

HomeWork -1

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2) What Types of Machine learning ?

- a) Supervised Learning in inferred. As learning isn't by algorithm as it's from pre-defined statistical feed.
- b) Supervised learning.
- c) Semi Supervised
- d) Un supervised
- e) Reinforcement learning. Here system takes the feedback from its moves, accordingly rewards and penalises it position to counter opponent.

3) answer is 0.666666667

explanation :

$$5) P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$\Rightarrow P(B) = (1)\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right) \cdot \left(\frac{1}{2}\right) = 3/4.$$

$$\Rightarrow P(A \cap B) = (1)\left(\frac{1}{2}\right) + (0)\left(\frac{1}{2}\right) = 1/2.$$

$$\therefore P(A|B) = \frac{1/2}{3/4} = 2/3 \approx 0.66.$$

4th)

(4) Given the sample of 10, drawn with a replacement, The probability of no red is $(0.35)^{10}$

$$\therefore P = 2.758547354 \times 10^{-5} //$$

(a) From above probability of no red happening in any trial is $1 - P$. The probability that event shouldn't occur over 1000 times is $(1 - P)^{1000}$

So, probability for at least once is $1 - [(1 - P)^{1000}]$

$$(b) = 1 - (0.9999724145^{-1000})$$

$$= 1 - (0.9727911609)$$

$$= 0.02720883906 //$$

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| x_n | y_n |
|-------|-------|
| 0 0 0 | 0 |
| 0 0 1 | 1 |
| 0 1 0 | 1 |
| 0 1 1 | 0 |
| 1 0 0 | 1 |
| 1 0 1 | |
| 1 1 0 | |
| 1 1 1 | |

possible f values

| b_1 | b_2 | b_3 | t_4 | t_5 | t_6 | t_7 | t_8 |
|-------|-------|-------|-------|-------|-------|-------|-------|
| 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 |
| 0 | 0 | 1 | 1 | 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 |

$$\begin{aligned}
 \text{(a) score} &= 1 \times 3 + 3 \times 2 + 3 \times 1 + 0 \\
 &\quad \uparrow \quad \quad \uparrow \quad \quad \uparrow \\
 &\quad b_3 \quad \quad b_2, t_6, t_4 \quad \quad b_2, t_3, t_5 \\
 &= 12.
 \end{aligned}$$

$$\begin{aligned}
 \text{(b) score} &= 1 \times 3 + 3 \times 2 + 3 \times 1 + 0 \\
 &\quad \uparrow \quad \quad \uparrow \quad \quad \uparrow \\
 &\quad b_1 \quad \quad b_2, b_3, t_5 \quad \quad b_4, t_6, b_7 \\
 &= 12.
 \end{aligned}$$

(c) ~~score~~ g is the XOR function, returns 0, 0, 1

$$\begin{aligned}
 \therefore \text{score} &= 1 \times 3 + 3 \times 2 + 3 \times 1 + 0 \\
 &= 12.
 \end{aligned}$$

(d) g is the inversion of XOR function, which returns 1, 1, 0

$$\begin{aligned}
 \therefore \text{score} &= 1 \times 3 + 3 \times 2 + 3 \times 1 + 0 \\
 &= 12.
 \end{aligned}$$

6) Exercise 1.3 from textbook solution

6) Exercise 1.3 solution:

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(a) Show that $y(t)w^T(t)x(t) < 0$

here $x(t)$ is misclassified by $w(t)$
so $y(t) \neq \text{sign}(w^T(t)x(t))$

This means $w^T(t)x(t)$ is having sign
opposite of $y(t)$

$$\therefore y(t)w^T(t)x(t) < 0$$

(b) Show that $y(t)w^T(t+1)x(t) > y(t)w^T(t)x(t)$
considering updated weight rule
 $w(t+1) = w(t) + y(t)x(t)$
misclassified value be $y(t)x(t)$

$$\Rightarrow y(t)x(t)(w^T(t+1)) \\ = y(t)[w^T(t) + y(t)x(t)] \cdot x(t)$$

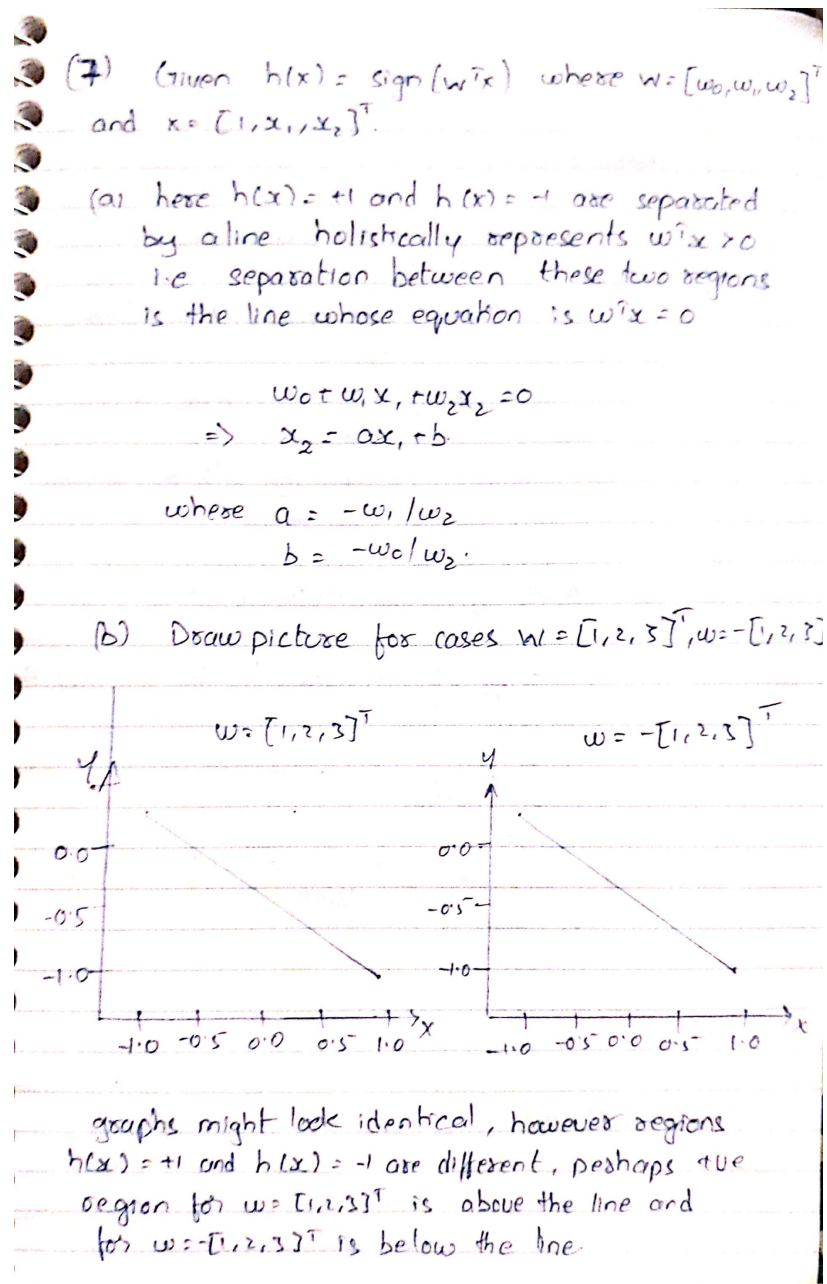
$$= [y(t)w^T(t) + y^2(t)]x(t)$$

$$= y(t)w^T(t)x(t) + y^2(t)|x(t)|^2$$

as $y^2(t)|x(t)|^2$ results +ve component

$$y(t)w^T(t+1)x(t) > y(t)w^T(t)x(t)$$

(c) As far as classifying $x(t)$ is concerned, argue that
the move from $w(t)$ to $w(t+1)$ is a move in right direction.
From a and b it clearly indicates PLA algorithm
increases $y(t)w^T(t)x(t)$ until it crosses 0, thus
 $|x(t), y(t)|$ are no longer misclassified.



8th and 9th solutions are attached as part of ipynb files uploaded along with this file.

10th)

10)

Supermarket:

$$\begin{aligned} E_{in}^{(s)}(h) &= \frac{1}{N} \sum_{n=1}^N e(h(x_n), f(x_n)) \\ &= \frac{1}{N} \left(\sum_{y_n=1} e(h(x_n), 1) + \sum_{y_n=-1} e(h(x_n), -1) \right) \\ &= \frac{1}{N} \left[\sum_{y_n=1} 10 \cdot [h(x_n) \neq 1] \right. \\ &\quad \left. + \sum_{y_n=-1} [h(x_n) \neq -1] \right] \end{aligned}$$

CQA:

$$\begin{aligned} E_{in}^{(c)}(h) &= \frac{1}{N} \sum_{n=1}^N e(h(x_n), f(x_n)) \\ &= \frac{1}{N} \left[\sum_{y_n=1} e(h(x_n), 1) + \sum_{y_n=-1} e(h(x_n), -1) \right] \\ &= \frac{1}{N} \left[\sum_{y_n=1} [h(x_n) \neq 1] \right. \\ &\quad \left. + \sum_{y_n=-1} 1000 \cdot [h(x_n) \neq -1] \right] \end{aligned}$$