

A Strategy-Proof Budget Feasible Online Mechanism for Crowdsensing with Time-Discounting Values

Jiapeng Xie, Shuo Yang, Fan Wu, Xiaofeng Gao, and Guihai Chen

Shanghai Key Laboratory of Scalable Computing and Systems

Shanghai Jiao Tong University, China

{xjpsjtu, wnmmy}@sjtu.edu.cn; {fwu, gao-xf, gchen}@cs.sjtu.edu.cn

Abstract—Crowdsensing has become increasingly popular due to its ability to collect a massive amount of real-time data with the help of many individual smartphone users. A crowdsensing platform can utilize the collected data to extract effective information and provide services to service requesters. Due to the rationality of smartphone users, designing an incentive mechanism to compensate the participants for their resources consumption is critical in attracting more participation. Offline incentive mechanism design has been widely studied in various crowdsensing applications, whereas the online scenario, is much more challenging due to the unavailability of future information when the platform has to make user selection decisions. In this paper, we investigate the problem of online crowdsensing by considering a critical property that the values of users contributions decrease as time goes by. The time-discounting property is common in inter-temporal choice scenarios but has not been carefully addressed in mechanism design perspective. To handle this problem, we propose a new method to select users based on a time-related threshold, and present a strategyproof framework where participants prefer to submit their true types, instead of manipulating the market by misreporting their private information. We consider two cases, one is that the total value is the summation of each participant's contributing value, the other is more general that the total value function is submodular. We name these two mechanisms TDM and TDMS. We prove that our two mechanisms can achieve computational efficiency, budget feasibility, strategy-proofness, and a constant competitive ratio. By comparing our mechanism TDM with two heuristic benchmarks, we show that our design achieves great performance in terms of the total obtained value.

I. INTRODUCTION

Mobile crowdsensing is a novel application paradigm that utilizes mobile devices to collect, analyze, and share their local information [14], [29], [46], [15], [42]. It usually consists of a service provider, service requesters, and mobile device users. The service provider (a.k.a., the crowdsensing platform), which usually resides in the cloud, recruits participants from mobile device users to upload their sensing data, and then provides services to service requesters based on the collected information. A wide variety of applications has emerged in recent years, including NoiseTube [33] and Ear-phone [40] for noise monitoring, SignalGuru [26] and CrowdAtlas [48] for traffic monitoring, and CrowdPark [50], Parknet [34] for finding on-street parking spots.

However, a well running crowdsensing application needs massive data contributed by the participants to ensure the service quality [47], [18]. Since participating in crowdsensing tasks requires the participants to devote resource consumptions

of their smartphones, participants are usually reluctant to share their sensing capabilities (e.g., [23], [10], [22]). Thus, it is necessary to design an incentive mechanism to compensate the participants. According to different settings of scenarios, two cases are often discussed, i.e., offline setting and online setting. Researches on incentive mechanism designs, such as [51], [27], are usually based on offline scenarios, where participants are present simultaneously while the online scenarios are more common in practice, where participants arrive and leave dynamically. Designing an incentive mechanism in online scenarios is much more complicated, due to the lack of future information. Besides, it brings challenges in the realization of strategy-proofness, since participants may misreport their arrival or departure time in order to gain higher benefits. Here, intuitively, strategy-proofness means that one can maximize her benefit by truthfully revealing her private information (e.g., arrival time, departure time, or sensing cost).

We note that most existing works on online mechanism design only consider flat values, i.e., the value of each participant's contributed data is fixed during her presence. However, in many time sensitive applications (e.g., real-time traffic or noise monitoring [9], [20], [52], [8]), the participants usually have time-discounting values, i.e., the value of each participant's contribution decreases as time goes by [2], [49]. The time-discounting property really complicates the mechanism design problem. For instance, it has been proved that no online algorithm can achieve a competitive ratio better than $\Omega(\log n / \log \log n)$ for discounted secretary problem [2]. The time-discounting property of values will bring much more difficulty, especially on the strategy-proofness. In the most of the incentive mechanisms designed for online crowdsensing, the payment to a selected participant is based on her contribution. If she can cheat her type, such as arrival time or cost, she may be selected at different time. If this time is earlier than the time with truly report information, the value of this participant calculated by the platform will be higher than the true value. For the purpose of more reward, the participant may have more incentives to bid mendaciously.

In this paper, we focus on the online scenario where a provider intends to select participants to perform sensing tasks and provide them with some rewards under a budget constraint. The objective of the problem is to maximize the total values of selected participants considering the time-discounting properties, while at the same time achieve budget

feasibility and strategy-proofness. Taking the budget constraint into account brings another challenge in designing a strategy-proof mechanism, since existing budget feasible mechanism design approaches(*e.g.*, [44], [6], [4], [7]) are not practical in scenarios where participants' values are time-discounting.

To address these challenges, we propose a budget feasible online incentive mechanism with time-discounting values. We first consider the case where the total value is the summation of each participant's value. We define the efficiency of a participant as her value divided by her cost. Since participants arrive dynamically, we take advantage of the efficiency information of those who have arrived (we call a sample set) to calculate a threshold, and use it to guide subsequent selections. The intuition of our design is to greedily choose participants with the highest efficiencies from the sample set, and calculate their average efficiency multiplying an increasing factor as a threshold. The increasing factor is used to prevent the participants from misreporting their arrival or departure time. We divide the total time into slots. At each time slot, we select participants with efficiencies higher than the threshold within the budget constraint, and then calculate their payments. The payment scheme is carefully designed to ensure strategy-proofness and individual rationality. We prove that our mechanism can achieve a constant competitive ratio compared with the optimal solution with full information. We next consider the case where the total value is a submodular function of the selected participants, which is a more general situation. We prove that the time and cost-truthfulness can still be guaranteed by the newly designed algorithms. The numerical results show that our proposed approach has superior performance to our benchmark mechanisms.

A. Key Contributions

The main contributions of this paper is listed as follows

- We design an online incentive mechanism for crowdsensing. In this process, participants arrive over time. Our mechanism is designed to take advantage of their efficiency to select them and give them a payment.
- As far as we know, we are the first to consider the time-discounting property of values. To address the potential new difficulty, we design a novel algorithm to calculate a time-related threshold to select participants and determine their payment.
- We think about two cases according to the value function. The value function in these two cases is additive and submodular, the latter is more general.

B. Paper Organization

The rest of the paper is organized as follows. We briefly review the related work in Section II. In Section III, We introduce the model of the budget feasible online mechanism problem with time-discounting values, and recall some important solution concepts. In Section IV, we present our design of a strategy-proof online mechanism where the value function is the summation of each participant's value. In Section V, we consider the case where the value function submodular.

In Section VI, we implement and evaluate our mechanism. Finally, we conclude this paper in Section VI.

II. RELATED WORKS

The problem of designing incentive mechanism for mobile crowdsensing has been extensively studied in recent years. Yang *et al.* [51] considered offline mechanism design problem based on stackelberg game, and proposed mechanisms for two different perspectives respectively: a user-centric model and a platform-centric model. Koutsopoulos [27] designed an incentive mechanism based on a reverse auction. In his design, when the cost of a participant is received, the mechanism calculates the participant's effort level and payment vector to achieve truthfulness, and minimizes the total payment with guaranteed service quality. Later, Zhao *et al.* [54] designed two online mechanisms, namely OMZ and OMG, that satisfied truthfulness and achieved constant competitiveness. Kumrai *et al.* [28] proposed a novel mechanism for participatory sensing based on the evolutionary algorithm that can maximize both the number of active participants and the sensing coverage. Singer [45] present a pricing mechanism for crowdsourcing. It uses a sample set to calculate the threshold, which is the lowest single price many workers may accept, with budget feasible. Peng *et al.* designed a quality based incentive mechanism and extend the well-known Expectation Maximization algorithm [39]. The innovation is to apply the classical Information Theory to measure the effective contribution of sensing data. J.S.Lee *et al.* designed a dynamic pricing incentive mechanism based on reverse auction and focused on minimizing and stabilizing the cost while preventing participants from dropping out of sensing tasks [31]. However, none of these researches took the time-discounting property into consideration.

There are few previous researches focusing on the property of time-discounting values [11], [38], [12]. Babaioff *et al.* [2] studied two extensions of the secretary problem, *i.e.*, the discounted secretary problem and weighted secretary problem. In discounted secretary problem, the benefit derived from selecting an item is its original value multiplied by a time-discounting factor. Wu *et al.* [49] designed a strategy-proof online mechanism with time-discounting values, and achieved a 2-competitive ratio. Unfortunately, these work cannot be easily applied to scenarios with budget constraint.

The budget feasible mechanism has been widely studied to address budget limited mechanism design problem [55], [3], [5], [17], [30], [32], [16]. Singer [44] first designed a budget feasible mechanism for scenarios where the value function is submodular. Chen *et al.* [6] further proposed a truthful budget feasible mechanism. It achieves a competitive ratio of larger than $\frac{1}{9}$, which is better than previously best result 233.83. Nevertheless, these work also failed to consider the time-discounting property.

Furthermore, there are some loosely related works on online mechanism design [35], [24], [13], *e.g.*, pricing and resource allocation in cloud computing [43], allocating tasks with temporal constraints [37], improving targeting to increase

total revenue [19], and dynamic resource bundling and VM provisioning in IaaS clouds [53].

In contrast to the previous works, we consider both the time discounting values and the budget limitation, and propose to design a budget feasible online mechanism that can guarantee strategy-proofness with a constant competitive ratio.

III. PRELIMINARIES

In this section, we present the model of our budget feasible online crowdsensing problem with time-discounting values and review some related solution concepts.

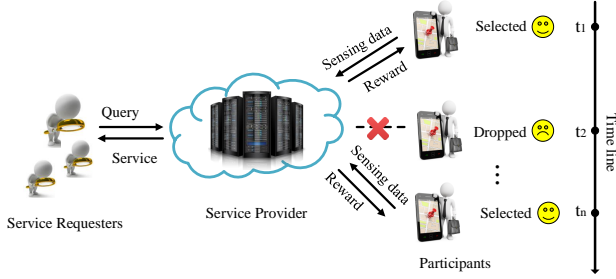


Fig. 1. A crowdsensing model

A. System Model

The crowdsensing model is shown in Fig. 1. We assume that there is a service provider, some service requesters and a set of participants $\mathbb{N} = \{1, 2, \dots, n\}$. The provider has a limited budget B to reward selected participants and intends to collect data and provide services to service requesters. For example, the service provider collects local traffic information from participants, performs data analysis process and builds a traffic heat map, which will be used to provide real-time road congestion information to drivers.

We mainly talk about two system models, one is the case where the value function is the summation of each participant's contributing value and the other model is more general where the value function is a submodular function. The submodular function maps a bid set or a participant set to a real positive number, *i.e.*, the total value.

In the case where the value of a participant has nothing to do others', the total is the summation of each participant's value. The type of each participant i is $\theta_i = (a_i, d_i, v_i, c_i)$, where a_i and d_i represent her arrival and departure time respectively, v_i denotes participant i 's value to the crowdsensing platform and c_i represents her cost or reserve price in performing the sensing task. Here, reserve price is the minimum payment that a participant is willing to receive. In other words, each selected participant should get a payment no less than her reserve price. We note that a_i , d_i and c_i are participant i 's private information that are unknown to the service provider unless being reported, while v_i is assumed to be i 's public information since participants' values can be known a prior or evaluated by the service provider [39], [21]. Upon participant i 's arrival, she will submit her bid $\hat{\theta}_i = (\hat{a}_i, \hat{d}_i, v_i, b_i)$ to the service provider. We note that since the participants are rational and selfish, they may cheat their

arrival time, departure time, or reserve prices for the purpose of earning more payment or improving the possibility to be selected [36], indicating that participant i 's bid may not be her true type. It is known that reporting earlier arrival or later departure can be prevented by heart-beat scheme [36], we focus on the scenario where each participant can only report an arrival time later than her true arrival time or a departure time earlier than her true departure time, *i.e.*, $\hat{a}_i \geq a_i, \hat{d}_i \leq d_i$. Participant i can also misreport her reserve price $b_i \neq c_i$ to manipulate the participant selection process.

The crowdsensing process is divided into T slots of equal lengths, *i.e.*, $\mathbb{T} = \{1, 2, \dots, T\}$. Upon a participant i 's arrival, the service provider will examine her bid and determine whether to select or not. Since participants arrive dynamically, the provider only knows the information of those arrived participants and has no prior knowledge of the bids of the subsequent arrivers. In the model of time-discounting values, the values of participants decrease sensitively over time. Specifically, when a participant i is selected at time t_i , her value equals v_i multiplying a discount factor. Following the settings in [41], the time-discounting factor in our paper is set to β^{-t} , *i.e.*, the value of participant i at time t_i is $v_i(t_i) = v_i \cdot \beta^{-t_i}$.

We denote the set of selected participants as \mathbb{S} . If participant i wins the auction, she will receive a payment p_i , having a utility of $u_i = p_i - c_i$; Otherwise, she will get zero utility, *i.e.*,

$$u_i = \begin{cases} p_i - c_i, & i \in \mathbb{S}, \\ 0, & \text{otherwise,} \end{cases} \quad (1)$$

In contrast to the participants who always want to maximize their own utilities, the provider expects to maximize the total obtained value $V = \sum_{i \in \mathbb{S}} v_i(t_i)$ under the budget constraint $\sum_{i \in \mathbb{S}} p_i \leq B$, where t_i means the time when participant i is selected. The objective of our mechanism is to maximize V .

Similarly, in the general case where the total value function is a submodular function, each participant has a type $\theta = (a, d, p, c)$, where a, d, c still represents the arrival time, departure time and her cost. Her bid is denoted as $\hat{\theta} = (\hat{a}, \hat{d}, p, \hat{c})$. The total value respected to a selected participant set \mathbb{S} is denoted as $f(\mathbb{S})$. Our objective is to select a set \mathbb{S} to maximize the function $f(\mathbb{S})$. More details are in section V.

B. Solution Concepts

These are several important solution concepts used in this paper from algorithmic game theory [36].

Definition 1 (Dominant Strategy). A participant i 's strategy s_i is called her dominant strategy, if for any strategy $s'_i \neq s_i$ and any other player's strategy profile s_{-i} , we have $u_i(s_i, s_{-i}) \geq u_i(s'_i, s_{-i})$.

Definition 2 (Truthfulness). An online mechanism is truthful if and only if it is the dominant strategy for every participant $i \in \mathbb{N}$ to report her true type.

Definition 3 (Individual-Rationality). A mechanism is individual rational if and only if $u_i \geq 0$ for all participant $i \in \mathbb{N}$.

Definition 4 (Strategy-Proof Direct Revelation Mechanism). A direct revelation mechanism is strategy-proof, when it satisfies both truthfulness and individual-rationality.

Our objective is to design a strategy-proof and budget feasible online mechanism with time-discounting values.

IV. MECHANISM DESIGN

In this section, we propose an online mechanism, which is named as TDM, satisfying the following properties:

- **Computational Efficiency:** Each step of the mechanism should be computed in polynomial time.
- **Strategy-Proofness:** Since individual-rationality can trivially achieved, we only need to guarantee truthfulness, i.e., each participant has no incentive to misreport her type at any circumstance.
- **Competitive Efficiency:** We define the competitive ratio as the ratio between the expected total value gained in our mechanism and the optimal value where this provider has full information of all participants [54]. We will prove our mechanism can achieve a constant competitive ratio. In our proof, we ignore the effect of time-discounting property because it will only change the constant coefficient.

A. Threshold Calculation

In determining whether to select a participant, the service provider compares her efficiency with a threshold, which is calculated at the beginning of each stage. We will show how to define the stage in the next subsection. In this subsection, we present the algorithm to calculate the threshold, which is treated as a benchmark to guide participant selection in the current stage. Since our objective is to maximize the total value under a limited budget, a natural idea is to give higher priorities to those participants with higher efficiency for the better use of the budget. We present the procedure to calculate

the threshold in Algorithm 1, which will be carried out at the beginning of each stage.

Algorithm 1: GetThreshold: $GetThreshold(B, T_k, \mathbb{S}')$

Input : Budget B , bid profile of sample set \mathbb{S}' , current stage T_k

Output : Threshold ρ

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1  $\mathbb{D}^{T_k} \leftarrow \emptyset$ ;
2 while  $\mathbb{D}^{T_k} \neq \mathbb{S}'$  do
3    $i \leftarrow \underset{i \in \mathbb{S}' \setminus \mathbb{D}^{T_k}}{\operatorname{argmax}} \frac{v_i}{b_i}$ ;
4   if  $b_i \leq \frac{\sum_{j \in \mathbb{D}^{T_k}} \frac{2U}{L} v_j}{v_j + v_i} B$  then
5      $\mathbb{D}^{T_k} = \mathbb{D}^{T_k} \cup \{i\}$ ;
6   else break;
7 return  $\frac{1}{\lambda} \frac{\sum_{i \in \mathbb{D}^{T_k}} \frac{v_i}{b_i}}{\sum_{i \in \mathbb{D}^{T_k}} \frac{v_i}{b_i}} \left(\frac{U}{L}\right)^{l-k}$ ;
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In the algorithm, B means the capped budget in this stage, \mathbb{S}' means the available sample set and T_k is the beginning time of this stage. We assume each participant has a bounded efficiency between L and U , i.e., $L \leq \frac{v_i}{b_i} \leq U, \forall i \in \mathbb{N}$. This procedure selects the participant with the highest efficiency into \mathbb{D}^{T_k} in proper order under the constraint $b_i \leq \frac{\sum_{j \in \mathbb{D}^{T_k}} \frac{2U}{L} v_j}{v_j + v_i} B$. We take the average efficiency of participants in \mathbb{D}^{T_k} multiplied by a stage related factor as the threshold, i.e., $\frac{1}{\lambda} \frac{\sum_{i \in \mathbb{D}^{T_k}} \frac{v_i}{b_i}}{\sum_{i \in \mathbb{D}^{T_k}} \frac{v_i}{b_i}} \left(\frac{U}{L}\right)^{l-k}$, where λ is a system parameter and l is the total number of stages.

The following results will help us to evaluate the total value of participants selected by this criterion when we estimate the competitive ratio.

Lemma 1. If there is a sequence of participants sorted by efficiency, i.e.,

$$\frac{v_1}{b_1} \geq \frac{v_2}{b_2} \geq \dots \geq \frac{v_m}{b_m}$$

and a budget B , then for any two participant x and y , if

$$\frac{v_x}{b_x} \geq \frac{v_y}{b_y} \text{ and } b_y \leq \frac{\sum_{j < y} \frac{2U}{L} v_j}{v_j + v_y} B, \text{ we have}$$

$$b_x \leq \frac{\sum_{j < x} \frac{2U}{L} v_j}{v_j + v_x} B. \quad (2)$$

Proof. Since $\frac{v_x}{b_x} \geq \frac{v_y}{b_y}$, it means $b_x \leq \frac{v_x}{v_y} b_y$. Thus, we have:

$$\begin{aligned}
b_x &\leq \frac{v_x}{v_y} b_y \leq \frac{v_x}{v_y} \frac{\sum_{j < y} \frac{2U}{L} v_j}{v_j + v_y} B \\
&\leq \frac{\sum_{j < y} \frac{2U}{L} v_j}{v_j + v_y} B \\
&\leq \frac{\sum_{j < x} \frac{2U}{L} v_j}{v_j + v_x} B
\end{aligned}$$

□

From this lemma, we can see that in Algorithm 1, if the loop is broken at some i , we do not need to consider another

TABLE I
NOTATIONS

Symbol	Description
$\mathbb{N} = 1, 2, \dots, n$	The participant set
B	The total budget
θ_i	Type of participant i
a_i	arrival time of participant i
d_i	departure time of participant i
v_i	value of participant i
c_i	cost of participant i
$\hat{\theta}_i$	bid of participant i
$\mathbb{T} = \{1, 2, \dots, T\}$	the time slot set
β	time-discounting factor
p_i	payment of participant i
\mathbb{S}	selected participant set
V	The total value
L, U	lower bound and upper bound of efficiency
ρ	efficiency threshold
V	The total value
λ	a system parameter
T_i	time stage
f	submodular value function

participant j whose efficiency is smaller than i , since from $\frac{v_i}{b_i} > \frac{v_j}{b_j}$, we can infer that $b_j > \frac{2U}{L} \frac{v_j}{v_i + v_j} B$.

Theorem 1. Assume that there is a sequence of participants and a total budget B , sorted by their efficiency, i.e., $\frac{v_1}{b_1} \geq \frac{v_2}{b_2} \geq \dots \geq \frac{v_r}{b_r}$, where the index r satisfies $\sum_{i \leq r} b_i \leq B$ but $\sum_{i \leq r+1} b_i > B$ (changing their order number will not affect our result). Let m denote the last participant satisfies $b_m \leq \frac{2U}{L} \frac{v_m}{v_j + v_m} B$. We say

$$\sum_{i=1}^m b_i > \sum_{i=m+1}^r b_i.$$

Proof. According to lemma 1, for $i \in \{1, 2, \dots, m-1\}$, participant i will also satisfy $b_i \leq \frac{2U}{L} \frac{v_i}{v_j + v_i} B$ and for $i \in \{m+1, m+2, \dots, r\}$, participant i will not satisfy this property. For the purpose of contraction, we assume that $\sum_{i=1}^m b_i \leq \sum_{i=m+1}^r b_i$. Since $b_i > \frac{2U}{L} \frac{v_i}{v_j + v_i} B$, when $i > m$,

$$\begin{aligned} \sum_{i=m+1}^r b_i &> \sum_{i=m+1}^r \frac{2U}{L} \frac{v_i}{v_j + v_i} B \\ &> \sum_{i=m+1}^r \frac{2U}{L} \frac{v_i}{\sum_{j=1}^m U b_j + \sum_{j=m+1}^r U b_j} B \\ &> \sum_{i=m+1}^r \frac{2U}{L} \frac{v_i}{\sum_{j=m+1}^r U b_j + \sum_{j=m+1}^r U b_j} B \\ &> \sum_{i=m+1}^r \frac{2U}{L} \cdot L \cdot \frac{b_i}{\sum_{j=m+1}^r U b_j + \sum_{j=m+1}^r U b_j} B = B. \end{aligned}$$

We have a contradiction. \square

Corollary 1. Using the same notation in Theorem 1, we say

$$\sum_{i=1}^m v_i > \frac{L}{U+L} \sum_{i=1}^r v_i.$$

Proof. Since $\sum_{i=1}^m b_i > \sum_{i=m+1}^r b_i$, then

$$\sum_{i=m+1}^r v_i \leq U \sum_{i=m+1}^r b_i \leq U \sum_{i=1}^m b_i \leq \frac{U}{L} \sum_{i=1}^m v_i.$$

So $\sum_{i=1}^r v_i = \sum_{i=1}^m v_i + \sum_{i=m+1}^r v_i \leq (1 + \frac{U}{L}) \sum_{i=1}^m v_i$, i.e., $\sum_{i=1}^m v_i > \frac{L}{U+L} \sum_{i=1}^r v_i$. \square

B. Participant Selection and Payment Determination

Having presented a method to calculate the threshold, we now use it to guide participant selection in this subsection. First, we compute the 2^i quantile, given the distribution of the arrival time of participants [45]. We denote T_k as the moment before which participants arrive with the probability 2^{-k} . Then, we get a set $\{T_1, \dots, T_l\}$. Based on this set, we divide the time slots into several stages, where each stage begins at T_i and ends at T_{i-1} . At each T_i , we calculate the threshold to guide the participant selection in this stage. We present our algorithm in Algorithm 2 to elaborate the processes of participant selection and payment calculation.

Algorithm 2: Participant Selection&Payment Calculation

Input : Budget B , set $\{T_1, \dots, T_l\}$

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1  $t \leftarrow 1, \rho \leftarrow \varepsilon, x \leftarrow l;$ 
2  $B' \leftarrow \frac{1}{2}B, \mathbb{S} \leftarrow \emptyset, \mathbb{S}' \leftarrow \emptyset, \mathbb{A} \leftarrow \emptyset;$ 
3 for  $t = 1$  to  $T$  do
4   if some participant  $i$  arrives then
5      $\mathbb{A} \leftarrow \mathbb{A} \cup \{i\};$ 
6   foreach participant  $i$  in  $\mathbb{A}$  do
7     if  $\frac{v_i(t)}{b_i} \geq \rho$  and  $\frac{v_i(t)}{\rho} \leq B' - \sum_{j \in \mathbb{S}} p_j$  then
8        $p_i \leftarrow \frac{v_i(t)}{\rho};$ 
9        $\mathbb{S} \leftarrow \mathbb{S} \cup \{i\};$ 
10   $\mathbb{A} \leftarrow \mathbb{A} \setminus \mathbb{S};$ 
11  Remove all participants that depart in  $t$  from  $\mathbb{A}$  and add them to  $\mathbb{S}'$ ;
12  if  $t = T_x$  then
13     $\rho \leftarrow \text{GetThreshold}(B', T_x, \mathbb{S}');$ 
14     $x \leftarrow x - 1, B' \leftarrow 2B';$ 

```

The algorithm iterates from $t = 1$ to $t = T$. At each time t , it adds all newly arrived participants to \mathbb{A} , where \mathbb{A} represents the participants who have arrived and not been selected or left the auction. If participant i has an efficiency $\frac{v_i(t)}{b_i} \geq \rho$ at that time and $\frac{v_i(t)}{\rho} \leq B' - \sum_{j \in \mathbb{S}} p_j$, she will win the auction and be compensated with payment p_i corresponding to her value at that time. Otherwise, she will be dropped and wait to be selected next time until her departure time.

If a participant has won the auction at some time, she will not be considered later on. For the purpose of truthfulness, we remove all departed participants from \mathbb{A} and add them to \mathbb{S}' which is the sample set. At the beginning of next stage T_i , the threshold and the remaining budget will be updated.

C. Mechanism Analysis

In this subsection, we analyze our proposed mechanism.

Theorem 2. The mechanism is computationally efficient.

Proof. In each time slot t , for each participant who arrives at this time, it takes up to $O(n)$ to decide whether to select her. So the total time cost in each time slot is bounded by $O(n^2)$. It costs at most $O(n \log n)$ to calculate the threshold. Thus, the time complexity of this mechanism is $O(Tn^2)$. \square

Theorem 3. The mechanism is budget feasible.

Proof. Since the total payment of each stage never exhaust the allocated budget, we can see that the total payment will not exceed the total budget. \square

Theorem 4. The mechanism is time-truthful.

Proof. A mechanism is time-truthful if participants cannot obtain higher utilities by simply misreporting their arrival or departure time [54]. We prove that for participant i , proposing her true arrival and departure time is a dominant strategy. Recall that each participant has a type (a_i, d_i, v_i, c_i) and a bid $(\hat{a}_i, \hat{d}_i, v_i, b_i)$, $\hat{a}_i \geq a_i, \hat{d}_i \leq d_i$. We fix the bids of all but

participant i . If she proposes her true type, we consider two cases.

Case 1: She can win the auction at time t which belongs to stage $[T_a, T_{a-1}]$. If $\hat{a}_i < t$, since she cannot win the auction until t , she won't be paid more. If $\hat{a}_i > t$, we assume she will win the auction at time \hat{t} which belongs to the stage $[T_b, T_{b-1}]$. Let ρ_a and ρ_b be the threshold of these two stages respectively, i.e., $\rho_a = \text{GetThreshold}(B_a, T_a, S_a)$ and $\rho_b = \text{GetThreshold}(B_b, T_b, S_b)$. The set \mathbb{D} in Algorithm 1 is denoted as \mathbb{D}^{T_a} and \mathbb{D}^{T_b} respectively. So $\rho_a = \frac{1}{\lambda} \frac{\sum_{i \in \mathbb{D}^{T_a}} v_i}{\sum_{i \in \mathbb{D}^{T_a}} b_i} \left(\frac{U}{L}\right)^{l-a}$ and $\rho_b = \frac{1}{\lambda} \frac{\sum_{i \in \mathbb{D}^{T_b}} v_i}{\sum_{i \in \mathbb{D}^{T_b}} b_i} \left(\frac{U}{L}\right)^{l-b}$. The payments calculated in these two time slots are $p_a = \frac{v_i(t)}{\rho_a}$ and $p_b = \frac{v_i(\hat{t})}{\rho_b}$ respectively. So we have

$$\frac{p_a}{p_b} = \frac{v_i(t)}{v_i(\hat{t})} \frac{\rho_b}{\rho_a} = \frac{v_i \cdot \beta^{-t}}{v_i \cdot \beta^{-\hat{t}}} \frac{\frac{1}{\lambda} \frac{\sum_{i \in \mathbb{D}^{T_b}} v_i}{\sum_{i \in \mathbb{D}^{T_b}} b_i} \left(\frac{U}{L}\right)^{l-b}}{\frac{1}{\lambda} \frac{\sum_{i \in \mathbb{D}^{T_a}} v_i}{\sum_{i \in \mathbb{D}^{T_a}} b_i} \left(\frac{U}{L}\right)^{l-a}}. \quad (3)$$

We assume that every participant has a bounded efficiency, i.e., $L \leq \frac{v_i}{b_i} \leq U$, then we have

$$\frac{p_a}{p_b} \geq \beta^{(\hat{t}-t)} \frac{L}{U} \cdot \left(\frac{U}{L}\right)^{a-b} > 1. \quad (4)$$

The above inequality is satisfied because if $T_a = T_b$, then $\rho_a = \rho_b$. It can be seen that $p_a \geq p_b$, since the time-discounting value reduces her payment. If $T_a < T_b$, the inequality is satisfied as well. This indicates that the participant will get a lower payment and she will have no incentive to cheat her arrival time. The analysis on the departure time is similar.

Case 2: If this participant can not win this auction, she will not satisfy the condition at any time within her present time. She has no incentive to misreport her arrival or departure time since she won't get more payment. \square

Theorem 5. *The mechanism is cost-truthful.*

Proof. A mechanism is cost-truthful if participants cannot obtain higher utilities by simply misreporting their reserve prices [54]. Different from previous works on the truthfulness problem which claim that an online auction is cost-truthful only if it is bid-independent, the case in our mechanism is more complicated because of the time discounting property. We consider the following two cases.

Case 1: Participant i can win the auction at time slot t_a which is in the stage $[T_a, T_{a-1}]$. If she declares a smaller bid b_i and wins the auction earlier, say at time t_b , which is in stage $[T_b, T_{b-1}]$, it would be impossible. We note that if some participant wins at t_a , she cannot win the auction before that time. We notice that in time slot t_a , $\frac{v_i(t_a)}{c_i} \geq \rho_a$, so according to the proof in Theorem 4, $\frac{v_i(t_b)}{c_i} \geq \rho_b$ still holds. But she was not allocated at that time t_b , the only reason is that her payment exceeds the remaining budget. So this participant will not gain more payment at t_b as well. Obviously, declaring a larger bid won't help her gain more.

Case 2: Participant i loses this auction. This means at any time t , $\frac{v_i(t)}{c_i} \leq \rho$, or $\frac{v_i(t)}{c_i} \geq \rho$ but $\frac{v_i(t)}{\rho} \geq B' - \sum_{j \in S} p_j$. The second condition means at that time, the payment calculated in our algorithm will exhaust the remaining budget. No matter how the participant changes her bid, this block always exists. If she declares a larger bid, the inequations still hold. If she declares a smaller bid b_i and gets a payment $\frac{v_i(t)}{\rho}$. Since $\frac{v_i(t)}{c_i} \leq \rho$, this new payment will be less than her true cost c_i and her utility will be less than zero. A strategic participant has no incentive to misreport in this case. \square

Theorem 6. *The mechanism is time-truthful and cost-truthful.*

Proof. We prove that participants cannot obtain higher utilities by simultaneously misreporting their arrival or departure time and their reserve prices. We consider the case that a participant may misreport her present time and cost at the same time. It should be noted that the payment has no *direct* relationship with the bid b_i . If this participant can win the auction at t and she can be selected after time t by misreporting her present time, as we show in Theorem 4, the payment decreases. If she can be selected at a time before t , it is equivalent to the case in Theorem 5. If the participant can't win the auction at any time, she has no incentive to misreport her bid b_i within the present time $[a_i, d_i]$. \square

The above theorems indicate the truthfulness of our mechanism. To quantify the performance of the mechanism, we compare the total value with the optimum.

Theorem 7. *The mechanism has a constant competitive ratio. In a large-scale crowdsensing system, this competitive ratio approaches to $\left(\frac{U}{L}\right)^{2-2l} \frac{U}{16(U+L)} (1 - \frac{1}{e})$.*

Proof. Here, a large-scale crowdsensing system means that there are a large number of participants and a single participant cannot affect the market significantly [1]. Let S' be the sample set at time T_1 and run the *GetThreshold* procedure on this set, we get a threshold ρ . Khuller *et al.* [25] proposed a *modified greedy algorithm*, which has a constant competitive ratio $\frac{1}{2}(1 - \frac{1}{e})$.

Algorithm 3: Modified greedy algorithm

Input : Budget B , the participant set $\mathbb{P} = \{p_1, p_2, \dots, p_n\}$
Output : Selected Participants

```

1  $\mathbb{S} \rightarrow \emptyset, C \rightarrow 0, \mathbb{U} \rightarrow \mathbb{S};$ 
2 while  $\mathbb{U} \neq \emptyset$  do
3   select  $p_i \in \mathbb{U}$  that maximizes  $\frac{v_i}{c_i}$ ;
4   if  $C + c_i \leq B$  then
5      $\mathbb{S} \rightarrow \mathbb{S} \cup p_i;$ 
6      $C \rightarrow C + c_i;$ 
7    $\mathbb{U} \rightarrow \mathbb{U} \setminus \{p_i\};$ 
8 Select a participant  $p^*$  that maximizes  $v^*$  over  $\mathbb{P}$ ;
9 if  $V(\mathbb{S}) \geq v^*$ , output  $\mathbb{S}$ , otherwise, output  $\{p^*\};$ 
```

We assume the output of this algorithm on S' is v_1, v_2, \dots, v_r and $\sum_{i \leq r} b_r \leq B'$ but $\sum_{i \leq r+1} b_r > B'$. B'

equals $\frac{B}{2}$ here. In the last step in *modified greedy algorithm*, we choose the participant with the highest value or those selected by the well-known greedy strategy. But when the number of participants are very large, the output will have a high probability to be the latter. So the expected output of this algorithm approaches to the greedy output when n is large enough. Our analysis is based on this fact that the bid of each participant is extremely tiny compared with the total budget. Assume that a bid satisfies $b_i \leq \epsilon B$. So $\sum_{i \leq r} b_i \geq B' - b_{r+1} \geq B' - \epsilon B = (\frac{1}{2} - \epsilon)B$. Let \mathbb{S}_{OPT} be the optimal set when the provider has full information of the participants, \mathbb{S}^1 be the set of participants who arrive and departure before time T_1 in \mathbb{S}_{OPT} , and \mathbb{S}^2 be the set of participants who arrive and departure in the last stage in \mathbb{S}_{OPT} . When participants arrive uniformly (this assumption will only affect the constant coefficient), it is easy to show the expected value in this set is $E[V(\mathbb{S}^1)] = \frac{1}{4}E[V(\mathbb{S}_{OPT})]$. So the ratio of *modified greedy algorithm* to the optimal solution \mathbb{S}_{OPT} is at least a constant.

Now, we compare the value of the participants selected in the last stage by our mechanism with the value of those selected by the *modified greedy algorithm*. If this ratio is a constant, the competitive ratio of our algorithm will be a constant.

We consider the participants who fail to be selected. We set the parameter λ to satisfy this condition: $\frac{(\frac{U}{L})^{l-1}}{\lambda} \leq \frac{1}{2}$. Then we claim that with a high probability, there will be at least one participant has an efficiency larger than ρ , i.e., $\frac{v_i(t_i)}{b_i} \geq \rho$ but $\frac{v_i(t_i)}{\rho} + \sum_j p_j > B$. The threshold in this stage is ρ , which is smaller than $\frac{U}{2}$ with a selection of the parameter λ . Denote P_i as the probability of the participant i having an efficiency higher than ρ . So for any number k of participants, there will be at least one participant having the efficiency larger than ρ with a probability $P = 1 - \prod_{i=1}^k P_i$, which tends to be 1 when k is large. Based on this, our expected total value approaches to the total value estimated below. For this participant i :

$$\begin{aligned} v_i(t_i) &\geq (B - \sum_j p_j) \rho \\ \Rightarrow v_i &\geq (B - \sum_j p_j) \rho \end{aligned}$$

Since $v_i \leq Ub_i \leq U\epsilon B$, we have $(B - \sum_j p_j) \rho \leq U\epsilon B$, i.e., $\sum_j p_j \geq (1 - \frac{U\epsilon}{\rho})B$. If we can choose an appropriate parameter λ s.t. $1 - \frac{U\epsilon}{\rho} > 0$, the total payment will be at least a constant fraction of the total budget B . Then, we have:

$$\begin{aligned} \sum_{i \in \mathbb{S}} v_i &\geq \sum_{i \in \mathbb{S}} \rho_i \cdot p_i \\ &\geq \sum_{i \in \mathbb{S}} \left(\frac{U}{L}\right)^{-l} \rho \cdot p_i \\ &\geq \frac{v_1 + \dots + v_m}{\lambda B} \left(\frac{U}{L}\right)^{1-l} \sum_{i \in \mathbb{S}} p_i, \end{aligned} \quad (5)$$

where ρ_i denotes the threshold when participant i is selected.

We can get

$$\frac{\sum_{i \in \mathbb{S}} v_i}{v_1 + \dots + v_m} > \frac{(1 - \frac{U\epsilon}{\rho})}{\lambda} \left(\frac{U}{L}\right)^{1-l} \quad (6)$$

The requirement for λ is:

$$U\epsilon < \frac{v_1 + \dots + v_m}{b_1 + \dots + b_m} \left(\frac{U}{L}\right)^{l-1},$$

i.e., $\lambda < \frac{v_1 + \dots + v_m}{b_1 + \dots + b_m} \left(\frac{U}{L}\right)^{l-1} \frac{1}{U\epsilon}$. It's noticed that $\frac{v_1 + \dots + v_m}{b_1 + \dots + b_m} \geq L$, so we can relax our restricted condition to $\lambda < \frac{L(\frac{U}{L})^{l-1}}{U\epsilon}$, i.e., $\lambda \leq \frac{(\frac{U}{L})^{l-2}}{\epsilon}$.

Based on the analysis above and the *Corollary 1*, the expected competitive ratio is at least

$$P \frac{L}{8(U+L)} \left(1 - \frac{1}{e}\right) \frac{(1 - \frac{U\epsilon}{\rho})}{\lambda} \left(\frac{U}{L}\right)^{1-l}. \quad (7)$$

We note that although ρ is a variable, it is bounded because of the bounded efficiency. So we can take the lower bound to be the competitive ratio. The calculation process is omitted here. When ϵ and P approach to 0 and 1 respectively, the competitive ratio is:

$$\frac{L}{8\lambda(U+L)} \left(1 - \frac{1}{e}\right) \left(\frac{U}{L}\right)^{1-l}. \quad (8)$$

The restriction condition on the parameter λ is:

$$2 \left(\frac{U}{L}\right)^{l-1} \leq \lambda < \frac{1}{\epsilon} \left(\frac{U}{L}\right)^{l-2}. \quad (9)$$

When ϵ is sufficiently small, we can always find such a parameter λ equals $2 \left(\frac{U}{L}\right)^{l-1}$. Then the expected competitive ratio is:

$$\left(\frac{U}{L}\right)^{2-2l} \frac{U}{16(U+L)} \left(1 - \frac{1}{e}\right). \quad (10)$$

□

V. MECHANISM WITH MONOTONE SUBMODULAR VALUE FUNCTION

In this section, we propose an online mechanism, which is named as TDMS, for the general model.

A. System Model

The general model is similar with the model we have presented in section III. However the task is divided into some sub-tasks and the bid of each participant includes the set of sub-tasks she can finish. The bid of participant i is $\theta_i = (a_i, d_i, p_i, c_i)$, where we use the same notation p_i to represent the sub-task set of participant p_i for brevity.

B. Mechanism Design

In last section, we propose an incentive mechanism for online crowdsensing with time-discounting values, specifically the total obtained value is linear summation of value contributed by each participant, *i.e.*,

$$V = \sum_{i \in \mathbb{S}} v_i(t_i) \quad (11)$$

However in many scenarios [54], the value of participants to the platform is $f(\mathbb{S})$, where f is a monotone submodular function and \mathbb{S} is the selected participants set. Particularly, we have solved the case where the value function $f(\mathbb{S}) = \sum_{i \in \mathbb{S}} v_i(t_i)$. Here we give the definition of monotone submodular function.

Definition 5 (Monotone Submodular Function). *A function $f : 2^{[n]} \rightarrow \mathbb{R}$ is submodular if and only if:*

$$f(\mathbb{A} \cup \{i\}) - f(\mathbb{A}) \geq f(\mathbb{B} \cup \{i\}) - f(\mathbb{B}), \forall \mathbb{A} \subseteq \mathbb{B}$$

In existing works focused on submodular function maximization in the realm of incentive mechanism design for crowdsensing, the marginal value contributed by a participant is related to the order she is selected. Besides, the total value is only decided by the tasks of the selected participants. However in this paper, considering the time-discounting property, the value function is a bit more complicated. We still use the notation f to denote the value function without considering time-discounting value. When a participant i is selected at time t_i , her marginal contribution given a subset \mathbb{S} is $f_{i|\mathbb{S}} = (f(\mathbb{S} \cup \{i\}) - f(\mathbb{S})) \times \beta^{-t_i}$. Assume the selected participant set is $\{i_1, i_2, \dots, i_n\}$ and their selected time is $t_{i_1}, t_{i_2}, \dots, t_{i_n}$ respectively. So when select the first participant i_1 , her real contribution value is $f_{t_{i_1}}(\{i_1\}) = f(\{i_1\}) \times \beta^{-t_{i_1}}$. The value contributed by the secondly selected participant without consider time-discounting property is $f(\{i_1, i_2\}) - f(\{i_1\})$ and her true contribution should be discounted by timing $\beta^{t_{i_2}}$. Thus, the total value contributed these two participants is $f_{t_{i_1}, t_{i_2}}(\{i_1, i_2\}) = f_{t_{i_1}}(\{i_1\}) \times \beta^{-t_{i_1}} + [f(\{i_1, i_2\}) - f(\{i_1\})] \times \beta^{-t_{i_1}}$. We use \tilde{f} to substitute f when considering time-discounting property. So, the total value contributed by all these n participants are

$$\begin{aligned} \tilde{f}(\{i_1, i_2, \dots, i_n\}) &= f_{t_{i_1}, t_{i_2}, \dots, t_{i_n}}(\{i_1, i_2, \dots, i_n\}) \\ &= f_{t_{i_1}}(\{i_1\}) \times \beta^{-t_{i_1}} + [f(\{i_1, i_2\}) - f(\{i_1\})] \times \beta^{-t_{i_1}} \\ &\quad + \dots + [f(\{i_1, i_2, \dots, i_n\}) - f(\{i_1, i_2, \dots, i_{n-1}\})] \times \beta^{-t_{i_n}} \end{aligned} \quad (12)$$

Theorem 8. *The new total value function \tilde{f} with time-discounting value is monotone submodular.*

Proof. We can prove this according to the definition of submodular function.

Let \mathbb{A} and \mathbb{B} are two arbitrary subsets and $\mathbb{A} \subseteq \mathbb{B}$. Then,

$$\begin{aligned} &\tilde{f}(\mathbb{A} \cup \{i\}) - \tilde{f}(\mathbb{A}) \\ &= \tilde{f}(\mathbb{A}) + [f(\mathbb{A} \cup \{i\}) - f(\mathbb{A})] \times \beta^{-t_i} - \tilde{f}(\mathbb{A}) \\ &= [f(\mathbb{A} \cup \{i\}) - f(\mathbb{A})] \times \beta^{-t_i}. \end{aligned}$$

Similarly,

$$\begin{aligned} &\tilde{f}(\mathbb{B} \cup \{i\}) - \tilde{f}(\mathbb{B}) \\ &= \tilde{f}(\mathbb{B}) + [f(\mathbb{B} \cup \{i\}) - f(\mathbb{B})] \times \beta^{-t_i} - \tilde{f}(\mathbb{B}) \\ &= [f(\mathbb{B} \cup \{i\}) - f(\mathbb{B})] \times \beta^{-t_i}. \end{aligned}$$

Since f is a submodular function, then we have $f(\mathbb{A} \cup \{i\}) - f(\mathbb{A}) \geq f(\mathbb{B} \cup \{i\}) - f(\mathbb{B})$. \square

We denote participant i 's marginal contribution given a subset \mathbb{A} as $\tilde{f}_{t_i}^i(\mathbb{A}) = [f(\mathbb{A} \cup \{i\}) - f(\mathbb{A})] \times \beta^{-t_i}$. Next we modify the procedure to calculate the threshold when the value function is submodular. Recall that we assume $L \leq \frac{v}{b} \leq U$ before, here we make a reasonable assumption that $L \leq \frac{f^i(\emptyset)}{b_i} \leq U$. Then we also can infer that $L \leq \frac{f^i(\mathbb{A})}{b_i} \leq U$ for all set \mathbb{A} .

Algorithm 4: ModifiedGetThreshold

Input : Budget B , bid profile of sample set \mathbb{S}' , current stage T_k

Output : Threshold ρ

```

1  $\mathbb{D}^{T_k} \leftarrow \emptyset$ ;
2 while  $\mathbb{D}^{T_k} \neq \mathbb{S}'$  do
3    $i \leftarrow \underset{i \in \mathbb{S}' \setminus \mathbb{D}^{T_k}}{\operatorname{argmax}} \frac{f^i(\mathbb{D}^{T_k})}{b_i}$ ;
4   if  $b_i \leq \frac{f^i(\mathbb{D}^{T_k})}{f(\mathbb{D}^{T_k} \cup \{i\})} B$  then
5      $\mathbb{D}^{T_k} = \mathbb{D}^{T_k} \cup \{i\}$ ;
6   else break;
7 return  $\frac{1}{\lambda} \frac{f(\mathbb{D}^{T_k})}{\sum_{i \in \mathbb{D}^{T_k}} \frac{f^i(\mathbb{D}^{T_k})}{b_i}} \left(\frac{U}{L}\right)^{t-k}$ ;
```

Most parameters have been explained after algorithm 1, so we just make some supplements. Line 3 in the procedure is to calculate the efficiency, which is the ratio of the marginal value and her cost. As we talked before, everytime we add the participant with the highest efficiency into the set.

Next we propose the participant selection algorithm as before. We should pay more attention to the truthfulness. Since the value function is submodular, the marginal distribution is related to a given subset. If the order of selection is changed, the marginal distribution will change as well. This is a new kind of opportunity for the participants to cheat her bids. Singer has ever studied a budget mechanism [44], where the value function is submodular. However it is used in offline scenario, we will give an online version.

C. Mechanism Analysis

Theorem 9. *The mechanism with submodular value function is computationally efficient and budget feasible.*

Proof. The proof is similar to the proof of theorem 2 and theorem 4. \square

Theorem 10. *The mechanism with submodular value function is time-truthful.*

Proof. We prove that a participant can not obtain higher utility by misreporting her arrival or departure time. Denote her true

Algorithm 5: Participant Selection&Payment Calculation

Input : Budget B , set $\{T_1, \dots, T_l\}$

```

1  $t \leftarrow 1, \rho \leftarrow \varepsilon, x \leftarrow l;$ 
2  $B' \leftarrow \frac{1}{2}B, \mathbb{S} \leftarrow \emptyset, \mathbb{S}' \leftarrow \emptyset, \mathbb{A} \leftarrow \emptyset;$ 
3 for  $t = 1$  to  $T$  do
4   if some participant  $i$  arrives then
5      $\mathbb{A} \leftarrow \mathbb{A} \cup \{i\};$ 
6   foreach Participant  $i \in \mathbb{A}$  do
7      $i^* \leftarrow \underset{i \in \mathbb{A}}{\operatorname{argmax}} \frac{\tilde{f}_t^i(\mathbb{S})}{b_i}$ 
8     if  $\frac{\tilde{f}_t^{i^*}(\mathbb{S})}{b_{i^*}} \geq \rho$  and  $\frac{\tilde{f}_t^{i^*}(\mathbb{S})}{\rho} \leq B' - \sum_{j \in \mathbb{S}} p_j$  then
9        $p_{i^*} \leftarrow \frac{\tilde{f}_t^{i^*}(\mathbb{S})}{\rho};$ 
10       $\mathbb{S} \leftarrow \mathbb{S} \cup \{i^*\};$ 
11    $\mathbb{A} \leftarrow \mathbb{A} \setminus \mathbb{S};$ 
12    $\mathbb{A}' \leftarrow \{i | i \in \mathbb{A} \text{ and } i \text{ departs at } t\}$ 
13   while  $\mathbb{A}' \neq \emptyset$  do
14      $i^* \leftarrow \underset{i \in \mathbb{A}'}{\operatorname{argmax}} \frac{\tilde{f}_t^{i^*}(\mathbb{S} \setminus \{i^*\})}{b_{i^*}}$ 
15     if  $b_{i^*} \leq \frac{\tilde{f}_t^{i^*}(\mathbb{S} \setminus \{i^*\})}{\rho} \leq B' - \sum_{j \in \mathbb{S}'} p_j + p_{i^*}$  and
         $\frac{\tilde{f}_t^{i^*}(\mathbb{S} \setminus \{i^*\})}{\rho} \geq p_{i^*}$  then
16        $p_{i^*} \leftarrow \frac{\tilde{f}_t^{i^*}(\mathbb{S} \setminus \{i^*\})}{\rho};$ 
17       if  $i^* \notin \mathbb{S}$  then
18          $\mathbb{S} \leftarrow \mathbb{S} \cup \{i^*\};$ 
19   Remove all participants that depart in  $t$  from  $\mathbb{A}$  and add them to  $\mathbb{S}'$ ;
20   if  $t = T_x$  then
21      $\rho \leftarrow \text{GetThreshold}(B', T_x, \mathbb{S}');$ 
22      $x \leftarrow x - 1, B' \leftarrow 2B';$ 
```

arrival and departure time is a_i, d_i and the misreporting time is \hat{a}_i and \hat{d}_i . Fix the bids of all participants but i , we consider two cases.

case 1: If she can win the auction at time t when she proposes her true type. If $\hat{a}_i \leq t$, she won't get more payment because she cannot win the until t . If $\hat{a}_i > t$, assume she will win the auction at \hat{t} . Assume t and \hat{t} belongs to stage $[T_a, T_{a-1}]$ and $[T_b, T_{b-1}]$ respectively and the corresponding threshold is $\rho_a = \text{GetThreshold}(B_a, T_a, \mathbb{S}'_a)$ and $\rho_b = \text{GetThreshold}(B_b, T_b, \mathbb{S}'_b)$. Assume the set \mathbb{D} in Algorithm 4 is \mathbb{D}^a and \mathbb{D}^b , so $\rho_a = \frac{1}{\lambda} \frac{f(\mathbb{D}^a)}{\sum_{i \in \mathbb{D}^a} b_i} \left(\frac{U}{L}\right)^{l-a}$ and $\rho_b = \frac{1}{\lambda} \frac{f(\mathbb{D}^b)}{\sum_{i \in \mathbb{D}^b} b_i} \left(\frac{U}{L}\right)^{l-b}$. Hence:

$$\begin{aligned}
\frac{P_a}{P_b} &= \frac{\tilde{f}_t^i(\mathbb{S}_a) \rho_b}{\tilde{f}_{t'}^i(\mathbb{S}_b) \rho_a} \\
&= \frac{(f(\mathbb{S}_a \cup \{i\}) - \mathbb{S}_a) \beta^{-t} \rho_b}{(f(\mathbb{S}_b \cup \{i\}) - \mathbb{S}_b) \beta^{-t'} \rho_a} \\
&= \frac{(f(\mathbb{S}_a \cup \{i\}) - \mathbb{S}_a) \beta^{-t} \frac{1}{\lambda} \frac{f(\mathbb{D}^a)}{\sum_{i \in \mathbb{D}^a} b_i} \left(\frac{U}{L}\right)^{l-a}}{(f(\mathbb{S}_b \cup \{i\}) - \mathbb{S}_b) \beta^{-t'} \frac{1}{\lambda} \frac{f(\mathbb{D}^b)}{\sum_{i \in \mathbb{D}^b} b_i} \left(\frac{U}{L}\right)^{l-b}} \\
&\geq 1 \cdot \beta^{t'-t} \frac{L}{U} \cdot \left(\frac{U}{L}\right)^{a-b} \\
&\geq 1
\end{aligned}$$

The inequality $f(\mathbb{S}_a \cup \{i\}) - \mathbb{S}_a \geq f(\mathbb{S}_b \cup \{i\}) - \mathbb{S}_b$ is due to the submodularity of function f . This indicates that the participant can't obtaining higher utility by misreporting her arrival time. The analysis on departure time similar.

case 2: In this case, this participant can not win the auction any time. She will not win the auction by misreporting her time because in her present period, her low efficiency always makes her lose the auction. \square

Theorem 11. *The mechanism with submodular value function is cost-truthful*

Proof. Here we prove that a participant can't misreport her cost for more utility. It suffices to show bidding her true cost is a dominant strategy. As we have proved before, we consider two cases.

case 1: Participant i can win the auction before she departs if she bids truthfully. Assume she is selected at time t_a in stage $[T_a, T_{a-1}]$. If she misreports her cost and fails, her utility will be zero. Otherwise, assume she misreports her cost and wins the auction at time t_b in stage $[T_b, T_{b-1}]$. With the analysis in the proof of theorem 5, she can not get higher payment calculated in line 9 in algorithm 5. We next prove she can not get higher payment calculated in line 15 in algorithm 5. From the analysis in the proof of theorem 10, her payment will not be updated because she can't get a higher payment. So we have proved she can't obtain more utility in this case.

case 2: Participant i can be selected when she departs and she misreports a cost b_i . If she still can not win the auction until she departs, she will get a payment equals $\frac{\tilde{f}_t^i(\mathbb{S} \setminus \{i\})}{\rho}$, which is the same as she bids truthfully because this payment has nothing to do with the bid. Otherwise, we assume she can win the auction at some time t by misreporting lower cost (Apparently, higher cost doesn't "help"). The participant's failure is due to two reasons: low efficiency or budget constraint. If it is because of the budget, she will still fails. If it is because the low efficiency, i.e., $\frac{\tilde{f}_t^i(\mathbb{S})}{c_i} \geq \rho$, we can derive $c_i \geq \frac{\tilde{f}_t^i(\mathbb{S})}{\rho}$. If she wins the auction and get a payment, this payment will be less than her cost. So we have proved this case.

case 3: Participant i can not win the auction all the time. If she can not win the auction by misreporting her cost, she will get the same payment 0. Otherwise, she can win the auction.

With the analysis in case 2, she can not win the auction before she departs for the reason of individual-rationality. So she can only be selected at the time she departs and she will get a payment $\frac{\hat{f}_i(S \setminus \{i\})}{\rho}$ calculated in line 15. When she bids her true type, she will fail in line 14. It is because of the budget constraint or the efficiency. If she proposes a lower cost for higher efficiency, she will get a negative utility. If she fails for the reason of the budget, she will fail again, because the budget has nothing to do with the bid. It is noted that she can't be compared earlier for a payment by misreporting a higher efficiency because she ever failed in the previous comparing rounds. \square

Theorem 12. *The mechanism has a constant competitive ratio in the large-scale crowdsensing system.*

Proof. In the case where the value is not time-discounting, Zhao *et al.* has proposed a different algorithm to calculate the threshold [54]:

Algorithm 6:

Input : Stage budget B' , sample set S'

```

1  $\mathbb{J} \rightarrow \emptyset; i \rightarrow \operatorname{argmax}_{j \in S'} V_j(\mathbb{J}) \setminus b_j;$ 
2 while  $b_i \leq \frac{v_i(\mathbb{J})B'}{V(\mathbb{J} \cup \{j\})}$  do
3    $\mathbb{J} \rightarrow \mathbb{J} \cup \{i\};$ 
4    $i \rightarrow \operatorname{argmax}_{j \in S' \setminus \mathbb{J}} V_j(\mathbb{J}) \setminus b_j;$ 
5  $\rho \rightarrow V(\mathbb{J}) \setminus B';$ 
6 return  $\rho \setminus \delta;$ 

```

They also proved that the competitive ratio is a constant times $\frac{2\alpha}{\delta}$ if δ satisfies that $\frac{1}{2} - (\frac{\delta}{1-2\alpha} - 1)\frac{1}{\omega} - \frac{1}{\delta} = \frac{2\alpha}{\delta}$, where $\alpha \in (0, \frac{1}{2}]$ and ω is a sufficiently large constant. It approaches to $\frac{1}{4}$ as $\omega \rightarrow \infty$ and $\delta \rightarrow 4$.

In line 7 in the algorithm 4, the threshold is defined as $\frac{1}{\lambda} \frac{f(\mathbb{D}^{T_k})}{\sum_{i \in \mathbb{D}^{T_k}} b_i} (\frac{U}{L})^{l-k} = \frac{1}{\lambda} \frac{f(\mathbb{D}^{T_k})}{B} \frac{B}{\sum_{i \in \mathbb{D}^{T_k}} b_i} (\frac{U}{L})^{l-k} \geq \frac{1}{\lambda} \frac{f(\mathbb{D}^{T_k})}{B} (\frac{U}{L})$. With the same analysis, it approaches to $\frac{1}{4}$ as $\omega \rightarrow \infty$ and $\lambda \rightarrow \frac{U}{4L}$. \square

VI. NUMERICAL RESULTS

In this section, we show the evaluation results.

A. Methodology

We implement the design of our budget feasible online mechanism with time-discounting values (namely TDM in the simulation). We compare its performance with the optimal offline mechanism (namely OPT) and an online mechanism which randomly selects participants. The optimal result is computed by solving a binary integer program to determine whether to select a participant. We will evaluate in two metrics:

- **Total Value:** Total value is the total contributions of all selected participants. In the TDM mechanism, the total value is the summation of each participant's value. In the TDMS mechanism, the total value is the output of a submodular function with the input of selected participant set. We will measure the total value from some aspects,

e.g., the total budget, the number of participants and some system parameters.

- **Select Ratio:** The select ratio is the percentage of participants who is selected by the mechanism.
- **Budget Utilization:** Budget Utilization is the percentage of the used budget.

In the setup of the evaluation, we first fix some system parameters. The auction period T is set to 50 and the time slots are divided into 5 stages. In the large-scale environment [1], we make a reasonable assumption that the cost of each participant accounts for a tiny part of the total budget. This ratio is set to 0.0015 in this paper. The initial threshold at the begin of this auction is set to 0.1 to avoid possible starvation. The upper bound and lower bound of efficiency are set respectively 2 and 1.

B. Total Value

We compare our total value with the OPT and Random algorithm. We change the budget and number of participants respectively.

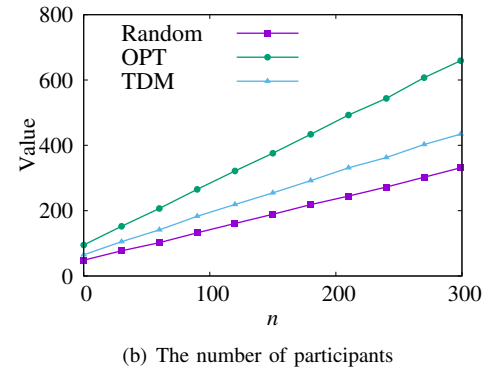
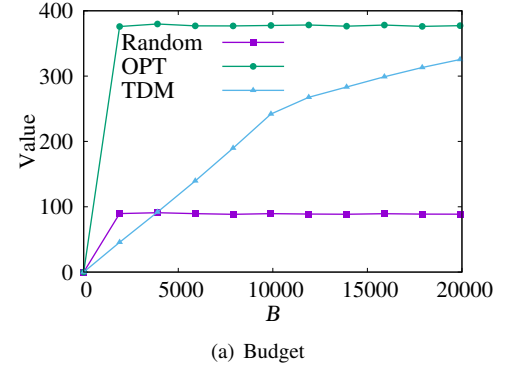
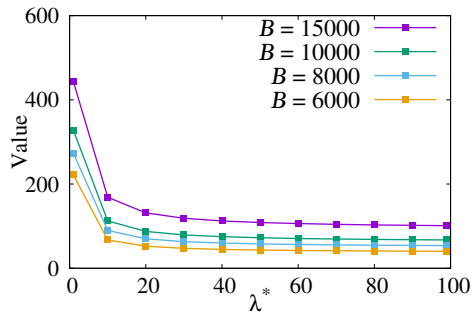
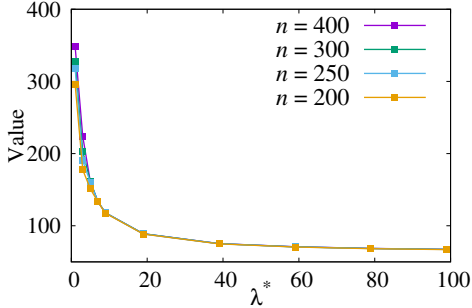


Fig. 2. Impact of varying the budget and the number of participants

In Fig. 2(a), we show the total value contributed by selected participants with varying budget. The number of participants n is set to be 200. We vary the budget from 0 to 20000 with the increment of 2000. The arrival time and departure time are uniformly distributed in $[1, T]$. The discounting function in our evaluation is set to $F(t) = 0.9^t$, so the time-discounting value of participant i is $v_i(t) = 0.9^t v_i$. The value and cost of each participant are randomly selected. All the results are averaged over 200 rounds. We observe that as the budget increases,



(a) Different budgets



(b) Different numbers of participants

Fig. 3. Impact of λ ($\lambda = \lambda_{min} + \frac{\lambda^*}{100}(\lambda_{max} - \lambda_{min})$).

the total value is becoming higher before the saturation is achieved. We note that when the budget is small, the value of TDM is less than value gained by random selection scheme. This is because that several participants will lose the auction with the small budget. These participants will be selected later or never. Due to the time-discounting property of values, the total value will decrease dramatically with time. However, we note that even with the strong constraint of truthfulness, our mechanism still achieves superior performance to the random scheme.

In Fig. 2(b), we vary the number of participants n from 0 to 600 and fix the budget to 15000. We can observe that with more participants, the total value increases. This is due to the fact that with more participants, the probability of the appearance of participants with high efficiencies gets higher.

We then find the effect of the system parameter λ on the total value, with different budget and number of participants.

In Fig. 3(a) and Fig. 3(b), we intend to investigate the effect of the system parameter λ . According to inequality (9), λ has an upper bound $\lambda_{max} = \frac{1}{\epsilon} \left(\frac{U}{L}\right)^{l-2}$ and a lower bound $\lambda_{min} = 2 \left(\frac{U}{L}\right)^{l-1}$, but we don't know how to choose λ to maximize the value (even though we can guarantee a constant competitive ratio). We divide the interval $[\lambda_{min}, \lambda_{max})$ into 100 pieces. We should also consider the effect of different budgets and participants. These two figures show us that with λ getting closer to λ_{min} , the value is getting higher regardless of the different budgets and participant numbers. This is because when λ gets smaller, the threshold gets larger and the total

value increases as well. The premise of this phenomenon is the huge number of participants. Considering that there are rare participants competing in this auction, if the threshold is large, some participants will be selected later. The total value will decrease due to the time-discounting property. When there are plentiful participants, the participants with less efficiency will lose and never be selected. In addition, we can also see the competitive ratio in expression (8) has a negative correlation with λ .

C. Select Ratio

D. Budget Utilization

VII. CONCLUSIONS AND FUTURE WORK

In this paper, we propose a strategy-proof and budget feasible online incentive mechanism for crowdsensing that considers the property of time-discounting values. The method proposed in our paper calculates a selection threshold, selects participants online and pays each selected participant with a carefully designed payment to guarantee strategy-proofness. We consider both the case with the function is a summation and a modular function. We have proved that no participant can get higher utility by misreporting her type. The competitive ratio of our mechanism is constant. The simulation results have shown that our mechanism achieves great performance in terms of the total obtained value.

In our paper, the time-discounting factor is β_{-t} , which is also used in the previous work. But in a general model, the value can be represented as $\max(v_i F_i(t) + D_i(t), 0)$, where F_i and D_i may be arbitrary functions. An attractive direction of future work is designing a general mechanism for the general discounting functions.

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