, 1, 1, 8, 2, 6)$$

using 1 block of 4 threads.

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Thread 0

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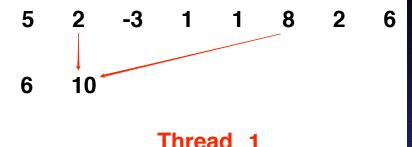
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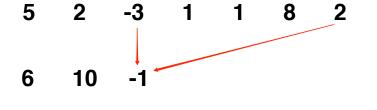
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Thread 2

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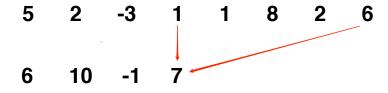
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Thread 3

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5 2 -3 1 1 8 2 6

6 10 -1 7

## **Synchronize threads**

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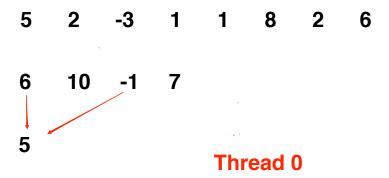
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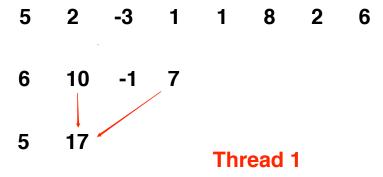
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5 2 -3 1 1 8 2 6

6 10 -1 7

5 17

**Synchronize Threads** 

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6 10 -1 7



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$$\begin{aligned} y_{g,n} & \overset{\text{ind}}{\sim} \mathsf{Poisson}(y_{g,n} \mid \mathsf{exp}(c_n + \varepsilon_{g,n} + \mu(n,\phi_g,\alpha_g,\delta_g))) \\ & \varepsilon_{g,n} \overset{\text{ind}}{\sim} \mathsf{N}(\varepsilon_{g,n} \mid 0,\eta_g^2) \\ & \eta_g^2 \overset{\text{ind}}{\sim} \mathsf{Inv\text{-}Gamma}\left(\eta_g^2 \mid \mathsf{shape} = \frac{d}{2} \;, \; \mathsf{rate} = \frac{d \cdot \tau^2}{2}\right) \\ & d \sim \mathsf{U}(d \mid 0,d_0) \\ & \tau^2 \sim \mathsf{Gamma}(\tau^2 \mid \mathsf{shape} = a_\tau,\mathsf{rate} = b_\tau) \\ p(\tau^2 \mid \cdots) \end{aligned}$$

$$=\mathsf{Gamma}\left(\tau^2 \mid \mathsf{shape} = a_\tau + \frac{\mathit{Gd}}{2} \;,\; \mathsf{rate} = b_\tau + \frac{d}{2} \sum_{g=1}^G \frac{1}{\eta_g^2}\right)$$

 Using a parallel reduction (NVIDIA's CUDA C/C++ Thrust library), calculate the sufficient statistic.

$$\sum_{g=1}^{G} \frac{1}{\eta_g^2}$$

Use an efficient rejection sampler to sample  $\tau^2$ .

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## Example: d

$$\begin{split} \mathbf{y}_{g,n} &\stackrel{\text{ind}}{\sim} \mathsf{Poisson}(\mathbf{y}_{g,n} \mid \exp(c_n + \varepsilon_{g,n} + \mu(n,\phi_g,\alpha_g,\delta_g))) \\ & \varepsilon_{g,n} \stackrel{\text{ind}}{\sim} \mathsf{N}(\varepsilon_{g,n} \mid 0,\eta_g^2) \\ & \eta_g^2 \stackrel{\text{ind}}{\sim} \mathsf{Inv\text{-}Gamma} \left( \eta_g^2 \mid \mathsf{shape} = \frac{d}{2} \;,\; \mathsf{rate} = \frac{d \cdot \tau^2}{2} \right) \\ & d \sim \mathsf{U}(d \mid 0,d_0) \\ & \tau^2 \sim \mathsf{Gamma}(\tau^2 \mid \mathsf{shape} = a_\tau,\mathsf{rate} = b_\tau) \\ & p(d \mid \cdots) \propto \Gamma\left(d/2\right)^{-G} \left( \frac{d \cdot \tau^2}{2} \right)^{Gd/2} \left( \prod_{g=1}^G \eta_g^2 \right)^{-(d/2+1)} \exp\left( -\frac{d \cdot \tau^2}{2} \sum_{g=1}^G \frac{1}{\eta_g^2} \right) I(0 < d < d_0) \end{split}$$

▶ Using parallel reductions (NVIDIA's CUDA C/C++ Thrust library), calculate the sufficient statistics:

$$\prod_{g=1}^{G} \eta_g^2 \qquad \qquad \sum_{g=1}^{G} \frac{1}{\eta_g^2}$$

▶ Use a random-walk metropolis step to sample d.

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# The Gibbs sampler

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- ► Ordinary C and GPU-accelerated versions, along with an R package wrapper, are available for download at https://github.com/wlandau/heterosis.
- ► Time for a demo...

GPU-parallel Gibbs sampling of a hierarchical model of hybrid vigor in RNA-seq experiments

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The Gibbs sample Gibbs steps Estimated heterosis probabilities GPU parallelism

## Thanks for coming.

► Slides and video will be available at http://will-landau.com/research.html. GPU-parallel Gibbs sampling of a hierarchical model of hybrid vigor in RNA-seq experiments

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