Practical implementation and analysis of an algorithm *

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1 Task 1

Schedule function has biggest complexity of $O(n^2)$ because of nested loops in it, first loop goes through every possible job, second one takes to attention days available to assignment before actual deadline (for instance if deadline is 5, we check if 5 is already taken, if yes check 4 etc.).

In main function there are sort function that is nlogn of complexity, and then function that prints the matrix which is $O(n^2)$ as schedule function. so the biggest complexity is $O(n^2)$ then complexity of this solution is $O(n^2)$.

2 Task 2

According to the book, complexity of disjoint set 3 is O(nlogm), this is because of attributes depth (makes sets to merge to a more compact structure, where root is always the biggest depth i.e assigned earlier than other members of the set) and smallest which contains in it the

Figure 1: task1_schedule

smallest member of the set which, if the deadlines before actual selected deadline are taken, will be 0, which means that job for that deadline cannot be assignmed in any way. Those modifications (depth and smallest) will save us some iterations, for example iteration to the top of the tree to find the smallest deadline that has been taken and in result we will achieve better complexity of O(nlogm)

The biggest complexity oin schedule function is merge that is O(nlogm), merge have this modification because root member always got to have smallest member so we got to update it and sinse it is a tree - O(nlogm)

Figure 2: task2_merge

3 Task 3

3.1 A

Greedy approach that is $O(n^2)$ because we go through matrix once, check each row for max value, take it, ban the column that we found it in, continue to the next row. With such approach we will find only local optimum, maybe sometimes it will be the same with global optimum

3.2 B

Steps are described in code with complexity for each function

Figure 3: task2_schedule

Figure 4: task3a_schedule

 $O(n\hat{3})$ is the classic complexity of the Hungarian algorithm but since steps 3 and 4 will be repeated until number of minimum lines is n that makes it undefined number of iterations (in reality for n 10 it is 1 - 3 iterations, but i couldnt predict why).

Step 3 (getMinimumLines) will be $O(n^2)$ because we need to check each zero in matrix and the worst case will be when we need n lines to cover all zeroes in each of such iteration (for each line) we have couple loops (total of O(n)) where we calculate the best line to draw to achieve minimum drawn lines.

Since step 3 has the biggest complexity of $O(n^2)$ and classic Hungarian algorithm is told to be $O(n^3)$ i can sugest that that loop for undefined iterations will have complexity of O(n) but there are still no visible arguments for this to be respectable statement.

Except Hungarian algorithm itself I had to find out how to choose such order that will be best, i found a way in which i try all 4 possible ways to start taking cells in rows (from top left, top right, bottom left, bottom right), to test each of them it takes $O(n^2)$ which is no bigger than other functions, it is not nested so the total complexity of lookin up the assignment order is $O(n^2)$

Figure 5: Hungarian algorithm

Figure 6: One of four possible ways to find assignment order that is the best $O(n^2)$