# Octave C++ Classes

Edition 1.0 for Octave version 4.0.1September 1993

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## Table of Contents

1	Acknowledgements1Contributors to Octave1
G	NU GENERAL PUBLIC LICENSE 2
<b>2</b>	A Brief Introduction to Octave
3	Arrays
4	Matrix and Vector Operations
5	Matrix Factorizations 32
6	Ranges
7	Nonlinear Functions
8	Nonlinear Equations
9	Optimization       39         9.1 Objective Functions       39         9.2 Bounds       39         9.3 Linear Constraints       40         9.4 Nonlinear Constraints       40         9.5 Quadratic Programming       40         9.6 Nonlinear Programming       41
1(	O Quadrature4210.1 Collocation Weights42
1	1 Ordinary Differential Equations 44
12	2 Differential Algebraic Equations 45
1:	3 Error Handling 46

14	Installation	47
15	Bugs	48
Con	cept Index	49
Fun	ction Index	<b>50</b>

## ${\bf 1} \ {\bf Acknowledgements}$

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## 2 A Brief Introduction to Octave

This manual documents how to run, install and port Octave's C++ classes, and how to report bugs.

Chapter 3: Arrays

## 3 Arrays

## 3.1 Constructors and Assignment

Array<T> (void) [Constructor]

Create an array with no elements.

Array<T> (int n [, const T &val]) [Constructor]

Create an array with n elements. If the optional argument val is supplied, the elements are initialized to val; otherwise, they are left uninitialized. If n is less than zero, the current error handler is invoked (see Chapter 13 [Error Handling], page 46).

Array<T> (const Array<T> &a) [Constructor]

Create a copy of the Array<T> chieft a Memory for the Array<T> class is managed

Create a copy of the *Array*<*T*> object a. Memory for the *Array*<*T*> class is managed using a reference counting scheme, so the cost of this operation is independent of the size of the array.

Array<T>& operator = (const Array<T> &a) [Assignment on Array<T>]
Assignment operator. Memory for the Array<T> class is managed using a reference counting scheme, so the cost of this operation is independent of the size of the array.

int capacity (void) const
int length (void) const
[Method on Array<T>]
[Method on Array<T>]

Return the length of the array.

 $T\& \ \text{elem (int n)} \qquad \qquad [Method \ on \ Array<T>]$ 

T& checkelem (int n) [Method on Array<T>]

If n is within the bounds of the array, return a reference to the element indexed by n; otherwise, the current error handler is invoked (see Chapter 13 [Error Handling], page 46).

T& operator () (int n) [Indexing on Array<T>]

T elem (int n) const [Method on ArrayT>]
T checkelem (int n) const [Method on ArrayT>]

If n is within the bounds of the array, return the value indexed by n; otherwise, call the current error handler. See Chapter 13 [Error Handling], page 46.

T operator () (int n) const [Indexing on Array<T>]

T& xelem (int n) [Method on Array<T>]

T xelem (int n) const [Method on Array<T>]

Return a reference to, or the value of, the element indexed by n. These methods never perform bounds checking.

void resize (int n [, const T &val]) [Method on Array<T>]

Change the size of the array to be n elements. All elements are unchanged, except that if n is greater than the current size and the optional argument val is provided,

Chapter 3: Arrays

the additional elements are initialized to val; otherwise, any additional elements are left uninitialized. In the current implementation, if n is less than the current size, the length is updated but no memory is released.

const T* data (void) const	[Method on Array <t>]</t>
Array2 <t> Array2<t> Array2 (void) Array2<t> (int n, int m) Array2<t> (int n, int m, const T &amp;val)</t></t></t></t>	[Constructor] [Constructor] [Constructor]
Array2 <t> (const Array2<t> &amp;a) Array2<t> (const DiagArray<t> &amp;a)</t></t></t></t>	[Constructor] [Constructor]
Array2 <t>&amp; operator = (const Array2<t> &amp;a)</t></t>	[Assignment on Array2 <t>]</t>
int dim1 (void) const int rows (void) const	[Method on Array2 <t>] [Method on Array2<t>]</t></t>
<pre>int dim2 (void) const int cols (void) const int columns (void) const</pre>	[Method on Array2 <t>] [Method on Array2<t>] [Method on Array2<t>]</t></t></t>
T& elem $(int \ i, int \ j)$ T& checkelem $(int \ i, int \ j)$	[Method on Array2 <t>] [Method on Array2<t>]</t></t>
T& operator () $(int \ i, int \ j)$	[Indexing on Array2 <t>]</t>
<pre>void resize (int n, int m) void resize (int n, int m, const T &amp;val)</pre>	[Method on Array2 <t>] [Method on Array2<t>]</t></t>
Array3 <t> (void) Array3<t> (int n, int m, int k) Array3<t> (int n, int m, int k, const T &amp;val) Array3<t> (const Array3<t> &amp;a)</t></t></t></t></t>	[Constructor] [Constructor] [Constructor]
Array3 <t>&amp; operator = <math>(const\ Array3<t>\ \&amp;a)</t></math></t>	[Assignment on Array3 <t>]</t>
<pre>int dim1 (void) const int dim2 (void) const int dim3 (void) const</pre>	[Method on Array3 <t>] [Method on Array3<t>] [Method on Array3<t>]</t></t></t>
T& elem $(int \ i, int \ j, int \ k)$ T& checkelem $(int \ i, int \ j, int \ k)$	[Method on Array3 <t>] [Method on Array3<t>]</t></t>
T& operator () (int i, int j, int k)	[Indexing on Array3 <t>]</t>
void resize (int $n$ , int $m$ , int $k$ ) void resize (int $n$ , int $m$ , int $k$ , const $T$ &val)	[Method on Array3 <t>] [Method on Array3<t>]</t></t>
DiagArray <t> (void) DiagArray<t> (int n) DiagArray<t> (int n, const T &amp;val) DiagArray<t> (int r, int c) DiagArray<t> (int r, int c, const T &amp;val) DiagArray<t> (const Array<t> &amp;a) DiagArray<t> (const DiagArray<t> &amp;a)</t></t></t></t></t></t></t></t></t>	[Constructor] [Constructor] [Constructor] [Constructor] [Constructor] [Constructor] [Constructor]
operator = (const DiagArray <t> &amp;a)</t>	[Assignment on DiagArray <t>&amp;]</t>

```
int dim1 (void) const
                                                          [Method on DiagArray<T>]
                                                          [Method on DiagArray<T>]
int rows (void) const
int dim2 (void) const
                                                          [Method on DiagArray<T>]
int cols (void) const
                                                          [Method on DiagArray<T>]
int columns (void) const
                                                          [Method on DiagArray<T>]
T& elem (int r, int c)
                                                          [Method on DiagArray<T>]
T& checkelem (int r, int c)
                                                          [Method on DiagArray<T>]
T& operator () (int r, int c)
                                                         [Indexing on DiagArray<T>]
void resize (int n, int m)
                                                          [Method on DiagArray<T>]
void resize (int n, int m, const T &val)
                                                          [Method on DiagArray<T>]
```

The real and complex ColumnVector and RowVector classes all have the following functions. These will eventually be part of an MArray<T> class, derived from the Array<T> class. Then the ColumnVector and RowVector classes will be derived from the MArray<T> class.

Element by element vector by scalar ops.

```
RowVector operator + (const RowVector &a, const double &s)
RowVector operator - (const RowVector &a, const double &s)
RowVector operator * (const RowVector &a, const double &s)
RowVector operator / (const RowVector &a, const double &s)
Element by element scalar by vector ops.

RowVector operator + (const double &s, const RowVector &a)
RowVector operator - (const double &s, const RowVector &a)
RowVector operator * (const double &s, const RowVector &a)
RowVector operator / (const double &s, const RowVector &a)
Element by element vector by vector ops.

RowVector operator + (const RowVector &a, const RowVector &b)
RowVector operator - (const RowVector &a, const RowVector &b)
RowVector product (const RowVector &a, const RowVector &b)
RowVector quotient (const RowVector &a, const RowVector &b)
Unary MArray ops.
```

### RowVector operator - (const RowVector &a)

The Matrix classes share the following functions. These will eventually be part of an MArray2<T> class, derived from the Array2<T> class. Then the Matrix class will be derived from the MArray<T> class.

Element by element matrix by scalar ops.

```
Matrix operator + (const Matrix &a, const double &s)
Matrix operator - (const Matrix &a, const double &s)
Matrix operator * (const Matrix &a, const double &s)
Matrix operator / (const Matrix &a, const double &s)
Element by element scalar by matrix ops.
```

```
Matrix operator + (const double &s, const Matrix &a)
Matrix operator - (const double &s, const Matrix &a)
Matrix operator * (const double &s, const Matrix &a)
Matrix operator / (const double &s, const Matrix &a)
  Element by element matrix by matrix ops.
Matrix operator + (const Matrix &a, const Matrix &b)
Matrix operator - (const Matrix &a, const Matrix &b)
Matrix product (const Matrix &a, const Matrix &b)
Matrix quotient (const Matrix &a, const Matrix &b)
  Unary matrix ops.
Matrix operator - (const Matrix &a)
  The DiagMatrix classes share the following functions. These will eventually be part of
an MDiagArray<T> class, derived from the DiagArray<T> class. Then the DiagMatrix class
will be derived from the MDiagArray<T> class.
  Element by element MDiagArray by scalar ops.
DiagMatrix operator * (const DiagMatrix &a, const double &s)
DiagMatrix operator / (const DiagMatrix &a, const double &s)
  Element by element scalar by MDiagArray ops.
DiagMatrix operator * (const double &s, const DiagMatrix &a)
  Element by element MDiagArray by MDiagArray ops.
DiagMatrix operator + (const DiagMatrix &a, const DiagMatrix &b)
DiagMatrix operator - (const DiagMatrix &a, const DiagMatrix &b)
DiagMatrix product (const DiagMatrix &a, const DiagMatrix &b)
  Unary MDiagArray ops.
DiagMatrix operator - (const DiagMatrix &a)
```

## 4 Matrix and Vector Operations

```
Matrix (void)
Matrix (int r, int c)
Matrix (int r, int c, double val)
Matrix (const Array2<double> &a)
Matrix (const Matrix &a)
Matrix (const DiagArray double > &a)
Matrix (const DiagMatrix &a)
Matrix& operator = (const Matrix &a)
int operator == (const Matrix &a) const
int operator != (const Matrix &a) const
Matrix& insert (const Matrix &a, int r, int c)
Matrix& insert (const RowVector &a, int r, int c)
Matrix& insert (const ColumnVector &a, int r, int c)
Matrix& insert (const DiagMatrix &a, int r, int c)
Matrix& fill (double val)
Matrix& fill (double val, int r1, int c1, int r2, int c2)
Matrix append (const Matrix &a) const
Matrix append (const RowVector &a) const
Matrix append (const ColumnVector &a) const
Matrix append (const DiagMatrix &a) const
Matrix stack (const Matrix &a) const
Matrix stack (const RowVector &a) const
Matrix stack (const Column Vector &a) const
Matrix stack (const DiagMatrix &a) const
Matrix transpose (void) const
Matrix extract (int r1, int c1, int r2, int c2) const
RowVector row (int i) const
RowVector row (char *s) const
ColumnVector column (int i) const
ColumnVector column (char *s) const
Matrix inverse (void) const
Matrix inverse (int &info) const
Matrix inverse (int &info, double &rcond) const
ComplexMatrix fourier (void) const
ComplexMatrix ifourier (void) const
DET determinant (void) const
DET determinant (int &info) const
DET determinant (int &info, double &rcond) const
Matrix solve (const Matrix &b) const
```

```
Matrix solve (const Matrix &b, int &info) const
Matrix solve (const Matrix &b, int &info, double &rcond) const
ComplexMatrix solve (const ComplexMatrix &b) const
ComplexMatrix solve (const ComplexMatrix &b, int &info) const
ComplexMatrix solve (const ComplexMatrix &b, int &info, double &rcond)
ColumnVector solve (const ColumnVector &b) const
ColumnVector solve (const ColumnVector &b, int &info) const
ColumnVector solve (const ColumnVector &b, int &info, double &rcond) const
ComplexColumnVector solve (const ComplexColumnVector &b) const
ComplexColumnVector solve (const ComplexColumnVector &b, int &info) const
ComplexColumnVector solve (const ComplexColumnVector &b, int &info,
         double &rcond) const
Matrix 1ssolve (const Matrix &b) const
Matrix 1ssolve (const Matrix &b, int &info) const
Matrix 1ssolve (const Matrix &b, int &info, int &rank) const
ComplexMatrix lssolve (const ComplexMatrix &b) const
ComplexMatrix 1ssolve (const ComplexMatrix &b, int &info) const
ComplexMatrix 1ssolve (const ComplexMatrix &b, int &info, int &rank) const
ColumnVector lssolve (const ColumnVector &b) const
ColumnVector lssolve (const ColumnVector &b, int &info) const
ColumnVector Issolve (const ColumnVector &b, int &info, int &rank) const
ComplexColumnVector lssolve (const ComplexColumnVector &b) const
ComplexColumnVector lssolve (const ComplexColumnVector &b, int &info)
ComplexColumnVector lssolve (const ComplexColumnVector &b, int &info, int
         &rank) const
Matrix& operator += (const Matrix &a)
Matrix& operator -= (const Matrix &a)
Matrix& operator += (const\ DiagMatrix\ \&a)
Matrix& operator -= (const DiagMatrix &a)
Matrix operator ! (void) const
ComplexMatrix operator + (const Matrix &a, const Complex &s)
ComplexMatrix operator - (const Matrix &a, const Complex &s)
ComplexMatrix operator * (const Matrix &a, const Complex &s)
ComplexMatrix operator / (const Matrix &a, const Complex &s)
ComplexMatrix operator + (const Complex &s, const Matrix &a)
ComplexMatrix operator - (const Complex &s, const Matrix &a)
ComplexMatrix operator * (const Complex &s, const Matrix &a)
ComplexMatrix operator / (const Complex &s, const Matrix &a)
ColumnVector operator * (const Matrix &a, const ColumnVector &b)
```

```
ComplexColumnVector operator * (const Matrix &a, const
         ComplexColumnVector &b)
Matrix operator + (const Matrix &a, const DiagMatrix &b)
Matrix operator - (const Matrix &a, const DiagMatrix &b)
Matrix operator * (const Matrix &a, const DiagMatrix &b)
ComplexMatrix operator + (const Matrix &a, const ComplexDiagMatrix &b)
ComplexMatrix operator - (const Matrix &a, const ComplexDiagMatrix &b)
ComplexMatrix operator * (const Matrix &a, const ComplexDiagMatrix &b)
Matrix operator * (const Matrix &a, const Matrix &b)
ComplexMatrix operator * (const Matrix &a, const ComplexMatrix &b)
ComplexMatrix operator + (const Matrix &a, const ComplexMatrix &b)
ComplexMatrix operator - (const Matrix &a, const ComplexMatrix &b)
ComplexMatrix product (const Matrix &a, const ComplexMatrix &b)
ComplexMatrix quotient (const Matrix &a, const ComplexMatrix &b)
Matrix map (d_-d_-Mapper f, const Matrix \&a)
void map (d_-d_-Mapper f)
Matrix all (void) const
Matrix any (void) const
Matrix cumprod (void) const
Matrix cumsum (void) const
Matrix prod (void) const
Matrix sum (void) const
Matrix sumsq (void) const
ColumnVector diag (void) const
ColumnVector diag (int k) const
ColumnVector row_min (void) const
ColumnVector row_min_loc (void) const
ColumnVector row_max (void) const
ColumnVector row_max_loc (void) const
RowVector column_min (void) const
RowVector column_min_loc (void) const
RowVector column_max (void) const
RowVector column_max_loc (void) const
ostream& operator << (ostream &os, const Matrix &a)
istream& operator >> (istream &is, Matrix &a)
ColumnVector (void)
ColumnVector (int n)
ColumnVector (int n, double val)
ColumnVector (const Array double > &a)
ColumnVector (const ColumnVector &a)
ColumnVector& operator = (const ColumnVector &a)
```

```
int operator == (const ColumnVector &a) const
int operator != (const ColumnVector &a) const
ColumnVector& insert (const ColumnVector &a, int r)
ColumnVector& fill (double val)
ColumnVector& fill (double val, int r1, int r2)
ColumnVector stack (const ColumnVector &a) const
RowVector transpose (void) const
ColumnVector extract (int r1, int r2) const
ColumnVector& operator += (const ColumnVector &a)
ColumnVector& operator -= (const ColumnVector &a)
ComplexColumnVector operator + (const ColumnVector &a, const Complex &s)
ComplexColumnVector operator - (const ColumnVector &a, const Complex &s)
ComplexColumnVector operator * (const ColumnVector &a, const Complex &s)
ComplexColumnVector operator / (const ColumnVector &a, const Complex &s)
ComplexColumnVector operator + (const Complex &s, const ColumnVector &a)
ComplexColumnVector operator - (const Complex &s, const ColumnVector &a)
ComplexColumnVector operator * (const Complex &s, const ColumnVector &a)
ComplexColumnVector operator / (const Complex &s, const ColumnVector &a)
Matrix operator * (const ColumnVector &a, const RowVector &a)
ComplexMatrix operator * (const ColumnVector &a, const ComplexRowVector
        &b)
ComplexColumnVector operator + (const ComplexColumnVector &a, const
         ComplexColumnVector &b)
ComplexColumnVector operator - (const ComplexColumnVector &a, const
         ComplexColumnVector &b)
ComplexColumnVector product (const ComplexColumnVector &a, const
         ComplexColumnVector &b)
ComplexColumnVector quotient (const ComplexColumnVector &a, const
         ComplexColumnVector &b)
ColumnVector map (d_-d_-Mapper f, const ColumnVector \&a)
void map (d_-d_-Mapper f)
double min (void) const
double max (void) const
ostream& operator << (ostream &os, const ColumnVector &a)
RowVector (void)
RowVector (int n)
RowVector (int n, double val)
RowVector (const Array double > &a)
RowVector (const RowVector &a)
RowVector& operator = (const RowVector &a)
```

```
int operator == (const RowVector &a) const
int operator != (const RowVector &a) const
RowVector& insert (const RowVector &a, int c)
RowVector& fill (double val)
RowVector& fill (double val, int c1, int c2)
RowVector append (const RowVector &a) const
ColumnVector transpose (void) const
RowVector extract (int c1, int c2) const
RowVector& operator += (const RowVector &a)
RowVector& operator -= (const RowVector &a)
ComplexRowVector operator + (const RowVector &a, const Complex &s)
ComplexRowVector operator - (const RowVector &a, const Complex &s)
ComplexRowVector operator * (const RowVector &a, const Complex &s)
ComplexRowVector operator / (const RowVector &a, const Complex &s)
ComplexRowVector operator + (const Complex &s, const RowVector &a)
ComplexRowVector operator - (const Complex &s, const RowVector &a)
ComplexRowVector operator * (const Complex &s, const RowVector &a)
ComplexRowVector operator / (const Complex &s, const RowVector &a)
double operator * (const RowVector &a, ColumnVector &b)
Complex operator * (const RowVector &a, const ComplexColumnVector &b)
RowVector operator * (const RowVector &a, const Matrix &b)
ComplexRowVector operator * (const RowVector &a, const ComplexMatrix &b)
ComplexRowVector operator + (const RowVector &a, const ComplexRowVector
ComplexRowVector operator - (const RowVector &a, const ComplexRowVector
ComplexRowVector product (const RowVector &a, const ComplexRowVector &b)
ComplexRowVector quotient (const RowVector &a, const ComplexRowVector
RowVector map (d_-d_-Mapper f, const RowVector \&a)
void map (d_-d_-Mapper f)
double min (void) const
double max (void) const
ostream& operator << (ostream &os, const RowVector &a)
DiagMatrix (void)
DiagMatrix (int n)
DiagMatrix (int n, double val)
DiagMatrix (int r, int c)
DiagMatrix (int r, int c, double val)
```

```
DiagMatrix (const RowVector &a)
DiagMatrix (const ColumnVector &a)
DiagMatrix (const DiagArray<double> &a)
DiagMatrix (const DiagMatrix &a)
DiagMatrix& operator = (const\ DiagMatrix\ \&a)
int operator == (const DiagMatrix &a) const
int operator != (const DiagMatrix &a) const
DiagMatrix& fill (double val)
DiagMatrix& fill (double val, int beg, int end)
DiagMatrix& fill (const ColumnVector &a)
DiagMatrix& fill (const RowVector &a)
DiagMatrix& fill (const ColumnVector &a, int beg)
DiagMatrix& fill (const RowVector &a, int beg)
DiagMatrix transpose (void) const
Matrix extract (int r1, int c1, int r2, int c2) const
RowVector row (int i) const
RowVector row (char *s) const
ColumnVector column (int i) const
ColumnVector column (char *s) const
DiagMatrix inverse (void) const
DiagMatrix inverse (int &info) const
DiagMatrix& operator += (const DiagMatrix &a)
DiagMatrix& operator -= (const DiagMatrix &a)
Matrix operator + (const DiagMatrix &a, double s)
Matrix operator - (const DiagMatrix &a, double s)
ComplexMatrix operator + (const DiagMatrix &a, const Complex &s)
ComplexMatrix operator - (const DiagMatrix &a, const Complex &s)
ComplexDiagMatrix operator * (const DiagMatrix &a, const Complex &s)
ComplexDiagMatrix operator / (const DiagMatrix &a, const Complex &s)
Matrix operator + (double s, const DiagMatrix &a)
Matrix operator - (double s, const DiagMatrix &a)
ComplexMatrix operator + (const Complex &s, const DiagMatrix &a)
ComplexMatrix operator - (const Complex &s, const DiagMatrix &a)
ComplexDiagMatrix operator * (const Complex &s, const DiagMatrix &a)
ColumnVector operator * (const DiagMatrix &a, const ColumnVector &b)
ComplexColumnVector operator * (const DiagMatrix &a, const
         ComplexColumnVector &b)
ComplexDiagMatrix operator + (const DiagMatrix &a, const
         ComplexDiagMatrix &b)
```

```
ComplexDiagMatrix operator - (const DiagMatrix &a, const
         ComplexDiagMatrix &b)
ComplexDiagMatrix product (const DiagMatrix &a, const ComplexDiagMatrix
         &b)
Matrix operator + (const DiagMatrix &a, const Matrix &b)
Matrix operator - (const DiagMatrix &a, const Matrix &b)
Matrix operator * (const DiagMatrix &a, const Matrix &b)
ComplexMatrix operator + (const DiagMatrix &a, const ComplexMatrix &b)
ComplexMatrix operator - (const DiagMatrix &a, const ComplexMatrix &b)
ComplexMatrix operator * (const DiagMatrix &a, const ComplexMatrix &b)
ColumnVector diag (void) const
ColumnVector diag (int k) const
ostream& operator << (ostream &os, const DiagMatrix &a)
ComplexMatrix (void)
ComplexMatrix (int r, int c)
ComplexMatrix (int r, int c, const Complex &val)
ComplexMatrix (const Matrix &a)
ComplexMatrix (const Array2<Complex> &a)
ComplexMatrix (const ComplexMatrix &a)
ComplexMatrix (const DiagMatrix &a)
ComplexMatrix (const DiagArray<Complex> &a)
ComplexMatrix (const ComplexDiagMatrix &a)
ComplexMatrix& operator = (const ComplexMatrix &a)
int operator == (const ComplexMatrix &a) const
int operator != (const ComplexMatrix &a) const
ComplexMatrix& insert (const Matrix &a, int r, int c)
ComplexMatrix& insert (const RowVector &a, int r, int c)
ComplexMatrix& insert (const ColumnVector &a, int r, int c)
ComplexMatrix& insert (const DiagMatrix &a, int r, int c)
ComplexMatrix& insert (const ComplexMatrix &a, int r, int c)
ComplexMatrix& insert (const ComplexRowVector &a, int r, int c)
ComplexMatrix& insert (const ComplexColumnVector &a, int r, int c)
ComplexMatrix& insert (const ComplexDiagMatrix &a, int r, int c)
ComplexMatrix& fill (double val)
ComplexMatrix& fill (const Complex &val)
ComplexMatrix& fill (double val, int r1, int c1, int r2, int c2)
ComplexMatrix& fill (const Complex &val, int r1, int c1, int r2, int c2)
ComplexMatrix append (const Matrix &a) const
{\tt ComplexMatrix\ append\ } (const\ RowVector\ \&{\tt a})\ const
ComplexMatrix append (const ColumnVector &a) const
ComplexMatrix append (const DiagMatrix &a) const
ComplexMatrix append (const ComplexMatrix &a) const
```

```
ComplexMatrix append (const ComplexRowVector &a) const
ComplexMatrix append (const ComplexColumnVector &a) const
ComplexMatrix append (const ComplexDiagMatrix &a) const
ComplexMatrix stack (const Matrix &a) const
ComplexMatrix stack (const RowVector &a) const
ComplexMatrix stack (const ColumnVector &a) const
ComplexMatrix stack (const DiagMatrix &a) const
ComplexMatrix stack (const ComplexMatrix &a) const
ComplexMatrix stack (const ComplexRowVector &a) const
ComplexMatrix stack (const ComplexColumnVector &a) const
ComplexMatrix stack (const ComplexDiagMatrix &a) const
ComplexMatrix transpose (void) const
Matrix real (const ComplexMatrix &a)
Matrix imag (const ComplexMatrix &a)
ComplexMatrix conj (const ComplexMatrix &a)
ComplexMatrix extract (int r1, int c1, int r2, int c2) const
ComplexRowVector row (int i) const
ComplexRowVector row (char *s) const
ComplexColumnVector column (int i) const
ComplexColumnVector column (char *s) const
ComplexMatrix inverse (void) const
ComplexMatrix inverse (int &info) const
ComplexMatrix inverse (int &info, double &rcond) const
ComplexMatrix fourier (void) const
ComplexMatrix ifourier (void) const
ComplexDET determinant (void) const
ComplexDET determinant (int &info) const
ComplexDET determinant (int &info, double &rcond) const
ComplexMatrix solve (const Matrix &b) const
ComplexMatrix solve (const Matrix &b, int &info) const
ComplexMatrix solve (const Matrix &b, int &info, double &rcond) const
ComplexMatrix solve (const ComplexMatrix &b) const
ComplexMatrix solve (const ComplexMatrix &b, int &info) const
ComplexMatrix solve (const ComplexMatrix &b, int &info, double &rcond)
ComplexColumnVector solve (const ComplexColumnVector &b) const
ComplexColumnVector solve (const ComplexColumnVector &b, int &info) const
ComplexColumnVector solve (const ComplexColumnVector &b, int &info,
        double &rcond) const
ComplexMatrix lssolve (const ComplexMatrix &b) const
ComplexMatrix 1ssolve (const ComplexMatrix &b, int &info) const
```

```
ComplexMatrix 1ssolve (const ComplexMatrix &b, int &info, int &rank) const
ComplexColumnVector lssolve (const ComplexColumnVector &b) const
ComplexColumnVector lssolve (const ComplexColumnVector &b, int &info)
        const
ComplexColumnVector lssolve (const ComplexColumnVector &b, int &info, int
        &rank) const
ComplexMatrix& operator += (const DiagMatrix &a)
ComplexMatrix& operator -= (const DiagMatrix &a)
ComplexMatrix& operator += (const ComplexDiagMatrix &a)
ComplexMatrix& operator -= (const ComplexDiagMatrix &a)
ComplexMatrix& operator += (const Matrix &a)
ComplexMatrix& operator -= (const Matrix &a)
ComplexMatrix& operator += (const ComplexMatrix &a)
ComplexMatrix& operator -= (const ComplexMatrix &a)
Matrix operator ! (void) const
ComplexMatrix operator + (const ComplexMatrix &a, double s)
ComplexMatrix operator - (const ComplexMatrix &a, double s)
ComplexMatrix operator * (const ComplexMatrix &a, double s)
ComplexMatrix operator / (const ComplexMatrix &a, double s)
ComplexMatrix operator + (double s, const ComplexMatrix &a)
ComplexMatrix operator - (double s, const ComplexMatrix &a)
ComplexMatrix operator * (double s, const ComplexMatrix &a)
ComplexMatrix operator / (double s, const ComplexMatrix &a)
ComplexColumnVector operator * (const ComplexMatrix &a, const
         ColumnVector &b)
{\tt ComplexColumnVector\ operator\ *\ } (const\ ComplexMatrix\ \&a,\ const
         ComplexColumnVector &b)
ComplexMatrix operator + (const ComplexMatrix &a, const DiagMatrix &b)
ComplexMatrix operator - (const ComplexMatrix &a, const DiagMatrix &b)
ComplexMatrix operator * (const ComplexMatrix &a, const DiagMatrix &b)
ComplexMatrix operator + (const ComplexMatrix &a, const ComplexDiagMatrix
ComplexMatrix operator - (const ComplexMatrix &a, const ComplexDiagMatrix
ComplexMatrix operator * (const ComplexMatrix &a, const ComplexDiagMatrix
        &b)
ComplexMatrix operator + (const ComplexMatrix &a, const Matrix &b)
ComplexMatrix operator - (const ComplexMatrix &a, const Matrix &b)
ComplexMatrix operator * (const ComplexMatrix &a, const Matrix &b)
ComplexMatrix operator * (const ComplexMatrix &a, const ComplexMatrix &b)
ComplexMatrix product (const ComplexMatrix &a, const Matrix &b)
```

```
ComplexMatrix quotient (const ComplexMatrix &a, const Matrix &b)
ComplexMatrix map (c_-c_-Mapper f, const ComplexMatrix \&a)
Matrix map (d_c_Mapper f, const ComplexMatrix \&a)
void map (c_-c_-Mapper f)
Matrix all (void) const
Matrix any (void) const
ComplexMatrix cumprod (void) const
ComplexMatrix cumsum (void) const
ComplexMatrix prod (void) const
ComplexMatrix sum (void) const
ComplexMatrix sumsq (void) const
ComplexColumnVector diag (void) const
ComplexColumnVector diag (int k) const
ComplexColumnVector row_min (void) const
ComplexColumnVector row_min_loc (void) const
ComplexColumnVector row_max (void) const
ComplexColumnVector row_max_loc (void) const
ComplexRowVector column_min (void) const
ComplexRowVector column_min_loc (void) const
ComplexRowVector column_max (void) const
ComplexRowVector column_max_loc (void) const
ostream& operator << (ostream &os, const ComplexMatrix &a)
istream& operator >> (istream &is, ComplexMatrix &a)
ComplexColumnVector (void)
ComplexColumnVector (int n)
ComplexColumnVector (int n, const Complex &val)
ComplexColumnVector (const ColumnVector &a)
ComplexColumnVector (const Array<Complex> &a)
ComplexColumnVector (const ComplexColumnVector &a)
ComplexColumnVector& operator = (const ComplexColumnVector &a)
int operator == (const ComplexColumnVector &a) const
int operator != (const ComplexColumnVector &a) const
ComplexColumnVector& insert (const ColumnVector &a, int r)
ComplexColumnVector& insert (const ComplexColumnVector &a, int r)
ComplexColumnVector& fill (double val)
ComplexColumnVector& fill (const Complex &val)
ComplexColumnVector& fill (double val, int r1, int r2)
ComplexColumnVector& fill (const Complex &val, int r1, int r2)
ComplexColumnVector stack (const ColumnVector &a) const
ComplexColumnVector stack (const ComplexColumnVector &a) const
ComplexRowVector transpose (void) const
```

```
ColumnVector real (const ComplexColumnVector &a)
ColumnVector imag (const ComplexColumnVector &a)
ComplexColumnVector conj (const ComplexColumnVector &a)
ComplexColumnVector extract (int r1, int r2) const
ComplexColumnVector& operator += (const ColumnVector &a)
ComplexColumnVector& operator -= (const ColumnVector &a)
ComplexColumnVector& operator += (const ComplexColumnVector &a)
ComplexColumnVector& operator -= (const ComplexColumnVector &a)
ComplexColumnVector operator + (const ComplexColumnVector &a, double s)
ComplexColumnVector operator - (const ComplexColumnVector &a, double s)
ComplexColumnVector operator * (const ComplexColumnVector &a, double s)
ComplexColumnVector operator / (const ComplexColumnVector &a, double s)
ComplexColumnVector operator + (double s, const ComplexColumnVector &a)
ComplexColumnVector operator - (double s, const ComplexColumnVector &a)
ComplexColumnVector operator * (double s, const ComplexColumnVector &a)
ComplexColumnVector operator / (double s, const ComplexColumnVector &a)
ComplexMatrix operator * (const ComplexColumnVector &a, const
         ComplexRowVector &b)
ComplexColumnVector operator + (const ComplexColumnVector &a, const
         ColumnVector &b)
ComplexColumnVector operator - (const ComplexColumnVector &a, const
        Column Vector &b)
ComplexColumnVector product (const ComplexColumnVector &a, const
         ColumnVector &b)
ComplexColumnVector quotient (const ComplexColumnVector &a, const
         Column Vector &b)
ComplexColumnVector map (c_{-}c_{-}Mapper\ f, const\ ComplexColumnVector\ \&a)
ColumnVector map (d_c_Mapper f, const ComplexColumnVector &a)
void map (c_cMapper f)
Complex min (void) const
Complex max (void) const
ostream& operator << (ostream &os, const ComplexColumnVector &a)
ComplexRowVector (void)
ComplexRowVector (int n)
ComplexRowVector (int n, const Complex &val)
ComplexRowVector (const RowVector &a)
ComplexRowVector (const Array<Complex> &a)
ComplexRowVector (const ComplexRowVector &a)
ComplexRowVector& operator = (const ComplexRowVector &a)
int operator == (const ComplexRowVector &a) const
int operator != (const ComplexRowVector &a) const
ComplexRowVector& insert (const RowVector &a, int c)
```

```
ComplexRowVector& insert (const ComplexRowVector &a, int c)
ComplexRowVector& fill (double val)
ComplexRowVector& fill (const Complex &val)
ComplexRowVector& fill (double val, int c1, int c2)
ComplexRowVector& fill (const Complex &val, int c1, int c2)
ComplexRowVector append (const RowVector &a) const
ComplexRowVector append (const ComplexRowVector &a) const
ComplexColumnVector transpose (void) const
RowVector real (const ComplexRowVector &a)
RowVector imag (const ComplexRowVector &a)
ComplexRowVector conj (const ComplexRowVector &a)
ComplexRowVector extract (int c1, int c2) const
ComplexRowVector& operator += (const RowVector &a)
ComplexRowVector& operator -= (const RowVector &a)
ComplexRowVector& operator += (const ComplexRowVector &a)
ComplexRowVector& operator -= (const ComplexRowVector &a)
ComplexRowVector operator + (const ComplexRowVector &a, double s)
ComplexRowVector operator - (const ComplexRowVector &a, double s)
ComplexRowVector operator * (const ComplexRowVector &a, double s)
ComplexRowVector operator / (const ComplexRowVector &a, double s)
ComplexRowVector operator + (double s, const ComplexRowVector &a)
ComplexRowVector operator - (double s, const ComplexRowVector &a)
ComplexRowVector operator * (double s, const ComplexRowVector &a)
ComplexRowVector operator / (double s, const ComplexRowVector &a)
Complex operator * (const ComplexRowVector &a, const ColumnVector &b)
Complex operator * (const ComplexRowVector &a, const ComplexColumnVector
        &b)
ComplexRowVector operator * (const ComplexRowVector &a, const
         ComplexMatrix &b)
ComplexRowVector operator + (const ComplexRowVector &a, const RowVector
ComplexRowVector operator - (const ComplexRowVector &a, const RowVector
ComplexRowVector product (const ComplexRowVector &a, const RowVector &b)
ComplexRowVector quotient (const ComplexRowVector &a, const RowVector
ComplexRowVector map (c_cMapper f, const ComplexRowVector \&a)
RowVector map (d_{-}c_{-}Mapper\ f, const\ ComplexRowVector\ \&a)
void map (c_-c_-Mapper f)
Complex min (void) const
Complex max (void) const
ostream& operator << (ostream &os, const ComplexRowVector &a)
```

```
ComplexDiagMatrix (void)
ComplexDiagMatrix (int n)
ComplexDiagMatrix (int n, const Complex &val)
ComplexDiagMatrix (int r, int c)
ComplexDiagMatrix (int r, int c, const Complex &val)
ComplexDiagMatrix (const RowVector &a)
ComplexDiagMatrix (const ComplexRowVector &a)
ComplexDiagMatrix (const ColumnVector &a)
ComplexDiagMatrix (const ComplexColumnVector &a)
ComplexDiagMatrix (const DiagMatrix &a)
ComplexDiagMatrix (const DiagArray<Complex> &a)
ComplexDiagMatrix (const ComplexDiagMatrix &a)
ComplexDiagMatrix& operator = (const ComplexDiagMatrix &a)
int operator == (const ComplexDiagMatrix &a) const
int operator != (const ComplexDiagMatrix &a) const
ComplexDiagMatrix& fill (double val)
ComplexDiagMatrix& fill (const Complex &val)
ComplexDiagMatrix& fill (double val, int beg, int end)
ComplexDiagMatrix& fill (const Complex &val, int beg, int end)
ComplexDiagMatrix& fill (const ColumnVector &a)
ComplexDiagMatrix& fill (const ComplexColumnVector &a)
ComplexDiagMatrix& fill (const RowVector &a)
ComplexDiagMatrix& fill (const ComplexRowVector &a)
ComplexDiagMatrix& fill (const ColumnVector &a, int beg)
ComplexDiagMatrix& fill (const ComplexColumnVector &a, int beg)
ComplexDiagMatrix& fill (const RowVector &a, int beg)
ComplexDiagMatrix& fill (const ComplexRowVector &a, int beg)
ComplexDiagMatrix transpose (void) const
DiagMatrix real (const ComplexDiagMatrix &a)
DiagMatrix imag (const ComplexDiagMatrix &a)
ComplexDiagMatrix conj (const ComplexDiagMatrix &a)
ComplexMatrix extract (int r1, int c1, int r2, int c2) const
ComplexRowVector row (int i) const
ComplexRowVector row (char *s) const
ComplexColumnVector column (int i) const
ComplexColumnVector column (char *s) const
ComplexDiagMatrix inverse (int &info) const
ComplexDiagMatrix inverse (void) const
ComplexDiagMatrix& operator += (const DiagMatrix &a)
ComplexDiagMatrix& operator -= (const DiagMatrix &a)
ComplexDiagMatrix& operator += (const ComplexDiagMatrix &a)
ComplexDiagMatrix& operator -= (const ComplexDiagMatrix &a)
ComplexMatrix operator + (const ComplexDiagMatrix &a, double s)
```

```
ComplexMatrix operator - (const ComplexDiagMatrix &a, double s)
ComplexMatrix operator + (const ComplexDiagMatrix &a, const Complex &s)
ComplexMatrix operator - (const ComplexDiagMatrix &a, const Complex &s)
ComplexDiagMatrix operator * (const ComplexDiagMatrix &a, double s)
ComplexDiagMatrix operator / (const ComplexDiagMatrix &a, double s)
ComplexMatrix operator + (double s, const ComplexDiagMatrix &a)
ComplexMatrix operator - (double s, const ComplexDiagMatrix &a)
ComplexMatrix operator + (const Complex &s, const ComplexDiagMatrix &a)
ComplexMatrix operator - (const Complex &s, const ComplexDiagMatrix &a)
ComplexDiagMatrix operator * (double s, const ComplexDiagMatrix &a)
ComplexColumnVector operator * (const ComplexDiagMatrix &a, const
         ColumnVector &b)
ComplexColumnVector operator * (const ComplexDiagMatrix &a, const
         ComplexColumnVector &b)
ComplexDiagMatrix operator + (const ComplexDiagMatrix &a, const
         DiagMatrix \&b
ComplexDiagMatrix operator - (const ComplexDiagMatrix &a, const
        DiagMatrix &b)
ComplexDiagMatrix product (const ComplexDiagMatrix &a, const DiagMatrix
        &b)
ComplexMatrix operator + (const ComplexDiagMatrix &a, const Matrix &b)
ComplexMatrix operator - (const ComplexDiagMatrix &a, const Matrix &b)
ComplexMatrix operator * (const ComplexDiagMatrix &a, const Matrix &b)
ComplexMatrix operator + (const ComplexDiagMatrix &a, const ComplexMatrix
        &b)
ComplexMatrix operator - (const ComplexDiagMatrix &a, const ComplexMatrix
ComplexMatrix operator * (const ComplexDiagMatrix &a, const ComplexMatrix
ComplexColumnVector diag (void) const
ComplexColumnVector diag (int k) const
ostream& operator << (ostream &os, const ComplexDiagMatrix &a)
```

### 5 Matrix Factorizations

```
AEPBALANCE (void)
AEPBALANCE (const Matrix &a, const char *balance_job)
AEPBALANCE (const AEPBALANCE &a)
AEPBALANCE& operator = (const\ AEPBALANCE\ \&a)
Matrix balanced_matrix (void) const
Matrix balancing_matrix (void) const
ostream& operator << (ostream &os, const AEPBALANCE &a)
ComplexAEPBALANCE (void)
ComplexAEPBALANCE (const ComplexMatrix &a, const char *balance_job)
ComplexAEPBALANCE (const ComplexAEPBALANCE &a)
ComplexAEPBALANCE& operator = (const ComplexAEPBALANCE &a)
ComplexMatrix balanced_matrix (void) const
ComplexMatrix balancing_matrix (void) const
ostream& operator << (ostream &os, const ComplexAEPBALANCE &a)
DET (void)
DET (const DET &a)
DET& operator = (const\ DET\ \&a)
int value_will_overflow (void) const
int value_will_underflow (void) const
double coefficient (void) const
int exponent (void) const
double value (void) const
ostream& operator << (ostream &os, const DET &a)
ComplexDET (void)
ComplexDET (const ComplexDET &a)
ComplexDET& operator = (const\ ComplexDET\ \&a)
int value_will_overflow (void) const
int value_will_underflow (void) const
Complex coefficient (void) const
int exponent (void) const
Complex value (void) const
ostream& operator << (ostream &os, const ComplexDET &a)
GEPBALANCE (void)
GEPBALANCE (const Matrix &a, const Matrix &, const char *balance_job)
GEPBALANCE (const GEPBALANCE &a)
GEPBALANCE& operator = (const GEPBALANCE \& a)
```

```
Matrix balanced_a_matrix (void) const
Matrix balanced_b_matrix (void) const
Matrix left_balancing_matrix (void) const
Matrix right_balancing_matrix (void) const
ostream& operator << (ostream &os, const GEPBALANCE &a)
CHOL (void)
CHOL (const Matrix &a)
CHOL (const Matrix &a, int &info)
CHOL (const CHOL &a)
CHOL& operator = (const CHOL &a)
Matrix chol_matrix (void) const
ostream& operator << (ostream &os, const CHOL &a)
ComplexCHOL (void)
ComplexCHOL (const ComplexMatrix &a)
ComplexCHOL (const ComplexMatrix &a, int &info)
ComplexCHOL (const ComplexCHOL &a)
ComplexCHOL& operator = (const ComplexCHOL &a)
ComplexMatrix chol_matrix (void) const
ostream& operator << (ostream &os, const ComplexCHOL &a)
HESS (void)
HESS (const Matrix &a)
HESS (const Matrix&a, int &info)
HESS (const HESS &a)
HESS& operator = (const HESS &a)
Matrix hess_matrix (void) const
Matrix unitary_hess_matrix (void) const
ostream& operator << (ostream &os, const HESS &a)
ComplexHESS (void)
ComplexHESS (const ComplexMatrix &a)
ComplexHESS (const ComplexMatrix &a, int &info)
ComplexHESS (const ComplexHESS &a)
ComplexHESS& operator = (const ComplexHESS &a)
ComplexMatrix hess_matrix (void) const
ComplexMatrix unitary_hess_matrix (void) const
ostream& operator << (ostream &os, const ComplexHESS &a)
SCHUR (void)
SCHUR (const Matrix &a, const char *ord)
SCHUR (const Matrix &a, const char *ord, int &info)
SCHUR (const SCHUR &a, const char *ord)
SCHUR& operator = (const SCHUR &a)
```

```
Matrix schur_matrix (void) const
Matrix unitary_matrix (void) const
ostream& operator << (ostream &os, const SCHUR &a)
ComplexSCHUR (void)
ComplexSCHUR (const ComplexMatrix &a, const char *ord)
ComplexSCHUR (const ComplexMatrix &a, const char *ord, int &info)
ComplexSCHUR (const ComplexSCHUR &a, const char *ord)
ComplexSCHUR& operator = (const ComplexSCHUR &a)
ComplexMatrix schur_matrix (void) const
ComplexMatrix unitary_matrix (void) const
ostream& operator << (ostream &os, const ComplexSCHUR &a)
SVD (void)
SVD (const Matrix &a)
SVD (const Matrix &a, int &info)
SVD (const SVD &a)
SVD& operator = (const\ SVD\ \&a)
DiagMatrix singular_values (void) const
Matrix left_singular_matrix (void) const
Matrix right_singular_matrix (void) const
ostream& operator << (ostream &os, const SVD &a)
ComplexSVD (void)
ComplexSVD (const ComplexMatrix &a)
ComplexSVD (const ComplexMatrix &a, int &info)
ComplexSVD (const ComplexSVD &a)
ComplexSVD& operator = (const\ ComplexSVD\ \&a)
DiagMatrix singular_values (void) const
ComplexMatrix left_singular_matrix (void) const
ComplexMatrix right_singular_matrix (void) const
ostream& operator << (ostream &os, const ComplexSVD &a)
EIG (void)
EIG (const Matrix &a)
EIG (const Matrix &a, int &info)
EIG (const ComplexMatrix &a)
EIG (const ComplexMatrix &a, int &info)
EIG (const EIG &a)
EIG& operator = (const EIG \& a)
ComplexColumnVector eigenvalues (void) const
ComplexMatrix eigenvectors (void) const
ostream& operator << (ostream &os, const EIG &a)
```

```
LU (void)
LU (const Matrix &a)
LU (const LU &a)
LU& operator = (const\ LU\ \&a)
Matrix L (void) const
Matrix U (void) const
Matrix P (void) const
ostream& operator << (ostream &os, const LU &a)
ComplexLU (void)
ComplexLU (const ComplexMatrix &a)
ComplexLU (const ComplexLU &a)
ComplexLU& operator = (const ComplexLU &a)
ComplexMatrix L (void) const
ComplexMatrix U (void) const
Matrix P (void) const
ostream& operator << (ostream &os, const ComplexLU &a)
QR (void)
QR (const Matrix &A)
QR (const QR &a)
QR& operator = (const QR \& a)
Matrix Q (void) const
Matrix R (void) const
ostream& operator << (ostream &os, const QR &a)
ComplexQR (void)
ComplexQR (const ComplexMatrix &A)
ComplexQR (const ComplexQR &a)
ComplexQR& operator = (const\ ComplexQR\ \&a)
ComplexMatrix Q (void) const
ComplexMatrix R (void) const
ostream& operator << (ostream &os, const ComplexQR &a)
```

### 6 Ranges

```
Range (void)
Range (const Range &r)
Range (double b, double 1)
Range (double b, double 1, double i)
double base (void) const
double limit (void) const
double inc (void) const
void set_base (double b)
void set_limit (double 1)
void set_inc (double i)
int nelem (void) const
double min (void) const
double max (void) const
void sort (void)
ostream& operator << (ostream &os, const Range &r)
istream& operator >> (istream &is, Range &r)
void print_range (void)
```

### 7 Nonlinear Functions

```
NLFunc (void)
NLFunc (const nonlinear_fcn)
NLFunc (const nonlinear_fcn, const jacobian_fcn)
NLFunc (const NLFunc &a)
NLFunc& operator = (const NLFunc &a)
nonlinear_fcn function (void) const;
NLFunc& set_function (const nonlinear_fcn f)
jacobian_fcn jacobian_function (void) const;
NLFunc& set_jacobian_function (const jacobian_fcn j)
```

### 8 Nonlinear Equations

```
NLEqn_options (void)
NLEqn_options (const NLEqn_options &opt)
NLEqn_options& operator = (const NLEqn_options &opt)
void init (void)
void copy (const NLEqn_options &opt)
void set_default_options (void)
void set_tolerance (double val)
double tolerance (void)
NLEqn (void)
NLEqn (const Column Vector&, const NLFunc)
NLEqn (const NLEqn &a)
NLEqn& operator = (const NLEqn &a)
void resize (int n)
void set_states (const ColumnVector &x)
ColumnVector states (void) const
int size (void) const
ColumnVector solve (void)
ColumnVector solve (const ColumnVector &x)
ColumnVector solve (int &info)
ColumnVector solve (const ColumnVector &x, int &info)
```

#### 9 Optimization

#### 9.1 Objective Functions

```
Objective (void)
Objective (const objective_fcn)
Objective (const objective_fcn, const gradient_fcn)
Objective (const Objective &a)
Objective& operator = (const Objective &a)
objective_fcn objective_function (void) const;
Objective& set_objective_function (const objective_fcn)
gradient_fcn gradient_function (void) const;
Objective& set_gradient_function (const gradient_fcn)
9.2 Bounds
Bounds (void)
Bounds (int n)
Bounds (const ColumnVector 1b, const ColumnVector ub)
Bounds (const Bounds &a)
Bounds& operator = (const Bounds &a)
Bounds& resize (int n)
double lower_bound (int index) const;
double upper_bound (int index) const;
ColumnVector lower_bounds (void) const;
ColumnVector upper_bounds (void) const;
int size (void) const;
Bounds& set_bound (int index, double low, double high)
Bounds& set_bounds (double low, double high)
Bounds& set_bounds (const ColumnVector 1b, const ColumnVector ub)
Bounds& set_lower_bound (int index, double low)
Bounds& set_upper_bound (int index, double high)
Bounds& set_lower_bounds (double low)
Bounds& set_upper_bounds (double high)
Bounds& set_lower_bounds (const ColumnVector 1b)
Bounds& set_upper_bounds (const ColumnVector ub)
```

ostream& operator << (ostream &os, const Bounds &b)

#### 9.3 Linear Constraints

```
LinConst (void)
LinConst (int nclin, int nx)
LinConst (int nclin_eq, int nclin_ineq, int nx)
LinConst (const ColumnVector &1b, const Matrix &A, const ColumnVector &ub)
LinConst (const Matrix &A_eq, const ColumnVector &b_eq, const Matrix
         &A_ineq, const ColumnVector &b_ineq)
LinConst (const LinConst &a)
LinConst& operator = (const LinConst &a)
LinConst& resize (int nclin, int n)
Matrix constraint_matrix (void) const;
LinConst& set_constraint_matrix (const Matrix &A)
Matrix eq_constraint_matrix (void) const;
Matrix ineq_constraint_matrix (void) const;
ColumnVector eq_constraint_vector (void) const;
ColumnVector ineq_constraint_vector (void) const;
ostream& operator << (ostream &os, const LinConst &b)
9.4 Nonlinear Constraints
NLConst (void)
NLConst (int n)
NLConst (const ColumnVector 1b, const NLFunc f, const ColumnVector ub)
NLConst (const NLConst &a)
NLConst& operator = (const NLConst &a)
9.5 Quadratic Programming
QP (void)
QP (const ColumnVector &x, const Matrix &H)
QP (const ColumnVector &x, const Matrix &H, const ColumnVector &c)
QP (const ColumnVector &x, const Matrix &H, const Bounds &b)
QP (const ColumnVector &x, const Matrix &H, const LinConst &lc)
QP (const ColumnVector &x, const Matrix &H, const ColumnVector &c, const
         Bounds &b)
QP (const ColumnVector &x, const Matrix &H, const ColumnVector &c, const
         LinConst &lc)
QP (const ColumnVector &x, const Matrix &H, const Bounds &b, const LinConst
```

virtual ColumnVector minimize (void) virtual ColumnVector minimize (double &objf)

Bounds &b, const LinConst &lc)

QP (const ColumnVector &x, const Matrix &H, const ColumnVector &c, const

&1c)

```
virtual ColumnVector minimize (double &objf, int &inform)
virtual ColumnVector minimize (double &objf, int &inform, ColumnVector
        &lambda) = 0;
virtual ColumnVector minimize (const ColumnVector &x)
virtual ColumnVector minimize (const ColumnVector &x, double &objf)
virtual ColumnVector minimize (const ColumnVector &x, double &objf, int
        &inform)
virtual ColumnVector minimize (const ColumnVector &x, double &objf, int
        &inform, Column Vector &lambda)
ColumnVector minimize (double &objf, int &inform, ColumnVector &lambda)
9.6 Nonlinear Programming
NLP (void)
NLP (const ColumnVector &x, const Objective &phi)
NLP (const ColumnVector &x, const Objective &phi, const Bounds &b)
NLP (const ColumnVector &x, const Objective &phi, const Bounds &b, const
        LinConst &lc)
NLP (const Column Vector &x, const Objective &phi, const Bounds &b, const
        LinConst &lc, const NLConst &nlc)
NLP (const ColumnVector &x, const Objective &phi, const LinConst &lc)
NLP (const ColumnVector &x, const Objective &phi, const LinConst &lc, const
        NLConst &nlc)
NLP (const Column Vector &x, const Objective &phi, const NLConst &nlc)
NLP (const Column Vector &x, const Objective &phi, const Bounds &b, const
        NLConst &nlc)
NLP& operator = (const\ NLP\ \&a)
int size (void) const
ColumnVector minimize (void)
ColumnVector minimize (double &objf)
ColumnVector minimize (double &objf, int &inform)
ColumnVector minimize (double &objf, int &inform, ColumnVector &lambda)
ColumnVector minimize (const ColumnVector &x)
ColumnVector minimize (const ColumnVector &x, double &objf)
ColumnVector minimize (const ColumnVector &x, double &objf, int &inform)
```

ColumnVector minimize (const ColumnVector &x, double &objf, int &inform,

Column Vector & lambda)

#### 10 Quadrature

```
Quad (integrand_fcn fcn)
Quad (integrand_fcn fcn, double abs, double rel)
virtual double integrate (void)
virtual double integrate (int &ier)
virtual double integrate (int &ier, int &neval)
virtual double integrate (int &ier, int &neval, double &abserr) = 0
Quad_options (void)
Quad_options (const Quad_options &opt)
Quad_options& operator = (const Quad_options &opt)
void init (void)
void copy (const Quad_options &opt)
void set_default_options (void)
void set_absolute_tolerance (double val)
void set_relative_tolerance (double val)
double absolute_tolerance (void)
double relative_tolerance (void)
DefQuad (integrand_fcn fcn)
DefQuad (integrand_fcn fcn, double 11, double u1)
DefQuad (integrand_fcn fcn, double 11, double u1, double abs, double rel)
DefQuad (integrand_fcn fcn, double 11, double u1, const ColumnVector &sing)
DefQuad (integrand_fcn fcn, const ColumnVector &sing, double abs, double rel)
DefQuad (integrand_fcn fcn, const ColumnVector &sing)
DefQuad (integrand_fcn fcn, double 11, double u1, const ColumnVector &sing,
         double abs, double rel)
IndefQuad (integrand_fcn fcn)
IndefQuad (integrand_fcn fcn, double b, IntegralType t)
IndefQuad (integrand_fcn fcn, double b, IntegralType t, double abs, double rel)
IndefQuad (integrand_fcn fcn, double abs, double rel)
10.1 Collocation Weights
CollocWt (void)
CollocWt (int n, int inc_1, int inc_r)
CollocWt (int n, int inc_1, int inc_r, double 1, double r)
CollocWt (int n, double a, double b, int inc_1, int inc_r)
CollocWt (int n, int inc_1, int inc_r, double 1, double r)
CollocWt (const CollocWt&)
CollocWt& operator = (const\ CollocWt\&)
```

```
CollocWt& resize (int ncol)
CollocWt& add_left (void)
CollocWt& add_right (void)
CollocWt& delete_left (void)
CollocWt& delete_right (void)
CollocWt& set_left (double val)
CollocWt& set_right (double val)
CollocWt& set_alpha (double val)
CollocWt& set_beta (double val)
int ncol (void) const
int left_included (void) const
int right_included (void) const
double left (void) const
double right (void) const
double width (void) const
double alpha (void) const
double beta (void) const
ColumnVector roots (void)
ColumnVector quad (void)
ColumnVector quad_weights (void)
Matrix first (void)
Matrix second (void)
ostream& operator << (ostream &os, const CollocWt &c)
```

#### 11 Ordinary Differential Equations

```
ODE_options (void)
ODE_options (const ODE_options &opt)
ODE_options& operator = (const ODE_options &opt)
void init (void)
void copy (const ODE_options &opt)
void set_default_options (void)
void set_absolute_tolerance (double val)
void set_initial_step_size (double val)
void set_maximum_step_size (double val)
void set_minimum_step_size (double val)
void set_relative_tolerance (double val)
double absolute_tolerance (void)
double initial_step_size (void)
double maximum_step_size (void)
double minimum_step_size (void)
double relative_tolerance (void)
ODE (void)
ODE (int n)
ODE (const ColumnVector &state, double time, const ODEFunc &f)
virtual int size (void) const
virtual ColumnVector state (void) const
virtual double time (void) const
virtual void force_restart (void)
virtual void initialize (const ColumnVector &x, double t)
virtual void set_stop_time (double t)
virtual void clear_stop_time (void)
virtual ColumnVector integrate (double t)
void integrate (int nsteps, double tstep, ostream &s)
Matrix integrate (const ColumnVector &tout)
Matrix integrate (const Column Vector & tout, const Column Vector & tcrit)
```

### 12 Differential Algebraic Equations

```
DAE (void)
DAE (int n)
DAE (const ColumnVector &x, double time, DAEFunc &f)
DAE (const ColumnVector &x, ColumnVector &xdot, double time, DAEFunc &f)
ColumnVector deriv (void)
virtual void initialize (const ColumnVector &x, double t)
virtual void initialize (const ColumnVector &x, ColumnVector &xdot, double t)

ColumnVector integrate (double t)

Matrix integrate (const ColumnVector &tout, Matrix &xdot_out)
Matrix integrate (const ColumnVector &tout, Matrix &xdot_out, const ColumnVector &tout, ColumnVector &tout, Matrix &xdot_out, const ColumnVector &tout, ColumnVector
```

## 13 Error Handling

### 14 Installation

### 15 Bugs

Concept Index 49

# Concept Index

$\mathbf{A}$	matrix manipulations
acknowledgements	
arrays	N
B bounds	NLP41nonlinear Constraints40nonlinear equations38
bugs, known	nonlinear functions
$\mathbf{C}$	numerical integration
collocation weights         42           contributors         1	O
copyright	objective functions
D	optimization
DAE	orthogonal conocation
F	Q
factorizations	QP
т	quadrature
I	_
installation         47           installation trouble         48	R
integration         42           introduction         13	ranges
K	$\mathbf{T}$
known causes of trouble	troubleshooting
known causes of trouble	
L	$\mathbf{V}$
linear Constraints	vector manipulations
$\mathbf{M}$	$\mathbf{W}$
matrix factorizations	warranty

Function Index 50

### Function Index

$\mathbf{A}$		ComplexRowVector	28
absolute_tolerance		ComplexSCHUR	
add_left		ComplexSVD	34
add_right		conj	30
AEPBALANCE.		constraint_matrix	40
all		copy 38, 42,	44
alpha		cumprod	27
any	-	cumsum	
append			
Array <t></t>			
Array2 <t></t>		D	
Array3 <t></t>	1 5	DAE	15
		data on Array <t></t>	
_		DefQuad	
В		delete_left	
balanced_a_matrix		delete_right	
balanced_b_matrix	99	derivderiv	
balanced_matrix	~ ~	determinant	
balancing_matrix	00	DET	
base	20		
beta	40	diag	
Bounds		DiagArray <t></t>	
		DiagMatrix	
		dim1 on Array2 <t></t>	
$\mathbf{C}$		dim1 on Array3 <t></t>	
capacity on Array <t></t>	1/	dim1 on DiagArray <t></t>	
checkelem on Array <t></t>	1.4	dim2 on Array2 <t></t>	
checkelem on Array2 <t></t>	15	dim2 on Array3 <t></t>	
checkelem on Array3 <t></t>	15	dim2 on DiagArray <t></t>	
checkelem on DiagArray <t></t>		dim3 on Array3 <t></t>	10
chol_matrix	33		
CHOL	33	$\mathbf{E}$	
clear_stop_time	44		
coefficient		eigenvalues	
CollocWt		eigenvectors	
cols on Array2 <t></t>		EIG	
cols on DiagArray <t></t>		elem on Array <t></t>	
column		elem on Array2 <t></t>	
column_max		elem on Array3 <t></t>	15
column_max_loc 20, 1		elem on DiagArray <t></t>	
column_min		eq_constraint_matrix	
column_min_loc		eq_constraint_vector	
columns on Array2 <t></t>		exponent	
columns on DiagArray <t></t>		extract 18, 21, 22, 23, 25, 28, 29,	30
ColumnVector			
ComplexAEPBALANCE		173	
ComplexCHOL		$\mathbf{F}$	
ComplexColumnVector		fill	30
ComplexDET	02	first	
ComplexDiagMatrix	<b>3</b> 0	force_restart	
ComplexLU	55	fourier	
ComplexMatrix	00	function	
ComplexQR	24		

Function Index 51

$\mathbf{G}$		NLConst	40
GEPBALANCE	32	NLEqn	38
gradient_function		NLEqn_options	38
		NLFunc	37
Н		NLP	41
hess_matrix	33	0	
HESS	33		
		Objective	
I		objective_function	
_		ODE	
ifourier		ODE_options	
imag		operator!	
inc		operator != 18, 21, 22, 23, 24, 27, 28,	
IndefQuad		operator () on Array <t></t>	
ineq_constraint_matrix		operator () on Array2 <t></t>	
ineq_constraint_vector		operator () on Array3 <t></t>	
init		operator () on DiagArray <t></t>	
initial_step_size		operator * 16, 17, 19, 20, 21, 22, 23, 24, 26, 229, 31	20,
insert		operator + 16, 17, 19, 20, 21, 22, 23, 24, 26,	28
integrate		29, 30, 31	20,
inverse		operator += 19, 21, 22, 23, 26, 28, 29,	30
10, 20, 20,	00	operator 16, 17, 19, 20, 21, 22, 23, 24, 26, 26, 26, 26, 26, 26, 26, 26, 26, 26	
_		29, 30, 31	<b>-</b> 0,
J		operator -= 19, 21, 22, 23, 26, 28, 29,	30
jacobian_function	37	operator / 16, 17, 19, 21, 22, 23, 26, 28, 29,	
_		operator << 20, 21, 22, 24, 27, 28, 29, 31, 32, 34, 35, 36, 39, 40, 43	
$\mathbf{L}$		operator = 18, 20, 21, 23, 24, 27, 28, 30, 32,	33.
left	43	34, 35, 37, 38, 39, 40, 41, 42, 44	
left_balancing_matrix		<pre>operator = on Array<t></t></pre>	14
left_included		operator = on Array2 <t></t>	15
left_singular_matrix		operator = on Array3 <t></t>	15
length on Array <t></t>	14	operator = on DiagArray <t>&amp;</t>	15
limit	36	operator $== \dots 18, 21, 22, 23, 24, 27, 28,$	
lower_bound	39	operator >>	36
lower_bounds			
lssolve		D	
L		P	
LinConst		print_range	36
LU	35	prod	27
		product 16, 17, 20, 21, 22, 24, 26, 28, 29,	31
$\mathbf{M}$		P	35
map 20, 21, 22, 27, 28,	29		
Matrix		Q	
max		•	
maximum_step_size		Q	
min	36	QP	
$\verb minimize  \dots \dots$		QR	
minimum_step_size	44	Quad	
		quad	
N		Quad_options	
		quad_weights	
ncol	43	quotient	29

Function Index 52

$\mathbf{R}$	set_minimum_step_size44
R 35	set_objective_function
Range	set_relative_tolerance
real	set_right 43
relative_tolerance	set_states
resize 38, 39, 40, 43	set_stop_time
resize on Array <t></t>	set_tolerance
resize on Array2 <t></t>	set_upper_bound
resize on Array3 <t></t>	set_upper_bounds
resize on DiagArray <t></t>	singular_values
right 43	size
right_balancing_matrix	solve
right_included	sort
right_singular_matrix34	stack
roots	state
row	states
row_max 20, 27	sum       20, 27         sumsq       20, 27
row_max_loc	SVD
row_min 20, 27	340
row_min_loc	
rows on Array2 <t></t>	${f T}$
rows on DiagArray <t></t>	time
RowVector	tolerance
	transpose
${f S}$	
schur_matrix	$\mathbf{U}$
SCHUR 33	
second	unitary_hess_matrix
set_absolute_tolerance	unitary_matrix
set_alpha	upper_bound
set_base	upper_bounds
set_beta	U
set_bound	
set_bounds	$\mathbf{V}$
set_constraint_matrix	value
set_default_options	value_will_overflow
set_function	value_will_underflow
set_gradient_function	value_will_underliow
set_inc       36         set_initial_step_size       44	
set_jacobian_function	$\mathbf{W}$
set_left	width43
set_limit	#1401
set_lower_bound	37
set_lower_bounds	Y
aer rower nonnoa	$\mathbf{X}$
set_lower_bounds	<b>A</b> xelem on Array <t></t>