

Computational Intelligence

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Outline

- Neural Networks in Practice
 - Regularization
 - Why Regularization Reduces Overfitting?
 - Regularization Techniques
 - L2 Regularization
 - Dropout

Neural Networks in Practice: Regularization

Regularization

What is it?

Technique that constrains our optimization problem to discourage complex models

Regularization

What is it?

Technique that constrains our optimization problem to discourage complex models

Why do we need it?

Improve generalization of our model on unseen data

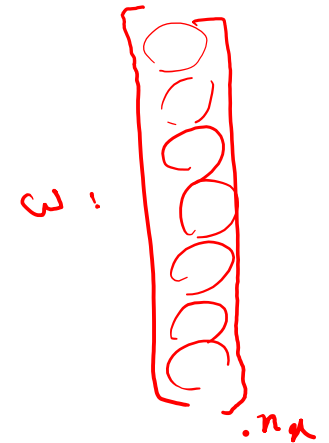
 m : training data
 n : sample size

Regularization in Logistic regression

$$\min_{w,b} J(w, b)$$

$$w \in \mathbb{R}^n \quad b \in \mathbb{R}$$

$$J(w, b) = \frac{1}{m} \sum_{i=1}^m \mathcal{L}(\hat{y}^{(i)}, y^{(i)}) + \boxed{\frac{\lambda}{2m} \|w\|_2^2} + \frac{\lambda}{2m} b^2$$



$$L_2 \text{ regularization: } \|w\|_2^2 = \sum_{j=1}^n w_j^2 = w^T w$$

$$L_1 \text{ reg...} : \frac{\lambda}{2m} \sum_{j=1}^n |w_j| = \frac{\lambda}{2m} \|w\|_1$$

λ = Regularization Parameter

Regularization in Neural network

$$J(\omega^{[1]}, b^{[1]}, \dots, \omega^{[L]}, b^{[L]}) = \frac{1}{m} \sum_{i=1}^m \ell(\hat{y}^{(i)}, y^{(i)}) + \frac{\lambda}{2m} \sum_{l=1}^L \|\omega^{[l]}\|_F^2$$

تعداد لا یبرها

$$\|\omega^{[l]}\|_F^2 = \sum_{i=1}^n \sum_{j=1}^n (\omega_{ij}^{[l]})^2$$

"Frobenius norm"

$$d\omega^{[l]} = \left(\text{from backprop} \right) + \frac{\lambda}{m} \omega^{[l]}$$

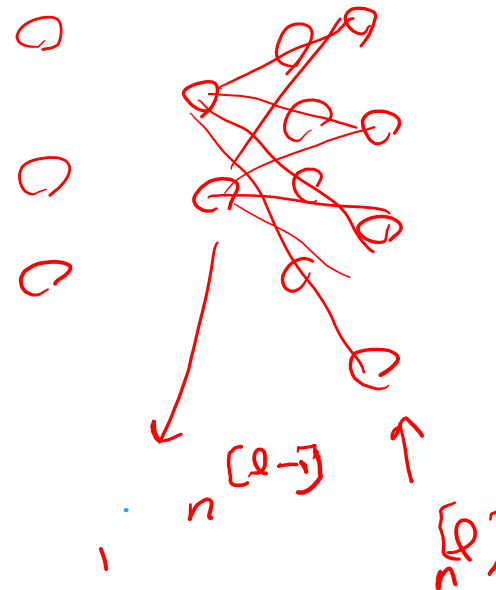
$$\omega^{[l]} = \omega^{[l]} - \alpha d\omega^{[l]}$$

$\frac{\partial J}{\partial \omega^{[l]}}$

$$\omega^{[l]} = \omega^{[l]} - \alpha \left[\left(\text{from back} \right) + \frac{\lambda}{m} \omega^{[l]} \right]$$

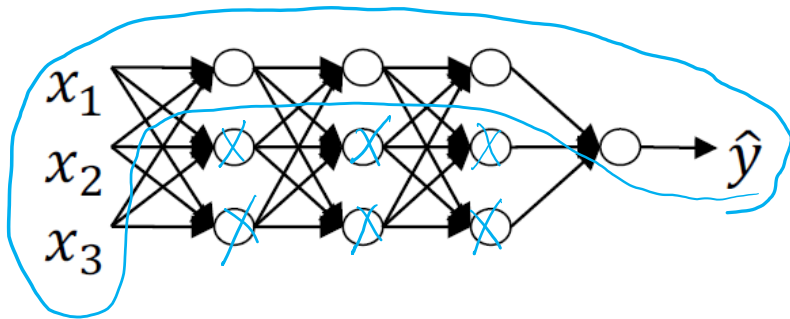
weight decay

$$= \left(1 - \frac{\alpha \lambda}{m} \right) \omega^{[l]} - \alpha (\text{from back} \dots)$$

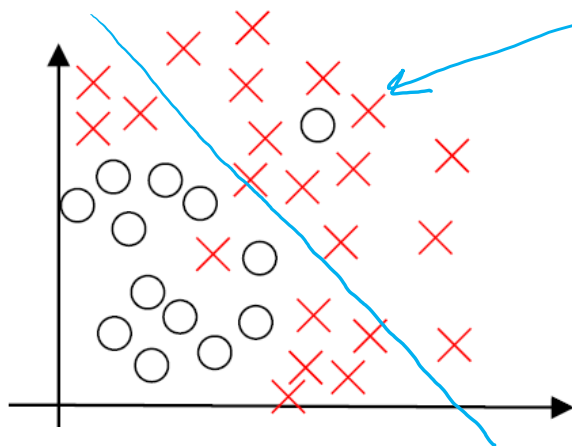


Regularization: Why Regularization Reduces Overfitting?

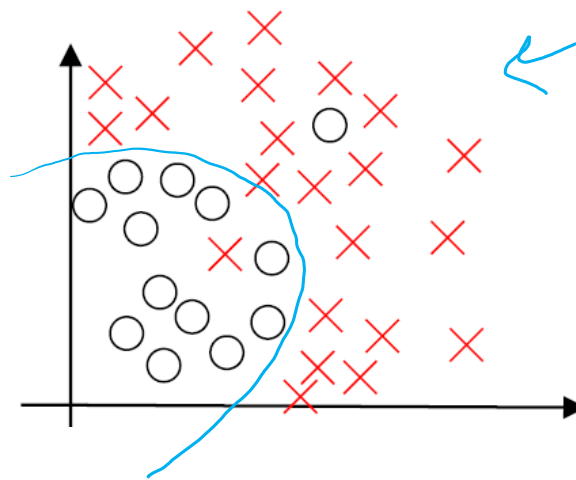
How does regularization prevent overfitting?



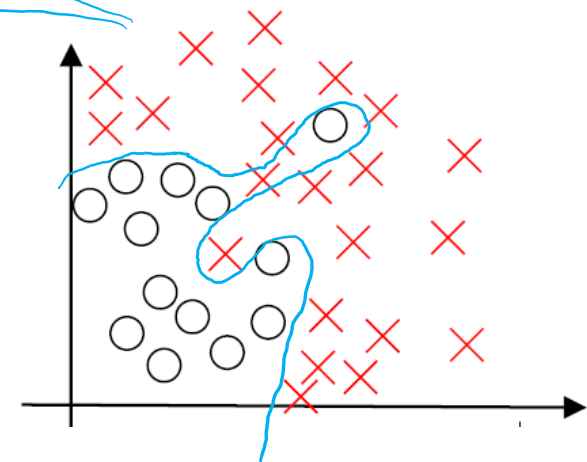
$$J(\omega^{[1]}, b^{[1]}, \dots, \omega^{[L]}, b^{[L]}) = \frac{1}{m} \sum_{i=1}^m \ell(\hat{y}^{(i)}, y^{(i)}) + \underbrace{\frac{\lambda}{2m} \sum_{l=1}^L \|\omega^{[l]}\|_F^2}_{\lambda \rightarrow \text{دَر} \quad \|\omega^{[l]}\| \approx 0}$$



high bias

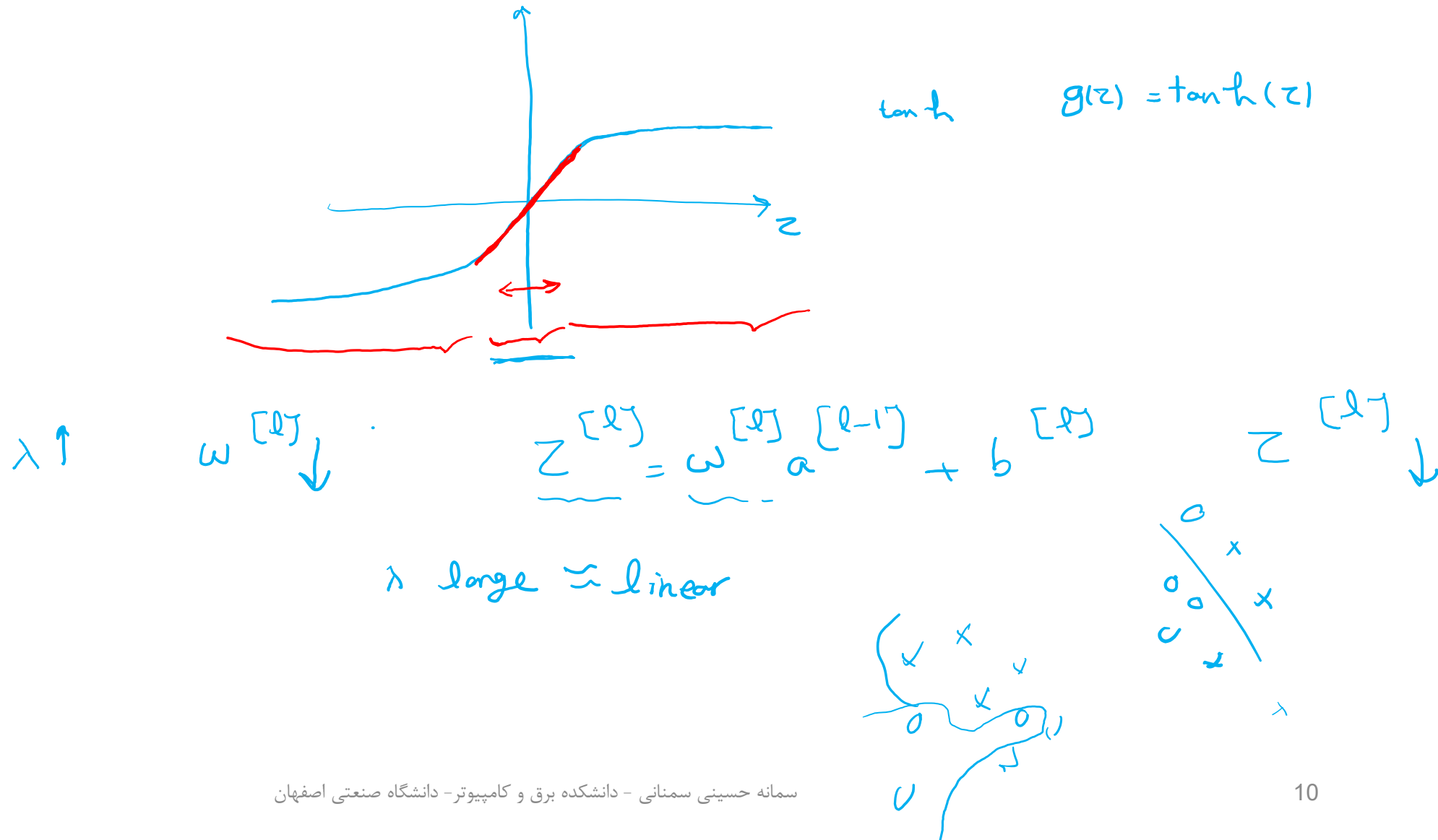


just right



high variance

How does regularization prevent overfitting?



Regularization Techniques:

II: Dropout

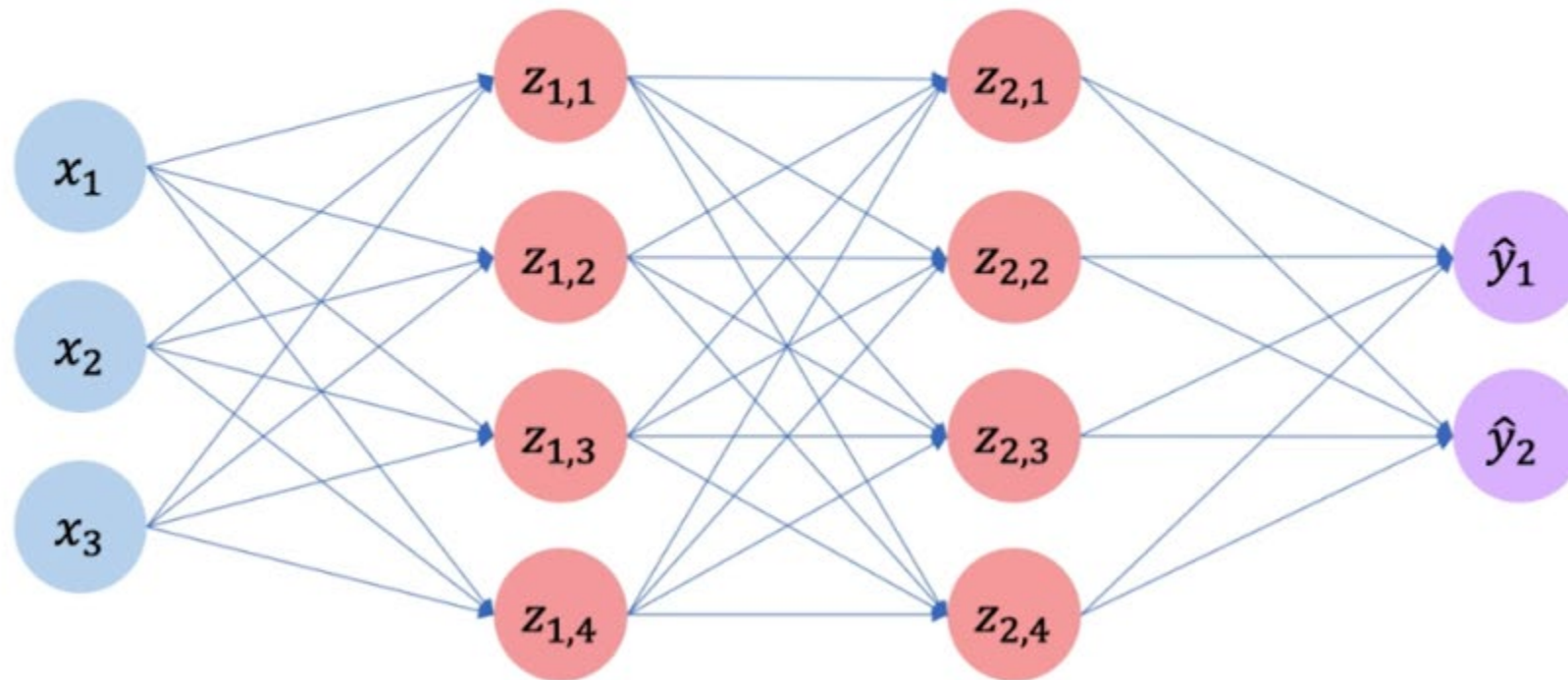
I : L_2 Regularization

II : Dropout

$$\frac{1}{2m} \sum_{i=1}^l \|w^{[l]}\|_F^2$$

Regularization II: Dropout

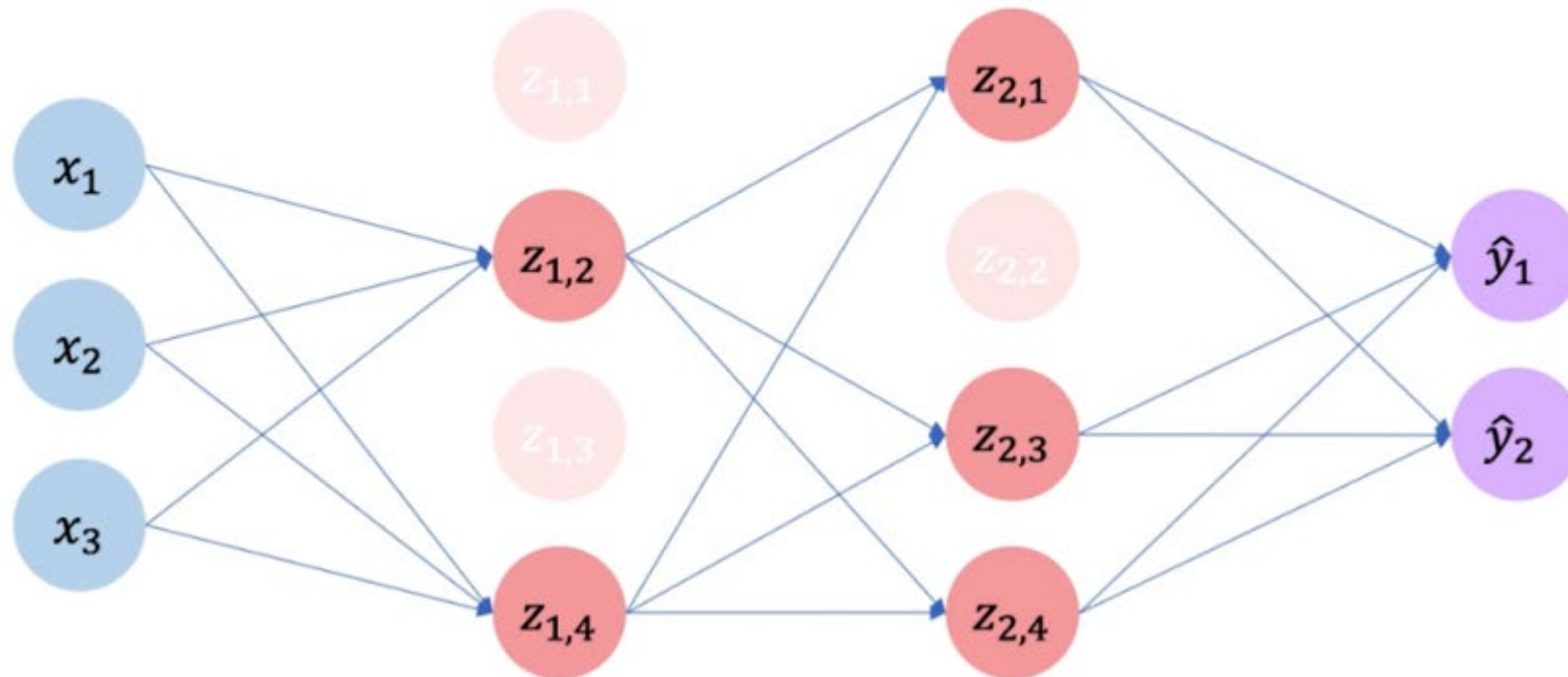
- During training, randomly set some activations to 0



Regularization II: Dropout

- During training, randomly set some activations to 0
 - Typically 'drop' 50% of activations in layer
 - Forces network to not rely on any 1 node

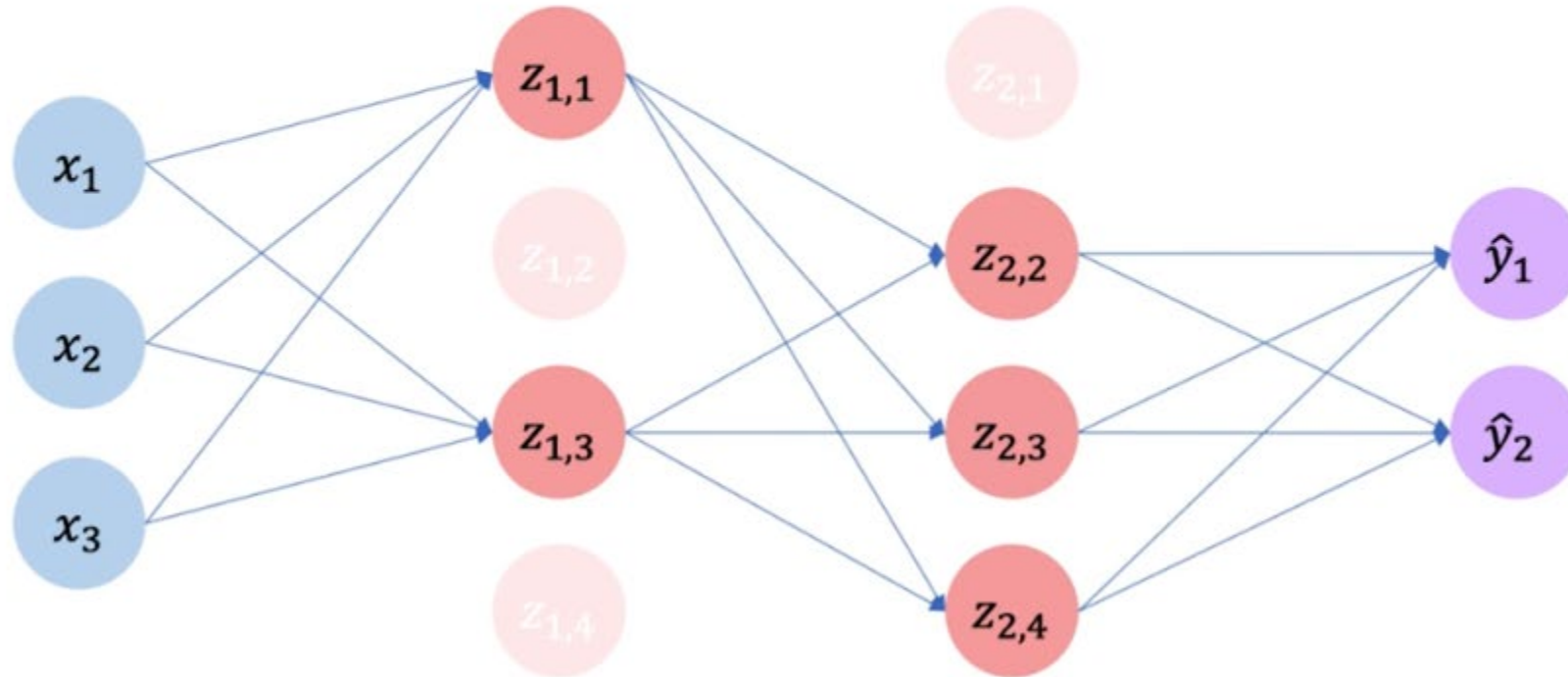
 `tf.keras.layers.Dropout(p=0.5)`



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Implementing dropout ("Inverted dropout")

Illustrate with layer $l=3$

keep-prob = 0.8 0.2

$d_3 = \text{np.random.rand}(a_3.\text{shape}[0], a_3.\text{shape}[1]) < \text{keep-prob}$

$a_3 = \text{np.multiply}(a_3, d_3)$

$a_3 /= \text{keep-prob}$

50 unit \longrightarrow 10 unit shut off

$z^{[4]} = w^{[4]} a^{[3]} + b^{[4]}$

\uparrow reduced 20%

$/= 0.8$

Making predictions at test time

$$a^{[0]} = X$$

No drop out

$$z^{[1]} = w^{[1]} a^{[0]} + b^{[1]}$$

$$a^{[1]} = g^{[1]}(z^{[1]})$$

$$z^{[2]} = w^{[2]} a^{[1]} + b^{[2]}$$

$$a^{[2]} = g^{[2]}(z^{[2]})$$

\vdots
 \downarrow
 \hat{y}

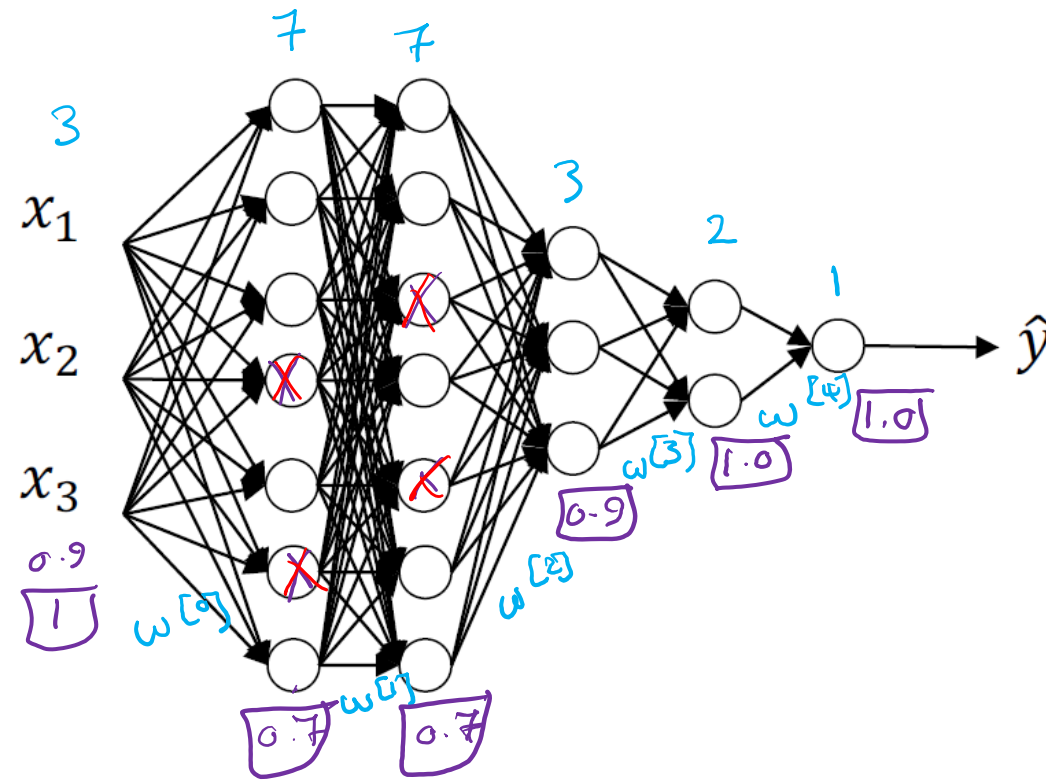
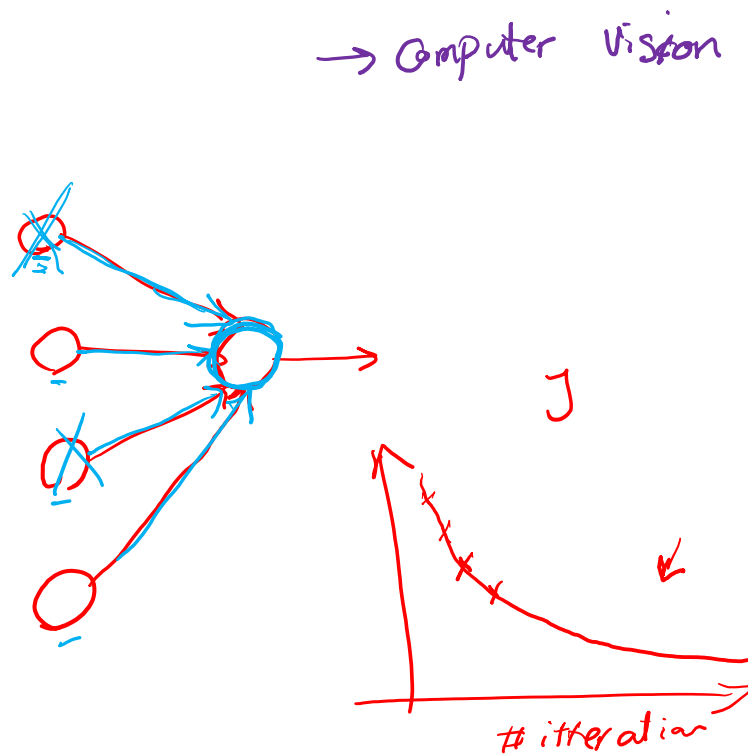
/ = keep-prob

Understanding Dropout

Why does drop-out work?

Intuition: Can't rely on any one feature, so have to spread out weights

Shrink weight $\rightarrow L_2$



Keep - prob



Core Foundation Review

Regularization

How does regularization
prevent overfitting

Regularization
techniques: L2, Dropout

*Technique that constrains our optimization
problem to discourage complex models*

