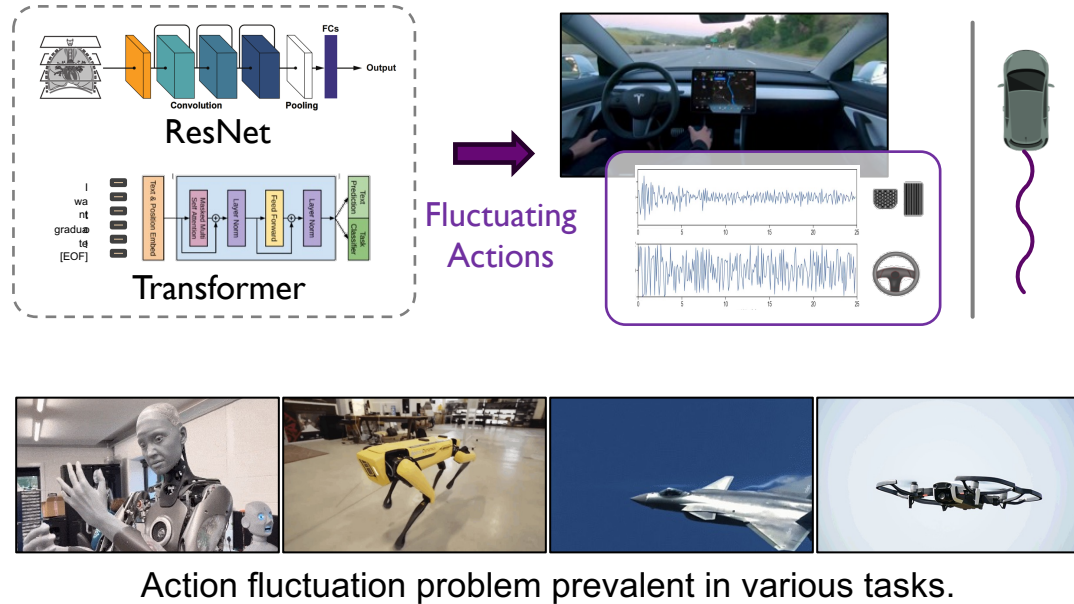


1. Background

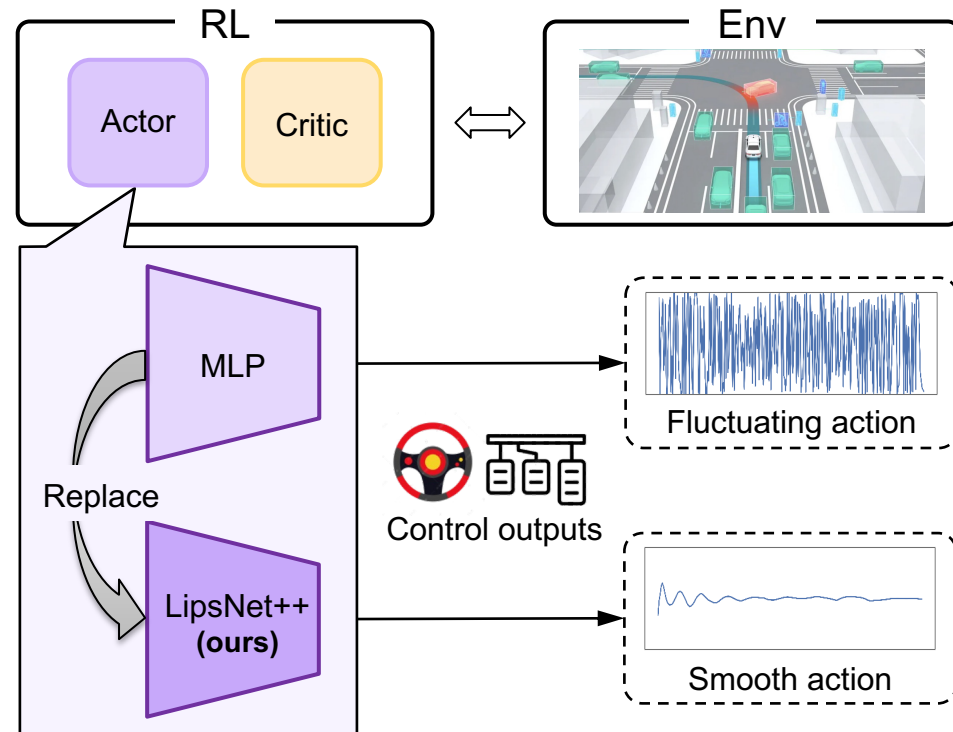
Deep **reinforcement learning (RL)** is effective for decision-making and control tasks like autonomous driving and embodied AI.

However, RL policies often suffer from the **action fluctuation problem** in real-world applications, resulting in severe actuator wear, safety risk, and performance degradation.



2. Objective

Our objective is to **smooth the action trajectory** in RL by designing the actor network, without complicating the RL algorithms.

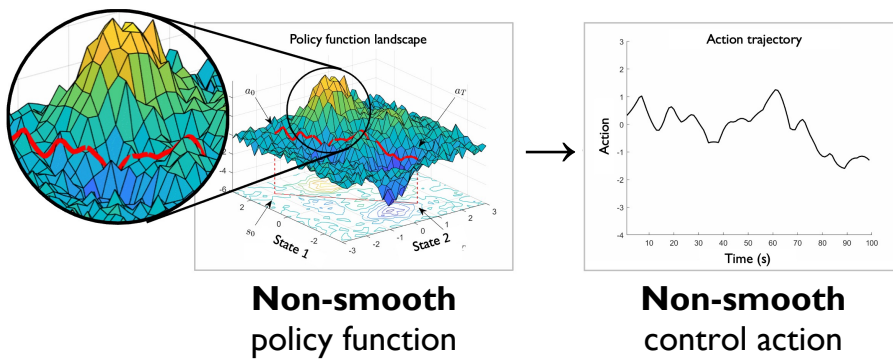


3. Reasons Identification of Action Fluctuation

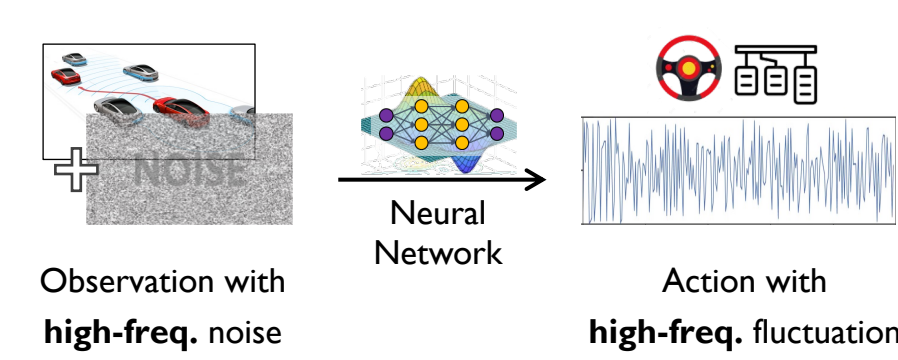
$$\text{Observation: } o_t = s_t + \xi_t \quad \text{Action: } a_t = \pi(o_t) \quad \text{Action change rate: } \frac{da_t}{dt} = \frac{d\pi(o_t)}{do_t} \cdot \frac{do_t}{dt}$$

$$\left\| \frac{da_t}{dt} \right\| \leq \left\| \frac{d\pi(o_t)}{do_t} \right\| \cdot \left(\left\| \frac{ds_t}{dt} \right\| + \left\| \frac{d\xi_t}{dt} \right\| \right)$$

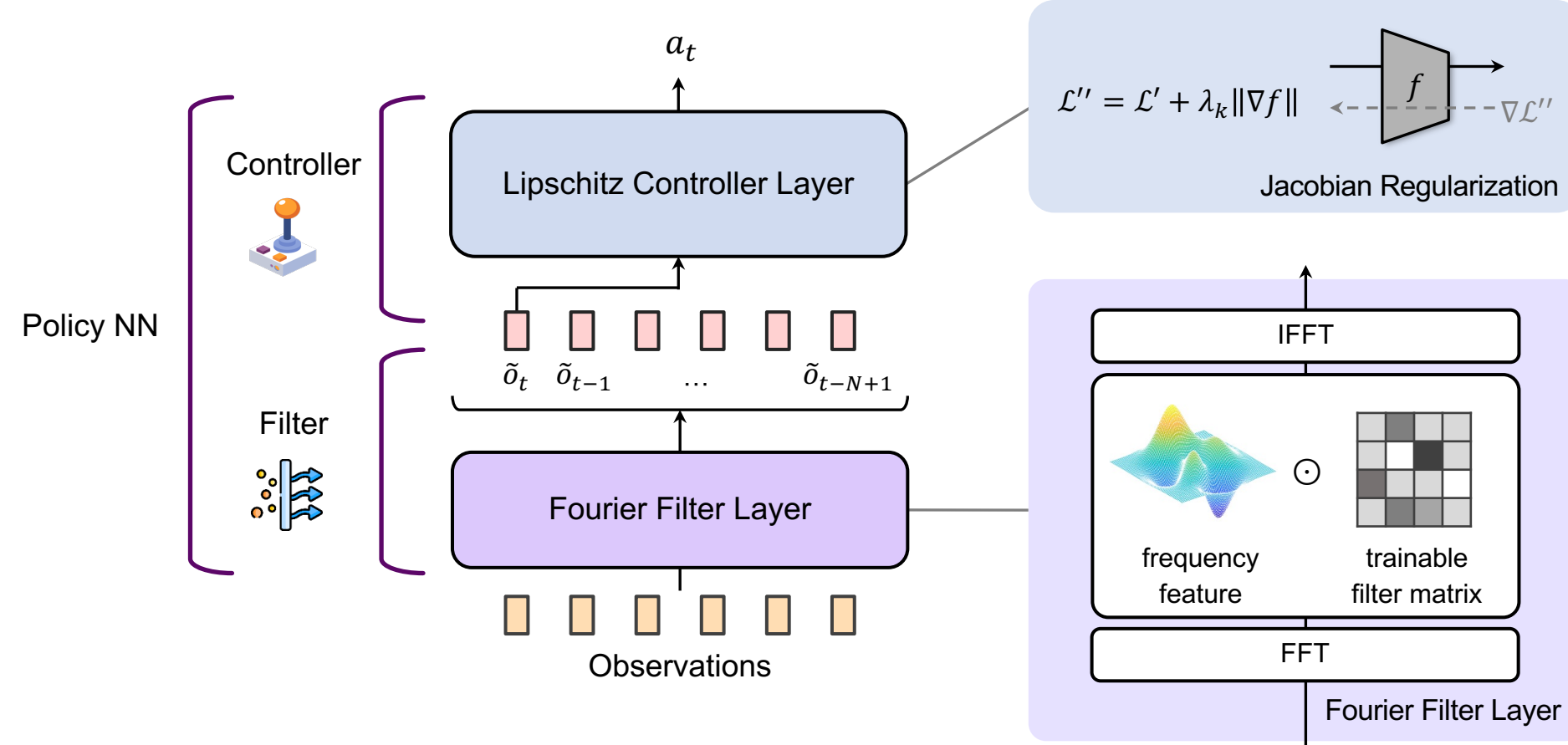
Reason 1: policy function's **non-smooth landscape**



Reason 2: existence of **observation noise**



4. Overall Structure of LipsNet++



5. Theorem & Learning Mechanism

Fourier Filter Layer

Tailor the policy improvement (PIM) loss as

$$\mathcal{L}' = \mathcal{L} + \lambda_h \|H\|_F$$

For policy improvement

For learning the filtering strength of each frequency

Lipschitz Controller Layer

In this layer, we propose Jacobian regularization to constrain the Lipschitz constant of policy network.

Definition 3.1 (Local Lipschitz Constant) Suppose $f: \mathbb{R}^n \rightarrow \mathbb{R}^m$ is a continuous neural network. The $K(x)$ is defined as the local Lipschitz constant of f on the neighborhood $\mathcal{B}(x, \rho) = \{x': \|x' - x\| < \rho\}$:

$$K(x) = \max_{x_1, x_2 \in \mathcal{B}(x, \rho)} \frac{\|f(x_1) - f(x_2)\|}{\|x_1 - x_2\|}$$

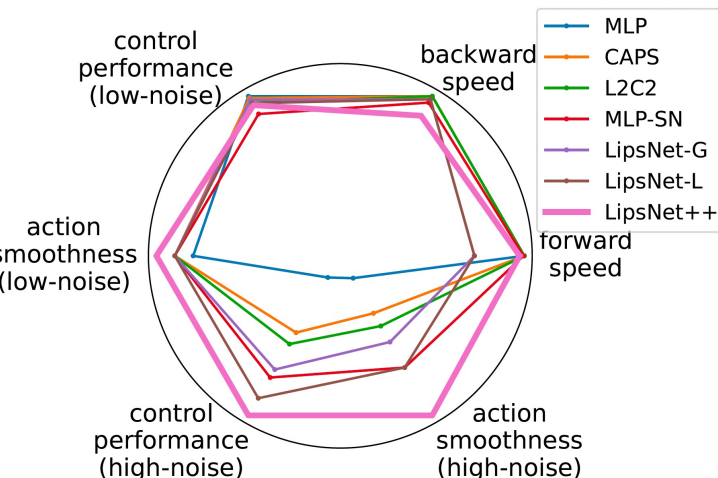
Theorem 3.2 (Lipschitz's Jacobian Approximation) Let $f: \mathbb{R}^n \rightarrow \mathbb{R}^m$ be a continuously differentiable network. The Jacobian norm $\|\nabla_x f\|$ is an approximation of $K(x)$ within $\mathcal{B}(x, \rho)$. The approximation error is

$$\max_{\delta \in \mathcal{B}(0, \rho)} \left[(\nabla_x \|\nabla_x f(x)\|)^T \delta + o(\delta) \right]$$

Moreover, as $\rho \rightarrow 0$, the Jacobian norm converges to the exact local Lipschitz constant, i.e. $\lim_{\rho \rightarrow 0} \|\nabla_x f\| = K(x)$.

6. Overall Performance

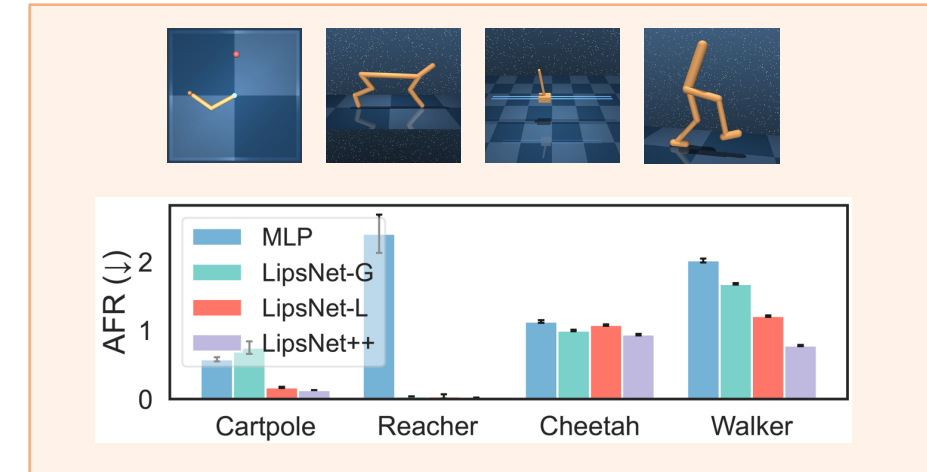
We evaluate the overall performance of LipsNet++ with 6 baselines across 6 metrics. It shows that **LipsNet++ achieves the SOTA overall performance**.



7. Experiment Results

DeepMind Control Suit

The results show that LipsNet++ has the **lowest** action fluctuation ratio (AFR) with the same level of total average return (TAR). E.g., LipsNet++ reduces the AFR by 35.5% in Walker env. compared to LipsNet (Song, ICML 2023).



Mini-Vehicle Driving

We evaluated LipsNet++ on the trajectory tracking and obstacle avoidance task in 4 scenarios with varies noise levels. The result implies that LipsNet++ has much better **action smoothness** and **noise robustness**.

