

Michigan Teen Smoking and Drug Use Survey Sample Design

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Abstract

1 Introduction

The State of Michigan Department of Education (MDE) requires data to monitor teenage smoking and drug use, partly to assess compliance with tobacco industry settlements. This report details the design of a statewide probability sample of Michigan teenagers (enrolled students in grades 7-12) developed to meet the Department's needs. The objective was to create a cost-effective sample design capable of producing estimates for key variables with desired mean and sampling variance for both the state overall and each of the nine official school regions. Based on cost considerations and a review of alternatives, a two-stage school-based sample design was chosen by the client. We outline in this report the overall design, stratification and allocation plan, selection procedures, and estimation methods. Our budget consist of a total of \$500,000; each school C_n cost \$3,000 and each student C_m cost \$50 to sample.

The MDE is specifically interested in three outcome variables; every smoked one cigarette, every smoked marijuana, and age when first approach to smoke cigarettes or marijuana. Moreover, they provided us with expected levels of precision for the survey in terms of the expected means and coefficient of variation (CV=0.05) which can be seen in Table 1.

Table 1: Key Variables and Desired Levels of Precision

Outcome	Type	Desired CV	Expected Mean
smoked_cig	prop	0.05	0.25
smoked_mj	prop	0.05	0.15
age_approached	mean	0.05	12.00

Given the desired levels of precision, we can compute the desired simple random sample (SRS) sample sizes when $CV = .05$ as $n = \frac{s^2}{se^2}$. We first must calculate the element variance for each key variable. For proportions we use $\hat{p}(1 - \hat{p})$, while for age we simply just square the estimated standard deviation of 1 that was given to us, $v(\bar{y}) = \sigma^2$. We then calculate the standard error as $se(\hat{p}) = CV \times \hat{p}$. Finally, we estimate the desired sampling variance as $var(\hat{p}) = se(\hat{p})^2$, where $se(\hat{p}) = \sqrt{var(\hat{p})}$. We show these results in Table 2, and note that these desired levels of precision would lead to large differences in sample sizes for each target variable. Therefore, we may wish to consider a more complex survey design.

Table 2: Estimating SRS Desired Sample Size

Outcome	Element Variance	SD	SE	Sampling Variables	SRS N
smoked_cig	0.1875	0.4330127	0.0125	0.0001563	1200
smoked_mj	0.1275	0.3570714	0.0075	0.0000562	2267
age_approached	1.0000	1.0000000	0.6000	0.3600000	3

2 Sampling Design

We propose a two-stage stratified cluster sampling as a complex survey sampling method for this project combining stratification with multi-stage cluster sampling. First, the entire population is divided into mutually exclusive and collectively exhausted subgroups called strata, based on shared characteristics relevant to the study (e.g., geographic region). Then, within each of these strata, the first stage of sampling occurs: a random sample of clusters (natural groupings like schools) is selected, and are called primary sampling units (PSUs). In the second stage, a random sample of individual elements known as secondary sampling units (SSUs), such as students, are drawn from within each of the clusters selected in the

first stage. This approach aims to improve sample efficiency and representation by ensuring subgroups are included (i.e., stratification) while reducing costs and logistical challenges associated with sampling individuals across large geographic areas.

The MDE has given us the 2024 7th through 12th grade student headcount for each public and private school within each of the nine regions resulting in a target frame of 830,138 across 2,443 schools (78% Public). Schools in the first stage will be selected with probability proportional to student body size (PPeS). The proportionate allocation $M_h / \sum M_h$ where M_h is the total number of students in stratum h , will be used to determine school number selection in the first stage. Table 3 presents for each of the 9 strata total students, number of schools, and proportionate allocation.

Table 3: Proportionate Allocation Across Strata

Region	Total Student	Total Schools	Proportionate Allocation
1	3561	20	0.0042896
2	5474	30	0.0065941
3	8631	33	0.0103971
4	4855	31	0.0058484
5	18907	80	0.0227757
6	33133	133	0.0399126
7	191992	644	0.2312772
8	188830	549	0.2274682
9	374755	923	0.4514370

We obtained design effects (DEFF) estimates (DEFF_cig=2.5, DEFF_mj=2.0,

DEFF_age=1.7) from a similar pilot study of 7,500 students based on 150 schools with 50 students each, and based on these we estimate the rate of homogeneity roh for each target variable. We use the provided DEFFs to estimate roh as $\hat{roh} = \frac{DEFF-1}{m-1}$, where m is the total sampled students in the pilot study, to consider alternative cluster sample designs along with cost-considerations. Table 4 provides the roh estimate for each target variable.

Table 4: We Use Pilot Study DEFFs to Estimate roh

Outcome	DEFF	roh
smoked_cig	2.5	0.0306122
smoked_mj	2.0	0.0204082
age_approached	1.7	0.0142857

2.1 Sampling Within Budget

Recall that our budget cost constraints as the cost per cluster as $c_n = \$3,000$ and cost per student as $c_m = \$50$, with a total budget constraint of $C = \$500,000$. We can use the roh estimates along with these costs to estimate the optimum subsample size m_{opt} needed to achieve the desired precision as $m_{opt} = \sqrt{\frac{c_n}{c_m} \frac{1-roh}{roh}}$. Note that since we have three target variables we also have three separate roh estimates and thus three m_{opt} estimates. Similarly, we can use m_{opt} to estimate the number of schools n_{opt} to sample, $n_{opt} = \frac{C}{c_n + m_{opt} \times c_m}$. Finally, we compute new DEFF for each variable as roh is portable and since we already computed m_{opt} as $DEFF_{new} = 1 + (m_{opt} - 1) \times roh$. By multiplying $m_{opt} \times n_{opt}$ for each variable we also get the total subsample size, as well as compute the total cost using $n_{opt} \times c_n + n_{opt} \times m_{opt} \times c_m$. Table 5 shows for each target variable m_{opt} , n_{opt} , $DEFF_{new}$,

total subsample size denoted by $total_{nm}$, and the total cost. Notice that our $DEFF_{new}$ estimates are close to those from the pilot study since again we used these to compute roh which is portable for estimating new design effects.

Table 5: Estimating New DEFF and Total Cost

Outcome	m_opt	n_opt	deff_new	total_nm	cost	Option
smoked_cig	43.58899	96.53536	2.303745	4207.879	\$500,000	1
smoked_mj	53.66563	87.97734	2.074809	4721.360	\$500,000	2
age_approached	64.34283	80.42281	1.904898	5174.631	\$500,000	3

2.2 Evaluating Alternative Clustering Designs

We are left with a dilemma since we now have three subsample sizes that we can use, thus giving us three clustering design options to choose from. Using the m_{opt} values from table 5 as our three options, we iterate over each set of three target variables using these values to recompute for each target variable a new design effect and evaluate the estimated sampling variance for each design. We estimate the SRS sampling variance as $var_{srs} = \frac{var}{total_{nm}-1}$ where var is the sampling variance calculated from the pilot study and the denominator is the degrees of freedom. Additionally, we estimate the sampling variance for the clustering design as $var_{crs} = var_{srs} \times deff_{new}$. After estimating var_{crs} , we can square it to estimate a standard error, $se = \sqrt{var_{crs}}$ to use to estimate 95% confidence intervals for the estimated means. Additionally, in our evaluation of m_{opt} we can determine if the estimated sampling variance from the complex design is smaller than what is desired from MDE, therefore Table 6 shows sampling variances, standard errors, confidence intervals, and a variance check (e.g., “Y” = yes if \leq to desired sampling variance) for each target variable using

the m_{opt} options in Table 5.

Table 6: Evaluating Alternative Clustering Designs

Outcome	Option	deff_new	var_srs	var_crs	se	lower	upper	var_ck
smoked_cig	1	2.303745	0.000057	0.000131	0.011464	0.227530	0.272470	Y
smoked_mj	1	1.869163	0.000030	0.000057	0.007527	0.135248	0.164752	N
age_approached	1	1.608414	0.002139	0.003441	0.058660	11.885027	12.114973	Y
smoked_cig	2	2.612213	0.000051	0.000133	0.011525	0.227412	0.272588	Y
smoked_mj	2	2.074809	0.000027	0.000056	0.007486	0.135327	0.164673	Y
age_approached	2	1.752366	0.001907	0.003341	0.057802	11.886707	12.113293	Y
smoked_cig	3	2.939066	0.000046	0.000136	0.011676	0.227114	0.272886	Y
smoked_mj	3	2.292711	0.000025	0.000057	0.007517	0.135267	0.164733	N
age_approached	3	1.904898	0.001740	0.003314	0.057565	11.887172	12.112828	Y

Upon evaluation of options from Table 6, we determine that option 2 has reasonable estimated design effects comparable to those from the pilot study as well as it is the only option to pass the estimated sampling variance check we designed. Option 2 with $m_{opt} = 53, n_{opt} = 88$ would cost a total of \$497,200. Since the total student population is 830138 and our now target sample is 4721 we can estimate the sampling fraction to be $f = n/N = 0.0056874$. The sampling fraction is the ratio of the sample size to the population size, and this estimate translates to the sample comprises approximately 0.57% of the total student population. In this case, the sampling fraction is low and the finite population correction factor is not needed for calculating variances to adjust for the fact that sampling without replacement from a finite population reduces variability compared to sampling from an infinite population.

2.3 Non-response Adjustments

The MDE anticipates 30% school response rates and 70% among students; therefore, we adjust the number of schools and within-school target by multiplying $m_{opt} \times RR_{student} = 53 \times .70 = 76.6651878$ students and for schools $n_{opt} \times RR_{schools} = \times .30 = 293.2578028$. We use these values to allocate the number of clusters for each strata based on the proportion allocated we calculated.

3 Stage 1 Selection

We consider stratified PPeS selection of schools from each strata by first sorting the list of schools to achieve implicit stratification. How we sort is by taking the number of 9th through 12th grade for each school divided by the total student body and descend order, and in this way we hypothesize that schools with older students are more likely to be positively associated with the target variables. For each strata h we assign our adjusted $n_{opt} \times proportionate_allocation$ estimated earlier to calculate the number of schools to sample, denoted as n_h in Table 7. We use n_h to calculated in this Table the sampling interval $k_h = \frac{\sum_{i \in h} MOS_{hi}}{n_h}$ where MOS_{hi} is the measure of size, total student head-count, for each school i in strata h . The k_h parameter is an important component of systematic sampling to determine how frequently units are selected from an ordered list. To conduct this selection, we randomly select a number between 1 and k_h for selecting schools from the list, which is captured in Table 7 as RN .

Table 7: Evaluating Alternative Clustering Designs

Region	prop_allocation	n_h	f_h	k_h	RN
1	0.0042896	1.257973	1.257973	3561.000	3168
2	0.0065941	1.933767	1.933767	2737.000	2310
3	0.0103971	3.049021	3.049021	2877.000	1321
4	0.0058484	1.715096	1.715096	2427.500	131
5	0.0227757	6.679161	6.679161	2701.000	2122
6	0.0399126	11.704693	11.704693	2761.083	2114
7	0.2312772	67.823846	67.823846	2823.412	374
8	0.2274682	66.706826	66.706826	2818.358	380
9	0.4514370	132.387420	132.387420	2839.053	1673