

1.

① a.  $(0201)_{16}$  F

$$\begin{aligned} \textcircled{2} \quad b. \quad & 0000 \quad 0000 \quad 0000 \quad 0011 = 1111 \quad 1111 \quad 1111 \quad 1100 \\ & = 1111 \quad 1111 \quad 1111 \quad 1101 \\ & = (FFFD)_{16} \end{aligned}$$

②  $(0201)_{16} = 16^0 + 2 \times 16^1 = 513$

$(FFFD)_{16} = 13 \times 16^0 + 15 \times 16^1 + 15 \times 16^2 + 15 \times 16^3 = 65533$

③ a.  $\min = -2^{15}$   $\max = 2^{15} - 1$

b.  $\min = 0$   $\max = 2^{16} - 1$

2.

a.  $x = C \quad C \quad 1100 \quad XXXX \quad 1100$

$\sim x = 0011 \quad XXXX \quad 0011$

$y = XXX1 \quad 1101 \quad 0XXX$

$x = C \geq C$

b.  $x = 110000101100$

$x = \boxed{3116}$

c.  $y = 001111010011 = \boxed{979}$

3.

N/a  $0$   $000000$

n/a  $-1$   $111111$

n/a  $2^9$   $011101$

n/a  $-17$   $101111$

n/a  $2^6$   $011010$

n/a  $-2^6$   $100110$

T/Max  $31$   $011111$

T/Min  $-32$   $100000$

$-T/Min$   $-32$   $100000$

$-T/Max$   $-31$   $100001$

$T/Max + T/Max$   $-2$   $011111$

$+ 011111$   
 $\boxed{111110}$



$$\begin{array}{r}
 T_{Min} + T_{Min} \quad 0 \quad 100000 \\
 + 100000 \\
 \hline
 000000
 \end{array}$$

$$\begin{array}{r}
 T_{Min} + 1 \quad -31 \quad 100001 \\
 T_{Min} - 1 \quad -31 \quad 100000 \\
 + 111111 \\
 \hline
 011111
 \end{array}$$

$$\begin{array}{r}
 T_{Max} + 1 \quad -32 \quad 011111 \\
 + 000001 \\
 \hline
 000000
 \end{array}$$

$$\begin{array}{r}
 T_{Min} + T_{Max} - 1 \quad 100000 \\
 + 011111 \\
 \hline
 111111
 \end{array}$$

$$\begin{array}{r}
 T_{Max} * 2 \quad -2 \quad 011111 \\
 + 011111 \\
 \hline
 111110
 \end{array}$$

$$\begin{array}{r}
 T_{Max} / 2 \quad 15 \quad 001111
 \end{array}$$

4. 1.G 2.C 3.B 4.F 5.I

5. 

```
int multFiveEighths (int x)
{
    int e = x >> 3;
    int re = x & 7;
    int se = (x >> 31 & 7);
    return (e + (e << 2) + (re + (re << 2) + (se >> 3))) ;
}
```

6. format A.

① 010110011

$$7 - 15 = -8$$

$$\frac{3}{8} + 1 = \frac{11}{8}$$

$$\frac{11}{8} \times 2^7 = 176$$



② 1 0 0 1 1 1 0 1 0

$7 - 1 = -8$

$-2^{-8} \times (1 + \frac{2}{8}) = -1.25 \times 2^{-8}$

③ 0 0 0 0 0 1 1 1

$\frac{7}{8} \times (2^{-14})$

$= 0.875 \times 2^{-14}$

④ 1 1 1 1 0 0 0 0

$-2^{13}$

⑤ 0 1 0 1 1 1 1 0 0

$(\frac{17}{8}) \times 2^8 = 384$

format B

① 0 1 1 1 0 0 0 0 0 0 +∞

② in A is 1 0 0 1 1 1 0 1 0  
in B  $S=1$   
 $f=-5$

the smallest is 1 0 0 0 0 0 0 0 which is  $-\frac{1}{32} \times 2^{-2}$   
and we need to roundup

So it is 0 0 0 0 0 0 0 0 0 0  $-\frac{1}{32} \times 2^{-2}$

③ in A is 0 0 0 0 0 1 1 1

round to nearest one

0 0 0 0 0 0 0 0 1  $(\frac{1}{32}) \times 2^{-2}$   
so it is 0 0 0 0 0 0 0 0 1  $(\frac{1}{32}) \times 2^{-2}$

④ in A is 1 1 1 1 0 0 0 0

the smallest non-infinit number is 1 1 1 0 1 1 1 1

$-2^3 \times (\frac{31}{32} + 1) = -15.75$

⑤ 0 1 1 1 0 0 0 0 0 0 +∞

7. if  $x > 0$   $x \neq x > 0$  false  $2^{16} \cdot 2^{16} = 2^{32}$  overflow  $< 0$   
 $((x > 0) < 1) == x$  False  $00001 >> 1 = 00000$

$(u \& 0) == 0$  true  
 $u < -1$  true  
 if  $x < 0$  then  $u > x$  false

max of  $u$  is  $2^{32}-1$   
 max of  $x$  is  $2^{32}+x$   
 So we can not determine  
 Which one is bigger

$u \geq 0$  true  
 if  $x > y$  then  $-x < -y$  False

if  $y$  is TMin  $x$  is TMin-1  
 $-y$  is also TMin  $-x$  is positive  
 So ~~is not~~  $-x \neq -y$