1. The graph is not balanced. For a graph to be balanced, there cannot exist a cycle that is unbalanced. For a triangle of nodes to be balanced, we must have  $w_{ij}w_{jk}w_{ik} \ge 0$ , where  $w_{ij}$  represents the value of the edge between nodes i and j (in our case, a 1 or -1 depending on the positivity or negativity of the edge). Looking at nodes 2, 3, and 4, we can see that  $w_{23}w_{34}w_{24} = (-1)(1)(1) = -1$  which is obviously not  $\ge 0$ . Therefore, the graph is unbalanced.

2.

a. Degree Centrality

Degree Centrality can be calculated by  $c_i = \frac{d_i}{n-1}$ .

- 1: 3/9 = 1/3
- 2:1/3
- 3: 1/3
- 4: 2/9
- 5: 1/3
- 6: 1/3
- 7:1/3
- 8:1/3
- 9:1/3
- 10:2/9

For the following centrality calculations, I wrote scripts in Python using the NetworkX Library

```
G = nx.Graph()
G.add_edge(1, 3)
G.add_edge(1, 2)
G.add_edge(1, 10)
G.add_edge(2, 4)
G.add_edge(2, 7)
G.add_edge(3, 5)
G.add_edge(3, 8)
G.add_edge(4, 6)
G.add_edge(5, 6)
G.add_edge(5, 6)
G.add_edge(5, 9)
G.add_edge(6, 7)
G.add_edge(7, 8)
G.add_edge(8, 9)
G.add_edge(9, 10)
```

#### b. Eigenvector Centrality:

```
nx.eigenvector_centrality(G)

{1: 0.3104883904772362,
3: 0.3579907069964069,
2: 0.3063031282514309,
10: 0.2231838875316019,
4: 0.21941202212603364,
7: 0.34561011840798544,
5: 0.35205192749011016,
8: 0.3607164531280917,
6: 0.3208440534144026,
9: 0.3274463984152574}
```

#### c. PageRank Centrality:

```
nx.pagerank(G)

{1: 0.1073109558303194,
3: 0.10491482880528645,
2: 0.10745807640817177,
10: 0.07562231436914846,
4: 0.07572421188603344,
7: 0.10542104280136726,
5: 0.10522110721859218,
8: 0.10481254791560028,
6: 0.10686587981512946,
9: 0.10664903495035094}
```

d. Katz Centrality:

```
nx.katz_centrality(6)

{1: 0.32055872140499675,
3: 0.3238045584037487,
2: 0.3205331921654917,
10: 0.29115201149015374,
4: 0.29114640100740213,
7: 0.32352934554074503,
5: 0.3235599185730798,
8: 0.3238295214709142,
6: 0.32083333110004352,
9: 0.32086388926988524}
```

3. For this question, I again wrote a Python script and found the assortativity coefficient using the NetworkX library.

```
G = nx.Graph()
G.add_edge('a', 'b')
G.add_edge('a', 'c')
G.add_edge('a', 'd')
G.add_edge('a', 'e')
G.add_edge('a', 'f')
G.add_edge('b', 'g')
G.add_edge('b', 'i')
G.add_edge('e', 'i')
G.add_edge('f', 'h')

nx.degree_assortativity_coefficient(G)

-0.45945945945945965
```

Adjacency List:

1:2,3

4.

2:1,3

3:1,2,4,5

4: 3, 5, 6, 7

5: 3, 4, 6, 7

6: 4, 5, 7, 8

7: 4, 5, 6, 8

8:6,7,9

9:8

## Edge List:

12

13

23

3 4

3 5

45

46

47

5 6

5 7

67

68

78

89

5.

a. BFS

Parent array:

v1:-

v2: v1

v3: v2

v4: v1

v5: v2

v6: v4

- v7: v5
- v8: v6
- v9: v5

## b. DFS

# Parent array:

- v1:-
- v2: v1
- v3: v2
- v4: v5
- v5: v3
- v6: v4
- v7: v6
- v8: v7
- v9: v8

# c. Dijkstra's

## Parent array:

- v1:-
- v2: v1
- v3: v2
- v4: v1
- v5: v2
- v6: v4
- v7: v6
- v8: v6
- v9: v5