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ALGORTIHMS

Detection of similarity between documents with hashing

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1 Introduction

In this (practica) we are going to create different algorithms to compute the difference between various documents in order to be able to detect if there may have been a possibility of copy any pair of the documents. To do it, we have started with a very basic algorithm that returns the Jaccard Similarity with two documents and we have finished obtaining a Locality-sensitive hashing algorithm that giving the paths of several documents will return which documents may have been copied. (All the algorithms are explained in the document).

2 Jaccard Similarity

The Jaccard Similarity, also known as Intersection Over Union (IOU), calculates the percentage of similarity between two sets.

For any pair of sets S and T , the Jaccard Similarity is defined as:

$$J(S, T) = \frac{|S \cap T|}{|S \cup T|} \quad (1)$$

We can easily deduce that the more common words, the bigger the Jaccard Similarity, which means that it is more probable that one set is a duplicate of the other.

Example 2.1. In Figure 2.1 we see two sets S and T . There are 3 elements in their intersection ("I", "love", "chocolate") and 6 in their union ("I", "love", "chocolate", "and", "pizza", "white"). Thus, $J(S, T) = 3/6$.

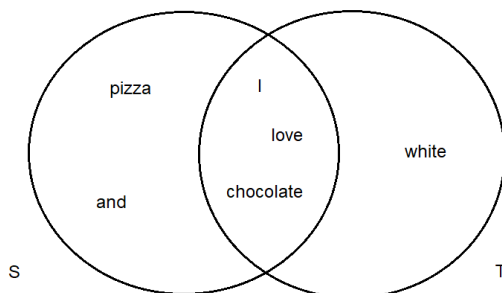


Figure 2.1: Two sets with Jaccard Similarity 3/6.

3 Shingling of Documents

Any pair of documents can be compared by watching the number of repeated strings they have. The more common strings, the more probable is that one is a duplicate from the other. One way to represent a document as a set is to insert in the set each string that appears in it. If we do so, then duplicated documents that have reorganized the sentences or even the entire text will have plenty of common strings, and will be detected as duplicated.

3.1 k-Shingles

The idea is not to insert in the set all the words, but a set of characters of size k . Thus, each element of the set will have the same size as the others.

The question now is how big k should be? If we take a small value of k , this will result in many shingles that are present in all documents. Suppose we choose the extreme case ($k = 1$). Then, all documents would result to be similar, as the most used characters are present in all documents. However, if we take a big value of k , then any pair of documents would not share a shingle.

The value of k depends on the size of the documents. A poem will not have the same k value than an article. Otherwise, we could have the problems mentioned before. According to Anand Rajaraman, Jure Leskovec, and Jeffrey D. Ullman (2011), "k should be picked large enough that the probability of any given shingle appearing in any given document is low." (p. 78).

4 Comparing Similarity Using The Sets

If we succeed in shingling the documents by using the k -Shingling technique, we will only have to compare all pairs of documents using the Jaccard Similarity and say if there is similarity between them or not. In order to do this, we have to store all the information in a data structure, for instance, a matrix. By doing this, we have two problems: time and space complexity.

4.1 Matrix Representation

To represent the matrix, we will put the documents' sets in the columns and the union of all the documents' sets in the rows. The values of the matrix will be the following:

$$\begin{cases} 1, & \text{if column } c \text{ contains row } r \\ 0, & \text{otherwise} \end{cases}$$

Example 4.1. *For this example we will use two sets representing the words "Nadal" and "Nadia". Let $k = 2$ to form the k -Shingles.*

<i>Element</i>	<i>S 1</i>	<i>S 2</i>
na	1	1
ad	1	1
da	1	0
al	1	0
di	0	1
ia	0	1

Figure 4.1: Representation of the matrix with two sets S and T .

In this type of matrices, for any pair of columns we can have 4 types of results, which are the permutations of 0s and 1s of size 2:

Element	S_1	S_2
a	0	0
b	0	1
c	1	0
d	1	1

Figure 4.1: Representation of the matrix with all the possible permutations.

Note that as the matrix is sparse, most of the rows will be of type *a*. If we try to calculate the similarity between two sets S_1 and S_2 using the matrix and the Jaccard Similarity, we will have the following result:

$$J(S_1, S_2) = \frac{Q(d)}{Q(b) + Q(c) + Q(d)} \quad (2)$$

Where $Q(x)$ is the number of rows of type x . $Q(d)$ is the intersection of the sets and $Q(b) + Q(c) + Q(d)$ is the union of the sets.

4.1.1 Time Complexity

Imagine we have n documents. Then, we have to compare each document with all the rest. Thus, the number of comparisons we have to do is $n * (n - 1)/2$ which is equal to $O(n^2)$.

Example 4.2. Suppose we have 1 million documents. The number of comparisons would be $5 * 10^{11}$ which is a huge number.

$$\frac{(1 * 10^6) * 999.999}{2} = 499.999, 5 * 10^6 \approx 5 * 10^{11} \quad (3)$$

4.1.2 Space Complexity

In typical applications the matrix is sparse, which means that there are more 0s than 1s.

If we take k shingles, then the document have relatively few of the possible shingles. Another way to think about this is with the toys in Christmas Day. Kids would be the columns of the matrix and toys, the rows. Usually, kids would like to have a specific toy, which is very popular at that moment. Then, lots of toys would not be bought for any kid.

4.2 Minhashing

The main goal using minhashing is to reduce a lot the space complexity. We can achieve this by substituting the matrix shown before by another matrix called "signature matrix".

Signatures are smaller representations of the sets, but they still preserve the similarity of the sets they represent. We will demonstrate this in the next section.

To minhash a set, first pick a random permutation of the rows. Then, the minhash value is the value of the first row that has a 1, preserving the permuted order.

Example 4.3. In this example we will reuse the two sets of Example 4.1. Suppose that the random permutation has given the following order: "di", "da", "ia", "na", "ad", "al". Let h be the minhash function.

<i>Element</i>	<i>S₁</i>	<i>S₂</i>
di	0	1
da	1	0
ia	0	1
na	1	1
ad	1	1
al	1	0

Figure 4.3: Permutation of the matrix of Example 4.1.

In the first column, we can see that $h(S_1) = "da"$ and in the second one we see that $h(S_2) = "di"$.

With this technique, we can see that every time we do a permutation, we only occupy one new row of the "signature matrix", which is reducing a lot the space.

4.2.1 Preserving the Jaccard Similarity

As we mentioned before, the Jaccard Similarity in the matrix is equal to the number of rows of type d divided by the number of rows of type $b + c + d$. And that Similarity is preserved in the "signature matrix".

Proof. Look down through the permuted columns C_1 and C_2 until we see a 1 in any of the two columns. Then, we can have a row of type b or c , where only one of the columns have a 1, or a row of type d , where both columns have a 1 in it. If we find a row of type d , then the minhash function will take the same row. Thus, $h(C_1) = h(C_2)$. Otherwise, we must have a row of type b or c and $h(C_1) \neq h(C_2)$.

We can see that this is exactly the Jaccard Similarity. The probability of two columns have the same minhash value is equal to the number of rows of type d divided by the number of rows of type $b + c + d$.

$$P[h(C_1) = h(C_2)] = J(C_1, C_2) \quad (4)$$

□

4.2.2 Optimizing the Time for Permutations

Doing a set of permutation would be very expensive, but we can use a trick to simulate the n permutations. We can use n random hash functions that maps row numbers to as many buckets as the size of the rows of the matrix. We say that this is a trick because we are not doing a literal permutation, as we can have collisions using the hash functions but the point is that the probability of a collision with a large number k for the shingling is very small. Thus, we can think of this new algorithm as a perfect permutation of the rows. The algorithm is the following:

for each row r **do**

```

    for each hash function  $h_i$  do
        compute  $h_i(r)$ ;
    end for
end for
for each column  $c$  do
    if  $c$  has 1 in row  $r$  then
        for each hash function  $h_i$  do
            if  $h_i(r)$  is smaller than  $M(i, c)$  then
                 $M(i, c) := h_i(r)$ ;
            end if
        end for
    end if
end if
end for

```

Every time we go to the next row, we first compute all the hash values using the row value as their input. Then, for each position in that row, if there is a 1 we compare the hashed value of that position with the value in the signature matrix for all the hash functions computed. In case that this new value is smaller we change the value of the signature matrix by this new one. Doing this, in the end we have the smallest possible number in each position of the signature matrix.

4.2.2.1 Hashing Functions

We will present you now all the types of hashing functions we have used in the previous algorithm and in the algorithms in the Section 6.

4.2.2.1.1 Modular Hashing

In this case we will receive a key k , a prime number p , a random number modulus the number of shingles m and the number of k-shingles z . The result will be a number modulus the number of k-shingles of the document.

$$\text{modularHashFunction}(k, p, m, z) = (k * p + m) \bmod z$$

Require: Four integers k, p, m, z

Ensure: An integer h

return $(k * p + m) \bmod z$

4.2.2.1.2 Robert Jenkins' 96 bit Mix Function

In this case we will receive a prime number p , a random number modulus the number of shingles m and a key k . We will compute the returning value h , that will be found making a sequence of subtraction, exclusive-or, and bit shift.

$$\text{mix}(p, m, k) = h$$

5 Locality Sensitive Hashing (LSH)

We have talked before about how to improve the space complexity, but we still have not introduced a technique to improve the time complexity.

The general idea is that only a few pair of documents will have a high Jaccard Similarity. Thus, we need an algorithm that chooses the candidates that are more likely to be similar. The Locality Sensitive Hashing will help on this a lot.

The approach of LSH is to hash groups of rows into buckets in the sense that if two or more documents are hashed into the same bucket for at least one time, they will be very likely to be similar and will be put as a candidate pair.

5.1 Band partition

LSH will divide the signature matrix into b bands of r rows per band. Then, the algorithm will hash the set of rows that form a band for all the documents. Finally, it will create a new pair of candidates for every pair of documents hashed into the same bucket (for at least one time).

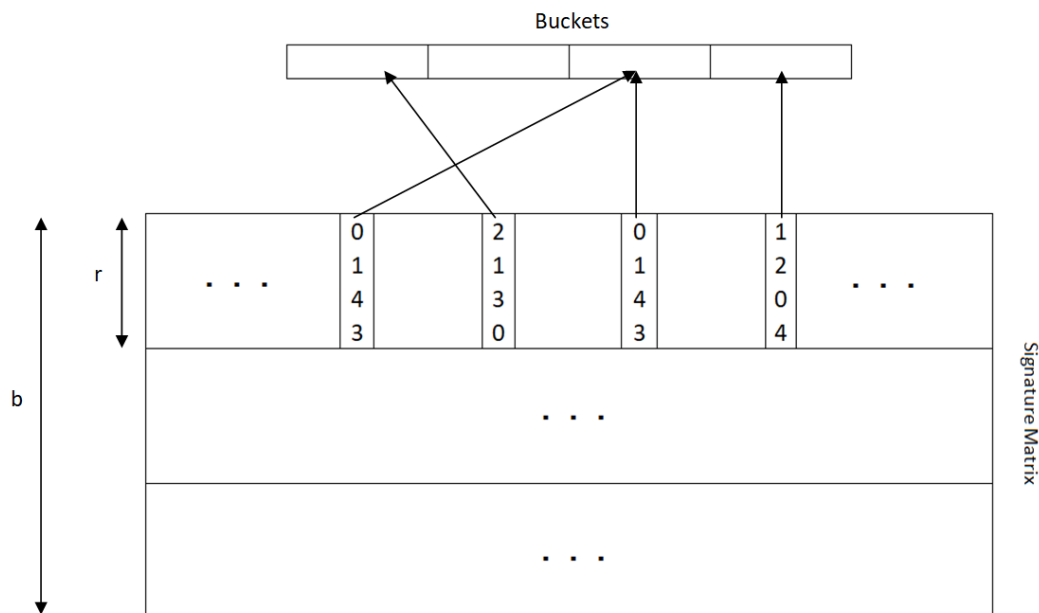


Figure 5.1: Band partition of a signature matrix and hashing the values of the rows of the first band into the buckets.

We can see that the set of rows of value "0143", from top to bottom, are hashed into the same bucket, and will be put as a candidate pair. However, the other two sets of rows ("2130" and "1204") will not be hashed into the same bucket, and will not be put as a candidate pair (with this band).

5.2 Choice of b and r values

The election of b and r values is a very important part of the algorithm. See that the bigger r , the less probable is to hash two sets of rows into the same bucket. This is because the probability that two sets of documents hashes into the same bucket decreases exponentially each time we add one row into r .

We want to get the least number of dissimilar documents that are hashed into the same bucket. These are called *false positives*. On the other hand, we also want to minimize the number of similar documents that are hashed into different buckets. These other ones are called *false negatives*.

The idea is to select a threshold, which is the minimum value that the Jaccard Similarity can have to consider two documents as similar, and then compute the b and r values.

According to Anand Rajaraman, Jure Leskovec, and Jeffrey D. Ullman (2011), "a good approximation to the threshold is $(1/b)^{1/r}$ " (p. 90). So if we take a threshold t , then we can calculate the b and r values as following:

Having that $r = \text{nhashFunctions}/b$,

$$t \approx \left(\frac{1}{b}\right)^{\frac{1}{r}} = \left(\frac{1}{b}\right)^{\frac{b}{\text{nhashFunctions}}} \quad (5)$$

Thus, using an arbitrary threshold, we can calculate the best approximate value of b and r .

6 Algorithms

The objective in this section is to show the idea behind the algorithms we have programmed and give you the time complexity for each one. If you want to see the code, you will have to go to the algorithms folder.

6.1 Jaccard Similarity

The main objective in this section is to calculate the Jaccard Similarity between two documents in different ways.

6.1.1 k-Shingles

The idea is to create two sets, one per document, and insert all substrings of size k of the documents. Afterwards, we will just have to make a division: the number of shingles in the intersection divided by the number of shingles in the union.

For each document:

Require: k

Ensure: Returns an `unordered_set` with all the substrings of size k of the document

$words$:= entire document

pos := 0

`unordered_set` S := \emptyset

while $pos + k \leq words.size()$ **do**


```

    sub := substring from pos to pos + (k - 1)
    insert sub into S
end while
return S

```

Once we have calculated the k -Shingles, we need to compute the intersection and the union of the sets. Note that we insert the substrings in an unordered set. This will be very usefull to improve the time complexity in the next two algorithms:

Require: Two sets S_1 and S_2

Ensure: Returns the intersection set between S_1 and S_2

```

unordered_set intersection :=  $\emptyset$ 
for each element in  $S_1$  do
    if  $S_2$  contains the element in  $S_1$  then
        insert the element into intersection
    end if
end for
return intersection

```

Require: Two sets S_1 and S_2

Ensure: Returns the union set between S_1 and S_2

```

unordered_set union :=  $S_1$ 
for each element in  $S_2$  do
    if the element in  $S_1$  is not contained in  $S_1$  then
        insert the element into union
    end if
end for
return union

```

As you can see, we visit only one set in each algorithm. The good thing is that finding if an element belongs to an unordered set or not is $O(1)$ (IN THE AVRE-AGE TIME????). Thus, the time complexity for these two algorithms is $O(n)$, where n is the size of the smallest unordered set¹, and the total time complexity is $O(n)$????????????????, as inserting elements in an unordered set is $O(1)$ (IN THE AVREAGE TIME????).

On the other hand, if we would have used the predefined functions *set_intersection* and *set_union*, we would have needed two ordered set, as it is a precondition of these two functions. Thus, the total cost would have been $O(n * \log(n))$.

Finally, we just have to divide the size of the intersection set by the size of the union set (and multiply by 100 if we want a percentage).

$$Jsim(D_1, D_2) = \frac{intersection.size()}{union.size()} * 100 \quad (6)$$

¹Note that we can change the set we are visiting by the other one. In the intersection, if S_2 is smaller than S_1 , we can visit S_2 . In the union, if S_2 is bigger than S_1 , we can match the unordered set with S_2 and visit S_1 .

6.1.1.1 Cost

The cost of the first algorithm is $O(k * (t - k))$, where k is the k-Shingle value and t is the size of *words*. As k is always a constant, the final cost of this algorithm is $O(k * t - k^2) = O(t)$. The cost of the next two algorithms are $O(n)$, as we have said in the previous section. Finally, the cost of a division and a multiplication is $O(1)$.

Thus, the total cost of calculating the Jaccard Similarity using only k-Shingles is $O(n) + O(t) + O(1) = O(n)$, as usually the number of shingles is much larger than the size of *words*.

6.1.2 Minhash Signatures

We know that implementing just k-Shingling is very expensive in terms of size and time (if we want to compare n documents between them, the complexity is $O(n^2)$). Implementing minhash signatures will help on this a lot. However, the Jaccard Similarity will not be the exact value. To do this, we will use as our input the k-Shingle sets calculated in the previous section.

Require: Two sets S_1 and S_2

Ensure: Returns an approximate Jaccard Similarity value between S_1 and S_2

unordered_set union = $S_1 \cup S_2$

matrix signatures = infinity???????????????????? S'enten que és cada posició?

vector h = all the hash functions we will use

for each row r **do**

for each hash function $h[i]$ **do**

 compute $h[i](r)$;

end for

for each column c **do**

if c has 1 in row r **then**

for each hash function $h[i]$ **do**

if $h[i](r)$ is smaller than $signatures[i][c]$ **then**

$signatures[i][c] := h[i](r)$;

end if

end for

end if

end for

end for

intersection := 0

doc1 := 0

doc2 := 1

for each hash function $h[i]$ **do**

if $signatures[i][doc1] == signatures[i][doc2]$ **then**

if $signatures[i][doc1] != infinity$ **then**

 ++intersection

end if

end if

end for

values b and r , it is very probable that some pair of candidates have less Jaccard Similarity than t . WATCH THE SECTION BLA BLA BLA TO SEE THE NUMBER OF FALSE POSITIVE AND NEGATIVES WE CAN REACH!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!

6.2.1 Cost

The LSH algorithm has two parts. The first one calculates the best possible values of b and r . The second one chooses the candidate pairs of documents.

1. The cost of this part is $O(h)$, where h is the total number of hash functions used in the signature matrix (h is the number of rows of the signature matrix).
2. Let c be the number of documents and b the number of bands. The cost of this part of the algorithm is $O(c * b^2)$. For each band b :
 - For each document compute the hash value of each set of rows of band b . The cost of doing this is $O(c)$, as the computational cost of calculating the hash values is $O(1)$.
 - For each non-empty position of the buckets, create pairs of candidates between all the documents of the bucket without repetitions. This means that documents 3 and 4 will only have one candidate pair (3, 4), and not two (3, 4) and (4, 3). The cost of this for loop is $O(c^2)$, as in the worst case all the documents will be in the same bucket and we will have to make $(c * (c - 1))/2$ candidate pairs.

7 Plots

Tots ESTAN FETS AMB PYTHON! PELS EXPERIMENTS HEM TRIAT ALEATORIAMENT PARELLES DE DOCUMENTS DE 50 PARAULES PERMUTADES ALEATORIAMENT! CODI? ¡- APPENDIX? CADA PLOT AMB 5 MOSTRES

7.1 Jaccard Similarity

7.1.1 k-Shingles

The following plot shows the evolution of the Jaccard Similarity when we vary the value of k .

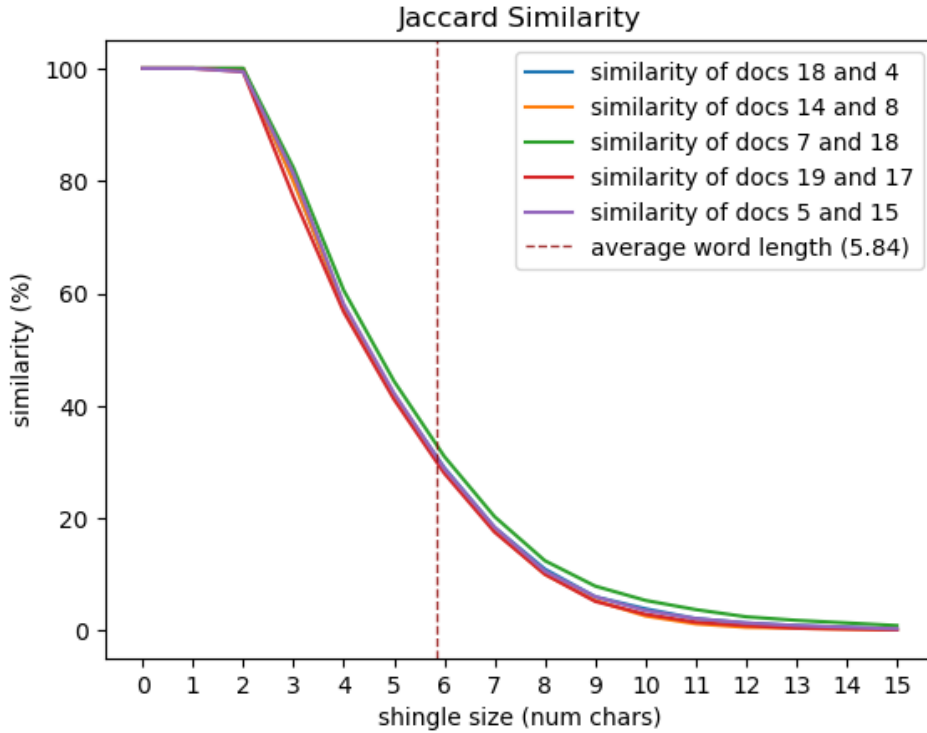


Figure 7.1.1: Jaccard Similarity varying the k value.

As you can see, the Jaccard Similarity of the different pairs is very similar because all the documents are a random permutation of the same 50 words. You can see that because when the shingle size is equal to 1 (we only take the characters), the Jaccard Similarity is 100%³.

Besides, it is important to remark the direction of the graphic. The bigger the shingle size, the lower Jaccard Similarity we get. This is because every time we increase the k value, it is more likely that the substrings start to take some characters of the next word. Thus, the probability that two different documents have the same shingles decreases a lot. You can see that when the shingle size is bigger or equal than 6, we begin to have a very low Jaccard Similarity (less than 20 from $k = 7$) because most of the substrings will have characters of the next words.

Now, we are going to represent the time cost of the same pair of documents when we vary the shingle size.

If we focus on the time cost we can see that the time does not vary at all when we use different shingle sizes. This may be because the documents have the same number of words. Thus, the number of shingles for each document must be very similar to the others.

We should also point that the time to compute the Jaccard Similarity of these pairs of documents is very small because the number of words is very small (50 words are very few compared to the number of words of an article).

³Note that in a document with few words, it is very probable that not all the characters are included in the document.

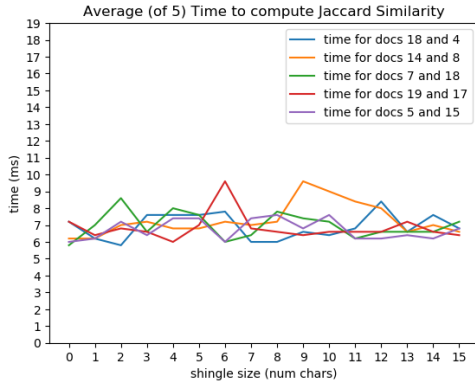


Figure 1: Time to compute the Jaccard Similarity when varying the k value.

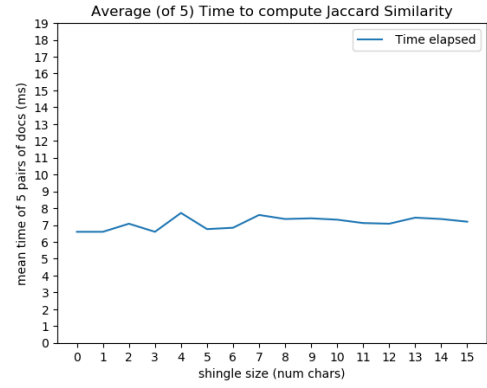


Figure 2: Average time to compute the Jaccard Similarity of the Figure 1.

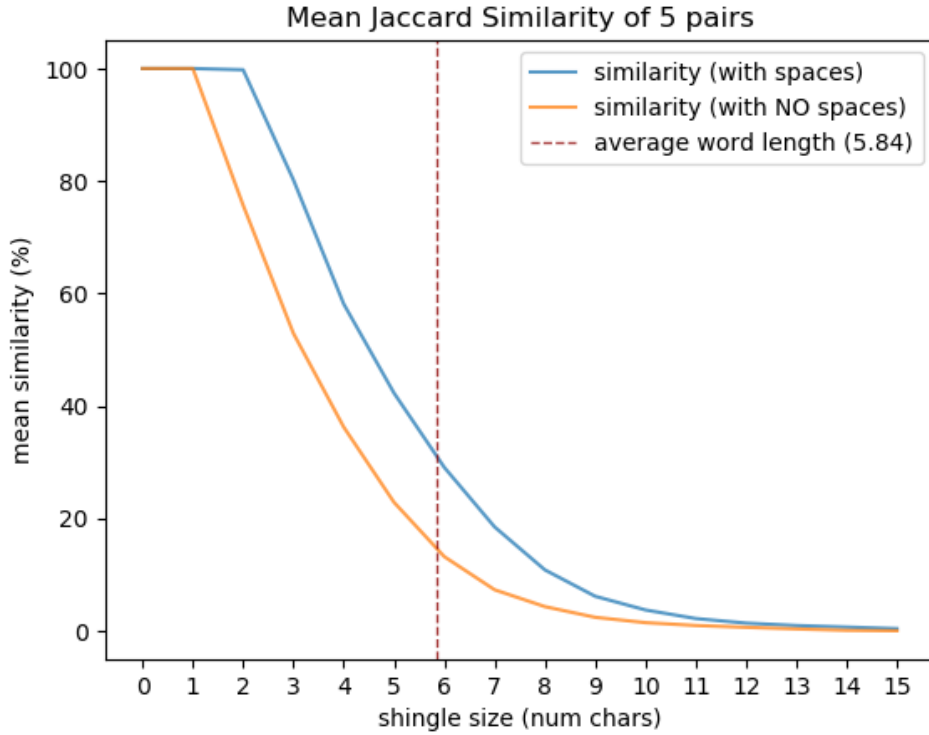


Figure XXXXXXXXXXXX: Time to compute the Jaccard Similarity when varying the k value.

In the following plot we can see the differences between the behaviour of the algorithm taking into account the spaces or not. The blue line (counting spaces) shows that the Jaccard Similarity calculated counting the spaces in the documents is higher than not counting them (orange line). This is due to the difference between the k -shingles created in both algorithms, because if we consider the spaces then we will need a higher k for the substring to start taking characters from the next word.

From now on, we will use spaces to experiment with the documents in the following plots.

We also have put the option to make all characters to lowercase or not. This does not affect on these documents, as all the characters are already in lowercase.

7.1.2 Signature Matrix

7.1.2.1 Using Modular Hashing

In the following plot, it is represented an approximation of the result of calculating the Jaccard Similarity using the signature matrix.

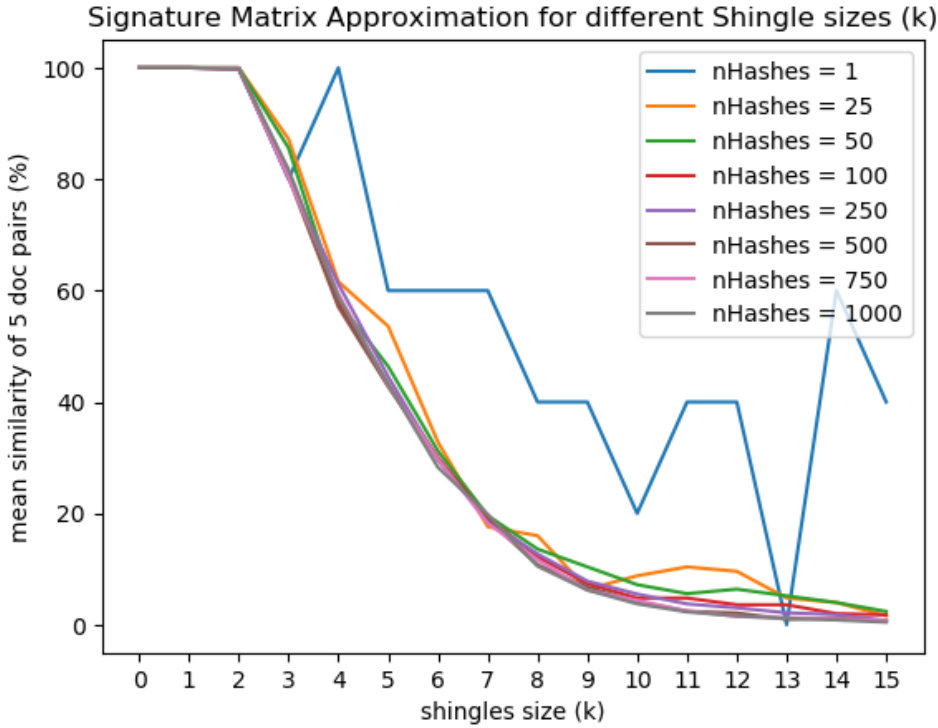


Figure XXXXXXXXXXXXXXXXXXXX: Jaccard Similarity approximation varying the shingle sizes.

The similarity between the documents is strictly related with the number of hashing functions that we use. When the number of hashing functions is a small value it is very different than the Jaccard Similarity, because the signature matrix has few rows and then, there are few chances that one row has the same hash values on two different columns. But when the number of hash functions increases, the functions are more alike to the Jaccard Similarity (Figure YYYYYYYYYYYYYYYYYYYYYYYYYYYY 7.1.1.1.1.1.1.1).

See that when the nHashes is 1, the Jaccard Similarity should only be 100 or 0 per cent, as there is only one row in the signature matrix, but remember that this plot is using the mean value of the result of computing the Jaccard Similarity of 5 pairs using the signature matrix.

Now, we are going to focus on the number of hash functions.

We can see in Figure 3 that the plot form begins to stay stable from number of hash functions equal to 200 more or less. Furthermore, in Figure 4 the time cost starts to increase a lot from number of hash function equal to 250.

Thus, even though using more number of hash function would be better to calculate an approximation of the Jaccard Similarity, it is not usefull to do so because with 200 hash functions we compute a very similar value in less time.

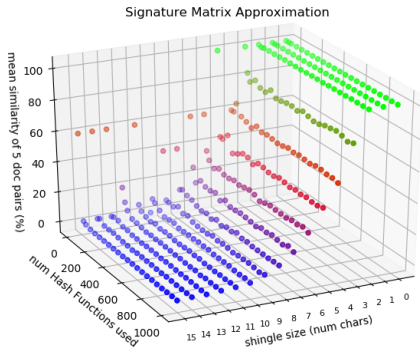


Figure 3: Jaccard Similarity approximation varying the number of hash function and the size of the shingles.

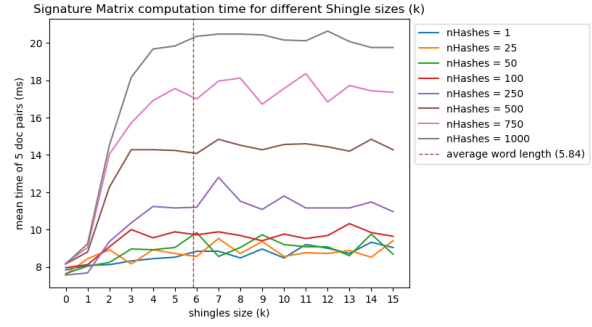


Figure 4: Average time to compute the Jaccard Similarity approximation varying the shingle sizes.

It is important to remark that in Figure 4 the time stabilize near the k equal to the average word length. FALTA AAAAAAAAAAAAAAAAAAAAAAAAAA DIR EL PERQUÈ CREIES QUE PASSA AIXÒ???????????? SI ÉS AIXÍ NO ESTIC MOLT SEGUR DE LA RESPOSTA XD.

In Figures 10, 6 and 7 there is represented how much is the error value obtained using the Jaccard Similarity and the Signature Matrix Approximation. Approximately we can arrive to the same conclusions as the ones that are before. The more number of hash functions, the less the error is.

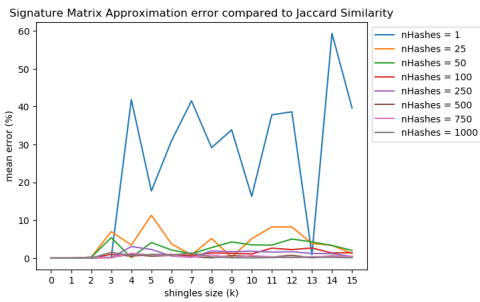


Figure 5: Error between the Jaccard Similarity and the Jaccard Similarity approximated in the signature matrix.

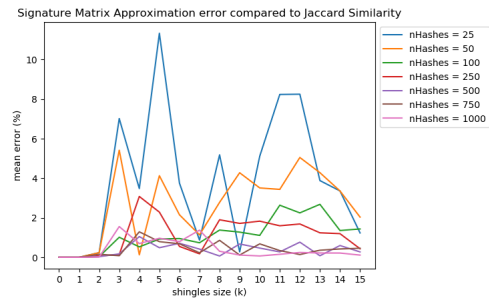


Figure 6: The same than Figure 10 but starting from nHashes = 25.

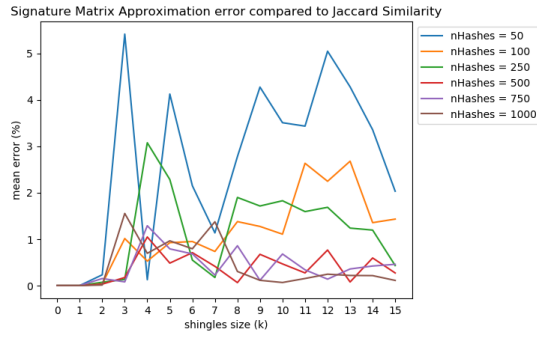


Figure 7: The same than Figure 10 but starting from $nHashes = 50$.

We have put the same plot three times so that you can see more closely the values of the mean error.

7.1.2.2 Using Robert Jenkins' 96 bit Mix Function

We will show the same plots shown in the previous section. If we do not say anything about any plot, it means that it has the same description as the previous section.

Signature Matrix Approximation using Jenkins Hash Fun for different Shingle sizes (k)

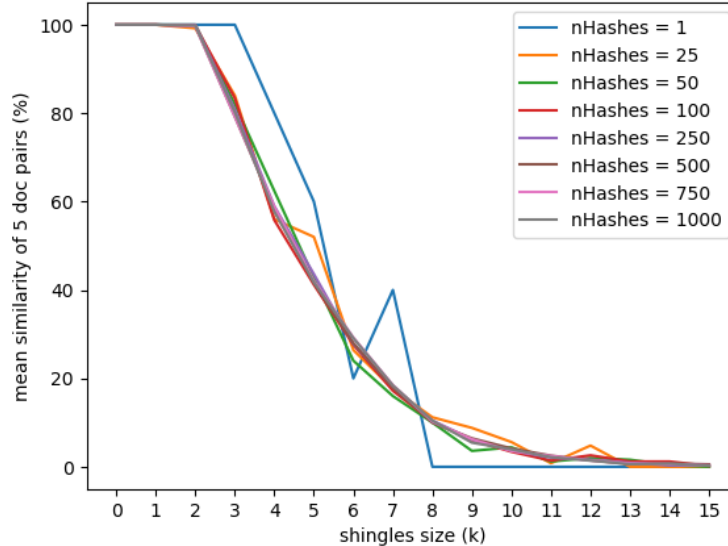


Figure 7.1.2.2: Jaccard Similarity approximation varying the k value.

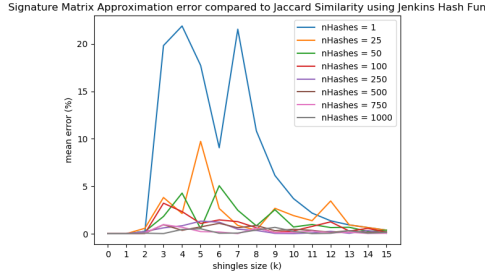


Figure 8: Time to compute the Jaccard Similarity approximation when varying the k value.

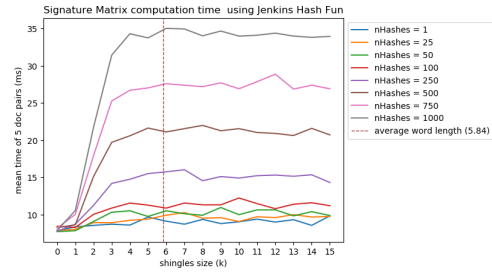


Figure 9: Average time to compute the Jaccard Similarity approximation varying the shingles sizes.

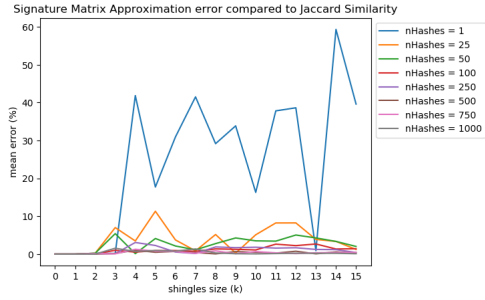


Figure 10: Error between the Jaccard Similarity and the Jaccard Similarity approximated in the signature matrix.

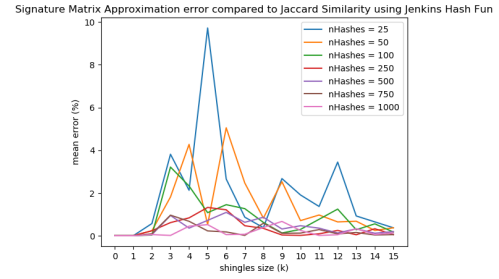


Figure 11: The same than Figure 10 but starting from nHashes = 25.

The only difference we should say is that in the first plot, where the number of hash functions is 1, the function is closer to the rest of number of hash functions, which is what we want.

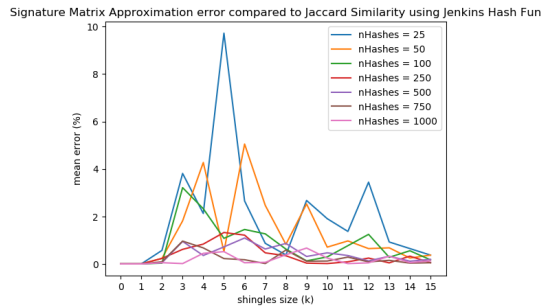


Figure 12: The same than Figure 10 but starting from nHashes = 50.

7.1.2.3 Modular Hashing vs. Robert Jenkins' 96 bit Mix Function

The following plots represent the error using the modular hashing minus the error using the jenkins hashing. If the line is in the positives Y, it means that the error using the modular hashing is greater than the error using the jenkins hashing, and viceversa.

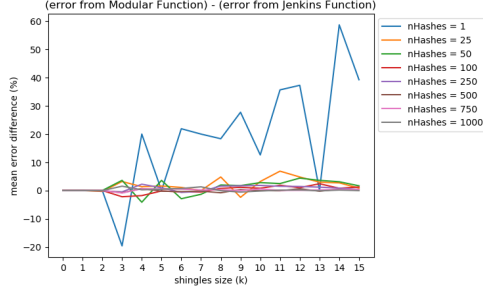


Figure 13: Difference between the error using the modular hashing and the one using the jenkins hashing.

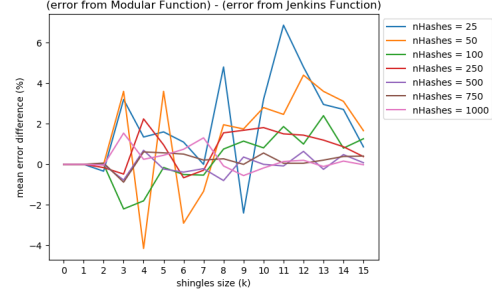


Figure 14: The same than Figure 13 but starting from nHashes = 25.

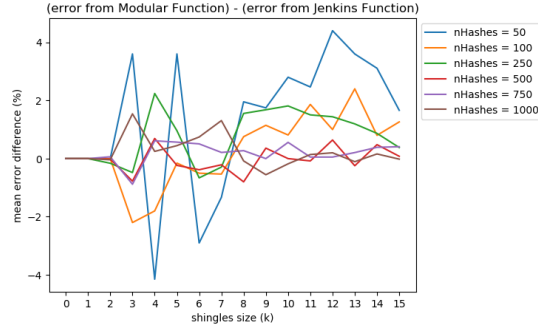


Figure 15: The same than Figure 13 but starting from nHashes = 50.

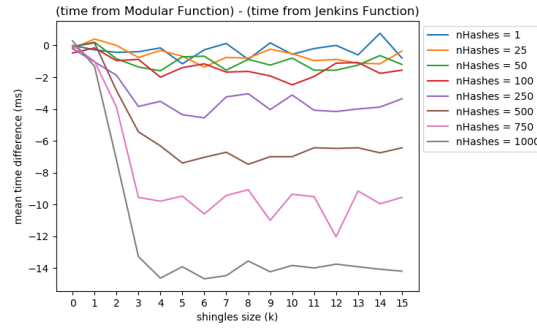


Figure 16: Difference of the time between the modular function and the Jenkins function.

We can see that the error using the modular hashing in Figures 13, 14 and 15 is greater most of the time, specially at the beginning. Thus, the Jaccard Similarity approximation using the Jenkins hashing is better than the one using the modular hashing.

In the Figure 16 we have represented the time cost using modular and Jenkins hashing. If we are in the positive Y, the modular functions spend more time on the algorithm. But we see that it is the contrary: the Jenkins hashing is the one that spends more time even though it has less error than the modular hashing.

References

- [1] Anand Rajaraman, Jure Leskovec and Jeffrey D. Ullman. *Mining of Massive Datasets*. Cambridge University Press. (December 30, 2011).
- [2] cmhteixeira. *Locality Sensitive Hashing (LSH)* [online]. (November 29, 2017). <<https://aerodatablog.wordpress.com/2017/11/29/locality-sensitive-hashing-lsh/>>[Consulted: December 12, 2018].
- [3] Hubert Brylkowski. *Locality sensitive hashing – LSH explained* [online]. (October 6, 2017). <<https://medium.com/engineering-brainly/locality-sensitive-hashing-explained-304eb39291e4>>[Consulted: December 15, 2018].
- [4] Jeffrey D. Ullman[Mining Massive Datasets]. (July 23, 2016). *3 2 Minhashing 25 18*. <<https://www.youtube.com/watch?v=96WOGPUgMfw>>.
- [5] Jeffrey D. Ullman[Mining Massive Datasets]. (July 23, 2016). *3 3 Locality Sensitive Hashing 19 24*. <https://www.youtube.com/watch?v=_1D35bN95Go>.
- [6] santhoshhari. *Locality Sensitive Hashing: Application of Locality Sensitive Hashing to Audio Fingerprinting* [online]. (n. d.). <<https://santhoshhari.github.io/Locality-Sensitive-Hashing/>>[Consulted: December 16, 2018].
- [7] Shikhar Gupta. *Locality Sensitive Hashing: An effective way of reducing the dimensionality of your data* [online]. (June 29, 2018).

<<https://towardsdatascience.com/understanding-locality-sensitive-hashing-49f6d1f6134>>[Consulted: December 16, 2018]