

# Flexible-C<sup>m</sup> GAN: Towards Precise 3D Dose Prediction in Radiotherapy

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## Abstract

Deep learning has been utilized in knowledge-based radiotherapy planning in which a system trained with a set of clinically approved plans is employed to infer a three-dimensional dose map for a given new patient. However, previous deep methods are primarily limited to simple scenarios, e.g., a fixed planning type or a consistent beam angle configuration. This in fact limits the usability of such approaches and makes them not generalizable over a larger set of clinical scenarios. Herein, we propose a novel conditional generative model, Flexible-C<sup>m</sup> GAN, utilizing additional information regarding planning types and various beam geometries. A miss-consistency loss is proposed to deal with the challenge of having a limited set of conditions on the input data, e.g., incomplete training samples. To address the challenges of including clinical preferences, we derive a differentiable shift-dose-volume loss to incorporate the well-known dose-volume histogram constraints. During inference, users can flexibly choose a specific planning type and a set of beam angles to meet the clinical requirements. We conduct experiments on an illustrative face dataset to show the motivation of Flexible-C<sup>m</sup> GAN and further validate our model's potential clinical values with two radiotherapy datasets. The results demonstrate the superior performance of the proposed method in a practical heterogeneous radiotherapy planning application compared to existing deep learning-based approaches.

## 1. Introduction

Radiation therapy (RT) is an essential modality for cancer treatment and is applicable to about 50% of patients [12, 25]. However, many studies demonstrate that millions of patients currently do not have access to radiotherapy due to limited infrastructures and trained experts to handle complex planning procedures [15, 20, 59].

RT treatment planning is a process that involves a multi-disciplinary team (e.g., oncologists, therapists, physicists) to figure out the treatment beam configurations and intensity for cancer patients [25]. The modern RT treatments can be

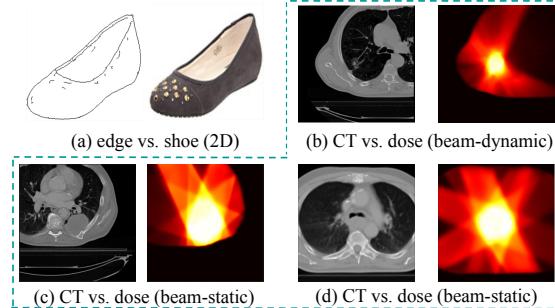


Figure 1. Vanilla image-to-image translation (a) and dose prediction (b)-(d). (a) has a clear shape match between the source and target domains. (b)-(d) illustrate our challenges, including heterogeneous patterns, no clear match between source and target, and 3D data (showing 2D for simplicity) is harder than 2Ds.

divided into two broad categories using static- or dynamic-beams. The intensity modulated radiotherapy (IMRT) [56] and volumetric modulated arc therapy (VMAT) [48, 57] are the most common static- and dynamic- beam types, respectively [10]. IMRT uses several personalized but fixed beam angles, delivering radiation precisely to the tumor while sparing the surrounding normal tissues according to the location of the tumor and anatomical organs at risk (OARs). During VMAT, the treatment beam is on while its treatment head is moving on an arc trajectory [10]. As shown in Figure 1, the dose maps of static- and dynamic- beam RT plans can look significantly different, which results from different delivery nature energy fluences in those two modes. Moreover, even using the same planning mode, different configurations (e.g., beam angles, isocenter) are needed for different patients due to different tumor locations/shapes, anatomy structures, and other clinical parameters.

Knowledge-based planning (KBP) aims to use computer technologies to reduce the time for individualized treatment plans [6, 43]. Historically, KBP technologies relied on statistical models or handcrafted features [46, 54]. While providing promising results, these methods are hard to generalize beyond an inherently targeted limited set of scenarios [33]. Advanced artificial intelligence (e.g., deep learning [37]) has shown great potential to alter the way oncology therapies are administered [25, 53]. An integral part of

KBP methods is to predict the dose distribution that should be delivered to a patient [6,32,59]. Three-dimensional (3D) deep learning models have been applied in dose map prediction across different cancers [7,32,33,41,45,55] where the inputs are generally computed tomography (CT) image/volume and masks of organs at risk (OARs) / planning target volume (PTV). However, the existing automatic dose prediction models mainly focus on relatively simple scenarios, e.g., single planning mode or/and consistent angle configuration, which significantly limits the model flexibility.

In this paper, we propose a novel conditional generative model, flexible-multiple-condition GAN, short for Flexible-C<sup>m</sup> GAN or FCGAN, for precise 3D dose prediction in heterogeneous RT contexts. In addition to the conditions (CT, PTV/OAR masks) that other methods in literature have used, we further integrate two conditions: the planning mode (i.e., static- or dynamic- beam) and the angle configuration. Furthermore, we show that our model is robust in those scenarios where angle configuration may not be available. Briefly, our contributions include

- We proposed a novel GAN variant, FCGAN, that considers multi-level conditions and handles missing condition values with a new miss-consistency loss.
- We derived a *differentiable* and *spatially-unbiased* loss function from a widely applied dose-volume histogram and show its effectiveness within the deep learning training for 3D dose prediction.
- We introduced the deep 3D dose prediction for practical heterogeneous treatment scenarios (i.e., multi-type, multi-beam configuration), which enables easy and fast user-interaction by changing input conditions and checking results interactively during inference.
- We conducted experiments on two clinical radiotherapy datasets and a face dataset, validating that our approach is superior to state-of-the-art deep models.

## 2. Related Work

**RT Dose Planning.** There are mainly two branches of dose prediction models: (1) handcrafted dose-volume (DV) feature-based and (2) deep learning-based. In the first branch, the dose-volume statistical models are mainly based on conventional machine learning or statistics at low-dimension feature bases [2, 3, 14, 29]. The cumulative dose-volume frequency distributions [13], simply as dose-volume histograms (DVHs), have been used for evaluation in both traditional models and recently deep learning models [14]. RapidPlan™ is a commercial KBP tool developed by Varian Medical Systems (Palo-Alto, CA), which is using DVHs as the feature set, and allows clinical objectives to be automatically inferred from previous plans [1]. Furthermore, the user is enabled to modify and integrate clinical

objectives into the iterative optimization pipeline to create a plan for a new patient [1, 16, 35].

Recently, 3D-based image models (especially UNet-based networks) have been adapted in dose map prediction for different cancers, such as in prostate [32, 33, 45], head-and-neck [41, 55, 58], esophageal [4, 64], and lung [7, 27]. Most of them use reconstruction (e.g., L1 or L2) or/and DVH-based losses to train the 3D dose prediction model in a single-mode context (e.g., only IMRT). For example, Kearney et al. [32] apply a fully convolutional neural network to predict the dose map. A cascaded 3D U-Net [41] has achieved the best performance in a KBP challenge of IMRT on head-and-neck cancer [6]. Vanilla adversarial losses [19, 26] are used with reconstruction loss to make the predicted dose more realistic [4, 33, 45]. Soomro et al. [55] extend [45] with a dilated DenseNet for head-and-neck cancer but in a narrow scenario of equidistant static beams.

**Conditional GAN and I2I Translation.** Generative adversarial nets (GANs) [19] have been successful in generating realistic images [8, 9, 21, 36]. However, there is no control on generated samples for vanilla GAN. Conditional GAN [44] provides a solution to guide the generation by feeding additional information, which has been widely explored in general computer vision such as image-to-image translation [11, 18, 26, 50, 65], text-to-image generation [49], and image imputation [38, 40]. Conditional GANs have also been extended to medical imaging addressing specific healthcare problems with some necessary modifications [63], such as CT-to-MRI translation [24], disease diagnosis or image segmentation after data imputation [17, 28].

Dose prediction can be formulated broadly as image-to-image translation (I2I), while it is significantly different from the well-known ones, as illustrated in Figure 1. Simple I2I translation usually shares similar structures between the source and target domains, e.g., edges to color image [26, 65] (as in Figure 1a), and MRI to CT [24]. The source (CT/masks) has a relatively weak connection and no unique mapping to the target (i.e., dose map) in the practical heterogeneous contexts (as in Figures 1b, 1c, and 1d).

## 3. Methodology

### 3.1. Problem Description and Motivation

In order to obtain precise individualized RT plans, three types of data are needed: (1) planning mode (static- or dynamic- beams), (2) beam angle configuration, and (3) fluence map for each beam, which determines the beam shape and intensity. (1) and (2) are relatively easy to tune in a human-computer interaction system, while obtaining (3) is labor-intensive and time-consuming. A typical target of the KBP pipeline, as in Figure 2, is to obtain the fluence map for each beam (or subfield), given the planning mode and beam angle configuration. There are two main steps to ob-

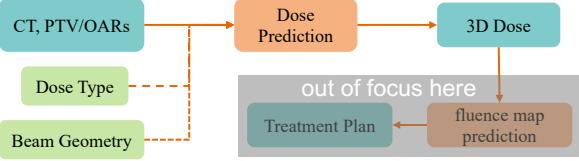


Figure 2. Overview of a typical KBP pipeline. The teal blocks are inputs or outputs, the orange blocks are algorithm modules, and the green ones are the introduced flexible conditions.

tain final fluence maps [5, 6, 61, 62]: (1) dose prediction, and (2) fluence map prediction when given the predicted dose map. As the first and essential step, the dose prediction is the main focus of this paper.

In most dose prediction models via deep learning (e.g., [4, 32, 33, 45, 64]), the inputs (i.e., source) are the computed tomography (CT) image/volume, the organ at risk (OAR) masks, and planning target volume (PTV) mask. However, the dose map (i.e., target) lacks clear structure or texture information from the source. Furthermore, the reference dose, used as ground truth during training, is subjective and can biased as it is designed by a group of expert humans. It is less challenging if 1) the planning context is simple such as using the same dose type or/and the same beam angles; 2) the relative locations of PTV and OARs are nearly consistent for some cancers, such as in prostate cancer and head-and-neck. However, in clinical practice, specialists may need to consider which dose types should be delivered (e.g., beam-static or beam-dynamic) and the suitable set of beam angles. Tumors in some cancers (e.g., lung cancer, liver cancer) can vary in a large range of locations within the host organ, resulting in the relative positions of PTV and OARs being largely heterogeneous.

We argue that two key points need to be addressed for precise dose prediction: individualism and realism. *Individualism* is required for the plan to be precise specifically in heterogeneous set of conditions. *Realism* makes the subsequent tasks (e.g., fluence map prediction [39, 42, 62], deliverable dose [5]) more manageable. GANs have been specifically useful in generating realistic samples, and their conditional versions allow additional restrictions and constraints which could be beneficial in our task. Conditional GAN [44] is defined as min-max game of discriminator  $D$  with generator  $G$  using following loss:

$$V(D, G) = \mathbb{E}_{x \sim p_{data}} [\log D(x|y)] + \mathbb{E}_{z \sim p_z(z)} [\log(1 - D(G(z|y)))] \quad (1)$$

where  $G$  generates samples based on the condition  $y$  and random noise  $z$ . A simple conditional GAN [44] can not satisfy our use-case as we need to handle (1) multi-level conditions with heterogeneous types and (2) missing conditions during training and testing.

### 3.2. Flexible-C<sup>m</sup> GAN Mechanism

We describe the general methodology of Flexible-C<sup>m</sup> GAN in this section, and the instantiation for 3D dose prediction is shown in Sec. 3.3. Math symbol explanations of our model are in Supplement A.

Given  $M$  conditions  $\{C^i\}_{i=1}^M$  (i.e.,  $\mathbf{C}$ ) and their missing indicators  $\mathbf{m}$  ( $m^i = 0$  if  $i$ -th condition is missing, otherwise  $m^i = 1$ ), our adversarial loss becomes:

$$V(D, G) = \mathbb{E}_{x \sim p_{data}} [\log D(x|\mathbf{C}, \mathbf{m})] + \mathbb{E}_{z \sim p_z(z)} [\log(1 - D(G(z|\mathbf{C}, \mathbf{m})))] \quad (2)$$

The  $i$ -th missing condition is imputed with default or random values (termed as  $\bar{C}^i$ ). To let the model be robust to the missing condition, we introduce a miss-consistency loss  $L_{mc}$  based on condition regularization loss  $L_{cr}$ :

$$L_{cr} = \sum_{i, m^i > 0} L^i(E^i(G(z|\mathbf{C}, \mathbf{m})), \cdot), \quad (3)$$

$$L_{mc} = \sum_{j \neq i, m^j > 0} |E^j(G(\cdot|m^i = 0, \cdot)) - E^j(G(\cdot))|. \quad (4)$$

where  $E^i(\cdot)$  extracts feature from the prediction  $G(\cdot)$  for the condition  $C^i$ .  $L^i(\cdot, \cdot)$  measures the discrepancy between the prediction and the reference corresponding to  $C^i$ , and  $L_{mc}$  reflects how predictions related to observed condition  $j$  are consistent when another condition  $i$  is given versus the scenario in which it is missing.

### 3.3. FCGAN Instantiation for 3D Dose Prediction

#### 3.3.1 3D Dose Prediction Framework

Our overall framework for 3D dose prediction is illustrated in Figure 3. The input includes CT, PTV/OAR masks, planning mode (beam-static or beam-dynamic), angle/beam plates, and a condition mask indicating if any condition is missing. The angle/beam plates computation and detailed generator  $G$  structures are described in Supplement D.

For three-dimensional conditions (CT, PTV/OARs masks, angle/beam plates), the condition regularization terms of Eq. 3 (related  $E^i$  is *Identity*) are jointly covered by a reconstruction loss  $L_{rec}$  and shift-dose-volume (SDV) loss  $L_{sdv}$ . The  $L_{rec}$  of  $N$  samples is the mean absolute error (MAE) of the reference dose  $\mathbf{Y}_i$  and its prediction  $\hat{\mathbf{Y}}_i$ :

$$L_{rec} = \frac{1}{N} \sum_{i=1}^N \|\mathbf{Y}_i - \hat{\mathbf{Y}}_i\|_1. \quad (5)$$

The details of  $L_{sdv}$  are shown in Sec. 3.3.2.

Inspired by [17, 47] with categorical condition, we introduce the cross-entropy loss (CEL) to instantiate Eq. 3 (related  $E^i$  is the pre-trained encoder in Figure 3) for the planning mode condition  $C^m$ :

$$L_{cls} = \frac{1}{N} \sum_{i=1}^N -C_i^m \log(\hat{p}_i) - (1 - C_i^m) \log(1 - \hat{p}_i). \quad (6)$$

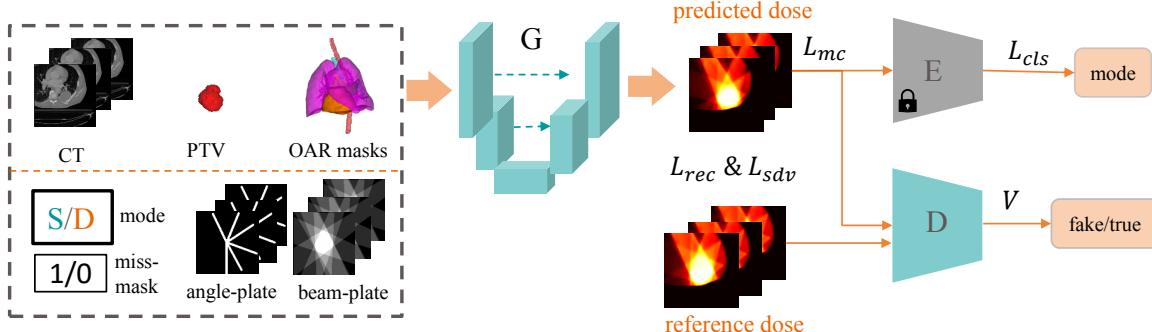


Figure 3. Flexible-C™ GAN for 3D dose prediction. CT, PTV/OAR masks, mode, angle/beam plates, and miss-mask are fed into a U-shape-based Generator ( $G$ ) to predict dose maps. Note that the condition can be missing, indicated by the missing indicator. Reconstruction loss ( $L_{rec}$ ) and SDV loss ( $L_{sdv}$ ) minimize the discrepancy between predicted and reference doses from different perspectives. With a pre-trained encoder ( $E$ ),  $L_{cls}$  regularizes the mode of predicted dose.  $L_{mc}$  enforces prediction consistency of one condition whether another condition is missing or not, and  $V$  is the GAN loss to achieve realistic prediction.

Thus, the total FCGAN loss for 3D dose prediction is:

$$L_{total} = V + 3L_{rec} + L_{cls} + L_{sdv} + L_{mc}, \quad (7)$$

where the adversarial loss  $V$  follows Eq. 2, and  $\mathbf{C}$  includes three types of condition: (1) CT and PTV/OAR masks, which are also used by previous methods, e.g., [6, 41, 45], (2) planning mode, and (3) angle/beam plates. The ratio of  $L_{rec}$  is set relatively larger to avoid the error is overwhelmed by small/zero dose voxels. The first three items are common in various conditional GANs [17, 19, 41, 47]. The last two losses ( $L_{sdv}$  and  $L_{mc}$ ) are our contributions, and we have a set of ablation studies to validate their effectiveness.

### 3.3.2 Shift-Dose-Volume Loss

Original DVH [13] is not differentiable (for error back-propagation) and can be sub-optimal from a spatial view. Several DVH-based loss functions have been proposed for dose prediction training [27, 45, 58]. The majority of those methods are empirically designed based on the computation of DVH, e.g., approximate *Sign* function with *Sigmoid* function. Differently, we derive a new DVH-based loss from DVH definition by shifting histogram errors to their voxel space, which holds a mathematical connection between the differentiable loss function and original DVH.

Assume the max dose is  $D_T$  and there are  $T$  bins with unique widths for the DVH. So, the bin width is  $w = \frac{D_T}{T}$ . Given a region of interest (ROI, i.e., PTV or OAR) mask  $M$  (as the teal region in Figure 4b), according to DVH definition: the fractional volume  $f(D_t)$  (y-axis) at t-th threshold  $D_t$  (x-axis) is  $f(D_t) = \frac{\sum_j \mathbb{1}(Y_j - D_t) M_j}{\sum_j M_j}$ , where  $j$  is voxel index and  $t = \frac{T D_t}{D_T}$  is bin index of  $D_t$ , as in Figure 4a.

Let us denote voxel indexes of  $t$ -th bin as  $\mathbf{M}_t$  (as the orange in Figure 4a). To minimize the error from a DVH perspective, we want errors of each bin to be minimized, and we shift the error measurement of each bin to the error of voxels that contribute to the fractional volume  $f(D_t)$ .

**Definition 1.** The shift-dose-volume loss  $L_{sdv}^t$  of each bin  $[D_t, D_t + \frac{D_T}{T}]$  is the absolute error  $\varepsilon(\cdot)$  of all voxels that contribute to  $f(D_t)$  multiply the bin width  $w$ , i.e., expected error of  $f(D_t)$  from voxel perspective. The  $L_{sdv}$  of each ROI is the sum of each bin  $L_{sdv}^t$ , i.e.,  $\sum_{t=1}^T L_{sdv}^t$ .

Given referenced dose  $\mathbf{Y}$ , we have:

$$\begin{aligned} \sum_j M_j \sum_{t=1}^T L_{sdv}^t &= \sum_{t=1}^T \sum_j \mathbb{1}(Y_j - D_t) \cdot \varepsilon(Y_j \cdot M_j) \cdot w \\ &= \sum_{t=1}^T \varepsilon(\mathbf{Y} \odot (\mathbf{M}_t + \dots + \mathbf{M}_T)) \cdot w \\ &= \sum_{t=1}^T t \cdot \varepsilon(\mathbf{Y} \odot \mathbf{M}_t) \cdot w = \sum_{t=1}^T D_t \cdot \varepsilon(\mathbf{Y} \odot \mathbf{M}_t), \end{aligned} \quad (8)$$

where  $\odot$  is the Hadamard product. When  $T$  is large enough to make every  $Y_j \in [D_t, D_t + \frac{D_T}{T}]$  indexed by  $\mathbf{M}_t$  is close to  $D_t$ , so  $\lim_{T \rightarrow \infty} D_t \cdot \varepsilon(\mathbf{Y} \odot \mathbf{M}_t) = \forall_{j \in \mathbf{M}_t} Y_j \cdot \varepsilon(\mathbf{Y} \odot \mathbf{M}_t)$ . Thus, the SDV loss for a single organ becomes

$$\sum_{t=1}^T L_{sdv}^t = \|\mathbf{Y} \odot (\mathbf{Y} - \hat{\mathbf{Y}}) \odot \mathbf{M}\|_1. \quad (9)$$

Generally, given  $S$  ROIs masked by  $\{\mathbf{M}_i^s\}$  for  $i$ -th patient, we have  $L_{sdv}$  for  $N$  patients as:

$$L_{sdv} = \frac{1}{N} \sum_{i=1}^N \sum_{s=1}^S \lambda_s \|\mathbf{Y}_i \odot (\mathbf{Y}_i - \hat{\mathbf{Y}}_i) \odot \mathbf{M}_i^s\|_1, \quad (10)$$

where  $\lambda_s = 1$  if  $\mathbf{M}_i^s$  mask PTV else  $\lambda_s = 0.5$ . In summary, the proposed  $L_{sdv}$  has the following properties (detailed derivation from Eq. 8 to Eq. 10, justification and math symbol clarification are in Supplement A and E).

**Property 1:** Higher dose voxels contribute more to both DVH computation and our SDV loss.

**Property 2:** Optimal  $L_{sdv}$  leads to an exact match of 3D dose maps in its ROI, while zero DVH gaps (i.e., optimum) theoretically can come from sub-optimal spatial mismatch.

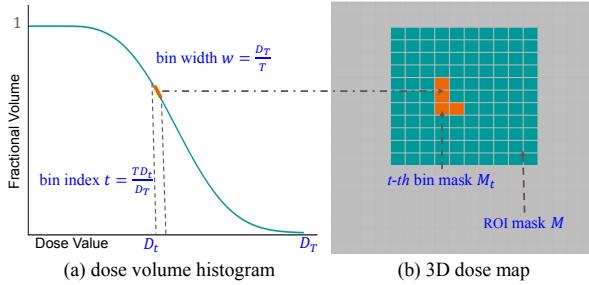


Figure 4. Shifting original (frequency-level) DVH definition to voxel-level loss. (a) shows a DVH and (b) is its relative volume. Teal is the ROI mask, the orange is corresponding to  $t$ -th bin.

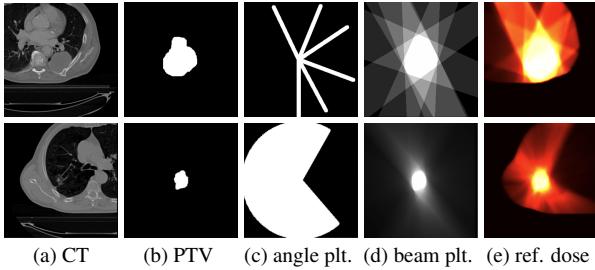


Figure 5. The illustration of beam-static (upper) and beam-dynamic (lower) samples (3D). The CT and PTV/OAR masks are source data. Angle-plate and beam-plate are created using our pre-processing pipeline. The last column is reference dose.

### 3.3.3 RT Data Pre-processing

We introduce an effective way to utilize RT geometry by creating spatial matrices (termed as *plates*). As in Figure 5, angle plates are binary masks indicating angles (dynamic beam plates like sectors due to covering a range of angles). The beam plates are created based on angles and PTV masks incorporating commonly-known geometry information. The details of creating angle/beam plates and data augmentation are in Supplement B and C.

Considering that closer regions to the isocenter (i.e., planning center) are more interesting for the planner, we centralize the isocenter as the volume center (Figure 5) with two physical ranges in our experiments: 96 mm  $\times$  225 mm  $\times$  225 mm and 144 mm  $\times$  256 mm  $\times$  256 mm. The axial range is smaller since treatment beam pass orthogonally to the axial direction. Our major experiments are conducted with 96 mm  $\times$  224 mm  $\times$  224 mm with data size 32  $\times$  192  $\times$  192. To separate the RT planning prediction from the clinically-dependent dose prescription, we normalize the reference dose to 0-5 during the training. Seven organs at risk (OARs) have been included in the multiple channel input: brachial, chest wall and rib, esophagus, heart, proximal bronchial, spinal cord, and lung. We follow [41] to impute zeros for missing organ masks.

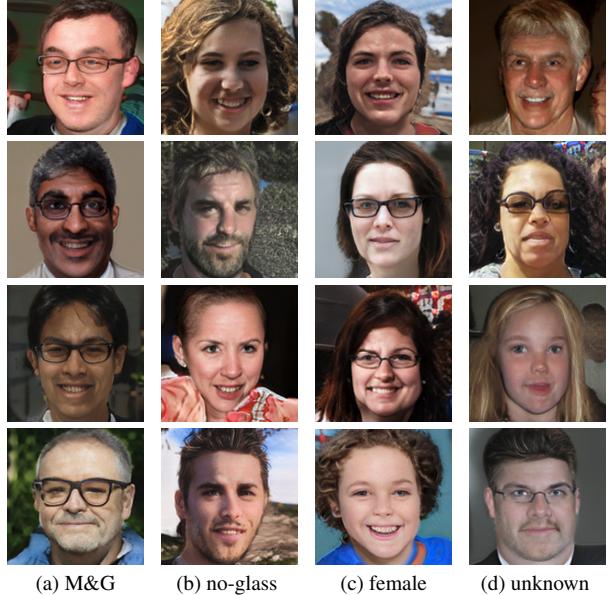


Figure 6. Illustration with face images demonstrates our method can be generalizable. A single generation model can accept multiple conditions (male and glass) as (a), single condition as in (b) and (c), and even no condition (d) with desired output.

## 4. Experiments

To evaluation our proposed model, we provide illustration examples with the FFHQ dataset [31] and in-depth validations in 3D dose prediction with two clinical datasets.

### 4.1. Illustration Example with Face Synthesis

We use a state-of-the-art GAN model (vision-aided mechanism [36] with StyleGAN3 [30]) as the backbone, which was initially developed for image generation without conditions. We extend the official source code <sup>1</sup> with our Flexible-C<sup>m</sup> GAN mechanism. FFHQ is a representative face dataset for evaluating GAN [31]. We include two conditions (wearing glasses and gender) trained on 2,000 128  $\times$  128 images and utilize the public annotation <sup>2</sup>.

Figure 6 shows the generated images with a single model from four different situations: (a) multiple conditions, (b,c) partial conditions, and (d) no condition. When all conditions are specified, the generated images follow those conditions (e.g., all faces are male and with glasses in Figure 6a). When one or more conditions are missing, the generated images are with a reasonable diversity in those conditions (e.g., male and female are shown in Figure 6b, 6d).

<sup>1</sup><https://github.com/nupurkmr9/vision-aided-gan/tree/main/stylegan3>

<sup>2</sup><https://github.com/DCGM/ffhq-features-dataset>





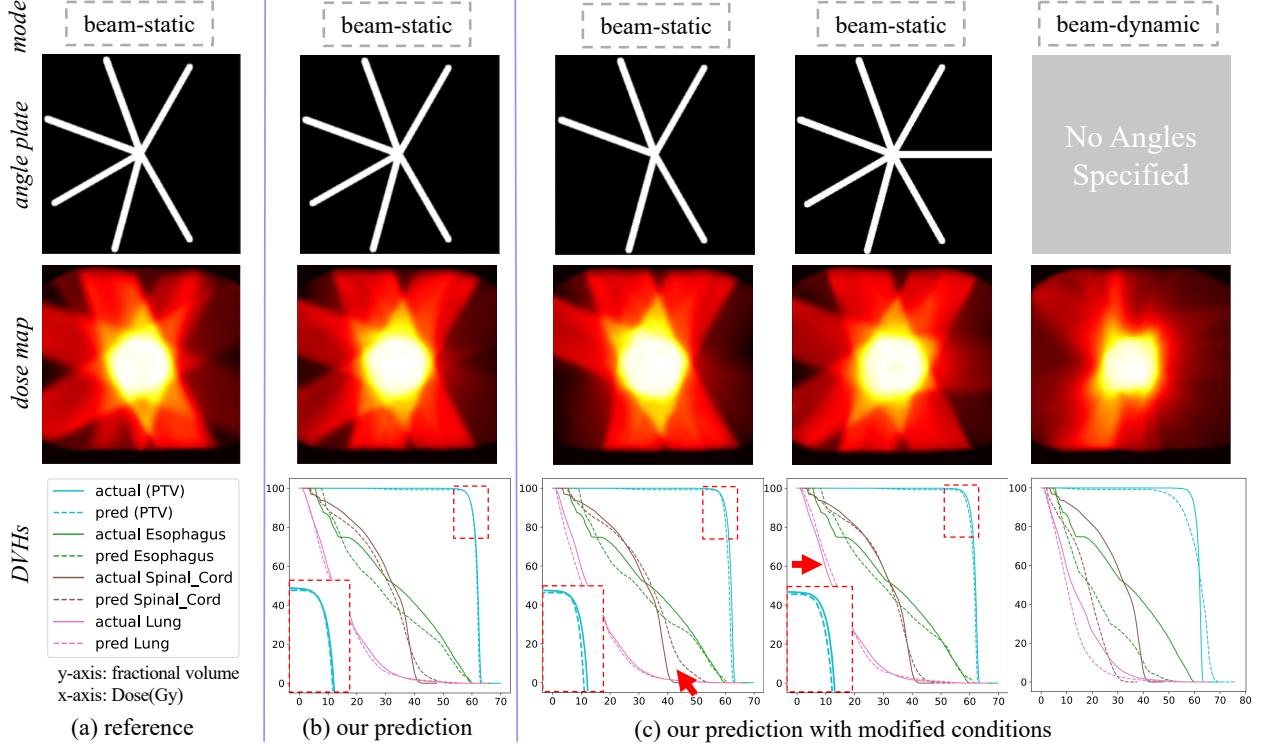


Figure 8. Dose prediction examples allowing user interface. The mode and angle plate are two types of condition that can be modified. When given the same conditions as reference (a), our prediction (b) has a reasonable match with the delivered dose. (c) shows three conditional modifications with the desired prediction, even if a condition is missing. The condition modification will be reflected on predicted dose maps and DVHs. The closer dash line and solid line in DVHs, the better matching between prediction and reference.

*istic* dose utilizing multi-condition and handle the potential missing condition in practical heterogeneous contexts. During inference, we allow the users to manipulate conditions or provide partial conditions to generate 3D dose (Figure 8). This is essential in a RT planning pipeline since the treatment is subjective to clinicians/experts, and different institutions may have different preferences. Previous dose prediction deep models have been explored mainly in a simpler context, e.g., single mode or single beam configuration. Considering a more practical and challenging context (e.g., lung cancer with multiple modes and different angle configurations), handling different situations with separate models is impractical due to implementation complexity. We enable the usage of additional geometry information and human-machine interaction with a single model.

**Limitations and Future Work.** Currently, our model has only been tested on lung cancer datasets. Lung cancer is one of the most heterogeneous compared to widely studied cancers (e.g., prostate) with RT planning. We have shown that our model is promising in this challenging context and will yet to show how it generalizes to other cancer sites in the near future. Second, although we use pretraining mechanism [36] (a state-of-the-art GAN) for the face dataset, the exact same approach is not applicable in 3D dose contexts

due to a shortage of external pretrained 3D dose model and memory constraints. For future work, we will explore other techniques, for example utilizing self-supervised learning, to obtain appropriate pretrained models and to boost performance. Third, another future work is to build an entire deep learning RT planning pipeline (adding fluence map prediction as in Figure 2 and other necessary parts).

**Conclusion.** We proposed a new GAN variant Flexible-C<sup>m</sup> GAN with two novel loss functions motivated by the practical challenges in RT dose planning. We are the first to advance the precision of 3D dose prediction by adding flexible conditions such as beam geometry and treatment mode within a deep learning framework. Our miss-consistency loss upgrades our model to be able to handle flexible conditions. Shift-dose-volume loss makes widely used DVH metric differentiable and allows us to use it in a deep learning context reducing the possibility of sub-optimal solutions. We conducted extensive experiments on two clinical datasets to validate our model and its sub-components. We also demonstrated that Flexible-C<sup>m</sup> GAN is generalizable to other tasks (e.g., face synthesis).

**Disclaimer.** The information in this paper is based on research results that are not commercially available. Future commercial availability cannot be guaranteed.

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