

# Computational Intelligence

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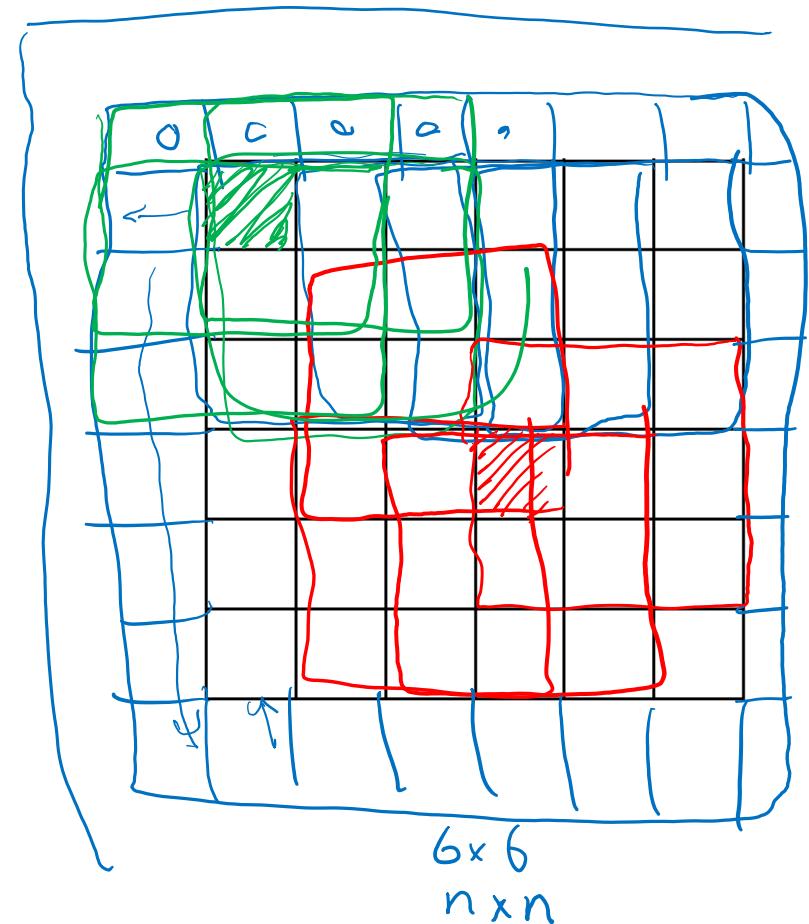
Isfahan University of Technology

# Outline

- Convolutional Neural Networks
  - Padding
  - Strided Convolutions
  - Convolutions Over Volume
  - One layer of a convolutional network

# Convolutional Neural Networks: Padding

# Padding



- ✓ Shrinking output
- ✓ throwing away info from edge

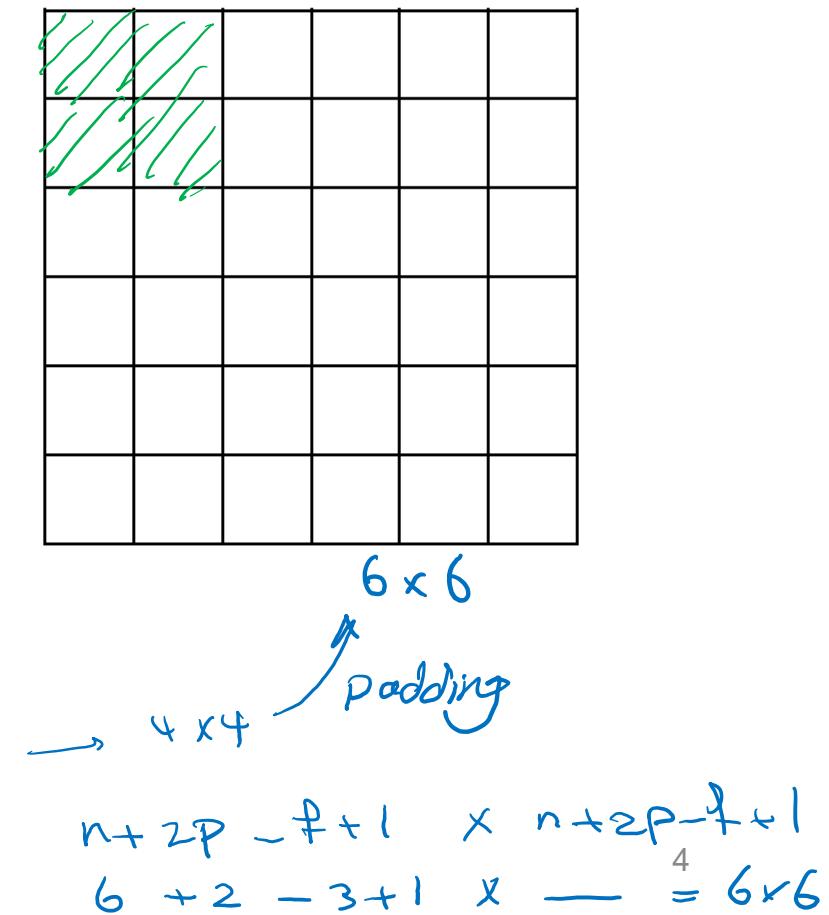
$$* \quad P = 2$$

$\begin{array}{|c|c|c|} \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array}$

=

$3 \times 3$   
 $f \times f$

$$\begin{matrix} n-f+1 & \times n-f+1 \\ 6-3+1 = 4 & \end{matrix}$$



# Valid and Same convolutions

“Valid”:  $\xrightarrow{\text{no padding}} n \times n * f \times f \rightarrow n-f+1 \times n-f+1$

$$6 \times 6 * 3 \times 3 \rightarrow 4 \times 4$$

“Same”: Pad so that output size is the same as the input size.

$$5 \times 5 \Rightarrow P = \frac{5-1}{2} = 2$$
$$\cancel{n+2P-f+1} \quad \times \quad n+2P-f+1$$
$$P = \frac{f-1}{2}$$
$$3 \times 3 \quad \quad \quad P = \frac{3-1}{2} = 1 \quad \quad \quad f=3$$

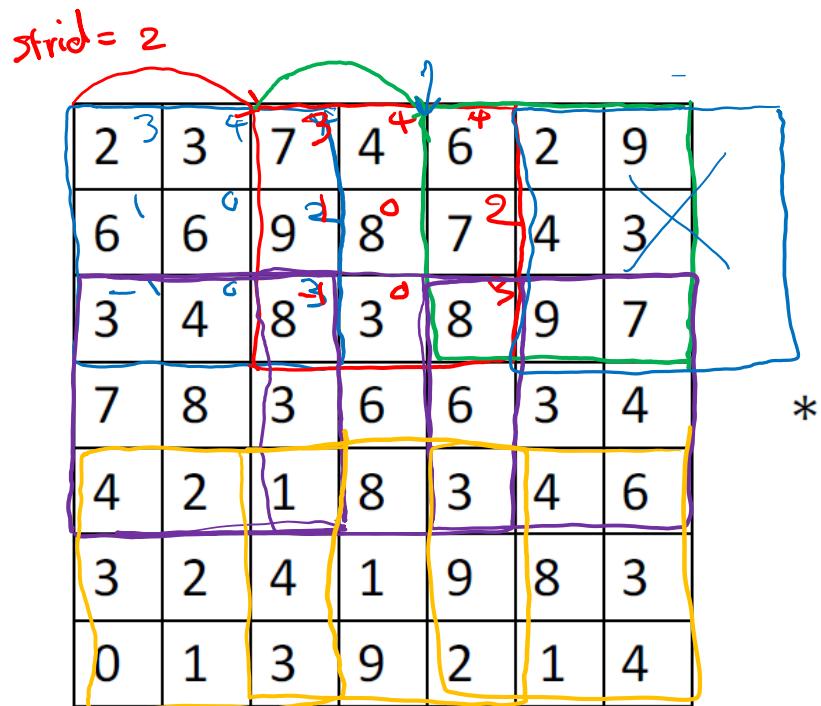
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$f \times 1$   
 $3 \times 3$   
 $5 \times 5$   
 $7 \times 7$



# Convolutional Neural Networks: Strided Convolutions

# Strided convolution



$$\begin{matrix} 3 & 4 & 4 \\ 1 & 0 & 2 \\ -1 & 0 & 3 \end{matrix}$$

$3 \times 3$

$$\begin{matrix} 91 & 100 & 83 \\ 69 & 91 & 127 \\ 44 & 72 & 74 \end{matrix}$$

$\underline{3 \times 3}$

stride = 2

$\underline{7 \times 7}$

$n \times n * f \times f$

padding  $P$       stride  $S$   
 $S=2$

سازنده مجموعی :

$$\left\lfloor \frac{n+2P-f}{S} + 1 \right\rfloor \times \left\lfloor \frac{n+2P-f}{S} + 1 \right\rfloor$$

$$\frac{7+0-3}{2} + 1 = 2 + 1 = 3$$

# Summary of convolutions

$n \times n$  image

$f \times f$  filter

padding  $p$

stride  $s$

ساختار فردی :

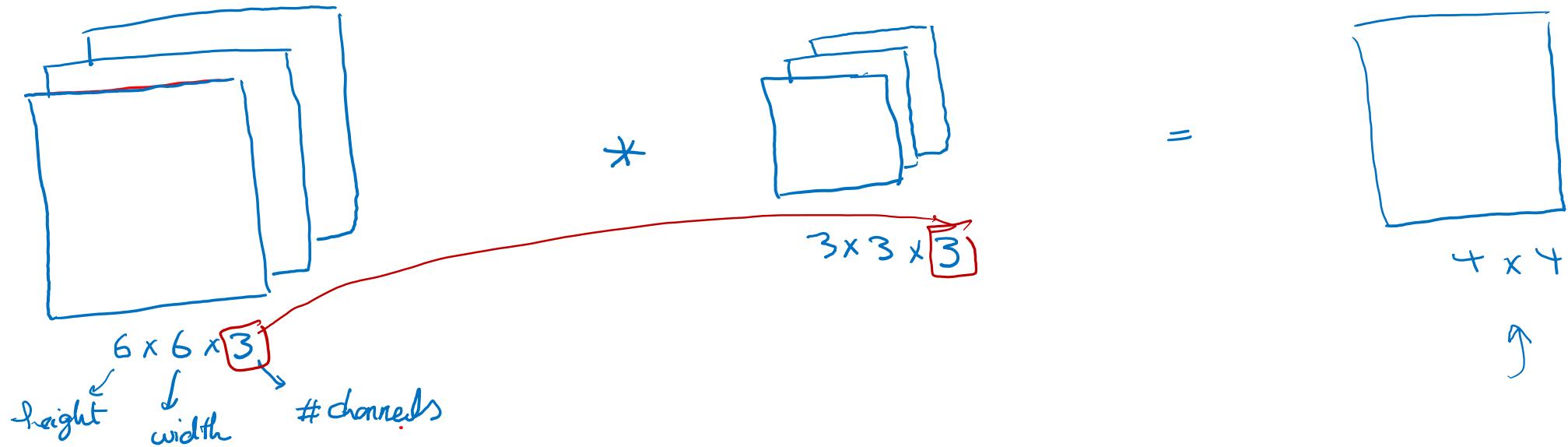
$$\left\lfloor \frac{n+2p-f}{s} + 1 \right\rfloor$$

$\times$

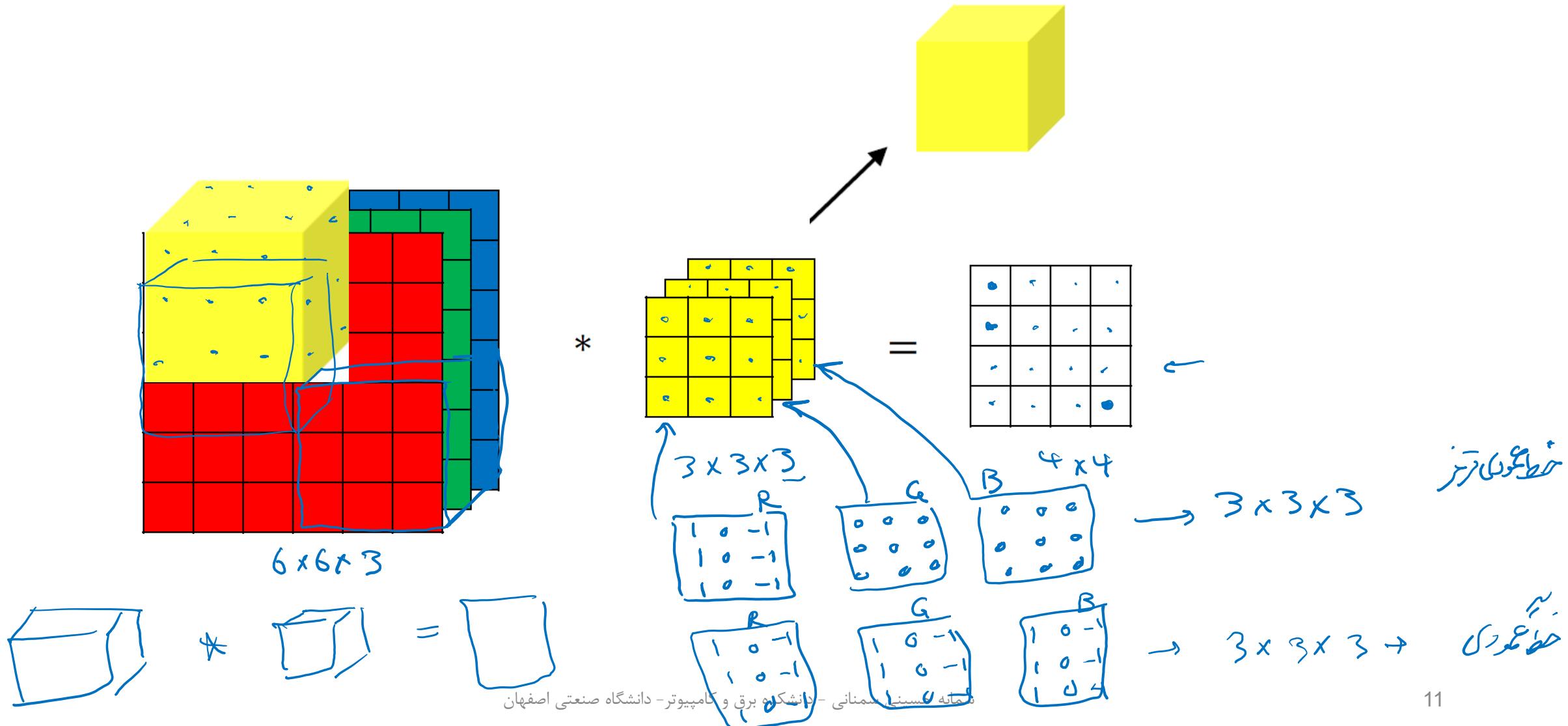
$$\left\lfloor \frac{n+2p-f}{s} + 1 \right\rfloor$$

# Convolutional Neural Networks: Convolutions over volumes

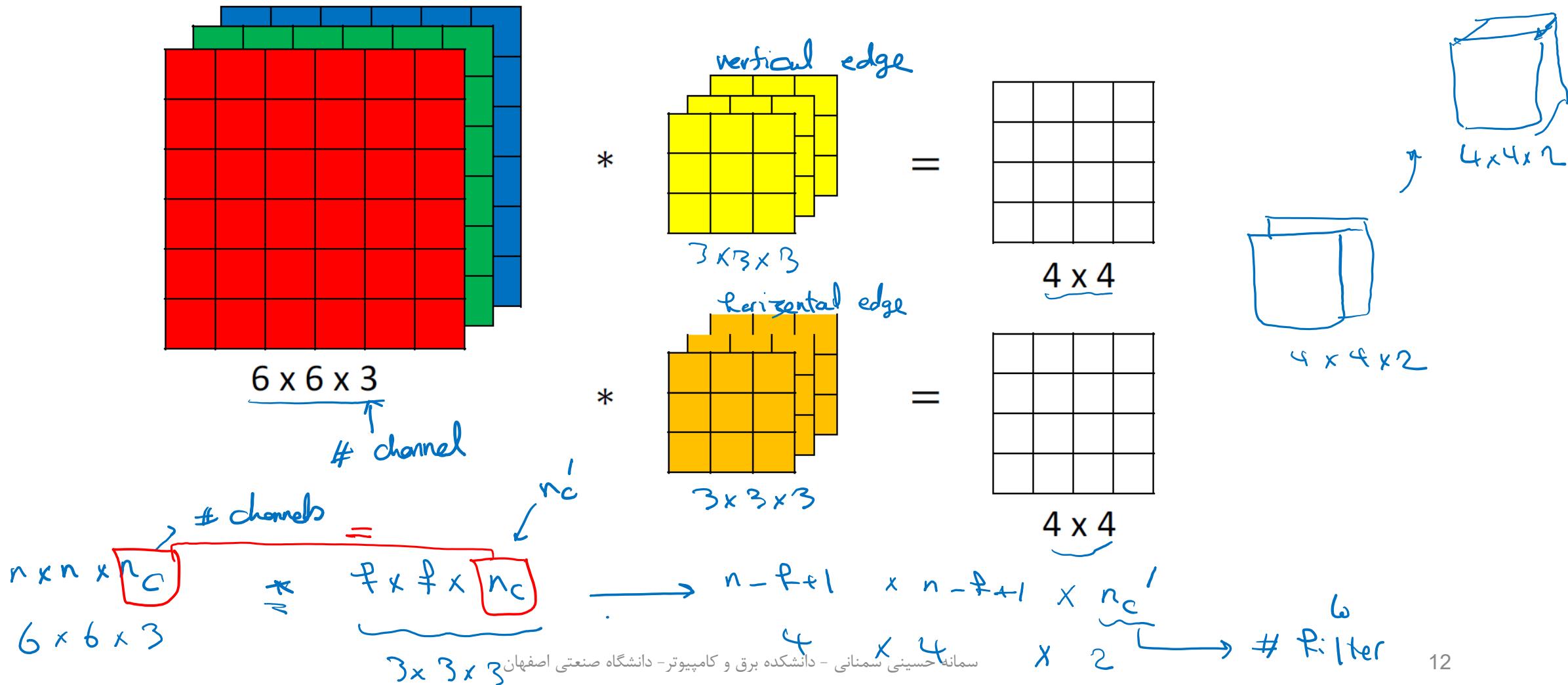
# Convolutions on RGB images



# Convolutions on RGB images



# Multiple Filters



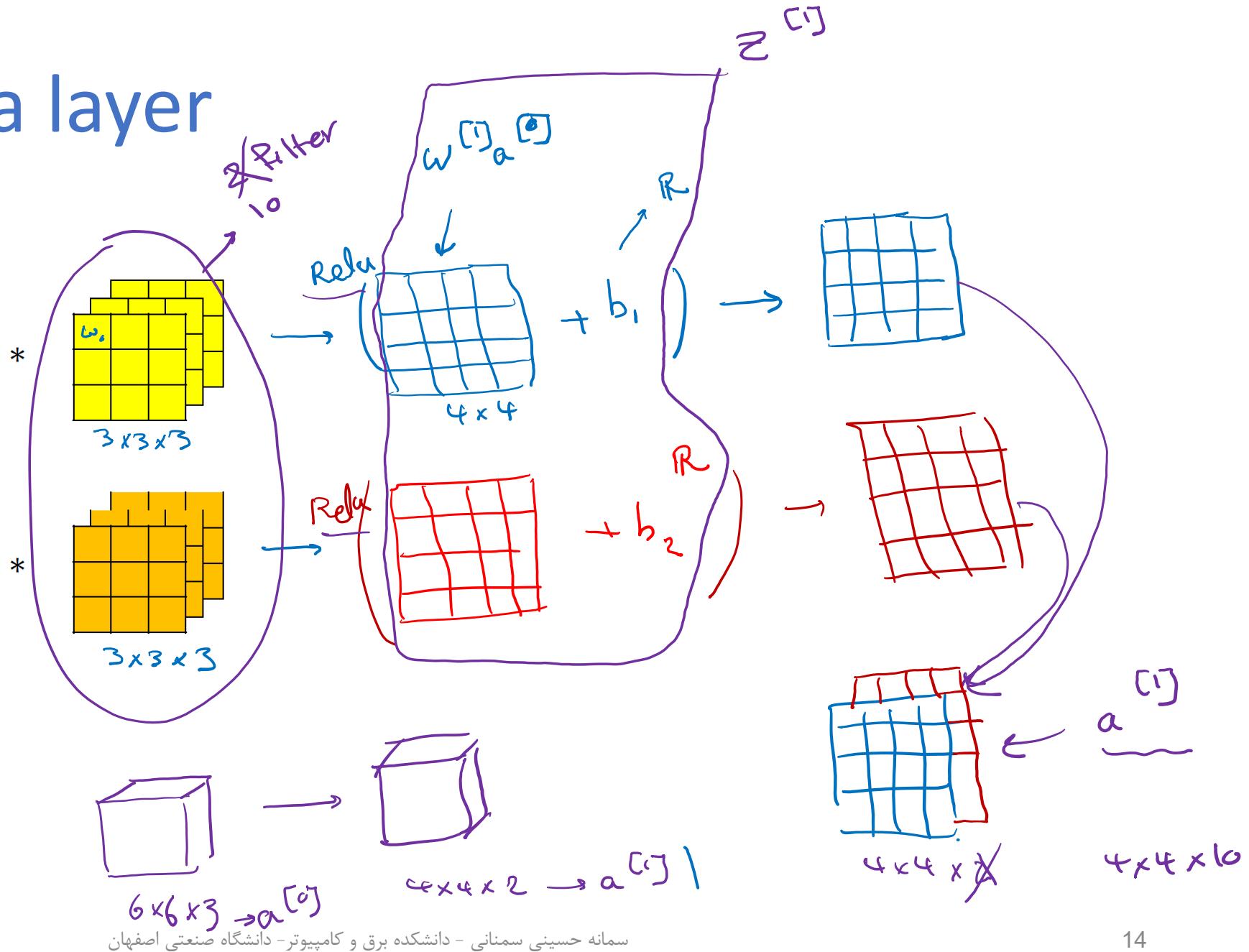
# Convolutional Neural Networks: One layer of a convolutional network

# Example of a layer

$$X \in \mathbb{R}^{6 \times 6 \times 3}$$

$$z^{[1]} = w^{[1]}\alpha^{[0]} + b^{[1]}$$

$$a^{[1]} = g(z^{[1]})$$



# Core Foundation Review

- Convolutional Neural Networks
  - Padding
  - Strided Convolutions
  - Convolutions Over Volume
  - One layer of a convolutional network