



$$MSE(\theta) = \frac{1}{n} \sum_{i=1}^n (\theta^T x_i - y_i)^2$$

$$\nabla MSE(\theta) = \begin{bmatrix} \frac{\partial MSE(\theta)}{\partial \theta_0} \\ \frac{\partial MSE(\theta)}{\partial \theta_1} \end{bmatrix} = \frac{1}{n} \cdot 2 \cdot (\theta^T x - y) x$$

$\hat{y} = \theta_0 + \theta_1 x_1$
 $[\theta] = \begin{bmatrix} \theta_0 \\ \theta_1 \end{bmatrix}$
 $[\hat{y}] = [x][\theta]$

$x = \begin{bmatrix} 49 \\ 69 \\ 89 \\ 99 \\ 109 \end{bmatrix}$ $y = \begin{bmatrix} 124 \\ 95 \\ 71 \\ 45 \\ 18 \end{bmatrix}$

$[\hat{y}] = [x][\theta]$

$$MSE(\theta) = \frac{1}{n} \sum_{i=1}^n (x_i^T \theta - y_i)^2$$

$$\nabla MSE(\theta) = \begin{bmatrix} \frac{\partial MSE}{\partial \theta_0} \\ \frac{\partial MSE}{\partial \theta_1} \end{bmatrix} = \frac{1}{n} \sum_{i=1}^n (\theta_0 + \theta_1 x_i - y_i)^2$$

$$= \frac{2}{n} (\theta_0 + \theta_1 x_i - y_i) \cdot (x_i)$$

$$\begin{bmatrix} 0 \\ 0 \end{bmatrix} = \frac{2}{n}$$

$\hat{\theta} = \theta - \nabla MSE(\theta) \cdot \alpha$ $\frac{2}{n} (\theta_0 x_0 + \theta_1 x_1 - y) \cdot (x_1)$