

Compiler Design

Fatemeh Deldar

Isfahan University of Technology

1403-1404

LALR(1) Grammar

- **مثال:** با داشتن گرامر و جدول تجزیه LALR(1) زیر، مراحل تجزیه رشته dab را بنویسید.
(پاسخ اسلاید بعد)

- 1- $A \rightarrow S$
- 2- $S \rightarrow E$
- 3- $S \rightarrow ab$
- 4- $E \rightarrow dEb$
- 5- $E \rightarrow T$
- 6- $T \rightarrow a$

| حالات | action | | | | goto | | |
|-------|--------|-------|-------|--------|------|-----|----|
| | a | b | d | \$ | E | T | S |
| 0 | s2 | | s3,10 | | 1 | 4,9 | 13 |
| 1 | r2 | | | r2 | | | |
| 2 | | s5 | | r6 | | | |
| 3,10 | s7 | | s3,10 | | 6,11 | 4,9 | |
| 4,9 | | r5 | | r5 | | | |
| 5 | | | | r3 | | | |
| 6,11 | | s8,12 | | | | | |
| 7 | | r6 | | | | | |
| 8,12 | | | | r4 | | | |
| 13 | | | | accept | | | |

LALR(1) Grammar

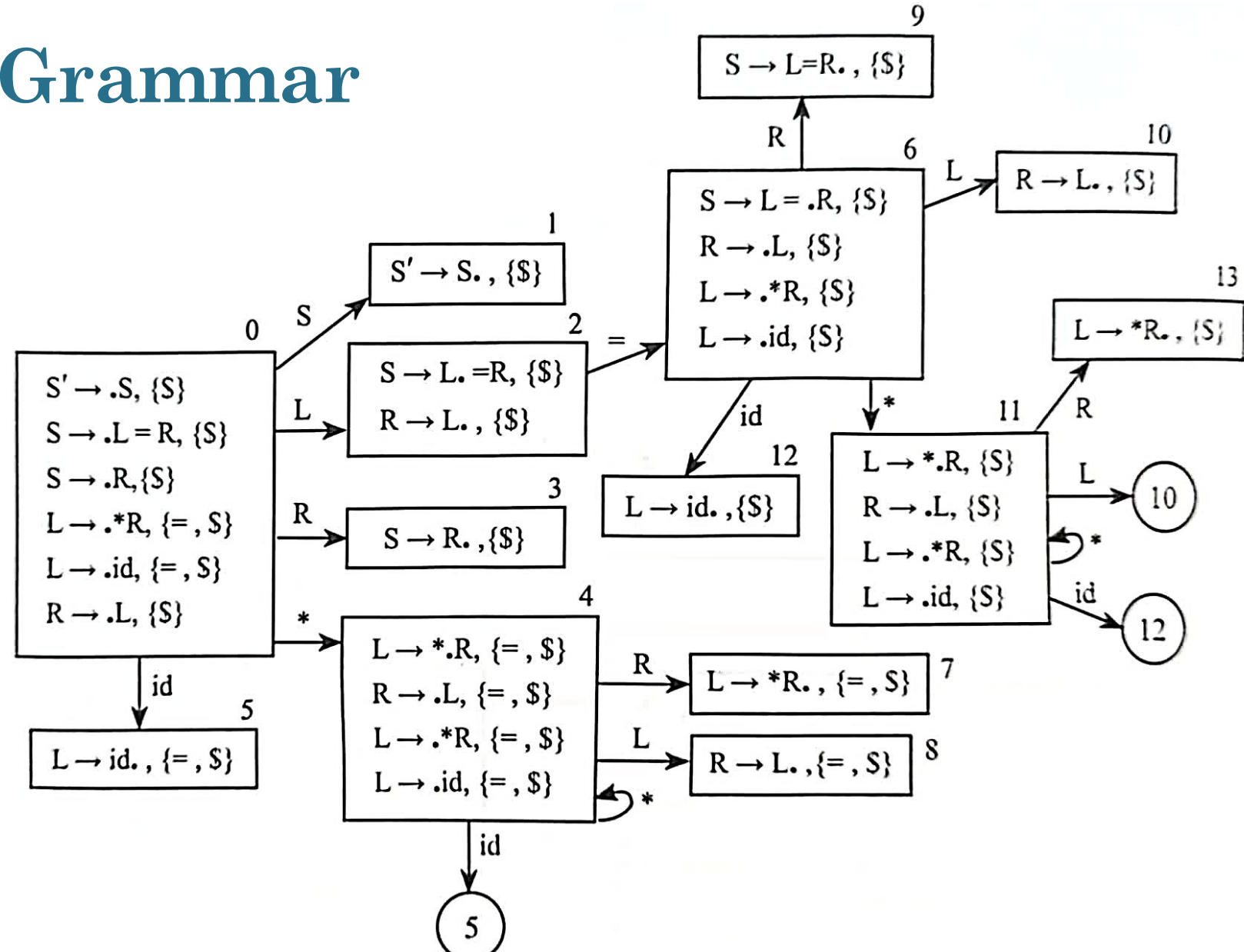
| پشته | رشته ورودی |
|------------------|------------|
| 0 | dab\$ |
| 0d3,10 | ab\$ |
| 0d3,10a7 | b\$ |
| 0d3,10T | b\$ |
| 0d3,10T4,9 | b\$ |
| 0d3,10E | b\$ |
| 0d3,10E6,11 | b\$ |
| 0d3,10E6,11b8,12 | \$ |
| 0E | \$ |
| 0E1 | \$ |
| 0S | \$ |
| 0S13 (accept) | \$ |

• مثال (ادامه)

LALR(1) Grammar

- **Example**
 - LR(1) Diagram

$S \rightarrow L = R \mid R$
 $L \rightarrow *R \mid \text{id}$
 $R \rightarrow L$



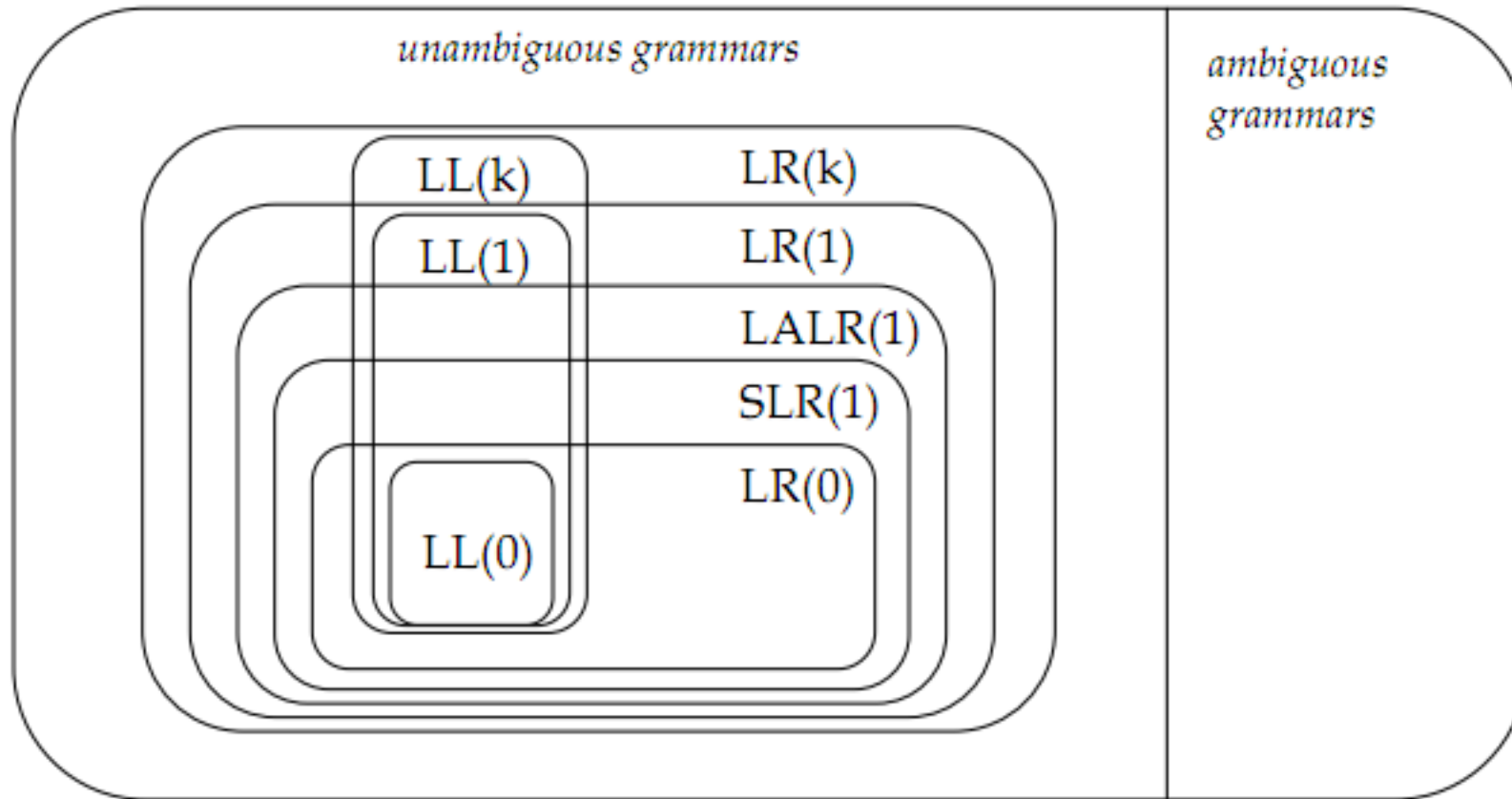
LALR(1) Grammar

- **Example**
 - LALR(1) parse table

$$\begin{aligned}
 S &\rightarrow L = R \mid R \\
 L &\rightarrow *R \mid \text{id} \\
 R &\rightarrow L
 \end{aligned}$$

| state | action | | | | goto | | |
|-------|--------|-------|-------|-----|------|------|------|
| | = | * | id | \$ | S | L | R |
| 0 | | S4-11 | S5-12 | | 1 | 2 | 3 |
| 1 | | | | acc | | | |
| 2 | S6 | | | r5 | | | |
| 3 | | | | r2 | | | |
| 4-11 | | S4-11 | S5-12 | | | 8-10 | 7-13 |
| 5-12 | r4 | | | r4 | | | |
| 6 | | S4-11 | S5-12 | | | 8-10 | 9 |
| 7-13 | r3 | | | r3 | | | |
| 8-10 | r5 | | | r5 | | | |
| 9 | | | | r1 | | | |

Hierarchy of Grammar Classes



Ambiguous Grammars

- *Every ambiguous grammar fails to be LR*
- *Every LR grammar is not ambiguous*
- **However, certain types of ambiguous grammars are quite useful in the specification and implementation of languages**
 - We can specify dis-ambiguating rules that allow only one parse tree for each sentence
- *Compilers usually use precedence and associativity to resolve conflicts*

Ambiguous Grammars

- Precedence and Associativity to Resolve Conflicts

- **Example** $E \rightarrow E + E \mid E * E \mid (E) \mid \text{id}$

- *This grammar is ambiguous because it does not specify the associativity or precedence of the operators + and **

- This grammar is equivalent to the above grammar, which is not ambiguous
- | | | |
|-----|---------------|------------------------|
| E | \rightarrow | $E + T \mid T$ |
| T | \rightarrow | $T * F \mid F$ |
| F | \rightarrow | $(E) \mid \text{id}$ |

- **There are two reasons why we might prefer to use the ambiguous grammar**
 - We can easily change the associativity and precedence of the operators without disturbing the productions or the number of states in the resulting parser
 - The parser for the ambiguous grammar will not waste time reducing by single productions

Ambiguous Grammar

- Assuming + and * are left associative and * takes precedence over +

| STATE | ACTION | | | | | | GOTO |
|-------|--------|----|----|----|----|-------|----------|
| | id | + | * | (|) | \$ | <i>E</i> |
| 0 | s3 | | | s2 | | | 1 |
| 1 | | s4 | s5 | | | acc | |
| 2 | s3 | | | s2 | | | 6 |
| 3 | | r4 | r4 | | | r4 r4 | |
| 4 | s3 | | | s2 | | | 7 |
| 5 | s3 | | | s2 | | | 8 |
| 6 | | s4 | s5 | | s9 | | |
| 7 | | r1 | s5 | | r1 | r1 | |
| 8 | | r2 | r2 | | r2 | r2 | |
| 9 | | r3 | r3 | | r3 | r3 | |

$I_0:$ $E' \rightarrow \cdot E$
 $E \rightarrow \cdot E + E$
 $E \rightarrow \cdot E * E$
 $E \rightarrow \cdot (E)$
 $E \rightarrow \cdot \text{id}$

$I_1:$ $E' \rightarrow E \cdot$
 $E \rightarrow E \cdot + E$
 $E \rightarrow E \cdot * E$

$I_2:$ $E \rightarrow (\cdot E)$
 $E \rightarrow \cdot E + E$
 $E \rightarrow \cdot E * E$
 $E \rightarrow \cdot (E)$
 $E \rightarrow \cdot \text{id}$

$I_3:$ $E \rightarrow \text{id} \cdot$

$I_4:$ $E \rightarrow E + \cdot E$
 $E \rightarrow \cdot E + E$
 $E \rightarrow \cdot E * E$
 $E \rightarrow \cdot (E)$
 $E \rightarrow \cdot \text{id}$

$I_5:$ $E \rightarrow E * \cdot E$
 $E \rightarrow \cdot E + E$
 $E \rightarrow \cdot E * E$
 $E \rightarrow \cdot (E)$
 $E \rightarrow \cdot \text{id}$

$I_6:$ $E \rightarrow (E \cdot)$
 $E \rightarrow E \cdot + E$
 $E \rightarrow E \cdot * E$

$I_7:$ $E \rightarrow E + E \cdot$
 $E \rightarrow E \cdot + E$
 $E \rightarrow E \cdot * E$

$I_8:$ $E \rightarrow E * E \cdot$
 $E \rightarrow E \cdot + E$
 $E \rightarrow E \cdot * E$

$I_9:$ $E \rightarrow (E) \cdot$