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         P2_Project_IA202410_MB1DC2ST3DH4JE5
         1. Libraries and functions
         Here we define the libraries and functions that will be used throughout the project.
          • fetch_data(): Returns the data from the MNIST dataset as a Pandas dataframe.
           • select_balanced_samples(): Select balanced data samples that are either grouped based on the samples per class when the method to be applied is 'random', or where data is clustered in a data frame and later processed into centroids whose distances are calculated and saved into an indexes that are used to access a group of rows from the original data source when the method to be applied is 'kmeans'. In both cases, a filtered dataframe is returned.
           • train_and_evaluate(): Trains a model and returns the accuracy score of the model.
           • plot_digits(): The function is used to create a visual representation of a set of images by creating a Matplotlib figure with a specific size (20 units tall). It then iterates through the images, displaying each one in a subplot. The images are reshaped to a 28x28 grid and displayed using a binary color map.
In [ ]: import pandas as pd
         import numpy as np
         from sklearn.cluster import KMeans
         from sklearn.metrics import pairwise_distances_argmin_min
         from sklearn.neural_network import MLPClassifier
         from sklearn.tree import DecisionTreeClassifier
         from sklearn.model_selection import train_test_split
         from sklearn.metrics import accuracy_score
         import matplotlib.pyplot as plt
         from typing import Literal
         MNIST_URL = 'https://raw.githubusercontent.com/sbussmann/kaggle-mnist/fd6de8baf8995ff26f441cd51c302f77bc7ec8c7/Data/train.csv'
         RANDOM\_SEED = 42
         np.random.seed(RANDOM_SEED) # set seed for reproducibility
         # Fetch MNIST data from GitHub
         def fetch_data() -> pd.DataFrame:
          return pd.read_csv(MNIST_URL)
         # Obtain n samples using the specified method
         def select_balanced_samples(df: pd.DataFrame, n: int, method: Literal['random', 'kmeans']) -> pd.DataFrame:
             samples_per_class = n // 10
             if method == 'random':
                return df.groupby('label', group_keys=False).apply(lambda x: x.sample(samples_per_class))
             elif method == 'kmeans':
                 indices = []
                 for label in range(10):
                     cluster_data = df[df['label'] == label]
                     kmeans = KMeans(n_clusters=samples_per_class, random_state=RANDOM_SEED, n_init=10)
                     kmeans.fit(cluster_data.drop('label', axis=1))
                     centroids = kmeans.cluster_centers_
                     closest, _ = pairwise_distances_argmin_min(centroids, cluster_data.drop('label', axis=1))
                     indices.extend(cluster_data.iloc[closest].index)
                 return df.loc[indices]
             else:
                 raise ValueError("Unknown method.")
         # Train the specified model and return the accuracy score on the test set
         def train_and_evaluate(model: MLPClassifier | DecisionTreeClassifier, X_train: pd.DataFrame, y_train: pd.Series, X_test: pd.DataFrame, y_test: pd.Series) -> float:
             model.fit(X_train, y_train)
             predictions = model.predict(X_test)
             return accuracy_score(y_test, predictions)
         # Plot the specified images
         def plot_digits(images: np.ndarray, title: str, images_per_row=10) -> None:
             plt.figure(figsize=(20, 2))
             for index, image in enumerate(images):
                 plt.subplot(1, images_per_row, index + 1)
                 plt.imshow(image.reshape(28, 28), cmap='binary')
                 plt.axis('off')
             plt.suptitle(title)
             plt.grid(True)
             plt.show()
         2. Fetch the data and generate the train and test sets
         We are defining a division of 80% of data that is going to be used for training.
In [ ]: mnist = fetch_data()
         # Split data into training and testing sets
         features = mnist.drop('label', axis=1)
         labels = mnist['label']
         X_train, X_test, y_train, y_test = train_test_split(features, labels, test_size=0.2, random_state=RANDOM_SEED)
         3. Define the classification models
         Once the training data is defined, we initialize the models together with a series of sample sizes that are going to be used for calculating which of the four multilayer perceptrons are more accurate. In this case, the values of 10, 50, 100 and 300 have been defined.
In [ ]: # Initialize models
         mlp = MLPClassifier(random_state=RANDOM_SEED)
         tree = DecisionTreeClassifier(random_state=RANDOM_SEED)
         # Test different sample sizes
         sample\_sizes = [10, 50, 100, 300]
         results = {'mlp_random': [], 'mlp_kmeans': [], 'tree_random': [], 'tree_kmeans': []}
         4. Train the classification models
         We iterate through the predefined sample sizes to create samples created at random and through the kmeans grouping to later be processed to be trained and evaluated. The results are saved into the results dictionary.
In [ ]: for size in sample_sizes:
             size = max(size, 10 * (size // 10))
             samples_random = select_balanced_samples(mnist, size, 'random')
             samples_kmeans = select_balanced_samples(mnist, size, 'kmeans')
             X_train_random, y_train_random = samples_random.drop('label', axis=1), samples_random['label']
             X_train_kmeans, y_train_kmeans = samples_kmeans.drop('label', axis=1), samples_kmeans['label']
             results['mlp_random'].append(train_and_evaluate(mlp, X_train_random, y_train_random, X_test, y_test))
             results['mlp_kmeans'].append(train_and_evaluate(mlp, X_train_kmeans, y_train_kmeans, X_test, y_test))
             results['tree_random'].append(train_and_evaluate(tree, X_train_random, y_train_random, X_test, y_test))
             results['tree_kmeans'].append(train_and_evaluate(tree, X_train_kmeans, y_train_kmeans, X_test, y_test))
         5. Graph the results
         Finally, we graph the results of the evaluation of the models.
In [ ]: # Plot results
         plt.figure(figsize=(10, 6))
         for key, value in results.items():
            plt.plot(sample_sizes, value, label=key)
         plt.xlabel('Sample Size')
         plt.ylabel('Accuracy')
         plt.title('Performance Comparison by Sample Size and Selection Method')
         plt.legend()
         plt.grid(True)
         plt.show()
         # Plot selected digits
         n_{digits} = 10
         digits_random = select_balanced_samples(mnist, n_digits, 'random').drop('label', axis=1).values
         plot_digits(digits_random, title='Randomly Selected Digits')
         digits_kmeans = select_balanced_samples(mnist, n_digits, 'kmeans').drop('label', axis=1).values
         plot_digits(digits_kmeans, title='Digits Selected with KMeans')
                                 Performance Comparison by Sample Size and Selection Method
                   — mlp_random
                      mlp_kmeans
                   tree_random
                  tree_kmeans
            0.5
                                                 100
                                                                 150
                                                                                 200
                                                                                                250
                                                                                                                 300
                                                              Sample Size
                                                                                               Randomly Selected Digits
                                                                                             Digits Selected with KMeans
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Semi-superivsed learning

Members:

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